

A MaxBCG CATALOG OF 13,823 GALAXY CLUSTERS FROM THE SLOAN DIGITAL SKY SURVEY

B. P. KOESTER,¹ T. A. MCKAY,^{1,2} J. ANNIS,³ R. H. WECHSLER,⁴ A. EVRARD,^{1,2} L. BLEEM,⁵ M. BECKER,¹ D. JOHNSTON,⁶
E. SHELDON,⁷ R. NICHOL,⁸ C. MILLER,⁹ R. SCRANTON,¹⁰ N. BAHCALL,¹¹ J. BARENTINE,¹² H. BREWINGTON,¹²
J. BRINKMANN,¹² M. HARVANEK,¹² S. KLEINMAN,¹² J. KRZESINSKI,^{12,13} D. LONG,¹² A. NITTA,¹²
D. P. SCHNEIDER,¹⁴ S. SNEDDIN,¹² W. VOGES,¹⁵ AND D. YORK¹⁶

Received 2006 July 5; accepted 2006 September 18

ABSTRACT

We present a catalog of galaxy clusters selected using the maxBCG red-sequence method from Sloan Digital Sky Survey photometric data. This catalog includes 13,823 clusters with velocity dispersions greater than $\approx 400 \text{ km s}^{-1}$ and is the largest galaxy cluster catalog assembled to date. They are selected in an approximately volume-limited way from a 0.5 Gpc^3 region covering 7500 deg^2 of sky between redshifts 0.1 and 0.3. Each cluster contains between 10 and 190 E/S0 ridgeline galaxies brighter than $0.4L_*$ within a scaled radius R_{200} . The tight relation between ridgeline color and redshift provides an accurate photometric redshift estimate for every cluster. Photometric redshift errors are shown by comparison to spectroscopic redshifts to be small ($\Delta_z \simeq 0.01$), essentially independent of redshift, and well determined throughout the redshift range. Runs of maxBCG on realistic mock catalogs suggest that the sample is more than 90% pure and more than 85% complete for clusters with masses $\geq 1 \times 10^{14} M_\odot$. Spectroscopic measurements of cluster members are used to examine line-of-sight projection as a contaminant in the identification of brightest cluster galaxies and cluster member galaxies. Spectroscopic data are also used to demonstrate the correlation between optical richness and velocity dispersion. Comparison to the combined NORAS and REFLEX X-ray-selected cluster catalogs shows that X-ray-luminous clusters are found among the optically richer maxBCG clusters. This paper is the first in a series that will consider the properties of these clusters, their galaxy populations, and their implications for cosmology.

Subject heading: galaxies: clusters: general

Online material: machine-readable table

1. INTRODUCTION

Galaxy clusters are the most visible features of large-scale structure. They occupy very massive dark matter halos and are observationally accessible by many means. Their locations are revealed by the presence of large numbers of tightly clustered galaxies, pools of hot X-ray-emitting gas, and relatively strong features in the gravitational lensing shear field. Many of their properties, including their number as a function of dark matter mass and their spatial clustering, can be predicted with confi-

dence from N -body simulations. Since clusters occupy the tail of the halo mass function, their numbers are exponentially sensitive to variations in cosmology. Precise observations of large numbers of clusters provide an important tool for testing our understanding of cosmology and structure formation. Clusters are also interesting laboratories for the study of galaxy evolution under the influence of extreme environments.

Clusters were first detected in the 18th century (Biviano 2000) as significant overdensities of galaxies on the sky. The early 20th century saw the first explorations of their physical properties, including the discovery of dark matter in Zwicky's study of Coma (Zwicky 1933, 1937). Statistical studies of the cluster population became possible with the introduction of large-area surveys implementing uniform selection methods. For example, Abell and his collaborators (Abell 1958; Abell et al. 1989) created a sample of 4073 clusters over the whole sky by visually inspecting photographic plates. They identified clusters as overdensities of 30 or more galaxies (each no more than 2 mag fainter than the third brightest member, m_3) within a fixed metric aperture on the sky. Distances were estimated on the basis of the magnitude of the 10th brightest cluster member. Similar catalogs, with somewhat different selection criteria, were developed by Zwicky et al. (1961).

