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A broadband achromatic metalens array for integral imaging in the visible

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Abstract

Integral imaging is a promising three-dimensional (3D) imaging technique that captures and reconstructs light field information. Microlens arrays are usually used for the reconstruction process to display 3D scenes to the viewer. However, the inherent chromatic aberration of the microlens array reduces the viewing quality, and thus, broadband achromatic imaging remains a challenge for integral imaging. Here, we realize a silicon nitride metalens array in the visible region that can be used to reconstruct 3D optical scenes in the achromatic integral imaging for white light. The metalens array contains 60 × 60 polarization-insensitive metalenses with nearly diffraction-limited focusing. The nanoposts in each high-efficiency (measured as 47% on average) metalens are delicately designed with zero effective material dispersion and an effective achromatic refractive index distribution from 430 to 780 nm. In addition, such an achromatic metalens array is composed of only a single silicon nitride layer with an ultrathin thickness of 400 nm, making the array suitable for on-chip hybrid-CMOS integration and the parallel manipulation of optoelectronic information. We expect these findings to provide possibilities for full-color and aberration-free integral imaging, and we envision that the proposed approach may be potentially applicable in the fields of high-power microlithography, high-precision wavefront sensors, virtual/augmented reality and 3D imaging.

Introduction

Integral imaging, first proposed in 1908 by Lippmann, is considered to be one of the most promising imaging techniques for 3D displays¹. The concept was subsequently verified in 1911 by using a pinhole array² and a suitable microlens array in 1948. Replacing the photographic film with a digital device such as a CCD or a LCD³ has considerably increased the attraction of integral imaging. Very recently, the possibility of merging integral imaging into a smartphone has been reported by utilizing a matching microlens array⁴. However, even though the microlens array has become a routine component of integral imaging, its inherent chromatic aberration still

²School of Physics, Sun Yat-sen University, Guangzhou 510275, China Full list of author information is available at the end of the article. These authors contributed equally: Zhi-Bin Fan, Hao-Yang Qiu, Han-Le Zhang reduces the viewing quality and prevents full-color imaging from being realized. Chromatic aberration represents the failure of a lens to

focus light of different wavelengths onto the same plane, resulting in blurring and color distortion. Correcting the chromatic aberration in the broadband region is fundamental for achieving full-color imaging. In traditional optical design, several lenses with different focal lengths are usually cascaded together to construct a multiwavelength achromatic lens system. The most common types are achromatic doublet lenses and apochromatic lenses, which are used to focus light of two and three wavelengths, respectively, onto the same focal plane. However, the bulky size of these achromatic lenses limits their applications in portable, wearable and integrated devices. Clearly, replacing these geometrical lenses with more compact components to perform the same achromatic task is imperative. Accordingly, the metalens⁵⁻³⁸ has recently attracted considerable attention. Numerous

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studies have already been performed to create achromatic metalenses^{24–30} at several discrete wavelengths. By tailoring the electromagnetic response of nanoposts, a narrowband achromatic metalens³¹ in the visible region has also been developed. Recently, broadband achromatic metalenses^{32–35} designed by either the group delay method or the plasmonic resonance method have been achieved in the visible region using Pancharatnam-Berry (PB) phasebased nanoposts. Unpolarized broadband achromatic metalenses have also been realized in the near-infrared³⁶ and visible³⁷ regions with the use of silicon and TiO₂, respectively. However, a method to fabricate a polarization-insensitive broadband achromatic metalens in a CMOS-compatible way for the visible region has yet to be developed, and hence, relevant research remains highly attractive for certain commercial applications.

