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**A DECISION SUPPORT MODEL FOR LARGE SYSTEMS USING QUALITY
FUNCTION DEPLOYMENT AND GOAL PROGRAMMING: A CAPITAL
BUDGETING PROBLEM**

by

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B.S. August 1981, Old Dominion University

A Thesis submitted to the Faculty of
Old Dominion University in Partial Fulfillment of the
Requirement for the Degree of

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ABSTRACT

A DECISION SUPPORT MODEL FOR LARGE SYSTEMS USING QUALITY FUNCTION DEPLOYMENT AND GOAL PROGRAMMING: A CAPITAL BUDGETING PROBLEM

**Kenneth Lindsey, Jr.
Old Dominion University, 1996
Director: Dr. Derya A. Jacobs**

Effective planning for the modernization of U.S. Air Force fighter aircraft requires a perception of the future tasks these aircraft will be called upon to perform, and the improvements and modifications that will be required to successfully accomplish those tasks. A great deal of research has been done in the areas of military strategy, quality function deployment, capital budgeting, and goal programming, as separate areas of study. This thesis details the research and analysis performed for a project called The Fighter Configuration Plan (FICOP), in which these areas were integrated in a decision support model to aid the Air Force in modernization planning. The unique modernization planning approach developed through this analysis has fundamentally changed the way the Air Force plans for modernizing fighters. This research process developed a perception of the future tasks based on a framework known as Strategies to Task (STT), incorporated Quality Function Deployment (QFD) to develop metrics for the various modernization projects, and used an Integer Goal Programming Model to perform the capital budgeting. This decision support model was applied to the problem of developing long-term modernization plans for each of the existing fighter aircraft (F-16 Fighting Falcon, F-15 Eagle, F-117 Nighthawk and A-10 Thunderbolt II).

To Alecia, Nicole, Caleb, Kenneth Sr., and Evelyn Lindsey.

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CHAPTER I

INTRODUCTION

BACKGROUND

In 1994, the Commander, Air Combat Command (COMACC) initiated a study to review the existing configuration and to develop a plan for the future configurations of the F-16 Fighting Falcon. With over 1,200 of these highly advanced fighter aircraft in inventory, a shrinking budget, and a new geo-political environment, the Air Force needed a new, quantifiable, responsive process for developing optional investment strategies. The study was to be an extension of the Air Force Modernization Planning Process (MPP). The MPP is a systematic method for assessing current and future needs within the Air Force, and for organizing and developing initiatives into plans for filling those needs. Initially, the study was to consider only the proposed initiatives for improving and sustaining the F-16, obtained from several Mission Area Plans (MAPs). MAPs are the output of the MPP. The objective of the project was to develop the best affordable plan for this fighter from hundreds of competing initiatives (candidate modification projects) which spanned nine different mission areas. The scope of the study was later expanded to include all existing fighters.

The project was based on the Strategies to Task framework, a hierarchical representation of National Goals related to Department of Defense Strategy. This framework, which will be explained in detail later, was the directed setting for conducting modernization planning. A critical part of this research involved the question of how to link the allocation of resources to this framework. In the past a subjective process, based on persuasive arguments, prioritized lists, and personable champions was used to develop spending outlay recommendations. The resulting spending recommendation was not reproducible, nor was it synthesized across the set of possible investment alternatives.

The journal model adopted for this thesis is the "Empirical Research Report" as defined by Paul V. Anderson in *Technical Writing: A Reader Centered Approach, 3rd ed.* (Fort Worth: Harcourt Brace College Publishers, 1995).

Fighter Configuration Plan 1996 (FICOP 96) was undertaken to provide Air Force leadership with a comprehensive plan on how to affordably modernize the fighter fleet of over 2,400 aircraft over the next 18 years. Air Combat Command is responsible for organizing, training and equipping the Combat Air Forces (CAF) and for deciding which programs will receive funding, through the Program Objective Memorandum (POM), each cycle. A logical process and accompanying toolset for assessing the value, quickly making the trade-offs, and analyzing the results was desired to facilitate this decision process.

STRATEGIES TO TASK

The Strategies to Task Framework (Figure 1), developed by Glenn Kent (Lieutenant General USAF, retired), is a hierarchical method for linking national goals and interests with operational activities at the tactical engagement level. In the strategy to task approach, it was recommended that this framework be used as a way to define (top down) what operational tasks are required to support our national goals (Kent 1989). This approach is similar to a work breakdown structure for managing large projects, whereby project managers structure the work into small manageable elements. The ultimate utility of this hierarchy for planners, can be realized by linking the allocation of resources to this framework in an optimal manner to achieve the best overall effect. In other words, the framework should promote the allocation of resources on the basis of the greatest effect in achieving objectives and winning campaigns to support the national goals of the United States.

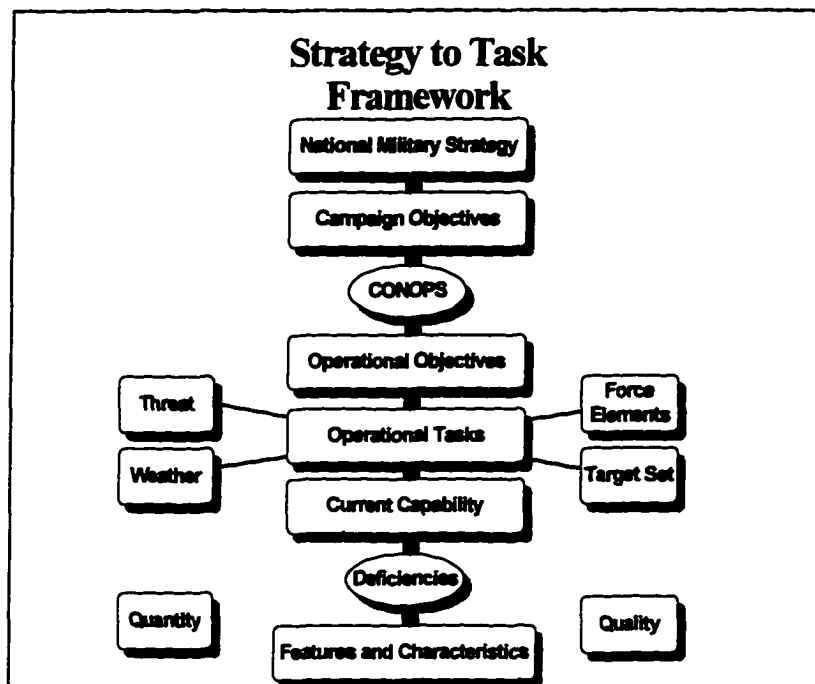


Figure 1 - Strategy to Task

National Goals (not shown here) which are at the top of this hierarchy are the nations most fundamental values. These goals are found in documents such as the U.S. Constitution and are permanent, regardless of the transient politics (Thaler 1993). The National Military Strategy of the United States of America 1995, lists the two national military objectives which U.S. Armed Forces are to accomplish. These objectives are promote stability and thwart aggression. The three components of the strategy are peacetime engagement, deterrence and conflict prevention, and fighting and winning our Nation's wars. The force required to support this strategy must possess (as a core requirement) the capability of fighting and winning two major regional conflicts (MRCs), nearly simultaneously. Five fundamental foundations brace the combat forces of the U.S. These are quality men and women, readiness, enhancements, modernization and balance (the appropriate mix of forces and capabilities). As described in the National Military Strategy (Joint Chiefs of Staff 1995): "The fourth foundation is modernization, which is vital to preserve the essential combat edge that U.S. forces now possess and to ensure future readiness. Due to budget constraints, major new investments will be pursued only where

there is a substantial payoff. Existing weapons systems and platforms will continue to be updated to take advantage of rapid technological advances.” This framework was directed for use within the Air Force for conducting modernization planning (HQ USAF 1994).

Figure 2 is a specific example of a strategies to task decomposition. In this example, the campaign objective is to establish air supremacy which means to gain and maintain control of the airspace. This broad, overarching objective can be further defined by the two operational objectives of reduce enemy sortie generation and defeat the enemy in the air. Reducing enemy sortie generation means to deny, damage or destroy manned air vehicles and/or their support facilities or equipment prior to vehicle launch. To defeat the enemy in the air is to deny, damage, or destroy airborne enemy aerospace vehicles prior to their employment of weapons against friendly forces including land, naval, and air units. The operational objectives can be further disaggregated and more specifically defined by the two operational tasks of neutralizing aircraft and neutralizing airfields. Using this systematic approach, beginning with the component of the U.S. National Military Strategy of fighting and winning our nations wars, and maintaining the capability of fighting and winning two major regional conflicts (MRCs), one can define discretely the military’s specific wartime operational tasks. Thus, this approach furnishes specific top down guidance to be used in modernization planning.

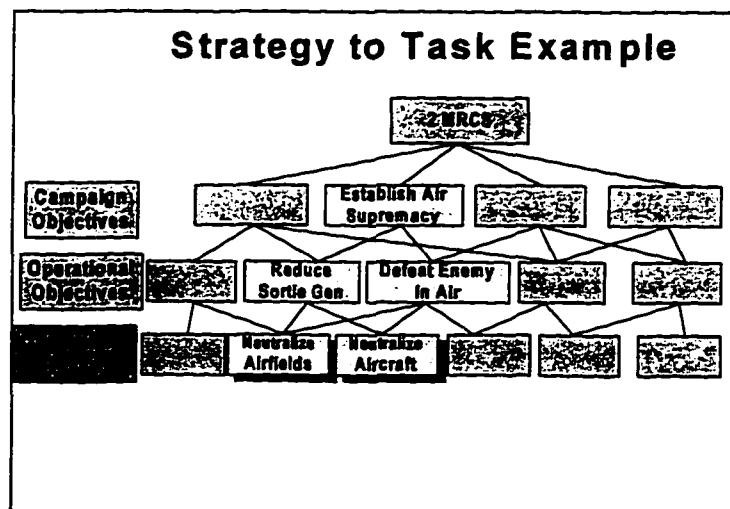


Figure 2- Strategy to Task Example

This system also provides a framework for advocating requirements from the bottom up. In other words, the tasks are directed units of work to be accomplished, and the modernization requirements are the necessary components to carry out that work. This approach also prescribes a philosophy, a systematic reasoned doctrine for advocating the importance of new modernization requirements. Although the construction of strategies to task framework is not the primary focus of this research, the significance of doing a credible job in this early definitional phase of a project cannot be over emphasized. Appendix A lists the campaign objectives, operational objectives, and operational tasks developed for this effort.

PROBLEM STATEMENT

Effective planning for the modernization of U.S. Air Force fighter aircraft requires a conception of what future tasks these aircraft will be called upon to perform, and what improvements and modifications will be required to successfully accomplish those tasks. In order to design a comprehensive, integrated plan from the myriad of potential candidate proposals, one must determine the value of individual projects and combinations of projects, assess the affordability, and finally allocate resources. This multifaceted problem affects every fighter in the Combat Air Forces (CAF) for the next eighteen years and includes programs valued at over \$20 billion (Table 1). The decision process for funding new systems at Air Combat Command was an intuitive process led by a resource management team, which did not participate in the planning and up front analysis. There was no traceability, repeatability, or measurability of the combat capability impact of the budget decisions. There was also no way to quickly develop a new plan when the circumstances changed. Decisions in the past based on persuasiveness, impractical priorities, and personalities led to disconnects in logic and funding, and lacked defensible criteria. There was no responsive and quantifiable method for developing investment plans to modernize the fleet of fighter aircraft which was based on analysis, capability, and executive guidance.

| Aircraft | Number of Aircraft | Number of Proposals | Capital Outlay Demand (\$M) |
|---------------|--------------------|---------------------|-----------------------------|
| A-10 | 375 | 34 | 1,713.9 |
| F-117 | 54 | 57 | 2,442.7 |
| F-15 A-D | 525 | 81 | 7,305.4 |
| F-15E | 203 | 55 | 6,022.9 |
| F-16 Blk 30 | 638 | 46 | 7,673.5 |
| F-16 Blk 40 | 434 | 46 | 12,607.0 |
| F-16 Blk 50 | 218 | 49 | 8,183.6 |
| Miscellaneous | N/A | 32 | 3,616.9 |

Table 1 - Fighter Aircraft and Proposed Modification Projects

RESEARCH OBJECTIVES

To support the attempt to link the planning process to the programming and budgeting process, a fundamental question of the value of proposed initiatives needed to be addressed. In order to assess the value, a clear understanding of management's objectives was required. Once the objectives were clearly understood, then the process of designing a decision support system to determine the most valuable alternatives could begin. The objective of this research was to design and develop a methodology which could be used to both measure the value of programs and to perform resource allocation based on that valuation process. The methodology was to develop an optimized, integrated plan of modernization programs considering the objectives of senior AF management. The optimized plan had to fit within the allocated budget, as determined by the Air Staff. The process was to consider proposed programs from several different aircraft and develop the best plan for investing across each type. In this problem, more than 400 projects, which spanned an 18 year planning window, were to be considered. Some of the projects were interrelated, which makes the resource allocation problem a more complex one. The ultimate objective was to build a decision support tool that could be used to develop a justifiable, analytical investment strategy.

CHAPTER II

LITERATURE REVIEW

INTRODUCTION

The purpose of this chapter is to review the previously published literature as it relates to multiple criteria decision making and capital budgeting, specifically military applications. The chapter is divided into three parts. The first part will describe knowledge gained from the review of published literature regarding capital budgeting and mathematical programming. The second part of the chapter will describe some relevant issues concerning the application of goal programming, as published in recent literature. The third section will focus on QFD literature which is most relevant to this research.

CAPITAL BUDGETING AND MATHEMATICAL PROGRAMMING

Capital Budgeting problems are not new, and in fact, some methods have been in existence for over 45 years. The published literature highlighted in this section will review the capital budgeting problem and related issues, discuss the application of mathematical programming, and give some related examples.

The capital budgeting problem can be broken down into the following four factors (Dean 1951):

- 1) Demand: how much money is needed for capital expenditures over the projected time periods? The “need” is generally measured by profitability.
- 2) Supply: how much money is available? This discussion centers on sources of funding (internal/external), retained earnings, etc.
- 3) Rationing: how should available capital be distributed among competing projects? Demand usually exceeds supply.

4) Timing: how should capital expenditures vary with adjustments in general business conditions? Here companies must balance savings against the risk that comes from imperfect foresight, which may produce obsolescence and excess capability.

“The capital budgeting decision is viewed as a many-sided decision of operating policy calling for collective wisdom in reconciling research dreams, production feasibility, competitive pressures and market acceptance” (Dean 1951). This statement has as much relevance today as it did 45 years ago. There are many different aspects involved in developing an investment recommendation, especially when the demand is not measured by profitability. There are many valuable lessons which can be taken from previous capital budgeting efforts which provide a useful starting point.

There are some key issues which should be addressed when dealing with capital budgeting problems. In a recent article, Dimkoff (1994) discusses some very basic budgeting mistakes, which he considers the most common ways to error when performing an economic analysis. The five mistakes highlighted are: ignoring the time value of money, basing decision on profits, emphasizing the payback method, letting sunk costs enter capital, and failure to consider only incremental costs. Mistakes number one, time value of money, number four, sunk costs, and number five, incremental costs are pertinent to this work. Regarding the time value of money issue, the author discusses problems with efforts which failed to capture the current worth of future sums of money. On the sunk costs question, there were many people who would argue that this approach should give credit to those programs which were already underway. In other words, programs which had already begun spending either R&D or acquisitions dollars. The author argues that these cost are historical and should not enter the decision. The only relevant costs are the additional outlays required to complete the project. Mistake number five, failure to consider only incremental costs is somewhat related to number four. In this area, the rule is that unless the organization will spend or receive more cash because of the project, the costs must not enter into the analysis. These lessons learned provided useful guidance in establishing capital budgeting philosophy.

In 1966 OR/MS analysts had a breakthrough linking some of the emerging optimization techniques to this type of problem and formulated and solved capital budgeting problems using linear

programming (Bierman 1980). Initially, these problems were performed with the simplex algorithm and eventually analysts began using integer programming techniques for project selection models. Early references to Goal Programming (GP) and Capital Budgeting articles date back to 1973 (Schniederjans 1995). The following articles give more recent examples of GP (and one multiple objective, mixed integer problem) applied to capital budgeting problems.

Khorranshahgol and Okoruwa (1994) developed a GP model to allocate funds among different shopping malls to maximize investor's revenue. In this article, the authors used a Poisson regression model to forecast the expected patronization for different malls as one of the inputs into their GP model. The Delphi technique was used to specify the objectives for allocating resources. The model had three goals: predicted patronization rate, average income, and number of major tenants. The model would suggest, an optimum solution that would allocate funds for footage leases at different shopping malls.

Ramanathan and Ganesh (1995) developed a GP model which was integrated with the Analytic Hierarchy Process (AHP) to evaluate energy alternatives for lighting in households in India. The model had seven decision variables representing the different energy sources (Kerosene to Electricity) and 12 objectives. AHP priorities were elicited and used for qualitative assessment of the objectives where there was no quantitative data available. System efficiency, for example could be computed using historical data. Safety factors, on the other hand were computed using AHP. The model allocated the amount of each source which should be used for lighting based on the energy, economic and environmental objectives.

Barbarosoglu and Pinhas (1995) used a mixed integer programming model (not goal programming) in conjunction with AHP to allocate funds from the World Bank among several water provision and waste water treatment projects. These authors dealt with multiple goals in a different manner. Their approach was to use AHP to compare the objectives (economic, social, and political) and then to develop a hierarchy linked to the individual alternatives. Using this approach, the four drinking water projects and five waste water projects were evaluated. The mixed integer problem would allocate the resources among the alternatives across a 15 year planning horizon.

Thus, mathematical programming, specifically GP applications continue to be applied to the field of capital budgeting. These examples demonstrate the wide variety of problems to which these techniques have been applied. In each of these cases, the number of alternatives was relatively small, and none of the literature revealed GP applications in military capital budgeting.

GOAL PROGRAMMING ISSUES

Goal Programming, an extension of linear programming, is a multiple objective approach that enables analysts and planners to come as close as possible to satisfying various goals and constraints. The subject of GP itself continues to be studied by researchers who draw on personal experience and study the experiences of others to further enhance the knowledge and understanding of this topic. The following publications were helpful in this research, and will provide key issues for discussion in subsequent chapters.

Schniederjans (1995), in his book reviewed several issues related to GP model formulation strategies which appeared in literature and offered some practical advice for improving GP models. Two of these issues which were related to those encountered in this research included “incommensurability of goal constraints” and “technological parameter estimation.”

