# A $0.5 \mathrm{~V}, 1.2 \mathrm{~mW}, 160 \mathrm{fJ}, 600 \mathrm{MS} / \mathrm{s} 5$ bit Flash ADC 

Masaya Miyahara, James Lin, Kei Yoshihara, and Akira Matsuzawa<br>Dept. of Physical Electronics, Tokyo Institute of Technology<br>S3-27, 2-12-1, Ookayama, Meguro-ku, Tokyo, 152-8552, Japan<br>Tel/Fax: +81-3-5734-2508, E-mail; masaya@ssc.pe.titech.ac.jp


#### Abstract

An ultra-low voltage operation of 0.5 V , 5-bit Flash ADC has been developed and achieved an ENOB of 4.2-bit at a conversion rate of $600 \mathrm{MS} / \mathrm{s}$. It consumes only 1.2 mW and attained an ultra-low FoM of 160 fJ/conv. steps at an ERBW of 200 MHz . A forward body bias technique and gate-interpolated double-tail latched comparator with variable delay method to compensate the mismatch voltage are introduced.


## I. INTRODUCTION

Five to seven-bit, several hundred MS/s to around one GS/s ADCs are required for disk drive front-ends, high speed backplane, ultra-wideband receivers, and millimeter-wave receivers.

An ultra-low power operation is strongly required for the portable applications, ubiquitious wireless sensor systems, and the green IT regulation. Furthermore, a low resolution and low latency flash ADC is an important circuit block for other higher resolution ADCs such as a delta-sigma ADC, subranging ADC , and pipeline ADC .

A low voltage operation is the most efficient way to reduce the power consumption and the challenges to realize low voltage operation for analog circuits and data converters will become more important along with further technology scaling where the conventional analog circuit technique will lose its validity. Therefore, we should investigate the use of low voltage operation to reduce the FoM of an ADC like digital circuits.

This paper describes the strategy to reduce the FoM of an ADC by reducing the operating voltage and the challenge for low voltage analog circuit design. The 5-bit flash ADC fabricated in 90 nm CMOS realizes an ultra-low voltage operation of 0.5 V and consumes very low power, 1.2 mW , at a conversion rate of $600 \mathrm{MS} / \mathrm{s}$. An ENOB of 4.2-bit and an ultra-low FoM of $160 \mathrm{fJ} /$ conv. step have been attained.

## II. StRATEGY FOR LOW-vOLTAGE OPERATION

The FoM of a flash ADC is

$$
\begin{equation*}
\mathrm{FoM}=\frac{P_{d}}{f_{\mathrm{c}} \times 2^{E N O B}} \tag{1}
\end{equation*}
$$

where $P_{\mathrm{d}}$ is the power dissipation of the $\mathrm{ADC}, f_{\mathrm{c}}$ is the conversion frequency, and ENOB is the effective number of bits.

If $E_{\mathrm{c}}$ is the energy consumption for each comparator and followed logic circuits, equation (1) yields

$$
\begin{equation*}
\mathrm{FoM}=\frac{f_{\mathrm{c}} \times E_{\mathrm{c}} \times 2^{N}}{f_{\mathrm{c}} \times 2^{N-\triangle E N O B}}=E_{\mathrm{c}} 2^{\triangle E N O B} \tag{2}
\end{equation*}
$$

where $\triangle E N O B$ is a reduction of $E N O B$ from the ideal value. Therefore, reductions of $E_{\mathrm{c}}$ and $\triangle E N O B$ are essential to attain low FoM [1].

The $E_{\mathrm{c}}$ can be expressed as the following with consideration of the sub-threshold leakage current.

$$
\begin{equation*}
E_{\mathrm{c}}=C_{\mathrm{c}} V_{\mathrm{DD}}^{2}+\frac{V_{\mathrm{DD}} \cdot I_{\mathrm{c}} \exp \left(-\frac{V_{\mathrm{T}}}{S}\right)}{f_{c}} \tag{3}
\end{equation*}
$$

where $C_{\mathrm{c}}$ is the unit capacitance for a comparator, $V_{\mathrm{DD}}$ is the supply voltage, $I_{\mathrm{c}}$ is the unit current for the sub-threshold leakage current, $V_{\mathrm{T}}$ is the threshold voltage, $S$ is the subthreshold swing.

The $\triangle E N O B$ is given by following, if comparator noise can be neglected,

$$
\begin{equation*}
\triangle E N O B=\frac{1}{2} \log _{2}\left(1+12\left(\frac{V_{\text {off }}(\sigma)}{V_{\mathrm{q}}}\right)^{2}\right) \tag{4}
\end{equation*}
$$

where $V_{\mathrm{q}}$ is the quantization voltage and $V_{\text {off }}(\sigma)$ is the sigma of offset voltage distribution.