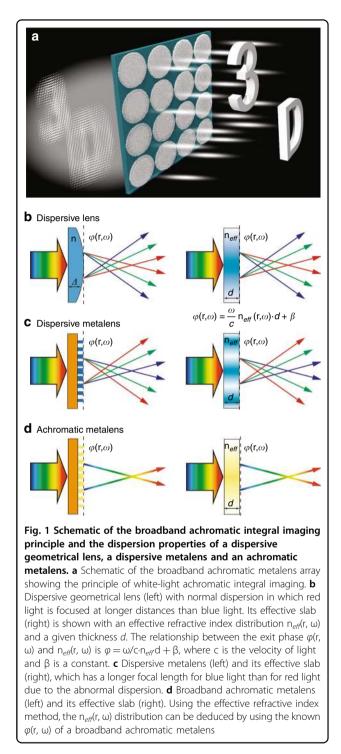
Furthermore, since a metalens is composed of only a single layer of subwavelength nanoposts, it can be designed with an ultrasmall aperture to enhance the quality of integral imaging. Very recently, metalenses have been used for light-field imaging³⁸, in which an achromatic metalens array is used to capture optical information experimentally and render the imaging on computers with different depths of focus; this constitutes a prospective application of a full-color light-field camera. However, insufficient research has been conducted on the use of metalenses in applications of integral imaging displays. As one of the most important types of 3D displays^{39,40}, integral imaging displays encode 3D objects with computational algorithms but reconstruct optical images experimentally in free space; thus, the workflow is somewhat opposite to that of a light-field camera. Since the polarization of light in different display devices are different, metalenses must also be insensitive to the polarization in integral imaging.

Here, we demonstrate a metalens array that can be used to reconstruct the light field experimentally, and we verify the concept of full-color integral imaging (Fig. 1a). We first present a single polarization-insensitive broadband achromatic metalens working in the entire visible region. A fully CMOS-compatible semiconductor material, silicon nitride, is used to design the high-transmission nanoposts with zero effective material dispersion and various values of the effective refractive index, thereby composing the single achromatic metalens. Composed of 60×60 metalenses, a broadband achromatic metalens array is then fabricated and used to demonstrate its whitelight integral imaging results experimentally.

Results

Broadband achromatic method

As is well known, the dispersion of a certain device refers to the derivative of its given performance parameter with respect to the frequency or wavelength; in this



article, we use the frequency as the independent variable for convenience. Hence, the dispersion of a lens can be defined as the derivative of the focal length versus the frequency $df/d\omega$. A conventional geometrical lens has a normal dispersion ($df/d\omega < 0$, Fig. 1b), indicating that blue light is deflected more than red light, while a diffractive lens or common metalens follows the anomalous dispersion $(df/d\omega > 0, Fig. 1c)$ insomuch that the focal length for blue light is larger than that for red light. A perfect achromatic lens, required to generate a full-color image, must be dispersionless $(df/d\omega = 0, Fig. 1d)$ and must be able to focus light at any wavelength within the working range onto the same focal plane. In our opinion, all these lens components can be effectively viewed as a relevant slab (Fig. 1b–d right) of uniform thickness under certain conditions. In the following, we propose a broadband achromatic method from a novel perspective of the effective refractive index, providing a more accessible manner with which to understand the impacts of dielectric materials on broadband achromatic design.

Previous studies used the phase profile of $\phi(r,\omega_0) = \omega_0 \Gamma(r,\omega_0)$, where Γ is a function of the desired performance, to create a metasurface device at a given frequency. To consider the broadband design of a metasurface device, we need to generalize the phase profile into a more general form for a continuous frequency region while maintaining the desired performance at each frequency. Since the phase distribution is relative to a reference point at a given position r and frequency ω , we can rewrite the phase profiles in the following form by adding two constants, namely, α and β , thereby guaranteeing that the performance of the metasurface device will not change, yielding $\phi(r,\omega) = \omega[\Gamma(r,\omega) + \alpha] + \beta$. Hence, the relative phase is provided by the metalens elements with respect to the following:

$$\phi(r,\omega) = \frac{\omega}{c} \left(-\sqrt{r^2 + f^2} + f + \alpha \right) + \beta \tag{1}$$

