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# A 200-GHz Inductively Tuned VCO With –7-dBm Output Power in 130-nm SiGe BiCMOS

Pei-Yuan Chiang, Student Member, IEEE, Omeed Momeni, Member, IEEE, and Payam Heydari, Senior Member, IEEE

Abstract—A highly efficient push-push voltage-controlled oscillator (VCO) with a new inductive frequency tuning topology for (sub) terahertz frequencies is presented. The tuning technique is based on a variable inductance seen at the emitter node of a base-degenerated transistor. The variable inductor exhibits high quality factor and high tuning range due to the tunable transistor transconductance via bias current. Fabricated in a 0.13-µm SiGe BiCMOS process, the VCO achieves a tuning range of 3.5% and an output power of -7.2 dBm at 201.5 GHz. The dc power consumption of the VCO is 30 mW, resulting in a high dc to RF power efficiency of 0.6% and a figure of merit (FoM<sub>T</sub>) of -165, which is the highest FoM for any silicon-based VCO reported to date at this frequency range. To demonstrate the functionality of the tuning technique, three VCO prototypes at different oscillation frequencies, including one operating in the 222.7-229-GHz range, are implemented and measured.

*Index Terms*—Clapp oscillator, Colpitts oscillator, inductive tuning, push–push oscillator, submillimeter wave, terahertz (THz), varactor-less tuning, voltage-controlled oscillator (VCO).

#### I. INTRODUCTION

IGH-FREQUENCY range including (sub) terahertz (THz) and millimeter-wave (mm-wave) presents a great promise for noninvasive active and passive imaging, chemical, and biological spectroscopy, multigigabit wireless communications, and short-range radars [1]-[5]. Towards realization of a high-performance (sub) THz system, one of the most challenging steps is to design a high-power, tunable, and efficient signal source [6]-[8]. A traditional way of designing a solid-state high-frequency signal source is to have a tunable low-frequency signal source, followed by a chain of Schottky diode multipliers and amplifiers in compound semiconductors [9]. Despite their limited cutoff frequency and breakdown voltage, recent advances in silicon-based technologies have made them potential candidates for implementation of highly integrated THz radiators and detectors. Recently, high-power and high-frequency oscillators have been demonstrated in silicon [10], [11]. However, having a power-efficient tunable

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signal source is necessary for many practical applications. A conventional and widely used way of controlling the oscillation frequency is to implement varactors in an *LC* oscillator [12], [13]. Nevertheless, a tight tradeoff exists between quality factor (*Q*-factor) and  $C_{\rm max}/C_{\rm min}$  tuning ratio of varactors, which will be more stringent at higher frequencies. While the use of minimum-length varactors can improve the *Q*-factor, it decreases the tuning ratio due to parasitic capacitors. Furthermore, the varactors' loss varies significantly across the tuning range, resulting in dramatic variation in output power due to the limited negative resistance that transistors can provide at high frequency.

On the other hand, as oscillation frequency increases towards the THz band, the inductor size will decrease almost quadratically. This implies: 1) achieving Q-factors as high as 15-20 for small-size inductors (around 100 pH) is possible and 2) magnetic coupling with a coupling coefficient of 0.7 or more can be achieved. Therefore, inductive tuning VCOs can be considered as viable candidates for wider tuning range and higher and relatively constant output power across the band at mm-wave and THz frequencies. Varactor-less voltage-controlled oscillators (VCOs) using transformer coupling feedback have already been proposed for a wide-tuning-range and high-Q-factor LC tank [14]–[16]. The tuning range of this transformer-coupled inductance is determined by the mutual inductance M and the primary and secondary windings' current ratio which degrades at high frequency. Another varactor-less tuning topology is to introduce controllable phase delay along a ring oscillator [17].