Figure 1 shows the estimated $E_{\mathrm{c}}$, FoM, and $2^{\triangle E N O B}$ vs. $V_{\mathrm{DD}}$ when the resolution is 5 bits, $V_{\text {off }}(\sigma)$ is $6 \mathrm{mV}, V_{\mathrm{T}}=0.1 \mathrm{~V}$, and $f_{\mathrm{c}}$ is 600 MHz . We used $C_{\mathrm{c}}=170 \mathrm{fF}, I_{\mathrm{c}}=156 \mu \mathrm{~A}, S=44 \mathrm{mV}$ from the measured data.

The $E_{\mathrm{c}}$ is basically proportional to $V_{\mathrm{DD}}{ }^{2}$ however $\triangle E N O B$ is inversely proportional to $V_{\mathrm{DD}}$ since the quantization voltage becomes lower with $V_{\mathrm{DD}}$ reduction. However $2^{\triangle E N O B}$ is not large enough to affect the FoM. Therefore, the FoM can be significantly reduced by reducing power supply voltage $V_{\mathrm{DD}}$.


Fig. 1. Estimated $E_{\mathrm{c}}$, FoM, and $2^{\triangle E N O B}$ vs. $V_{\mathrm{DD}}$.


Fig. 2. FoM, Delay, and FD product vs. $V_{\text {DD }}$.
To increase the conversion frequency, an interleaving operation with multiple unit ADCs can be used and FoM can be kept almost the same, if the power consumption of additional circuits and the reduction of ENOB can be neglected.

However, excessive number of interleaving causes many issues such as an increase of occupied area, a reduction of PVT margins, a reduction of ENOB, furthermore an increase of input drive difficulty. Thus we should introduce FoM delay product (FD) like the energy-delay product (ED) in digital circuits [2][3]. The delay time should be defined as the reciprocal value of the maximum conversion frequency for a given operating voltage and we estimated it by using the following equation.

$$
\begin{equation*}
T_{\mathrm{d}}=k \frac{V_{\mathrm{DD}}}{\left(V_{\mathrm{DD}}-V_{\mathrm{T}}\right)^{\alpha}} \tag{5}
\end{equation*}
$$

where $k$ and $\alpha$ are the fitting constants, $V_{\mathrm{T}}$ is the effective threshold voltage. Figure 2 shows FoM shown in figure 1, with $T_{\mathrm{d}}$ derived from the equation (5), and FoM delay products. We used $V_{\mathrm{T}}=0.4 \mathrm{~V}$ (higher than the conventional definition of $V_{\mathrm{T}}$ ) and $\alpha=1.2$. 0.7 V may offer the best $V_{\mathrm{DD}}$ to minimize the FD product.

This FD product suggests the balance between the number of interleaving and decrease of energy consumption. The lower value is preferable for low energy and high speed operation and the same value means the decrease of conversion speed by reducing the operating voltage can decrease the conversion energy equivalently.


Fig. 3. Logic gates with forward body bias (FBB) and the gate delay time vs. supply voltage.


Fig. 4. Delay time of each circuit block for $V_{\mathrm{DD}}=1.2 \mathrm{~V}$, and $V_{\mathrm{DD}}=0.5$ V with and without FBB.

## III. Circuit design

## A. Forward body bias technique

A gate delay time will increase significantly when the supply voltage is reduced to 0.5 V . Thus we introduced the forward body bias technique to address this issue. At the ultra low voltage operation which is lower than the built-in potential of the PN junction, the forward body bias (FBB) technique can be used easily to connect the body of NMOS to $V_{\mathrm{DD}}$ and the body of PMOS to the ground. This configuration makes circuit and layout simple, as shown in figure 3 (a). The reductions of $V_{\mathrm{T}}$ by FBB have been measured 100 mV for NMOS and 60 mV for PMOS. The gate delay time can be reduced to about half for the conventional CMOS circuit, as shown in figure 3 (b).

Figure 4 shows the delay time of each circuit block for $V_{\mathrm{DD}}=1.2 \mathrm{~V}$ and $V_{\mathrm{DD}}=0.5 \mathrm{~V}$ with and without FBB . The delay time is increased by about 6 x without FBB , however it can be suppressed by about $3.5 x$ with FBB. The comparator is the most sensitive to the voltage lowering.

## B. Mismatch compensation by variable delay

We used a double-tail latched comparator [4] since this is suitable for low voltage operation compared with the conventional single-tail latched comparator owing to the reduced number of transistor stack. However, we had to
develop a new mismatch compensation technique using variable time delay method.

