A COMPARATIVE STUDY OF SINGLE-SWITCH, THREE-PHASE, HIGH-POWER-FACTOR RECTIFIERS

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Abstract - Three three-phase, single-switch, high-powerfactor rectifier implementations were evaluated on a comparative basis. Specifically, the discontinuousconduction-mode boost rectifier with a 5th-harmonic-trap filter, the discontinuous-conduction-mode boost rectifier with a harmonic-injection circuit, and the multi-resonant, zero-current-switching buck rectifier were compared with respect to their efficiencies, compliance with the IEC555-2 specifications, volumes, weights, and costs. comparisons were done for the three-phase, line-to-line input voltage of 380 $V_{rms} \pm 20\%$ and for 0 - 6 kW outputpower range.

I. Introduction

Low-harmonic, high-power-factor (HPF) rectification in three-phase power systems can be implemented with a large number of topologies and control strategies [1]. Based on the number of controllable switches, HPF rectifiers can be classified as multi- or single-switch rectifiers. Generally, the rectification performance of the multi-switch rectifiers is superior to that of the single-switch rectifiers since the multiple-switch rectifiers can achieve higher power factors and lower harmonic distortions of the line currents. Specifically, six-switch rectifiers have been extensively used in a variety of HPF applications [1].

While the use of multi-switch rectifiers is quite justified in high-power, high-performance applications, the increased number of switches and the complexity of their control make multi-switch rectifiers too expensive in lower power, cost-sensitive applications. For example, today's HPF telecommunication rectifiers, which only need to reduce the total harmonic distortion (THD) of the line current to below 10-15%, are exclusively implemented either with passive LC filters or active, single-switch rectifiers.

So far, several three-phase, HPF rectifiers employing a single switch have been introduced [2]-[4]. Since these rectifiers have a single active switch and perform HPF rectification naturally without a need for a complex control circuitry, they are very suitable for the low-cost, low-power, three-phase ac-dc applications.

In this paper, three single-switch HPF rectifiers were studied and evaluated on a comparative basis. The comparisons were done with respect to their efficiencies, compliance with the IEC555-2 specifications, volumes, weights, and costs. The rectifiers were designed for the three-phase, line-to-line input voltage of 380 $V_{rms} \pm 20\%$ and for 0 - 6 kW output-power range. The three topologies compared in this paper are:

- the single-switch, three-phase, discontinuous-conduction-mode (DCM) boost rectifier with a 5th-harmonic-trap filter;
- the single-switch, three-phase, DCM boost rectifier with a harmonic-injection circuit; and
- the single-switch, three-phase, multi-resonant, zero-currentswitching (ZCS) buck rectifier.

II. Single-Switch, Three-Phase, DCM Boost Rectifier

The circuit diagram of the power stage of the single-switch, three-phase, PWM, DCM boost rectifier is shown in Fig. 1(a). Since the boost rectifier in Fig. 1(a) is operated in DCM with a constant frequency and constant duty cycle, all three-phase input currents, ia, ib, and ic, are zero at the end of a switching period, immediately before boost switch S is turned on. After switch S is turned on, ia, ib, and ic increase linearly to the peak values, which are proportional to the lineto-neutral voltages as shown in Fig. 1(b). Therefore, during the switch-on period, each line current forms a triangular pulse with the peak value proportional to the associated lineto-neutral voltage. As a result, during the switch-on period, the average line currents are proportional to the line-toneutral voltages. When the switch is turned off, the input currents start decreasing because output voltage V_O is higher than the peak of the input voltage. In DCM, the input currents reach zero before the end of the switching period. Since the rate of the input-current decrease is proportional to the difference between output voltage Vo and line-to-neutral voltage, the average line currents during the off period of the switch are not proportional to the line voltages, i.e., even if the line voltages are perfectly balanced and sinusoidal, the line currents are distorted. Figure 2 shows the normalized harmonic content of the rectifier input current as a function of the voltage-conversion ratio M, which is defined as

$$M = \frac{V_o}{\sqrt{3}V_m} \tag{1}$$

where V_O is the rectifier output voltage and V_m is the peak line-to-neutral voltage. As can be seen from Fig. 2, the