In this paper, which is an extension of the work published in [18], an inductive tuning topology based on a variable inductance seen at the emitter of an RL-degenerated amplifier has been developed. This variable inductor exhibits a high quality factor and high tuning range due to the base-degenerated inductor and resistor. This inductor introduces a negative resistance that compensates fpr  $1/g_m$  loss seen from the emitter node. Moreover, the base-degenerated resistor forms a tunable inductor controlled by the transistor's bias current. To verify the feasibility of this approach, multiple VCOs at different frequencies, including 198~205 GHz, 209~215 GHz, 218~225 GHz, and 223~229 GHz, are designed and implemented. The VCO, operating at 198~205 GHz, can achieve an output power of  $-7.2 \sim -7.75$  dBm and a dc power of 30 mW. The tuning range is 3.5% and the power efficiency is 0.6%. To the best of the authors' knowledge, this work presents the highest frequency inductively tuned oscillator with the highest power efficiency among silicon-based VCOs.

This paper is organized as follows. In Section II, the proposed inductive tuning circuit is introduced and analyzed. In

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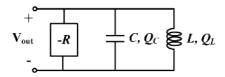


Fig. 1. *LC* tank with negative resistance.

Section III, test setup and measurement results of the 200-GHz inductively tuned push–push VCO are illustrated. In Section IV, we present the experimental results of the proposed tuning circuit, and Section V concludes the paper.

#### II. INDUCTIVE TUNING CIRCUIT

Shown in Fig. 1 is an *LC* tank with a negative resistance cell where  $Q_C$  and  $Q_L$  represent the *Q* factor of the capacitor and the inductor, respectively. If the negative resistance cell, which is usually implemented using cross-coupled or Colpitts topologies, compensates for the loss of the *LC* tank, then the *LC* tank starts to oscillate. The oscillation frequency  $\omega_{osc}$  and *Q* factor of the tank  $Q_{tank}$  are expressed as [19]

$$\omega_{\rm osc} = \frac{1}{\sqrt{L(C+C_P)}} \quad Q_{\rm tank} = \frac{Q_C Q_L}{Q_C + Q_L} \tag{1}$$

where  $C_p$  denotes the parasitic capacitor of the negative resistor. The conventional varactor tuning is losing its advantages at high frequencies. The parasitic capacitors dominate the total capacitance and degrade the tuning range. Furthermore, low Q factor of varactors (i.e., only 2~5 at 100 GHz) compared with  $Q_L$  of 20 decreases the Q factor of the *LC* tank, leading to smaller output power and higher phase noise. On the other hand, inductive tuning can be used to achieve higher  $Q_{tank}$  and tuning range, making it attractive for high-frequency VCO design.

#### A. Inductive Tuning Mechanism Using RL-Degenerated Transistor

It is commonly known that an emitter follower circuit with a small base resistor will generate an inductive reactance seen at the emitter node. Also, an inductor placed at the base terminal causes the emitter follower circuit to go to an unstable region due to the negative resistor at the emitter node. We investigate a series RL circuit to be employed as the degeneration network of an emitter follower circuit for frequency tuning. To illustrate the idea, we first look into a differential base-degenerated amplifier shown in Fig. 2(a). The circuit is comprised of transistors  $T_3 - T_4$ , the series RL network  $R_{BB} - L_{BB}$ , and a tail current  $I_E$ . The input impedance  $Z_{in}$  can be expressed as

$$Z_{\rm in} = \frac{R_{BB} + r_{\pi} + j\omega(L_{BB} + r_{\pi}C_{\pi}R_{BB}) - \omega^2 r_{\pi}C_{\pi}L_{BB}}{1 + g_{m_{3,4}}r_{\pi} + j\omega r_{\pi}C_{\pi}}$$
(2)

$$\cong \frac{(R_{BB} + r_{\pi} - \omega^2 r_{\pi} C_{\pi} L_{BB})(1 + j\omega/z_0)}{g_{m_{3,4}} r_{\pi} (1 + j\omega/p_0)}$$
(3)

$$=R_1 \|j\omega L_1 + R_2 \tag{4}$$

in which

$$z_0 = \frac{R_{BB} + r_\pi - \omega^2 r_\pi C_\pi L_{BB}}{L_{BB} + r_\pi C_\pi R_{BB}} \quad p_0 = \frac{g_{m_{3,4}}}{C_\pi} = \omega_T \quad (5)$$

$$R_2 = \frac{R_{BB}}{g_{m_{3,4}}r_{\pi}} + \frac{1}{g_{m_{3,4}}} - \frac{\omega^2 L_{BB}}{\omega_T}.$$
 (6)