A variable capacitance method is widely used to compensate the offset voltage mismatch of dynamic comparator [5]. However, it loses its advantage with lowering the operating voltage, since the sensitivity of capacitance of the MOS varactor to the control voltage is reduced. Thus we developed mismatch compensation technique using variable delay circuit, as shown in figure 5 .

This figure shows the dynamic preamplifier circuit in the double-tail latched comparator. The activation clock timing for the output nodes are controlled by variable delay circuits. Figure 6 shows the variable delay circuits for NMOS type and PMOS type.

Table 1 compares several mismatch compensation methods. Input offset mismatch voltage of the comparator is about 10 mV without any mismatch compensations. The capacitance method can't compensate the mismatch with sufficient accuracy. The current method can compensate sufficiently however power consumption is large.

This timing method using a NMOS transistor, shown in figure 6 (a), exhibits a smaller mismatch voltage; however, power consumption is very large. This is due to the large PMOS transistor for variable delay inverter inserted to the clock circuit. PMOS type, shown in figure 6 (b), provides the best balance between compensation accuracy, delay time, and power consumption. Thus we used this PMOS type circuit.

Figure 7 shows the layout of the comparator. The area for compensation is not too large in comparison with the core comparator circuit.


Fig. 5. Mismatch compensation by variable delay circuit.

(a) NMOS type

(b) PMOS type

Fig. 6. Variable delay circuits for NMOS type and PMOS type.

Table 1. The comparison of several mismatch methods.

|  | no CAL | Cur CAL | Cap CAL | Time CAL_N | Time CAL_P |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\sigma_{\text {offser }}[\mathrm{mV}]$ | 10.1 | 1.32 | 5.79 | 1.09 | 1.49 |
| Power@ 500 MHz <br> $[\mu \mathrm{W}]$ | 14.5 | 41.3 | 21.4 | 49.4 | 24.5 |
| Delay $[\mathrm{ps}]$ | 365 | 450 | 756 | 682 | 511 |

## C. Overall design of $A D C$

Figure 8 shows an overall block diagram of this ADC. Eight sample and hold circuits are located at the input part. Two-bit gate-interpolated comparators [6] are located between the sample and hold circuits. The sample and hold circuit is useful to increase available input frequency and to realize flexible interfacing to the signal whose common voltage is different from the common voltage of the ADC. It however increases input capacitance, input switching current, and power dissipation of the ADC since the driving power for the sample and hold circuit will increase. In contrast, the gateinterpolation method can reduce these power consumptions without a serious scarifice in the ADC's performance. 6-bit up and down counters are used for the digital mismatch compensation.

Figure 9 shows a chip layout of this ADC. An occupied area is about $0.083 \mathrm{~mm}^{2}$. The chip has been fabricated in 90 nm CMOS technology with deep N -well option.


Fig. 7 The layout of comparator.


Fig. 8. Overall block diagram of the ADC.


Fig. 9. Chip layout of the ADC.

## IV. EXPERIMENTAL RESULTS

Figure 10 shows the measured DNL and INL at the conversion rate of $600 \mathrm{MS} / \mathrm{s}$ at $V_{\mathrm{DD}}$ of 0.5 V , with and without offset calibration. The DNL is less than $+/-0.8$ LSB and INL is less than $+/-1.0$ LSB.

Figure 11 (a) shows a spur free dynamic range (SFDR) and signal to noise and distortion ratio (SNDR) versus the conversion rate when the input signal frequency is about 50 MHz. The SNDR remains higher than 27 dB (4.2 ENOB) until $600 \mathrm{MS} / \mathrm{s}$. Figure 11 (b) shows SFDR and SNDR versus the input frequency at the sampling rate of $600 \mathrm{MS} / \mathrm{s}$. The effective resolution bandwidth (ERBW) is about 200 MHz .

An ultra-low voltage operation of 0.5 V has been attained with a small power consumption of 1.2 mW and a high conversion frequency of $600 \mathrm{MS} / \mathrm{s}$. Also, a very low FoM of $160 \mathrm{fJ} /$ conv.step has been obtained from ERB. The current for the reference ladder is about $300 \mu \mathrm{~A}$ and the body bias leakage current is $10 \mu \mathrm{~A}$. Table 2 summarizes the performance of this ADC and compares it to the previous relevant works.


Fig. 10. DNL and INL at $600 \mathrm{MS} / \mathrm{s}$ and 0.5 V .


Fig. 11. SFDR and SNDR vs. conversion rate and input frequency.