where *f* is the focal length and *c* is the velocity of light in vacuum; for convenience, *c* is placed outside the bracket. Equation (1) implies that β represents the spectral reference phase at the zero frequency (wavelength $\lambda \rightarrow \infty$), and α decides the spatial reference phase at the center of the lens (r = 0). Therefore, broadband achromatic elements can be achieved when the phase profiles satisfy the form of Equation (1) with a fixed focal length at any working frequency. Figure 2a plots a sketch map of three-phase profiles (blue, green, and red light) in the r- ω space. When neglecting reflection and considering only the phase of transmitted light, the metalens can be regarded as a slab (Fig. 1) with a fixed thickness *d* and an inhomogeneous effective refractive index n_{eff} , therefore, Equation (1) can be rewritten as

$$\phi(r,\omega) = \frac{\omega}{c} n_{eff}(r,\omega) \cdot d + \beta,$$

where $n_{eff}(r,\omega) = \frac{1}{d} \left(-\sqrt{r^2 + f^2} + f + \alpha \right)$ (2)

For a dispersionless metalens (df /d ω = 0), we have

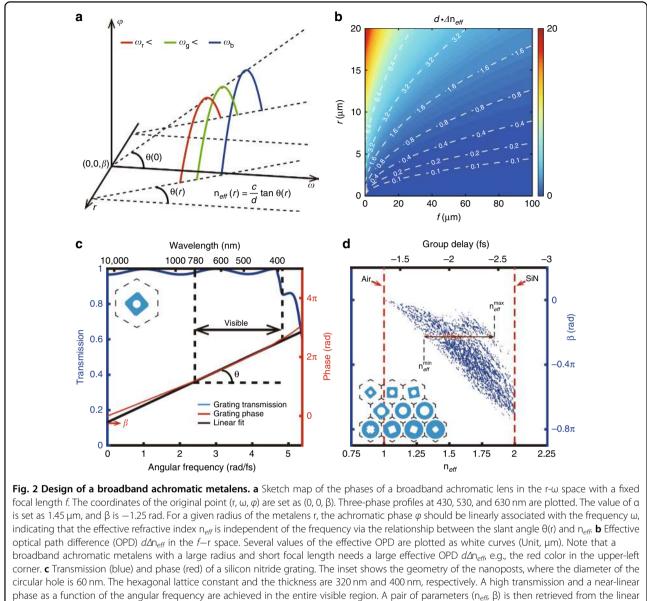
$$\frac{\partial}{\partial \omega} n_{eff}(r,\omega) = 0 , \qquad \omega \in [\omega_{min}, \ \omega_{max}]$$
(3)

The left-hand side of Equation (3) represents the effective material dispersion. That is, the zero effective material dispersion is necessary for the broadband achromatic metalens, and the achromatic bandwidth $\Delta \omega = \omega_{\text{max}} - \omega_{\text{min}}$ depends on the spectrum range sustained by the zero effective material dispersion. As n_{eff} is independent of the frequency, the phase must change linearly with the frequency according to Equation (2). Through a simple derivation, we can further acquire the relationship $n_{eff} = \frac{c}{d} \cdot \frac{\partial \varphi}{\partial \omega} = -\frac{c}{d} \tau_g = \frac{c}{d} tan \theta$, where τ_g is the group delay and θ is the slant angle (Fig. 2a) of the intersection between the phase and ω -axis. Note that the above formula not only gives the relationship between n_{eff} and the group delay τ_g but also provides a way to calculate the value of n_{eff} through the slant angle θ .

