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A Comparative Study on Open Circuit Voltage Models for Lithium-ion Batteries

Quan-Qing Yu¹, Rui Xiong^{1*}, Le-Yi Wang² and Cheng Lin¹

Abstract

The current research of state of charge (SoC) online estimation of lithium-ion battery (LiB) in electric vehicles (EVs) mainly focuses on adopting or improving of battery models and estimation filters. However, little attention has been paid to the accuracy of various open circuit voltage (OCV) models for correcting the SoC with aid of the ampere-hour counting method. This paper presents a comprehensive comparison study on eighteen OCV models which cover the majority of models used in literature. The low-current OCV tests are conducted on the typical commercial LiFePO₄/ graphite (LFP) and LiNiMnCoO₂/graphite (NMC) cells to obtain the experimental OCV-SoC curves at different ambient temperature and aging stages. With selected OCV and SoC points from experimental OCV-SoC curves, the parameters of each OCV model are determined by curve fitting toolbox of MATLAB 2013. Then the fitting OCV-SoC curves based on diversified OCV models are also obtained. The indicator of root-mean-square error (RMSE) between the experimental data and fitted data is selected to evaluate the adaptabilities of these OCV models for their main features, advantages, and limitations. The sensitivities of OCV models to ambient temperatures, aging stages, numbers of data points, and SoC regions are studied for both NMC and LFP cells. Furthermore, the influences of these models on SoC estimation are discussed. Through a comprehensive comparison and analysis on OCV models, some recommendations in selecting OCV models for both NMC and LFP cells are given.

Keywords: State of charge, Open circuit voltage model, Lithium-ion battery, NMC, LFP

1 Introduction

Due to the global energy crisis and environmental deterioration, electric vehicles (EVs) have had an unprecedented development opportunity in recent years [1]. A large number of advanced batteries with higher power and energy densities are connected in series or parallels to provide required power and energy for EVs. Therefore, a smart battery management system (BMS) is critical for safe and reliable operations of EVs [2]. One of the basic BMS functions is to monitor and estimate the state of charge (SoC) of lithium ion batteries in real time [3]. Among different approaches for estimating the SoC, the model-based methods have been used extensively for their self-correct ability [4, 5]. The models require an

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accurate open circuit voltage (OCV) representation for correcting SoC calculation [6, 7].

The OCV equals the terminal voltage when there are no polarization effects or voltage drop on the internal impedance. The OCV is related to the battery SoC and this relationship is commonly obtained by offline OCV tests [8, 9]. Due to the hysteresis effects of lithium ion batteries, the average values of the OCV charge curve and OCV discharge curve is defined as the experimental OCV curve [10]. The experimental OCV-SoC curves differ among battery types and vary with ambient temperatures, aging stages, and current rates. Therefore, the OCV model should represent experimental OCVs with high fidelity. So far, a large number of nonlinear functions have been proposed to represent the OCV-SoC relationship. Plett proposed an OCV model which contains a linear function [5], a power function, and a logarithmic function. Polynomial functions were added into the OCV models in Refs. [11–13]. Tong et al. [14] removed the power function from the OCV models. Subsequently,



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several references replaced the logarithmic functions from OCV models by exponential functions [15–17]. Zhang et al. [18] reported an OCV model that contains a linear function, an exponential function, and a logarithmic function. In addition, polynomial functions with different orders are developed to fit OCV data points obtained from offline OCV tests [19–21].

All the reported OCV models have been shown in their original publications to be suitable for SoC estimation under their selected operating conditions. However, there are few studies that provide a comprehensive comparison of these diversified OCV models. Hu et al. [21] compared five OCV models and the 6th order polynomial function was reported to be the most accurate OCV model among them. However, the study is only conducted on LiFePO₄ (LFP) batteries. Its adaptability to other battery types needs to be further investigated. Moreover, sensitivities of these OCV models to ambient temperatures, aging stages, and numbers of data points remain largely an open issue. Only three OCV models were compared by Zhang et al. [18] from the viewpoints of sensitivities to ambient temperatures and aging stages, without exploring the sensitivities to numbers of data points. In addition, an overwhelming majority of these OCV models are proposed based on the experimental data of middle SoC regions between 10% and 90%, and their applicability to the entire SoC region is worth further study.