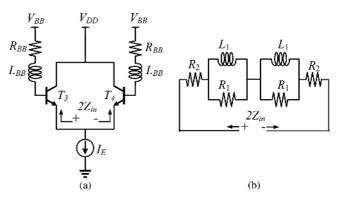


Fig. 2. (a) Differential RL-degenerated transistor pair and (b) its equivalent circuit.

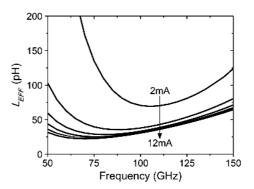


Fig. 3. Simulated  $L_{\rm EFF}$  with respect to frequency for different values of  $I_E$  from 2 to 12 mA.

Assuming  $g_{m3,4}r_{\pi}$ , (2) is simplified to (3), which resembles the expression for the impedance of a network comprising a parallel  $R_1 - L_1$  in series with  $R_2$ , as shown in Fig. 2(b). Substituting (5) and (6) into (2) results in the following closed-form expressions for  $R_1$  and  $L_1$ :

$$R_{1} = R_{2} \left(\frac{p_{0}}{z_{0}} - 1\right)$$
$$= R_{BB} - \frac{1}{g_{m_{3,4}}} + \left(\left(\frac{\omega}{\omega_{T}}\right)^{2} + \frac{1}{g_{m_{3,4}}r_{\pi}}\right)\omega_{T}L_{BB}$$
(7)

$$L_{1} = \frac{R_{1}}{p_{0}} = \frac{R_{BB}}{\omega_{T}} - \frac{1}{g_{m_{3,4}}\omega_{T}} + \left(\left(\frac{\omega}{\omega_{T}}\right)^{2} + \frac{1}{g_{m_{3,4}}r_{\pi}}\right)L_{BB}.$$
 (8)

Substituting (6)–(8) into (4) yields a closed-form expression for driving point impedance seen from the emitter node of  $T_3$ , i.e.,

$$Z_{\rm in} \cong \frac{1}{g_{m_{3,4}}} - \frac{\omega^2 L_{BB}}{\omega_T} + \frac{\omega^2 R_{BB}}{\omega_T^2} + j\omega \left[ \frac{R_{BB}}{\omega_T} - \frac{1}{g_{m_{3,4}}\omega_T} + \frac{\omega^2 L_{BB}}{\omega_T^2} \right] = R_{EFF} + j\omega L_{\rm EFF}.$$
(9)

 $R_2$  in (6) is dominated by the last two terms, as  $R_{BB}$  (in the range of tens of ohms) is divided by the transistor's current gain  $\beta_{3,4}$  ( $\geq 100$ ). It will be equal to  $1/g_{m3,4}$  if there is no  $L_{BB}$  and  $R_{BB}$ , as expected.  $L_{BB}$  contributes a negative term to both  $R_2$  and  $Z_{in}$ , thereby decreasing equivalent series loss of the variable inductor.  $R_{BB}$  is added to have inductance tuning ability via  $I_E$ . From (8),  $R_{BB}$  helps to boost variable inductance. From

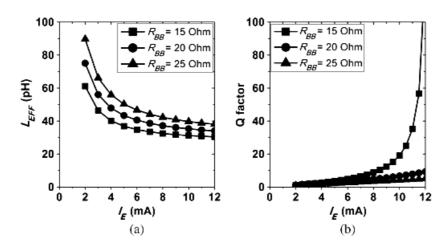


Fig. 4. (a) Simulated  $L_{\rm EFF}$  versus  $I_E$  at 100 GHz for three different values of  $R_{BB}$ . (b) Corresponding quality factor.

