

1 **A BIOECONOMIC APPROACH TO OPTIMIZE MUSSEL CULTURE**  
2 **PRODUCTION**

3 **Runnig head:** Bioeconomic approach for mussel culture

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12

13 **Abstract**

14           The fast rise of aquaculture practices during the last decades has increased the  
15 need of adopting culture strategies to optimize production and guarantee the  
16 sustainability of the sector. This study aims to provide a management tool to help  
17 mussel farmers identify optimal culture strategies and use production inputs efficiently.  
18 For this purpose, we evaluated the productivity and efficiency of different stocking  
19 densities and culture lengths by the joint application of parametric and non-parametric  
20 frontier analysis at the farm-scale. The translog production function outperformed the  
21 Cobb-Douglas model currently applied in most farm-scale frontier analyses. This model  
22 estimates that the optimal culture density is ca. 700 ind/m, given that at lower densities  
23 efficiency decreases (under-usage of available space) and mussel quality did not  
24 improve, and at higher densities mortality and dislodgements from the ropes led to  
25 economic losses. This work also showed that marginal analysis does not provide an  
26 accurate estimation of the economic efficiency when unitary costs and prizes are not  
27 constant. According to the Malmquist indices mussel farmers should shorten the culture  
28 period in order to improve their productivity. All these results support the joint use of  
29 parametric and non-parametric frontier analysis as management tool for optimizing  
30 input use and scheduling aquaculture production.

31

32 **Keywords**

33 Aquaculture management, culture strategies, Malmquist index, marginal analysis,  
34 stochastic frontier function.

35

## 36 1. Introduction

37 Aquaculture is the fastest growing food sector in the world, with production  
38 increasing at an annual rate of 7.8% between 1990 and 2010, and an expected annual  
39 growth up to 4.14% from 2014 to 2022 (FAO 2014). Nowadays aquaculture provides  
40 50% of the fishery output for human consumption, of which 23.6% is shellfish culture  
41 (14.2 million tons; FAO 2014). With 80% of the total consumed shellfish being  
42 cultured, this is an important activity in many coastal zones worldwide. The fast rise of  
43 aquaculture practices points out the need of adopting culture strategies in order to  
44 optimize production and guarantee the sustainability of the sector. Industry-scale  
45 frontier analysis has been widely used to assist producers and decision-makers in  
46 identifying optimal production system designs, operation management strategies, and  
47 alternative development and policy approaches, although its use in aquaculture is  
48 limited when compared with agriculture or other manufacturing industries (Iliyasu et al.,  
49 2014). Farm-scale analysis of productivity and environmental impact of shellfish  
50 aquaculture has been addressed by Ferreira et al., (2007) and Hawkins et al., (2013),  
51 which developed simulation procedures based on the interaction between suspension-  
52 feeding bivalves and the environment.

53 The productivity and efficiency measures introduced by Farrell, (1957)  
54 motivated the development of several parametric and nonparametric techniques for  
55 frontier analysis. The stochastic frontier production function (SFPPF) approach involving  
56 econometric estimation of parametric functions (Aigner et al., 1977; Meeusen and  
57 Broeck, 1977), and data envelopment analysis (DEA) involving linear programming  
58 (Charnes et al., 1978) are the most popular techniques used in frontier analysis. The  
59 main advantage of the SFPPF is that it can decompose the deviation from the frontier in  
60 stochastic noise and technical inefficiency components. The main drawback of this

61 approach is the need of a functional form for the technology and the inefficiency error  
62 term, as the misspecification of the model can lead to biased estimations and wrong  
63 conclusions. DEA eliminates the need of a parametric assumption, but due its  
64 deterministic nature, this approach attributes all deviations from the frontier to  
65 inefficiency effects overlooking the stochastic noise. This drawback was partially  
66 overcome by the bootstrap procedure introduced by Simar and Wilson, (2000, 1998) to  
67 create confidence intervals for DEA scores. As neither approach is strictly preferable,  
68 Murillo-Zamorano and Vega-Cervera, (2001) suggested that the joint use of both  
69 techniques can improve the accuracy of frontier analysis. Nevertheless, as in other areas  
70 of knowledge, economic efficiency of aquaculture production has been analyzed either  
71 by stochastic frontier production functions or DEA (see Iliyasu et al., (2014) and  
72 references therein) and to our knowledge the joint use of both techniques is still lacking.

73       The Farm Aquaculture Resource Management (FARM, Ferreira et al., (2007))  
74 and ShellSIM (Hawkins et al., 2013) are farm-scale models that simulate the  
75 interactions between suspension-feeding bivalves and the environment in order to  
76 estimate carrying capacity, shellfish production and quantify the ecological impact of  
77 aquaculture on the ecosystem. These models can be a useful management tool for both  
78 farmers and regulators, as they allow the development of culture strategies in order to  
79 optimize economic profits and minimize the environmental impact. Both procedures use  
80 marginal analysis based on a Cobb-Douglas SFPP model with stocking biomass as the  
81 unique variable input, in order to determine the optimal culture density. The dynamic  
82 ecological-economic model proposed by Nobre et al., (2009) also uses a Cobb Douglas  
83 model to estimate the marginal productivity of capital and labour. To our knowledge,  
84 more general parametric models, such as the translogarithmic SFPP, and nonparametric  
85 frontier analysis have not been used at farm-scale level.

86           The extensive culture of the blue mussel (*Mytilus galloprovincialis*), with a  
87 production volume that ranged between 200,000-300,000 tonnes and a production value  
88 that exceeded 100 million Euros in 2012 ([www.pescadegalicia.com](http://www.pescadegalicia.com)), is the main  
89 aquaculture industry in Galicia. Mussels are cultured in floating systems (rafts)  
90 consisting of a 500m<sup>2</sup> wood structure anchored to the seafloor, from which culture ropes  
91 and/or seed collectors are suspended. Nowadays, the number of ropes per raft is limited  
92 to 500. Besides, the maximum number of rafts allowed in the Galician Rias (ca. 3300)  
93 has been reached. Mussel culture is scheduled according to the availability of natural  
94 resources for feeding and seed recruitment, the biological cycle of mussels and the  
95 fluctuations of market demand (Labarta et al., 2004). Subjected to all these constraints,  
96 mussel farmers have focused on optimizing the use of available space in the raft to  
97 maximize profits, following two strategies: increasing culture densities and/or  
98 decreasing the length of the culture cycle.

99           This study aims to develop a management tool that allows mussel farmers to  
100 identify optimal farm-based culture strategies and use production inputs efficiently. To  
101 this purpose, we conducted an experiment to evaluate the performance of different  
102 culture strategies (testing different cycle lengths and mussel stocking densities) by the  
103 joint application of parametric and non-parametric frontier analysis at the farm-scale.  
104 We applied parametric frontier analysis to determine the optimal culture density and  
105 evaluated whether marginal analysis can be applied to estimate the economic efficiency  
106 of suspended mussel culture. We estimated the nonparametric Malmquist indices to  
107 analyze the productivity change along the culture period in order to determine the  
108 optimal cycle length.

109

## 110 2. Material and Methods

### 111 2.1. Experimental design

112 The study area was located in the raft polygon of Lorbé in Ría de Ares-Betanzos,  
113 on the NW coast of Spain (43°22'39.20''N, 8°12'39.77''W). This Ría has great  
114 bioeconomical importance due to extensive mussel culture (*Mytilus galloprovincialis*).

115 Data were collected during the traditional thinning-out to harvest period,  
116 employing the culture and handling techniques used by the local industry (Labarta et al.,  
117 2004). In late April 2008, mussels from collector ropes deployed 8 months before  
118 (September 2007) were thinned out at seven densities (treatments), encompassing the  
119 current commercial densities in Galicia (600–800 ind/m). The mean shell length of  
120 these mussels was 48.78mm (sd=1.27), which is close to the minimum commercial size  
121 (50mm). Stocking biomass (Kg/rope) was measured as rope weight at the beginning of  
122 the culture (in this case at thinning-out). Production costs (€/rope) were obtained from a  
123 survey of several mussel aquaculture farms, and included labour, estimated as time  
124 spent per rope for thinning-out and harvesting, boat fuel consumption for deploying and  
125 harvesting the ropes, and raft occupation costs (Table 1, Appendix I). As mussels were  
126 obtained from collector ropes, their cost (€/Kg) was estimated as the occupation cost of  
127 these collector ropes in the raft.