The key contribution of this paper is using an innovative approach to give a systematic comparison on the practicality of diversified OCV models. First, adaptability of these OCV models to different battery types is investigated. Second, sensitivities to ambient temperatures, aging stages, numbers of data points, and SoC regions are studied. Third, the impacts of these models on SoC estimation are explored. Finally, suggestions about the selection of OCV models are given based on comparison analyses.

The remainder of this paper is organized as follows. In Section 2, the experimental setup, battery specifications, and experimental OCV-SoC curves under different ambient temperatures and aging stages for two types of lithium ion batteries are given. Section 3 introduces eighteen OCV models to be studied and compared. A systematic comparison of diversified OCV models is presented in Section 4, followed by the conclusions in Section 5.

2 Experiments

2.1 Experimental Setup

The battery test bench in Refs. [11, 22] is used to carry out battery tests in this study. Considering the OCV-SoC curves differ among battery types, typical commercial LiFePO₄/graphite (LFP) and LiNiMnCoO₂/graphite (NMC) lithium ion battery cells are selected as the test samples, and their basic specifications are given in Table 1. It's worth noting that both the nominal capacity and actual capacity are measured through capacity test under 25 °C [22]. The capacity losses of the aged NMC and LFP cells are 10.2% and 10.5%, respectively.

2.2 OCV Tests

The low-current OCV tests are performed to obtain the experimental OCV-SoC curves [17]. The fully charged battery cells are discharged at a constant low rate of 0.05 °C until fully discharged. After rest 2 h, the battery cells are then charged at the same current rate until the upper cutoff voltage is reached. Afterwards, the cells will be fully charged with constant current constant voltage (CCCV) method. The voltage at this low current rate reflects the OCV at a close-to-equilibrium status. Due to the OCV is independent of ambient temperatures and aging stages, the OCV tests are performed under three temperatures (i.e., $10 \degree$ C, $25 \degree$ C and $40 \degree$ C) and two aging stages (i.e., fresh and aged battery cells) in this study.

The average OCV-SoC curves between the measures obtained during charge and discharge are illustrated in Figure 1. The OCV-SoC curves of NMC cells shown in Figure 1(a) change dramatically as the SoCs drop to 0% and gradually increase between 10% and 100% SoC regions, but for LFP cells shown in Figure 1(b), the OCV-SoC curves change dramatically as the SoCs drop to 0% and rise to 100%, and there are wide flat OCV plateau in the middle SoC regions. Which indicate the OCV-SoC relationships differ among battery types and its adaptability to different battery types needs to be further investigated. The large OCV errors of NMC cells occur in the middle and low SoC regions, but for LFP cells, the large OCV errors occur in the whole SoC regions, especially in the low and high SoC regions. The large errors may be caused by the rest effects at difference operation conditions. Which confirmed that the OCV-SoC relationship is independent of ambient temperatures and aging stages. In addition, the OCV models may be sensitive to SoC regions and numbers of data points for the different features of experimental OCV-SoC curves.

Table 1 Basic specifications of the battery cells

Cell	Nominal voltage (V)	Nominal capacity (Ah)	Actual capacity (Ah)	Cutoff voltage (V)
NMC (Fresh)	3.7	25	28.40	2.5/4.2
NMC (Aged)	3.7	25	25.51	2.5/4.2
LFP (Fresh)	3.2	20	19.84	2.0/3.65
LFP (Aged)	3.2	20	17.77	2.0/3.65





2.3 UDDS Tests

The urban dynamic driving sequence (UDDS) test is a typical driving test that is often used to evaluate the performance of the SoC estimation [23]. In this paper, the UDDS tests, as shown in Figure 2, are performed to evaluate the impact of OCV models on SoC estimation for both NMC and LFP fresh cells under 25 °C.

