Another simulation was made, with the circuit simulated in the basic form, without enhancement circuits, assuming  $G_m/G_{\rm ds}$  and  $C_{\rm gs}/C_{\rm gd}$  ratios of 1000, with the biasing and signal current sources assumed as ideal. This is not realistic for the basic structures, but is reasonable when it is assumed that the additional enhancement circuits are present. The result is curve "d". The same simulation for the alternative realizations resulted in similar curves (not shown).

In the simulations, it was assumed that the circuit stabilizes completely between the switching instants. Errors due to signal-dependent clock feedthrough and other nonlinear effects were not considered (these errors are dependent on details of the final implementation).

# IV. CONCLUSION

The direct synthesis of exact SI bilinear simulations of passive filters using second-generation Euler integrators was demonstrated. A low-pass filter was used as example, but, as in SC realizations, the method can be extended to all the filter types. Second generation integrators were used due to their superior sensitivity characteristics, and simpler final structure. Comparisons made with alternative realizations demonstrate that the proposed synthesis method is preferable, at least in the examined case of single-path filters, with unbalanced signals.

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# A CMOS Analog Circuit for Gaussian Functions

J. Madrenas, M. Verleysen, P. Thissen, and J. L. Voz

Abstract—A simple CMOS analog circuit that performs the Gaussian function for classification applications is introduced. Combining the exponential characteristics of MOS transistors in weak inversion and the square characteristics in strong inversion the function is built. Design constraints and mismatch effects are discussed, as well as the layout optimization. The circuit has been designed in a SOI technology and manufactured. Good experimental results are obtained which shows that the circuit is suitable to be included as a building block of an IC to perform classification tasks or other possible applications.

# I. INTRODUCTION

Data classification is an application where neural algorithms show promising capabilities [1]. In many neural classification algorithms, the decision on the class associated to an input pattern is based on the comparison of the different probabilities to belong to each possible class [2]. In the associated calculations, the probability density functions are needed. In many cases these functions can be modeled by normal distributions (or combinations).

Even though these algorithms can be conveniently implemented on workstations, in real time, portable and other space or power constrained applications, dedicated hardware implementation is a promising solution [3]. Because of its good integration of processing capabilities, the analog approach has been taken in many CMOS neural network IC's. In this paper a compact analog circuit that generates the Gaussian function for neural or signal processing algorithms is proposed.

Other approaches to implement in CMOS technologies the Gaussian function in weak inversion operation [4] or as a piece-wise linear approximation [5] have been reported. The circuit we propose generates a true Gaussian form in weak inversion using only five transistors and can approximate the function also in strong inversion operation mode. The Gaussian function is defined in (1), where x is the input and y the output of the

$$y = Ae^{-\frac{x^2}{2\sigma^2}} \tag{1}$$

function, and A,  $\sigma$  are adjustable constants which define, respectively, the amplitude and the width of the Gaussian function.

The function is constructed in two steps. First the input x is squared by means of the quadratic V-I characteristic of a MOS transistor in saturation, secondly a negative exponential obtained with a MOS transistor operating in weak inversion mode completes the transfer function. If the input variable is a current instead of a voltage, the MOS transistor can be replaced by a current squarer circuit [6].

In our approach, the circuit performs one half of the function. Since the Gaussian is an even function, the other half side can be easily

Manuscript received September 19, 1994; revised June 12, 1995. This work was supported in part by the EC Esprit Project ELENA-Nerves 2 (6891). This paper was recommended by Associate Editor M. Steyaert.

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Publisher Item Identifier S 1057-7130(96)00879-8.

implemented by rectifying the input variable [3] (or, in the case of using a current squarer this is directly done).

Sections II and III present the exponential circuit principle and the Gaussian circuit. The two next sections consider the modification of the  $\sigma$  parameter and mismatch effects, which lead to design constraints. In Sections VI and VII the design and experimental results are reported. Section VIII discusses the operation in strong inversion. Finally the conclusion of this brief is presented.