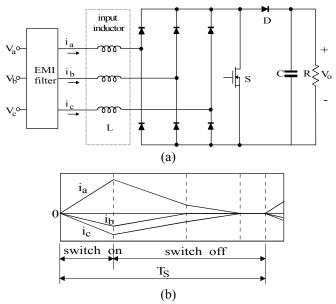


Fig. 1 Single-switch, three-phase DCM boost rectifier: (a) circuit diagram; (b) input current waveforms during switching cycle.

rectifier input-current spectrum, which contains only odd harmonics, is dominated by the 5^{th} -order harmonic, *i.e.*, the lowest order harmonic. For example, at M = 1.2, the 5^{th} -order harmonic is 8 times larger than the 7^{th} -order harmonic, which is the next largest. Also, it should be noted that the value of the normalized 5^{th} -order harmonic monotonically decreases as the value of M increases. In fact, it decreases from slightly over 30% of the fundamental component at M = 1.1 to approximately 7% at M = 2.

Generally, the maximum input power at which the threephase, constant-frequency, DCM boost rectifier can meet the IEC555-2 specifications is limited by the 5th-order harmonic of the input current. As an illustration, Fig. 3 shows the 5th,

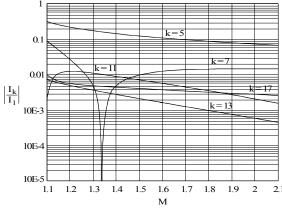


Fig. 2 Normalized input-current harmonics of the singleswitch, three-phase, constant-frequency, constantduty-cycle, DCM boost rectifier. Harmonics are normalized with respect to the fundamental component.

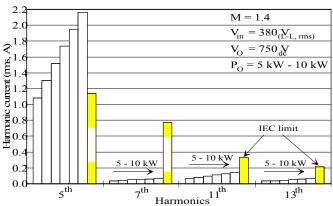


Fig. 3 Comparison between the input-current harmonic content of the single-switch, three-phase, constant-frequency, constant-duty-cycle, DCM boost rectifier and harmonic-current limits of the IEC555-2 for M = 1.4, $V_O = 750 \text{ V}$, $V_{in(L-L)} = 380 \text{ V}_{rms}$, $P_{in} = 5 \text{ kW} - 10 \text{ kW}$

 $7^{\rm th}$, $11^{\rm th}$, and $13^{\rm th}$ harmonics of the DCM boost rectifier with M = 1.4 and input power levels from 5 kW to 10 kW along with the corresponding IEC555-2 limits. As can be seen from Fig. 3, for M = 1.4 the rectifier can meet the IEC555-2 requirements only for power levels up to 5 kW because of the $5^{\rm th}$ -harmonic limitation. The higher-order harmonics, *i.e.*, $7^{\rm th}$, $11^{\rm th}$, $13^{\rm th}$, etc., are well below the IEC555-2 limits, even for power levels over $10 \, \rm kW$.

To meet the IEC555-2 specifications at power levels above 5 kW, the three-phase, constant-frequency, constant-duty-cycle DCM boost rectifier needs to be designed with a higher M. However, it should be noted that for a given power line voltage, larger M requires a boost switch with a higher voltage rating, which has a detrimental effect on the conversion efficiency and cost. Nevertheless, the IEC555-2 limits can be met with a relatively low value of M if either a passive 5th-order harmonic-trap filter is used, or the duty-cycle of the switch is modulated by a harmonic-injection signal to attenuate the 5th-order harmonic.