128 Production data were collected monthly from late May to late November (see  
129 details in (Cubillo et al., 2012c) so that the length of growing season or cycle length  
130 (days) can be considered as an input. Density was calculated as the number of mussels  
131 per linear meter of rope (ind/m). Total production (Kg/rope) was estimated as the  
132 weight of commercial (>50 mm shell length) mussels. Production prices (€/Kg) and  
133 revenues (€/rope) were estimated taking into account the two markets: fresh sale

134 (mussels sold as fresh product) and industry sale (frozen, canned and processed  
135 mussels). Fresh sale prices are based on mussel size, measured as number of mussels  
136 per Kg (ind/Kg), according to the average classification used by several distribution  
137 companies (Pérez-Camacho et al., 2013): Extra1 (< 21 ind/Kg, 1€/Kg), Extra2 (21-27  
138 ind/Kg, 0.9 €/Kg), Large (28-35 ind/Kg, 0.75 €/Kg), Normal (36-45 ind/Kg, 0.6€/Kg)  
139 and Small (46-70 ind/Kg, 0.5 €/Kg). Industry sale prices build on mussel quality in  
140 terms of mussel size (ten categories ranging from > 276 to < 98 ind/Kg tissue), and  
141 Condition Index measured as the meat to total weight ratio of mussels (from 12% to  
142 27%), according to a pool of processing industries, so that small mussel (>276 ind/Kg  
143 tissue) prices ranged between 0.22 and 0.50 €/Kg and large mussel (< 98 ind/Kg tissue)  
144 prices between 0.35 and 0.78 €/Kg.

## 145 **2.2. Data analysis.**

146 We first conducted an exploratory analysis of the variables involved in the  
147 mussel culture process. We applied two-way repeated measures ANOVA to test the  
148 effects of density treatment and cycle length on production and product quality. In  
149 addition, we applied generalized additive models (GAM) to estimate the effect of  
150 stocking biomass and cycle length on the profits obtained by fresh and industry sale,  
151 and to analyze the differences between both. Section 2.2.1 provides detailed information  
152 about the GAM model. Model fitting was conducted with the mgcv package of R (R  
153 Core Team, 2013; Wood, 2006a)

154 The analysis of productivity and efficiency was conducted by the joint use of  
155 parametric (SFF) and non-parametric techniques (DEA). We applied Stochastic frontier  
156 analysis, considering stocking biomass (Kg/rope) and cycle length (days) as inputs, and  
157 total production (Kg/rope) as output to determine which density is closer to the

158 production carrying capacity of the system without exceeding it, i.e. the optimal density  
159 treatment. In addition, we estimated the non-parametric Malmquist indices for  
160 productivity, efficiency and technology change, considering stocking biomass (Kg/rope)  
161 and culture costs (€/rope) as inputs and total production (Kg/rope) or profits (€/rope), as  
162 outputs. This analysis allows us to determine the optimal cycle length for each market  
163 and the most profitable market for each cycle length. The parametric and non-  
164 parametric frontier analysis were conducted with the frontier (Coelli and Henningsen,  
165 2011) and FEAR (Wilson, 2008) packages of R. Sections 2.2.2 and 2.2.3 provide  
166 information about these procedures.

#### 167 2.2.1. Generalized additive models (GAM)

168 For both fresh and industry sale, we fitted the profits (P, €/rope) obtained as the  
169 difference between costs and revenues, according to cycle length (T, days) and stocking  
170 biomass (S, Kg/rope) by generalized additive models (GAM) with second order  
171 interaction (Hastie and Tibshirani, 1990; Wood, 2006b). As the response variables are  
172 normal, we assumed a Gaussian family with identity link function (Hastie and  
173 Tibshirani, 1990; Wood, 2006a). Our model can be expressed as follows:

$$174 \quad E(P) = \alpha + f_1(S) + f_2(T) + f_{12}(S, T) \quad (1)$$

175 where, for each transaction, E(P) are the estimated profits,  $\alpha$  is the intercept,  $f_j$ ,  $j=1,2$  the  
176 smooth terms for each covariate, which were represented by penalized regression  
177 splines, and  $f_{12}$  the smooth term for the interaction between stocking biomass and cycle  
178 length, estimated using a scale-invariant tensor product of penalized regression splines  
179 (Wood, 2006b). Finally, we obtained 95% confidence intervals for the predicted values  
180 in order to compare profits between fresh and industry sale.



181 2.2.2. Stochastic frontier production function (SFPF) with a model for technical  
182 inefficiency effects and marginal analysis

183 We applied one-step stochastic frontier analysis (see details in Appendix II) to  
184 estimate the potential production and efficiency levels of the different density  
185 treatments. Model selection was conducted by several likelihood ratio tests (Table 2).  
186 Our data rejected the Cobb-Douglas model for the stochastic frontier function  
187 (Appendix II). Total efficiency, deterministic efficiency and independence between  
188 inefficiency and density treatment were also rejected. Thus, we fitted the SFPF for total  
189 production (B, Kg/rope) by a translogarithmic model with stocking biomass (S,  
190 Kg/rope) and cycle length (T, days) as inputs and density treatment as inefficiency  
191 factor (Z) (Battese and Broca, 1997; Battese and Coelli, 1995). This model can be  
192 expressed as follows:

$$193 \quad \ln B_{it} = \beta_0 + \beta_1 \ln S_{it} + \beta_2 \ln T_{it} + \frac{1}{2} \left( \beta_{11} (\ln S_{it})^2 + 2\beta_{12} \ln S_{it} \ln T_{it} + \beta_{22} (\ln T_{it})^2 \right) + V_{it} - U_{it} \quad (2)$$

194 where  $U_{it}$  is the estimator of the technical inefficiency,  $TE_{it} = \exp(-U_{it})$ , and can be  
195 expressed as  $U_{it} = z_{it}\delta + W_{it}$ , where,  $z_{it}$  is the vector of dummy variables associated to  
196 each density treatment,  $\delta$  is the associated vector of parameters and  $W_{it}$  are random error  
197 terms ( $N(0, \sigma_w^2)$ ). Positive coefficients ( $\delta > 0$ ) indicate relative technical inefficiency  
198 while negative coefficients ( $\delta < 0$ ) point out relative technical efficiency. The more the  
199 estimated value differs from zero, the stronger the efficiency/inefficiency.

200 In order to measure the effect of any input change on total production we  
201 estimated the output elasticity for each input (Appendix II). The sum of these  
202 parameters yields the return to scale (RTS), which measures the percentage change in

203 output from a 1% change in all inputs. When  $RTS > 1$  ( $RTS < 1$ ) the production  
204 function exhibits increasing (decreasing) returns to scale, i.e. a simultaneous increase in  
205 all inputs by a certain percentage results in greater (lower) percentage increase in  
206 output. If  $RTS = 1$ , the farm has constant returns to scale, implying that a proportionate  
207 increase in inputs will lead to the same increase in output. The cross-elasticity of  
208 substitution  $H_{jk}$ , (Chiang et al., 2004) was estimated to measure the relationship between  
209 inputs (Appendix II).  $H_{12} > 0$  indicates that the inputs are jointly complementary, i.e. we  
210 need to increase stocking biomass and cycle length together to raise total production.  
211  $H_{12} < 0$  indicates a competitive relationship between inputs, i.e. a decrease in stocking  
212 biomass could be compensated elongating the culture period, and viceversa.

213 Finally, we analyzed the economic efficiency of the stocking biomass (S) by  
214 comparison between the incremental benefit of an additional unit (VMP) and its  
215 incremental cost ( $P_x$ ). If the value of the marginal product (VMP) of an input is greater  
216 than its cost ( $P_x$ ), profit could be raised increasing the use of that input, and conversely.  
217 The efficient use of an input is achieved when the value of its marginal product equals  
218 its price. Marginal analysis is usually built under some regularity conditions: (i) inputs  
219 are unlimited, (ii) inputs purchase and output sales are made in a perfect competitive  
220 market situation, (iii) the farm is a small production system that sells only this product  
221 and (iv) mussel seed is the unique variable input, as other cost (such that lease or  
222 labour) are fixed (Ferreira et al., 2007). These conditions are not necessarily true in  
223 mussel suspended culture. On one hand, on contrast with assumption (iv) the relative  
224 raft occupation, labour and transport costs decrease as the stocking biomass increases  
225 (see Fig. A1 in Appendix I). On the other hand, as explained in Section 2.1 mussel  
226 prices depend on mussel size and quality. In this work, we conduct the marginal  
227 analysis for each cycle length taking into account the variability of costs and prices

228 along the density gradient. Thus, for each density treatment and cycle length, we  
 229 estimate the ratio VMP/Px and check whether these values equal 1 to indentify optimal  
 230 input use.