#### II. PRINCIPLE OF THE EXPONENTIAL CIRCUIT

The principle of the exponential circuit is shown in Fig. 1(a).  $V_{\rm SX}$ ,  $V_{\rm DX}$ , and  $V_{\rm GX}$  are, respectively, the source, drain and gate voltages of transistor  $M_X$ . In this circuit the two MOS transistors form a current mirror, with resistors  $R_1$  and  $R_2$  serially connected to the transistor sources. If the two resistors  $R_1$  and  $R_2$  are identical, currents  $I_o$  and  $I_R$  will also be identical at the equilibrium, when there is no current  $I_1$ . When a current  $I_1$  is sourced to the cell, voltages  $V_{\rm S1}$  and  $V_{\rm S2}$  differ, and the circuit behaves as a Widlar or logarithmic current mirror [7].

Reference current  $I_R$  is set small enough to make transistors  $M_1$  and  $M_2$  working in weak inversion. Under this condition, we can express the currents in  $M_1$  and  $M_2$  as [8]

$$I_{R} = I_{s} e^{\frac{V_{G1}}{nu_{T}}} \left( e^{-\frac{V_{S1}}{u_{T}}} - e^{-\frac{V_{D1}}{u_{T}}} \right)$$

$$I_{o} = I_{s} e^{\frac{V_{G2}}{nu_{T}}} \left( e^{-\frac{V_{S2}}{u_{T}}} - e^{-\frac{V_{D2}}{u_{T}}} \right)$$
(2)

where  $u_T = KT/q$ , n is the slope factor (slightly higher than unity), and  $I_s$  is the specific current, related to technology parameters.  $V_{D1}$  and  $V_{D2}$  are much higher than  $u_T$  at the operating point of the transistors; since we have also  $V_{G2} = V_{G1}$ , we obtain.

$$I_R \cong I_s e^{\frac{V_{G1}}{nu_T}} e^{-\frac{V_{S1}}{u_T}}, \quad I_o \cong I_s e^{\frac{V_{G1}}{nu_T}} e^{-\frac{V_{S2}}{u_T}}.$$
 (3)

Substituting  $V_{S1}$  and  $V_{S2}$  leads then to

$$I_o = I_R e^{\left(\frac{R_1 I_R - R_2 I_o - R_2 I_1}{u_T}\right)}. (4)$$

Finally, assuming that  $I_1$  is greater than  $I_R$  (and thus  $I_o$  lower than  $I_R$ ), which can be easily guaranteed since  $I_R$  is small as stated before,

$$I_o \cong I_R e^{-\frac{R_2 I_1}{u_T}} = I_R e^{-\frac{V_{S2}}{u_T}}.$$
 (5)

The output current  $I_o$  decreases exponentially with current  $I_1$ , which linearly modifies  $V_{S2} \cdot R_2$  determines the exponential constant. In order to have a good control on the output current,  $R_1$  is set equal to  $R_2$  in further analysis, and thus  $I_o = I_R$  for  $I_1 = 0$ . Furthermore, by taking  $R_1 = R_2$  (5) holds not only for  $I_1 \gg I_R$ , but also for values of  $I_1$  in the order of  $I_R$  (since  $R_1I_R - R_2I_o$  approaches 0).

Notice that the circuit has a current input instead of the usual voltage input. This allows a higher flexibility for input current summing, and also, the biasing of the circuit is straightforward done by the reference current.

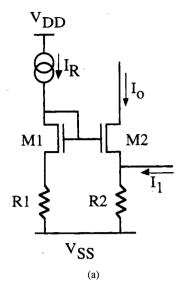
### III. THE GAUSSIAN CIRCUIT

The complete circuit is shown in Fig. 1(b)  $M_3$  and  $M_4$  work in their linear region and are used in strong inversion as variable resistors. In this region, the drain current can be expressed by

$$I_D = \beta (V_D - V_S) \left[ V_C - V_{TN} - \frac{n}{2} (V_D - V_S) \right].$$
 (6)

The gate voltage  $V_C$  controls the output conductance of  $M_3$  and  $M_4$ , whose value is approximately given by (since  $V_{S3}=V_{S4}=0$ )

$$g_{\text{ds3,4}} = \frac{\partial I_{D3,4}}{\partial V_{D3,4}} \cong \beta_{3,4} (V_C - V_{\text{TN3,4}})$$
 (7)



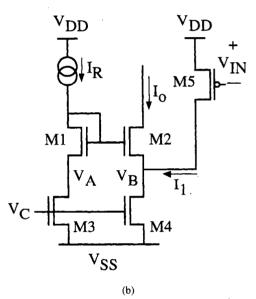


Fig. 1. (a) Principle of the exponential circuit. (b) The Gaussian circuit.