The Abell catalog has been very influential (see, e.g., Bahcall 1999 and references therein), supporting a wide range of cluster science. Among its most important achievements is that it enabled some of the first studies of the large-scale distribution of matter in the universe (Bahcall & Soneira 1983; Postman et al. 1992; Miller et al. 1999). The brightest galaxies in clusters have also been used to construct Hubble diagrams (Gunn & Oke 1975; Sandage et al. 1976; Postman & Lauer 1995). Studies of the Abell cluster catalogs have been hampered by problems of projection

¹ Department of Physics, University of Michigan, Ann Arbor, MI; bkoester@umich.edu, tamckay@umich.edu.

² Michigan Center for Theoretical Physics, University of Michigan, Ann Arbor, MI.

³ Fermi National Accelerator Laboratory, Batavia, IL.

⁴ Kavli Institute for Cosmological Physics, Department of Astronomy and Astrophysics, and Enrico Fermi Institute, University of Chicago, Chicago, IL; Hubble Fellow.

⁵ Department of Physics, University of Chicago, Chicago, IL.

⁶ Jet Propulsion Laboratory, California Institute of Technology, Pasadena, CA.

⁷ Center for Cosmology and Particle Physics, New York University, New York, NY.

⁸ Institute of Cosmology and Gravitation, University of Portsmouth, Portsmouth, UK.

⁹ Cerro Tololo Inter-American Observatory, NOAO, La Serena, Chile.

¹⁰ Department of Physics and Astronomy, University of Pittsburgh, Pittsburgh, PA.

¹¹ Princeton University Observatory, Princeton, NJ.

¹² Apache Point Observatory, Sunspot, NM.

¹³ Mount Suhora Observatory, Cracow Pedagogical University, Cracow, Poland.

¹⁴ Department of Astronomy and Astrophysics, Pennsylvania State University, University Park, PA.

¹⁵ Max-Planck-Institut für extraterrestrische Physik, Garching, Germany.

¹⁶ Department of Astronomy and Astrophysics and Enrico Fermi Institute, University of Chicago, Chicago, IL.

(Sutherland 1988; Collins et al. 1995), false clusters (Lucey 1983), and an uncertain selection function. Projection refers to the unwanted effect of unassociated foreground and background galaxies on the measured properties of clusters (richness, m_3 , etc.), while “false clusters” are objects that are overdense in projection, but not physically bound. Uncertainties in the selection function arise from the use of visual selection and the relatively poor calibration of photographic data.

These problems prompted the construction of new optically selected samples of clusters using digitized photographic material and automated cluster selection algorithms (Lumsden et al. 1992; Dalton et al. 1994; Gal et al. 2003). In recent years, the increased availability of large-area CCD photometry has prompted a new round of optical cluster selection (e.g., Gal 2006 and references therein). For example, Postman et al. (1996) constructed a sample of clusters using a “matched filter” technique, smoothing the galaxy distribution with a filter optimized for the detection of distant clusters. Another example is the direct search for clusters as resolved sources of diffuse optical light (Dalcanton 1996; Zaritsky et al. 1997; Gonzalez et al. 2001).

The advent of multicolor CCD photometry obtained over large areas has had a major impact. Precise measurement of galaxy color has literally added a new dimension to optical cluster finding. Clusters are dominated by old, red E/S0 galaxies that occupy a narrow region in color-magnitude space known as the E/S0 ridgeline (Bower et al. 1992). This tight clustering of galaxies in color, magnitude, and space allows significant improvements in cluster finding (Ostrander et al. 1998; Gladders & Yee 2000; Bahcall et al. 2003; Gladders & Yee 2005). The location of this ridgeline in color shifts smoothly with redshift, providing quite precise estimates of cluster redshift. These new “red-sequence” techniques have largely eliminated projection effects and false clusters from optical cluster catalogs, making it possible to perform accurate measurements of the large-scale structure in the universe by using such samples.