(9), one can infer that the equivalent inductor  $L_{\text{EFF}}$  varies with  $I_E$  (through  $g_{m3,4}$ ). Furthermore,  $R_{\text{EFF}}$  is reduced due to  $L_{BB}$ , and, thus, the quality factor is improved.

Fig. 3 shows the simulated  $L_{\rm EFF}$  as a function of frequency with differential tail current  $I_E$  varying from 2 to 12 mA. In this simulation, the transistor size is 6  $\mu$ m/0.13  $\mu$ m,  $R_{BB}$  is 15  $\Omega$ , and  $L_{BB}$  is 60 H. From Fig. 3, as  $I_E$  increases from 2 to 12 mA  $L_{\rm EFF}$  decreases from 70 to 30 pH around the 100-GHz fundamental frequency.

A tradeoff exists between the tuning range and quality factor of  $L_{\rm EFF}$ , as both  $L_{\rm EFF}$  and  $R_{\rm EFF}$  are directly affected by  $R_{BB}$ . Shown in Fig. 4(a) is  $L_{\rm EFF}$  versus  $I_E$  at 100 GHz with three different values of  $R_{BB}$ , where  $L_{BB}$  is set to 60 pH. The simulated  $L_{\rm EFF}$  increases with  $R_{BB}$ , while  $L_{\rm EFF} - I_E$  variation follows the same behavior for all three values of  $R_{BB}$ . Fig. 4(b) depicts simulated Q factor of  $L_{\rm EFF}$  with respect to  $I_E$  and shows that higher values of  $R_{BB}$  results in lower Q factor. Fig. 5 shows the simulated Q factor at 100 GHz versus  $I_E$  for three different values of  $L_{BB}$ , where  $R_{BB}$  is fixed at 15  $\Omega$ . In the low- $I_E$  region, the Q factor is low because the transistors are not fully biased in forward active region. Once the transistors are biased in forward active region, the Q factor will increase. The Q factor will be boosted from 5 to 25 at  $I_E = 10$  mA when  $L_{BB}$  increases from 50 to 60 pH. This notion is also verified in (9).

Note that, if  $L_{BB}$  is chosen to be too large, it may cause an undesired oscillation due to the fact that the negative part of  $R_{\text{EFF}}$  will start dominating the other terms.

#### B. Transformer-Coupled Inductive Tuning Circuit

The proposed inductive tuning circuit is shown in Fig. 6(a), where a 1:1 differential  $L_T$  transformer with coupling factor  $k_C$ is used to couple  $L_{EFF}$  to the oscillator's tank. The transformer isolates the dc bias current of the core oscillator from  $I_E$ , which is varying to achieve inductive tuning. A separate constant dc bias current is necessary for a VCO core because it provides constant negative resistance even in lower current tuning region. Furthermore, transformer coupling decreases the variation of Qfactor. As shown in Fig. 5, the Q factor variation with a constant  $L_{BB}$  can be as high as 55. Such variation may lead to significant change in VCO output power, or it may even dampen the oscillation in the low Q region. To address this, the half equivalent

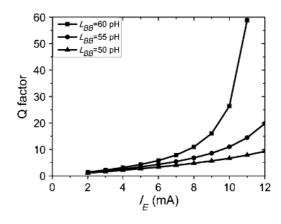


Fig. 5. The simulated Q factor of  $L_{EFF}$  at 100 GHz for three values of  $L_{BB}$ .

