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# A bar signature and central disc in the gaseous and stellar velocity fields of NGC 5448 

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#### Abstract

We analyse Spectrographic Areal Unit for Research on Optical Nebulae (SAURON) kinematic maps of the inner kiloparsec of the early-type (Sa) barred spiral galaxy NGC 5448. The observed morphology and kinematics of the emission-line gas is patchy and perturbed, indicating clear departures from circular motion. The kinematics of the stars is more regular, and display a small inner disc-like system embedded in a large-scale rotating structure. We focus on the [ $\mathrm{O}_{\mathrm{III}}$ ] gas, and use a harmonic decomposition formalism to analyse the gas velocity field. The higher order harmonic terms and the main kinematic features of the observed data are consistent with an analytically constructed simple bar model. The bar model is derived using linear theory, considering an $m=2$ perturbation mode, and with bar parameters that are consistent with the large-scale bar detected via imaging. We also study optical and near infrared images to reveal the asymmetric extinction in NGC 5448, and we recognize that some of the deviations between the data and the analytical bar model may be due to these complex dust features. Our study illustrates how the harmonic decomposition formalism can be used as a powerful tool to quantify non-circular motions in observed gas velocity fields.


Key words: galaxies: bulges - galaxies: evolution - galaxies: formation - galaxies: kinematics and dynamics - galaxies: spiral - galaxies: structure.

## 1 INTRODUCTION

Dynamical studies of spiral galaxies often make the distinction between the bulge and the disc: the bulge is associated with the hot 'spheroidal' component which mainly contains stars, and the disc is a rapidly rotating thin structure which also contains a substantial fraction of the total amount of interstellar gas. Line-of-sight velocity distributions are efficient probes of the dynamical structures of these systems, and can be used to derive the mass distribution, structural properties and perturbations of the gravitational potential linked to $m=1$ or $m=2$ modes, or to external triggers such as interactions. These can be obtained with classical long-slit spectrography, although it requires a priori assumptions for the orientation of the slits. A time-consuming way to obtain velocity fields through single slits is to spatially scan the galaxy with successive individual exposures (e.g. Statler 1994; Ohtani 1995). Integral field spectrography in the optical (IFS; Adam et al. 1989; Afanasiev et al. 1990;

[^0]Bacon et al. 1995; Davies et al. 1997; García-Lorenzo, Arribas \& Mediavilla 2000; Roth, Laux \& Heilemann 2000; Bacon et al. 2001; Bershady et al. 2004) was designed to uniformly cover the field of view, which makes it possible to study these systems in a much improved way: the analysis is not constrained by a priori choices of slit position, and the gaseous and stellar components can be observed simultaneously. Optical IFS is often used complementarily to $\mathrm{H}_{\mathrm{I}}$ and Fabry-Perot scanning interferometers (e.g. van Gorkom et al. 1986; Plana \& Boulesteix 1996) as the latter usually have excellent spatial coverage but a limited spectral domain, only probing a couple of lines (mostly in emission).

Although circular rotation is the dominant kinematic feature of the disc component, previous observational as well as theoretical studies have shown the presence of non-circular motions (e.g. Freeman 1965; Combes \& Gerin 1985; Shlosman, Frank \& Begelman 1989; Shlosman \& Noguchi 1993; Athanassoula 1994; Moiseev 2000; Regan \& Teuben 2004; Wong, Blitz \& Bosma 2004). Cold disc-like systems are more prone than bulges to perturbations and instabilities, the dissipative gaseous component being more responsive than the stellar component (e.g. Thielheim \& Wolff 1982). Perturbations of
the gas dynamics can lead to significant galaxy evolution via, e.g. redistribution of the angular momentum, triggering of star formation or building of a central mass concentration.

Bars are potential actors in this context as they can drive mass inwards or outwards, and may participate in the complex process which eventually leads to the fuelling of an active nucleus (e.g. Simkin, Su \& Schwarz 1980; Sakamoto, Baker \& Scoville 2000). The presence of large-scale bars has been correlated with starbursts (e.g. Martinet \& Friedli 1997) and nuclear rings (Shlosman 1999), but only weakly, if at all, with nuclear activity (e.g. Knapen et al. 2000). This may not be so surprising as the fuelling of an active galactic nucleus (AGN), i.e. gas accretion onto a massive black hole involves rather small spatial and short time-scales, so might not be related to the kiloparsec-scale bar. Inner small bars (Shlosman et al. 1989) may sometimes help to link the different spatial scales (Emsellem, Goudfrooij \& Ferruit 2003), but they probably cannot serve as a universal mechanism. AGN activity is short lived and occurs in the central astronomical units of galaxies, whereas current studies have focused on long-lived phenomena influencing the central kiloparsec scale. In order to properly study the influence of a bar on the redistribution of mass in the central kiloparsec of a galaxy, we need to obtain constraints both on the source of the underlying gravitational potential and on some tracer of the ongoing perturbations. This can be achieved by simultaneously studying the stellar and gas dynamics.

