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A FORTRAN COMPUTER CODE PACKAGE FOR THE EVALUATION OF
GAS-PHASE, MULTICOMPONENT TRANSPORT PROPERTIES

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Abstract

This report documents a FORTRAN computer code package that is used for the evaluation of gas-phase multicomponent viscosities, thermal conductivities, diffusion coefficients, and thermal diffusion coefficients. The TRANSPORT Property package is in two parts. The first is a preprocessor that computes polynomial fits to the temperature dependent parts of the pure species viscosities and binary diffusion coefficients. The coefficients of these fits are passed to a library of subroutines via a linking file. Then, any subroutine from this library may be called to return either pure species properties or multicomponent gas mixture properties. This package uses the gas-phase chemical kinetics package CHEMKIN-III, and the TRANSPORT property subroutines are designed to be used in conjunction with the CHEMKIN-III subroutine library.

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I. INTRODUCTION

Characterizing the molecular transport of species, momentum, and energy in a multicomponent gaseous mixture requires the evaluation of diffusion coefficients, viscosities, thermal conductivities, and thermal diffusion coefficients. Although evaluation of pure species properties follows standard kinetic theory expressions, one can choose from a range of possibilities for evaluating mixture properties. Moreover, computing the mixture properties can be expensive, and depending on the use of the results, it is often advantageous to make simplifying assumptions to reduce the computational cost.

For most applications, gas mixture properties can be determined from pure species properties via certain approximate mixture averaging rules. However, there are some applications in which the approximate averaging rules are not adequate. The software package described here therefore addresses both the mixture-averaged approach and the full multicomponent approach to transport properties. The TRANSPORT property program is fully compatible with the CHEMKIN Thermodynamic Database ¹ and the CHEMKIN-III Gas-phase kinetics package. ² The multicomponent methods are based on the work of Dixon-Lewis ³ and the methods for mixture-averaged approach are reported in Warnatz ⁴ and Kee et al. ⁵

The multicomponent formulation has several important advantages over the relatively simpler mixture formulas. The first advantage is accuracy. The mixture formulas are only correct asymptotically in some special cases, such as in a binary mixture, or in diffusion of trace amounts of species into a nearly pure species, or systems in which all species except one move with nearly the same diffusion velocity. ⁶ A second deficiency of the mixture formulas is that overall mass conservation is not necessarily preserved when solving the species continuity equations. To compensate for this shortcoming one has to apply some *ad hoc* correction procedure. ^{5,7} The multicomponent formulation guarantees mass conservation without any correction factors, which is a clear advantage. The only real deficiency of the multicomponent formulation is its computational expense. Evaluating the ordinary multicomponent diffusion coefficients involves inverting a $K \times K$ matrix, and evaluating the thermal conductivity and thermal diffusion coefficients requires solving a $3K \times 3K$ system of algebraic equations, where K is the number of species.

To maximize computational efficiency, the multicomponent transport package is structured such that a large portion of the calculations are done in a preprocessor that provides information to the application code requiring the transport properties through a Linking File. Polynomial fits are thus computed *a priori* for the temperature-dependent parts of the kinetic theory expressions for pure species viscosities and binary diffusion coefficients. (The pure species thermal conductivities are also fit, but are only used in the mixture-averaged formulation.) The coefficients from the fit are passed to

a library of subroutines that can be used to return either mixture-averaged properties or multicomponent properties. This fitting procedure is used so that expensive operations, such as evaluation of collision integrals, need be done only once and not every time a property is needed.

This document first reviews the kinetic theory expressions for the pure species viscosities and the binary diffusion coefficients. Then, we describe how momentum, energy, and species mass fluxes are computed from the velocity, temperature and species gradients and either mixture-averaged or multicomponent transport properties. Having these relationships in mind, the report next describes the procedures to determine multicomponent transport properties from the pure species expressions. The third part of the report describes how to use the software package and how it relates to CHEMKIN. The following chapter describes each of the multicomponent subroutines than can be called by the package's user. The last chapter lists the data base that is currently available.

II. THE TRANSPORT EQUATIONS

Pure Species Viscosity and Binary Diffusion Coefficients

The single component viscosities are given by the standard kinetic theory expression ⁸

$$\eta_k = \frac{5}{16} \frac{\sqrt{\pi m_k k_B T}}{\pi \sigma_k^2 \Omega^{(2,2)*}}, \quad (1)$$

where σ_k is the Lennard-Jones collision diameter, m_k is the molecular mass, k_B is the Boltzmann constant, and T is the temperature. The collision integral $\Omega^{(2,2)*}$ depends on the reduced temperature given by

$$T_k^* = \frac{k_B T}{\epsilon_k},$$

and the reduced dipole moment given by

$$\delta_k^* = \frac{1}{2} \frac{\mu_k^2}{\epsilon_k \sigma_k^3}. \quad (2)$$

In the above expression ϵ_k is the Lennard-Jones potential well depth and μ_k is the dipole moment. The collision integral value is determined by a quadratic interpolation of the tables based on Stockmayer potentials given in Monchick and Mason. ⁹

The binary diffusion coefficients ⁸ are given in terms of pressure and temperature as

$$\mathcal{D}_{jk} = \frac{3}{16} \frac{\sqrt{2\pi k_B^3 T^3 / m_{jk}}}{P \pi \sigma_{jk}^2 \Omega^{(1,1)*}}, \quad (3)$$

where m_k is the reduced molecular mass for the (j,k) species pair

$$m_{jk} = \frac{m_j m_k}{m_j + m_k}, \quad (4)$$

and σ_{jk} is the reduced collision diameter. The collision integral $\Omega^{(1,1)*}$ (based on Stockmayer potentials) depends on the reduced temperature, T_{jk}^* which in turn may depend on the species dipole moments μ_k , and polarizabilities α_k . In computing the reduced quantities, we consider two cases, depending on whether the collision partners are polar or nonpolar. For the case that the partners are either both polar or both nonpolar the following expressions apply:

$$\frac{\varepsilon_{jk}}{k_B} = \sqrt{\frac{\varepsilon_j}{k_B} \left| \frac{\varepsilon_k}{k_B} \right|} \quad (5)$$

$$\sigma_{jk} = \frac{1}{2}(\sigma_j + \sigma_k) \quad (6)$$

$$\mu_{jk}^2 = \mu_j \mu_k. \quad (7)$$

For the case of a polar molecule interacting with a nonpolar molecule:

$$\frac{\varepsilon_{np}}{k_B} = \xi^2 \sqrt{\frac{\varepsilon_n}{k_B} \left| \frac{\varepsilon_p}{k_B} \right|} \quad (8)$$

$$\sigma_{np} = \frac{1}{2}(\sigma_n + \sigma_p) \xi^{-\frac{1}{6}} \quad (9)$$

$$\mu_{np}^2 = 0, \quad (10)$$

where,

$$\xi = 1 + \frac{1}{4} \alpha_n^* \mu_p^* \sqrt{\frac{\varepsilon_p}{\varepsilon_n}}. \quad (11)$$

In the above equations α_n^* is the reduced polarizability for the nonpolar molecule and μ_p^* is the reduced dipole moment for the polar molecule. The reduced values are given by

$$\alpha_n^* = \frac{\alpha_n}{\sigma_n^3} \quad (12)$$

$$\mu_p^* = \frac{\mu_p}{\sqrt{\varepsilon_p \sigma_p^3}}. \quad (13)$$

The table look-up evaluation of the collision integral $\Omega^{(1,1)*}$ depends on the reduced temperature

$$T_{jk}^* = \frac{k_B T}{\varepsilon_{jk}}, \quad (14)$$

and the reduced dipole moment,

$$\delta_{jk}^* = \frac{1}{2} \mu_{jk}^{*2}. \quad (15)$$

Although one could add a second-order correction factor to the binary diffusion coefficients¹⁰ we have chosen to neglect this since, in the multicomponent case, we specifically need only the first approximation to the diffusion coefficients. When higher accuracy is required for the diffusion coefficients, we therefore recommend using the full multicomponent option.