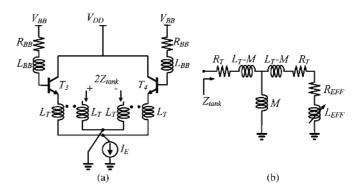


Fig. 6. (a) Proposed transformer coupled inductive tuning circuit and (b) it's half equivalent circuit.

circuit of the differential transformer coupled inductive tuning circuit in Fig. 6(a) is shown in Fig. 6(b). A T model [20] is used to represent the 1:1 transformer in Fig. 6(a).  $R_T$  represents the series loss of primary and secondary inductors and M denotes the mutual inductance. Assuming  $Q^2$  of both the transformer and  $L_{\rm EFF}$  to be much larger than 1,  $Z_{\rm tank}$  can be expressed as

$$Z_{\text{tank}} \cong R_T + \frac{(R_T + R_{\text{EFF}})M^2}{(L_T + L_{\text{EFF}})^2} + j\omega \left(\frac{L_T L_{\text{EFF}} + L_T^2 - M^2}{L_T + L_{\text{EFF}}}\right).$$
(10)

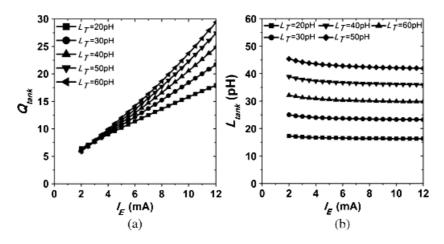


Fig. 7. (a) Simulated quality factor  $Q_{\text{tank}}$  of  $Z_{\text{tank}}$ . (b) Inductor  $L_{\text{tank}}$  of  $Z_{\text{tank}}$  at 100 GHz, where  $L_{BB}$  is 60 pH,  $R_{BB}$  is 15  $\Omega$ , and the coupling factor  $k_C$  is 0.7.

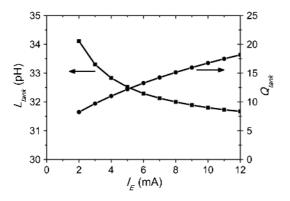


Fig. 8. Simulated inductance and Q factor of  $L_{\text{tank}}$  at 100 GHz, where  $L_T = 30 \text{ pH}$ ,  $k_C = 0.7$ ,  $L_{BB} = 60 \text{ pH}$ , and  $R_{BB} = 15 \Omega$ .

Since, according to (10),  $Z_{tank}$  will retain higher percentage of the tuning range contributed by  $L_{\rm EFF}$  as the transformer coupling increases, the transformer is designed to achieve a  $k_C$ factor of 0.7 and a Q factor of 15. Shown in Fig. 7(a) is the simulated Q factor of  $Z_{tank}$ ,  $Q_{tank}$ , with five  $L_T$  values, where  $L_{BB}$  and  $R_{BB}$  are set to be 50 pH and 15  $\Omega$ , respectively. At the low  $I_E$  region,  $Q_{\text{tank}}$  is 6, which is higher than that of  $L_{\text{EFF}}$ in Fig. 5. As  $I_E$  increases,  $Q_{tank}$  will increase due to a decrease in  $R_{\rm EFF}$ . Moreover, higher  $L_T$  leads to additional improvement in  $Q_{\text{tank}}$ , for a given  $I_E$ . As also shown in Fig. 7(b), for  $L_T$  varying from 20 to 60 pH, the tuning range slightly increases from 7% to 9%, while the average value of  $L_{tank}$  also increases from 18 to 45 pH. Therefore, the  $L_T$  transformer has to be designed based on the desired oscillation frequency with maximum achievable coupling factor. For the VCO in this work,  $L_T = 30 \text{ pH}, L_{BB} = 60 \text{ pH}$  and  $R_{BB} = 15 \Omega$ , and the simulated  $L_{tank}$  and  $Q_{tank}$  versus  $I_E$  are shown in Fig. 8. The VCO with the proposed inductive tuning topology achieves an overall Q factor three times as high as the varactors' at 100 GHz. This Q factor will further increase towards the higher end of the tuning range. This helps the flatness of the VCO output power across the tuning range, because the higher Q factor at higher oscillation frequency compensates for degradation of the transistors' transconductance with frequency.