We have observed 24 early-type spiral (Sa) galaxies with the Spectrographic Areal Unit for Research on Optical Nebulae (SAURON) Integral Field Spectrograph (Bacon et al. 2001), mounted at the 4.2-m William Herschel Telescope of the Observatorio del Roque de los Muchachos at La Palma (de Zeeuw et al. 2002). Most of these galaxies are found to have gas velocity fields that strongly deviate from that of a simple rotating disc. For the present study, we selected NGC 5448 out of the Sa SAURON sample, which shows a clear sign of the presence of a bar in its photometry and which has a significant amount of ionized gas (Falcón-Barroso et al. 2005). In this paper, we analyse both the stellar and gas kinematics obtained with SAURON, and quantify the non-circular gaseous motions in NGC 5448. To this aim, we build models with elliptical streaming motion and compare the resulting velocity structures with our observational data, using a harmonic decomposition technique. In Section 2, we present our data. Section 3 outlines our analysis method of the gas kinematics. In Section 4, we build a bar model for NGC 5448, and we present and discuss the corresponding results in Sections 5 and 6.

## 2 THE DATA

NGC 5448 is a barred Sa active galaxy with prominent irregular dust lanes at different spatial scales. The RC3 classification of NGC 5448 is (R)SAB(r)a, with inclination of $64^{\circ}$, systemic velocity of $1971 \mathrm{~km} \mathrm{~s}^{-1}$, position angle (PA) of $115^{\circ}$ and total $B$-band magnitude of 11.93 . Photometry shows that this galaxy hosts a large-scale bar with two well-defined spiral arms emerging near the ends of the bar (Eskridge 2002). The inner parts of the arms are somewhat patchy and form a broken ring, the outer parts of the arms being smoother (Sandage \& Bedke 1994). This galaxy has a nuclear elongated feature of about $10 \operatorname{arcsec}$ (Fathi \& Peletier 2003) with bluer $V-H$ colour than its surroundings (Carollo et al. 2002). Ho, Filippenko \& Sargent (1995) classified the nucleus as an AGN: its central aperture spectrum exhibits a clear broadline emitting region. Laine et al. (2002) classified NGC 5448 as a non-Seyfert.

Table 1. SAURON data characteristics.

| Field of view | $41 \times 33 \mathrm{arcsec}^{2}$ |
| :--- | :--- |
| Pixel size | 0.8 arcsec |
| Instrumental disp. | $108 \mathrm{~km} \mathrm{~s}^{-1}$ |
| Spectral range | $[4820-5280] \AA$ |
| Spectral features | $\mathrm{H} \beta,\left[\mathrm{O}_{\mathrm{III}}\right], \mathrm{Fe} 5015, \mathrm{Mg} b,[\mathrm{~N} \mathrm{I}], \mathrm{Fe} 5270$ |

### 2.1 SAURON observations

We observed NGC 5448 with SAURON on 2004 April 14. Detailed specifications for the instrument, data, reduction procedure and the data preparation procedure can be found in Bacon et al. (2001), de Zeeuw et al. (2002) and Emsellem et al. (2004). A brief summary of the instrument and data characteristics is presented in Table 1. We obtained four exposures of 1800 s each, producing a total of 1431 simultaneous galaxy spectra per frame, together with 146 sky spectra 1.9 arcmin away from the main field. We also observed standard stars to be used for accurate velocity, flux and line-strength calibration of our observed galaxy. Wavelength calibration was done using arc lamp exposures taken before and after each target exposure. The standard reduction was performed using the XSAURON software package developed at the Centre de Recherche Astronomique de Lyon (CRAL, Lyon), providing a fully calibrated datacube for each individual exposure. We merged the four spatially dithered exposures after a resampling to a common spatial scale of $0.8 \times$ $0.8 \mathrm{arcsec}^{2}$ pixel $^{-1}$, leading to a total of 1973 spectra within our field.

### 2.2 Stellar and gaseous kinematic maps

The signal-to-noise ratio $(S / N)$ of individual spectra varies considerably throughout the field; in order to homogenize the $S / N$ we applied the Voronoi 2D binning technique of Cappellari \& Copin (2003). We have set a target $S / N$ value of 60 to be able to derive reliable higher order moments of the stellar velocity distribution. Penalized Pixel Fitting (pPXF; Cappellari \& Emsellem 2004) was used to derive the stellar line-of-sight velocity distribution parametrized by a Gauss-Hermite series up to and including the fourth order (Gerhard 1993; van der Marel \& Franx 1993). The optimal stellar template in pPXF was built with a combination of stellar spectra from Jones (1997) and synthesis spectra from Vazdekis (1999) as in Emsellem et al. (2004). The derived stellar mean velocity $V$, mean velocity dispersion $\sigma$ and higher order velocity moments $h_{3}$ and $h_{4}$ maps, are presented in bottom row of Fig. 1. We discuss the maps in Section 5.

The method which we have applied to derive the emission-line kinematics is described and validated in Sarzi et al. (2005) and Falcón-Barroso et al. (2005). It consists of iteratively searching for the emission-line velocities and velocity dispersions, while solving at each step for both their amplitudes and the optimal combination of the stellar templates over the full SAURON wavelength range. No masking of the regions affected by emission is thus required.