III. DCM Boost Rectifier with 5th-Order Harmonic Trap

To reduce the magnitude of the 5^{th} harmonic in the input current, the 5^{th} -order harmonic-trap filter, which consists of inductances L_{T1} and L_{T2} and capacitance C_{T2} , needs to be added at the input of the power stage, as shown in Fig. 4. If the resonant frequency of the series resonant tank L_{T2} - C_{T2} is selected at the frequency of the 5^{th} harmonic of the line, the 5^{th} harmonic of the rectifier current will be mainly flowing through the L_{T2} - C_{T2} branches of the filter and not through the source. The harmonic-trap inductance L_{T1} can also be utilized as a part of the differential-mode input filter formed by the addition of filter capacitor C_{T1} .

Figure 5 shows the harmonic-trap filter and its magnitude frequency response. This filter has a passband between dc and

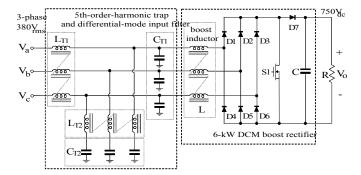


Fig. 4 Single-switch, three-phase DCM boost rectifier with 5th-harmonic trap.

cut-off frequency f_c and provides a steep rate of attenuation from f_c to notch frequency f_{∞} . The characteristics of the filter in Fig. 5 are completely described by the following design equations [5]:

$$\begin{split} m &= \sqrt{1 - \frac{f_c^2}{f_\infty^2}} \;, \;\; L_{T1} = m L_k \;, \;\; L_{T2} = \frac{1 - m^2}{m} L_k \;, \\ C_{T2} &= m C_k \;, \;\; f_c = \frac{1}{2\pi \sqrt{L_k C_k}} \;, \text{ and } \;\; f_\infty = \frac{1}{2\pi \sqrt{L_{T2} C_{T2}}} \;. \end{split}$$

The ratio m represents the slope of the magnitude characteristic from f_c to f_∞ . If the value of m is unity, then L_{T2} becomes zero, and L_{T1} and C_{T2} are equal to L_k and C_k respectively. Therefore, this circuit becomes a simple L-C lowpass filter where L_k and C_k are the filter elements which define the cut-off frequency f_c . As m in the filter in Fig. 5 decreases, the filter attenuation rate increases. The filter has the flattest impedance over the greatest part of the passband when m is designed as approximately 0.6. However, the value of m should be selected so that it results in a good compromise between the attenuation performance and volume and cost.

One problem in using a harmonic trap in a harmonic generating power system (e.g., DCM boost rectifier) is the possibility to excite harmonic resonances [6]. Both series and parallel resonances may occur in a power system due to the existence of the filter and power line reactive components. To further explain these resonances, Fig. 6 shows the equivalent harmonic circuit for a power system that consists of the rectifier bridge and the harmonic trap. In Fig. 6, the DCM boost rectifier is modeled as a harmonic current source. The

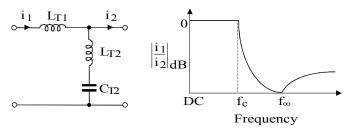


Fig. 5 Harmonic-trap circuit and its frequency response.

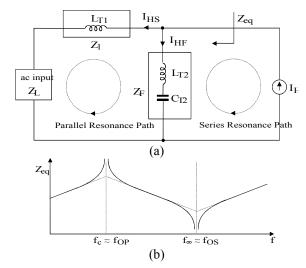


Fig. 6 Harmonic resonances of harmonic-trap filter: (a) equivalent circuit of DCM boost rectifier with harmonic-trap circuit. (b) magnitude vs. frequency plot of output impedance of the filter.