Pure Species Thermal Conductivities

The pure species thermal conductivities are computed only for the purpose of later evaluating mixture-averaged thermal conductivities; the mixture conductivity in the multicomponent case does not depend on the pure species formulas stated in this section. Here we assume the individual species conductivities to be composed of translational, rotational, and vibrational contributions as given by Warnatz.⁴

$$\lambda_k = \frac{\eta_k}{M_k} (f_{\text{trans.}} C_{v,\text{trans.}} + f_{\text{rot.}} C_{v,\text{rot.}} + f_{\text{vib.}} C_{v,\text{vib.}}) \quad (16)$$

where

$$f_{\text{trans.}} = \frac{5}{2} \left| 1 - \frac{2}{\pi} \frac{C_{v,\text{rot.}}}{C_{v,\text{trans.}}} \frac{A}{B} \right| \quad (17)$$

$$f_{\text{rot.}} = \frac{\rho \mathcal{D}_{kk}}{\eta_k} \left| 1 + \frac{2}{\pi} \frac{A}{B} \right| \quad (18)$$

$$f_{\text{vib.}} = \frac{\rho \mathcal{D}_{kk}}{\eta_k} \quad (19)$$

and,

$$A = \frac{5}{2} - \frac{\rho \mathcal{D}_{kk}}{\eta_k} \quad (20)$$

$$B = Z_{\text{rot.}} + \frac{2}{\pi} \left| \frac{5}{3} \frac{C_{v,\text{rot.}}}{R} + \frac{\rho \mathcal{D}_{kk}}{\eta_k} \right|. \quad (21)$$

The molar heat capacity C_v relationships are different depending on whether or not the molecule is linear or not. In the case of a linear molecule,

$$\frac{C_{v,\text{trans.}}}{R} = \frac{3}{2} \quad (22)$$

$$\frac{C_{v,\text{rot.}}}{R} = 1 \quad (23)$$

$$C_{v,\text{vib.}} = C_v - \frac{5}{2}R. \quad (24)$$

In the above, C_v is the specific heat at constant volume of the molecule and R is the universal gas constant. For the case of a nonlinear molecule,

$$\frac{C_{v,\text{trans.}}}{R} = \frac{3}{2} \quad (25)$$

$$\frac{C_{v,\text{rot.}}}{R} = \frac{3}{2} \quad (26)$$

$$C_{v,\text{vib.}} = C_v - 3R. \quad (27)$$

The translational part of C_v is always the same,

$$C_{v,\text{trans.}} = \frac{3}{2}R. \quad (28)$$

In the case of single atoms (H atoms, for example) there are no internal contributions to C_v , and hence,

$$\lambda_k = \frac{\eta_k}{M_k} f_{\text{trans.}} \frac{3}{2}R \quad (29)$$

where $f_{\text{trans.}} = 5/2$. The “self-diffusion” coefficient comes from the following expression,

$$\mathcal{D}_{kk} = \frac{3}{16} \frac{\sqrt{2\pi k_B^3 T^3 / m_k}}{P\pi\sigma_k^2 \Omega^{(1,1)*}}. \quad (30)$$

The density comes from the equation of state for a perfect gas,

$$\rho = \frac{PM_k}{RT}, \quad (31)$$

with p being the pressure and M_k the species molar mass.

The rotational relaxation collision number is a parameter that we assume is available at 298K (included in the data base). It has a temperature dependence given in an expression by Parker¹¹ and Brau and Jonkman,¹²

$$Z_{\text{rot.}}(T) = Z_{\text{rot.}}(298) \frac{F(298)}{F(T)}, \quad (32)$$

where,

$$F(T) = 1 + \frac{\pi^2}{2} \left| \frac{\varepsilon/k_B}{T} \right|^2 + \frac{\pi^2}{4} + 2 \left| \frac{\varepsilon/k_B}{T} \right| + \pi^2 \frac{\varepsilon/k_B}{T} \left| \frac{\varepsilon/k_B}{T} \right|^2. \quad (33)$$

The Pure-Species Fitting Procedure

To expedite the evaluation of transport properties in a computer code, such as a flame code, we fit the temperature dependent parts of the pure species property expressions. Then, rather than evaluating the complex expressions for the properties, only comparatively simple fits need to be evaluated.

We use a polynomial fit of the logarithm of the property versus the logarithm of the temperature. For the viscosity

$$\ln \eta_k = \sum_{n=1}^N a_{n,k} (\ln T)^{n-1}, \quad (34)$$

and the thermal conductivity,

$$\ln \lambda_k = \sum_{n=1}^N b_{n,k} (\ln T)^{n-1}. \quad (35)$$

The fits are done for each pair of binary diffusion coefficients in the system.

$$\ln \mathcal{D}_{jk} = \sum_{n=1}^N d_{n,jk} (\ln T)^{n-1}. \quad (36)$$

By default TRANSPORT uses third- order polynomial fits (i.e., $N=4$) and we find that the fitting errors are well within one percent. The fitting procedure must be carried out for the particular system of gases that is present in a given problem. Therefore, the fitting can not be done “once and for all,” but must be done once at the beginning of each new problem.

The viscosity and conductivity are independent of pressure, but the diffusion coefficients depend inversely on pressure. The diffusion coefficient fits are computed at unit pressure; the later evaluation of a diffusion coefficient is obtained by simply dividing the diffusion coefficient as evaluated from the fit by the actual pressure.

Even though the single component conductivities are fit and passed to the subroutine library they are not used in the computation of multicomponent thermal conductivities; they are used only for the evaluation of the mixture-averaged conductivities.

The Mass, Momentum, and Energy Fluxes

The momentum flux is related to the gas mixture viscosity and the velocities by

$$\boldsymbol{\tau} = -\eta(\nabla \boldsymbol{v} + (\nabla \boldsymbol{v})^T) + \frac{2}{3}\eta - \kappa |(\nabla \cdot \boldsymbol{v})\boldsymbol{\delta}, \quad (37)$$

where \boldsymbol{v} is the velocity vector, $(\nabla \boldsymbol{v})$ is the dyadic product, $(\nabla \boldsymbol{v})^T$ is the transpose of the dyadic product, and $\boldsymbol{\delta}$ is the unit tensor.⁶ In this software package we provide average values for the mixture viscosity η , but we do not provide information on the bulk viscosity κ .

The energy flux is given in terms of the thermal conductivity λ_0 by

$$\mathbf{q} = \sum_{k=1}^K \mathbf{j}_k h_k - \lambda_0 \nabla T - \sum_{k=1}^K \frac{RT}{M_k X_k} D_k^T \mathbf{d}_k, \quad (38)$$

where,

$$\mathbf{d}_k = \nabla X_k + (X_k - Y_k) \frac{1}{p} \nabla p. \quad (39)$$

The multicomponent species flux is given by

$$\mathbf{j}_k = \rho Y_k \mathbf{V}_k, \quad (40)$$

where Y_k are the mass fractions and the diffusion velocities are given by

$$\mathbf{V}_k = \frac{1}{X_k \bar{M}} \sum_{j \neq k}^K M_j D_{k,j} \mathbf{d}_j - \frac{D_k^T}{\rho Y_k} \nabla T. \quad (41)$$

The species molar masses are denoted by M_k and the mean molar mass by \bar{M} . $D_{k,j}$ are the ordinary multicomponent diffusion coefficients, and D_k^T are the thermal diffusion coefficients.

By definition in the mixture-average formulations, the diffusion velocity is related to the species gradients by a Fickian formula as,

$$\mathbf{V}_k = -\frac{1}{X_k} D_{km} \mathbf{d}_k - \frac{D_k^T}{\rho Y_k} \frac{1}{T} \nabla T. \quad (42)$$

The mixture diffusion coefficient for species k is computed as ⁶

$$D_{km} = \frac{1 - Y_k}{\sum_{j \neq k}^K X_j / \mathcal{D}_{jk}} \quad (43)$$

A potential problem with this expression is that it is not mathematically well-defined in the limit of the mixture becoming a pure species. Even though diffusion itself has no real meaning in the case of a pure species, the numerical implementation must ensure that the diffusion coefficients behave reasonably and that the code does not “blow up” when the pure species condition is reached. We circumvent these problems by evaluating the diffusion coefficients in the following equivalent way.

$$D_{km} = \frac{\sum_{j \neq k}^K X_j M_j}{\bar{M} \sum_{j \neq k}^K X_j / \mathcal{D}_{jk}} \quad (44)$$

In this form the roundoff is accumulated in roughly the same way in both the numerator and denominator, and thus the quotient is well-behaved as the pure species limit is approached. However, if the mixture is exactly a pure species, the formula is still undefined.

To overcome this difficulty we always retain a small quantity of each species. In other words, for the purposes of computing mixture diffusion coefficients, we simply do not allow a pure species situation to occur; we always maintain a residual amount of each species. Specifically, we assume in the above formulas that

$$X_k = \hat{X}_k + \delta, \quad (45)$$

where \hat{X}_k is the actual mole fraction and δ is a small number that is numerically insignificant compared to any mole fraction of interest, yet which is large enough that there is no trouble representing it on any computer. A value of 10^{-12} for δ works well.