Our binning scheme was optimized for the derivation of reliable stellar kinematics, but is not necessarily well adapted to analyse the emission-line gas. Since the gaseous component commonly rotates faster than the stellar component, to obtain reliable gas kinematics, in general a lower $S / N$ is required. Moreover, gas and stars do not necessarily share the same spatial distributions. As a consequence, the stellar bins are often larger than necessary for the gas, implying a loss of spatial information for analysing the gaseous component (Fathi 2004). Accordingly, the data that we present in this paper


Figure 1. Top left: Digitized Sky Survey image with SAURON footprint and north-east orientation arrow. All other panels show the SAURON data. The stellar flux map and unsharp-masked SAURON image are given in mag arcsec ${ }^{-2}$ with arbitrary zero point, and north-east direction as indicated. The titles are indicated at the bottom-right corner of each panel with plotting ranges according to the top colour bar. All SAURON maps have the same orientation with overplotted stellar contours in magnitude steps of 0.25 , and all velocities and velocity dispersions are given in $\mathrm{km} \mathrm{s}^{-1}$.
have a minimum stellar $S / N$ of 60 and a minimum emission-line amplitude-over-noise ratio of 3 .

Finally, we have carefully inspected the emission-line profiles to search for possible asymmetric profiles, but have not found any significant deviation from a pure Gaussian, nor any significant indication for more than one component being present in the profiles, at least at the instrumental resolution of SAURON. We know from other SAURON studies of, e.g. NGC 1068 (Emsellem et al. 2005) that we can resolve several components in very strong AGNs.

## 3 ANALYSING GAS VELOCITY FIELDS

### 3.1 Circular and non-circular kinematics

In this section, we start with a simple mathematical model, and then add complexity as required by the observational constraints. In the simplest model, the galactic disc is purely rotational, has negligible velocity dispersion and is infinitesimally thin. In the presence of axisymmetric radial and vertical velocities, and when taking into account the effect of projection and the convention that positive line-of-sight velocities correspond to recession, the line-of-sight veloci-
ties $V_{\text {los }}$ can be represented by

$$
\begin{align*}
V_{\mathrm{los}}(R, \psi, i)=V_{\mathrm{sys}} & +V_{\mathrm{rot}}(R) \cos \psi \sin i \\
& +V_{\mathrm{rad}}(R) \sin \psi \sin i \\
& +V_{z}(R) \cos i, \tag{1}
\end{align*}
$$

where $V_{\text {sys }}$ is the systemic velocity of the galaxy, $V_{\text {rot }}$ and $V_{\text {rad }}$ are the rotational and radial velocities and $V_{z}$ is the vertical velocity component, which we set to zero throughout this paper. The inclination $i$ of the galaxy ranges from $i=0^{\circ}$ for a face-on viewing and $i=90^{\circ}$ for an edge-on viewing. Furthermore, $(R, \psi)$ are polar coordinates in the plane of the galaxy related to observable Cartesian coordinates $x$ and $y$ (in the plane of the sky) by

$$
\left\{\begin{array}{l}
\cos \psi=\frac{-\left(x-X_{\mathrm{cen}}\right) \sin \phi_{0}+\left(y-Y_{\mathrm{cen}}\right) \cos \phi_{0}}{R}  \tag{2}\\
\sin \psi=\frac{-\left(x-X_{\mathrm{cen}}\right) \cos \phi_{0}-\left(y-Y_{\mathrm{cen}}\right) \sin \phi_{0}}{R \cos i}
\end{array}\right.
$$

where $X_{\text {cen }}$ and $Y_{\text {cen }}$ are the coordinates for the centre, and $\phi_{0}$ is the PA of the projected major axis of the disc, measured with respect to north in counterclockwise direction. This simple model cannot
explain most observed velocity fields. The gas kinematics in real galaxies exhibits radial and/or vertical motions due to, e.g. the presence of bars, spiral arms, which create angle-dependent velocities that cannot be explained using equation (1), and hence additional ingredients in the analysis method are required.

Several attempts have been made to investigate more complex velocity fields [Sakhibov \& Smirnov 1989; Canzian 1993; Schoenmakers, Franx \& de Zeeuw 1997 (hereafter SFdZ); Fridman \& Khoruzhii 2003; Wong et al. 2004; Krajnović et al. 2005]. The main idea of these techniques is to deal separately with the 'unperturbed' underlying component and the residual velocity field, obtained by subtracting the reconstructed unperturbed velocity field from the data. To solve the problem, as stated, one would have to know the unperturbed velocity component at a given radius. Unfortunately, we do not know beforehand the unperturbed velocity field. A powerful technique for unveiling the perturbations makes use of the expansion of the velocity information in Fourier harmonic components. Following the terminology of SFdZ (see their appendix for the detailed derivation), given that the line-of-sight velocity can be expressed as a two-dimensional analytic function of galactocentric coordinates, it can be written as a Fourier series
$V_{\mathrm{los}}=V_{\mathrm{sys}}+\sum_{n=1}^{k}\left[c_{n}(R) \cos n \psi+s_{n}(R) \sin n \psi\right] \sin i$,
where $k$ is the number of harmonics and $c_{n}$ and $s_{n}$ give us information about the nature of the perturbations, and they are tightly connected to the underlying potential. Note that $c_{1}=V_{\text {rot }}$ and $s_{1}=V_{\text {rad }}$. Furthermore, numerical simulations by Burlak et al. (2000) have shown that this formalism is very stable and its results are rather insensitive to the presence of holes in the velocity field.