The aforementioned text discusses the bandwidth restriction on the achromatic metalens. The size limitation can be analyzed from Equation (2). At the center (r =0) of the metalens, we have $n_{eff}^{max} = \frac{\alpha}{d}$. For the whole metalens, we have $\Delta n_{e\!f\!f} = \frac{1}{d} \left(\sqrt{r_{max}^2 + f^2} - f \right)$. Note that the maximum n_{eff} is reached at the center of the metalens, and the constant α represents the maximum effective optical path (OP) $d \cdot n_{eff}$. The maximum size r_{max} of the metalens depends on the effective optical path difference (OPD) $d \cdot \Delta n_{eff}$. Figure 2b shows a map of the $d \cdot \Delta n_{eff}$ that the achromatic metalens needs. For a given focal length, a larger aperture achromatic metalens requires a larger effective OPD value by either increasing the metalens thickness d or enlarging the range of the n_{eff} distribution. However, the size of an achromatic metalens is always restricted on a small scale due to the difficulty of fabricating high-ratio nanoposts and the limitation on the n_{eff} range. For example, for silicon nitride (n = 2) and air (n = 2)1) materials and for a given thickness $d = 0.8 \,\mu\text{m}$, the maximum $d \cdot \Delta n_{eff}$ is 0.8 µm. Figure 2b shows that, in principle, the radius of an achromatic metalens with a focal length of 50 μ m can only be less than 9 μ m. As a whole, to create a broadband achromatic metalens, one needs to achieve zero effective material dispersion in the spectral region and to enlarge the range of the n_{eff} distribution as much as possible in the spatial region.

Design of the broadband achromatic metalens

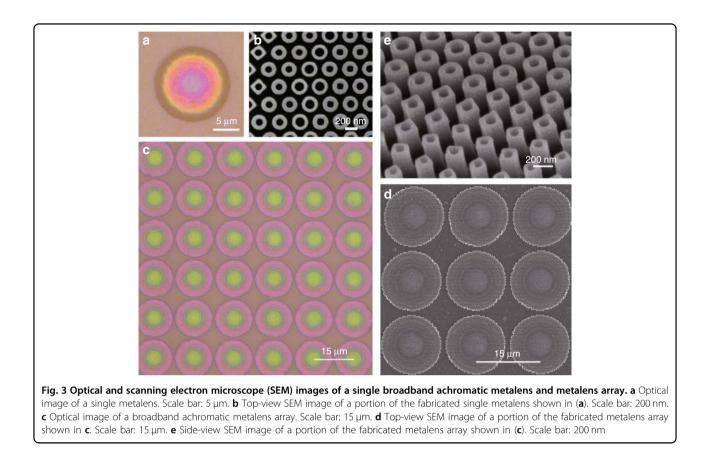
As mentioned above, we need to design nanoposts to achieve zero effective material dispersion. For our purpose of manipulating unpolarized visible light, nanoposts with 90° spatial rotational symmetries are given priority over other nanoposts. Here, a hexagonal silicon nitride grating with a subwavelength lattice constant (a = 320 nm) on a silica substrate is considered. The basic geometrical shape is shown in the inset of Fig. 2c, where the diameter of the circular hole is 60 nm. The thickness of the silicon nitride



fitting of the phase (black), where $n_{eff} = c/d \tan(\theta)$ and β is the crossing point at zero frequency. **d** Calculated (n_{eff} , β) results for all considered silicon nitride gratings. Each blue point represents a different grating. Red dashed lines indicate the air and silicon nitride materials; the results show that the n_{eff} values of all considered gratings are mostly located between the background material (air) and the chosen dielectric material (SiN). By selecting the optimal β value to obtain the maximum Δn_{eff} the gratings at red points can be screened out; finally, ten kinds of gratings (inset) are chosen after the discretization of n_{eff} to compose the broadband achromatic metalens

grating is set as 400 nm. Figure 2c plots the simulation results of the transmission and phase spectra for normal incidence light with y-polarization calculated by using rigorous coupled-wave analysis (RCWA)⁴¹. The blue curve shows that high transmission can be kept well over an ultralarge spectral region, in which the wavelength λ is greater or far greater than the lattice constant *a*. When the wavelength is near or less than the lattice constant, the transmission drops sharply. The red curve shows that the phase increases almost linearly in the visible region,

implying that zero effective material dispersion can be achieved in such frequency regions. After a linear fitting calculation (black line), one can obtain the frequencyindependent n_{eff} from the slant angle θ and the parameter β of such a nanopost. In this way, a pair of values (n_{eff} , β) can be used to describe the nearly linear phase spectrum over the entire visible region for a single kind of nanopost. One simple way to enlarge the range of the n_{eff} distribution is to calculate these values for as many as types of nanoposts with different structural parameters as possible