In some cases (for example, Warnatz ¹³ and Coltrin et al. ¹⁴) it can be useful to treat multicomponent diffusion in terms of an equivalent Fickian diffusion process. This is sometimes a programming convenience in that the computer data structure for the multicomponent process can be made to look like a Fickian process. To do so supposes that a mixture diffusion coefficient can be defined in such a way that the diffusion velocity is written as Eq. (42) rather than Eq. (41). This equivalent Fickian diffusion coefficient is then derived by equating Eq. (41) and (42) and solving for D_{km} as

$$D_{km} = - \frac{\sum_{j \neq k}^K M_j D_{k,j} \mathbf{d}_j}{\bar{M} \mathbf{d}_k} \quad (46)$$

Unfortunately, this equation is undefined as the mixture approaches a pure species condition. To help deal with this difficulty a small number ($\varepsilon = 10^{-12}$) may be added to both the numerator and denominator to obtain

$$D_{km} = -\frac{\sum_{j \neq k}^K M_j D_{kj} \mathbf{d}_j + \varepsilon}{\bar{M}(\mathbf{d}_k + \varepsilon)}$$

Furthermore, for the purposes of evaluating the “multicomponent” D_{km} , it may be advantageous to compute the \mathbf{d}_k in the denominator using the fact that $\nabla X_k = -\sum_{j \neq k}^K \nabla X_j$. In this way the summations in the numerator and the denominator accumulate any rounding errors in roughly the same way, and thus the quotient is more likely to be well behaved as the pure species limit is approached. Since there is no diffusion due to species gradients in a pure species situation, the exact value of the diffusion coefficient is not as important as the need for it simply to be well defined, and thus not cause computational difficulties.

In practice we have found mixed results using the equivalent Fickian diffusion to represent multicomponent processes. In some marching or parabolic problems, such as boundary layer flow in channels,¹⁴ we find that the equivalent Fickian formulation is preferable. However, in some steady state boundary value problems, we have found that the equivalent Fickian formulation fails to converge, whereas the regular multicomponent formulation works quite well. Thus, we cannot confidently recommend which formulation should be preferred for any given application.

The Mixture-Averaged Properties

Our objective in this section is to determine mixture properties from the pure species properties. In the case of viscosity, we use the semi-empirical formula due to Wilke¹⁵ and modified by Bird et al.⁶ The Wilke formula for mixture viscosity is given by

$$\eta = \frac{\sum_{k=1}^K X_k \eta_k}{\sum_{j=1}^K X_j \Phi_{kj}} \quad (48)$$

where,

$$\Phi_{kj} = \frac{1}{\sqrt{8}} \left| 1 + \frac{M_k}{M_j} \right|^{-\frac{1}{2}} \left| 1 + \frac{\eta_k}{\eta_j} \right|^{\frac{1}{2}} \left| \frac{M_j}{M_k} \right|^{\frac{1}{4}} \Bigg|^2. \quad (49)$$

For the mixture-averaged thermal conductivity we use a combination averaging formula¹⁶

$$\lambda = \frac{1}{2} \sum_{k=1}^K X_k \lambda_k + \frac{1}{\sum_{k=1}^K X_k / \lambda_k} \quad (50)$$

Thermal Diffusion Ratios

The thermal diffusion coefficients are evaluated in the following section on multicomponent properties. This section describes a relatively inexpensive way to estimate the thermal diffusion of light species into a mixture. This is the method that is used in our previous transport package, and it is included here for the sake of upward compatibility. This approximate method is considerably less accurate than the thermal diffusion coefficients that are computed from the multicomponent formulation.

A thermal diffusion ratio Θ_k can be defined such that the thermal diffusion velocity w_k is given by

$$w_{k_i} = \frac{D_{km} \Theta_k}{X_k} \frac{1}{T} \frac{\partial T}{\partial x_i} \quad (51)$$

where x_i is a spatial coordinate. The mole fractions are given by X_k , and the D_{km} are mixture diffusion coefficients Eq. (42). In this form we only consider thermal diffusion in the trace, light component limit (specifically, species k having molecular mass less than 5). The thermal diffusion ratio¹⁷ is given by

$$\Theta_k = \sum_{j \neq k}^K \theta_{kj} \quad (52)$$

where

$$\theta_{kj} = \frac{15}{2} \frac{(2A_{kj}^* + 5)(6C_{kj}^* - 5)}{A_{kj}^* (16A_{kj}^* - 12B_{kj}^* + 55)} \frac{M_j - M_k}{M_j + M_k} X_j X_k \quad (53)$$

Three ratios of collision integrals are defined by

$$A_{ij}^* = \frac{1}{2} \frac{\Omega_{ij}^{(2,2)}}{\Omega_{ij}^{(1,1)}} \quad (54)$$

$$B_{ij}^* = \frac{1}{3} \frac{5\Omega_{ij}^{(1,2)} - \Omega_{ij}^{(1,3)}}{\Omega_{ij}^{(1,1)}} \quad (55)$$

$$C_{ij}^* = \frac{1}{3} \frac{\Omega_{ij}^{(1,2)}}{\Omega_{ij}^{(1,1)}} \quad (56)$$

We have fit polynomials to tables of A_{ij}^* , B_{ij}^* , and C_{ij}^* .⁹

In the preprocessor fitting code (where the pure species properties are fit) we also fit the temperature dependent parts of the pairs of the thermal diffusion ratios for each light species into all the other species. That is, we fit $\theta_{kj}/(X_j X_k)$ for all species pairs in which $M_k < 5$. Since the θ_{kj} depend weakly on temperature, we fit to polynomials in temperature, rather than the logarithm of temperature. The coefficients of these fits are written onto the linking file.

The Multicomponent Properties

The multicomponent diffusion coefficients, thermal conductivities, and thermal diffusion coefficients are computed from the solution of a system of equations defined by what we call the L matrix. It is convenient to refer to the L matrix in terms of its nine block sub-matrices, and in this form the system is given by

$$\begin{array}{ccc|c} L^{00,00} & L^{00,10} & 0 & a_{00}^1 \\ L^{10,00} & L^{10,10} & L^{10,01} & a_{10}^1 \\ 0 & L^{01,10} & L^{01,01} & a_{01}^1 \end{array} = \begin{array}{c} 0 \\ X \\ X \end{array} \quad (57)$$

where right hand side vector is composed of the mole fraction vectors X_k . The multicomponent diffusion coefficients are given in terms of the inverse of the $L^{00,00}$ block as

$$D_{i,j} = X_i \frac{16T}{25p} \frac{\bar{m}}{m_j} (P_{ij} - P_{ii}), \quad (58)$$

where

$$(P) = L^{00,00^{-1}} \quad (59)$$

The thermal conductivities are given in terms of the solution to the system of equations by

$$\lambda_{0,\text{tr.}} = - \sum_{k=1}^K X_k a_{k10}^1 \quad (60)$$

$$\lambda_{0,\text{int.}} = - \sum_{k=1}^K X_k a_{k01}^1 \quad (61)$$

$$\lambda_0 = \lambda_{0,\text{tr.}} + \lambda_{0,\text{int.}} \quad (62)$$

and the thermal diffusion coefficients are given by

$$D_k^T = \frac{8m_k X_k}{5R} a_{k00}^1 \quad (63)$$

The components of the L matrix are given by Dixon-Lewis,³

$$L_{ij}^{00,00} = \frac{16T}{25p} \sum_{k=1}^K \frac{X_k}{m_i \mathcal{D}_{ik}} \{m_j X_j (1 - \delta_{ik}) - m_i X_j (\delta_{ij} - \delta_{jk})\}$$

$$L_{ij}^{00,10} = \frac{8T}{5p} \sum_{k=1}^K X_j X_k (\delta_{ij} - \delta_{ik}) \frac{m_k (1.2C_{jk}^* - 1)}{(m_j + m_k) \mathcal{D}_{jk}}$$

$$L_{ij}^{10,00} = L_{ji}^{00,10}$$

$$L_{ij}^{01,00} = L_{ji}^{00,01} = 0$$

$$L_{ij}^{10,10} = \frac{16T}{25p} \sum_{k=1}^K \frac{m_i}{m_j} \frac{X_i X_k}{(m_i + m_k)^2 \mathcal{D}_{ik}} \times \left(\delta_{jk} - \delta_{ij} \right) \frac{15}{2} m_j^2 + \frac{25}{4} m_k^2 - 3m_k^2 B_{ik}^* - 4m_j m_k A_{ik}^* (\delta_{jk} + \delta_{ij}) \left[1 + \frac{5}{3\pi} \frac{c_{i,\text{rot}}}{k_B \xi_{ik}} + \frac{c_{k,\text{rot}}}{k_B \xi_{ki}} \right] \quad (64)$$