where we assume that  $V_{D3}, V_{D4}$  are small for the linear operation

$$V_C - V_{\rm TN} \gg V_{D3}, V_{D4}.$$
 (8)

This condition guarantees the operation far from the saturation region.  $M_5$  works in saturated region and in strong inversion. Its drain current is thus a square function of the gate voltage

$$I_1 = \frac{\beta_5}{2n} (V_{\rm IN} - |V_{\rm TP}|)^2 \tag{9}$$

where  $V_{\rm IN}$  is the gate voltage of  $M_5$  referred to  $V_{\rm DD}$  [Fig. 1(b)]. Combining (5) and (9), the global transfer function of the cell is then

$$I_o = I_R e^{-\frac{I_1}{u_T g_{ds4}}} = I_R e^{-\frac{\beta_5 (V_{in} - |V_{TP}|)^2}{2n u_T \beta_4 (V_C - V_{TN})}}$$
(10)

which has the desired Gaussian form given in (1), provided  $x = V_{\rm in} - |V_{\rm TP}|$ . The constant  $V_{\rm TP}$  can be compensated (if necessary) by an offset voltage generated with a diode-connected MOS transistor biased by a small current, and connected to  $M_5$  gate.

#### IV. MODIFICATION OF $\sigma$

The value of  $\sigma$  in (1) is controlled by  $V_C$  in the circuit, but it could be controlled by a multiplying factor of the input signal as well. If it is to be controlled internally, its limits of variation can be calculated.

The lower limit of  $I_o$  (Fig. 1) for a maximum input current  $I_1$  sets an upper limit for  $V_{S2}$  which in turn determines a minimum value for  $V_C$ , (8) having to apply for the whole dynamics of the output current. The upper bound of  $I_o$  is obviously  $I_R$ , when  $I_1=0$ . Let us assume an equivalent 8-b precision over the output current. The upper bound of  $V_{S2}$  may be calculated by

$$I_{o \min} = \frac{I_R}{2^8} = I_R e^{-\frac{V_{S2 \max}}{u_T}} \Rightarrow V_{S2 \max} = u_T \ln(256).$$
 (11)

We obtain, for  $u_T=26$  mV,  $V_{S2\,\mathrm{max}}=144$  mV, which is the voltage drop that  $I_1$  has to generate in order to decrease  $I_o$  to its minimum value  $I_{o\,\mathrm{min}}$ . Neglecting the voltage drop produced by the small  $I_R$ , 250 mV can be taken as a practical lower limit for  $V_{C\,\mathrm{min}}-V_{\mathrm{TN}}$  to satisfy (8). Using  $V_C$  to control  $\sigma$  in (1), the maximum variation of conductances  $g_{\mathrm{ds3},4}$  is

$$\beta(V_{\rm DD} - V_{\rm TN}) \ge g_{\rm ds} \ge (V_{C \min} - V_{\rm TN}). \tag{12}$$

The maximum swing of  $\sigma$  is thus given by

$$\frac{\sigma_{\text{max}}}{\sigma_{\text{min}}} = \sqrt{\frac{g_{\text{ds max}}}{g_{\text{ds min}}}} = \sqrt{\frac{V_{\text{DD}} - V_{\text{TN}}}{V_{\text{C min}} - V_{\text{TN}}}}$$
(13)

which leads to a factor 4 for a 5 V supply and typical threshold voltages.

### V. LIMITATIONS OF MISMATCH

Since the circuit is based on the symmetry of a current mirror, performance is limited by mismatches in the  $M_1-M_2$  and  $M_3-M_4$  pairs. Slight differences in  $\beta$  and  $V_{\rm TN}$  of the pairs are considered to analyze the effects in circuit operation.

Taking into account these mismatches, the following output current expression for the current mirror at equilibrium  $(I_1=0)$  can be obtained

$$I_o = I_R(1 + \varepsilon_\beta) e^{\frac{\Delta V_{\rm TN}}{n u_T}} e^{\frac{\Delta V_S}{u_T}}$$
(14)

where  $\varepsilon_{\beta}$  is the relative error of  $\beta$  in pair  $M_1-M_2$ ,  $\Delta V_{\rm TN}=V_{\rm TN1}-V_{\rm TN2}$ , and  $\Delta V_S$  is the error produced by the  $M_3-M_4$  mismatches

$$\Delta V_S = V_{S1} - V_{S2} = \frac{I_R}{g_{ds3}} - \frac{I_o}{g_{ds4}}.$$
 (15)

If there is no mismatch, the output current is equal to the reference current,  $I_o = I_R$ .