impedances Z_F and Z_I , and Z_L are the filter impedances and the line impedance, respectively. The harmonic current flowing through the trap filter is

$$I_{HF} = I_{H} \frac{Z_{1} + Z_{L}}{Z_{1} + Z_{L} + Z_{F}} = I_{H} \frac{Z_{S}}{Z_{S} + Z_{F}},$$
 (2)

while the harmonic current flowing through the source is

$$I_{HS} = I_H \frac{Z_F}{Z_1 + Z_L + Z_F} = I_S \frac{Z_F}{Z_S + Z_F},$$
 (3)

where $Z_S=Z_1+Z_L$

Since at series resonant frequency $f_{OS}\!\!=\!\!f_{\infty}$, $|Z_F|<<|Z_S|$, most of the harmonic current flows through the harmonic trap impedance Z_F . However, at parallel resonant frequency f_{OP} , $|Z_F|=|Z_S|$, and a high circulating current flows in the loop consisting of the trap filter and the ac source. Therefore, to avoid this problem, the cut-off frequency of the trap filter should always be below the 5^{th} -harmonic line frequency, including possible frequency variations.

For 60 Hz line frequency, the 5th-harmonic trap filter should have a notch frequency f_{∞} of 300 Hz. To ensure that the cut-off frequency of the filter is safely below 300 Hz, cut-off frequency f_c should be selected to be f_{∞} - 10%, or approximately 275 Hz. With this selection of the filter, the parameters and the components values of the filter are m = 0.36, L_k = 5.9 mH, C_k = 55 uF, L_{T1} = 2.2 mH, L_{T2} = 14.1 mH, and C_{T2} = 20 uF.

IV. DCM Boost Rectifier with Harmonic-Injection Circuit

The harmonic-injection approach does not increase the voltage stress of the boost switch and requires only a few additional components for its implementation [7] - [10]. In the technique presented in [10], a voltage signal which is

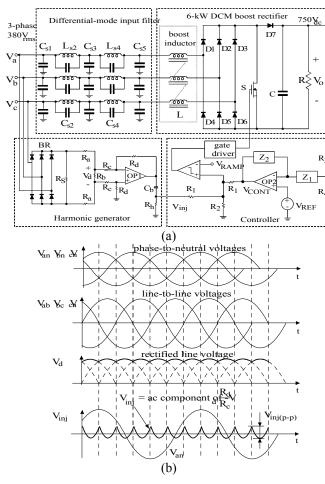


Fig. 7 Single-switch, three-phase DCM boost rectifier with harmonic injection circuit: (a) circuit diagram; (b) key voltage waveforms.

proportional to the inverted ac component of the rectified, three-phase, line-to-line input voltage is injected into the output-voltage feedback loop to vary the duty cycle of the rectifier within a line cycle in order to reduce the 5th-order harmonic and improve the THD of the rectifier input currents.

The simplest implementation of the harmonic injection circuit and its key waveforms are shown in Fig. 7 [10]. In the implementation in Fig. 7(a), the three-phase line voltage is first rectified by three-phase bridge rectifier BR, and then attenuated by the resistive voltage divider R_a - R_b . The scaled-down line voltage developed across R_b , V_d , is then inverted by difference amplifier OP1 before it is processed through the high-pass filter C_b - R_h to remove the dc component of V_d and generate injection signal V_{inj} . Finally, V_{inj} is injected in the control circuit at the noninverting input of the PWM comparator through summing resistor R_1 .

When signal $V_{\rm inj}$, shown in Fig. 7(b), is injected at the PWM modulator, it modifies the duty cycle so that the 5th-order harmonic of the input current is reduced and the THD is improved. In fact, since the variation of duty cycle d(t) is

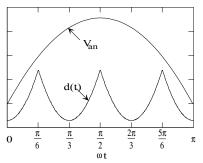


Fig. 8 Duty-cycle variations during half of fundamental line period.

directly proportional to signal V_{inj} , the modulation of the duty ratio during a line cycle can be described as

$$D_{MOD}(t) = D[1 + d(t)],$$
 (4)

where D_{MOD} is the modulated duty cycle, D is the duty cycle in the absence of the modulation, and d(t) is the duty cycle modulation. Since d(t) is proportional to the inverted ac component of the rectified three-phase line-to-line input voltage, the variation of duty cycle d(t) during half of the fundamental line period can be plotted along with the line-to-neutral input voltage, as shown in Fig. 8.