The first issue, incommensurability of goal constraint, deals with one of the more inherent problems with using GP. That is, the various goals are measured using different units. For example, one goal, profitability, may be measured in dollars and another goal, trouble-free miles driven, may be measured in miles. Since a weighted, non-preemptive GP model attempts to minimize the total deviation from all goals, the solution would be biased towards the goals which have the largest magnitude, since this would result in the largest reduction in the objective function. The way Schniederjans recommends dealing with this is by scaling or normalizing of goal constraint parameters. Schniederjans offers the example:

$$\text{Minimize: } Z = P_1 (d_1^- + d_1^+) + 0.1P_2 (d_2^- + d_2^+) + 0.9P_2 (d_3^- + d_3^+)$$

$$\begin{aligned} \text{subject to: } \quad & x_1 + x_2 - d_1^- + d_1^+ = 100 \\ & 1,000x_1 - d_2^- + d_2^+ = 100,000 \end{aligned}$$

$$x_2 - d_3^+ + d_3^- = 100$$

$$d_i^-, d_i^+, x_j \geq 0, \text{ for } i=1, \dots, 3; \text{ for } j=1, \dots, 2$$

The recommended correction method is to convert the technological coefficients and right-hand side values to percentages of their objectives by dividing by the goal constraint's respective right-hand side value and multiplying the ratio by 100. In this case, using the 2nd constraint equation above, divide $1,000(x_1)$ by 100,000 to get 0.01 and multiply by 100 to get a normalized value of 1. The new model would be as follows:

$$\text{Minimize: } Z = P_1 (d_1^- + d_1^+) + 0.1P_2 (d_2^- + d_2^+) + 0.9P_2 (d_3^- + d_3^+)$$

$$\text{subject to: } x_1 + x_2 - d_1^+ + d_1^- = 100$$

$$x_1 - d_2^+ + d_2^- = 100$$

$$x_2 - d_3^+ + d_3^- = 100$$

$$d_i^-, d_i^+, x_j \geq 0, \text{ for } i=1, \dots, 3; \text{ for } j=1, \dots, 2$$

The second issue deals with the estimation of technological parameter estimates. In his book Schniederjans discusses an approach based on the use of economics called *Input-output analysis*. This type of analysis can be used to create technological coefficients which reflect real world impact of different types of *posterior* system behavior. This means that one should be able to have some measure of this *posterior* behavior. The example given deals with the percentage of scrap generated in a multi-stage production process. In the case of evaluating these proposed modernization projects for conducting air combat, there is no way to accurately ascertain the posterior behavior, short of procuring the system and taking it to war, which is not feasible. The examples cited above, used AHP and regression techniques to evaluate alternatives, to determine the weights of their technological parameters, and perform capital budgeting.

Gass (1987), in his article, describes his experience in determining goal weights when solving large-scale goal programs. He makes the point that preemptive linear-goal programming for these type of problems is too restrictive and imposes unrealistic burden on the decision maker by requiring them

to make strict statements of preemptive priorities. He also stresses that the idea of goal norming has little relevance in terms of what the basic problem really is: i.e. finding a suitable set of objective function weights that can be applied to over-and under-achievement deviation variables. This article makes a point that the analyst must determine how to best provide the decision makers with a selected set of compromise solutions from which to choose build a solution to implement. The approach the author recommends is referred to as multigoal programming. In this approach, the analyst elicits goal weightings from the decision makers as best he or she can. The resulting weighted objective linear program is solved along with sensitivity analysis about the goal. The results will therefore, include a number of compromise solutions using different weights.

Markland and Vickery (1986) describe the development of a solution strategy for solving large-scale integer goal programming problems. The application of the strategy was a computer-based multi-stage lot sizing model used for production scheduling. The paper emphasized the implementation of their model using commercial software. The reason that this article was found to be of particular interest, was due to the fact that most of the articles encountered which discussed integer goal programming approaches were applied to relatively small problems that did not propose a significant challenge to available solvers and machines. This problem consisted of 3,300 structural variables, of which, 78 were integer (production run quantities), and 85 were binary integer variables (occurrences of resource set-ups). The strategy adopted and applied was an iterative process which solved six sequential GP models in a stagewise fashion. The purpose of this approach was to reduce the number of explicit integer variables at each stage. The authors successfully applied the strategy and overcame, to some degree, the problem of sub-optimization across time periods by running the model in a stagewise-forward and a stagewise-backward approach.

Lessons learned from GP applications include issues which require careful attention, techniques for improving models and methods for solving large problems.

QUALITY FUNCTION DEPLOYMENT

In this section of the literature review, a focused discussion of pertinent QFD publications will be offered to put the application of this tool into context. The first publication is a book by two of the early Japanese QFD pioneers and the second article is a related application.

In their recently translated work, two early pioneers, Dr. Shigeru Mizuno and Yoji Akao (1994) provide a comprehensive discussion of various topics related to development and application of QFD. One of the areas discussed in their book deals with prioritization. Large, complex systems require prioritization in order to provide a strategic focus based on customer demands. The suggested method of prioritization in this text, starts with the customer demands, establishes themes for improvement based on evaluations of current circumstances, and assigning high scores to cases where there is a high level of achievement towards the stronger demands. These authors give some advice on carefully specifying the members of the evaluation team in advance, so that a bias does not develop in the scoring process. And, even though the judgments of individual members will vary based on experience, this can help rather than detract from the results. Although the specific judgments can be expected to be of the common sense variety, through combining the knowledge and wisdom of a number of properly selected evaluators, it is possible to gain a consensus regarding critical areas. Multidimensional evaluations of multiple factors, such as profitability, productivity, equipment investment, etc., must be performed to develop a business strategy. This prioritization based on customer demands is only a part of the process, and not a decision in itself. This step is simply a means to making higher-level decisions more definitive. The book concludes the chapter on prioritization with some ambiguous statements on the methodological maturity of prioritization via the demanded quality deployment table. The question of whether other operations research techniques might produce better results is raised. Clearly, this is an area where more research is needed.

In a NATO report (AGARD 1993), QFD was applied in a two-matrix architecture to study the problem of determining the potential effectiveness of 87 possible mobility improvements for NATO aircraft. The study recommends that a cost and operational effectiveness analysis (COEA) be performed to do a more thorough economic analysis. Thus, no bonafide, integrated cost and benefit

analysis is offered through this work, rather a general, rough estimation of low, medium, or high for each project with a note for follow-on analysis.

The results of the literature review provide a basis for continued research. Capital budgeting problems have established links to mathematical programming, and research continues to provide new information about the formulation of GP models in this area. However, large integer GP models to perform capital budgeting were not discovered in the review of literature, and techniques for estimating the value of military systems were not revealed. The QFD literature shows that there is a precedent for using this tool for prioritization, however, no publications linked the output of QFD to capital budgeting or GP. Thus, there is a basis for the research and an opportunity to examine the integration of these techniques.

CHAPTER III

METHODOLOGY

The methodology applied in this research was an integrated approach combining Quality Function Deployment (QFD), Capital Budgeting, and Goal Programming (GP) in a unique manner (Figure 3). QFD was applied to the Strategies to Task framework to develop weights and priorities for the various candidate modification projects. These weights were termed combat capability. Capital budgeting objectives, elicited from senior leadership (called executive guidance in this diagram) served as a basis for setting management priorities. An Integer GP model was developed using the weights, generated by QFD to perform the capital budgeting and to allocate resources in an optimum manner. This chapter will describe the methodology and application.

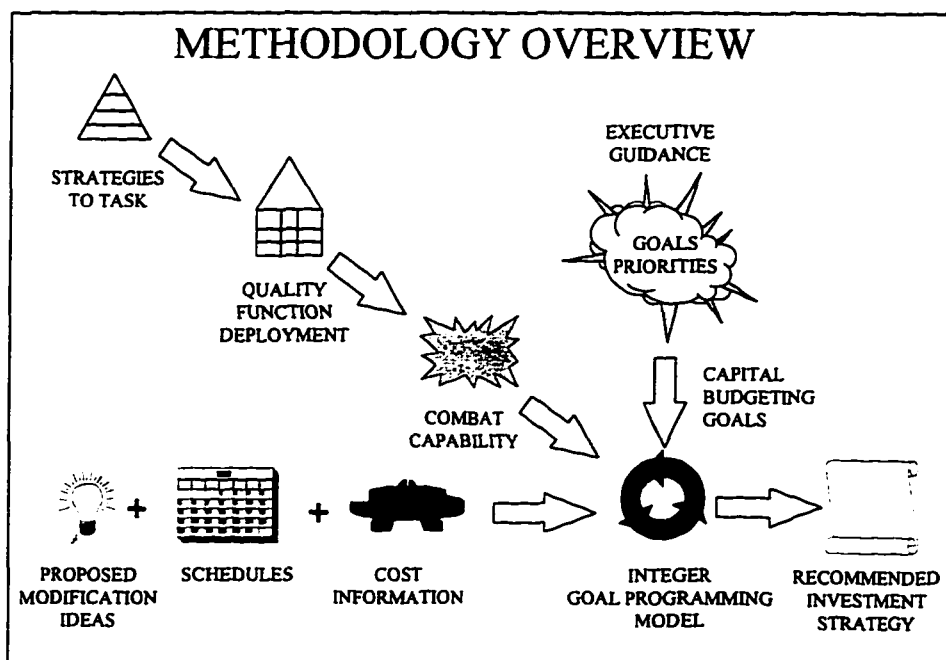


Figure 3 - Methodology Overview

QUALITY FUNCTION DEPLOYMENT AND PRIORITIZATION

QFD was used in this analysis not only to link the proposed modernization projects to the Strategies to Task framework, but was also used to establish priorities (and weights) for each project. The definition for QFD, most appropriate for the application in this thesis, is as follows: “a systematic way of ensuring that the development of product features, characteristics, and specifications, as well as the selection and development of process equipment, methods, and controls, are driven by the demands of the customer or marketplace” (Eureka and Ryan 1994). These authors also offer the following collection of definitions from practitioners to describe this tool:

- “A sophisticated Pareto analysis.
- A fundamental, commonsense approach to product development that focuses on proactive rather than reactive quality control.
- A technique to help neutralize the voice of the customer.
- A systematic way of documenting and breaking down customer needs into manageable, actionable details.
- A planning methodology that organizes relevant information to facilitate better decision making.
- A framework for customer-derived product development objectives.
- A way of reducing the uncertainty involved in product and process design.
- A technique that promotes cross-functional teamwork.
- A methodology that gets the right people together early onto work efficiently and effectively to meet customer needs.” (Eureka and Ryan 1994).

One thing that is apparent from these definitions, is that QFD involves a customer, an analysis process, a product, and a team approach. This section of the methodology chapter will explain the fundamental philosophy, the basic QFD house of quality chosen, the design of the QFD matrices and the role of the evaluation team.

Fundamental Philosophy

The fundamental philosophy behind QFD and the basic philosophy of strategies to task have a very similar theme, well suited for this research. That philosophy (QFD), starts with top level strategy, systematically disaggregates the strategy into actionable details and links lower level activities to this strategy. An underlying philosophy behind QFD, called *hoshin* management, is “a system of deploying

corporate strategies and plans into yearly activities, promoted by specific targets and implementation means at all levels in the organization” (Mizuno and Akao 1994). Thus, quality planning, quality design, and quality assurance activities needed to be linked to top corporate strategies, through the use of quality functions which are cross-functional and their control interdepartmental. “*Hoshin* management is implemented not merely to achieve quality targets but also to link TQM activities for fulfillment of all critical management objectives” (Mizuno and Akao 1994). So, the corporate goals are not merely a charming rhetorical phrase. Rather, these goals become the defining force, or the underlying tactics weaving together all daily activities and focusing them on a common goal. In this context *hoshin* management has a mobilizing effect, interlocking activities from all functional areas with the strategic focus of management. QFD is a proven method for linking functional level activities to management objectives.

Strategies to task, a hierarchical method for linking national goals and interests with operational activities at the tactical engagement level, has a very similar philosophy. This method starts with the broadest national goals, and systematically links specific functional level tasks to these goals. In order to formulate the best strategic investment plan, the allocation of resources must be linked to the strategies to task framework. This linkage should be accomplished with an operational focus, in an optimal manner to achieve the best overall effect (Kent 1989).

Therefore, in the context of this research, QFD has two primary purposes. First, to translate the top level strategies into specific actionable details. This is often called the voice of the customer. In this case, the Air Combat Command (ACC) top level strategies can be derived and translated into specific detailed requirements, representing the voice of the customer. QFD provides a way of linking modernization planning activities to these critical management objectives. Secondly, QFD provides a way of prioritizing fighter aircraft modernization features, characteristics, and specifications and ensuring these are driven by the demands of the customer or ACC.

In order to determine which modernization projects would potentially yield the best overall effect in achieving objectives and winning campaigns, a scoring scheme was needed. This scheme

would develop measures of worth for each candidate modification (sometimes referred to as a “solution”) project. QFD was chosen as the method to generate pseudo combat capability measures. It is difficult, if not impossible to measure, in absolute terms, the marginal, potential combat capability of every modification, even with very large, complex simulations. Some of the projects considered, such as color displays, landing gear wires and switches, and improved aircraft batteries would never affect a change in the outcome of large simulation models, because these models generally do not include this level of detail. These projects however, are important candidates and provide significant capability to the user (ACC), and therefore merit careful consideration in the development of investment strategies. Many corporate organizations are turning to QFD, a market-driven product definition process, to ensure they satisfy the requirements of all important customers (Farrell 1994).

Basic House of Quality Adapted

There are many different QFD designs available, which can be customized to fit various applications. The model selected for use in this study is called a house of quality. Figure 4 shows a typical QFD House of Quality. On the left are the “what” items or the objectives (customer requirements), which have all been defined in a previous step. These “whats” often begin as loosely stated objectives of what is to be accomplished, that require further detailed definition. In order to satisfy the customer, we must attack and disaggregate these objectives into more actionable details. These details are the “how” items which you see across the top of the matrix. The roof of the house is a triangular correlation matrix, which may be used to describe the degree of correlation between each “how” item. The part of the house to the far right is labeled “why”. This room is where the priorities of the what items are captured. Some objectives may be more important than others. The bottom room of the matrix, “how much” describes the relative weighting of the “hows” in the respective column above. The mechanics are based on a recurring “what” to “how” theme where you enter from the top and assess each intersection, to determine the amount of contribution a “how” has to a particular “what”. This room is the relationship matrix. QFD uses a (9-3-1) standard scale placing stronger (9) emphasis on most important items, in terms of contribution strength.

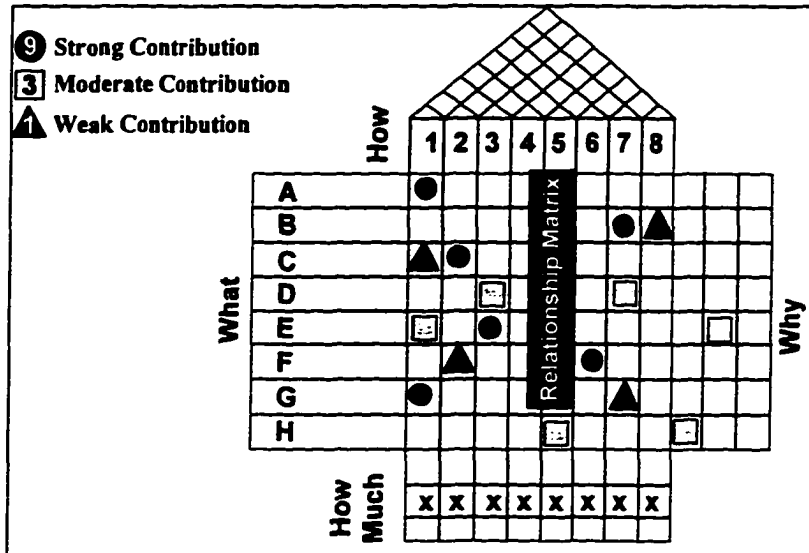


Figure 4 - QFD House of Quality

Integrated Matrix Design

The first step in this phase of the project was to lay out an inter-linked matrix design. The design process addressed some very basic but essential questions. Which operational objective is the most important? Which task is most important? Thus, the desired output at every stage in the process shaped the final matrix designs. The command defined deficiencies were prioritized through this cascading (deploying) of objectives from strategies to task analysis using interlinked houses of quality (Figure 5). This method is not foolproof, but does provide structured process for capturing intuition and knowledge that is documented and repeatable.

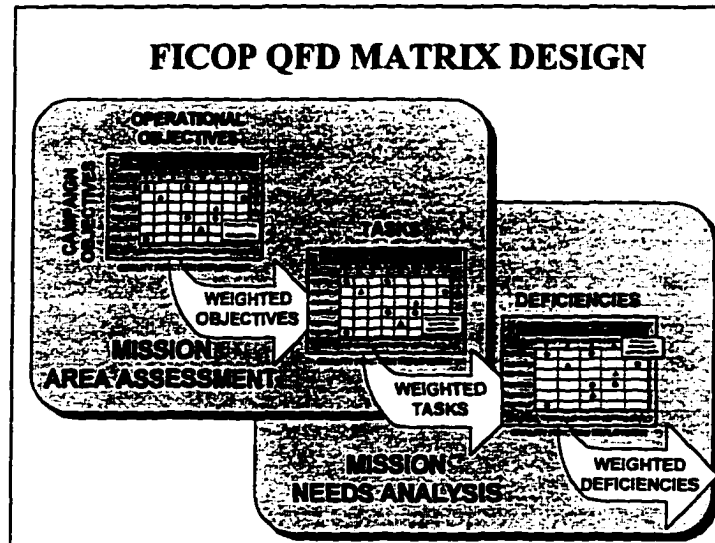


Figure 5 - FICOP QFD Matrix Design

At the end of this matrix design, the prioritized and weighted command deficiencies were generated. The next step in the matrix design was to adjust the weighting of the deficiencies by aircraft (Figure 6). The question to be answered at this step was: Where (which aircraft) does this capability need to reside? Deficiencies are not equally relevant across platforms. A deficiency that is critical to the mission of one aircraft may have a lower applicability to another. The intent of this step was to add platform relevance to the deficiency score. The deficiencies, by the previously designed matrices, would already have a command priority and weighting, relative to all of the other deficiencies. The desired outcome of this process was to increase or decrease weights of specific prioritized deficiencies according to aircraft type, by considering the mission performed, current capability, and projected requirements. This assessment would result in 10 separate lists of deficiency weights. These deficiencies and their adjusted weightings were "deployed" in the design to the next evaluation level, the solution assessment phase.

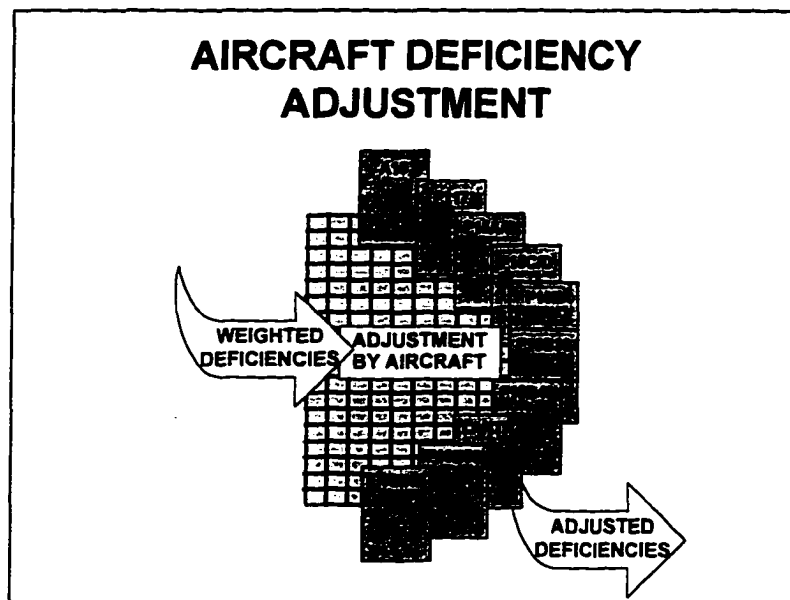


Figure 6 - Aircraft Deficiency Adjustment

The next step was to evaluate each of the candidate modification projects (solutions to deficiencies) against each of the deficiencies (Figure 7). The question to be answered by this step in the integrated matrix design was: What is the overall relative worth of the solutions in providing the capability prescribed in the deficiency descriptions? The design was meant to capture the total contribution value of each solution. A solution which could greatly assist in solving (alleviating) capability shortfall over a large number of deficiencies should receive a high score by this design. A solution which contributes to only one or a few deficiencies would receive a lower resultant weighting. This relative, marginal contribution value was referred to as a combat capability measure. Thus, at this step, every modification proposal was examined to determine which deficiencies it would help alleviate and to what degree. The results were weighted scores which were used as a measure of the potential, relative combat capability offered by that solution. This score was attributable to strategies to task, developed using a systematic analytical approach, reproducible, and consistent for each of the modifications.