231

### 232 2.2.3. Malmquist productivity indices

233 Productivity change between sequential months for each density treatment was  
 234 analyzed through the input-based Malmquist productivity, efficiency and technology  
 235 indices. We obtained these indices following the estimation and bootstrap methods  
 236 proposed by Simar and Wilson (1999) under the assumption of constant returns to scale.  
 237 Productivity was measured in terms of total production (Kg/rope) and revenue (€/rope)  
 238 for both fresh and industry sale. As we are interested in productivity change over time,  
 239 we cannot consider cycle length as input, as we did above. Thus, our inputs are  
 240 stocking biomass (Kg/rope), which depend on the density treatment but remains  
 241 constant over time, and culture costs (defined as the sum of labour, transport and  
 242 occupation, Appendix I), which depend on both density treatment and cycle length.

243 Given a set of density treatments ( $i = 1, 2, \dots, 7$ ) observed at times  $t_1 < t_2$ , the  
 244 input-based Malmquist index for treatment  $i$  (Färe et al., 1992; Simar and Wilson, 1999)  
 245 is defined as:

$$246 \quad M_i(t_1, t_2) = \frac{D_i^{t_2/t_2}}{D_i^{t_1/t_1}} \left( \frac{D_i^{t_2/t_1}}{D_i^{t_2/t_2}} \frac{D_i^{t_1/t_1}}{D_i^{t_1/t_2}} \right)^{1/2} = \varepsilon_i(t_1, t_2) F_i(t_1, t_2), \quad (3)$$

247 where  $D_i^{t_j/t_k}$  is the Shephard input distance function for treatment  $i$  at time  $t_j$  relative to  
 248 the technology at time  $t_k$  (Shephard, 1970). Values of  $M_i(t_1, t_2) < 1$  indicate

249 improvements in productivity, while values  $M_i(t_1, t_2) > 1$  indicate productivity regress  
250 from  $t_1$  to  $t_2$ . When the estimated Malmquist index is 1, there is no productivity change.

251 The Malmquist productivity index can be decomposed into an index of input-  
252 based efficiency, the ratio outside the bracket in (3), and an index of input-based  
253 technology change, the geometric mean of the two ratios inside the bracket in (3), which  
254 measure the shift in the production frontier. As with  $M_i(t_1, t_2)$ , values of  $\varepsilon_i(t_1, t_2)$  and  
255  $T_i(t_1, t_2)$  lower (greater) than unity reflect efficiency/technology progress (regress)  
256 between times  $t_1$  and  $t_2$ .

257

### 258 3 Results

#### 259 3.1 Exploratory analysis

260 Fig. 1a-1d shows an exploratory analysis of the population dynamics along the  
261 experiment. We observe a significant effect of cycle length, density treatment and their  
262 interaction (2-way repeated measures ANOVA,  $p < 0.001$ ) on density (ind/m), total  
263 production (Kg/rope) and mussel size (ind/Kg), while meat yield (Condition index),  
264 which is mainly determined by the reproductive cycle of mussels, depended only on  
265 cycle length, reaching its maximum values from June to September.

266 Total production (Fig 1b, Kg/rope) increased up to August for the higher density  
267 treatments (570-1150 ind/m) and up to September for the lower (220-500 ind/m).  
268 Despite the negative effects of overcrowding on mussel survivorship (Fig. 1a) and  
269 growth (Fig. 1c) total production increased along the density gradient. In June,  
270 commercial mussels ( $L > 50\text{mm}$ ) accounted for 90% total rope weight, and from August  
271 onwards the percentage was over the 99%. For all density treatments, mussels reached  
272 the Medium commercial category (66mm and 37 ind/Kg) in August and the Large

273 category (70mm and 33 ind/Kg) in September. Only two density treatments, 220 ind/m  
274 and 700 ind/m reached the Extra2 category (73mm and 29ind/Kg) in November.  
275 Therefore, fresh sale prices (€/Kg) increased up to September (Fig 1e) and remained  
276 constant thereafter (Fig 1e). Industry-sale prices (€/Kg), as expected given their  
277 dependence on the condition index, were only affected by cycle length and reached  
278 maximum values between June and September (Fig 1f). Due to the small differences  
279 found in the size and quality of mussels among density treatments, the revenues per Kg  
280 were similar (Fig. 1e and 1f), while the revenues per rope increased along the density  
281 gradient for both fresh and industry sale (Fig. 2).

282 Figs. 2 and 3 show the estimated profits for fresh (Adjusted R2 = 0.801) and  
283 industry sale (Adjusted R2 = 0.77). For all density treatments, fresh sale profits  
284 increased over time, although this increase ameliorated from September onwards.  
285 Industry sale profits increased up to August and decreased thereafter. The higher  
286 densities (> 500 ind/m) amortized culture costs in June (L ≈57 mm) by industry sale and  
287 in July (L ≈61 mm) by fresh sale, while the lower densities needed an extra month to be  
288 profitable. Smaller mussels (up to August) provided higher profits through industry sale  
289 due to the increase in meat yield during summer, while larger mussels (>70 mm) are  
290 more suitable for fresh sale. In August, industry sale overcame at least a 15% fresh sale  
291 profits, whereas in September fresh sale overcame at least a 26% industry sale profits.

### 292 **3.2 Stochastic frontier function and marginal analysis**

293 Table 3 shows the parameters estimated by the translog SFPF model for total  
294 production introduced in section 2.2.2. Both output elasticities are positive and close to  
295 0.5, implying that a 1% increase in any input would increase production by ≈0.5%,  
296 though the elasticity for cycle length (0.50) is significantly higher than the elasticity for

297 stocking biomass (0.47) (t-test,  $p = 0.042$ ). We obtained constant returns to scale (RTS =  
298  $0.973 = 1$ ; t-test,  $p\text{-value} > 0.05$ ), so that a given simultaneous increase in culture days  
299 and stocking biomass will give the same percentage increase in production. The Hicks  
300 substitution elasticity for stocking biomass and cycle length ( $H_{12} = 0.905 > 0$ ) indicates  
301 a complementary relationship between inputs, i.e. they need to be increased together to  
302 raise total production. Finally, our results show that only 1.14% of the deviation from  
303 the stochastic frontier can be attributed to technical inefficiency.

304 The lower half of Table 3 shows the estimated inefficiency effects of each  
305 culture density and the respective technical efficiencies (TE). Relative inefficiency ( $\delta >$   
306  $0$ ) was statistically significant for mussels cultured at 220-570 and 800 ind/m, while  
307 relative efficiency ( $\delta < 0$ ) was found for 1150 ind/m. Despite density-dependent mussel  
308 losses, technical efficiency increased with stocking biomass, being 700 ind/m and 1150  
309 ind/m (which achieved total efficiency) the most efficient densities, whereas the lowest  
310 density operated 51.6% below the production frontier.

311 The results of the economic efficiency analysis for stocking biomass are shown  
312 in Fig. 4. Marginal costs ( $P_x$ ) increased linearly along the culture period and decreased  
313 along the density gradient. For fresh sale, marginal benefits (VMP) increased over time  
314 (Tukey HSD,  $p\text{-value} < 0.001$ ) and decreased over the density gradient, 1150 reported  
315 the lower economic efficiency and 700-800 ind/m were less efficient than 220-500 ind/m  
316 (Tukey HSD,  $p\text{-values} < 0.001$ ). For industry sale, the VMP stabilized in August  
317 (Tukey HSD,  $p\text{-value} > 0.1$ ) and the densities of 700, and 1150 ind/m reported lower  
318 economic efficiency than 220-570 ind/m (Tukey HSD,  $p\text{-value} < 0.01$ ). For both fresh  
319 an industry sale, the ratio between VMP and the marginal costs (Fig 4, bottom) shows  
320 the same temporal pattern as the VMP and remained constant along the density gradient  
321 (Tukey HSD,  $p\text{-value} > 0.05$ ). As all ratios are below 1, optimal input use was not

322 reached for any market. Comparison between markets reported higher relative  
323 efficiency for fresh sale than for industry sale from September onwards for all density  
324 treatments.

### 325 **3.3 Malmquist productivity indices**

326 Consistent with Färe et al. (1992) we report the reciprocals of the original non-  
327 parametric indices (Tables 4-6 and Fig. 5), so that numbers greater than unity denote  
328 progress while numbers lower than unity denote regress. As expected given the low  
329 proportion of deviation from the production frontier attributed to technical inefficiency  
330 (1.14%), its effect on Malmquist productivity indices was very low, and changes in  
331 productivity over time were mainly explained by shifts in the production frontier.

332 The estimated indices for efficiency change (Table 4-6, Fig 5 centre) did not  
333 show a clear pattern along culture, except for the highest density (1150 ind/m) that  
334 reported constant efficiency over time.