The periodic function d(t) in Fig. 8 can be expressed in terms of the Fourier series representation as

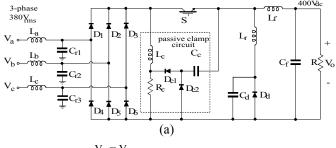
$$d(t) = \frac{m}{\pi} \int_{n=1}^{\infty} \frac{(-1)^n 6}{(6n)^2 - 1} \cos(6n\omega t).$$
 (5)

From Eq. (5), it can be seen that the generated injection signal contains not only the 6th-order harmonic but also higher-order harmonics such as 12th, 18th, etc. As shown in [10], these higher-order harmonics help to improve the THD more than if only the 6th-order harmonic is injected.

At any given voltage-conversion ratio M, the optimal modulation index m which produces the minimum THD can be determined. To maximize the input power of the rectifier at which the IEC555-2 specifications are met, modulation index m should be determined so that the ratio of the 7th-order harmonic and the 5th-order harmonic is equal to corresponding IEC555-2 limits [10].

V. Single-Switch, Three-Phase, Multi-Resonant, ZCS Buck Rectifier

Figure 9 shows the three-phase, multi-resonant, ZCS buck rectifier and the voltage waveform across input-side resonant capacitor C_{r1} . Since input-filter inductors L_a , L_b , L_c , and output-filter inductor L_f are relatively large, they have small switching-frequency current ripples. In a steady state, the average voltages of C_{r1} - C_{r3} during a switching period are equal to the associated input voltages. Because the peak voltages of C_{r1} - C_{r3} are proportional to the input currents, and switching frequency f_S is much higher than line frequency f_L , the input-current waveforms follow the input-voltage waveforms. As a result, the circuit possesses a high power factor and a low harmonic content in the input current.



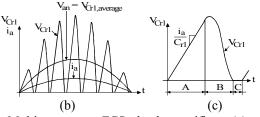


Fig. 9 Multi-resonant, ZCS buck rectifier: (a) circuit diagram, (b) voltage waveform of C_{r1} and input current waveform i_a , and (c) enlarged V_{Cr1} waveform during one switching period.

In the circuit shown in Fig. 9, the amount of input-current distortion depends on the shape of the voltage waveform across C_{rl} , shown in Fig. 9(c). During the first period, when

switch S is off, V_{Cr1} is increasing linearly with a slope proportional to input current i_a . During the second period when switch S is on, resonant capacitor C_{r1} resonates with inductor L_r , until V_{Cr1} reaches zero voltage. Finally, V_{Cr1} remains at zero for the third period, during which switch S is still on. Since V_{Cr1} is proportional to input current i_a only during the off time of switch S, the input-current waveform becomes more proportional to the input-voltage waveform if the first period is longer than the sum of the second and the third periods. Because in the multi-resonant scheme in Fig. 9 the durations of the second and third periods are significantly reduced, the circuit performs the rectification with a low THD.

VI. Evaluation Results

To compare the performance of the three rectifier topologies, the three circuits were built for the three-phase, line-to-line input voltage of 380 $V_{\rm rms}\pm20\%$ and for 0- 6~kW output-power range. The power-stage and input-filter components used in the three experimental prototypes are given in Table 1.