$$L_{ii}^{10,10} = -\frac{16m_i X_i^2}{R\eta_i} \left[1 + \frac{10c_{i,\text{rot}}}{k_B \xi_{ii}} \right] - \frac{16T}{25p} \sum_{k \neq i}^K \frac{X_i X_k}{(m_i + m_k)^2 \mathcal{D}_{ik}} \times \left(\frac{15}{2} m_i^2 + \frac{25}{4} m_k^2 - 3m_k^2 B_{ik}^* + 4m_i m_k A_{ik}^* \right) \times \left[1 + \frac{5}{3\pi} \frac{c_{i,\text{rot}}}{k_B \xi_{ik}} + \frac{c_{k,\text{rot}}}{k_B \xi_{ki}} \right]$$

$$L_{ij}^{10,01} = \frac{32T}{5\pi p c_{j,\text{int}}} \sum_{k=1}^K \frac{m_j A_{jk}^*}{(m_j + m_k) \mathcal{D}_{jk}} (\delta_{ik} + \delta_{ij}) X_j X_k \frac{c_{j,\text{rot}}}{k_B \xi_{jk}}$$

$$L_{ii}^{10,01} = \frac{16}{3\pi} \frac{m_i X_i^2 k_B}{R\eta_i c_{i,\text{int}}} \frac{c_{i,\text{int}}}{k_B \xi_{ii}} + \frac{32T k_B}{5\pi p c_{i,\text{int}}} \sum_{k \neq i}^K \frac{m_i A_{ik}^*}{(m_i + m_k) \mathcal{D}_{jk}} X_j X_k \frac{c_{i,\text{rot}}}{k_B \xi_{ik}}$$

$$L_{ij}^{01,10} = L_{ji}^{10,01}$$

$$L_{ii}^{01,10} = -\frac{8k_B^2}{\pi c_{i,int}^2} \frac{m_i X_i^2}{R \eta_i} \frac{c_{i,rot}}{k_B \xi_{ii}}$$

$$-\frac{4k_B T}{c_{i,int} p} \left| \frac{K}{k=1} \frac{X_i X_k}{D_{i,int,k}} + \frac{K}{k \neq i} \frac{12 X_i X_k}{5 \pi c_{i,int}} \frac{m_i}{m_k} \frac{A_{ik}^*}{\mathcal{D}_{ik}} \frac{c_{i,rot}}{\xi_{ii}} \right|$$

$$L_{ij}^{01,01} = 0 \quad (i \neq j)$$

In these equations T is the temperature, p is the pressure, X_k is the mole fraction of species k , \mathcal{D}_{ik} are the binary diffusion coefficients, and m_i is the molecular mass of species i . Three ratios of collision integrals A_{jk}^* , B_{jk}^* , and C_{jk}^* are defined by Eqs. (54-56). The universal gas constant is represented by R and the pure species viscosities are given as η_k . The rotational and internal parts of the species molecular heat capacities are represented by $c_{k,rot}$ and $c_{k,int}$. For a linear molecule

$$\frac{c_{k,rot}}{k_B} = 1, \quad (65)$$

and for a nonlinear molecule

$$\frac{c_{k,rot}}{k_B} = \frac{3}{2}. \quad (66)$$

The internal component of heat capacity is computed by subtracting the translational part from the full heat capacity as evaluated from the CHEMKIN Thermodynamic Database. ¹

$$\frac{c_{k,int}}{k_B} = \frac{c_p}{k_B} - \frac{3}{2}. \quad (67)$$

Following Dixon-Lewis, ³ we assume that the relaxation collision numbers ξ_{ij} depend only on the species i , i.e., all $\xi_{ij} = \xi_{ii}$. The rotational relaxation collision number at 298K is one of the parameters in the transport data base, and its temperature dependence was given in Eqs. (32) and (33).

For non-polar gases the binary diffusion coefficients for internal energy $\mathcal{D}_{i,int,k}$ are approximated by the ordinary binary diffusion coefficients. However, in the case of collisions between polar molecules, where the exchange is energetically resonant, a large correction of the following form is necessary,

$$\mathcal{D}_{p \text{ int}, p} = \frac{\mathcal{D}_{pp}}{(1 + \delta'_{pp})}, \quad (68)$$

where,

$$\delta'_{pp} = \frac{2985}{\sqrt{T^3}} \quad (69)$$

when the temperature is in Kelvins.

There are some special cases that require modification of the L matrix. First, for mixtures containing monatomic gases, the rows that refer to the monatomic components in the lower block row and the corresponding columns in the last block column must be omitted. That this required is clear by noting that the internal part of the heat capacity appears in the denominator of terms in these rows and columns (e.g., $L_{ij}^{10,01}$). An additional problem arises as a pure species situation is approached, because all X_k except one approach zero, and this causes the L matrix to become singular. Therefore, for the purposes of forming L we do not allow a pure species situation to occur. We always retain a residual amount of each species by computing the mole fractions from

$$X_k = \frac{\bar{M}Y_k}{M_k} + \delta \quad (70)$$

A value of $\delta = 10^{-12}$ works well; it is small enough to be numerically insignificant compared to any mole fraction of interest, yet it is large enough to be represented on nearly any computer.

Species Conservation

Some care needs to be taken in using the mixture-averaged diffusion coefficients as described here. The mixture formulas are approximations, and they are not constrained to require that the net species diffusion flux is zero, i.e., the condition.

$$\sum_{k=1}^K \mathbf{V}_k Y_k = 0 \quad (71)$$

need not be satisfied. Therefore, one must expect that applying these mixture diffusion relationships in the solution of a system of species conservation equations should lead to some nonconservation, i.e., the resultant mass fractions will not sum to one. Therefore, one of a number of corrective actions must be invoked to ensure mass conservation.

Unfortunately, resolution of the conservation problem requires knowledge of species flux, and hence details of the specific problem and discretization method. Therefore, it is not reasonable in the general setting of the present code package to attempt to enforce conservation. Nevertheless, the user

of the package must be aware of the difficulty, and consider its resolution when setting up the difference approximations to his particular system of conservation equations.

One attractive method is to define a “conservation diffusion velocity” as Coffee and Heimerl⁷ recommend. In this approach we assume that the diffusion velocity vector is given as

$$\mathbf{V}_k = \hat{\mathbf{V}}_k + \mathbf{V}_c, \quad (72)$$

where $\hat{\mathbf{V}}_k$ is the ordinary diffusion velocity Eq. (42) and \mathbf{V}_c is a constant correction factor (independent of species, but spatially varying) introduced to satisfy Eq. (71). The correction velocity is defined by

$$\mathbf{V}_c = -\sum_{k=1}^K Y_k \hat{\mathbf{V}}_k. \quad (73)$$

This approach is the one followed by Miller et al.¹⁸⁻²⁰ in their flame models.

An alternative approach is attractive in problems having one species that is always present in excess. Here, rather than solving a conservation equation for the one excess species, its mass fraction is computed simply by subtracting the sum of the remaining mass fractions from unity. A similar approach involves determining locally at each computational cell which species is in excess. The diffusion velocity for that species is computed to require satisfaction of Eq. (71).

Even though the multicomponent formulation is theoretically forced to conserve mass, the numerical implementations can cause some slight nonconservation. Depending on the numerical method, even slight inconsistencies can lead to difficulties. Methods that do a good job of controlling numerical errors, such as the differential/algebraic equation solver DASSL (Petzold, 1982), are especially sensitive to inconsistencies, and can suffer computational inefficiencies or convergence failures. Therefore, even when the multicomponent formulation is used, it is often advisable to provide corrective measures such as those described above for the mixture-averaged approach. However, the magnitude of any such corrections will be significantly smaller.

III. THE MECHANICS OF USING THE PACKAGE

Using the TRANSPORT package requires the manipulation of several FORTRAN programs, libraries and data files. Also, it must be used in conjunction with the CHEMKIN-III gas-phase chemical kinetics package. The general flow of information is depicted in Fig. 1.

The first step is to execute the CHEMKIN Interpreter. The gas-phase CHEMKIN kinetics package is documented separately,² so we only outline its use here. The CHEMKIN Interpreter first reads (Unit 5) user-supplied information about the species and chemical reactions in a problem. It then extracts further information about the species' thermodynamic properties from the Thermodynamics Database.¹ This information is stored on the CHEMKIN Linking File, a file that is needed by the TRANSPORT Property Fitting routine, and later by the CHEMKIN subroutine library.

The next code to be executed is the TRANSPORT Property Fitting routine. It needs input from the TRANSPORT Property Database, and from the CHEMKIN Linking File. The TRANSPORT database contains molecular parameters for a number of species; these parameters are: The Lennard-Jones well depth ε/k_B in Kelvins, the Lennard-Jones collision diameter σ in Angstroms, the dipole moment μ in Debyes, the polarizability α in cubic angstroms, the rotational relaxation collision number Z_{rot} and an indicator regarding the nature and geometrical configuration of the molecule. The information coming from the CHEMKIN Linking File contains the species names in both the CHEMKIN and the TRANSPORT databases must correspond exactly. Like the CHEMKIN Interpreter, the TRANSPORT Fitting routine produces a TRANSPORT Linking File that is later needed in the TRANSPORT Property Subroutine Library.