Let us first consider the variation of the output current Io produced by mismatches of pair  $M_1-M_2$ . As expressed by (14),  $I_o$  depends exponentially with  $\Delta V_{\rm TN}$ , and linearly with  $\varepsilon \beta$ , which suggests that mismatch in  $V_{\rm TN}$  is more critical than mismatch in  $\beta$ .

In Fig. 2, output current relative error  $(I_o-I_R)/I_R$  is shown as a function of  $\Delta V_{\rm TN}$  and  $\varepsilon_\beta$ . As a numerical example [9], for a typical process and a NMOS transistor of  $W=L=20~\mu{\rm m}$  we obtain  $\Delta V_{\rm TN}=1.5~{\rm mV}$  and  $\varepsilon_\beta=0.12\%$ . These values are displayed in the figure as a circle and a cross. As expected, the dominant error is produced by  $\Delta V_{\rm TN}$ . This explains that  $\Delta V_{\rm TN}$  is the principal agent of mismatch in current mirrors working at weak inversion [6]. In our circuit, the resistance of pair  $M_3-M_4$  reduces the error because of the negative feedback that  $\Delta V_S$  introduces in (14). However, since resistance values are small, this reduction has almost no significance.

Even though mismatches cannot be eliminated, they can be kept small enough by means of an accurate technology and suitable layout techniques. Large transistors and proper layout design can reduce the

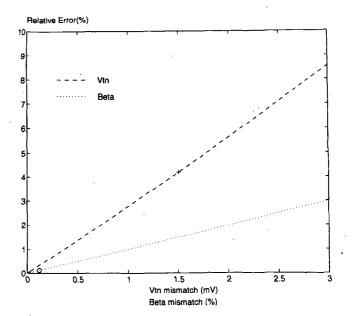


Fig. 2. Relative output current error as a function of  $\beta$  and  $V_{\rm TN}$  mismatch of pair  $M_1-M_2$ .

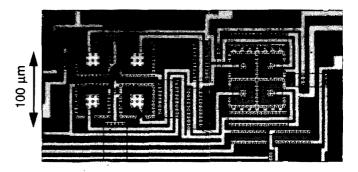


Fig. 3. Photograph of the circuit.

TABLE I TRANSISTOR SIZES IN A 3- $\mu$ m SOI TECHNOLOGY

Transistor	W/L (μm/μm)				
$M_1, M_2$	240/8				
M <sub>3</sub> , M <sub>4</sub>	90/6				
M <sub>5</sub>	60/8				

error to a small percent, since the mismatch mainly depends on  $\frac{1}{\sqrt{WL}}$  [9], [10].

Another error source is mismatch in pair  $M_3-M_4$ , that produces different output currents for  $I_1=0$  when  $g_{\mathrm{ds3,4}}$  are different as (15) shows. However this error is made negligible in front of the other error sources by design. The way to minimize the effect of  $\Delta V_S$  is to make the value of  $V_S$  small. Keeping  $g_{\mathrm{ds3}}$  and  $g_{\mathrm{ds4}}$  high,  $V_{\mathrm{S1}}$  and  $V_{\mathrm{S2}}$  will be small for  $I_1=0$ , and consequently  $\Delta V_S$ . But  $g_{\mathrm{ds3}}$  and  $g_{\mathrm{ds4}}$  cannot be arbitrarily large because this leads to a high  $I_1$  current to achieve at least a drop of 250 mV in  $V_{\mathrm{S2}}$  for all the range of values of  $g_{\mathrm{ds4}}$  that  $V_C$  can produce. To reduce the error under 1%,

$$e^{\frac{\Delta V_S}{u_T}} < 1.01 \Rightarrow \Delta V_S \le 0.26 \text{ mV}$$
 (16)

and considering a mismatch of 5% between  $g_{ds3}$  and  $g_{ds4}$ ,  $V_{S1,2} \le$ 