The output voltage of the DCM boost rectifiers with the 5th-order harmonic trap and the harmonic injection was 750 V, whereas the output voltage of the ZCS buck rectifier

Table 1 Components of rectifiers

| Rectifiers | DCM boost rectifier with 5 th -harmonic trap filter | DCM boost rectifier with harmonic-injection circuit | Multi-resonant, ZCS buck rectifier | | | | | | |
|-------------------------------------|--|--|---|--|--|--|--|--|--|
| Power Stage Components | | | | | | | | | |
| Switch S | APT10026 | APT10026 | 2 × IXSH35N140A | | | | | | |
| | (1000 V, 33 A) | (1000 V, 33 A) | (1400 V, 35 A) in Parallel | | | | | | |
| Input Bridge | BYT230PIV-1000 | BYT230PIV-1000 | 2 × DSEI30-10A | | | | | | |
| $\textbf{Diode} \; \textbf{D}_{in}$ | (1000 V, 30 A) | (1000 V, 30 A) | (1000 V, 30 A) in series | | | | | | |
| Output Diode D | DSEI60-10A | DSEI60-10A | 2 × DSEI30-10A | | | | | | |
| | (1000 V, 60 A) | (1000 V, 60 A) | (1000 V, 30 A) in series | | | | | | |
| Boost Inductor | $L = 3 \times 42 \text{ uH}$ | $L = 3 \times 42 \text{ uH}$ | None | | | | | | |
| Input Filter Components | | | | | | | | | |
| Inductors | L_{T1} = 3 × 2.2 mH, L_{T2} = 3 × 14 mH | L_{S2} = 3 × 140 uH, L_{S4} = 3 × 160 uH | L_{a} - L_{c} = 0.9 mH | | | | | | |
| Capacitors | $C_{T1} = 3 \times 1 \text{ uF}$ | $C_{S1} = 3 \times 2.7 \text{ uF}, C_{S2} = 3 \times 47 \text{ nF}$ | None | | | | | | |
| | $C_{T2}=3\times20 \text{ uF}$ | $C_{S3} = 3 \times 6.8 \text{ uF}, C_{S4} = 3 \times 0.1 \text{ uF}$ | | | | | | | |
| | C_{85} = 3 × 5.6 uF | | | | | | | | |
| Output Filter Components | | | | | | | | | |
| Inductors | None | None | $L_f = 0.8 \text{ mH}$ | | | | | | |
| Capacitors | C = 330 uF | C = 330 uF | $C_f = 470 \text{ uF}$ | | | | | | |
| Resonant Components | | | | | | | | | |
| Inductors | None | None | $L_r = 43 \text{ uH}$ | | | | | | |
| Capacitors | None | None | C_{r1} - C_{r3} = 133 nF, C_d = 80 nF | | | | | | |

| Table 2 Comparisons of volumes, weights, and costs of rectifiers | | | | | | | | | | |
|--|-------------------------|--------------------------|---------------------|---------------------|----------------------|-------------------|--------|--|--|--|
| | Inductive Components | Capacitive Components | Control Circuit | Power Stage | Overall Volume | Overall Weight | Cost | | | |
| | 3000 cm^3 | 2000 cm ³ | 1000 cm^3 | 2000 cm^3 | 8000 cm ³ | 10.5 kg | Mediur | | | |

Rectifiers DCM boost rectifier with 5th-harmonic trap filter 1000 cm^3 1000 cm³ 1000 cm^3 2000 cm³ 5000 cm² DCM boost rectifier 5 kg Low with harmonic injection 1000 cm^{-3} Multi-resonant, ZCS 1700 cm^3 1000 cm^3 2300 cm³ 6000 cm^3 6.4 kgHigh

was 400 V. The output voltages of the boost prototype circuits were controlled with a constant-frequency PWM control at 45 kHz. Due to the wide input-voltage and load ranges, the closed-loop control of the buck prototype rectifier was implemented by a combination of a variable- and constant-frequency control. The circuit is controlled by the frequency control for the output power in the range from 6 kW to 600 W. In this power range, the switching frequency of the rectifier varies from 90 kHz at full power to 20 kHz at 10% load. When the output power falls below 600 W at the nominal input voltage, the constant frequency PWM control takes over [11]. Since with a constant-frequency PWM control, the switch operates with "hard" switching, the passive clamp circuit is used to limit the maximum voltage of the switch. Because in the constant-frequency PWM control mode the output power is low, the clamping circuit operates with negligible losses.

buck rectifier

Table 2 summarizes the overall volumes and weights of the three prototypes. In addition, Table 2 also shows the volumes of inductive and capacitive components separately, as well as the volumes of the control circuits and power stages. Similarly, Figs. 10 to 12 show the comparisons between the measured input-current harmonic content of the experimental rectifiers and the IEC555-2 harmonic-current limits at different input voltages. Finally, Fig. 13 presents the measured efficiencies of the experimental prototypes.