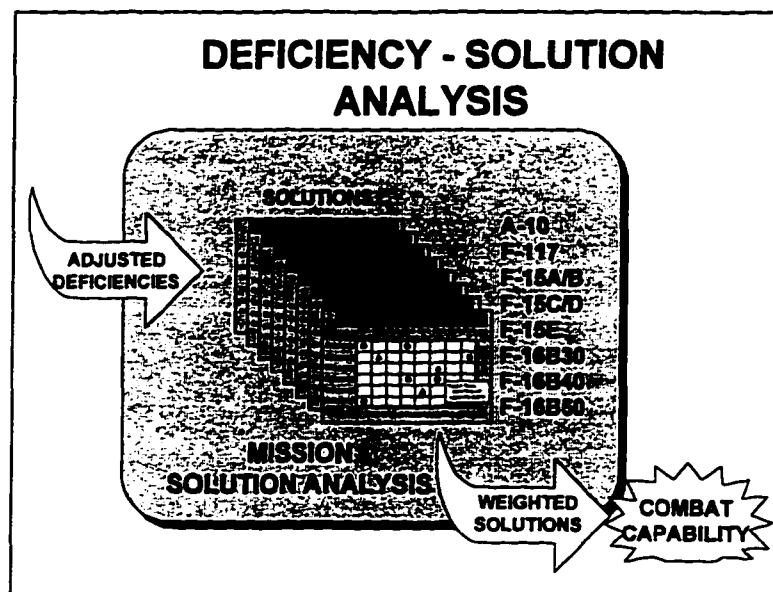


Figure 7- Deficiency - Solution Analysis

Using this integrated matrix design approach, the methodology can capture the benefit of programs which have cross-cutting contributions (Figure 8). Program A contributes to four mission areas, whereas program F contributes to 11 mission areas. Therefore, program F, in all likelihood, would have a higher contribution value score than would program A. The strength of the contribution relationships is not apparent in this example. In this case, QFD accumulates the potential benefit score for each program based on the number of deficiencies that program addresses and the degree to which the solution contributes. The interlinked matrix design explicitly captures this cross-cutting effect.

The Evaluation Team

A multifunctional group of evaluators was formed to collect the necessary information and make the necessary evaluations for the QFD analysis. The evaluation team was composed of fighter pilots, analysts, engineers, maintenance officers, intelligence and communications officers, other functional representatives (e.g. Air National Guard) and, periodically, program managers. The FICOP core team was made up of six individuals, including the author.

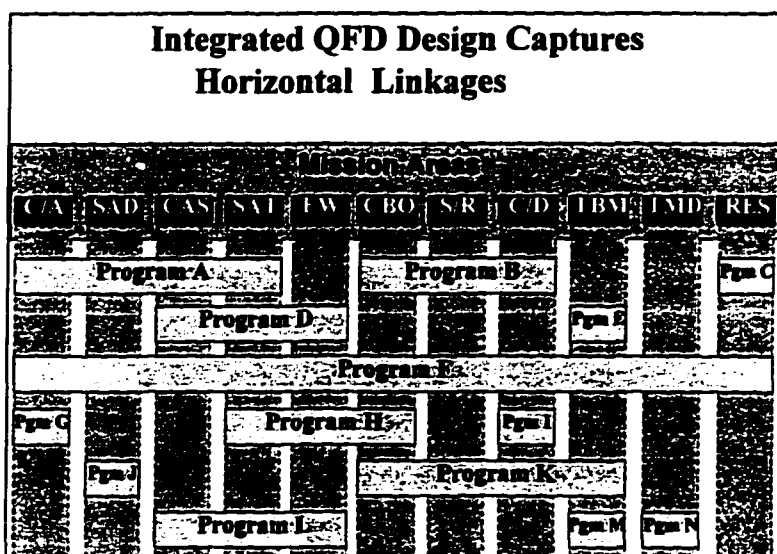


Figure 8- QFD Horizontal Linkages

The core team would often meet to prepare the matrices for the expanded team's review and evaluation, and perform consistency checks after the evaluations were completed. The expanded FICOP team would bring additional expertise, research on specific issues and functional experience to help inform the group's judgments for the evaluation process.

The core team met frequently, on average of three to times per week, over the six month time span. The job of this team was to manage the generation of the information and ensure consistency, completeness, and accuracy. The expanded evaluation group met twice a week in the early phases and about once a week after the first six weeks. Initially, the meetings were mostly brainstorming sessions to validate the strategy to task elements and definitions. The evaluation sessions were very dynamic, and the discussion at each of the intersections invaluable. Typically, the core team would meet for about two hours at a time, and the expanded evaluation group from two to four hours.

Figure 9 shows a typical (partial) QFD matrix which was generated by the evaluation team. In this matrix, the team evaluated each operational objective ("Hows") in terms of its contribution to the campaign objectives ("Whats"). While performing this type of evaluation, contributions by those with particular knowledge on a given topic were offered to the group, thus increasing the group's

overall awareness through a focused dialogue. This approach proved to be a very productive means of capturing wisdom and experience which could be used later in the process.

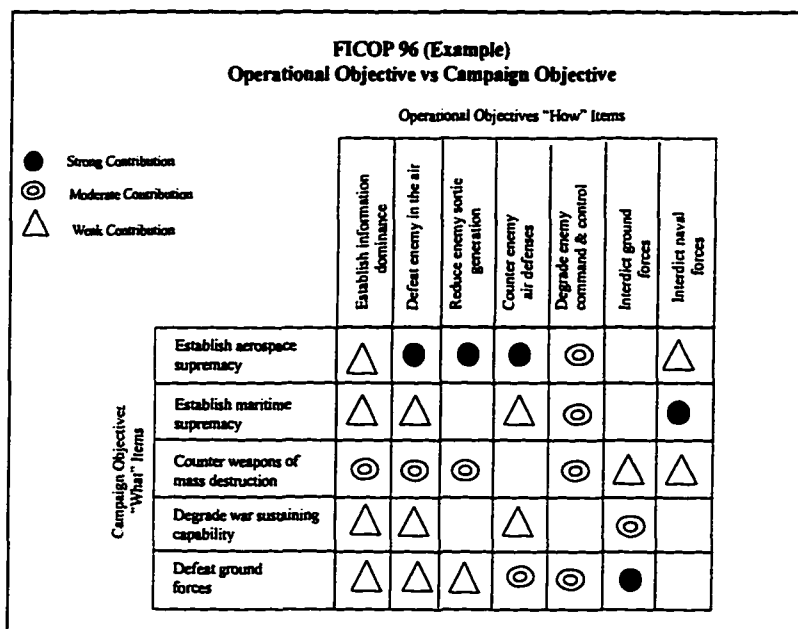


Figure 9 - FICOP Example Matrix

The QFD process described above provided a structured way to articulate the Combat Air Force's fighter requirements. This process also guided the study to investigate specific issues in a deliberate fashion, rather than in an ad hoc approach. The process involved many different functional representatives and integrated their inputs into systematic scheme for assessing priorities. Thus the stage was set for a robust approach for linking the allocation of resources to this framework.

CAPITAL BUDGETING DEVELOPMENT

The capital budgeting methodology is based on research which has evolved over the years to include the use of mathematical programming algorithms that efficiently develop solutions to complex problems. Many capital budgeting models use some estimate of the potential monetary gain to be realized from the respective investments as a measure of merit in the objective function. Popular choices were Net Terminal Value (NTV), Internal Rate of Return (IRR) or Yield. In this case, since

these fighter modification projects do not yield any monetary returns, the primary measure of merit is the combat capability metric. However, there are other factors which influence the investment decision which must be considered as well. This section will describe the development of the capital budgeting approach.

Integer programming models have long been applied to capital budgeting problems where the decision variables are binary. The initial problem formulation is based on a classical capital budgeting problem formulation:

$$\text{Maximize } Z = \sum_{j=1}^n w_j x_j$$

subject to

$$\sum_{j=1}^n c_{ij} x_j \leq C_t, \quad t=1, \dots, T$$

where

n = the number of projects

w_j = the coefficient which represents the per unit, marginal value associated with each project j

(Typically, w_j represents the marginal return associated with investments in various capital projects. In this case, w_j is a measure of marginal combat capability increase associated with the different projects.)

c_{ij} = cost of project j in year t

C_t = the maximum allowable budget for time period t

T = the total number of years, and

x_j = 0 or 1, represents decision variables for each project j

The problem with this approach was that there were other factors which the decision makers wanted considered in the development of an investment strategy. The other goals to be considered were

reducing the cost of operating the fleet (operations and support), managing technical risk, and maximizing opportunities to share development and acquisition cost. The addition of the cost of ownership goal was the most significant, and required considerable development to define and generate. The technical risk and cost sharing were reasonably straightforward. The desire of senior leadership to broaden the factors considered moved the research away from the classical integer programming model to an integer, goal programming model (also called zero-one, goal programming, ZOGP) which will be explained below. The capital budgeting goals used in this analysis were as follows:

Combat Capability: Maximize the total combat capability value of projects selected, as measured by the QFD score of each modification project. This approach gives more credit to modification which deliver the most potential combat capability. Those projects with higher QFD score are more attractive to the model.

Cost of Ownership (Savings) : This objective was chosen to highlight projects which have a potentially significant impact (if funded and installed) in reducing the cost of operating the Air Combat Command fleet. There are projects which are proposed on the merit of their potential to save operations and support (O&S) funds over some more costly procedure currently practiced. This savings could come from either consumables, fuel, contractor support, software maintenance, manpower, or depot level repair/maintenance. Essentially, this factor captures the total possible O&S savings of a project over the time span of the study. The calculation of savings starts after the first full year of installation.

This objective considers the time value of money by computing the present value of future savings. The basic concept behind present value is that cash available in the near future is worth more than the same amount of cash at some distant point in the future (Shillinglaw and McGahran 1993). This method allows a single measure (total present value) for the cost of ownership savings, and permits each project to compete on a common basis. One of the most common mistakes made in capital budgeting is ignoring the time value of money (Dimkoff 1994). The present value calculation allowed the time value of money to be considered in determining an aggregate measure for the cost of ownership savings goal.

FMS/Joint: Maximize the participation in projects which have a significant potential/agreement for cost sharing between foreign military sales and/or joint services. Give more credit to those modifications which have FMS or Joint agreements.

Technical Risk: Minimize the technical risk value associated with the selection of the various projects which have a technical risk rating. Give more credit to modifications which have lower technical risk.

Budget Utilization: Maximize utilization of the available budget. Use as much of the available budget as possible.

The capital budgeting framework developed the basis on which to allocate resources according to the critical objectives of management. This analysis began with a more classical approach and incorporated revised direction and input from leadership. Thus, this framework provides a way of linking the allocation of resources to strategies to task and to achieving critical management objectives. Goal programming provides the multiple criteria decision making tool to perform the resource rationing.

GOAL PROGRAMMING MODEL DEVELOPMENT

Goal Programming (GP) is a multiple objective approach which allows the trade-off of different goals which are not commensurate and often conflicting. The capital budgeting model developed for this analysis, is a weighted GP model, that assigns relative weights to the deviation variables to control the level of importance of the respective goals. Within the model, the emphasis on the different variables was adjusted according to senior leadership direction. This was accomplished by adjusting the objective function coefficients for the deviation variables which correspond to the various goals. Figure 10 shows a representative output of the level of achievement for each goal. The model is a nonpreemptive model that strives to minimize the total weighted deviation from all goals stated in the model according the desired emphasis on each of these goals. The model formulation is given below.

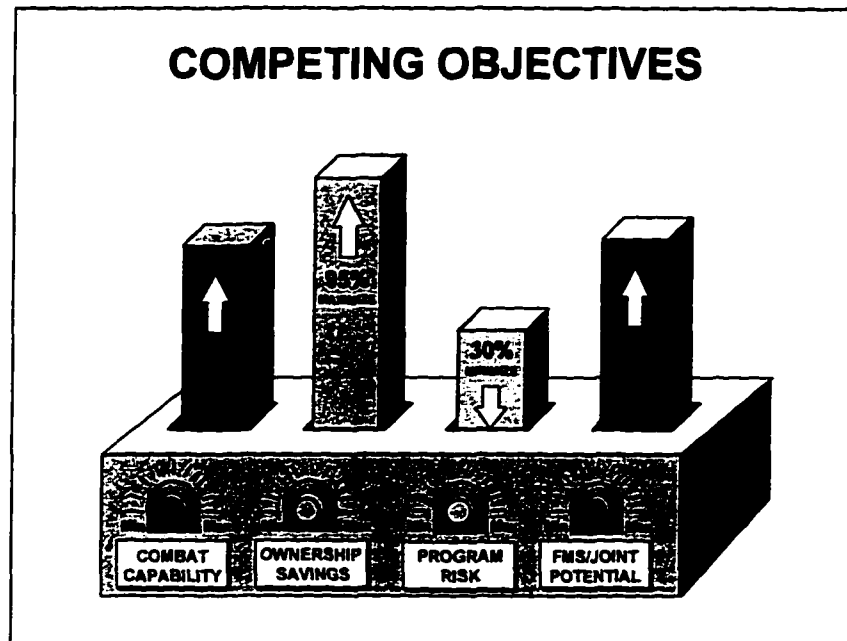


Figure 10 - Competing Objectives

Model Formulation

The GP model developed was a weighted, nonpreemptive model consisting of five goals, 400 binary decision variables and 120 constraints.

Decision Variables: $x_1, x_2, x_3, \dots, x_j, \dots, x_{400}$ representing the 400 proposed, candidate modification projects. x_j is a binary variable taking the value 1 when the j^{th} project is selected or 0 if the j^{th} project is not selected.

Objective Function:

$$\text{Minimize } Y_1 d_{wu} + Y_2 d_{cu} + Y_3 d_{fu} + Y_4 d_{rv} + Y_5 \sum_{i=1}^m d_{pi}$$

where

Y_1 to Y_5 = nonnegative constants representing the relative weight assigned to the deviation variables.

m = number of years considered.

d_{wu} = underachievement deviation variable for combat capability weight.

d_{cu} = underachievement deviation variable for cost of ownership savings.

d_{fu} = underachievement deviation variable for cost sharing (FMS/Joint).

d_{tv} = overachievement deviation variable for technical risk, and

d_{pu} = underachievement deviation variable for budget utilization.

Goal Constraints

Subject to:

- **Combat Capability:** Minimize the underachievement of the goal of attaining the total importance weight. The constraint equation for this goal is as follows:

$$\sum_{j=1}^n w_j x_j + d_{wu} - d_{wv} = W_{Goal}$$

where

n = the total number of projects.

w_j = the combat capability weight (QFD score) associated with each project

j .

x_j = 0 or 1, represents decision variables for each project j

d_{wu} = underachievement deviation variable for combat capability.

d_{wv} = overachievement deviational variables for combat capability, and

W_{Goal} is the weight goal, the total weight possible summing across all projects.

- **Cost of Ownership Savings:** Minimize the underachievement of the goal of attaining the total O&S savings. The constraint equation for this goal is as follows:

$$\sum_{j=1}^n c_j x_j + d_{cu} - d_{cv} = C_{Goal}$$

where

c_j = the O&S savings (NPV) associated with each project j .

x_j = 0 or 1, represents decision variables for each project j

d_{cu} = underachievement deviational variable for O&S savings.

d_{cv} = overachievement deviational variable for O&S savings, and

C_{Goal} = the cost of ownership savings goal, the total cost of ownership savings possible summing across all projects.

- **Cost Sharing (FMS/Joint Participation):** Minimize the underachievement of the goal of attaining the total FMS/Joint score. The constraint equation for this goal is as follows:

$$\sum_{j=1}^n f_j x_j + d_{fu} - d_{fv} = F_{Goal}$$

where

f_j = the cost sharing score associated with each project j .

x_j = 0 or 1, represents decision variables for each project j

d_{fu} = underachievement deviational variable for cost sharing.

d_{fv} = overachievement deviational variable for cost sharing, and

F_{Goal} = the total cost sharing goal possible, summing across all projects.

- **Technical Risk:** Minimize the overachievement of the goal of attaining the lowest possible technical risk score. The constraint equation for this goal is as follows:

$$\sum_{j=1}^n t_j x_j + d_{tu} - d_{tv} = T_{Goal}$$

where

t_j = the technical risk score associated with each project j .

x_j = 0 or 1, represents decision variables for each project j

d_{tu} = underachievement deviational variable for technical risk.

d_{tv} = overachievement deviational variable for technical risk, and

T_{Goal} is the technical risk goal, in this case zero (0).

- **Budget Utilization:** Minimize the underachievement of the goal of spending the projected annual budget. The series of m constraint equations (one for each year) for this goal are as follows:

$$\sum_{j=1}^n p_{ij} x_j + d_{pu_i} - d_{pv_i} = B_{Goal_i}, \quad i=1..m$$

where

m = the number of years considered.

p_{ij} = the price (outlay required) of project j in year i .

x_j = 0 or 1, represents decision variables for each project j

d_{pu} = underachievement deviational variable for budget utilization.

d_{pv} = overachievement deviational variable for budget utilization, and

B_{Goal_i} = the maximum allowable budget for year i , $i=1, \dots, m$ (years).

Nonnegativity Constraints

$x_1, x_2, x_3, \dots, x_j, \dots, x_{400}$ = nonnegative and binary.

$Y_k \geq 0$, for $k=1, \dots, 4$ and

$d_{wu}, d_{wv}, d_{cu}, d_{cv}, d_{fu}, d_{fv}, d_{tu}, d_{tv}, d_{pu}, d_{pv} \geq 0$.

System Dependency Constraints (there were more than 100 interdependency equations):

Type 1: $x_j - x_k = 0$ Project j and project k are codependent, if one is selected then the other must also be selected. Project j will not function without project k and the reverse also holds true.

Type 2: $x_j + x_k \leq 1$ Project j and project k are mutually exclusive, if one is selected then the other cannot be selected. Project j cannot be used in conjunction with project k and the reverse also holds true.

Type 3: $x_j - x_k \geq 0$ Project k needs project j, if project k is selected then project j must also be selected. Project j can be selected alone, however project k cannot. Project j can be used alone or in conjunction with project k and the reverse is not true. Project k provides no useful function without project j.