### 3.2 Tilted-ring and harmonic decomposition

Our quantitative analysis uses the formalism of equation (3) combined with the tilted-ring method (Rogstad, Lockart \& Wright 1974; Rogstad, Wright \& Lockart 1976), inspired from the rotcur routine in the GIPSY package (Begeman 1987; van der Hulst et al. 1992). Accordingly, we divide the galaxy disc into concentric ellipses within which we fit the rotation velocity and the set of geometric parameters of equation (3). The method assumes that each pixel in the velocity field is identified with a unique position in the galaxy and that circular rotation is the dominant feature. We assume that our measurements refer to positions on a single inclined disc, i.e. that we do not expect a strong warp and/or overlapping spiral arms within the observed field. Accounting for harmonic perturbations up to order 3, this method results in a large parameter-space problem, and it requires some additional assumptions to obtain a physically meaningful solution. We obtain the parameters by proceeding as follows.
(i) We start from a simple inclined two-dimensional disc. In case of erroneous inclination, one would detect systematics in the residual field as explained in Section 3.3. Using a two-dimensional disc produces a robust model, in the sense that warps and other deviations from this basic model should be prominent in the residual maps.
(ii) Secondly, we fix the dynamical centre of the galaxy to coincide with the photometric centre. The photometric centre is obtained by fixing the centre of the $H$-band image, since the $H$-band image is less affected by dust. The Hubble Space Telescope (HST) $V$-band image and the SAURON image are then aligned with the HST H-band image.
(iii) At every radius, we fit $V_{\text {los }}=c_{0}+c_{1} \cos \psi \sin i$, varying $c_{0}$, PA and $c_{1}$. The result is used to fix the systemic velocity ( $V_{\text {sys }}=c_{0}$ ) simply as the mean value over radius, using Tukey's biweight mean formalism (Mosteller \& Tukey 1977), which is particularly advantageous for being non-sensitive to outliers. After $V_{\text {sys }}$, we fit the PA and $c_{1}$, followed by fixing the PA in the same way as the $V_{\text {sys }}$ was fixed.
(iv) For each ring, we import the values derived according to the recipe above, and fit the rotation curve and the higher harmonic components (up to order 3) applying a $\chi^{2}$-minimization scheme. These results are presented in Fig. 2.

Analysing the first, second and third harmonic components only, is an efficient way to analyse specific elements of the perturbations on the underlying potential. A perturbation of order $m$ creates $m-1$ and $m+1$ line-of-sight velocity terms (see e.g. Canzian 1993 and SFdZ). As a result, our fitted $c_{1}, s_{1}, c_{3}$ and $s_{3}$ terms contain information about possible $m=2$ perturbations.

When sectioning the field into concentric rings, the radial extent of each ring is a free parameter, which has to be pre-determined. For a range of possible ring radii, we have examined the fitted velocity information. Determination of the radial thickness of the rings becomes a trade-off between smoothness of the fitted velocity field and robustness of the fit. Radially thin rings result in smooth fits, and thus smooth residual (Data - Fit) fields, whereas radially thick rings result in lower errors for the fitted parameters. Patchy gas distribution causes non-uniform distribution of points, and it is important to make sure that all the rings include enough points to fit harmonic parameters to reasonable accuracy. This is particularly important in the innermost and outermost points. We adopt a geometric increase of the ring radii (meaning that the radial width of the rings is increased by a factor $1+$ step). Here, we adopt a step of 0.2 , and only fit the inner 30 arcsec of the SAURON velocity field, since rings larger than this radius are not sufficiently covered and hence do not deliver reliably derived parameters. Finally, since we are simultaneously fitting six harmonic components, we make sure that each ellipse contains at least 25 data points, in order to obtain reliable errors.

### 3.3 Errors

Warner, Wright \& Baldwin (1973) and van der Kruit \& Allen (1978) showed that assuming wrong input disc parameters could cause recognizable signatures in the residual velocity fields. SFdZ quantified these signatures in terms of harmonic expansion, and showed that the Fourier components due to non-circular motions will mix with those due to erroneous disc parameters $X_{\text {cen }}, Y_{\text {cen }}, i$ and PA. Errors in the kinematic centre translate to the $c_{0}, c_{2}$ and $s_{2}$ terms, while PA errors appear in the $s_{1}$ and $s_{3}$ terms, and inclination errors in the $c_{1}$ and $c_{3}$ terms. In the case of erroneous kinematic centre, the $c_{0}$ and the $c_{2}$ terms fall off as $\frac{1}{R}$, whereas the presence of a radius-independent $m=1$ mode shows the relation $c_{0} \sim 3 c_{2}$ (Schoenmakers 1999). Our chosen centre coordinates do not deliver any of these situations. Another source of error is 'pixel sampling' for which errors propagate onto the $c_{1}$ (as the rotation curve rises more gradually) and the $c_{3}$ term (as if inclination changes). This effect may also propagate onto the $s_{1}$ and $s_{3}$ parameters, although not significantly (Wong 2000). Our data and analysis do not require consideration of this effect since our spatial resolution is high enough.

Our data-extraction code delivers error measurements for each individual pixel (Falcón-Barroso et al. 2005). We calculate the errors for the tilted-ring and harmonic parameters by means of Monte Carlo


Figure 2. Top row, from left to right: observed SAURON gas velocity field of NGC 5448; reconstruction based on the harmonic decomposition of the SAURON gas velocity field; residual field (data - harmonic reconstruction); and the analytic bar model, which reproduces best the main kinematic features of the observed gas velocity field. Middle and bottom row: the harmonic parameters as a function of outer radius of each ring, and $v^{*}=c_{1} \sin i$. The overplotted red filled circles are the analytically calculated first and third harmonic terms for the bar model (the second terms are zero by construction), with the error bars corresponding to the $3 \sigma$ ( 99.7 per cent) confidence level (see Section 4 for details). The orientation of the maps is the same as in Fig. 1, and the mean PA value is given in the north-east direction.
simulations. Repeated application of the tilted-ring method to the Gaussian randomized gas velocity field yields the uncertainties on the harmonic parameters. Our 500 simulations show that choosing geometrically increasing ring radii with steps of 0.2 indeed yields satisfactory errors. The errors are low, and the parameter profiles are represented by an adequate number of points.