$I_{\mathbf{R}}(\mu \mathbf{A})$	1				100				
$V_{c}(V)$	5	4.05	3.10	2.15	1.20	5	4	3	2
Er(%)	0.19	0.18	0.21	0.36	1.05	1.64	1.64	1.88	1.96

TABLE II Relative Error to Gaussian Shape for the Range of  $V_C$  at  $I_R=1~\mu{\rm A},~100~\mu{\rm A}$ 

5.2 mV. Notice that this small value is in accordance with assumptions in Section III. For  $I_R=1~\mu A$ , we have  $g_{\rm ds3,4}\geq 1.9\cdot 10^{-4}\Omega^{-1}$ . A  $I_1$  high enough to produce a 250 mV drop in  $g_{\rm ds4}$  is needed for all the margin of values of  $g_{\rm ds4}$  (when  $V_C$  is used to control  $\sigma$ ). For  $\frac{g_{\rm ds\,max}}{g_{\rm ds\,max}}=16$ ,  $I_{1\,\rm min}=250~{\rm mV}\cdot g_{\rm ds\,max}\cong760~\mu A$ , the current that the squarer circuit has to be able to supply to the exponential circuit. Of course, if  $\sigma$  is not to be modified, a current  $I_{1\,\rm min}\cong47.5~\mu A$  is enough.

#### VI. DESIGN AND LAYOUT CONSIDERATIONS

Because of the importance of matching and the  $\sigma$  the good matching characteristics that the Silicon-On-Insulator (SOI) MOS technology promises [11], the proposed circuit has been designed and fabricated in a 3- $\mu$ m SOI technology. Table I shows the dimensions of transistors in this technology.

The test circuit was designed to work in weak inversion for  $I_R=1$   $\mu A$ . At  $V_{\rm IN}=3$  V output current is to be zero for any selected  $\sigma$  value.

The pairs  $M_1$ ,  $M_2$  and  $M_3$ ,  $M_4$  have been designed with a common centroid geometry to reduce mismatching [12]. Also, the edgeless design (ring-shaped transistors) avoids the bird's beak effect that could produce undesirable influence on the transistors in weak inversion. Large dimensions of the transistors are needed to achieve the reference current of 1  $\mu$ A in weak inversion, to reduce mismatches, and to build edgeless transistors.

The size of the circuit is about  $0.07~\mathrm{mm}^2$  in a single-metal single-poly technology. For a double metal technology it could be easily reduced. Care has been taken to keep overall symmetry and also to avoid contacts or polysilicon wires in series with  $M_3, M_4$ , since parasitic resistances could modify the circuit behavior. Access to all the points of the circuit has been provided for this test cell, that is not necessary for normal operation.

# VII. EXPERIMENTAL RESULTS

The chip has been manufactured and tested. The layout photograph of the measured cell is shown in Fig. 3.

The measured threshold voltage of the NMOS transistors is 0.87 V. It has been experimentally determined that  $V_C$  can be varied from 5 to 1.2 V, for reasonable good Gaussian forms. It is approximately at  $V_C=1.2$  V when transistor M4 starts to leave the linear region and enter saturation. Then, condition (8) is not accomplished anymore. The ratio  $\frac{\sigma_{\rm max}}{\sigma_{\rm min}}$  is thus 3.5. Measured conductances range from a value of  $g_{\rm ds4}=3.58$  mA/V for  $V_C=5$  V to 1 mA/V for  $V_C=2$  V.

The output current relative error is about 2%, which indicates a good mirror matching. Measures have been done at  $I_R=1~\mu A$ . The inversion coefficient (IC =  $I_D/2n\beta u_T^2$ , that indicates the border between weak and strong inversion), is 0.46, a value between the weak and moderate inversion regions as desired in order to maximize current while still being in weak inversion. Curves of less than 0.2% of relative error to a Gaussian shape have been obtained. This error is obtained calculating the mean square error between the experimentally measured points and that corresponding to a pure Gaussian curve, and then dividing by the current dynamics, namely

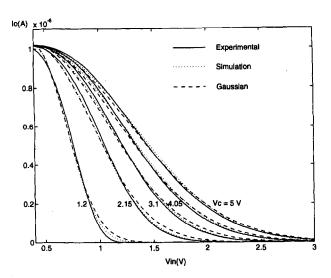


Fig. 4. Output current for  $I_R=1~\mu\mathrm{A}$  and  $V_C=1.2,~2.15,~3.10,~4.05,$  and 5 V.

the reference current. Table II shows the errors for different  $V_C$  values.