335 Total production and fresh sale revenues reported technology progress up to  
336 September. The production frontier stagnated thereafter for the two lower densities,  
337 while the higher densities suffered a regress during October followed by a new increase  
338 during the last month. For industry sale prices technology progress ceased in August  
339 (Table 4-6, Fig 5 right).

340 Finally, the Malmquist indices reported productivity improvements up to  
341 September in all density treatments for total production and fresh sale revenues, while  
342 for industry sale some density treatments suffered productivity regress in September  
343 (Table 4-6, Fig 5 left). The productivity losses observed in October for the higher

344 densities ( $\geq 500$  ind/m) and November for the lower ( $\leq 570$ ) were caused by reductions  
345 in potential production and efficiency, respectively.

346

#### 347 **4. Discussion and conclusions**

348 This work provides a productivity analysis for suspended mussel aquaculture at  
349 the farm-scale, based on monitoring of mussel growth and survivorship. Prior studies  
350 have focused on industry-scale analysis (see Iliyasu et al., (2014) and references therein)  
351 or have conducted farm-scale productivity analysis based on simulation models for  
352 mussel growth (Ferreira et al., 2007; Hawkins et al., 2013). Most research works on the  
353 production frontier in aquaculture have focused on efficiency measurement using either  
354 Stochastic Production Frontier (SPF) or Data Envelopment Analysis (DEA). This work  
355 incorporates empirical data to productivity analysis and evaluates the performance of  
356 different culture strategies (defined as mussel density and cycle length) through the joint  
357 application of parametric (SFPPF) and non-parametric frontier analysis (Malmquist  
358 indices).

359 This study shows that both parametric (SFPPF) and non-parametric (Malmquist  
360 indices) approaches reflect the effect of mussel population dynamics (intraspecific  
361 competition, mussel growth and mortality) on production. Population dynamics were  
362 previously described on the same data set by Cubillo et al., (2012b) and Fuentes-Santos  
363 et al., (2013). The former found a negative effect of stocking rate on mussel growth  
364 rates, and the later found significant mussel losses at higher density ( $> 500$  ind/m), being  
365 1150 ind/m the treatment with the highest mortality. Both studies concluded stronger  
366 competition effects at higher densities.



367 The current farm-scale productivity analyses use the Cobb-Douglas model  
368 (Ferreira et al., 2007; Hawkins et al., 2013; Nobre et al., 2009) to estimate the stochastic  
369 frontier function. However, when the effects of the inputs on production are not  
370 independent, we need more general models. Following the methodology applied at  
371 industry-scale level (Battese and Broca, 1997; Chiang et al., 2004; Iliyasu et al., 2014)  
372 we fitted a translog stochastic frontier function with density treatment as efficiency  
373 factor, which improved the understanding of multiple dependency and interaction  
374 between production inputs (stocking biomass and cycle length) and estimates the effect  
375 of the density treatment on technical efficiency. The likelihood ratio tests confirmed that  
376 the translog model is more accurate than the Cobb Douglas frontier function.

377 Most of the industry-scale studies in aquaculture have focused on technical  
378 efficiency and total production (Iliyasu et al., 2014). However, maximizing biological  
379 production does not lead to maximize profits, and management tools should rely on  
380 economic instead of technical efficiency. Following Ferreira et al., (2007), which stated  
381 that the profit maximization rule is based on marginal principles; we applied marginal  
382 analysis to determine the optimal stocking biomass. However, we should note that  
383 suspended mussel culture violates the principle of constant production costs  
384 (occupation, labour and transport), as these values depend on the density treatment. To  
385 estimate the marginal cost of the stocking biomass (Kg/m) we need to decompose each  
386 production cost into a constant part and a part that varies with the density treatment, and  
387 sum the latter to the cost of mussels (or mussel seed). However, in practice we cannot  
388 determine which proportion of each production cost depends on the density treatment. If  
389 we just consider the cost of mussel seed to estimate  $P_X$  we shall underestimate the  
390 marginal cost and obtain wrong conclusions in the comparison between density  
391 treatments. Estimating  $P_X$  as the sum of mussels, labour and occupation costs provides a

392 proper comparison between density treatments, but overestimates the marginal cost.  
393 Therefore we cannot rely on the comparison between VMP and  $P_X$  to determine the  
394 optimal input use in either case. Taking into account these drawbacks and that  
395 comparison between markets did not provide further information than that provided by  
396 the GAM models, we do not recommend the use of marginal analysis in suspended  
397 mussel aquaculture.

398 The use of the Malmquist productivity indices to measure productive growth at  
399 the industry-scale in aquaculture has gained popularity in recent years (Iliyasu et al.,  
400 2014). These works focus on optimizing total production, but did not considered  
401 economic capacity. Given that culture strategies should focus on maximizing profits  
402 instead on maximizing total production, we proposed to estimate the Malmquist  
403 productivity indices considering revenues as output. We point out that the variability in  
404 output prices regarding the quality of the product and the market (fresh or industry sale)  
405 should be taken into account in the economic analysis. These indices measured the  
406 change in economic capacity and efficiency along culture and allowed us to determine  
407 the optimal cycle length.

408 The parametric stochastic frontier analysis determined that 700 ind/m is the  
409 optimal culture density. The relative inefficiency observed at lower densities, which did  
410 not suffered mortality due to intraspecific competition but did not provide better mussel  
411 quality than higher densities, indicates an underuse of the available resources. The  
412 relative efficiency of 1150 ind/m, which suffered the strongest competition effects on  
413 mussel growth and survivorship (Cubillo et al., 2012a; Fuentes-Santos et al., 2013),  
414 indicates that this density exceeded the carrying capacity of the rope. Apart from the  
415 economic losses, mussel mortality also implies the increase of biodeposits beneath  
416 culture leases that alter the physical and chemical conditions of the bottom sediments,

417 and thus affect the natural biodiversity. As in (Ferreira et al., 2007; Hawkins et al.,  
418 2013) models, the environmental effects of mussel culture should be taken into  
419 consideration to develop decision making tools that guarantee the sustainability of  
420 suspended mussel culture.

421 The Malmquist productivity, efficiency and technology indices allowed us to  
422 determine the optimal cycle length. The risk of productivity regress from October  
423 onwards suggests that it is not worth extending the culture beyond September, i.e. when  
424 individuals reach lengths of  $\approx 70$  mm. In addition, the economic analysis points out that  
425 farmers would maximize profits in August ( $L = 66$  mm) by industry sale and September  
426 ( $L = 70$  mm) by fresh sale, due to the differences in the type of product that these two  
427 markets demand. These results together with the recent shift to smaller sizes ( $L \leq$   
428  $75$ mm) in mussel market, highlights the suitability of shortening the current cycle  
429 length.

430 Thus, this work provides a suitable management tool for optimizing input use in  
431 aquaculture practices and scheduling production according to market demand. Our  
432 results indicate that the current stocking densities in Galician mussel aquaculture (600-  
433 800ind/m) are close to the optimum culture density (700ind/m) and their technical  
434 efficiency is above 85%. However, according to the Malmquist indices mussel farmers  
435 should shorten the thinning-out to harvest period in order to improve their productivity.  
436 In addition to optimizing profits, this reduction of cycle length results in a more  
437 efficient use of the available space.