(Fig. S2). As illustrated in Fig. 2d, the red dashed lines correspond to the air and silicon nitride materials. Each point in Fig. 2d represents a different nanopost, and all points are located between the air and silicon nitride lines, implying that the n_{eff} values of all considered nanoposts cannot fall outside the scope between the chosen dielectric material and the background material. Then, the value of the constant β is chosen to achieve the maximum Δn_{eff} highlighted by the red points in Fig. 2d. Finally, ten kinds of nanoposts (inset of Fig. 2d) are selected to map different values of n_{eff} and are placed on the silicon dioxide substrate to form a hexagonal lattice with a subwavelength lattice constant *a*. It is worth noting that there is no longer a need to set a given frequency in the design process because the n_{eff} values of all selected nanoposts are independent of the frequency throughout the working region. This constitutes a considerable difference between the previously proposed metalenses and the proposed achromatic metalens.

Characteristics of the broadband achromatic metalens

Figure 3a, b illustrate optical and scanning electron microscope (SEM) images, respectively, of the proposed achromatic metalens with a diameter of $14 \,\mu\text{m}$. The metalens sample is achieved by a top-down nanofabrication process via standard electron-beam lithography

(EBL) technique. The top-view SEM image (Fig. 3b) of a portion of the metalens with a relatively high magnification shows the well-fabricated nanoposts with circular or square holes. The measurement and simulation results of the field distributions between 430 and 780 nm are shown in Fig. 4a, b. The y-polarized plane wave is normally incident onto the metalens from the silicon dioxide substrate as measurement setup (Fig. S3) shown. Visible light can be focused approximately onto the same focal plane with a relatively long focal depth. Figure 4c displays the measured and simulated normalized intensity distributions on a linear scale in the focal plane. The related xdirection cross-sections are shown on the bottom. The simulated (blue squares) and measured (red triangles) focal lengths are plotted in Fig. 4d. One can see that the average measured focal length is ~ $81.5 \,\mu$ m, yielding an experimental NA of 0.086. To describe the focal depth, we define the depth of focus (DOF) here as the range around the focus at which the normalized intensity has fallen to 0.95 and use an error bar to denote it. Analyzing the DOF at all measured wavelengths, an overlapping region from z = 82.5 to 89.4 µm can be obtained (yellow in Fig. 4d). Such a region is regarded as the achromatic focusing region of the proposed single metalens. The purple dotted line shows that the measured focusing efficiency can be maintained in the range of 36% ~ 55% at all visible