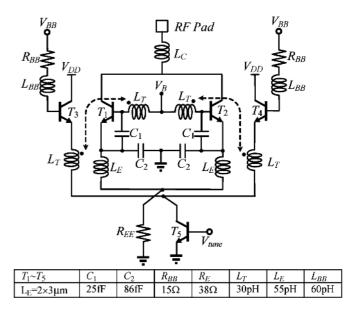


Fig. 9. Proposed inductively tuned push-push 200-GHz VCO.

#### III. INDUCTIVELY TUNED PUSH-PUSH VCO

Colpitts topology has proved to achieve a higher maximum oscillation frequency than a cross-coupled pair counterpart [21], [22], due to a nonunity-gain feedback loop realized using the tapped capacitor resonator, which decreases the capacitance contribution of  $C_{\pi}$  into the *LC* tank. Moreover, the phase noise of a Colpitts oscillator is a function of capacitive division ratio [22], making it more flexible to achieve a lower phase noise. Shown in Fig. 9 is the proposed schematic of the Colpitts push-push inductively tuned VCO. Owing to the core circuit comprising the transistor  $T_1(T_2)$  and tapped capacitor network  $C_1 - C_2$ , a negative resistance can be seen at the base or collector nodes due to a capacitive feedback around these two nodes. The tank inductor  $L_T$  is placed at the base of  $T_1(T_2)$ , whose loss is compensated by the negative resistance. The oscillation frequency will be  $1/[L_T C_1 C_2/(C_1 + C_2)]^{1/2}$ . Together with the inductive tuning circuit composed of  $R_{BB}$ ,  $L_{BB}$ , and  $T_3(T_4)$ , the oscillation frequency can be tuned by changing  $V_{\rm tune}$ . Note that, once oscillating, the second-harmonic signal

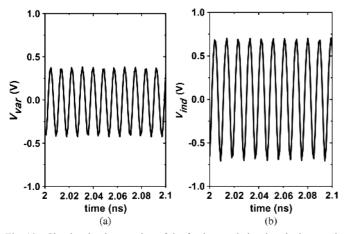


Fig. 10. Simulated voltage swing of the fundamental signal at the base node of a Colpitts VCO core for (a) conventional varactor-tuning VCO and (b) the proposed inductive-tuning VCO.

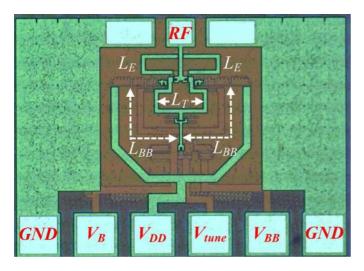


Fig. 11. Die photograph of the inductively tuned VCO where the chip area is  $250 \times 290 \ \mu m^2$  excluding the pad ring.

can be extracted at any common-mode node of the VCO. In Fig. 9, the second harmonic is extracted from collectors in order to achieve higher output power. The primary reason is that the major portion of the second-harmonic current generated by transistors  $T_1 - T_2$  will flow out from their collector nodes to the output load, while, for the other common-mode nodes, the inherent current division will degrade the output power. Also, placing the tank inductor at the base node eliminates the passive loss in the second signal path which would otherwise exist if that inductor would have been placed at collector node. The resistor  $R_{EE}$  is used to improve common mode rejection. However, there is a tradeoff between the second-harmonic output power and  $R_{EE}$  value to improve common-mode rejection, as  $R_{EE}$  is also in the second-harmonic path.

The inductor  $L_C$  in Fig. 9 models the wiring interconnection from collectors to RF pads and is considered to be part of the output-matching network along with the RF pad's parasitic capacitor. The common-mode node between  $C_2$ 's is grounded to improve output matching at the second harmonic. With a bias-T implemented on a ground–signal–ground (GSG) waveguide probe, the dc supply voltage can be applied directly into

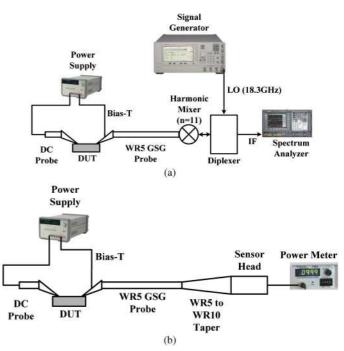


Fig. 12. (a). The 200-GHz VCO oscillation frequency measurement setup. (b). The 200-GHz VCO output power measurement setup.