This model is the baseline from which many derivatives were built. One such derivative was constructed to deal with the issue of incommensurability of goal constraints. The recommended approach above (Schniederjans 1995) was very similar to the one adopted for this research with the exception of the multiplication by 100. In this particular case the above stated model changed as follows:

$$\text{Minimize } Y_1 d_{wu} + Y_2 d_{cu} + Y_3 d_{fu} + Y_4 d_{rv} + Y_5 \sum_{i=1}^m d_{pi}$$

$$\sum_{j=1}^n (w_j / W_{Goal}) x_j + d_{wu} - d_{wv} = W_{Goal} / W_{Goal}$$

$$\sum_{j=1}^n (c_j / C_{Goal}) x_j + d_{cu} - d_{cv} = C_{Goal} / C_{Goal}$$

$$\sum_{j=1}^n (f_j / F_{Goal}) x_j + d_{fu} - d_{fv} = F_{Goal} / F_{Goal}$$

$$\sum_{j=1}^n (t_j / T_{Goal}) x_j + d_{tu} - d_{tv} = T_{Goal} / T_{Goal}$$

$$\sum_{j=1}^n (p_{ij} / B_{Goal_i}) x_j + d_{pu_i} - d_{pv_i} = B_{Goal_i} / B_{Goal_i}$$

This GP model was designed to permit management to trade off different levels of importance assigned to each of the goals, which represented critical objectives. The flexibility offered by GP to consider competing objectives which are not necessarily commensurate is one of the strengths of this tool. For example, with technical risk, the model is attempting to minimize this goal, whereas the other goals are maximizing functions. It is important to understand how the goals are developed, how they relate to one another, and what the weights are actually accomplishing.

DATA GENERATION

ACC Mission Area Plans (MAPs) provided much of the initializing data for this project. MAPs, the official documentation of the Air Force Modernization Planning Process, cover a 25 year period and use prescribed guidance (including Defense Planning Guidance and Strategies to Task) to document the most effective means of correcting task deficiencies from among nonmateriel solutions, changes in force structure, systems modifications or upgrades, science and technology applications, and new acquisitions. ACC MAPs are developed by integrated product teams with representatives from Air Force Materiel Command (AFMC), National Laboratories, and the independent research and development efforts of academic institutions and industry. The primary data derived from these documents were the descriptions of the operational tasks and the operational deficiencies and proposed solutions (aircraft modification projects).

The generation of cost data proved to be a difficult and time consuming part of this research. Although some of the proposed projects were not new ideas, unless a project was previously funded, generally there was not a completed cost estimate which could be used directly. Some of the modification projects were conceptual and therefore specific configurations and quantities had to be

developed in a concept of operations before costing activities could begin. AFMC supports the MPP through Technical Planning Integrated Product Teams (TPIPTs). TPIPTs support the MPP with analysis, concept development, technology need identification, and cost estimating. In addition to coordinating and integrating AFMC support, the TPIPTs coordinate national laboratories, industry, and academia input into the MPP. AFMC provided the cost estimates as well as the assessment of technical risk and cost sharing opportunities. Table 2 lists a sample of the summarized input data.

| AC Type | ID NUMBER | Weight (QFD) | FMS/Joint | Tech Risk | CostOwn | FY98 | FY99 |
|---------|-----------|--------------|-----------|-----------|---------|------|------|
| A-10 | A100001 | 216011 | 0 | 0 | 21.99 | 3 | 5.9 |
| A-10 | A100002 | 1750597 | 10 | 5 | 162.64 | 37.6 | 30.1 |
| A-10 | A100003 | 904230 | 10 | 5 | 0.00 | 33.6 | 17.1 |
| A-10 | A100004 | 179856 | 0 | 0 | 0.00 | 0 | 6 |
| A-10 | A100005 | 1937092 | 0 | 5 | 33.93 | 0 | 2.4 |
| Engines | ENGN002 | 134409 | 0 | 0 | 14.83 | 0.9 | 0.9 |
| Engines | ENGN003 | 79821 | 0 | 0 | 0.00 | 0.7 | 0.7 |
| Engines | ENGN004 | 16974 | 0 | 0 | 11.29 | 3.5 | 3.5 |

Table 2 - Sample Data Sheet

The first column is the system or aircraft type. Next is the project ID number, followed by the QFD score. The next column is the cost sharing metric. In this case, either a project has a cost sharing agreement (indicated by a score of 10) or it does not (indicated by a score of 0). The next column is the technical risk assessment. There were three values given to technical risk, high (10), medium (5), or low (0). The next column contained the cost of ownership value, the net present value of the O&S savings over the 18 year period in consideration. Then there were 18 columns which contained a total outlay required for each specific year. This sample sheet represents a Microsoft Excel (Microsoft 1994) spreadsheet which was linked to 12 other Microsoft Excel spreadsheets which contained the specific strategies to task scores, deficiency scores, modification project scores, as well as the cost data sheets. Thus, an interactive decision support system was built which could recalculate quickly. Therefore, the inputs to the goal programming model were dynamic and easily accessible. SAS (SAS 1988a) data

analysis software read the inputs directly from the Excel spreadsheets and put the outputs of the GP model back into a spreadsheet.

METHODOLOGY SUMMARY

The methodology developed for this research integrated in a new way QFD, capital budgeting, and goal programming. As seen from this chapter, QFD helps to structure the information about the various proposals and develop priorities. Capital budgeting provides a well established approach to allocating resources to competing projects. Goal programming provides a way to integrate this information to meet other key management objectives. This approach is similar to some that have been applied before using other tools.

CHAPTER IV

DISCUSSION OF RESULTS AND CONCLUSIONS

RESULTS

Through this research, three very useful findings were obtained. First, a multi-stage QFD model can provide consistent technological parameter weights as inputs into a capital budgeting process. Secondly, QFD and Integer Goal Programming can be run interactively, even for large scale problems. Thirdly, and most importantly, these types of decision support tools can provide usable, responsive information to decision makers. This section will examine each of these findings and offer data to substantiate these claims.

The technological parameter estimation method adopted here is very different from any approach which was found in the literature, and is at the core of this research. Specifically, w_j , the technological parameter which represents the marginal contribution values which we call combat capability was computed using QFD. The challenge for this research was to develop technological parameter estimates which could be used as inputs into a GP model, and that were tied to the strategies to task framework. Technological parameter estimates should permit variation in range that is roughly proportional to the range of cost, in order to reach an optimal solution which makes sense. This simply means that things that are very expensive should have an opportunity, via this parameter, to receive a proportionally high combat capability score. How does one know if the answer which is produced by this decision support system is "right?" There is not just one "right" answer. The answer which is most correct is the one which the decision makers find logical, defensible, and *acceptable*. The following discussion will describe the approach taken in this research for deriving technological parameter estimates for combat capability.

In order to have meaningful results from a capital budgeting problem, as stated above the estimates for value must be uniform for all proposals (Dean 1951). The combat capability metric used in this analysis was the most important criterion. This metric was developed by using QFD to link each of the modification projects to the strategies to task framework, and to develop uniform measures of value for each proposed modification. Early in the project, during discussions with the senior leadership, the Commander of ACC drew a chart similar to Figure 11 below. The point was made during the discussion that one should be able to plot the capability versus the cost for each project and that a good selection process would pick those projects which would yield the best value. Thus, the logical, defensible and acceptable answer in this case is the set of alternatives which give the most capability for the least cost.

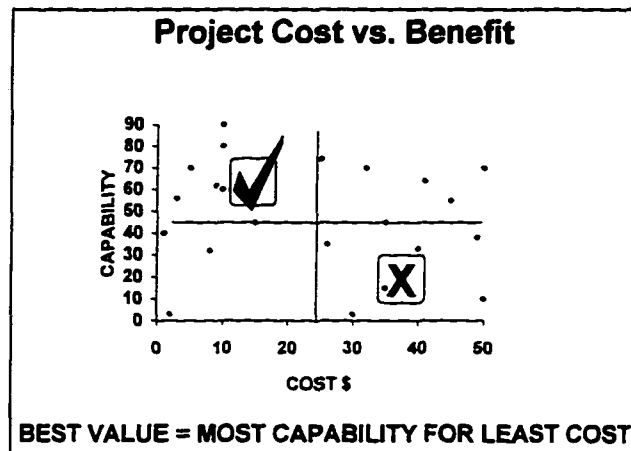


Figure 11 - Cost vs. Benefit

Using the QFD approach described above in Figures 5 through 7, this result was achieved. The magnitude of the combat capability scores adequately distinguished the importance of the projects, so that those which were expensive were only selected if their respective capability value was very high. Of course, as mentioned above there were other objectives which were considered such as reducing O&S cost, minimizing technical risk and maximizing cost sharing opportunities. The metric for each of these objectives also influenced the selection of alternatives in the goal programming model

outcome. The combat capability metric, however, was the objective which appeared to be of paramount importance, both in terms of development effort and management emphasis. Therefore, it was essential that the QFD score representing this metric exhibit the desired behavior.

Figure 12 below shows an actual example with nine projects of varying cost and capability values (QFD Weights). Circles represent projects which were selected and "X" represents projects which were not. Specific project names are not given due to sensitivities about cost. Notice that the project, Mod 15 and Mod 44 are about equal in capability, but Mod 44 is more expensive. Thus it makes sense that Mod 15 would be selected. Mod 33 and Mod 21 are about the same cost, however, Mod 33 is significantly greater in capability (QFD Weight) than Mod 21. Thus Mod 33 is selected in this instance.

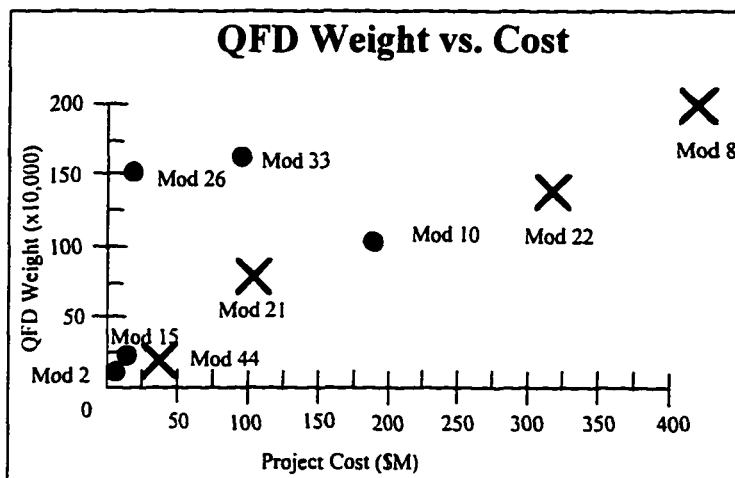


Figure 12 - QFD Weight vs. Cost

In Appendix B there are seven charts which give more detailed examples of this phenomenon. In general, it is obvious why different modifications were selected and others were not. Other forces were at work, such as the fact that there was a separate budget for each year. If a project required a large outlay in one particular year when the budget was tight, then chances were that the project would not get selected. Also, as discussed above there were over 100 interdependency relationships among

the various projects. So some of the projects were mutually exclusive and some were codependent. Both of these facts directly affected which projects were selected.

QFD and Integer Goal Programming can be run interactively, even for large scale problems. By taking advantage of the available technology, and by exploring the available options in the solver, SAS/OR (SAS 1989), the cycle time was reduced dramatically. Initially, the Microsoft Excel spreadsheets were copied to a series of about 10 diskettes and moved from machine to machine to transfer the necessary information. This method was extremely time-consuming and error-prone. Thus to generate a scenario to run for the GP model, it took essentially an entire morning or afternoon just to prepare the input file from the different spreadsheets. Then, once this was done, there was the problem of solving this large integer problem. Early editions of the code took 10 hours to run on a 100Mhz pentium personal computer system, and required at least 200 Megabytes of free disk space. Obviously, if this tool was to be usable, the cycle time had to be reduced. There were three primary enhancements introduced to reduce the cycle time.

The first place to realize a time savings was in preparing and transmitting the data for the GP. First, Excel had a capability to link different spreadsheets together, which required a good deal of work up front, but would pay substantial dividends later. By linking the output of the spreadsheets which computed the combat capability score, and spreadsheets which contained the cost data, the "cutting and pasting" operation was eliminated. Thus the generation of a linear programming tableau was nearly automatic. Thus whenever any change was made to the QFD calculations, only "dragging and dropping" was required to connect the spreadsheets.

The second significant improvement was the movement of the headquarters to a local area network. This technology leap preempted the requirement to carry stacks of diskettes from one place to another to move information. The timely creation of the LAN provided a medium for again "dragging and dropping" files to move them from one place to another. Common LAN servers were made available to the members of the team that provided data or acted on that data.

Finally, the time required to solve the large integer goal programming model was reduced. As noted in the literature review, large integer problems can be troublesome to solve. The only way to

attack the time aspect is to experiment with the options provided by the commercial solver (SAS/OR) and the structure of the problem. SAS (SAS 1989) provided various options to use in working with integer models. One such option, *pobjective*, allowed the analyst to specify that the model only consider nodes which could lead to an integer solution within a certain range (percentage) of the objective function value from the relaxed solution. This option effectively prunes the branch and bound tree and limits the search of the solver, which can save time.

By performing analysis with the available solver options, and restructuring some of the constraint equations, the run time for the GP model was reduced to less than one hour. On average, the model would solve in about 40 minutes, and sometimes as quickly as 10 minutes. As stated in the SAS documentation (SAS 1989), the time varies with the problem structure, and the branch and bound search strategy and cannot be predicted. However, by spending some time tailoring the search options to fit a specific problem, some increase in efficiency may be possible.

Thus, QFD and Integer Goal Programming can be run interactively for a large problem. Using the changes described above, the cycle time was reduced for running a complete problem from about one per day, to about six executions per day. As the PC technology continues to evolve, there is potential to run larger problems, and to solve them even faster.

The results should provide usable, responsive information to decision makers. The spreadsheet below, Table 3, shows example summary output. The chart shows eight different runs of the GP model in the columns following the ID Number. This was one of the primary output formats used by decision makers. For each run, typically there was a baseline, meaning at the projected budget amounts for each year, and budget amounts which vary from the baseline, e.g. -10%, or -20%, etc.

| ID NUMBE | b18jan01 | b19jan02 =1.0 | b19jan01 = 0.9 | b19jan03 = 0.8 | sun19jan overspend | d21feb01 baseline, qfd 10, coo 5, le, Falcon Up | d21feb02 -10%\$, qfd 10, coo 5, le, Falcon Up | b21feb02 -40%\$, qfd 10, coo 5, le, Falcon Up |
|----------|----------|------------------|-------------------|-------------------|-----------------------|---|---|---|
| F15C041 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 |
| F15C042 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| F15C043 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| F15C044 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| F15C045 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| F15C046 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 0 |
| F15C047 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| F15C048 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| F15C049 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 0 |
| F15C050 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

Table 3 - Sample Summary Output

Other parameters were also varied. The weights assigned to the different goals, the deviational variable objective function coefficients, were adjusted according to senior leadership direction. The cases given in this example used a coefficient of 10 for the QFD weight, five for the cost of ownership value, and one for the technical risk and cost sharing. The scenario parameters were recorded for each column, and an abbreviated form was listed at the top of the column for quick reference. The way this summary spreadsheet was used was to look at the changes in the parameters, and look at the value of the decision variable for each modification program. If a program was always selected (decision variable=1), across every scenario, then this indicated that this project was a likely core requirement. In other words if the budget is reduced, it is still important. If the priorities among the goals change, and it is still selected, then it has merit under a variety of potential circumstances. The third project on this list, F15C043, has these qualities from this summary. On the other hand, F15C042 has just the opposite outcome. It is never selected by the GP model. Thus, under any of the scenarios above, this project is not a cost effective option. The data and model indicate that this would not be part of a recommended investment plan. Then there are those projects which are in the gray area. F15C041 is a good example. This project would be selected in most cases, however, if the budget gets reduced then this project becomes

a less cost-effective option. This proved to be an effective way of examining possible perturbations and developing an understanding of the relative importance of different options.

The senior leadership gave direction for setting the weights of the GP model to gain a sense of why different programs were selected and recommended. Sometimes a program would be included in the baseline and fall out if the cost of ownership weight was reduced, indicating that it's value was highly dependent on the fact that the proposed project had a significant O&S cost savings. In fact, some projects with low combat capability values were selected because of their potential to save the Air Force O&S expenditures in the future. There were projects which were cost-effective choices because of both the combat capability score and the cost of ownership value. These projects were selected no matter how the weights were adjusted. The chart below, Figure 13 shows how the data was summarized and presented to leadership in the form of a plan for modernizing and sustaining each aircraft type.

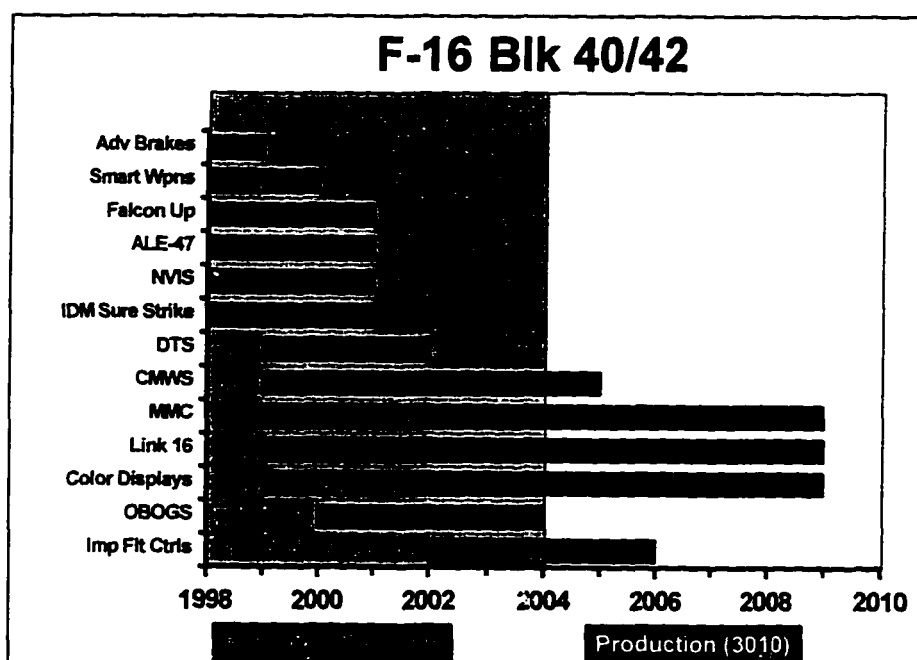


Figure 13 - Sample F-16 Plan

The findings of this research demonstrate the capacity for decision support tools to effectively deal with large complex problems. The confederation of QFD, integer goal programming, and capital budgeting provides a systematic approach to the resource allocation problem. QFD can be used to develop technological parameter estimates for qualitative objectives, such as combat capability. Integer goal programming is an efficient method to resolve conflicting objectives of management in capital budgeting decision. The analyst must be cognizant of methods and technologies which lend themselves to improving the responsiveness of these tools and must work with management to make the output meaningful.