Both the CHEMKIN and the TRANSPORT subroutine libraries must be initialized before use and there is a similar initialization subroutine in each. The TRANSPORT subroutine library is initialized by a call to SUBROUTINE MCINIT. Its purpose is to read the TRANSPORT Linking File and set up the internal working and storage space that must be made available to all other subroutines in the library. Once initialized, any subroutine in the library may be called from the application programs.

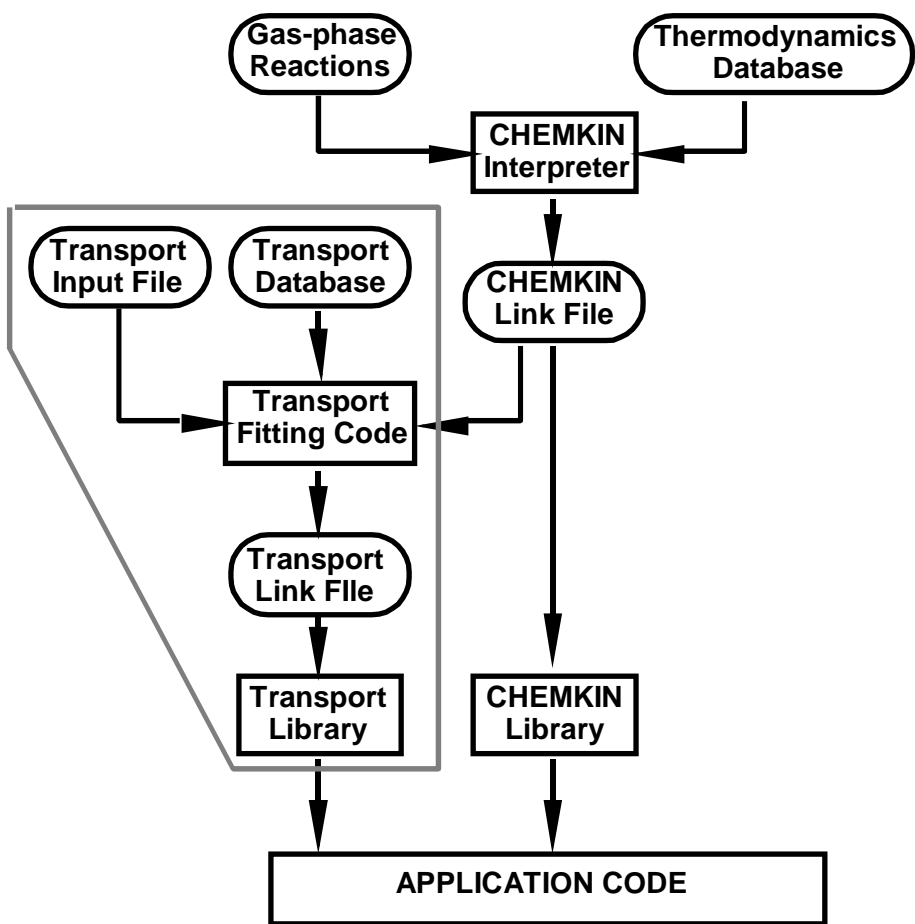


Figure 1. Schematic representing the relationship of the TRANSPORT package, CHEMKIN, and the application code.

IV. SUBROUTINE DESCRIPTIONS

This section provides the detailed descriptions of all subroutines in the library. There are eleven user-callable subroutines in the package. All subroutine names begin with MC. The following letter is either an S and A or an M, indicating whether pure species (S), mixture-averaged (A), or multicomponent (M) properties are returned. The remaining letters indicate which property is returned: CON for conductivity, VIS for viscosity, DIF for diffusion coefficients, CDT for both conductivity and thermal diffusion coefficients, and TDR for the thermal diffusion ratios.

A call to the initialization subroutine MCINIT must precede any other call. This subroutine is normally called only once at the beginning of a problem; it reads the linking file and sets up the internal storage and working space - arrays IMCWRK and RMCWRK. These arrays are required input to all other subroutines in the library. Besides MCINIT there is only one other non-property subroutine, called MCPGRAM; it is used to return the arrays of molecular parameters that came from the data base for the species in the problem. All other subroutines are used to compute either viscosities, thermal conductivities, or diffusion coefficients. They may be called to return pure species properties, mixture-averaged properties, or multicomponent properties.

In the input to all subroutines, the state of the gas is specified by the pressure in dynes per square centimeter, temperature in Kelvins, and the species mole fractions. The properties are returned in standard CGS units. The order of vector information, such as the vector of mole fractions or pure species viscosities, is the same as the order declared in the CHEMKIN Interpreter input.

We first provide a short description of each subroutine according to its function. Then, a longer description of each subroutine, listed in alphabetical order, follows.

Initialization and Parameters

SUBROUTINE MCINIT (LINKMC, LOUT, LENIMC, LENRMC, IMCWRK, RMCWRK)

This subroutine serves to read the linking file from the fitting code and to create the internal storage and work arrays, IMCWRK(*) and RMCWRK (*). MCINIT must be called before any other transport subroutine is called. It must be called after the CHEMKIN package is initialized.

SUBROUTINE MCPGRAM (IMCWRK, RMCWRK EPS, SIG, DIP, POL, ZROT, NLIN)

This subroutine is called to return the arrays of molecular parameters as read from the transport data base.

Viscosity

SUBROUTINE MCAVIS (T, RMCWRK, VIS)

This subroutine computes the array of pure species viscosities given the temperature.

SUBROUTINE MCAVIS (T, X, RMCWRK, VISMIX)

This subroutine computes the mixture viscosity given the temperature and the species mole fractions. It uses modifications of the Wilke semi-empirical formulas.

Conductivity

SUBROUTINE MCSCON (T, RMCWRK, CON)

This subroutine computes the array pure species conductivities given the temperature.

SUBROUTINE MCACON (T, X, RMCWRK, CONMIX)

This subroutine computes the mixture thermal conductivity given the temperature and the species mole fractions.

SUBROUTINE MCMCDT (P, T, X, KDIM, IMCWRK, RMCWRK, ICKWRK, CKWRK, DT, COND)

This subroutine computes the thermal diffusion coefficients and mixture thermal conductivities given the pressure, temperature, and mole fractions.

Diffusion Coefficients

SUBROUTINE MCSDIF (P, T, KDIM, RMCWRK, DJK)

This subroutine computes the binary diffusion coefficients given the pressure and temperature.

SUBROUTINE MCADIF (P, T, X, RMCWRK, D)

This subroutine computes the mixture-averaged diffusion coefficients given the pressure, temperature, and species mole fractions.

SUBROUTINE MCMDIF (P, T, X, KDIM, IMCWRK, RMCWRK, D)

This subroutine computes the ordinary multicomponent diffusion coefficients given the pressure, temperature, and mole fractions.

Thermal Diffusion

SUBROUTINE MCATDR (T, X, IMCWRK, RMCWRK, TDR)

This subroutine computes the thermal diffusion ratios for the light species into the mixture.

SUBROUTINE MCMCDT (P, T, X, IMCWRK, RMCWRK, ICKWRK, CKWRK, DT, COND)

This subroutine computes the thermal diffusion coefficients, and mixture thermal conductivities given the pressure, temperature, and mole fractions.

Detailed Subroutine Descriptions

The following pages list detailed descriptions for the user interface to each of the package's eleven user-callable subroutines. They are listed in alphabetical order.

```
MCACON  MCACON  MCACON  MCACON  MCACON  MCACON  MCACON  MCACON
*****
*****
*****
```

```
SUBROUTINE MCACON (T, X, RMCWRK, CONMIX)
Returns the mixture thermal conductivity given temperature and
species mole fractions.
```

INPUT

```
T          - Real scalar, temperature.
             cgs units, K
X(*)       - Real array, mole fractions of the mixture;
             dimension at least KK, the total species count.
RMCWRK(*)  - Real workspace array; dimension at least LENRMC.
```

OUTPUT

```
CONMIX     - Real scalar, mixture thermal conductivity.
             cgs units, erg/cm*K*s
```

MCADIF MCADIF MCADIF MCADIF MCADIF MCADIF MCADIF MCADIF

SUBROUTINE MCADIF (P, T, X, RMCWRK, D)

Returns mixture-averaged diffusion coefficients given pressure,
temperature, and species mass fractions.

INPUT

P - Real scalar, pressure.
cgs units, dynes/cm**2
T - Real scalar, temperature.
cgs units, K
X(*) - Real array, mole fractions of the mixture;
dimension at least KK, the total species count.
RMCWRK(*) - Real workspace array; dimension at least LENRMC.