## 4 A BAR MODEL FOR NGC 5448

The SFdZ formalism is a very powerful tool for analysing velocity fields. One can analytically derive the higher order harmonic parameters for potentials of desired form. Schoenmakers (1999) derived the harmonic parameters for a lopsided potential, and a more extensive expansion was done by Wong et al. (2004), who derived the higher order harmonics for simple bar and two-armed spiral perturbations.

We import their model for a globally elongated gravitational potential, which, in the plane of the galaxy, consists of an axisymmetric component $\Phi_{0}(R)$ from Kuijken \& Tremaine (1994), with a bisymmetric potential of the form $\Phi_{2}(R) \cos 2 \theta$ added to it. In the case of flat rotation curve, the potential is written as
$\left\{\begin{array}{l}\Phi_{0}(R)=v_{\mathrm{c}}^{2} \ln R, \\ \Phi_{2}(R)=-\varepsilon v_{\mathrm{c}}^{2} / 2,\end{array}\right.$
where $v_{\mathrm{c}}$ is the circular velocity and $\varepsilon$ is the elongation of the potential. Introducing a constant damping term into the equations of motion and considering only the $m=2$ perturbation term (Lindblad \& Lindblad 1994; Wada 1994), linear epicyclic approximation of Lin \& Shu (1964) was applied to obtain an analytical solution for gaseous orbits in this barred potential. Since this model is restricted to $m=2$ perturbation, it affects only the first and third harmonic parameters $\left(c_{1}, s_{1}, c_{3}\right.$ and $\left.s_{3}\right)$. These depend on the amplitude of the damping term ( $\lambda$ ), the ellipticity of the potential $(\varepsilon)$, the corotation radius (CR) and the viewing angle $(\theta)$, where $\theta=0$ corresponds to end-on view.

We use these analytic harmonic parameters to reconstruct the signatures of prominent non-circular motions in the observed velocity fields. We build a library of models with varying bar parameters ( $0<\varepsilon<0.5,0<\lambda<0.5$ and a range of bar sizes), viewed from different angles $\left(0^{\circ} \leqslant \theta \leqslant 180^{\circ}\right)$. The effects of $\lambda$ and $\varepsilon$ on the velocity field are predictable. The bar signature is weaker for a larger damping factor and/or a smaller flattening of the potential. However, the effect of varying $\theta$ is not straightforward.

Investigating our library of dissipative bar models, we find that only for a certain combination of parameters the model exhibits a strong twist of the gas zero-velocity curve similar to our data (Fig. 1). We quantify the comparison by calculating, for each bar model in our library, the discrepancy between the reconstructed velocity field and
the observed velocity field, in terms of the goodness-of-fit parameter $\chi^{2}$. Care has to be taken at the inner Lindblad resonance (ILR), since there the linear epicyclic theory breaks down. At the ILR, due to the presence of non-linear terms, which are not accounted for by the analytic epicyclic theory, the weak bar model is not expected to reproduce the velocity field. Hence, for a small region around the ILR, we interpolate the bar models.

The minimum goodness-of-fit parameter $\chi_{\text {min }}^{2}$ yields the bestfitting bar model, for which we show in Fig. 2 the reconstructed velocity field and harmonic terms (red filled circles). The best-fitting model accounts for an $m=2$ perturbation of a single bar, with potential ellipticity $\varepsilon=0.15 \pm 0.02$, damping term $\lambda=0.12 \pm$ 0.03 , viewing angle $\theta=19^{\circ} \pm 3^{\circ}$, and $\mathrm{CR}=37 \pm 4 \mathrm{arcsec}$. The $3 \sigma$ errors on the bar parameters follow from the bar models for which the difference between the corresponding $\chi^{2}$ and $\chi_{\text {min }}^{2}$ is below the 99.7 per cent level. From the harmonic terms of these bar models, we also obtain an estimate on the uncertainty in $c_{1}, s_{1}, c_{3}$ and $s_{3}$, indicated by the red error bars in Fig. 2. Given the significant second harmonic term and the simplicity of the analytic bar model, it is not surprising that it cannot provide a perfect fit to the data. Still, this generic bar model does reproduce the main features in the observed velocity field, as well as the overall behaviour of the first and third harmonic terms. This supports the case of a bar as the main driver behind the observed non-circular motions.