CONCLUSIONS

The literature demonstrates that mathematical modeling in capital budgeting problems in industry is a well-established process. This research has demonstrated that these powerful techniques can be applied to government and other non-profit seeking organizations as well. Non-economic measures can be developed with careful, deliberate analysis of the goals of the organization. QFD can help in developing the prioritization and weighting, as well as estimating technological parameters for a GP model. Decision support tools such as the one described in this thesis, can be developed and used in a responsive manner to assist in the development of plans in a rapidly changing environment. This capital budgeting model was run over 300 times performing different sensitivity analyses and refining inputs. The important point here is that the key decision makers were involved in an interactive role, changing priorities (goal weights), changing projected budget amounts, and formulating plans based on objective, quantifiable, traceable, repeatable output.

Two important lessons were derived from this analysis. First, there must be “buy-in” and acceptance of the methodology by senior management personnel, and other stake holders. Marketing of the process is a never-ending task. Leadership must be convinced that the philosophy and methodology is sound. Above all, the process must be *understandable*. Stakeholders must be convinced that the methodology addresses their functional areas in a fair and equitable manner, and that

it is in their best interest to participate. Secondly, the model does not *make* decisions, but rather *suggests* “optimized” investment plans. Expectations should be managed. This methodology is not a *crystal ball*, which knows all. The output of the model required sanity checks, by an integrated team of analysts and functional experts (e.g. pilots). The model was refined to provide results which are consistent with sound judgment by improving inputs such as cost, cost of ownership, combat capability metrics, and goal importance weights. However, there were still intangibles which the model did not capture such as legislation requiring changes to aircraft navigation systems. These exceptions were processed during the analysis of the results of the optimization. The key benefit of this work was that the command now has a tool which contains collective wisdom, qualitative and quantitative data, and an engine (goal programming) which allowed multiple excursions to be performed quickly. Senior leadership now has the ability to quickly respond to changes in the budget and various programs, through this automated, capital budgeting process.

The most encouraging fact that these tools are useful comes after the work is complete and the plans are adopted and carried forward to the budgeting phase. The results of this research were used by Air Combat Command in preparation and defense of the command’s POM submission. This method has revolutionized the way the command did business in analyzing, preparing and defending it’s position, and has now been expanded into several other areas. On July 3, 1996 COMACC released the document titled Fighter Configuration Plan (FICOP 96) Release to Industry, which explained the methodology and gave specific, detailed results to industry.

DEVELOPMENTS ADDED BY THIS RESEARCH

The developments of this research have contributed to the investigated areas in varying degrees. Capital budgeting developments: An approach was developed to capture, integrate and prioritize collective wisdom into development of measures for non-profit organizations. QFD Developments: Prioritization using the structured expanded house of quality can produce acceptable customer-based priorities, if done correctly. This is accomplished through a well-designed, logical matrix flow where the evaluation team is guided through the process by trained facilitators. Goal Programming developments: A novel method for estimating technological parameters was developed.

Solving large integer problems has long been a troublesome challenge. It is possible to solve large-scale integer goal programming problems efficiently and obtain a solution in a relatively short time. The technology has dramatically changed over the past 23 years with desktop PC's which are significantly more capable than some of the older mainframe computers. Large integer problems are most commonly solved with the branch-and-bound solution method. Due to computational requirements, this class of problems can be difficult to solve and would not have been feasible to run in the early years of Goal Programming (GP). However, this problem which had up to 450 integer, decision variables and over 120 constraints was successfully executed on a pentium PC and generally solved within 30 minutes.

FUTURE RESEARCH

The area of capital budgeting in strategic planning activities provides a rich environment for follow-on research. The questions are very old, but the development of scientific methods and the technological advances permit the application of efficient, responsive decision support systems in new and imaginative ways. Perhaps the *crystal ball* is not as far off as one might think. There appears to be a high degree of interest in applying these types of methods to a broader problem involving initiatives and programs from across the spectrum, not only fighter modifications. There are some interesting areas which might be helpful to study in the future.

Time value of capability: Economic analyses use the net present value to capture and account for the fact that cash available in the near future is worth more than the same amount of cash at some distant point in the future. Using a non-economic measure of value, in this case, combat capability, poses an interesting question which is analogous to the idea of the time value of money. Should there be a "capability discount factor" applied to programs over the multiple years for which these program span. Using QFD, it was possible to prioritize and weight the alternatives. If there was a way to efficiently develop time-based value weights, then it would be possible to make trade-offs across the time-horizon as well as within a given year. This would allow the process to consider the rate at which technologies become obsolete, as well as the cumulative expected value of each alternative based on the remaining service life of the system.

Knowledge-Based, Goal Programming: As mentioned above, the GP model was run in excess of 300 times, performing different excursions and sensitivity analysis. There is a wealth of knowledge which is derived from an iterative analytical approach. It would have been extremely helpful to have the results of the optimization, the inputs, and the decision maker's judgment somehow captured and used to form either new goals or new constraints. This would help the results of the ultimate model to "learn" from early runs and also become more stable. This idea would allow analysts to capture relevant output data and turn it into useable information. Decision makers would perhaps become even more comfortable, if the model reached a steady state and was not so erratic.

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EDUCATION

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APPENDIX A

FICOP 96 STRATEGY TO TASK

Campaign Objectives

Establish aerospace supremacy
 Establish maritime supremacy
 Counter weapons of mass destruction
 Degrade war sustaining capability
 Defeat ground forces

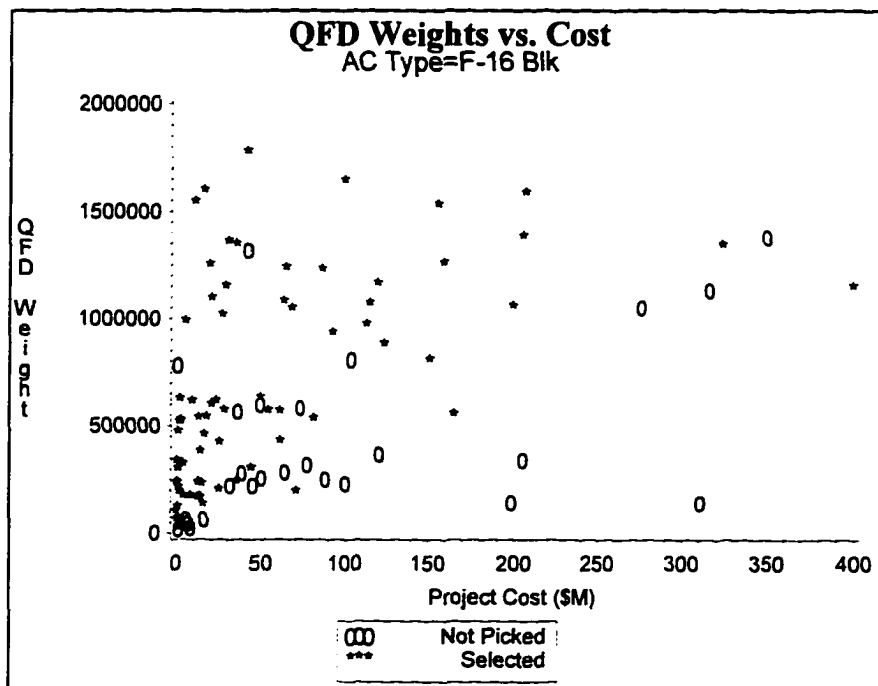
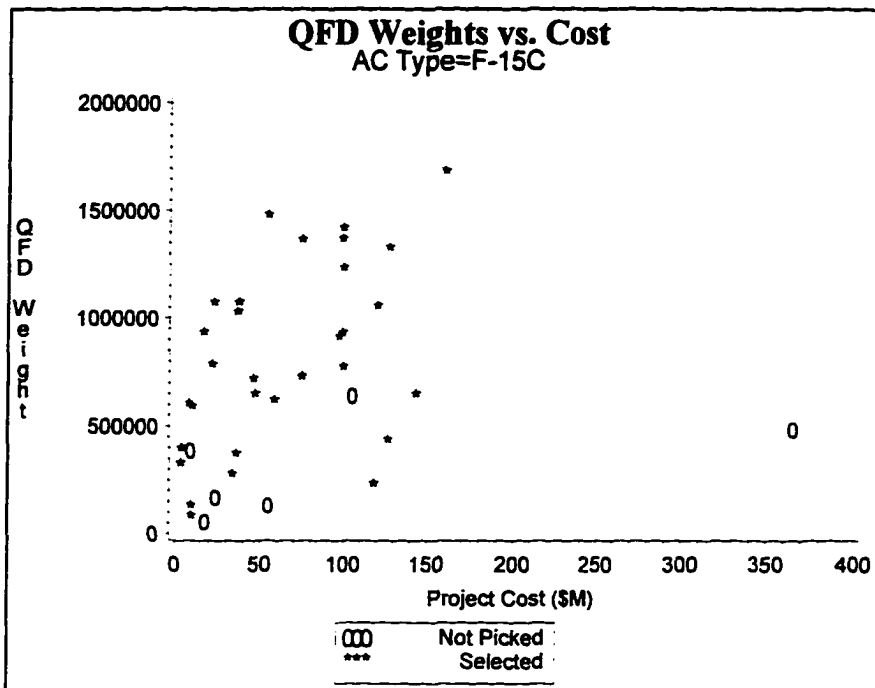
Operational Objectives

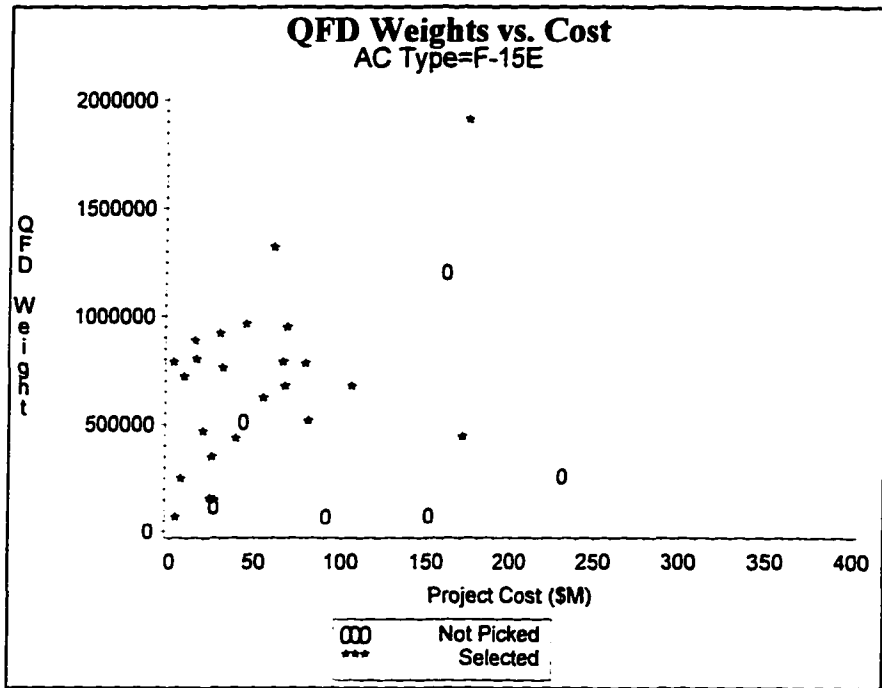
Defeat enemy in the air
 Counter enemy air defenses
 Reduce enemy sortie generation
 Interdict ground forces
 Degrade enemy command & control
 Interdict naval forces
 Degrade military support base
 Sustain operations tempo
 Defeat enemy close to friendlies
 Deny economic support base
 Establish information dominance
 Rapidly deploy an overwhelming force
 Protect forces and friendly vulnerabilities
 Disrupt political base

Operational Tasks

Produce aircraft sorties
 Repair equipment, tools, spares
 Resupply munitions, spares, consumables, POL
 Destroy/damage/suppress mobile surface to air threats
 Pack/configure/assemble personnel & supplies
 Destroy/damage/suppress fixed surface to air threats
 Collect intelligence data
 Disseminate intelligence data
 Destroy/damage/neutralize TMs & support on the ground
 Destroy/damage/neutralize TMs inflight
 Preposition equipment and supplies.
 Sustain efficient operations
 Deliver/maintain timely flow of personnel & supplies
 Train personnel
 Destroy/disable/neutralize fighter aircraft inflight
 Destroy/disable/neutralize helicopters inflight
 Destroy/damage/neutralize lines of communication (LOCs)
 Destroy/degrade/neutralize radar and comm (EW/GCI)
 Destroy/damage/neutralize power production
 Destroy/damage/neutralize advancing combat forces
 Destroy/disable/neutralize heavy aircraft inflight
 Destroy/disable/neutralize cruise missiles & UAVs inflight

Destroy/damage/neutralize aircraft on the ground
Destroy/disable/neutralize engaged ground forces
Destroy/damage/neutralize national C4I
Destroy/damage/neutralize ports & harbors
Perform psychological operations
Neutralize enemy political and military leaders
Destroy/neutralize/deny access to WMD production & storage
Destroy/damage/neutralize airfield operating surfaces
Destroy/disable/neutralize fixed forces
Destroy/damage/neutralize industrial production
Provide warning of ballistic missile and air attack
Destroy/damage/neutralize weapons factories
Destroy/damage/neutralize naval vessels
Destroy/damage/neutralize naval support facilities
Identify/assess air sovereignty threat
Destroy/damage/neutralize mobile C2 with advancing forces
Recover Downed aircrew/isolated personnel
Destroy/damage/neutralize weapons storage sites
Destroy/damage/neutralize airfield support facilities
Destroy/disable/neutralize satellites
Conduct/coordinate airborne airstrike terminal control
Conduct/coordinate groundbased airstrike terminal control
Protect rescue operations
Escort air sovereignty threat





APPENDIX C

SAS/OR CODE OPTIONS

The following is the SAS code used to execute the model:

```
proc lp data=copdata.lpdata maxit1=200000 maxit2=200000 time=43200 imaxit=200000
      printfreq=9999999 primalout=copdata.solfr1 canselect=obj
      varselect=penalty penaltydepth=12 backtrack=project
      ifeasiblepause=1 pobjective=.03;
run;
reset canselect=obj backtrack=project ifeasiblepause=9999999 printfreq=99999999;
run;
```

The options of interest are canselect, varselect, penaltydepth, and pobjective. The canselect option controls the rule used to choose the next active problem when solving an integer problem. Canselect typical options are LIFO (last-in, first out), FIFO (first-in, first out), OBJ (chooses the problem whose parent has the least objective value), and PROJECT (chooses the project with the least project objective value). The varselect option controls the strategy for searching the branch and bound tree. The default option is varselect=far, which means that the strategy should use the variable to branch on which has a value farthest from an integer value. The option chosen in the code above, varselect=penalty, causes the LP to look at the cost of branching on an integer variable, in terms of the objective function. This option at times improved the solution time by cutting down the number of integer iterations. Penaltydepth is used in conjunction with the varselect=penalty option. Penaltydepth assigns the number of variables to be used as branching candidates. Pobjective is another key option which can have a significant impact on the running time. Pobjective tells the model to ignore active nodes unless the node could lead to an integer solution with an objective value at least as small as $r+p|r$. In this example p is the fractional range specified in Pobjective= p , and r is the objective of the relaxed non-integer constrained problem. In the above example $p=0.03$, which means the model will only consider nodes which could lead to an integer solution within 3% of the objective function value from the relaxed

solution. Of course, this option effectively prunes the tree and could possibly cut-off sections of the branch and bound tree that may contain an optimal solution.

APPENDIX D

SAS SAMPLE OUTPUT

LINEAR PROGRAMMING PROCEDURE

PROBLEM SUMMARY

| | |
|-----------------|--------------------|
| Min OBJECT | Objective Function |
| RHS | Rhs Variable |
| TYPE | Type Variable |
| Problem Density | 0.040588 |

| Variable Type | Number |
|---------------|--------|
| Non-negative | 44 |
| Binary | 476 |
| Slack | 47 |
| Surplus | 62 |
| Total | 629 |

| Constraint Type | Number |
|-----------------|--------|
| LE | 47 |
| EQ | 8 |
| GE | 62 |
| Objective | 1 |
| Total | 118 |

SOLUTION SUMMARY

Integer Optimal Solution

| | |
|----------------------------------|------------------|
| Objective value | 9222.042 |
| Phase 1 iterations | 368 |
| Phase 2 iterations | 115 |
| Phase 3 iterations | 122400 |
| Integer iterations | 8072 |
| Integer solutions | 1 |
| Initial basic feasible variables | 112 |
| Time used (secs) | 2298 |
| Number of inversions | 8043 |
| Machine epsilon | 1E-8 |
| Machine infinity | 1.7976931349E308 |
| Maximum phase 1 iterations | 200000 |
| Maximum phase 2 iterations | 200000 |
| Maximum phase 3 iterations | 99999999 |
| Maximum integer iterations | 200000 |
| Time limit (secs) | 43200 |

The SAS System

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09:30 Wednesday, February

21, 1996

LINEAR PROGRAMMING PROCEDURE

VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|---------|----------|----------|--------------|
| 1 | D98U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 2 | D98V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 3 | D99U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 4 | D99V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 5 | D00U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 6 | D00V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 7 | D01U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 8 | D01V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 9 | D02U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 10 | D02V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 11 | D03U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 12 | D03V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 13 | D04U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 14 | D04V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 15 | D05U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 16 | D05V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 17 | D06U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 18 | D06V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 19 | D07U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 20 | D07V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 21 | D08U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 22 | D08V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 23 | D09U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 24 | D09V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 25 | D10U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 26 | D10V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 27 | D11U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 28 | D11V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 29 | D12U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 30 | D12V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 31 | D13U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 32 | D13V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 33 | D14U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 34 | D14V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 35 | D15U | | NON-NEG | 1 | 0.000000 | 1.000000 |
| 36 | D15V | ALTER | NON-NEG | 0 | 0.000000 | 0.000000 |
| 37 | DWU | BASIC | NON-NEG | 0.000071 | 79311201 | 0.000000 |
| 38 | DWV | | NON-NEG | 0 | 0.000000 | 0.000071 |
| 39 | DTU | | NON-NEG | 0 | 0.000000 | 1.930000 |
| 40 | DTV | BASIC | NON-NEG | 1.93 | 295.000 | 0.000000 |
| 41 | DJU | BASIC | NON-NEG | 1 | 580.000 | 0.000000 |
| 42 | DJV | | NON-NEG | 0 | 0.000000 | 1.000000 |