OUTPUT

D(*) - Real array, mixture diffusion coefficients;
dimension at least KK, the total species count.
cgs units, cm**2/s

MCAVIS MCAVIS MCAVIS MCAVIS MCAVIS MCAVIS MCAVIS MCAVIS

SUBROUTINE MCAVIS (T, X, RMCWRK, VISMIX)
Returns mixture viscosity, given temperature and species mole fractions. It uses modification of the Wilke semi-empirical formulas.

INPUT

- T - Real scalar, temperature.
cgs units, K
- X(*) - Real array, mole fractions of the mixture;
dimension at least KK, the total species count.
- RMCWRK(*) - Real workspace array; dimension at least LENRMC.

OUTPUT

- VISMIX - Real scalar, mixture viscosity.
cgs units, gm/cm*s

```

MCINIT  MCINIT  MCINIT  MCINIT  MCINIT  MCINIT  MCINIT  MCINIT
*****
*****
*****

```

```

SUBROUTINE MCINIT (LINKMC, LOUT, LENIMC, LENRMC, IMCWRK, RMCWRK,
                  IFLAG)

```

This subroutine reads the transport linkfile from the fitting code and creates the internal storage and work arrays, IMCWRK(*) and RMCWRK(*). MCINIT must be called before any other transport subroutine is called. It must be called after the CHEMKIN package is initialized.

INPUT

- LINKMC - Integer scalar, transport linkfile input unit number.
- LOUT - Integer scalar, formatted output file unit number.
- LENIMC - Integer scalar, minimum dimension of the integer storage and workspace array IMCWRK(*);
LENIMC must be at least:
 $LENIMC = 4*KK + NLITE$,
where KK is the total species count, and
NLITE is the number of species with molecular weight less than 5.
- LENRMC - Integer scalar, minimum dimension of the real storage and workspace array RMCWRK(*);
LENRMC must be at least:
 $LENRMC = KK*(19 + 2*NO + NO*NLITE) + (NO+15)*KK**2$,
where KK is the total species count,
NO is the order of the polynomial fits (NO=4),
NLITE is the number of species with molecular weight less than 5.

OUTPUT

- IMCWRK(*) - Integer workspace array; dimension at least LENIMC.
- RMCWRK(*) - Real workspace array; dimension at least LENRMC.

MCLLEN MCLLEN MCLLEN MCLLEN MCLLEN MCLLEN MCLLEN MCLLEN

SUBROUTINE MCLLEN (LINKMC, LOU, LI, LR, IFLAG)
Returns the lengths required for work arrays.

INPUT

LINKMC - Integer scalar, input file unit for the linkfile.
LOU - Integer scalar, formatted output file unit.

OUTPUT

LI - Integer scalar, minimum length required for the integer work array.
LR - Integer scalar, minimum length required for the real work array.
IFLAG - Integer scalar, indicates successful reading of linkfile; IFLAG>0 indicates error type.

MCMCDT MCMCDT MCMCDT MCMCDT MCMCDT MCMCDT MCMCDT MCMCDT

SUBROUTINE MCMCDT (P, T, X, IMCWRK, RMCWRK, ICKWRK, CKWRK,
DT, COND)

Returns thermal diffusion coefficients, and mixture thermal
conductivities, given pressure, temperature, and mole fraction.

INPUT

P - Real scalar, pressure.
cgs units, dynes/cm**2
T - Real scalar, temperature.
cgs units, K
X(*) - Real array, mole fractions of the mixture;
dimension at least KK, the total species count.

IMCWRK(*) - Integer TRANSPORT workspace array;
dimension at least LENIMC.

RMCWRK(*) - Real TRANSPORT workspace array;
dimension at least LENRMC.

ICKWRK(*) - Integer CHEMKIN workspace array;
dimension at least LENICK.

RCKWRK(*) - Real CHEMKIN workspace array;
dimension at least LENRCK.

OUTPUT

DT(*) - Real array, thermal multicomponent diffusion
coefficients;
dimension at least KK, the total species count.
cgs units, gm/(cm*sec)
CGS UNITS - GM/(CM*SEC)
COND - Real scalar, mixture thermal conductivity.
cgs units, erg/(cm*K*s)

MCMDIF MCMDIF MCMDIF MCMDIF MCMDIF MCMDIF MCMDIF MCMDIF

SUBROUTINE MCMDIF (P, T, X, KDIM, IMCWRK, RMCWRK, D)

Returns the ordinary multicomponent diffusion coefficients,
given pressure, temperature, and mole fractions.

INPUT

P - Real scalar, pressure.
cgs units, dynes/cm**2
T - Real scalar, temperature.
cgs units, K
X(*) - Real array, mole fractions of the mixture;
dimension at least KK, the total species count.
KDIM - Integer scalar, actual first dimension of D(KDIM, KK);
KDIM must be at least KK, the total species count.
IMCWRK(*) - Integer workspace array; dimension at least LENIMC.
RMCWRK(*) - Real workspace array; dimension at least LENRMC.

OUTPUT

D(*,*) - Real matrix, ordinary multicomponent diffusion
coefficients;
dimension at least KK, the total species count, for
both the first and second dimensions.
cgs units, cm**2/s

MCPNT MCPNT MCPNT MCPNT MCPNT MCPNT MCPNT MCPNT

SUBROUTINE MCPNT (LSAVE, LOUT, NPOINT, V, P, LI, LR, IERR)
Reads from a binary file information about a Transport linkfile,
pointers for the Transport Library, and returns lengths of work
arrays.

INPUT

LSAVE - Integer scalar, input unit for binary data file.
LOUT - Integer scalar, formatted output file unit.

OUTPUT

NPOINT - Integer scalar, total number of pointers.
V - Real scalar, version number of the Transport linkfile.
P - Character string, machine precision of the linkfile.
LI - Integer scalar, minimum dimension required for integer
workspace array.
LR - Integer scalar, minimum dimension required for real
workspace array.
IERR - Logical, error flag.

MCPGRAM MCPGRAM MCPGRAM MCPGRAM MCPGRAM MCPGRAM MCPGRAM MCPGRAM

SUBROUTINE MCPGRAM (IMCWRK, RMCWRK, EPS, SIG, DIP, POL, ZROT, NLIN)
 Returns the arrays of molecular parameters as read from the
 transport database.

INPUT

IMCWRK(*) - Integer workspace array; dimension at least LENIMC.
 RMCWRK(*) - Real workspace array; dimension at least LENRMC.

OUTPUT

EPS(*) - Real array, Lennard-Jones Potential well depths for
 the species;
 dimension at least KK, the total species count.
 cgs units, K
 SIG(*) - Real array, Lennard-Jones collision diameters for
 the species;
 dimension at least KK, the total species count.
 cgs units, Angstrom
 DIP(*) - Real array, dipole moments for the species;
 dimension at least KK, the total species count.
 cgs units, Debye
 POL(*) - Real array, polarizabilities for the species;
 dimension at least KK, the total species count.
 cgs units, Angstrom**3
 ZROT(*) - Real array, rotational collision numbers evaluated at
 298K for the species;
 dimension at least KK, the total species count.
 NLIN(*) - Integer array, flags for species linearity;
 dimension at least KK, the total species count.
 NLIN=0, single atom,
 NLIN=1, linear molecule,
 NLIN=2, linear molecule.

```
MCSAVE  MCSAVE  MCSAVE  MCSAVE  MCSAVE  MCSAVE  MCSAVE  MCSAVE
*****
*****
*****
```

SUBROUTINE MCSAVE (LOUT, LSAVE, IMCWRK, RMCWRK)
Writes to a binary file information about a Transport linkfile,
pointers for the Transport library, and Transport work arrays.

INPUT
LOUT - Integer scalar, formatted output file unit number.
LSAVE - Integer scalar, unformatted output file unit number.
IMCWRK(*) - Integer workspace array; dimension at least LENIMC.
RMCWRK(*) - Real workspace array; dimension at least LENRMC.


```
MCSCON  MCSCON  MCSCON  MCSCON  MCSCON  MCSCON  MCSCON  MCSCON
*****
*****
*****
```

SUBROUTINE MCSCON (T, RMCWRK, CON)
Returns the array of pur species conductivities given temperature.

INPUT

T - Real scalar, temperature.
cgs units, K
RMCWRK(*) - Real workspace array; dimension at least LENRMC.

OUTPUT

CON(*) - Real array, species thermal conductivities;
dimension at least KK, the total species count.
cgs units, erg/cm*K*s

MCS DIF MCS DIF MCS DIF MCS DIF MCS DIF MCS DIF MCS DIF MCS DIF

SUBROUTINE MCS DIF (P, T, KDIM, RMCWRK, DJK)

Returns the binary diffusion coefficients given pressure and temperature.