Table. 2 Performance summary and comparison.

| Reference \# | $[7]$ | $[8]$ | $[9]$ | $[10]$ | This work |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Resolution (bit) | 5 | 5 | 5 | 5 | $\mathbf{5}$ |
| fs (GS/s) | 0.5 | 1.75 | 1.75 | 0.06 | $\mathbf{0 . 6}$ |
| SNDR (dB) | 26 | 30 | 30 | 26 | $\mathbf{2 7}$ |
| Pd (mW) | 5.9 | 2.2 | 7.6 | 1.3 | $\mathbf{1 . 2}$ |
| Active area $\left(\mathrm{mm}^{2}\right)$ | 0.87 | 0.017 | 0.03 | - | $\mathbf{0 . 0 8 3}$ |
| Vdd (V) | 1.2 | 1 | 1 | 0.6 | $\mathbf{0 . 5}$ |
| FoM(fJ) | 750 | 50 | 150 | 1060 | $\mathbf{1 6 0}$ |
| CMOS Tech. $(\mathrm{nm})$ | 65 | 90 | 90 | 90 | $\mathbf{9 0}$ |
| Architecture | SAR | Fold+Flash | Flash | Flash | Flash |

## V. CONCLUSION

We attempted to reduce the supply voltage of a high speed ADC down to 0.5 V for future voltage lowering and low energy operation. A 5-bit Flash ADC has achieved a high conversion rate of $600 \mathrm{MS} / \mathrm{s}$ at a low supply voltage of 0.5 V . It consumes only 1.2 mW and an ultra-low FoM of 160 $\mathrm{fJ} /$ conv. step was attained. A forward body bias method and a gate-interpolated double-tail latched comparator with a variable delay method to compensate for the mismatch voltage are introduced.

## ACKNOWLEDEMENT

This work was partially supported by NEDO, CREST in JST and VDEC in collaboration with Cadence Design Systems, Inc.

## REFERENCES

[1] A. Matsuzawa, "High speed and low power ADC design with dynamic analog circuits", IEEE ASICON 2009, Changsha, China, pp. 218-221, Oct. 2009.
[2] T. Kuroda and T. Sakurai," Overview of low power ULSI circuit techniques," IEICE Tran, on Electronics, E78-C [4], pp. 334344, 1995.
[3] S. Muto, T. Douseki, Y. Matsuya, T. Aoki, S. Shigematsu, and J. Yamada, "1-V Power Supply High-Speed Digital Circuit Technology with Multi-threshold-Voltage CMOS,"IEEE J. Solid-State Circuits, Vol. 30, No. 8, pp. 847-854, 1995.
[4] M. Miyahara, Y. Asada, D. Paik, and A. Matsuzawa, "A LowNoise Self-Calibrating Dynamic Comparator for High-Speed ADCs," in Proc. IEEE A-SSCC, pp. 269-272, Nov. 2008.
[5] V. Giannini, et al., "An 820uW 9b 40MS/s Noise Tolerant Dynamic-SAR ADC in 90 nm Digital CMOS," in IEEE ISSCC 2008, Dig. of Tech. Papers, pp.238-239, Feb. 2008.
[6] Y. Asada, K. Yoshihara,T. Urano, M. Miyahara and A. Matsuzawa, "A 6bit, 7mW, 250fJ, 700MS/s Subranging ADC" in Proc. IEEE A-SSCC, pp. 141-144, Nov. 2009.
[7] B. P. Ginsburg and A. P. Chandrakasan, "500-MS/s 5-bit ADC in $65-\mathrm{nm}$ CMOS With Split Capacitor Array DAC," IEEE J. Solid-State Circuits, Vol. 42, No. 4, pp. 739-747, 2007.
[8] B. Verbruggen, J. Craninckx, M. Kuijk, P. Wambacq, and G. Van der Plas, " A $2.2 \mathrm{~mW} 5 \mathrm{~b} 1.75 \mathrm{GS} / \mathrm{s}$ Folding Flash ADC in 90 nm Digital CMOS," IEEE, ISSCC 2008, Dig. Tech. Papers, pp. 252-253, Feb. 2008.
[9] B. Verbruggen, P. Wambacq, M. Kuijk, and G. Van der Plas, "A $7.6 \mathrm{~mW} 1.75 \mathrm{GS} / \mathrm{s} 5 \mathrm{~b}$ Flash A/D converter in 90 nm digital CMOS," in Dig. Symp. VLSI Circuits, pp.14-15, June, 2008.
[10] J. E. Proesel and L. T. Pileggi, "A 0.6-to-1V Inverter-Based 5bit Flash ADC in 90nm Digital CMOS," IEEE, CICC 2008, Dig. Tech. Papers, pp. 153-156, Sep. 2008.