The SAS System

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09:30 Wednesday, February

21, 1996

LINEAR PROGRAMMING PROCEDURE

VARIABLE SUMMARY

| Variable Col Name | Status | Type | Price | Activity | Reduced Cost |
|----------------------|--------|---------|-------|----------|-----------------|
| 43 DCU | BASIC | NON-NEG | 1.74 | 1403.216 | 0.000000 |
| 44 DCV | | NON-NEG | 0 | 0.000000 | 1.740000 |
| 45 A100001 | | BINARY | 0 | 1.000000 | -46.447981 |
| 46 A100002 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 47 A100003 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 48 A100004 | | BINARY | 0 | 0.000000 | -12.769776 |
| 49 A100005 | | BINARY | 0 | 1.000000 | -186.922 |
| 50 A100006 | | BINARY | 0 | 0.000000 | 19298.070 |
| 51 A100007 | | BINARY | 0 | 1.000000 | -26.809534 |
| 52 A100008 | | BINARY | 0 | 1.000000 | -21.327903 |
| 53 A100009 | | BINARY | 0 | 1.000000 | -63.140731 |
| 54 A100010 | | BINARY | 0 | 1.000000 | -59.491580 |
| 55 A100011 | | BINARY | 0 | 1.000000 | -67.796659 |
| 56 A100012 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 57 A100013 | | BINARY | 0 | 1.000000 | -123.760 |
| 58 A100014 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 59 A100015 | | BINARY | 0 | 0.000000 | 19150.193 |
| 60 A100016 | | BINARY | 0 | 1.000000 | -98.484567 |
| 61 A100017 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 62 A100018 | | BINARY | 0 | 1.000000 | -55.874728 |
| 63 A100019 | | BINARY | 0 | 1.000000 | -59.205121 |
| 64 A100020 | | BINARY | 0 | 1.000000 | -23.778757 |
| 65 A100021 | | BINARY | 0 | 0.000000 | -4.095818 |
| 66 A100022 | | BINARY | 0 | 0.000000 | -27.940139 |
| 67 A100023 | | BINARY | 0 | 0.000000 | -80.927865 |
| 68 A100026 | | BINARY | 0 | 0.000000 | 5.054951 |
| 69 A100027 | | BINARY | 0 | 1.000000 | -16.746562 |
| 70 A100028 | | BINARY | 0 | 0.000000 | -1.124179 |
| 71 A100029 | | BINARY | 0 | 0.000000 | -2.817351 |
| 72 A100030 | | BINARY | 0 | 0.000000 | 5.841560 |
| 73 A100031 | | BINARY | 0 | 1.000000 | -55.365516 |
| 74 A100032 | | BINARY | 0 | 0.000000 | 19705.706 |
| 75 A100033 | | BINARY | 0 | 0.000000 | 19298.070 |
| 76 A100034 | | BINARY | 0 | 1.000000 | -176.891 |
| 77 A100035 | | BINARY | 0 | 0.000000 | 19298.070 |
| 78 A100036 | | BINARY | 0 | 0.000000 | 19298.070 |
| 79 A100037 | | BINARY | 0 | 0.000000 | 19298.070 |
| 80 A100038 | | BINARY | 0 | 0.000000 | 19298.070 |
| 81 A100039 | | BINARY | 0 | 0.000000 | 19298.070 |
| 82 A100040 | | BINARY | 0 | 0.000000 | 19298.070 |
| 83 A100041 | | BINARY | 0 | 0.000000 | 19298.070 |
| 84 A100042 | | BINARY | 0 | 0.000000 | 19298.070 |

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LINEAR PROGRAMMING PROCEDURE

VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|--------|-------|----------|--------------|
| 85 | ENGN002 | | BINARY | 0 | 1.000000 | -35.347239 |
| 86 | ENGN003 | | BINARY | 0 | 1.000000 | -5.667291 |
| 87 | ENGN004 | | BINARY | 0 | 1.000000 | -20.849754 |
| 88 | ENGN005 | | BINARY | 0 | 0.000000 | -160.442 |
| 89 | ENGN006 | | BINARY | 0 | 1.000000 | -9.409803 |
| 90 | ENGN007 | | BINARY | 0 | 1.000000 | -19.200250 |
| 91 | ENGN008 | | BINARY | 0 | 1.000000 | -12.330219 |
| 92 | ENGN009 | | BINARY | 0 | 0.000000 | -5.707819 |
| 93 | ENGN010 | | BINARY | 0 | 1.000000 | -2.559195 |
| 94 | ENGN011 | | BINARY | 0 | 0.000000 | 2.564555 |
| 95 | ENGN012 | | BINARY | 0 | 1.000000 | -9.279036 |
| 96 | ENGN013 | | BINARY | 0 | 1.000000 | -51.105481 |
| 97 | ENGN014 | | BINARY | 0 | 1.000000 | -344.884 |
| 98 | ENGN015 | | BINARY | 0 | 1.000000 | -559.171 |
| 99 | ENGN016 | | BINARY | 0 | 1.000000 | -36.190703 |
| 100 | ENGN017 | | BINARY | 0 | 1.000000 | -14.601789 |
| 101 | ENGN018 | | BINARY | 0 | 1.000000 | -289.719 |
| 102 | ENGN019 | | BINARY | 0 | 1.000000 | -87.148326 |
| 103 | ENGN020 | | BINARY | 0 | 1.000000 | -3.119619 |
| 104 | ENGN021 | | BINARY | 0 | 1.000000 | -14.579424 |
| 105 | ENGN022 | | BINARY | 0 | 1.000000 | -657.698 |
| 106 | ENGN023 | | BINARY | 0 | 1.000000 | -182.687 |
| 107 | ENGN024 | | BINARY | 0 | 0.000000 | -10.643610 |
| 108 | ENGN025 | | BINARY | 0 | 1.000000 | -18.544774 |
| 109 | ENGN026 | | BINARY | 0 | 0.000000 | -18.165670 |
| 110 | ENGN027 | | BINARY | 0 | 1.000000 | -5.912262 |
| 111 | ENGN028 | | BINARY | 0 | 1.000000 | -16.970083 |
| 112 | ENGN029 | | BINARY | 0 | 1.000000 | -1.709754 |
| 113 | ENGN030 | | BINARY | 0 | 1.000000 | -1.205154 |
| 114 | ENGN031 | | BINARY | 0 | 1.000000 | -1.205154 |
| 115 | ENGN032 | | BINARY | 0 | 1.000000 | -1.205154 |
| 116 | ENGN033 | | BINARY | 0 | 1.000000 | -15.036789 |
| 117 | ENGN034 | | BINARY | 0 | 0.000000 | 19282.375 |
| 118 | ENGN035 | | BINARY | 0 | 1.000000 | -8.078154 |
| 119 | ENGN036 | | BINARY | 0 | 1.000000 | -277.897 |
| 120 | ENGN037 | | BINARY | 0 | 1.000000 | -4.572462 |
| 121 | ENGN038 | | BINARY | 0 | 1.000000 | -10.917315 |
| 122 | ENGN039 | | BINARY | 0 | 0.000000 | 11.392233 |
| 123 | ENGN040 | | BINARY | 0 | 0.000000 | 19298.070 |
| 124 | ENGN041 | | BINARY | 0 | 0.000000 | 19298.070 |
| 125 | ENGN042 | | BINARY | 0 | 0.000000 | 19298.070 |
| 126 | ENGN043 | | BINARY | 0 | 0.000000 | 19298.070 |

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L I N E A R P R O G R A M M I N G P R O C E D U R E
V A R I A B L E S U M M A R Y

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|--------|-------|----------|--------------|
| 127 | ENGN044 | | BINARY | 0 | 0.000000 | 19298.070 |
| 128 | ENGN045 | | BINARY | 0 | 0.000000 | 19298.070 |
| 129 | ENGN046 | | BINARY | 0 | 0.000000 | 19298.070 |
| 130 | ENGN047 | | BINARY | 0 | 0.000000 | 19298.070 |
| 131 | ENGN048 | | BINARY | 0 | 0.000000 | 19298.070 |
| 132 | ENGN049 | | BINARY | 0 | 0.000000 | 19298.070 |
| 133 | ENGN050 | | BINARY | 0 | 0.000000 | 19298.070 |
| 134 | ENGN051 | | BINARY | 0 | 0.000000 | 19298.070 |
| 135 | ENGN052 | | BINARY | 0 | 0.000000 | 19298.070 |
| 136 | F117001 | | BINARY | 0 | 1.000000 | -59.920251 |
| 137 | F117002 | | BINARY | 0 | 0.000000 | -15.809499 |
| 138 | F117003 | | BINARY | 0 | 0.000000 | -20.935344 |
| 139 | F117004 | | BINARY | 0 | 1.000000 | -22.191334 |
| 140 | F117005 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 141 | F117006 | | BINARY | 0 | 1.000000 | -71.692081 |
| 142 | F117007 | | BINARY | 0 | 1.000000 | -147.868 |
| 143 | F117008 | | BINARY | 0 | 1.000000 | -59.253831 |
| 144 | F117009 | | BINARY | 0 | 1.000000 | -34.773462 |
| 145 | F117010 | | BINARY | 0 | 0.000000 | 19298.070 |
| 146 | F117011 | | BINARY | 0 | 0.000000 | 19237.414 |
| 147 | F117012 | | BINARY | 0 | 0.000000 | 19298.070 |
| 148 | F117013 | | BINARY | 0 | 1.000000 | -56.423680 |
| 149 | F117014 | | BINARY | 0 | 1.000000 | -33.147508 |
| 150 | F117015 | | BINARY | 0 | 1.000000 | -5.003583 |
| 151 | F117016 | | BINARY | 0 | 1.000000 | -42.136563 |
| 152 | F117017 | | BINARY | 0 | 1.000000 | -17.537355 |
| 153 | F117018 | | BINARY | 0 | 1.000000 | -10.846386 |
| 154 | F117019 | | BINARY | 0 | 1.000000 | -17.537355 |
| 155 | F117020 | | BINARY | 0 | 1.000000 | -38.597908 |
| 156 | F117021 | | BINARY | 0 | 0.000000 | -102.886 |
| 157 | F117022 | | BINARY | 0 | 0.000000 | -0.035075 |
| 158 | F117023 | | BINARY | 0 | 0.000000 | -29.819574 |
| 159 | F117024 | | BINARY | 0 | 0.000000 | -16.549000 |
| 160 | F117025 | | BINARY | 0 | 0.000000 | 19298.070 |
| 161 | F117027 | | BINARY | 0 | 0.000000 | -23.863591 |
| 162 | F117028 | | BINARY | 0 | 1.000000 | -9.362868 |
| 163 | F117029 | | BINARY | 0 | 0.000000 | 19285.490 |
| 164 | F117030 | | BINARY | 0 | 1.000000 | -43.277092 |
| 165 | F117031 | | BINARY | 0 | 1.000000 | -6.062193 |
| 166 | F117032 | | BINARY | 0 | 1.000000 | -5.330041 |
| 167 | F117033 | | BINARY | 0 | 1.000000 | -3.808440 |
| 168 | F117035 | | BINARY | 0 | 1.000000 | -32.270497 |

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LINEAR PROGRAMMING PROCEDURE

VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|--------|-------|----------|--------------|
| 169 | F117036 | | BINARY | 0 | 1.000000 | -85.708183 |
| 170 | F117037 | | BINARY | 0 | 1.000000 | -0.073663 |
| 171 | F117038 | | BINARY | 0 | 0.000000 | 2.033120 |
| 172 | F117039 | | BINARY | 0 | 1.000000 | -5.329438 |
| 173 | F117040 | | BINARY | 0 | 0.000000 | 3.504524 |
| 174 | F117041 | | BINARY | 0 | 1.000000 | -15.411026 |
| 175 | F117042 | | BINARY | 0 | 1.000000 | -17.046745 |
| 176 | F117044 | | BINARY | 0 | 0.000000 | 2.400758 |
| 177 | F117046 | | BINARY | 0 | 0.000000 | 5.548259 |
| 178 | F117047 | | BINARY | 0 | 0.000000 | 5.548259 |
| 179 | F117048 | | BINARY | 0 | 1.000000 | -78.366073 |
| 180 | F117049 | | BINARY | 0 | 1.000000 | -206.964 |
| 181 | F117050 | | BINARY | 0 | 1.000000 | -32.539158 |
| 182 | F117051 | | BINARY | 0 | 1.000000 | -69.510594 |
| 183 | F117052 | | BINARY | 0 | 1.000000 | -115.636 |
| 184 | F117053 | | BINARY | 0 | 1.000000 | -32.392297 |
| 185 | F117054 | | BINARY | 0 | 1.000000 | -23.812089 |
| 186 | F117055 | | BINARY | 0 | 1.000000 | -20.392468 |
| 187 | F117056 | | BINARY | 0 | 1.000000 | -272.766 |
| 188 | F117057 | | BINARY | 0 | 1.000000 | -209.009 |
| 189 | F117058 | | BINARY | 0 | 1.000000 | -104.753 |
| 190 | F117059 | | BINARY | 0 | 0.000000 | -27.874996 |
| 191 | F117060 | | BINARY | 0 | 0.000000 | 19298.070 |
| 192 | F117061 | | BINARY | 0 | 0.000000 | 19298.070 |
| 193 | F117062 | | BINARY | 0 | 0.000000 | 19298.070 |
| 194 | F117063 | | BINARY | 0 | 0.000000 | 19298.070 |
| 195 | F117064 | | BINARY | 0 | 0.000000 | 19298.070 |
| 196 | F117065 | | BINARY | 0 | 0.000000 | 19298.070 |
| 197 | F15A003 | | BINARY | 0 | 1.000000 | -25.296311 |
| 198 | F15A004 | | BINARY | 0 | 0.000000 | 19298.070 |
| 199 | F15A005 | | BINARY | 0 | 0.000000 | 19298.070 |
| 200 | F15A006 | | BINARY | 0 | 0.000000 | 19298.070 |
| 201 | F15A008 | | BINARY | 0 | 0.000000 | 19298.070 |
| 202 | F15A009 | | BINARY | 0 | 1.000000 | -67.388210 |
| 203 | F15A010 | | BINARY | 0 | 1.000000 | -12.826612 |
| 204 | F15A011 | | BINARY | 0 | 0.000000 | 19298.070 |
| 205 | F15A012 | | BINARY | 0 | 0.000000 | 19298.070 |
| 206 | F15A013 | | BINARY | 0 | 1.000000 | -40.724535 |
| 207 | F15A015 | | BINARY | 0 | 0.000000 | 19298.070 |
| 208 | F15A017 | | BINARY | 0 | 0.000000 | 19298.070 |
| 209 | F15A018 | | BINARY | 0 | 0.000000 | 19298.070 |
| 210 | F15A019 | | BINARY | 0 | 0.000000 | 19298.070 |

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VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|--------|-------|----------|--------------|
| 211 | F15A020 | | BINARY | 0 | 0.000000 | 19298.070 |
| 212 | F15A021 | | BINARY | 0 | 1.000000 | -82.972309 |
| 213 | F15A022 | | BINARY | 0 | 1.000000 | -80.000746 |
| 214 | F15A023 | | BINARY | 0 | 1.000000 | -17.907975 |
| 215 | F15A024 | | BINARY | 0 | 0.000000 | 19298.070 |
| 216 | F15A025 | | BINARY | 0 | 0.000000 | 19298.070 |
| 217 | F15A026 | | BINARY | 0 | 1.000000 | -23.440011 |
| 218 | F15A027 | | BINARY | 0 | 1.000000 | -30.750917 |
| 219 | F15A028 | | BINARY | 0 | 0.000000 | 19298.070 |
| 220 | F15A029 | | BINARY | 0 | 1.000000 | -88.387763 |
| 221 | F15A030 | | BINARY | 0 | 0.000000 | 19298.070 |
| 222 | F15A032 | | BINARY | 0 | 0.000000 | 19298.070 |
| 223 | F15A033 | | BINARY | 0 | 0.000000 | 19298.070 |
| 224 | F15A035 | | BINARY | 0 | 1.000000 | -19.319739 |
| 225 | F15A036 | | BINARY | 0 | 0.000000 | 19298.070 |
| 226 | F15A037 | | BINARY | 0 | 0.000000 | 19298.070 |
| 227 | F15A038 | | BINARY | 0 | 0.000000 | 19298.070 |
| 228 | F15A039 | | BINARY | 0 | 0.000000 | 19298.070 |
| 229 | F15A040 | | BINARY | 0 | 0.000000 | 19298.070 |
| 230 | F15A041 | | BINARY | 0 | 0.000000 | 19298.070 |
| 231 | F15A042 | | BINARY | 0 | 0.000000 | 19298.070 |
| 232 | F15A043 | | BINARY | 0 | 0.000000 | 19298.070 |
| 233 | F15C003 | | BINARY | 0 | 1.000000 | -89.893353 |
| 234 | F15C004 | | BINARY | 0 | 1.000000 | -29.104751 |
| 235 | F15C005 | | BINARY | 0 | 1.000000 | -41.308794 |
| 236 | F15C006 | | BINARY | 0 | 0.000000 | -32.864876 |
| 237 | F15C007 | | BINARY | 0 | 0.000000 | -12.034287 |
| 238 | F15C008 | | BINARY | 0 | 1.000000 | -46.345649 |
| 239 | F15C009 | | BINARY | 0 | 0.000000 | 19298.070 |
| 240 | F15C010 | | BINARY | 0 | 1.000000 | -32.408980 |
| 241 | F15C011 | | BINARY | 0 | 1.000000 | -150.300 |
| 242 | F15C012 | | BINARY | 0 | 0.000000 | -15.417757 |
| 243 | F15C013 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 244 | F15C015 | | BINARY | 0 | 1.000000 | -55.766773 |
| 245 | F15C016 | | BINARY | 0 | 1.000000 | -87.058466 |
| 246 | F15C017 | | BINARY | 0 | 1.000000 | -409.352 |
| 247 | F15C018 | | BINARY | 0 | 1.000000 | -93.799916 |
| 248 | F15C019 | | BINARY | 0 | 0.000000 | 19298.070 |
| 249 | F15C020 | | BINARY | 0 | 1.000000 | -25.737429 |
| 250 | F15C022 | | BINARY | 0 | 0.000000 | 19298.070 |
| 251 | F15C024 | | BINARY | 0 | 0.000000 | -6.183781 |
| 252 | F15C026 | | BINARY | 0 | 0.000000 | -18.575167 |

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LINEAR PROGRAMMING PROCEDURE