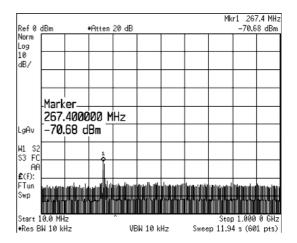


Fig. 13. IF tone shown on the spectrum analyzer after the VCO's 201.6-GHz output signal was down-converted by a harmonic mixer  $(n\ =\ 11)$  and LO frequency of 18.3 GHz.

the circuit, while the signal can be brought out from this probe to measurement equipment.

As illustrated in Section II, the Q factor of the proposed inductive-tuning LC tank is higher than that of the conventional varactor-tuning LC tank. A varactor-tuning VCO with the same oscillation frequency and tuning range is designed for comparison. The base voltage swing of the fundamental signal for transistor  $T_1(T_2)$  is simulated and shown in Fig. 10, where the voltage swing of the inductive-tuning VCO is higher than the conventional one. This higher voltage swing means that: 1) the Q factor of the LC tank is higher as long as the swing does not exceed saturation region; 2) transistors  $T_1 - T_2$  can generate a stronger second-harmonic signal; and 3) phase noise is improved due to

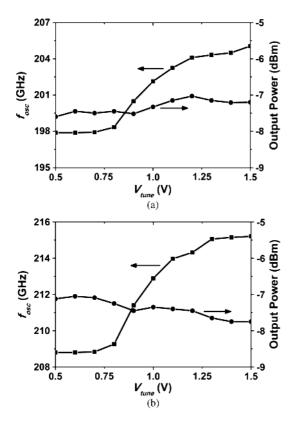


Fig. 14. Measured oscillation frequency and output power versus  $V_{tune}$  of (a) 200-GHz VCO and (b) 210-GHz VCO.

the fact that it is proportional to  $1/Q_{\text{tank}}$  [23]. In our simulation, the output power of the proposed inductive-tuning VCO is 3 dBm higher than that of the conventional counterpart.

#### IV. MEASUREMENT SETUP AND EXPERIMENTAL RESULTS

The proposed inductive tuning VCO was designed and fabricated in a 0.13- $\mu$ m SiGe BiCMOS technology. All of the transformers and inductors were implemented on the two topmost metal layers, M5-M6, with the bottom metal layer M1 being used as a ground plain, shielding from the lossy substrate. Fig. 11 shows the chip photograph of the VCO with a chip area of  $250 \times 290 \ \mu$ m<sup>2</sup> excluding the pad ring. All of the elements and routing lines have been placed symmetrically in order to minimize mismatch and improve overall performance.

The 200-GHz VCO frequency and power measurement setups were configured as shown in Fig. 12(a) and (b). For frequency measurement, the VCO output signal was brought through the RF probe to a harmonic mixer, then down-converted to around 5 GHz, and measured on a spectrum analyzer. In Fig. 12(a), a GGB WR5 GSG probe with bias tee, an Agilent E4407 spectrum analyzer, a Pacific Millimeter GM harmonic mixer and MD4A diplexer are used to verify the oscillation frequency. Fig. 13 shows the down-converted 201.6-GHz VCO output signal when an LO signal of 18.3 GHz and a harmonic number of 11 is utilized. Due to the narrow IF bandwidth of the diplexer compared with the tuning range of the VCO, the LO frequency needs to be adjusted with respect to the VCO oscillation frequency. To accurately measure the output

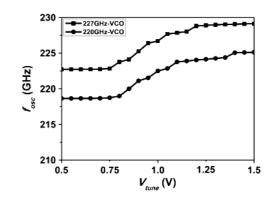


Fig. 15. Measured oscillation frequency of the 220- and 227-GHz VCOs.