3 OCV Model Structures

A total of eighteen OCV models are selected from literature and compared in this study. Which cover the overwhelming majority of OCV models presented in the past studies. These OCV models are summarized in Table 2. Noted that U_{oc} and *s* are battery OCV and SoC, respectively. K_i , α_i , β_i , *m* and *n*, (*i*=0, 1, 2, ..., 12) are the parameters of OCV models, which are determined by MATLAB curve fitting toolbox (Fit Option: Custom Equation; Robust: Bisquare; Algorithm: Trust-Region).

As shown in Table 2, these OCV models generally can be divided into four classes from the perspective of component terms.

- 1. A generalized polynomial function + a logarithmic function + a power function, such as model 1 to 5;
- 2. A generalized polynomial function + an exponential function, such as model 6 to 9;
- 3. A generalized polynomial function + an exponential function + a logarithmic function, such as model 10;
- 4. A generalized polynomial function, such as model 11 to 18.

4 Comparison and Analysis of OCV Models

As shown in Table 2, there are distinct difference in structures of these OCV models. Some models are very simple with fewer numbers of parameters while some models are quite complicated with many parameters. Additionally, some models have limits on the SoC regions. In this section, we will give a comprehensive comparison and analysis on these OCV models, including the adaptabilities to battery types, sensitivities to temperatures, aging stages, SoC regions, numbers of data points, and impacts on SoC estimation. The fitted OCV should be as close to experimental OCV as possible. The fitting performance will be evaluated by the indicator of root-mean-square error (RMSE) between the experimental data and fitted data.

4.1 Sensitivity to SoC Regions

The most of OCV models focus on the middle SoC regions between 10% and 90%, however, it is difficult to obtain accurate SoC initial value in real applications. Hence, if the parameters of OCV models are determined by fitting the experimental data of middle SoC regions (i.e., between 10% and 90%), the OCVs will inaccurate in the low (i.e., 0%–10%) and high SoC (i.e., 90%–100%) regions for their great features at these two regions, which will in turn contributed large SoC errors. Therefore, it is better to model the OCV by fitting the entire SoC region data.

Due to the logarithmic function exists in some OCV models, the entire or whole SoC region is selected from 0.001% to 99.999%. The fitted OCV-SoC curves of different OCV models at 25 °C for both NMC and LFP fresh cells are shown in Figure 3. Note that the SoCs change dramatically when drop to 0% or rise to 100%, the RMSEs are collected the SoC regions between 2.5% and 97.5%.