## 5 RESULTS

The gas velocity field decomposition of Section 3.2 provides the radial profiles for the primary disc parameters and the higher order harmonic terms. Assuming the inclination $i=64^{\circ}$ from the RC3 catalogue (de Vaucouleurs et al. 1991), we apply this method to our observed gas velocity field in an iterative manner by first varying the $V_{\text {sys }}$ and PA. We then fix these parameter to their mean values and we proceed by deriving the $V_{\text {rot }}$ and higher harmonic terms (see Fig. 2). We detect a varying zeroth harmonic term ( $V_{\text {sys }}$ ) with variation amplitude up to $40 \mathrm{~km} \mathrm{~s}^{-1}$ in the central 10 arcsec . We find a strong PA twist of about $30^{\circ}$ in the central 10 arcsec , and outside this radius the PA goes back to the central values. The circular velocity component $c_{1}$ rises steeply and peaks at 5 -arcsec radius, followed by a very slow decline out to the outer radii. We find that the behaviour of the $s_{1}$ term could be compared with the $V_{\text {sys }}$ or the PA: the $s_{1}$ term changes sign at around 12 arcsec , and at the same galactocentric radius, the $V_{\text {sys }}$ and the PA change sign around their mean values. The $s_{1}$ exhibits amplitudes of the order of
$0.2 c_{1} \sin i$. The bottom row in Fig. 2 shows that, apart from the $s_{2}$ term, the higher harmonic terms significantly deviate from zero, and indeed account for the considerable deviation of the velocity field of NGC 5448 from pure rotation.

In the following sections, we describe the distinct features that we find in our kinematic maps.

### 5.1 The stellar component

The SAURON flux map in Fig. 1 displays a smooth stellar distribution and the presence of prominent dust lanes to the south of the nucleus. The stellar kinematics shows a prominent regular disc-like rotation with a smaller inner stellar disc within the central 7 -arcsec radius. The stellar velocity dispersion decreases towards the centre, and at the location of the maximum line-of-sight velocities for the central structure, $h_{3}$ anticorrelates with $V$, which supports the argument that the central component of NGC 5448 is a central disc. We approximate the stellar velocity field with that of an exponential thin disc (Freeman 1970) to emphasize the kinematic signatures of the central disc. Fig. 3 shows this simple inclined disc model, where the inner stellar disc rotates faster than the outer disc. The best-fitting model for the outer stellar disc, omitting the central 7 arcsec and assuming an inclination fixed to the RC3 catalogue value, yields $V_{\text {sys }}=2002 \mathrm{~km} \mathrm{~s}^{-1}$, a disc scalelength $R_{d}=18$, and a disc PA $=91^{\circ}$. Repeating the same exercise for the region inside 7 arcsec, we find that the central disc is misaligned with respect to the outer disc by $\sim 13^{\circ}$.

### 5.2 Gas distribution and kinematics

Fig. 1 demonstrates that along the strong dust lanes, the gas shows a patchy distribution, with an asymmetric elongation of [ $\mathrm{O}_{\mathrm{III}}$ ] gas towards the east as well as the galactic poles. The $\mathrm{H} \beta$ distribution is found to be more regular, and we have found that all kinematic features of the $\left[\mathrm{O}_{\mathrm{III}}\right]$ gas are accompanied by $\mathrm{H} \beta$-emitting gas. The [ $\left.\mathrm{O}_{\mathrm{III}}\right] / \mathrm{H} \beta$ map in Fig. 1 displays a prominent ring-like structure at 5-15 arcsec, indicating high ionization of the gas in this region.

The gas velocity map clearly shows very prominent ' S '-shaped zero-velocity curve with very sharp edges indicating very strong non-circular gas motions (Peterson \& Huntley 1980). This ' S '-shaped gaseous zero-velocity curve is confirmed by the PA variation derived by the tilted-ring decomposition in Fig. 2. Zero-velocity curve twists can be indicative of strong radial motions, created by, e.g. interactions, mergers or elliptical streaming due to a barred potential. Wong (2000) distinguished differences between radial


Figure 3. A thin isothermal disc model for the stellar velocity field of NGC 5448. The circle marks the 7-arcsec region within which we find a disc-like structure. The disc model, fitted to the field outside this region, implies for the outer disc a scalelength of 18 arcsec, $V_{\text {sys }}=2002 \mathrm{~km} \mathrm{~s}{ }^{-1}$, and PA $=91^{\circ}$. The orientation of the maps is the same as in Fig. 1.


Figure 4. First and third sinusoidal harmonic terms normalized to $v^{*}=$ $c_{1} \sin i$. Both the data and the bar model show a negative slope (dashed and solid line, respectively), indicating that elliptical streaming, due to the bar potential, is the main driver of the radial motions observed in the gas velocity field of NGC 5448.
motion mechanisms by comparing the $s_{3}$ versus $s_{1}$ harmonic terms, and found that the behaviour of $s_{3}$ versus $s_{1}$ is different between a bar model and a pure axisymmetric or warped model. As demonstrated in Wong et al. (2004; fig. 5) the $s_{3}$ versus $s_{1}$ of a warped disc lie on a positive slope. Moreover, in case of an externally triggered radial flow, the points in the $s_{3}$ versus $s_{1}$ graph should lie on a zero slope. Setting up the same diagnostics, in Fig. 4, we find that for our data, the $s_{3}$ versus $s_{1}$ curve has a negative slope very similar to that of the bar model presented in Fig. 2. This confirms the signature of elliptical streaming in the gas velocity field of NGC 5448.

Comparing the stellar maps with the gas maps, we find that the gas velocities are considerably higher: this is confirmed with the rotation curve presented in Fig. 6. We find that the gaseous $\sigma$ map displays some features comparable to the stellar $\sigma$ map. Although the stellar velocity dispersion is more steeply rising towards the centre, both maps show a prominent dip in the centre. This supports the hypothesis of the presence of a central dynamically cold disclike structure, present both in the stellar and gaseous component. Both maps also show a dispersion increase in bipolar directions just a few arcsec from the centre. This is much more prominent in the gas map, as its $\sigma$ reaches values $\simeq 250 \mathrm{~km} \mathrm{~s}^{-1}$. This may be indicative of significant outflows in this AGN host.