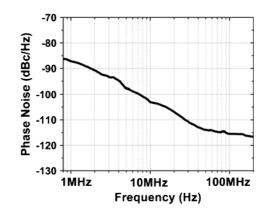


Fig. 16. Measured phase noise of the 200-GHz VCO.

power, a direct power measurement setup was used, as shown in Fig. 12(b). The WR5 GSG probe is converted to a WR10 waveguide via a taper, and then connected to a power sensor and an Erickson PM4 power meter. The measured output power levels need to be calibrated by 3.25 dB to account for the loss of the probe, waveguide extension, and taper.

Fig. 14(a) shows the measured oscillation frequency and output power of the 200-GHz VCO with respect to the tuning voltage,  $V_{\text{tune}}$ . By controlling  $V_{\text{tune}}$  from 0.5 to 1.5 V, the oscillation frequency is varied from 198 to 205 GHz, resulting in a tuning range of 3.5%. The measured output power is -7.2 dBm with less than 0.5-dB variation across the band. Fig. 14(b) shows the measured performance of a 212-GHz VCO prototype, which was designed using the same topology. The tuning range is from 209 to 215 GHz with -7.1-dBm output power. Both VCOs consume a dc power of 30-57 mW with respect to  $V_{tune}$ . As shown in Fig. 15, two additional VCOs were implemented for 220 and 227 GHz. The measured tuning range is 6 GHz when the maximum oscillation frequency extends to 229 GHz. Due to the bandwidth limitation of WR5 waveguide (140-220 GHz), the output power of these two VCOs could not be measured accurately. Fig. 16 shows the measured phase-noise profile of the 200-GHz VCO, wherein the phase noises of -87.2 and -103.1 dBc/Hz are reported at 1- and 10-MHz offset, respectively. Table I shows the performance comparison with prior work. The proposed VCOs show a maximum figure of merit (FoM) (FoM<sub>T</sub>) of -165.6,

	This Work	This Work	[24]	[25]	[26]	[27]	[28]	[29]
Frequency (GHz)	201.5	212	161.1	184.2	277.6	196.5	139	290
Tuning Range	3.5%	2.8%	4.7%	2%	1.5%	1.5%	0.09%	4.5%
Power(dBm)	-7.2	-7.1	-15	-11	-20	-19	-19	-1.2*
DC Power (mW)	30 (min.)	30 (min.)	46.5	95	132	29	9.6	325
Power Efficiency	0.64%	0.65%	0.068%	0.084%	0.0076%	0.087%	0.13%	0.23%
PN @ 1MHz (dBc/Hz)	-87	-92	-86	NA	NA	-94	-79	-78
FOM <sub>T</sub> **	-162	-165.6	-151.9	NA	NA	-150	-112.1	-154
Technology	0.13μm SiGe	0.13μm SiGe	0.25μm SiGe	0.13µm SiGe	0.13μm SiGe	90nm CMOS	90nm CMOS	65nm CMOS

TABLE I VCO Performance Comparison

\* Power combination of four cross-coupled oscillators.

\*\* FoM<sub>T</sub> =  $PN - 20 \log((f_o/\Delta f) \cdot (FTR/10)) + 10 \log(P_{\text{DISS}}/1 \text{ mW}) - P_{\text{out}}$ 

which was the highest compared with the state of the art in silicon-based VCOs.

#### V. CONCLUSION

A varactor-less push-push VCO topology has been presented and analyzed for mm-wave and THz frequency bands. Four VCOs with different frequencies have been implemented to show the feasibility of the proposed approach. The maximum tuning range is 3.5% and highest oscillation frequency is 229 GHz. A power efficiency of 0.65% was achieved with an output power of -7.2 dBm. The proposed inductive tuning topology increases the Q factor of the VCO *LC* tank, which improves the output power and phase noise, resulting in a higher FoM among the other silicon-based low-THz VCOs.

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