Table 2 OCV models evaluated in this study

Model	Reference	OCV model expression	
1	[24–26]	$U_{\rm oc} = K_0 + K_1 s + K_2 / s + K_3 \ln(s) + K_4 \ln(1 - s)$	
2	[27, 28]	$U_{oc} = K_0 + K_1 s + K_2 s^2 + K_3 / s + K_4 \ln (s) + K_5 \ln (1 - s)$	
3	[11, 12]	$U_{oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 / s + K_5 \ln(s) + K_6 \ln(1 - s)$	
4	[14]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 \ln(s) + K_5 \ln(1-s)$	
5	[29]	$U_{\rm oc} = K_0 + K_1 \ln(s) + K_2 \ln(1-s)$	
6	[16]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 \exp(K_5 s)$	
7	[15]	$U_{\rm oc} = K_0 + K_1 s + K_2 (1 - \exp(\alpha s)) + K_3 (1 - \exp(\beta (1 - s)^{-1}))$	
8	[17]	$U_{\rm oc} = K_0 s + K_1 (1 + \exp(\alpha_1 (s - \beta_1))^{-1} + K_2 (1 + \exp(\alpha_2 s))^{-1}$	
		+ $K_3(1 + \exp(\alpha_3(s - \beta_2))^{-1} + K_4(1 + \exp(\alpha_4(s - 1))^{-1} + K_5)$	
9	[18, 30]	$U_{\rm oc} = K_0 + K_1 s + K_2 (1 - \ln))^m + K_3 \exp(n(s - 1))$	
10	[14, 31]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2$	
11	[32]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3$	
12	[20]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 s^4$	
13	[33]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 s^4 + K_5 s^5$	
14	[34, 35]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 s^4 + K_5 s^5 + K_6 s^6$	
15	[36, 37]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 s^4 + K_5 s^5 + K_6 s^6 + K_7 s^7$	
16	[38]	$U_{oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 s^4 + K_5 s^5 + K_6 s^6 + K_7 s^7 + K_8 s^8$	
17	[39, 40]	$U_{oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 s^4 + K_5 s^5 + K_6 s^6 + K_7 s^7 + K_8 s^8 + K_9 s^9$	
18	[41]	$U_{\rm oc} = K_0 + K_1 s + K_2 s^2 + K_3 s^3 + K_4 s^4 + K_5 s^5 + K_6 s^6 + K_7 s^7 + K_8 s^8 + K_9 s^9 + K_{10} s^{10} + K_{11} s^{11} + K_{12} s^{12}$	

The RMSEs of different SoC regions are given in Figure 4. Although these models perform well in fitting the SoC regions between 10% and 90%, but some models perform poorly in fitting the entire SoC regions for both NMC and LFP fresh cells, especially in the low and high SoC regions.

Theoretically, the fitting performance is better with higher order polynomial function, however, the 2nd to 4th order polynomial functions perform well in middle SoC regions, but perform poorly in low and high SoC regions. But for 5th and 6th order polynomial functions, the OCV-SoC curves pass through data points 0% and 100% and fluctuate sharply in the middle SoC regions. The fitting performances are become better for the 7th to 12th order polynomial functions. Therefore, we may conclude from Figure 4 that the models 16, 17 and 18 are suitable for NMC cell and models 7, 17 and 18 are suitable for LFP cell, which perform well in both the entire and middle SoC regions. In the following sections, all the OCV models are determined from the experimental data of entire SoC regions.

4.2 Sensitivity to Numbers of Data Points

As mentioned above, the OCV models are determined by fitting certain numbers of experimental data points with MATLAB curve fitting toolbox. Some studies used 21 data points (i.e., in every 5% SoC interval) to determine the OCV model [13, 14, 42], but some other studies used 11 data points (i.e., in every 10% SoC interval) [43-45] or 51 data points (i.e., in every 2% SoC interval) [30] to determine the OCV models. The comparison results depicted in Figure 5 indicate that the OCV models are more sensitive to the data points for LFP cell than NMC cell. These may be caused by their differences in low and high SoC regions of OCV-SoC curves. In addition, the RMSEs of NMC cell change slightly with increasing the numbers of data points except the models 5, 7, 12 and 13, but for the LFP cell, the RMSEs are generally decrease greatly with 21 data points than with 11 data points, but the RMSEs virtually unchanged if change the number of data points from 21 to 51 except models 8 and 14. Note that the models 8 and 18



require more than 12 and 13 data points, respectively, to fit by MATLAB curve fitting toolbox.

With the low-current OCV test, we can easily obtain certain numbers of data points, but for the other OCV test method, such as incremental OCV test, the experimental time will be greatly raised with increasing numbers of data points, therefore, it is recommended to model OCV by 21 data points by compromising the test time and model accuracy. In addition, we may conclude from Figure 5 that the models 4, 16 and 17 are suitable for NMC cell and models 4, 7 and 17 are suitable for LFP cell for their robustness against numbers of data points.