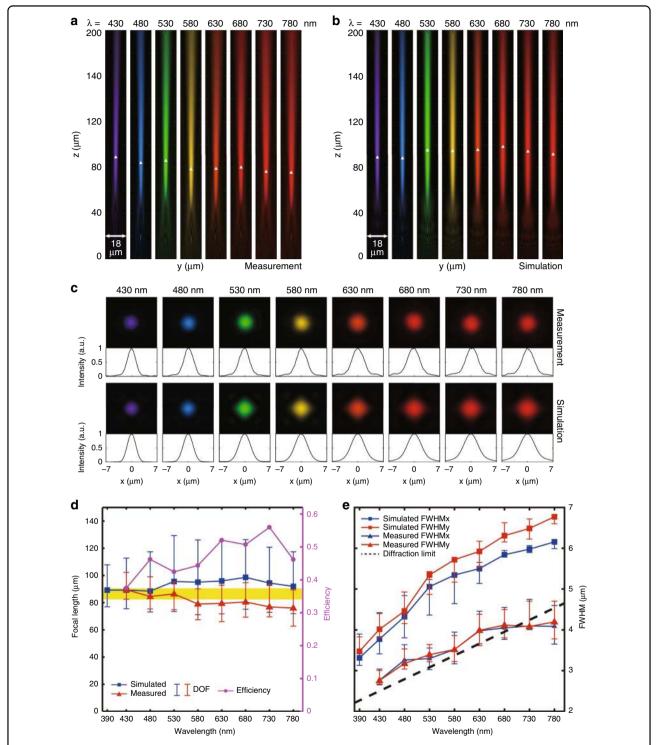


Fig. 4 Measurement and simulation results for a single broadband achromatic metalens with a diameter of 14 μm. a Measured normalized intensity distributions on a linear scale in the y–z plane using pseudo colors corresponding to their respective wavelengths. The wavelengths of incidence are denoted on the top. The focal points are marked by white triangles. **b** Corresponding simulated normalized intensity distributions. **c** Measured and simulated normalized intensity distributions on a linear scale in the focal plane. **d** Measured (blue square points) and simulated (red triangle points) focal lengths at different wavelengths. The average measured focal length is approximately 81.5 μm, yielding an NA of 0.086. The error bars show the depth of focus (DOF), which is defined here as the range around the focus at which the normalized intensity has fallen to 0.95. Since the metalens can still effectively perform imaging inside the DOF, an achromatic region (yellow area) can be obtained by analyzing the error bars at all wavelengths. The purple dotted line shows that the measured focusing efficiency can be maintained in the range of 36% ~ 55% at the measured wavelengths, while the maximum is reached at 730 nm. **e** Measured (triangles) and simulated (squares) full width at half maximums (FWHMs) at different wavelengths. The blue color denotes the results in the x-direction, while the red color denotes the results in the y-direction. The error bars show the ranges of the FWHM inside the DOF regions

wavelengths. An average efficiency of 47% is achieved, and the maximum is reached at 730 nm. The full width at half maximums (FWHMs) at different wavelengths are also plotted in Fig. 4e, and the corresponding error bars denote the ranges of the FWHM within the DOF regions. It can be seen that the FWHMs increase with the wavelengths in both the simulation and the measurement results; additionally, with the nearly diffraction-limited spot (λ /2NA), the measured values are lower than the simulated values because the actual measured focal lengths are shorter.