438

439

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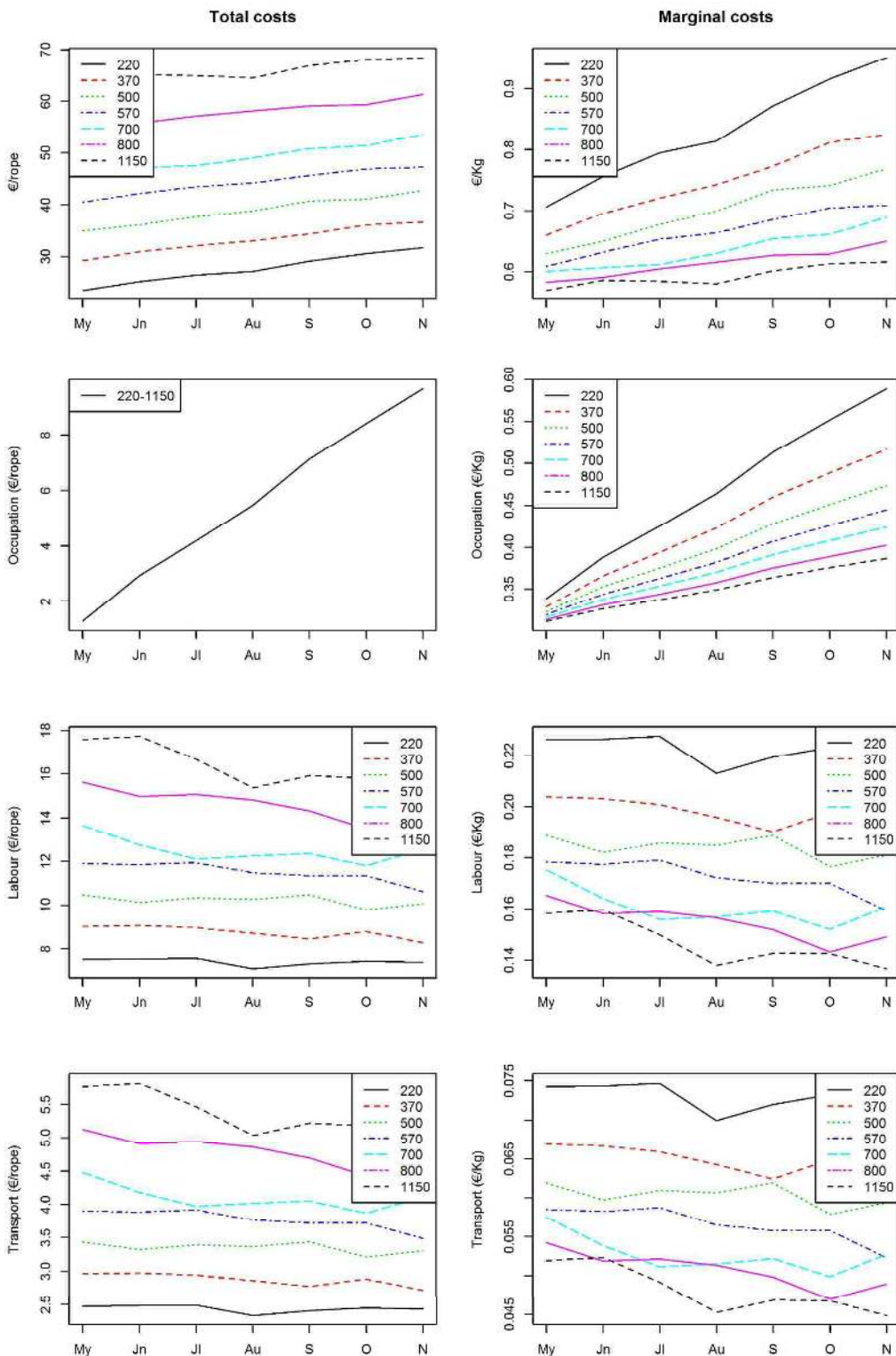
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551 **APPENDIX I**552 **Culture costs**

553 Figure A1 shows total (€/rope) and marginal costs (€/Kg) for each density treatment  
554 along the culture period. Total and occupation costs increase linearly over time, while  
555 labour and transport can be considered constant over time. Total, labour and transport  
556 costs increased with stocking density, while occupation costs remain constant along the  
557 density gradient. However, marginal costs decreased with stocking density.

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558

559 **Fig A 1:** Total (€/rope) and marginal (€/Kg) production costs by months and density treatment.

560

561

562 **APPENDIX II**

563 Parametric approach: Stochastic frontier production function (SFPF) with a model for  
564 technical inefficiency effects

565 In order to estimate the potential production and efficiency levels of the different  
566 density treatments we applied one-step stochastic frontier analysis assuming a translog  
567 frontier function with a model for inefficiency, which is assumed to depend on the  
568 density treatments (Battese and Broca, 1997; Battese and Coelli, 1995) Our model can  
569 be expressed as follows

$$570 \quad Y_{it} = \exp(f(X_{it}) + v_{it} - u_{it}) \quad (4)$$

571 where  $Y_{it}$  is the output expressed as harvest production (*Kg/rope*) for the  $i$ -th density  
572 treatment at time  $t$ ,  $X_{it}$ : is the vector of inputs, in our case stocking biomass ( $X_1$ ) and  
573 cycle length ( $X_2$ ),  $V_{it}$  is the stochastic error term and  $U_{it}$  is the estimate of the technical  
574 inefficiency  $TE_{it} = \exp(-U_{it})$ . The stochastic error term are assumed to be independent  
575 and identically distributed  $N(0, \sigma_v^2)$  and independent of  $U_{it}$ . The distribution of the  
576 inefficiency error term is a truncation (at zero) of the normal distribution with mean  $\mu =$   
577  $z_{it}\delta$  and variance  $\sigma_u^2$ , i.e  $U_{it} = z_{it}\delta + W_{it}$ , where,  $z_{it}$  is the vector of variables that may  
578 affect technical inefficiency,  $\delta$  is the associated vector of parameters and  $W_{it}$  are random  
579 error terms ( $N(0, \sigma_w^2)$ ). Positive coefficients ( $\delta > 0$ ) indicate relative technical  
580 inefficiency while negative coefficients ( $\delta < 0$ ) point out relative technical efficiency.  
581 The more the estimated value differs from zero, the stronger the efficiency/inefficiency.  
582 In this study, initial density was introduced as dummy variable to account for  
583 differences in efficiency across the density gradient.

584 The most common parametric model for the stochastic frontier function,  $f(X_{it})$   
 585 , is the translog production frontier function:

$$586 \quad \ln Y_{it} = \beta_0 + \beta_1 \ln X_{1it} + \beta_2 \ln X_{2it} + \frac{1}{2} \left( \beta_{11} (\ln X_{1it})^2 + 2\beta_{12} \ln X_{1it} \ln X_{2it} + \beta_{22} (\ln X_{2it})^2 \right) + v_{it} - u_{it} \quad (5)$$

587 where the interaction between stocking biomass and cycle length implies non-neutral  
 588 technical change. If all  $\beta_{jk} = 0$ , then the previous model reduces to a Cobb–Douglas (C–  
 589 D) SFPF model:

590 The parameters of the stochastic frontier and the model for the technical  
 591 inefficiency effects were simultaneously estimated by maximum likelihood. The  
 592 likelihood function is expressed in terms of the variance parameters  $\sigma^2 = \sigma_v^2 + \sigma_u^2$  and  
 593  $\gamma = \sigma_u / \sigma$ , which measures the proportion of deviation from the frontier due to technical  
 594 inefficiency (Battese and Coelli, 1993). Model selection for the frontier function and the  
 595 inefficiency effects were performed by one-side generalized likelihood-ratio tests (LR):

$$596 \quad LR = -2 \left\{ \ln \left\{ L(H_0) / L(H_1) \right\} \right\} = -2 \left\{ \ln [L(H_0)] - \ln [L(H_1)] \right\} \sim \chi^2 \quad (6)$$

597 Where  $L(H_0)$  and  $L(H_1)$  are the likelihood functions under the null and alternative  
 598 hypotheses, respectively. The stochastic frontier model selection was conducted testing  
 599 the null hypothesis:  $H_0: \beta_{jk} = 0$ , i.e. testing whether the translog SFPF (eq. 3) can be  
 600 reduced to a Cobb-Douglas SFPF. The inefficiency model selection was conducted by  
 601 the following multistage hypothesis test:

- 602 1.  $H_0: \gamma = \delta_0 = \delta_1 = \dots = \delta_7 = 0$ , which implies total efficiency, i.e. the model can be  
 603 reduced to the traditional mean response function, without the inefficiency error  
 604 term  $u_i$ .  
 605

- 606 2.  $H_0: \gamma = 0$ , which implies that the inefficiencies are not stochastic.
- 607 3.  $H_0: \delta_1 = \dots = \delta_7 = 0$ , which implies that the inefficiency effects are independent of
- 608 the density treatment.

609

610 The output elasticity for each input factor,  $X_j$  ( $j=1, 2$ ), defined as the percentage

611 change of the  $i$ -th output at time  $t$  for a 1% change in the  $j$ -th input, is given by:

$$612 \quad EX_{jit} = \frac{\partial \ln(Y_{it})}{\partial \ln(X_{jit})} = \frac{\partial Y_{it}}{\partial X_{jit}} \frac{X_{jit}}{Y_{it}} = \beta_j + \sum_{k=1}^m \beta_{jk} \ln(X_{kit}) \quad (7)$$

613

614 Since for the translog SFPF,  $EX_{jit}$  is different for each treatment and time, we use the

615 sample mean of each input factor across all treatments and times,  $EX_j$  to represent  $EX_{jit}$ .

616 The sum of these parameters is the return to scale (RTS), which measures the

617 percentage change in output from a 1% change in all input factors. When  $RTS > 1$  ( $RTS$

618  $< 1$ ) the production function exhibits increasing (decreasing) returns to scale, i.e. a

619 simultaneous increase in all inputs by a certain percentage results in greater (lower)

620 percentage increase in output. If  $RTS = 1$ , the farm present constant returns to scale,

621 implying that a proportionate increase in inputs will lead to the same increase in output.