### 5.3 Position angle values

The projected and deprojected PA profiles from Laine et al. (2002) in Fig. 5 display strong variations in the central few arcsec. The HST images display asymmetrically distributed dust within the central few arcsec, which may cause these strong central PA variations (also found by Kornreich et al. 2001). At larger radii, we find that the PA profile shows a variation of the order of $10^{\circ}$, but overall it stays fairly constant around the nominal RC3 value, i.e. $115^{\circ}$. Our tiltedring decomposition of the gaseous velocity field, yields a mean gas kinematic PA of $119^{\circ} \pm 5^{\circ}$, which is consistent with the photometric PA from RC3. In the case of the large stellar disc, as described in Section 5.1, we find an offset of $\sim 25^{\circ}$ between the stellar kinematic


Figure 5. The top panels show HST/NICMOS $H$-band (F160W) and WFPC2 $V$-band (F606W) images of NGC 5448. The bottom-left panel is the $V-H$ map obtained by convolving the $H$-band image with the $V$-band image point spread function (PSF) and vice versa, and subtracting one from the other. All maps have pixel size of 0.0455 arcsec, and the same orientation as the DSS image with the centre marked by a cross. The bottom-right profiles are the observed (open symbols) and deprojected (filled symbols) ellipticity and PA profiles from Laine et al. (2002). Circles represent values derived from the NICMOS image, and triangles show the values derived using the DSS image. Here, we only focus on the region beyond 1 arcsec.

PA and the photometric mean PAs. This misalignment could be due to the effect of the bar on the observed stellar velocity field.

### 5.4 The inner few arcsec

In Fig. 6, we zoom into the central few arcsec of the stellar and the gaseous velocity fields of NGC 5448 to emphasize the observed kinematic differences between the two components. The gaseous component exhibits a strongly twisting zero-velocity curve, and the gas rotates faster than the stars. We find that the inner stellar disc not only is misaligned with the outer stellar disc, but also is shifted to the south-east. In contrast, we find from the photometric profiles in Fig. 5, that the ellipticity of the central disc is similar to that of the outer disc $(\sim 0.55)$, as well as its PAs. The prominent dust lanes at the south of this galaxy may explain the kinematic misalignment between the outer and inner stellar discs.

In the central $\sim 4$ arcsec the gas isovelocity contours are comparatively straight and parallel. In the same region, the stellar isovelocity contours are indicative of the presence of a central disc. The tiltedring decomposition of the gas velocity field provides the gas rotation curve illustrated in Fig. 6. The gas rotates about $70 \mathrm{~km} \mathrm{~s}^{-1}$ faster than the stars in the region outside $\sim 4$ arcsec, with some indication that outside this radius the negative velocities reach lower values than the positive line-of-sight velocities. This asymmetry could be caused by complex dust distribution or attributed to a signature of lopsidedness.

### 5.5 Dust effects or lopsidedness?

Although the unsharp-masked SAURON image shows strong signature of dust lanes in the region south of the nucleus, the central dust


Figure 6. Zooming into the central few arcsec of the stellar and gaseous velocity maps of NGC 5448, using the same velocity range as in Fig. 1. Indicated are the north-east direction (arrow), the photometric PA (straight line) and the photometric centre (cross). The overplotted circle indicates the 7 -arcsec radius for comparison with Fig. 3. In the right panel, we present the stellar rotation curve (extracted along the photometric PA) together with the gas rotation curve derived from tilted-ring decomposition.
distribution is easier to study when looking at the HST images and the $V-H$ colour map in Fig. 5. The colour map shows a strong dust lane about 1 arcsec at the south-east of the galaxy nucleus as well as an asymmetrically distributed overall dust distribution. The larger scale WFPC2 image shows that this central dust lane is accompanied by several other dust lanes further away from the nucleus. Using the Galactic extinction law of Rieke \& Lebofsky (1985), the HST images yield an average extinction value of $A_{V} \simeq 0.5$ over the central 3 arcsec, with a maximum value of 1.5 . The extinction increases significantly towards the centre, with a prominent peak a few arcsec south of the nucleus (see Fig. 5).

Some of the observational effects of the asymmetrical dust distribution could be interpreted as signatures of lopsidedness. Lopsidedness in galaxies has been investigated by, e.g. Baldwin, Lynden-Bell \& Sancisi (1980) and Swaters et al. (1999). The amplitude of this effect may depend on galactocentric radius, and viewed from different viewing angles will produce different signatures in the observed velocity field. These studies have shown that the residuals are dominated by the zeroth harmonic term for viewing angle of $90^{\circ}$, and by the second harmonic term for viewing angle of $0^{\circ}$. In the special case of radius-dependent lopsidedness, $c_{0} \sim 3 c_{2}$. NGC 5448 has a large inclination, thus the zeroth term dominates, and we find no correlation between the $c_{0}$ and the $c_{2}$ terms. Our harmonic decomposition results display strongly varying zeroth and second terms. This was shown by SFdZ to be a possible indication of an $m=1$ perturbation, i.e. lopsidedness (cf., fig 2. of SFdZ). In this case, subtracting the rotational component from the perturbed velocity field, one should find a ring-like feature. In Fig. 7, we present this residual field for NGC 5448 and find no ring-like feature. Therefore, dust is most likely the cause for the asymmetric features that we observe in NGC 5448.