As can be seen from the presented experimental data, the 5th-harmonic trap reduces the 5th-order harmonic in the input current so that the rectifier produces THD from 6% to 11%, and achieves 95.8% to 97.6% efficiency at the full load and output voltage $V_0 = 750 V_{dc}$. The THD and all harmonic currents meet the IEC555-2 requirements over the entire input-voltage and output-power ranges. However, as shown in Table 2, the size and, especially, the weight of the circuit with the 5th-harmonic trap is significantly greater than the size and weight of the other topologies. The approximate overall volume and weight are 8000 cm³ and 10.5 kg, respectively.

The DCM boost-rectifier with the harmonic-injection circuit has THD from 7.5% to 12.9% and efficiency from 96.4% to 98% at the full load and for $V_0 = 750 V_{dc}$. The approximate overall volume and weight are 5000 cm³ and 5 kg, respectively.

Finally, the multi-resonant ZCS buck rectifier can achieve the THD less than 5% over the input-voltage and outputpower ranges. Efficiency of the rectifier is about 95% at the full load and for $V_0 = 400 \text{ V}$. The approximate overall volume and weight are 6000 cm³ and 6.4 kg, respectively. Although the multi-resonant, buck-type rectifier exhibits the lowest THD, the stresses on the semiconductor devices, together with their conduction losses, result in its limited efficiency and higher cost.

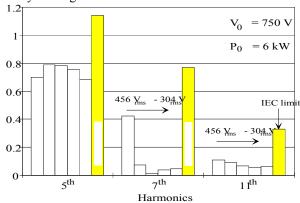


Fig. 10 Comparison of input-current harmonic content of experimental 6-kW DCM boost rectifier with 5thharmonic trap and IEC555-2 harmonic-current limits at different input voltages.

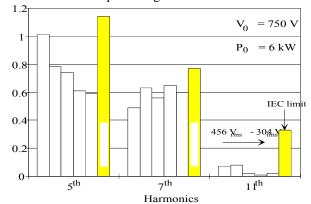


Fig. 11 Comparison of input-current harmonic content of experimental 6-kW DCM boost rectifier with harmonic injection circuit and IEC555-2 harmoniccurrent limits at different input voltages.

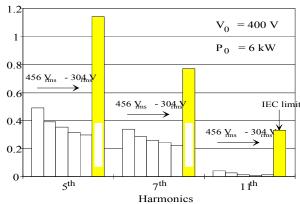


Fig. 12 Comparison of input-current harmonic content of experimental 6-kW multi-resonant, ZCS buck rectifier and IEC555-2 harmonic-current limits at different input voltages.

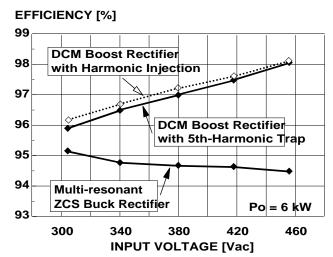


Fig. 13 Measured efficiency of experimental prototypes.

VII. Summary

The performance comparisons of the three-phase, DCM boost rectifiers with the 5th-harmonic trap filter and the harmonic-injection control, and the multi-resonant, zero-current-switching buck rectifier show that the DCM boost rectifier with harmonic-injection control can be implemented to meet the IEC555-2 specification with the smallest size and weight, as well as the highest efficiency. However, if total-harmonic distortion below 5% is required, the single-switch, multi-resonant, ZCS buck rectifier appears to be the only viable approach.

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