INPUT

P - Real scalar, pressure.

cgs units, dynes/cm**2

T - Real scalar, temperature.

cgs units, K

KDIM - Integer scalar, actual first dimension of DJK(KDIM, KK).

RMCWRK(*) - Real workspace array; dimension at least LENRMC.

OUTPUT

DJK(*, *) - Real matrix, binary diffusion coefficients; dimension at least KK, the total species count, for both the first and second dimensions.

cgs units, cm**2/s

CJK(J, K) is the diffusion coefficient of species J in species K.

```
MCSVIS  MCSVIS  MCSVIS  MCSVIS  MCSVIS  MCSVIS  MCSVIS  MCSVIS
*****
*****
*****
```

SUBROUTINE MCSVIS (T, RMCWRK, VIS)

Returns the array of pure species viscosities, given temperature.

INPUT

T - Real scalar, temperature.
cgs units, K

RMCWRK(*) - Real workspace array; dimension at least LENRMC.

OUTPUT

VIS(*) - Real array, species viscosities;
dimension at least KK, the total species count.
cgs units, gm/cm*s

V. TRANSPORT DATA BASE

In this section we list the data base that we currently use. New species are easily added and as new or better data becomes available, we expect that users will change their versions of the data base to suit their own needs. This data base should not be viewed as the last word in transport properties. Instead, it is a good starting point from which a user will provide the best available data for his particular application. However, when adding a new species to the data base, be sure that the species name is exactly the same as it is in the CHEMKIN Thermodynamic Database.¹

Some of the numbers in the data base have been determined by computing “best fits” to experimental measurements of some transport property (e.g. viscosity). In other cases the Lennard-Jones parameters have been estimated following the methods outlined in Svehla.²¹

The first 15 columns in each line of the data base are reserved for the species name, and the first character of the name must begin in column 1. (Presently CHEMKIN is programmed to allow no more than 10-character names.) Columns 16 through 80 are unformatted, and they contain the molecular parameters for each species. They are, in order:

1. An index indicating whether the molecule has a monatomic, linear or nonlinear geometrical configuration. If the index is 0, the molecule is a single atom. If the index is 1 the molecule is linear, and if it is 2, the molecule is nonlinear.
2. The Lennard-Jones potential well depth ϵ/k_B in Kelvins.
3. The Lennard-Jones collision diameter σ in Angstroms.
4. The dipole moment μ in Debye. Note: a Debye is $10^{-18}\text{cm}^3/2\text{erg}^{1/2}$.
5. The polarizability α in cubic Angstroms.
6. The rotational relaxation collision number Z_{rot} at 298K.
7. After the last number, a comment field can be enclosed in parenthesis.

Species Name	Geometry	ϵ/k_B	σ	μ	α	Z_{rot}
Al2Me6	2	471.	6.71	0.0	0.0	1.0
AlMe3	2	471.	5.30	0.0	0.0	1.0
AR	0	136.500	3.330	0.000	0.000	0.000
AR*	0	136.500	3.330	0.000	0.000	0.000
AS	0	1045.5	4.580	0.000	0.000	0.000
AS2	1	1045.5	5.510	0.000	0.000	1.000
ASH	1	199.3	4.215	0.000	0.000	1.000
ASH2	2	229.6	4.180	0.000	0.000	1.000
ASH3	2	259.8	4.145	0.000	0.000	1.000
AsH3	2	259.8	4.145	0.000	0.000	1.000
BCL3	2	337.7	5.127	0.000	0.000	1.000
C	0	71.400	3.298	0.000	0.000	0.000
C-Si3H6	2	331.2	5.562	0.000	0.000	1.000
C2	1	97.530	3.621	0.000	1.760	4.000
C2F4	2	202.6	5.164	0.000	0.000	1.000
C2F6	2	194.5	5.512	0.000	0.000	1.000
C2H	1	209.000	4.100	0.000	0.000	2.500
C2H2	1	209.000	4.100	0.000	0.000	2.500
C2H2OH	2	224.700	4.162	0.000	0.000	1.000
C2H3	2	209.000	4.100	0.000	0.000	1.000
C2H4	2	280.800	3.971	0.000	0.000	1.500
C2H5	2	252.300	4.302	0.000	0.000	1.500
C2H5OH	2	362.6	4.53	0.000	0.000	1.000
C2H6	2	252.300	4.302	0.000	0.000	1.500
C2N	1	232.400	3.828	0.000	0.000	1.000
C2N2	1	349.000	4.361	0.000	0.000	1.000
C2O	1	232.400	3.828	0.000	0.000	1.000
C3H2	2	209.000	4.100	0.000	0.000	1.000
C3H3	1	252.000	4.760	0.000	0.000	1.000
C3H4	1	252.000	4.760	0.000	0.000	1.000
C3H4P	1	252.000	4.760	0.000	0.000	1.000
C3H6	2	266.800	4.982	0.000	0.000	1.000
C3H7	2	266.800	4.982	0.000	0.000	1.000
C3H8	2	266.800	4.982	0.000	0.000	1.000
C4H	1	357.000	5.180	0.000	0.000	1.000
C4H2	1	357.000	5.180	0.000	0.000	1.000
C4H2OH	2	224.700	4.162	0.000	0.000	1.000
C4H3	1	357.000	5.180	0.000	0.000	1.000
C4H4	1	357.000	5.180	0.000	0.000	1.000
C4H6	2	357.000	5.180	0.000	0.000	1.000
C4H8	2	357.000	5.176	0.000	0.000	1.000
C4H9	2	357.000	5.176	0.000	0.000	1.000
C4H9	2	357.000	5.176	0.000	0.000	1.000
C5H2	1	357.000	5.180	0.000	0.000	1.000
C5H3	1	357.000	5.180	0.000	0.000	1.000
C5H5OH	2	450.000	5.500	0.000	0.000	1.000

Species Name	Geometry	ϵ/k_B	σ	μ	α	Z_{rot}
C6H2	1	357.000	5.180	0.000	0.000	1.000
C6H5	2	412.300	5.349	0.000	0.000	1.000
C6H5(L)	2	412.300	5.349	0.000	0.000	1.000
C6H5O	2	450.000	5.500	0.000	0.000	1.000
C6H6	2	412.300	5.349	0.000	0.000	1.000
C6H7	2	412.300	5.349	0.000	0.000	1.000
CF	1	94.2	3.635	0.000	0.000	1.000
CF2	2	108.0	3.977	0.000	0.000	1.000
CF3	2	121.0	4.320	0.000	0.000	1.000
CF4	2	134.0	4.662	0.000	0.000	1.000
CH	1	80.000	2.750	0.000	0.000	0.000
CH2	1	144.000	3.800	0.000	0.000	0.000
CH2(S)	1	144.000	3.800	0.000	0.000	0.000
CH2(SING)	1	144.000	3.800	0.000	0.000	0.000
CH2CHCCH	2	357.000	5.180	0.000	0.000	1.000
CH2CHCCH2	2	357.000	5.180	0.000	0.000	1.000
CH2CHCH2	2	260.000	4.850	0.000	0.000	1.000
CH2CHCHCH	2	357.000	5.180	0.000	0.000	1.000
CH2CHCHCH2	2	357.000	5.180	0.000	0.000	1.000
CH2CO	2	436.000	3.970	0.000	0.000	2.000
CH2F2	2	318.0	4.080	0.000	0.000	1.000
CH2HCO	2	436.000	3.970	0.000	0.000	2.000
CH2O	2	498.000	3.590	0.000	0.000	2.000
CH2OH	2	417.000	3.690	1.700	0.000	2.000
CH3	1	144.000	3.800	0.000	0.000	0.000
CH3CC	2	252.000	4.760	0.000	0.000	1.000
CH3CCCH2	2	357.000	5.180	0.000	0.000	1.000
CH3CCCH3	2	357.000	5.180	0.000	0.000	1.000
CH3CCH2	2	260.000	4.850	0.000	0.000	1.000
CH3CH2CCH	2	357.000	5.180	0.000	0.000	1.000
CH3CHCH	2	260.000	4.850	0.000	0.000	1.000
CH3CHO	2	436.000	3.970	0.000	0.000	2.000
CH3CO	2	436.000	3.970	0.000	0.000	2.000
CH3O	2	417.000	3.690	1.700	0.000	2.000
CH3OH	2	481.800	3.626	0.000	0.000	1.000
CH4	2	141.400	3.746	0.000	2.600	13.000
CH4O	2	417.000	3.690	1.700	0.000	2.000
CHF3	2	240.0	4.330	0.000	0.000	1.000
CL	0	130.8	3.613	0.000	0.000	1.000
CL-	0	130.8	3.613	0.000	0.000	1.000
CL2BNH2	2	337.7	5.127	0.000	0.000	1.000
CN	1	75.000	3.856	0.000	0.000	1.000
CN2	1	232.400	3.828	0.000	0.000	1.000
CNC	1	232.400	3.828	0.000	0.000	1.000
CNN	1	232.400	3.828	0.000	0.000	1.000
CO	1	98.100	3.650	0.000	1.950	1.800