### 5.6 The large-scale bar

In Fig. 2, we find that the harmonic parameters derived from the data are consistent with the bar model outlined in Section 4. Our simple model is limited to an $m=2$ perturbation. Complicated flow patterns in bars studied by, e.g. Lindblad (1999), imply a significant contribution from $m=4$ and higher order modes. The third harmonic terms are also influenced by $m=4$, which could explain the differences between our model bar and the data for these parameters, but a detailed model is beyond the scope of this paper.

We now compare the modelled bar with the deprojected Digitized Sky Survey (DSS) image. The inclination from the RC3 and the PA


Figure 7. Residual field after subtracting the best-fitting rotational model from the observed gas velocity field. This map reveals the strong non-circular motions in NGC 5448, however, no ring-like feature is found.


Figure 8. Observed (left) and deprojected (right) DSS image of NGC 5448. The inclination of $64^{\circ}$ and PA of $115^{\circ}$ from the RC3 catalogue have been used to deproject the image according to the two-dimensional deprojection of a circular thin disc.
from our tilted-ring model were used to deproject the DSS image in a simple way by assuming that the galaxy disc is thin. The outer spiral arms are clearly emphasized in the deprojected DSS image (Fig. 8).

It is somewhat difficult to identify the size of the large-scale bar from the image. From our bar model we find a CR of about 37 arcsec.

In practice, this is done by assuming that at $C R$ the circular frequency of the axisymmetric potential is identical to bar angular frequency. According to this definition and since we use a flat rotation curve, the ILR is located at $1-1 / \sqrt{2}$ of the CR, i.e. at about 11 arcsec . If we assume that the bar in NGC 5448 ends close to the starting point of the spiral arms (Sanders \& Huntley 1976), we can then also associate its CR with the inner radius of the arms. Fig. 8 shows that our analytic bar model is of reasonable size. The assumed CR radius is confirmed by the ellipticity profile presented in Fig. 5, since the high-ellipticity plateau starts at around this radius. At around the ILR (i.e. 11 arcsec ), there is a good agreement between the $s_{1}$ profiles from the data and the model, with in both cases the a change in sign at the ILR.

## 6 DISCUSSION AND CONCLUSIONS

We have used linear theory to construct a bar model ( $m=2$ mode) for NGC 5448. The best-fitting model considers the effects of a single weak bar with a potential ellipticity $\varepsilon=0.15$ and a damping amplitude of $\lambda=0.12$. We compare the harmonic terms of the model with those derived from the data and find an overall consistency (see Fig. 2). Using this model, we have been able to associate the radial motion of gas with that of the large-scale bar (see Fig. 4).

NGC 5448 exhibits clear signatures of the presence of other components than a single bar, which affect the observed velocity field. Inspecting the photometry and the central parts of the gaseous and stellar velocity field, we have detected a central rotating disc-like stellar component embedded in the larger disc (see Fig. 3). The WFPC2 image shows one very sharp dust lane 1 arcsec from the centre of this galaxy. This image also shows three more fuzzy and almost parallel dust lanes further out in the south-east direction. The dusty centre is also apparent in the $V-H$ image in Fig. 5. Dust is inhomogeneously distributed and continues down to the very bright nucleus. Light from the central light source is absorbed by the dust asymmetrically and the centre appears to be located at the northwest of its actual position.

Investigating the projected and deprojected ellipticity profiles derived from the H -band data from Laine et al. (2002) confirms the presence of a central disc in the inner 7 arcsec . Although the projected ellipticity profile decreases at $\sim 4$ arcsec and outwards, we cannot pin down the exact size of the central disc. The observed ellipticity decrease could be partly caused by the strongly asymmetric dust distribution. The stellar kinematic maps show that the central disc rotates faster than the main disc, and our observed gas distribution and kinematics indicate that this central disc also hosts gas which rotates faster than its stellar counterpart. This is not unexpected, since due to its dissipative nature, the gas is not slowed down by asymmetric drift. It is important to note that, in NGC 5448, the gas velocities are well ordered but larger in magnitude than the stellar velocities. However, Fig. 6 indicates that this velocity difference dies out at larger radii. The difference between the stellar and gas velocities can be explained because the stars are in a thicker structure (bulge) in the central regions, while at larger radii both the gas and the stars are in a flatter disc, and both move closer to the circular velocity.

It is known that bars are efficient in transferring mass towards the inner regions of their host galaxies. The centrally concentrated matter may be able to form a central disc (Yuan \& Yen 2004), or an inner bar (e.g. Maciejewski \& Sparke 2000; Englmaier \& Shlosman 2004). Our analysis has shown that the non-circular gas kinematics in NGC 5448 could be driven by the large-scale bar. The central disc
could then have been formed as a result of the gas accumulation at the centre.

To conclude, we have been able to analytically model the bar signatures in the AGN host NGC 5448. We have unveiled a central disc, and have distinguished the effects of a lopsided perturbation from strong dust features. NGC 5448 hosts considerable amounts of dust, which is asymmetrically distributed all the way to the centre, resembling the 'Evil Eye' galaxy (Braun, Walterbos \& Kennicutt 1992). This study shows the power of the harmonic decomposition formalism to quantify non-circular motions in observed velocity fields, and we plan to apply this approach to the full set of bulges observed with SAURON.

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