4.3 Sensitivity to Ambient Temperatures

The comparison results of OCV models at different ambient temperatures are illustrated in Figure 6. It is can be seen that most OCV models are sensitive to the ambient temperatures, especially the low temperature for both NMC and LFP cells. In addition, models 5 to 12 are more sensitive to temperatures than other models for NMC cell, but for the LFP cell, models 8, 13 and 14 are more sensitive to temperatures than other models. Besides, a conclusion can be drawn from Figure 6 is that models 16, 17 and 18 are recommended for NMC cell and models 4, 17 and 18 are recommended for LFP cell for their robustness against ambient temperatures.

4.4 Sensitivity to Aging Stages

Not only the temperatures but also the battery aging stages can influence the battery OCV [46, 47]. The comparison results of OCV models at different aging stages are illustrated in Figure 7. It is can be seen that most OCV models are sensitive to battery aging affects, especially models 5, 7, 8, 11 and 12 for NMC cells and models 8, 13 and 14 for LFP cells. In addition, a conclusion can be drawn from Figure 7 is that models 3, 17 and 18 are recommended for NMC cells and models 4, 17 and 18 are recommended for LFP cell for their robustness against aging affects.

4.5 Impacts on SoC Estimation

OCV model is commonly used to correct the SoC with aid of ampere-hour counting in SoC estimation process. In this study, the OCV can be regarded as part of the parameters of first RC battery model and can be identified by the H infinity filter [22, 38], then the OCV models only affect the SoC estimation process other than the parameters identification process. With the same online parameters delivered to SoC estimation process, it is more easily to observe the impacts of OCV models on SoC estimation with unscented Kalman filter (UKF) [22]. The results are shown in Figure 8. It is clear that these OCV models perform generally better for LFP than NMC cells except model 8 at 25 °C. In addition, a conclusion can be drawn from Figure 8 is that models 16, 17 and 18 are recommended for both NMC and LFP cells.

Based on the comparisons above, the compared fitting results of OCV models can be summarized in Table 3. Model 18 is a little bit better than model 17 representing experimental OCV-SoC relationship. Considering quite a few studies will still choose 11 data points from incremental OCV test data to model the OCV-SoC relationship, which only suit to fit no more than 10th order polynomial functions. Hence, Model 17 is more suitable than model 18. Furthermore, one could speculate that the improvement of accuracy between 9 and 10 order polynomial functions can be quite small. Therefore, it can be concluded that model 17, namely 9th order polynomial function, is better than others for both NMC and LFP cells. And this study recommends 9th order polynomial function to model the OCV for both the NMC and LFP cells.





5 Conclusions

1. This study conducts a systematic comparative study on eighteen OCV models. Low-current OCV tests are employed to obtain experimental OCV-SoC curves as the basis for comparison. The parameters of these OCV models are determined by experimental OCV data points.





- 2. NMC and LFP cells are used to evaluate how well the OCV models can accurately represent the OCV-SoC curves. Two representative experimental SoC regions (0%–100% and 10%–90%) data are used to fit the OCV models. The results show that some OCV models perform poorer over the entire SoC region than the middle SoC region.
- 3. The data size plays an important role in model selection. A set of 21 data points is employed to compare



Table 3 Comprehensive comparison of OCV models



Note: Mark \blacktriangle indicates the NMC cell and mark \blacktriangledown indicates the LFP cell

models with data size constraints. In addition, model sensitivity and robustness against temperatures and aging stages investigated. The results indicate that 9th order polynomial model is more robust than other models. These conclusions are further validated by comparing model impact on SoC estimation.

4. By thorough analyses of OCV models, the 9th order polynomial model is recommended for both NMC and LFP cells.

Authors' Contributions

RX was in charge of the whole trial and computational work, proposed the OCV model and implemented the verification; Q-QY wrote the manuscript; L-YW corrected the language and gave some suggestions. CL assisted with sampling and laboratory analyses. All authors read and approved the final manuscript.

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Competing Interests

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