622 The cross-elasticity of substitution (Chiang et al., 2004) for factors  $j$  and  $k$  under

623 the translog SFPF (eq. 3) model is defined as:

$$624 \quad H_{jk} = \frac{\beta_{jk}}{EX_j + EX_k} - 1 \quad (8)$$

625  $H_{12} > 0$  indicates that the inputs are jointly complementary, i.e. we need to increase

626 stocking biomass and cycle length together to raise total production.  $H_{jk} < 0$  indicates a

627 competitive relationship between inputs, i.e. a decrease in stocking biomass could be  
628 compensated elongating the culture period.

629 The economic efficiency of an input can be analyzed by comparison between the  
630 incremental benefit of an additional unit and its incremental cost. Assuming constant  
631 unit input cost,  $P_x$ , and output price,  $P_y$ , the value of marginal product (VMP) is defined  
632 as:

$$633 \quad VMP_{it} = MPP_{it} \cdot P_y \quad (9)$$

634 where MPP is the marginal physical product, which according to Ferguson, (2008) is  
635 equal to the elasticity of scale. If the value of the marginal product (VMP) of an input is  
636 greater than its price ( $P_x$ ), profit could be increased by increasing the use of that input,  
637 and conversely. To achieve efficient use of an input, the value of its marginal product  
638 should be equal to its price.

639

640

641 **Table 1:** Summary of production costs included in the efficiency models.

€/rope	Min (220 ind/m)	Mean (sd)	Max (1150 ind/m)
<b>Mussel</b>	10.5	23.43 (8.77)	39.9
<b>Labour</b>	6.7	11.62 (3.02)	18.67
<b>Transport</b>	2.2	3.81 (0.99)	6.13
<b>Occupation</b>		1.38 €/month	

642

643

644 **Table 2:** Hypothesis test for stochastic production function and inefficiency models.

H <sub>0</sub>	loglik H <sub>0</sub>	loglik H <sub>1</sub>	df	LR	p-value	
<b>CD vs translog</b>	93.374	106.316	3	25.883	1.01E-05	***
$\gamma = \delta_1 = \dots = \delta_7 = 0$	76.699	106.316	8	59.235	2.88E-10	***
$\gamma = 0$	76.699	83.901	3	14.406	0.001	**
$\delta_1 = \dots = \delta_7 = 0$	76.718	106.316	6	59.196	6.55E-11	***

645

(\*\*\*) p-value < 0.001, (\*\*) p-value < 0.01, (\*) p-value < 0.05.

646

647 **Table 3:** Model parameters, output elasticities and technical efficiencies for the translog

648 SFPF.

	Parameter	p-value		
<b>Elasticities</b>				
<b>Stocking rate</b>	0.473	<2.2e-16	***	
<b>Days</b>	0.500	<2.2e-16	***	
<b>RTS</b>	0.973	0.057		
$\sigma^2$	0.0198	<2.2e-16	***	
$\gamma$	0.0114	<2.2e-16	***	
<b>Inefficiency factors (<math>\delta</math>)</b>				
			<b>TE</b>	
<b>220</b>	0.725	7.67E-10	***	0.484
<b>370</b>	0.347	0.0002	***	0.707
<b>500</b>	0.164	0.0429	*	0.850
<b>570</b>	0.163	0.0187	*	0.850
<b>700</b>	0.084	0.1502		0.921
<b>800</b>	0.132	0.0026	**	0.877
<b>1150</b>	-1.025	1.68E-06	***	1.000

649

(\*\*\*) p-value < 0.001, (\*\*) p-value < 0.01, (\*) p-value < 0.05.

650

651 **Table 4:** Changes in productivity, efficiency and technology for total production.

652 Number greater (lower) than 1 indicate progress (regress).

<b>Total production (kg/rope)</b>												
<b>Malmquist indices</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	1.788	**	1.294	**	0.986	**	1.253	**	1.219	**	0.989	**
370	1.555	**	1.323	**	1.141	**	1.216	**	1.113	**	0.911	**
500	1.500	**	1.327	**	1.202	**	1.181	**	0.917	**	1.077	**
570	1.800	**	1.147	**	1.273	**	0.992		1.001		0.911	**
700	1.458	**	1.156	**	1.202	**	1.168	**	0.860	**	1.381	**
800	1.454	**	1.371	**	1.208	**	1.032	**	0.831	**	1.312	**
1150	2.041	**	1.037	**	1.208	**	1.207	**	0.852	**	1.094	**
<b>Efficiency</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	1.107	**	1.042	**	0.819	**	1.051		1.183	**	0.955	
370	0.963		1.065	**	0.947	**	1.021		1.096		0.880	**
500	0.929	**	1.082	**	1.000		1.000		0.981		0.957	
570	1.114	**	0.982		1.031		0.864	**	1.099	**	0.756	**
700	0.903	**	1.045	**	0.983	**	0.997		0.965	*	1.121	**
800	0.814	**	1.285	**	0.994		0.858	**	0.952	**	1.137	**
1150	1.087		1.000		1.000		1.000		1.000		1.000	
<b>Technology</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	1.615	**	1.242	**	1.205	**	1.192	**	1.030		1.036	
370	1.615	**	1.242	**	1.205	**	1.192	**	1.015		1.036	
500	1.615	**	1.227	**	1.202	**	1.181	**	0.935	**	1.125	**
570	1.615	**	1.168	**	1.235	**	1.148	**	0.911	**	1.205	**
700	1.615	**	1.106	**	1.222	**	1.171	**	0.891	*	1.233	**
800	1.787	**	1.067		1.215	**	1.202	**	0.873	**	1.154	*
1150	1.878	**	1.037		1.208	**	1.207	**	0.852	**	1.094	

653 (\*\*\*) p-value < 0.001, (\*\*) p-value < 0.01, (\*) p-value < 0.05.



654 **Table 5:** Changes in productivity, efficiency and technology for fresh sale revenues.

655 Number greater (lower) than 1 indicate progress (regress).

<b>Fresh sale (€/rope)</b>												
<b>Malmquist index</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
<b>220</b>	NA		1.498	**	1.279	**	1.253	**	1.330	**	0.997	**
<b>370</b>	6.014	**	1.403	**	1.291	**	1.672	**	1.003		1.093	**
<b>500</b>	2.807	**	1.413	**	1.361	**	1.403	**	0.963	**	1.074	**
<b>570</b>	NA		1.214	**	1.546	**	1.116	**	1.040	**	0.910	**
<b>700</b>	NA		1.320	**	1.331	**	1.367	**	0.858	**	1.581	**
<b>800</b>	NA		1.335	**	1.437	**	1.239	**	0.823	**	1.447	**
<b>1150</b>	NA		1.340	**	1.452	**	1.500	**	0.722	**	1.291	**
<b>Efficiency</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
<b>220</b>	NA		1.122	**	0.893	**	0.876	**	1.303	*	0.831	**
<b>370</b>	2.004	**	1.051		0.901	**	1.177	**	1.000		0.911	*
<b>500</b>	0.935		1.069	**	0.950		1.026		1.025		0.810	**
<b>570</b>	NA		0.955		1.047		0.843	**	1.186	**	0.620	**
<b>700</b>	NA		1.000		0.944	*	0.991		1.049	**	1.019	
<b>800</b>	NA		1.005		1.015		0.853	**	1.078	**	0.966	
<b>1150</b>	NA		1.000		1.000		1.000		1.000		0.886	**
<b>Technology</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
<b>220</b>	NA		1.335	**	1.432	**	1.429	**	1.021		1.200	**
<b>370</b>	3.001	**	1.335	**	1.432	**	1.420	**	1.003		1.200	**
<b>500</b>	3.001	**	1.322	**	1.432	**	1.367	**	0.939	**	1.325	**
<b>570</b>	NA		1.271	**	1.476	**	1.323	**	0.877	**	1.469	**
<b>700</b>	NA		1.320	**	1.409	**	1.379	**	0.818	**	1.551	**
<b>800</b>	NA		1.329	**	1.415	**	1.452	**	0.763	**	1.499	**
<b>1150</b>	NA		1.340	**	1.452	**	1.500	**	0.722	**	1.456	**

656 (\*\*\*) p-value < 0.001, (\*\*) p-value < 0.01, (\*) p-value < 0.05.

657 **Table 6:** Changes in productivity, efficiency and technology for industry sale revenues.  
 658 Number greater (lower) than 1 indicate progress (regress).