Achromatic metalens array and integral imaging

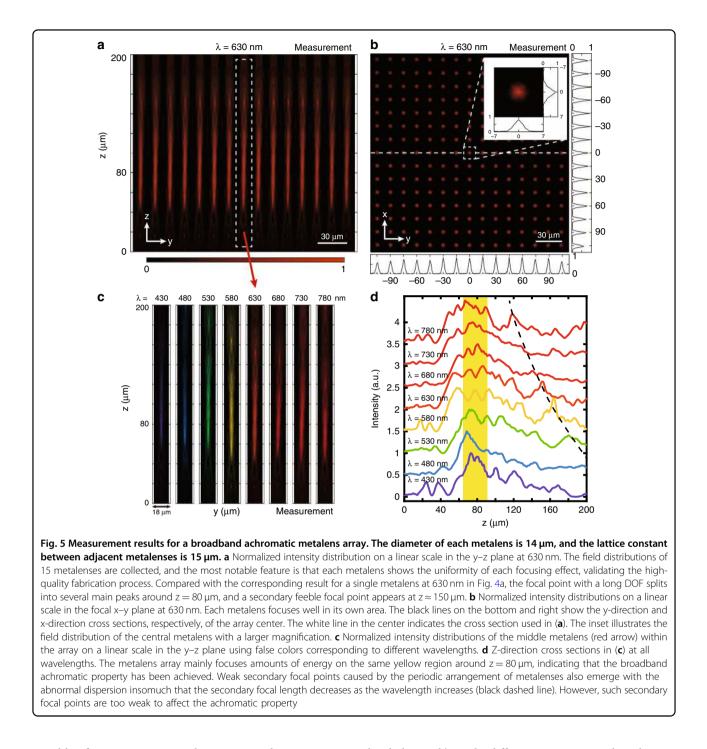
To further demonstrate our purpose, we take the metalens as a subsystem by constructing a metalens array. We first fabricate an achromatic metalens array composed of 15×15 metalenses as discussed above; the optical and SEM images are shown in Fig. 3c-e. The side-view SEM image of the metalens in Fig. 3e describes the vertical profile of the nanoposts. Figure 5a, b show the measured normalized intensity distributions on a linear scale in the y-z plane and the focal x-y plane at 630 nm, respectively. It is obvious in Fig. 5a that each metalens demonstrates the uniformity of each focusing effect. Compared with the results for a single metalens in Fig. 4a, the focal point with a long DOF splits into several main peaks around z =80 μ m, and a secondary focal point appears at $z = 150 \mu$ m. A 15×15 spot array is shown in Fig. 5b, implying that each metalens focuses well on its own area. The crosssections in the y- and x-directions are plotted on the bottom and right of Fig. 5b, respectively, while the intensity distribution of the central metalens is illustrated with a larger magnification (inset). Furthermore, the achromatic focusing effect of the central metalens (red arrow) is also illustrated in Fig. 5c, and the z-direction cross sections at different wavelengths are plotted in Fig. 5d. Note that the metalens array mainly focuses on the whole visible spectrum within the same region around z $= 80 \,\mu m$ (yellow area), implying that the broadband achromatic property is achieved. A weak secondary focal point, caused by the periodic arrangement of metalenses, also emerges with the abnormal dispersion insomuch that the secondary focal length decreases as the wavelength increases (black dashed line). However, due to the long secondary focal length and the feeble intensity (values less than 0.5 at most measured results), the influence of this secondary focal point is weak for the achromatic property.

To better demonstrate the imaging quality, we further fabricate another array of 60×60 broadband achromatic metalenses. The measurement configuration for this imaging demonstration is shown in Fig. 6a, and the imaging results are shown in Fig. 6b–d. The object film is an elemental image array calculated by the computational algorithm using the integral imaging acquisition

principle⁴² (Supplementary material S4). The light from the 3D object (the number "3" and the letter "D" on different planes) passes through an ideal achromatic microlens array to form the elemental image array. The object film illuminated by the blue, green, red and white light from the lamp and the corresponding reconstructed images can be captured by the following microscopy system. Blue, green and red light is generated by inserting narrowband (10 nm) filters of 488, 532, and 633 nm, respectively. In these experiments, we adjust the light path system to make the image clear and then change only the narrowband filter to another filter or remove it entirely to observe the imaging qualities for light of different colors. Here, we consider two cases to show the optical reconstruction effect. In the computer modeling process, we set the distance between the number "3" (letter "D") and the central depth plane as d_3 (d_D), as shown in Fig. S4. In the first case of $d_{\rm D} = d_3$, the two characters are on the same depth plane (Fig. S5a), and hence, they will always become clear together (Fig. 6b). It is obvious that the characters can be reconstructed well in blue, green and red light and even white light. This is powerful evidence for the realization of our broadband achromatic metalens array over the entire visible region. To further show the image depth effect, we set $d_{\rm D} > d_3$ in the second case, which means that the number "3" is closer to the central depth plane than is the letter "D" (Fig. S5b). When we move the microscopy system along the optical axes to focus on the number "3" (Fig. 6c), the letter "D" continues to blur. On the other hand, when we focus on the letter "D" (Fig. 6d), the number "3" will become blurred compared with that in Fig. 6c. We also provide videos of these two cases in the supplementary material. One can clearly see the unambiguous infocus/blurry effect when the reconstruction plane locates different image depths. Video m1 for the case of $d_{\rm D} = d_3$ shows that both characters become clear or blurred together, while Video m2 for the case of $d_D > d_3$ illustrates that the number "3" becomes clear first, followed by the letter "D". These imaging results verify the 3D image depth effect using our metalens array in integral imaging.