VARIABLE SUMMARY

| Variable Col Name | Status | Type | Price | Activity | Reduced Cost |
|----------------------|--------|--------|-------|----------|-----------------|
| 253 F15C027 | | BINARY | 0 | 0.000000 | 19298.070 |
| 254 F15C028 | | BINARY | 0 | 0.000000 | -1260.633 |
| 255 F15C029 | | BINARY | 0 | 0.000000 | 19298.070 |
| 256 F15C030 | | BINARY | 0 | 1.000000 | -166.952 |
| 257 F15C031 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 258 F15C032 | | BINARY | 0 | 0.000000 | 5.746988 |
| 259 F15C033 | | BINARY | 0 | 0.000000 | -44.123452 |
| 260 F15C034 | | BINARY | 0 | 0.000000 | 0.395363 |
| 261 F15C035 | | BINARY | 0 | 1.000000 | -180.247 |
| 262 F15C036 | | BINARY | 0 | 1.000000 | -247.371 |
| 263 F15C037 | | BINARY | 0 | 1.000000 | -27.372630 |
| 264 F15C038 | | BINARY | 0 | 1.000000 | -150.718 |
| 265 F15C039 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 266 F15C040 | | BINARY | 0 | 0.000000 | 19298.070 |
| 267 F15C041 | | BINARY | 0 | 0.000000 | -104.291 |
| 268 F15C042 | | BINARY | 0 | 0.000000 | -35.530069 |
| 269 F15C043 | | BINARY | 0 | 1.000000 | -65.148819 |
| 270 F15C044 | | BINARY | 0 | 0.000000 | -78.294718 |
| 271 F15C045 | | BINARY | 0 | 1.000000 | -374.216 |
| 272 F15C046 | | BINARY | 0 | 0.000000 | -53.192495 |
| 273 F15C047 | | BINARY | 0 | 0.000000 | -99.115290 |
| 274 F15C048 | | BINARY | 0 | 1.000000 | -157.238 |
| 275 F15C049 | | BINARY | 0 | 0.000000 | -30.110958 |
| 276 F15C050 | | BINARY | 0 | 1.000000 | -84.115196 |
| 277 F15C052 | | BINARY | 0 | 0.000000 | -50.823930 |
| 278 F15C054 | | BINARY | 0 | 0.000000 | 4.540556 |
| 279 F15C055 | | BINARY | 0 | 0.000000 | -53.907744 |
| 280 F15C056 | | BINARY | 0 | 0.000000 | -1072.493 |
| 281 F15C057 | | BINARY | 0 | 1.000000 | -64.887544 |
| 282 F15C058 | | BINARY | 0 | 0.000000 | -172.688 |
| 283 F15C059 | | BINARY | 0 | 0.000000 | -182.338 |
| 284 F15C060 | | BINARY | 0 | 0.000000 | 19298.070 |
| 285 F15C061 | | BINARY | 0 | 0.000000 | 19298.070 |
| 286 F15C062 | | BINARY | 0 | 0.000000 | 19298.070 |
| 287 F15C063 | | BINARY | 0 | 0.000000 | 19298.070 |
| 288 F15C064 | | BINARY | 0 | 0.000000 | 19298.070 |
| 289 F15C065 | | BINARY | 0 | 0.000000 | 19298.070 |
| 290 F15C066 | | BINARY | 0 | 0.000000 | 19298.070 |
| 291 F15E003 | | BINARY | 0 | 1.000000 | -20.047991 |
| 292 F15E004 | | BINARY | 0 | 0.000000 | 19298.070 |
| 293 F15E005 | | BINARY | 0 | 0.000000 | -18.608502 |
| 294 F15E006 | | BINARY | 0 | 0.000000 | 19298.070 |

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VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|--------|-------|----------|--------------|
| 295 | F15E007 | | BINARY | 0 | 0.000000 | 19298.070 |
| 296 | F15E008 | | BINARY | 0 | 0.000000 | 19298.070 |
| 297 | F15E009 | | BINARY | 0 | 1.000000 | -65.702056 |
| 298 | F15E010 | | BINARY | 0 | 0.000000 | 5.904182 |
| 299 | F15E011 | | BINARY | 0 | 0.000000 | 19298.070 |
| 300 | F15E012 | | BINARY | 0 | 1.000000 | -84.172108 |
| 301 | F15E013 | | BINARY | 0 | 0.000000 | 0.254996 |
| 302 | F15E014 | | BINARY | 0 | 1.000000 | -64.231717 |
| 303 | F15E015 | | BINARY | 0 | 0.000000 | -45.134026 |
| 304 | F15E016 | | BINARY | 0 | 0.000000 | 19298.070 |
| 305 | F15E017 | | BINARY | 0 | 0.000000 | 19298.070 |
| 306 | F15E018 | | BINARY | 0 | 1.000000 | -82.883448 |
| 307 | F15E020 | | BINARY | 0 | 0.000000 | 19298.070 |
| 308 | F15E021 | | BINARY | 0 | 0.000000 | 19298.070 |
| 309 | F15E022 | | BINARY | 0 | 0.000000 | -26.574271 |
| 310 | F15E023 | | BINARY | 0 | 1.000000 | -66.457532 |
| 311 | F15E024 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 312 | F15E025 | | BINARY | 0 | 1.000000 | -178.720 |
| 313 | F15E026 | | BINARY | 0 | 1.000000 | -32.137014 |
| 314 | F15E028 | | BINARY | 0 | 0.000000 | -55.427327 |
| 315 | F15E029 | | BINARY | 0 | 0.000000 | 19298.070 |
| 316 | F15E031 | | BINARY | 0 | 0.000000 | -37.148869 |
| 317 | F15E032 | | BINARY | 0 | 0.000000 | -7.002979 |
| 318 | F15E033 | | BINARY | 0 | 0.000000 | 19298.070 |
| 319 | F15E034 | | BINARY | 0 | 0.000000 | 19298.070 |
| 320 | F15E035 | | BINARY | 0 | 0.000000 | -216.147 |
| 321 | F15E036 | | BINARY | 0 | 0.000000 | -49.423846 |
| 322 | F15E037 | | BINARY | 0 | 0.000000 | 4.477508 |
| 323 | F15E038 | | BINARY | 0 | 1.000000 | -179.600 |
| 324 | F15E039 | | BINARY | 0 | 0.000000 | 4.775495 |
| 325 | F15E040 | | BINARY | 0 | 0.000000 | -21.828312 |
| 326 | F15E041 | | BINARY | 0 | 1.000000 | -62.975230 |
| 327 | F15E042 | | BINARY | 0 | 0.000000 | -39.722020 |
| 328 | F15E043 | | BINARY | 0 | 1.000000 | -120.083 |
| 329 | F15E044 | | BINARY | 0 | 0.000000 | 19298.070 |
| 330 | F15E045 | | BINARY | 0 | 0.000000 | -124.790 |
| 331 | F15E046 | | BINARY | 0 | 0.000000 | -25.788372 |
| 332 | F15E047 | | BINARY | 0 | 0.000000 | -33.498475 |
| 333 | F15E048 | | BINARY | 0 | 0.000000 | -140.755 |
| 334 | F15E049 | | BINARY | 0 | 0.000000 | -85.591535 |
| 335 | F15E050 | | BINARY | 0 | 0.000000 | -18.245443 |
| 336 | F15E051 | | BINARY | 0 | 1.000000 | -77.188294 |

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LINEAR PROGRAMMING PROCEDURE

VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|--------|-------|----------|--------------|
| 337 | F15E052 | | BINARY | 0 | 0.000000 | -35.434361 |
| 338 | F15E053 | | BINARY | 0 | 1.000000 | -50.128272 |
| 339 | F15E056 | | BINARY | 0 | 1.000000 | -54.776784 |
| 340 | F15E057 | | BINARY | 0 | 0.000000 | -31.053128 |
| 341 | F15E058 | | BINARY | 0 | 0.000000 | 19298.070 |
| 342 | F15E059 | | BINARY | 0 | 0.000000 | 19298.070 |
| 343 | F15E060 | | BINARY | 0 | 0.000000 | 19298.070 |
| 344 | F15E061 | | BINARY | 0 | 0.000000 | 19298.070 |
| 345 | F15E062 | | BINARY | 0 | 0.000000 | 19298.070 |
| 346 | F15E063 | | BINARY | 0 | 0.000000 | 19298.070 |
| 347 | F15E064 | | BINARY | 0 | 0.000000 | 19298.070 |
| 348 | F15E065 | | BINARY | 0 | 0.000000 | 19298.070 |
| 349 | F163001 | | BINARY | 0 | 0.000000 | -39.647044 |
| 350 | F163002 | | BINARY | 0 | 1.000000 | -52.812432 |
| 351 | F163003 | | BINARY | 0 | 1.000000 | -45.826174 |
| 352 | F163004 | | BINARY | 0 | 1.000000 | -47.723786 |
| 353 | F163006 | | BINARY | 0 | 1.000000 | -53.481394 |
| 354 | F163007 | | BINARY | 0 | 0.000000 | 19298.070 |
| 355 | F163008 | | BINARY | 0 | 0.000000 | -69.859690 |
| 356 | F163010 | | BINARY | 0 | 0.000000 | -28.029385 |
| 357 | F163011 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 358 | F163012 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 359 | F163013 | | BINARY | 0 | 1.000000 | -13.745818 |
| 360 | F163014 | | BINARY | 0 | 0.000000 | -33.011171 |
| 361 | F163015 | | BINARY | 0 | 0.000000 | -118.099 |
| 362 | F163016 | | BINARY | 0 | 1.000000 | -47.677144 |
| 363 | F163017 | | BINARY | 0 | 0.000000 | -41.206554 |
| 364 | F163018 | | BINARY | 0 | 1.000000 | -261.081 |
| 365 | F163019 | | BINARY | 0 | 1.000000 | -41.028268 |
| 366 | F163020 | | BINARY | 0 | 1.000000 | -293.201 |
| 367 | F163021 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 368 | F163022 | | BINARY | 0 | 1.000000 | -54.016379 |
| 369 | F163023 | | BINARY | 0 | 0.000000 | -49.501063 |
| 370 | F163024 | | BINARY | 0 | 1.000000 | -49.755385 |
| 371 | F163025 | | BINARY | 0 | 0.000000 | -137.362 |
| 372 | F163026 | | BINARY | 0 | 1.000000 | -104.949 |
| 373 | F163027 | | BINARY | 0 | 0.000000 | -52.299244 |
| 374 | F163028 | | BINARY | 0 | 1.000000 | -10.890127 |
| 375 | F163029 | | BINARY | 0 | 1.000000 | -13.056763 |
| 376 | F163030 | | BINARY | 0 | 1.000000 | -3.268024 |
| 377 | F163031 | | BINARY | 0 | 1.000000 | -21.523868 |
| 378 | F163032 | | BINARY | 0 | 0.000000 | -64.708513 |

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LINEAR PROGRAMMING PROCEDURE

VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|--------|-------|----------|--------------|
| 379 | F163033 | | BINARY | 0 | 0.000000 | -95.045611 |
| 380 | F163036 | | BINARY | 0 | 1.000000 | -98.293825 |
| 381 | F163037 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 382 | F163038 | | BINARY | 0 | 0.000000 | 6.789658 |
| 383 | F163039 | | BINARY | 0 | 0.000000 | 19298.070 |
| 384 | F163040 | | BINARY | 0 | 0.000000 | 9.329683 |
| 385 | F163041 | | BINARY | 0 | 1.000000 | -69.477264 |
| 386 | F163042 | | BINARY | 0 | 0.000000 | -24.466601 |
| 387 | F163043 | | BINARY | 0 | 0.000000 | 3.037024 |
| 388 | F163044 | | BINARY | 0 | 1.000000 | -4.012885 |
| 389 | F163045 | | BINARY | 0 | 0.000000 | -38.998850 |
| 390 | F163046 | | BINARY | 0 | 0.000000 | 19298.070 |
| 391 | F163047 | | BINARY | 0 | 0.000000 | 19298.070 |
| 392 | F163048 | | BINARY | 0 | 0.000000 | 19298.070 |
| 393 | F163049 | | BINARY | 0 | 0.000000 | 19298.070 |
| 394 | F163050 | | BINARY | 0 | 0.000000 | 19298.070 |
| 395 | F163051 | | BINARY | 0 | 0.000000 | 19298.070 |
| 396 | F163052 | | BINARY | 0 | 0.000000 | 19298.070 |
| 397 | F163053 | | BINARY | 0 | 0.000000 | 19298.070 |
| 398 | F164001 | | BINARY | 0 | 0.000000 | 19298.070 |
| 399 | F164002 | | BINARY | 0 | 0.000000 | -68.711995 |
| 400 | F164003 | | BINARY | 0 | 1.000000 | -113.336 |
| 401 | F164004 | | BINARY | 0 | 1.000000 | -33.705296 |
| 402 | F164005 | | BINARY | 0 | 1.000000 | -10.884904 |
| 403 | F164006 | | BINARY | 0 | 1.000000 | -22.605339 |
| 404 | F164007 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 405 | F164008 | | BINARY | 0 | 1.000000 | -51.772495 |
| 406 | F164009 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 407 | F164010 | | BINARY | 0 | 0.000000 | -34.054942 |
| 408 | F164011 | | BINARY | 0 | 1.000000 | -280.421 |
| 409 | F164013 | | BINARY | 0 | 1.000000 | -24.133402 |
| 410 | F164014 | | BINARY | 0 | 1.000000 | -11.863106 |
| 411 | F164017 | | BINARY | 0 | 1.000000 | -54.878290 |
| 412 | F164018 | | BINARY | 0 | 0.000000 | -366.227 |
| 413 | F164020 | | BINARY | 0 | 1.000000 | -42.652261 |
| 414 | F164021 | | BINARY | 0 | 0.000000 | -73.349588 |
| 415 | F164022 | | BINARY | 0 | 0.000000 | -72.325393 |
| 416 | F164023 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 417 | F164024 | | BINARY | 0 | 0.000000 | -59.809411 |
| 418 | F164025 | | BINARY | 0 | 1.000000 | -25.984372 |
| 419 | F164026 | | BINARY | 0 | 1.000000 | -79.489546 |
| 420 | F164027 | | BINARY | 0 | 1.000000 | -81.528737 |

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VARIABLE SUMMARY

| Variable Col Name | Status | Type | Price | Activity | Reduced Cost |
|----------------------|--------|--------|-------|----------|-----------------|
| 421 F164028 | | BINARY | 0 | 0.000000 | -14.257018 |
| 422 F164029 | | BINARY | 0 | 0.000000 | 649.500 |
| 423 F164030 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 424 F164031 | | BINARY | 0 | 1.000000 | -10.890127 |
| 425 F164032 | | BINARY | 0 | 1.000000 | -16.583617 |
| 426 F164033 | | BINARY | 0 | 1.000000 | -21.523868 |
| 427 F164034 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 428 F164035 | | BINARY | 0 | 1.000000 | -33.916771 |
| 429 F164037 | | BINARY | 0 | 0.000000 | 6.789658 |
| 430 F164038 | | BINARY | 0 | 0.000000 | -3.180659 |
| 431 F164039 | | BINARY | 0 | 0.000000 | 9.329683 |
| 432 F164040 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 433 F164041 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 434 F164042 | | BINARY | 0 | 0.000000 | 6.249064 |
| 435 F164044 | | BINARY | 0 | 0.000000 | 5.587238 |
| 436 F164045 | | BINARY | 0 | 0.000000 | 11.246683 |
| 437 F164046 | | BINARY | 0 | 1.000000 | -67.435978 |
| 438 F164047 | | BINARY | 0 | 1.000000 | -9.143203 |
| 439 F164048 | | BINARY | 0 | 1.000000 | -292.497 |
| 440 F164049 | | BINARY | 0 | 1.000000 | -302.147 |
| 441 F164050 | | BINARY | 0 | 1.000000 | -22.127800 |
| 442 F164051 | | BINARY | 0 | 0.000000 | 19298.070 |
| 443 F164052 | | BINARY | 0 | 0.000000 | 19298.070 |
| 444 F164053 | | BINARY | 0 | 0.000000 | 19298.070 |
| 445 F164054 | | BINARY | 0 | 0.000000 | 19298.070 |
| 446 F164055 | | BINARY | 0 | 0.000000 | 19298.070 |
| 447 F164056 | | BINARY | 0 | 0.000000 | 19298.070 |
| 448 F165001 | | BINARY | 0 | 0.000000 | -29.961650 |
| 449 F165002 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 450 F165003 | | BINARY | 0 | 1.000000 | -95.071706 |
| 451 F165004 | | BINARY | 0 | 1.000000 | -10.884904 |
| 452 F165005 | | BINARY | 0 | 1.000000 | -17.784937 |
| 453 F165006 | BASIC | BINARY | 0 | 1.000000 | 0.000000 |
| 454 F165007 | | BINARY | 0 | 1.000000 | -52.776577 |
| 455 F165008 | | BINARY | 0 | 0.000000 | -140.037 |
| 456 F165009 | | BINARY | 0 | 0.000000 | -35.896114 |
| 457 F165010 | | BINARY | 0 | 1.000000 | -303.979 |
| 458 F165011 | | BINARY | 0 | 0.000000 | 19298.070 |
| 459 F165012 | | BINARY | 0 | 1.000000 | -25.839532 |
| 460 F165013 | | BINARY | 0 | 0.000000 | 19.300000 |
| 461 F165014 | | BINARY | 0 | 1.000000 | -10.000000 |
| 462 F165015 | | BINARY | 0 | 1.000000 | -48.823090 |

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VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|------------------|--------|--------|-------|----------|-----------------|
| 463 | F165016 | | BINARY | 0 | 1.000000 | -73.887398 |
| 464 | F165017 | | BINARY | 0 | 0.000000 | 19298.070 |
| 465 | F165018 | | BINARY | 0 | 1.000000 | -41.706257 |
| 466 | F165019 | | BINARY | 0 | 0.000000 | -27.364075 |
| 467 | F165020 | | BINARY | 0 | 1.000000 | -87.013310 |
| 468 | F165021 | | BINARY | 0 | 0.000000 | -57.425977 |
| 469 | F165022 | | BINARY | 0 | 0.000000 | -90.268553 |
| 470 | F165023 | | BINARY | 0 | 0.000000 | -107.541 |
| 471 | F165024 | | BINARY | 0 | 1.000000 | -47.966711 |
| 472 | F165025 | | BINARY | 0 | 1.000000 | -25.984372 |
| 473 | F165026 | | BINARY | 0 | 1.000000 | -118.930 |
| 474 | F165027 | | BINARY | 0 | 1.000000 | -122.902 |
| 475 | F165028 | | BINARY | 0 | 1.000000 | -105.911 |
| 476 | F165029 | | BINARY | 0 | 1.000000 | -11.419006 |
| 477 | F165030 | | BINARY | 0 | 0.000000 | 19298.070 |
| 478 | F165031 | | BINARY | 0 | 1.000000 | -13.745818 |
| 479 | F165032 | | BINARY | 0 | 1.000000 | -21.523868 |
| 480 | F165033 | | BINARY | 0 | 0.000000 | -116.415 |
| 481 | F165034 | | BINARY | 0 | 0.000000 | 6.789658 |
| 482 | F165035 | | BINARY | 0 | 0.000000 | 19298.070 |
| 483 | F165036 | | BINARY | 0 | 0.000000 | 9.329683 |
| 484 | F165037 | | BINARY | 0 | 1.000000 | -56.693430 |
| 485 | F165038 | | BINARY | 0 | 0.000000 | -22.988381 |
| 486 | F165039 | | BINARY | 0 | 0.000000 | 3.037024 |
| 487 | F165040 | | BINARY | 0 | 0.000000 | 0.063722 |
| 488 | F165041 | | BINARY | 0 | 0.000000 | 16.615561 |
| 489 | F165042 | | BINARY | 0 | 0.000000 | 19298.070 |
| 490 | F165043 | | BINARY | 0 | 0.000000 | 9.650000 |
| 491 | F165044 | | BINARY | 0 | 0.000000 | -6.551845 |
| 492 | F165045 | | BINARY | 0 | 1.000000 | -333.114 |
| 493 | F165046 | | BINARY | 0 | 1.000000 | -333.114 |
| 494 | F165047 | | BINARY | 0 | 1.000000 | -342.764 |
| 495 | F165048 | | BINARY | 0 | 1.000000 | -60.760036 |
| 496 | F165049 | | BINARY | 0 | 0.000000 | 19298.070 |
| 497 | F165050 | | BINARY | 0 | 0.000000 | 19298.070 |
| 498 | F165051 | | BINARY | 0 | 0.000000 | 19298.070 |
| 499 | F165052 | | BINARY | 0 | 0.000000 | 19298.070 |
| 500 | F165053 | | BINARY | 0 | 0.000000 | 19298.070 |
| 501 | LANT001 | | BINARY | 0 | 0.000000 | -81.289041 |
| 502 | LANT002 | | BINARY | 0 | 1.000000 | -65.903341 |
| 503 | LANT003 | | BINARY | 0 | 1.000000 | -61.975905 |
| 504 | LANT004 | | BINARY | 0 | 0.000000 | -21.237454 |