Species Name	Geometry	ϵ/k_B	σ	μ	α	Z_{rot}
CO2	1	244.000	3.763	0.000	2.650	2.100
DMG	2	675.8	5.22	0.000	0.000	1.000
E	0	850.	425.	0.000	0.000	1.000
F	0	80.000	2.750	0.000	0.000	0.000
F2	1	125.700	3.301	0.000	1.600	3.800
GA	0	2961.8	4.62	0.000	0.000	0.000
GACH3	2	972.7	4.92	0.000	0.000	1.000
GAH	1	335.5	4.24	0.000	0.000	1.000
GAME	2	972.7	4.92	0.000	0.000	1.000
GAME2	2	675.8	5.22	0.000	0.000	1.000
GAME3	2	378.2	5.52	0.000	0.000	1.000
GaMe3	2	378.2	5.52	0.000	0.000	1.000
H	0	145.000	2.050	0.000	0.000	0.000
H2	1	38.000	2.920	0.000	0.790	280.000
H2ASCH3	2	408.0	4.73	0.000	0.000	1.000
H2C4O	2	357.000	5.180	0.000	0.000	1.000
H2CCCCH	2	357.000	5.180	0.000	0.000	1.000
H2CCCCH2	2	357.000	5.180	0.000	0.000	1.000
H2CCCH	2	252.000	4.760	0.000	0.000	1.000
H2CN	1	569.000	3.630	0.000	0.000	1.000
H2NO	2	116.700	3.492	0.000	0.000	1.000
H2O	2	572.400	2.605	1.844	0.000	4.000
H2O2	2	107.400	3.458	0.000	0.000	3.800
H2S	2	301.000	3.600	0.000	0.000	1.000
H2SISIH2	2	312.6	4.601	0.000	0.000	1.000
H3SISIH	2	312.6	4.601	0.000	0.000	1.000
HC2N2	1	349.000	4.361	0.000	0.000	1.000
HCCHCCH	2	357.000	5.180	0.000	0.000	1.000
HCCO	2	150.000	2.500	0.000	0.000	1.000
HCCOH	2	436.000	3.970	0.000	0.000	2.000
HCL	1	344.7	3.339	0.000	0.000	1.000
HCN	1	569.000	3.630	0.000	0.000	1.000
HCNO	2	232.400	3.828	0.000	0.000	1.000
HCO	2	498.000	3.590	0.000	0.000	0.000
HCO+	1	498.000	3.590	0.000	0.000	0.000
HE	0	10.200	2.576	0.000	0.000	0.000
HF	1	330.000	3.148	1.920	2.460	1.000
HF0	1	352.000	2.490	1.730	0.000	5.000
HF1	1	352.000	2.490	1.730	0.000	5.000
HF2	1	352.000	2.490	1.730	0.000	5.000
HF3	1	352.000	2.490	1.730	0.000	5.000
HF4	1	352.000	2.490	1.730	0.000	5.000
HF5	1	352.000	2.490	1.730	0.000	5.000
HF6	1	352.000	2.490	1.730	0.000	5.000
HF7	1	352.000	2.490	1.730	0.000	5.000
HF8	1	352.000	2.490	1.730	0.000	5.000

Species Name	Geometry	ϵ/k_B	σ	μ	α	Z_{rot}
HNCO	2	232.400	3.828	0.000	0.000	1.000
HNNO	2	232.400	3.828	0.000	0.000	1.000
HNO	2	116.700	3.492	0.000	0.000	1.000
HNOH	2	116.700	3.492	0.000	0.000	1.000
HO2	2	107.400	3.458	0.000	0.000	1.000
HOCN	2	232.400	3.828	0.000	0.000	1.000
HSO2	2	252.000	4.290	0.000	0.000	1.000
I*C3H7	2	266.800	4.982	0.000	0.000	1.000
I*C4H9	2	357.000	5.176	0.000	0.000	1.000
K	0	850.	4.25	0.000	0.000	1.000
K+	0	850.	4.25	0.000	0.000	1.000
KCL	1	1989.	4.186	0.000	0.000	1.000
KH	1	93.3	3.542	0.000	0.000	1.000
KO	1	383.0	3.812	0.000	0.000	1.000
KO2	2	1213.	4.69	0.000	0.000	1.000
KOH	2	1213.	4.52	0.000	0.000	1.000
N	0	71.400	3.298	0.000	0.000	0.000
N*C3H7	2	266.800	4.982	0.000	0.000	1.000
N2	1	97.530	3.621	0.000	1.760	4.000
N2H2	2	71.400	3.798	0.000	0.000	1.000
N2H3	2	200.000	3.900	0.000	0.000	1.000
N2H4	2	205.000	4.230	0.000	4.260	1.500
N2O	1	232.400	3.828	0.000	0.000	1.000
NCN	1	232.400	3.828	0.000	0.000	1.000
NCNO	2	232.400	3.828	0.000	0.000	1.000
NCO	1	232.400	3.828	0.000	0.000	1.000
NH	1	80.000	2.650	0.000	0.000	4.000
NH2	2	80.000	2.650	0.000	2.260	4.000
NH3	2	481.000	2.920	1.470	0.000	10.000
NNH	2	71.400	3.798	0.000	0.000	1.000
NO	1	97.530	3.621	0.000	1.760	4.000
NO2	2	200.000	3.500	0.000	0.000	1.000
O	0	80.000	2.750	0.000	0.000	0.000
O(Si(OC2H5)3)2	2	522.7	5.25	0.000	0.000	1.000
O2	1	107.400	3.458	0.000	1.600	3.800
O3	2	180.000	4.100	0.000	0.000	2.000
OH	1	80.000	2.750	0.000	0.000	0.000
OSi(OC2H5)2	2	522.7	7.03	0.000	0.000	1.000
PH3	2	251.5	3.981	0.000	0.000	1.000
S	0	847.000	3.839	0.000	0.000	0.000
S*C4H9	2	357.000	5.176	0.000	0.000	1.000
S2	1	847.000	3.900	0.000	0.000	1.000
SH	1	847.000	3.900	0.000	0.000	1.000
SI	0	3036.	2.910	0.000	0.000	0.000
Si(OC2H5)4	2	522.7	7.03	0.000	0.000	1.000
SI(OC2H5)4	2	522.7	7.03	0.000	0.000	1.000

Species Name	Geometry	ϵ/k_B	σ	μ	α	Z_{rot}
Si(OH)(OC2H5)3	2	522.7	7.03	0.000	0.000	1.000
SI(OH)(OC2H5)3	2	522.7	7.03	0.000	0.000	1.000
SI(OH)2(OC2H5)2	2	522.7	6.35	0.000	0.000	1.000
Si(OH)2(OC2H5)2	2	522.7	6.35	0.000	0.000	1.000
SI(OH)3(OC2H5)	2	522.7	5.75	0.000	0.000	1.000
SI(OH)4	2	522.7	5.25	0.000	0.000	1.000
SI2	1	3036.	3.280	0.000	0.000	1.000
SI2H2	2	323.8	4.383	0.000	0.000	1.000
SI2H3	2	318.2	4.494	0.000	0.000	1.000
SI2H4	2	312.6	4.601	0.000	0.000	1.000
SI2H5	2	306.9	4.717	0.000	0.000	1.000
SI2H6	2	301.3	4.828	0.000	0.000	1.000
SI3	2	3036.	3.550	0.000	0.000	1.000
SI3H8	2	331.2	5.562	0.000	0.000	1.000
SIF	1	585.0	3.318	0.000	0.000	1.000
SIF3	2	309.6	4.359	0.000	0.000	1.000
SIF3NH2	2	231.0	4.975	0.000	0.000	1.000
SIF4	2	171.9	4.880	0.000	0.000	1.000
SIH	1	95.8	3.662	0.000	0.000	1.000
SIH2	2	133.1	3.803	0.000	0.000	1.000
SIH2(3)	2	133.1	3.803	0.000	0.000	1.000
SIH3	2	170.3	3.943	0.000	0.000	1.000
SIH3SIH2SIH	2	331.2	5.562	0.000	0.000	1.000
SIH4	2	207.6	4.084	0.000	0.000	1.000
SIHF3	2	180.8	4.681	0.000	0.000	1.000
SO	1	301.000	3.993	0.000	0.000	1.000
SO2	2	252.000	4.290	0.000	0.000	1.000
SO3	2	378.400	4.175	0.000	0.000	1.000
TMG	2	378.2	5.52	0.000	0.000	1.000

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