<b>Industry (€/rope)</b>												
<b>Malmquist indices</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
<b>220</b>	2.986	**	1.374	**	1.023	**	1.138	**	1.011	**	0.957	**
<b>370</b>	2.649	**	1.399	**	1.083	**	1.180	**	0.965	**	0.811	**
<b>500</b>	3.133	**	1.418	**	1.210	**	1.003	**	0.892	**	0.960	**
<b>570</b>	4.087	**	1.219	**	1.341	**	0.782	**	0.900	**	0.890	**
<b>700</b>	2.378	**	1.168	**	1.128	**	1.093	**	0.772	**	1.321	**
<b>800</b>	3.281	**	1.464	**	1.187	**	0.982	**	0.703	**	1.314	**
<b>1150</b>	4.588	**	1.122	**	1.171	**	1.160	**	0.633	**	1.193	**
<b>Efficiency</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
<b>220</b>	1.174	**	1.035		0.813	**	1.172	**	1.032		1.003	
<b>370</b>	1.042	*	1.054	**	0.862	**	1.216	**	1.000		0.849	**
<b>500</b>	1.232	**	1.080	**	0.962	*	1.039		1.000		0.926	*
<b>570</b>	1.607	**	0.972		1.029		0.816	**	1.112	**	0.775	**
<b>700</b>	0.935		0.980		0.903	**	1.068		1.042	**	1.086	**
<b>800</b>	1.166	**	1.271	**	0.977	**	0.891	**	1.037	**	1.091	**
<b>1150</b>	1.551	**	1.000		1.000		1.000		1.000		1.000	
<b>Technology</b>												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
<b>220</b>	2.544	**	1.328	**	1.257	**	0.971		0.980		0.955	
<b>370</b>	2.544	**	1.328	**	1.257	**	0.970		0.965		0.955	
<b>500</b>	2.544	**	1.313	**	1.257	**	0.965		0.892	**	1.036	
<b>570</b>	2.544	**	1.254	**	1.303	**	0.959		0.809	**	1.148	**
<b>700</b>	2.544	**	1.191	**	1.249	**	1.024		0.740	**	1.217	**
<b>800</b>	2.815	**	1.152	**	1.214	**	1.102	**	0.678	**	1.204	**
<b>1150</b>	2.958	**	1.122	*	1.171	**	1.160	**	0.633	**	1.193	**

659 (\*\*\*) p-value < 0.001, (\*\*) p-value < 0.01, (\*) p-value < 0.05.

660 **Figure captions**

661 Fig. 1. Interaction plots of density (ind/m), total production (Kg/rope), individuals per  
662 kilogram of mussels (ind/Kg), individuals per kilogram of tissue (ind/Kg of tissue),  
663 condition index (%), fresh and industry sale prices (€/Kg) and costs (€/rope).

664 Fig. 2: GAM fit showing the effect of stocking biomass (Kg/rope) and cycle length  
665 (days) on fresh sale and industry sale profits (€/rope).

666 Fig. 3: GAM fits for the temporal evolution of profits obtained by fresh (black) and  
667 industry sale (red) by density treatment.

668 Fig. 4: Top: Marginal costs ( $P_x$  left) and VMP indices for total production of stocking  
669 biomass for fresh (centre) and industry (right) sale. Bottom: ratio between VMP and  
670 marginal costs for fresh and industry sale.

671 Fig. 5: Malmquist productivity, efficiency and technology indices for total production  
672 (top), fresh sale revenues (centre) and industry sale revenues (bottom).

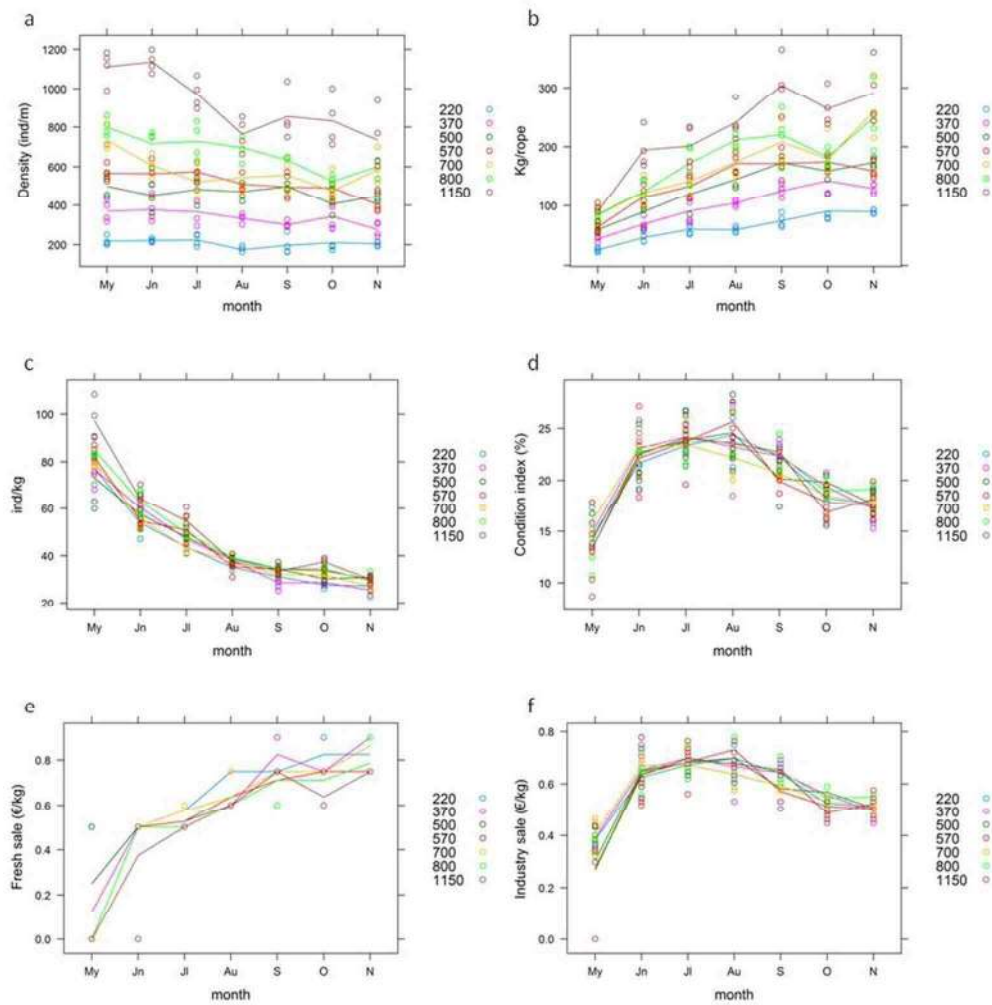


Fig. 1. Interaction plots of density (ind/m), total production (Kg/rope), individuals per kilogram of mussels (ind/Kg), individuals per kilogram of tissue (ind/Kg of tissue), condition index (%), fresh and industry sale prices (€/Kg) and costs (€/rope).  
151x154mm (150 x 150 DPI)

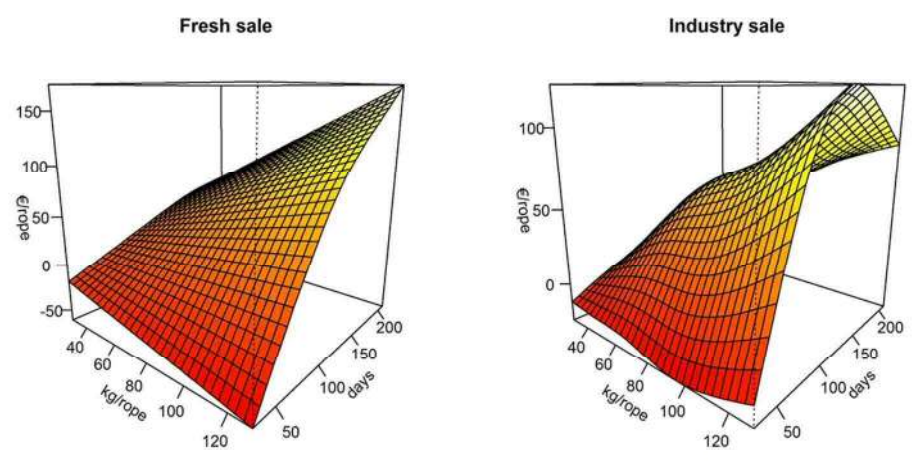


Fig. 2: GAM fit showing the effect of stocking biomass (Kg/rope) and cycle length (days) on fresh sale and industry sale profits (€/rope).  
99x55mm (300 x 300 DPI)