Discussion

By designing the geometries of nanoposts, a series of polarization-insensitive silicon nitride gratings are obtained by using zero effective material dispersion and different values of the effective refractive index. According to the achromatic effective refractive index distribution, a transmissive achromatic metalens is realized in the visible spectrum from 430 to 780 nm. By composing the metalenses in a rectangular lattice, a 60×60 achromatic metalens array is achieved. We also show the broadband achromatic integral imaging performance with a white-light source. Finally, the low-cost and CMOS-compatible fabrication process makes the achromatic metalens array



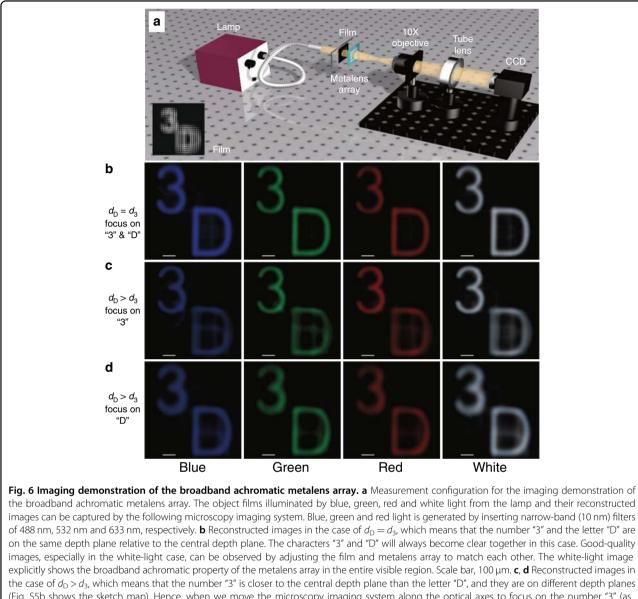
suitable for numerous applications, such as microlithography, wavefront sensors, and 3D imaging.

Materials and methods

Imaging setup

In the experimental setup (Fig. 6a), a white-light source (Thorlabs OSL2) is applied to illuminate the metal film, and a series of narrow-band (10 nm) filters (not shown in

the light path) with different center wavelengths are placed between the lamp and the film. A microscopy imaging system composed of a ×20 objective lens (Olympus MPLFLN20xBD), a tube lens (Thorlabs TTL180) and a color CCD camera (Mshot MC20) is used to observe the images. Note that such a microscopy imaging system is mounted on a large translation stage for convenient movement.



explicitly shows the broadband achromatic property of the metalens array in the entire visible region. Scale bar, 100 µm. **c**, **d** Reconstructed images in the case of $d_D > d_3$, which means that the number "3" is closer to the central depth plane than the letter "D", and they are on different depth planes (Fig. S5b shows the sketch map). Hence, when we move the microscopy imaging system along the optical axes to focus on the number "3" (as shown in **c**), the letter "D" continues to blur since they are not on the same depth plane. When we focus on the letter "D" in (**d**), the number "3" will become blurred compared with that in (**c**). These imaging results effectively demonstrate the three-dimensional image depth using our metalens array in integral imaging. Scale bar, 100 µm

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Authors' contributions

J.W.D. and Q.H.W. conceived the project. Z.B.F., H.L.Z., and X.N.P. performed the simulations and developed codes; H.L.Z. and H.R. calculated the object information; H.Y.Q., L.D.Z., and L.L fabricated the metalens and metalens arrays; Z.B.F. and H.Y.Q. measured the metalens and metalens arrays; all authors contributed to data analysis, discussions and manuscript writing.

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Conflict of interest

The authors declare that they have no conflict of interest.

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