Fig. 4 depicts the experimentally obtained curves compared to half Gaussian functions. The curves have also been compared with simulated Cseverny-Oguey continuous model for weak/strong inversion [13] and fit very well. The effective threshold voltage of the PMOS transistor is 0.4 V and the maximum of  $I_o$  is 1.02  $\mu$ A. This error of 2% is a very low value for a mirror in weak inversion, as discussed in Section V. The different maximum value of the output current for  $V_C=1.2$  V is produced also by mismatches, that have worse effects for the smaller  $g_{\rm ds}$ .

To characterize the speed performance of this nonlinear circuit, the settling time (10 to 90% of the output current for a small-signal step function) has been measured. Simulations show  $t_{\rm ss}=0.1~\mu \rm s$ . The measured settling time is  $t_{\rm sm}=1.0~\mu \rm s$ . The difference can be found mainly because of the pad capacitance, since there is no current buffer provided in the prototype cell.

These experimental results are referred to measurements on three samples of the same process, leading to close results. While the output current relative error is random, due to mismatch, the shape error is systematic, probably due to the difference of the exponential and square models of the transistors. Because of this, measurements in other batches would be of interest in order to characterize precisely random errors.

# VIII. STRONG INVERSION OPERATION

The circuit has also been tested in strong inversion operation ( $I_R=100~\mu\mathrm{A}$ ), which has the advantage of faster operation, at the price of some shape degradation as Table II shows.  $V_c$  is restricted to a lower bound of 2 V.

The analytical expression for the output current as a function of  $I_1$  of the exponential circuit in strong inversion results

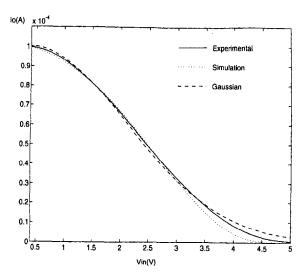


Fig. 5. Output current for strong inversion operation.

$$I_{o} = g_{ds4}(V_{G2} - V_{TN2}) - I_{1} + \frac{g_{ds4}^{2}}{\beta} \times \left[ 1 - \sqrt{1 + \frac{2\beta}{g_{ds4}} \left( V_{G2} - V_{TN2} - \frac{I_{1}}{g_{ds4}} \right)} \right].$$
(17)

Substitution of  $I_1$  in (9) results in the transfer function of the Gaussian circuit. Even though the analytical function is not Gaussian, it is a  $\sigma$  the od approximation, as Fig. 5 shows, where the simulated, experimental and half Gaussian curves are plotted for  $I_R=100~\mu\mathrm{A}$  and  $V_c=5~\mathrm{V}$ . Now the input voltage swing has to go to 5 V in order to decrease to zero the output current, since  $\frac{g_{m3}}{I_R}$  is smaller for strong inversion (and thus the decreasing slope of the exponential is smaller too). Simulated and measured settling times are  $t_{ss}=20~\mathrm{and}$   $t_{sm}=200~\mathrm{ns}$ , respectively.

#### IX. CONCLUSION

A simple 5-transistor circuit that implements a Gaussian function has been proposed. The input voltage is squared and converted to current, and a current mirror in weak inversion then performs the negative exponential function. Adding an offset to  $V_{\rm IN}$  alloud to shift the Gaussian center. The input voltage may be easily substituted by an input current through the use of a squarer circuit.

One limitation of the circuit is the mismatch of the transistors in weak inversion. Because of this, design constraints have to be taken into account and a careful layout design is to be done.

A test circuit has been fabricated and tested in a 3  $\mu$ m SOI CMOS technology. The experimental results show a very good approximation of true Gaussian functions. At a cost of some shape accuracy (systematic errors), the circuit can work also in the strong inversion mode, with the associated speed benefits. Furthermore, random errors due to mismatch are also reduced in strong inversion. The proposed circuit can be readily integrated as an analog Gaussian transfer function circuit in a neural classifier IC or other applications.

#### ACKNOWLEDGMENT

The authors would like to acknowledge B. Gentinne and D. Flandre for fruitful discussions on transistor characterization and fabrication.

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