view Only

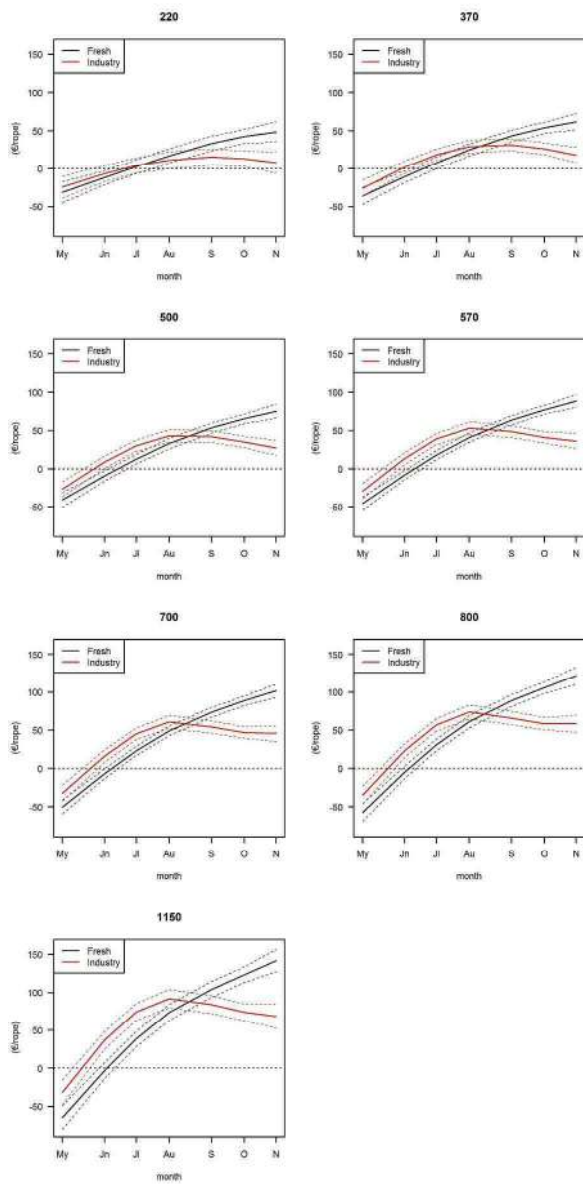


Fig. 3: GAM fits for the temporal evolution of profits obtained by fresh (black) and industry sale (red) by density treatment.  
239x479mm (300 x 300 DPI)

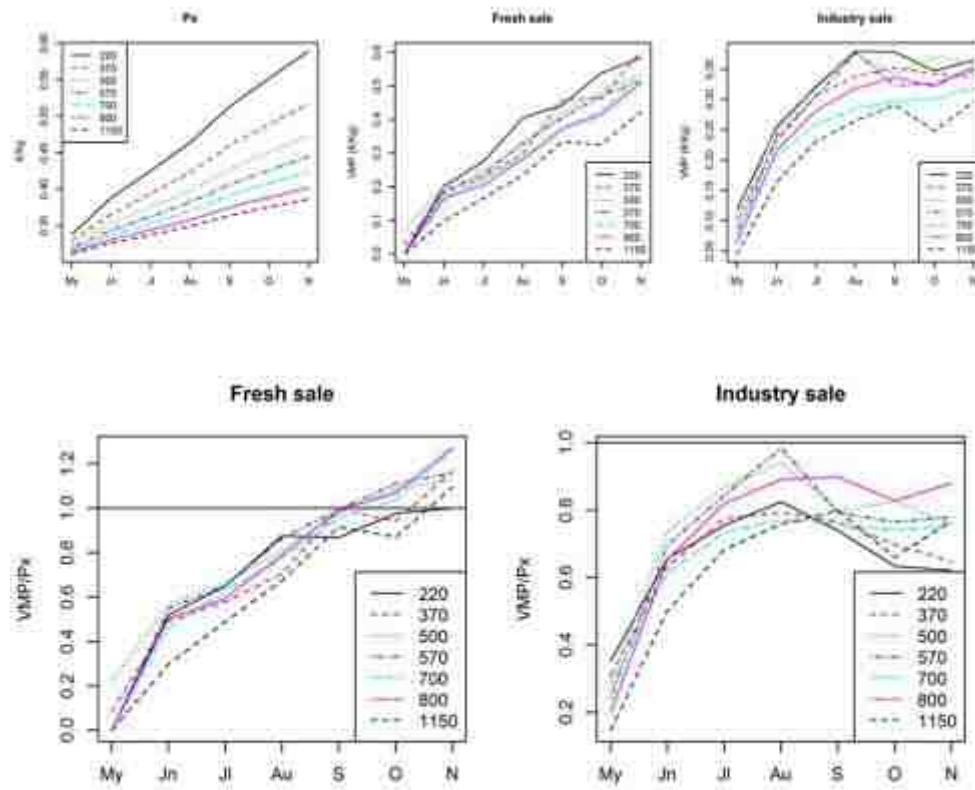


Fig. 4: Top: Marginal costs (Px left) and VMP indices for total production of stocking biomass for fresh (centre) and industry (right) sale. Bottom: ratio between VMP and marginal costs for fresh and industry sale.  
160x137mm (150 x 150 DPI)

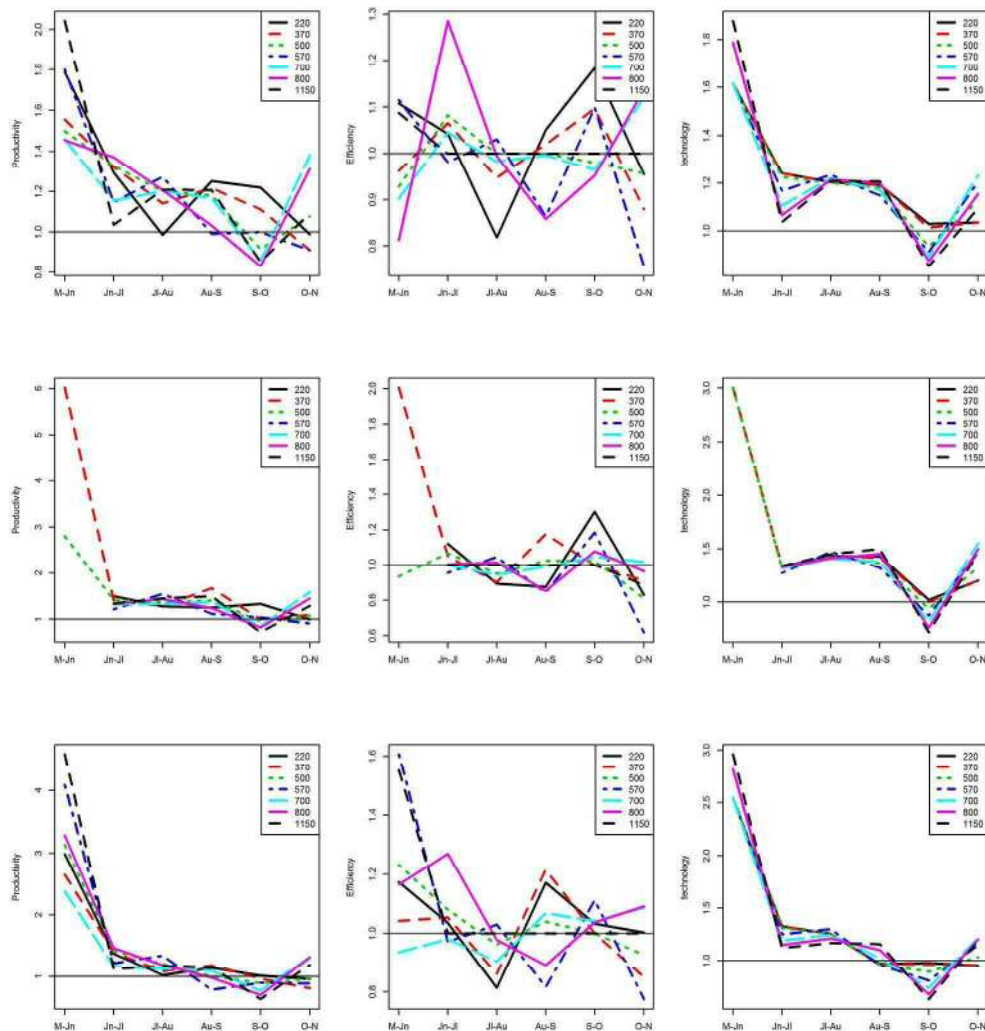


Fig. 5: Malmquist productivity, efficiency and technology indices for total production (top), fresh sale revenues (centre) and industry sale revenues (bottom).  
219x241mm (300 x 300 DPI)