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VARIABLE SUMMARY

| Variable Col Name | Status | Type | Price | Activity | Reduced Cost |
|----------------------|--------|---------|-------|----------|-----------------|
| 505 LANT005 | DEGEN | BINARY | 0 | 0.000000 | 0.000000 |
| 506 LANT006 | | BINARY | 0 | 1.000000 | -30.779344 |
| 507 LANT007 | | BINARY | 0 | 0.000000 | -16.251337 |
| 508 LANT008 | | BINARY | 0 | 1.000000 | -59.905687 |
| 509 LANT009 | | BINARY | 0 | 1.000000 | -22.597814 |
| 510 LANT010 | | BINARY | 0 | 1.000000 | -130.931 |
| 511 LANT011 | | BINARY | 0 | 0.000000 | -17.737864 |
| 512 LANT012 | | BINARY | 0 | 1.000000 | -24.224282 |
| 513 LANT013 | | BINARY | 0 | 0.000000 | -11.447335 |
| 514 LANT014 | | BINARY | 0 | 0.000000 | 19298.070 |
| 515 LANT015 | | BINARY | 0 | 0.000000 | 19298.070 |
| 516 LANT016 | | BINARY | 0 | 0.000000 | 19298.070 |
| 517 LANT017 | | BINARY | 0 | 0.000000 | 19298.070 |
| 518 LANT018 | | BINARY | 0 | 0.000000 | 19298.070 |
| 519 LANT019 | | BINARY | 0 | 0.000000 | 19298.070 |
| 520 LANT020 | | BINARY | 0 | 0.000000 | 19298.070 |
| 521 A1011505 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 522 A1012305 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 523 A1020232 | | SLACK | | 0.000000 | 407.636 |
| 524 A1020313 | | SLACK | | 0.000000 | 77.961312 |
| 525 A1021314 | | SLACK | | 0.000000 | 44.707498 |
| 526 ENG22239 | DEGEN | SLACK | | 0.000000 | 0.000000 |
| 527 F1710105 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 528 F1710558 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 529 F1715605 | | SURPLUS | | 0.000000 | 233.505 |
| 530 F1721057 | DEGEN | SLACK | | 0.000000 | 0.000000 |
| 531 F1721157 | DEGEN | SLACK | | 0.000000 | 0.000000 |
| 532 F1721256 | DEGEN | SLACK | | 0.000000 | 0.000000 |
| 533 F1722558 | DEGEN | SLACK | | 0.000000 | 0.000000 |
| 534 F1722957 | DEGEN | SLACK | | 0.000000 | 0.000000 |
| 535 F5A12710 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 536 F5C11817 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 537 F5C13128 | | SURPLUS | | 0.000000 | 17.728381 |
| 538 F5C13156 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 539 F5C13513 | | SURPLUS | | 0.000000 | 106.326 |
| 540 F5C14212 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 541 F5C14342 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 542 F5C14542 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 543 F5C15657 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 544 F5C15728 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 545 F5C22829 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 546 F5C23254 | BASIC | SLACK | | 1.000000 | 0.000000 |

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VARIABLE SUMMARY

| Col | Variable Name | Status | Type | Price | Activity | Reduced Cost |
|-----|---------------|--------|---------|-------|----------|--------------|
| 547 | F5C24144 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 548 | F5C24447 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 549 | F5C25628 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 550 | F5E12524 | | SURPLUS | | 0.000000 | 57.583184 |
| 551 | F5E14145 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 552 | F5E15345 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 553 | F5E24548 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 554 | F5E25248 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 555 | F6310102 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 556 | F6310126 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 557 | F6311225 | | SURPLUS | | 0.000000 | 29.573848 |
| 558 | F6311423 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 559 | F6312018 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 560 | F6312118 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 561 | F6312120 | | SURPLUS | | 0.000000 | 157.393 |
| 562 | F6312518 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 563 | F6312926 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 564 | F6313218 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 565 | F6313318 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 566 | F6313711 | | SURPLUS | | 0.000000 | 42.391975 |
| 567 | F6314218 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 568 | F6321911 | | SLACK | | 0.000000 | 56.349302 |
| 569 | F6323719 | DEGEN | SLACK | | 0.000000 | 0.000000 |
| 570 | F6410307 | | SURPLUS | | 0.000000 | 39.164599 |
| 571 | F6410807 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 572 | F6411102 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 573 | F6411109 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 574 | F6411110 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 575 | F6411123 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 576 | F6411124 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 577 | F6411134 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 578 | F6411140 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 579 | F6411141 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 580 | F6411144 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 581 | F6411809 | | SURPLUS | | 0.000000 | 135.701 |
| 582 | F6411834 | | SURPLUS | | 0.000000 | 112.325 |
| 583 | F6411840 | | SURPLUS | | 0.000000 | 55.966248 |
| 584 | F6420641 | | SLACK | | 0.000000 | 3.198125 |
| 585 | F6421009 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 586 | F6422441 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 587 | F6422923 | | SLACK | | 0.000000 | 752.930 |
| 588 | F6423035 | | SLACK | | 0.000000 | 57.603867 |

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VARIABLE SUMMARY

| Variable Col Name | Status | Type | Price | Activity | Reduced Cost |
|----------------------|--------|---------|-------|-----------|-----------------|
| 589 F6423409 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 590 F6510306 | | SURPLUS | | 0.000000 | 47.263924 |
| 591 F6510706 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 592 F6511008 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 593 F6511009 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 594 F6511021 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 595 F6511022 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 596 F6511023 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 597 F6511033 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 598 F6511037 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 599 F6511038 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 600 F6511040 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 601 F6511608 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 602 F6511633 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 603 F6511637 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 604 F6520138 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 605 F6520908 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 606 F6522338 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 607 F6523308 | BASIC | SLACK | | 1.000000 | 0.000000 |
| 608 LAN10313 | BASIC | SURPLUS | | 1.000000 | 0.000000 |
| 609 LAN11105 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 610 LAN11107 | DEGEN | SURPLUS | | 0.000000 | 0.000000 |
| 611 LAN20506 | | SLACK | | 0.000000 | 38.846874 |
| 612 YEAR01 | BASIC | SLACK | | 40.789000 | 0.000000 |
| 613 YEAR02 | BASIC | SLACK | | 2.716000 | 0.000000 |
| 614 YEAR03 | BASIC | SLACK | | 1.807000 | 0.000000 |
| 615 YEAR04 | BASIC | SLACK | | 1.182000 | 0.000000 |
| 616 YEAR05 | BASIC | SLACK | | 0.250000 | 0.000000 |
| 617 YEAR06 | BASIC | SLACK | | 0.370000 | 0.000000 |
| 618 YEAR07 | BASIC | SLACK | | 0.005000 | 0.000000 |
| 619 YEAR08 | BASIC | SLACK | | 10.953000 | 0.000000 |
| 620 YEAR09 | BASIC | SLACK | | 66.423000 | 0.000000 |
| 621 YEAR10 | BASIC | SLACK | | 190.742 | 0.000000 |
| 622 YEAR11 | BASIC | SLACK | | 14.876000 | 0.000000 |
| 623 YEAR12 | BASIC | SLACK | | 31.090000 | 0.000000 |
| 624 YEAR13 | BASIC | SLACK | | 140.849 | 0.000000 |
| 625 YEAR14 | BASIC | SLACK | | 185.280 | 0.000000 |
| 626 YEAR15 | BASIC | SLACK | | 253.037 | 0.000000 |
| 627 YEAR16 | BASIC | SLACK | | 252.900 | 0.000000 |
| 628 YEAR17 | BASIC | SLACK | | 308.900 | 0.000000 |
| 629 YEAR18 | BASIC | SLACK | | 314.300 | 0.000000 |

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CONSTRAINT SUMMARY

| Constraint Row Name | Type | S/S Col | Rhs | Activity | Dual Activity |
|------------------------|------|------------|-----------|----------|------------------|
| 1 A1011203 | EQ | | 0 | 0.000000 | 13.410982 |
| 2 A1011505 | GE | 521 | 0 | 1.000000 | 0.000000 |
| 3 A1011517 | EQ | | 0 | 0.000000 | 19298.070 |
| 4 A1012305 | GE | 522 | 0 | 1.000000 | 0.000000 |
| 5 A1020232 | LE | 523 | 1 | 1.000000 | -407.636 |
| 6 A1020313 | LE | 524 | 1 | 1.000000 | -77.961312 |
| 7 A1021314 | LE | 525 | 1 | 1.000000 | -44.707498 |
| 8 COSTOWN | EQ | | 4737.5763 | 4737.576 | 1.740000 |
| 9 ENG22239 | LE | 526 | 1 | 1.000000 | 0.000000 |
| 10 F1710105 | GE | 527 | 0 | 0.000000 | 0.000000 |
| 11 F1710558 | GE | 528 | 0 | 0.000000 | 0.000000 |
| 12 F1715605 | GE | 529 | 0 | 0.000000 | 233.505 |
| 13 F1721057 | LE | 530 | 1 | 1.000000 | 0.000000 |
| 14 F1721157 | LE | 531 | 1 | 1.000000 | 0.000000 |
| 15 F1721256 | LE | 532 | 1 | 1.000000 | 0.000000 |
| 16 F1722558 | LE | 533 | 1 | 1.000000 | 0.000000 |
| 17 F1722957 | LE | 534 | 1 | 1.000000 | 0.000000 |
| 18 F5A12710 | GE | 535 | 0 | 0.000000 | 0.000000 |
| 19 F5C11817 | GE | 536 | 0 | 0.000000 | 0.000000 |
| 20 F5C13128 | GE | 537 | 0 | 0.000000 | 17.728381 |
| 21 F5C13156 | GE | 538 | 0 | 0.000000 | 0.000000 |
| 22 F5C13513 | GE | 539 | 0 | 0.000000 | 106.326 |
| 23 F5C13839 | EQ | | 0 | 0.000000 | -75.359187 |
| 24 F5C14212 | GE | 540 | 0 | 0.000000 | 0.000000 |
| 25 F5C14342 | GE | 541 | 0 | 1.000000 | 0.000000 |
| 26 F5C14542 | GE | 542 | 0 | 1.000000 | 0.000000 |
| 27 F5C15657 | GE | 543 | 0 | 1.000000 | 0.000000 |
| 28 F5C15728 | GE | 544 | 0 | 1.000000 | 0.000000 |
| 29 F5C22829 | LE | 545 | 1 | 0.000000 | 0.000000 |
| 30 F5C23254 | LE | 546 | 1 | 0.000000 | 0.000000 |
| 31 F5C24144 | LE | 547 | 1 | 0.000000 | 0.000000 |
| 32 F5C24447 | LE | 548 | 1 | 0.000000 | 0.000000 |
| 33 F5C25628 | LE | 549 | 1 | 0.000000 | 0.000000 |
| 34 F5E12524 | GE | 550 | 0 | 0.000000 | 57.583184 |
| 35 F5E14145 | GE | 551 | 0 | 1.000000 | 0.000000 |
| 36 F5E15345 | GE | 552 | 0 | 1.000000 | 0.000000 |
| 37 F5E24548 | LE | 553 | 1 | 0.000000 | 0.000000 |
| 38 F5E25248 | LE | 554 | 1 | 0.000000 | 0.000000 |
| 39 F6310102 | GE | 555 | 0 | 1.000000 | 0.000000 |
| 40 F6310126 | GE | 556 | 0 | 1.000000 | 0.000000 |
| 41 F6311225 | GE | 557 | 0 | 0.000000 | 29.573848 |
| 42 F6311423 | GE | 558 | 0 | 0.000000 | 0.000000 |

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LINEAR PROGRAMMING PROCEDURE

CONSTRAINT SUMMARY

| Constraint Row Name | Type | S/S Col | Rhs | Activity | Dual Activity |
|------------------------|------|------------|-----|----------|------------------|
| 43 F6312018 | GE | 559 | 0 | 0.000000 | 0.000000 |
| 44 F6312118 | GE | 560 | 0 | 0.000000 | 0.000000 |
| 45 F6312120 | GE | 561 | 0 | 0.000000 | 157.393 |
| 46 F6312518 | GE | 562 | 0 | 1.000000 | 0.000000 |
| 47 F6312926 | GE | 563 | 0 | 0.000000 | 0.000000 |
| 48 F6313218 | GE | 564 | 0 | 1.000000 | 0.000000 |
| 49 F6313318 | GE | 565 | 0 | 1.000000 | 0.000000 |
| 50 F6313711 | GE | 566 | 0 | 0.000000 | 42.391975 |
| 51 F6314218 | GE | 567 | 0 | 1.000000 | 0.000000 |
| 52 F6321911 | LE | 568 | 1 | 1.000000 | -56.349302 |
| 53 F6323719 | LE | 569 | 1 | 1.000000 | 0.000000 |
| 54 F6410307 | GE | 570 | 0 | 0.000000 | 39.164599 |
| 55 F6410807 | GE | 571 | 0 | 0.000000 | 0.000000 |
| 56 F6411102 | GE | 572 | 0 | 1.000000 | 0.000000 |
| 57 F6411109 | GE | 573 | 0 | 1.000000 | 0.000000 |
| 58 F6411110 | GE | 574 | 0 | 1.000000 | 0.000000 |
| 59 F6411123 | GE | 575 | 0 | 0.000000 | 0.000000 |
| 60 F6411124 | GE | 576 | 0 | 1.000000 | 0.000000 |
| 61 F6411134 | GE | 577 | 0 | 1.000000 | 0.000000 |
| 62 F6411140 | GE | 578 | 0 | 1.000000 | 0.000000 |
| 63 F6411141 | GE | 579 | 0 | 1.000000 | 0.000000 |
| 64 F6411144 | GE | 580 | 0 | 1.000000 | 0.000000 |
| 65 F6411809 | GE | 581 | 0 | 0.000000 | 135.701 |
| 66 F6411834 | GE | 582 | 0 | 0.000000 | 112.325 |
| 67 F6411840 | GE | 583 | 0 | 0.000000 | 55.966248 |
| 68 F6420641 | LE | 584 | 1 | 1.000000 | -3.198125 |
| 69 F6421009 | LE | 585 | 1 | 0.000000 | 0.000000 |
| 70 F6422441 | LE | 586 | 1 | 0.000000 | 0.000000 |
| 71 F6422923 | LE | 587 | 1 | 1.000000 | -752.930 |
| 72 F6423035 | LE | 588 | 1 | 1.000000 | -57.603867 |
| 73 F6423409 | LE | 589 | 1 | 0.000000 | 0.000000 |
| 74 F6510306 | GE | 590 | 0 | 0.000000 | 47.263924 |
| 75 F6510706 | GE | 591 | 0 | 0.000000 | 0.000000 |
| 76 F6511008 | GE | 592 | 0 | 1.000000 | 0.000000 |
| 77 F6511009 | GE | 593 | 0 | 1.000000 | 0.000000 |
| 78 F6511021 | GE | 594 | 0 | 1.000000 | 0.000000 |
| 79 F6511022 | GE | 595 | 0 | 1.000000 | 0.000000 |
| 80 F6511023 | GE | 596 | 0 | 1.000000 | 0.000000 |
| 81 F6511033 | GE | 597 | 0 | 1.000000 | 0.000000 |
| 82 F6511037 | GE | 598 | 0 | 0.000000 | 0.000000 |
| 83 F6511038 | GE | 599 | 0 | 1.000000 | 0.000000 |
| 84 F6511040 | GE | 600 | 0 | 1.000000 | 0.000000 |

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L I N E A R P R O G R A M M I N G P R O C E D U R E

CONSTRAINT S U M M A R Y

| Constraint Row Name | Type | S/S Col | Rhs | Activity | Dual Activity |
|------------------------|--------|------------|-----------|-----------|------------------|
| 85 F6511608 | GE | 601 | 0 | 1.000000 | 0.000000 |
| 86 F6511633 | GE | 602 | 0 | 1.000000 | 0.000000 |
| 87 F6511637 | GE | 603 | 0 | 0.000000 | 0.000000 |
| 88 F6520138 | LE | 604 | 1 | 0.000000 | 0.000000 |
| 89 F6520908 | LE | 605 | 1 | 0.000000 | 0.000000 |
| 90 F6522338 | LE | 606 | 1 | 0.000000 | 0.000000 |
| 91 F6523308 | LE | 607 | 1 | 0.000000 | 0.000000 |
| 92 FALCONUP | EQ | | 3 | 3.000000 | -18.882668 |
| 93 FMS | EQ | | 1650 | 1650.000 | 1.000000 |
| 94 LAN10313 | GE | 608 | 0 | 1.000000 | 0.000000 |
| 95 LAN11105 | GE | 609 | 0 | 0.000000 | 0.000000 |
| 96 LAN11107 | GE | 610 | 0 | 0.000000 | 0.000000 |
| 97 LAN20506 | LE | 611 | 1 | 1.000000 | -38.846874 |
| 98 OBJECT | OBJECT | | | 9222.042 | . |
| 99 TECHRISK | EQ | | 0 | 0.000000 | -1.930000 |
| 100 WEIGHT | EQ | | 232307671 | 232307671 | 0.000071 |
| 101 YEAR01 | LE | 612 | 484.2 | 443.411 | 0.000000 |
| 102 YEAR02 | LE | 613 | 527.4 | 524.684 | 0.000000 |
| 103 YEAR03 | LE | 614 | 567.6 | 565.793 | 0.000000 |
| 104 YEAR04 | LE | 615 | 564 | 562.818 | 0.000000 |
| 105 YEAR05 | LE | 616 | 771.6 | 771.350 | 0.000000 |
| 106 YEAR06 | LE | 617 | 760.2 | 759.830 | 0.000000 |
| 107 YEAR07 | LE | 618 | 802.2 | 802.195 | 0.000000 |
| 108 YEAR08 | LE | 619 | 832.2 | 821.247 | 0.000000 |
| 109 YEAR09 | LE | 620 | 774 | 707.577 | 0.000000 |
| 110 YEAR10 | LE | 621 | 689.4 | 498.658 | 0.000000 |
| 111 YEAR11 | LE | 622 | 475.8 | 460.924 | 0.000000 |
| 112 YEAR12 | LE | 623 | 364.2 | 333.110 | 0.000000 |
| 113 YEAR13 | LE | 624 | 382.2 | 241.351 | 0.000000 |
| 114 YEAR14 | LE | 625 | 286.2 | 100.920 | 0.000000 |
| 115 YEAR15 | LE | 626 | 345 | 91.963000 | 0.000000 |
| 116 YEAR16 | LE | 627 | 334.8 | 81.900000 | 0.000000 |
| 117 YEAR17 | LE | 628 | 340.8 | 31.900000 | 0.000000 |
| 118 YEAR18 | LE | 629 | 346.2 | 31.900000 | 0.000000 |