In parallel with advances in optical searches for clusters, there has been considerable progress in cluster identification in X-rays. Over the last decade, a variety of cluster catalogs have been constructed from X-ray surveys of the sky (Gioia & Luppino 1994; Ebeling et al. 1996; Rosati et al. 1998; Romer et al. 2000; Böhringer et al. 2000; Mullis et al. 2003; Böhringer et al. 2004). These surveys are less sensitive to projection effects, although they can be contaminated by active galactic nucleus (AGN) emission. In addition, the relation of X-ray luminosity and temperature to the underlying total mass of a cluster is thought to be more accessible to theoretical predictions than optical mass proxies. The principal limitation of X-ray cluster surveys is the relative scarcity of the observing resource. Existing all-sky surveys are limited to the detection of rare, high-flux sources. As a result, the total number of groups and clusters yet detected in X-rays is modest; there are only 1579 objects in the BAX database, a compendium of all X-ray groups and clusters detected as of 2004 (Sadat et al. 2004). With no future all-sky X-ray survey planned, it is unlikely that the number of X-ray-detected clusters will increase substantially over the next decade, although important contributions will be made by serendipitous surveys in the *XMM-Newton* and *Chandra* archives (Romer et al. 2001; Green et al. 2004; Romano et al. 2004).

Clusters have also been detected as peaks in the shear field of deep weak-lensing surveys (Erben et al. 2000; Clowe et al. 2001; Miralles et al. 2002; Wittman et al. 2001; Dahle et al. 2003; Wittman et al. 2003, 2006). This method has the virtue of directly probing the projected surface mass density of the clusters. Unfortunately, this projection introduces substantial noise in the mass

estimation for individual clusters (White et al. 2002; de Putter & White 2005). While lensing provides a unique test for the presence of truly dark clusters, it is otherwise an expensive detection method. To detect a cluster using lensing, images must be obtained of a large number of faint galaxies in the background of a cluster. The same images used to detect the shear always contain very high signal-to-noise ratio detections of many cluster galaxies, galaxies that would have been easily detected in much shallower imaging. While lensing is probably not an optimal method for cluster detection, it is a vital tool in cluster mass calibration (Sheldon et al. 2001; Johnston et al. 2007; Sheldon et al. 2006) for clusters detected by any other method.

In the future, large cluster catalogs will be constructed using observations of the Sunyaev-Zel’dovich (SZ) effect. The X-ray-emitting hot gas in clusters causes Compton upscattering of a small fraction of the cosmic microwave background (CMB) photons that pass through it. This leads to a characteristic distortion in the transmitted CMB spectrum (Carlstrom et al. 2002). Observation of these distortions provides an additional method for cluster detection. The SZ effect nicely combines the guarantee of a deep potential well provided by the hot gas along with a detection signature that is essentially independent of redshift. Of course SZ surveys must be supplemented by follow-up optical observations to determine redshifts if they are to be useful for cosmology. They will also benefit from the mass calibrations that weak-lensing measurements provide. As a result, combined SZ and optical surveys are a particularly promising approach for cluster study in the coming years.

The most significant challenge in cluster science lies in relating what is best understood about clusters from theory to what is measured in observations. Structure formation simulations can predict the evolution of the dark matter component of clusters with great confidence (e.g., Evrard et al. 2002). Observations provide measures of the cluster galaxies and gas with ever-increasing precision. Unfortunately, the cluster baryons that we observe participate in hydrodynamic and thermodynamic interactions that are too complex for current simulations to confidently model. This leaves an uncomfortably uncertain gap between theory and observation. Closing this gap is the goal of a substantial body of current research. New simulations of many kinds are pushing the ability to predict the evolution of galaxies and gas (e.g., Springel et al. 2005; Kravtsov et al. 2006), while new observations are extracting ever more direct and precise measurements of total cluster mass proxies (Vikhlinin et al. 2006; Diaferio et al. 2005; Majumdar & Mohr 2004; Katgert et al. 2004).

This paper describes a large new catalog of galaxy clusters extracted from Sloan Digital Sky Survey (SDSS) optical imaging data (York et al. 2000). It is the first in a series of papers that will explore the properties of optically selected SDSS cluster samples and their use for cosmology. Galaxy clusters are selected by calculating the likelihood that each observed galaxy is the brightest galaxy in a cluster. This likelihood is based on the galaxy’s color and magnitude, along with the degree to which other galaxies are clustered around it in color, magnitude, and space. The resulting catalog is an essentially volume-limited list of galaxy group and cluster locations, together with estimates of their total galaxy content and redshift. We present here a catalog of the richest objects detected by this method, including 13,823 clusters, each containing 10 or more E/S0 ridgeline galaxies brighter than $0.4L^*$ (in the i band) within a scaled radius R_{200} , drawn from about 7500 deg^2 of sky, and extending over a redshift range from $z = 0.1$ to 0.3 .

Section 2 presents a brief description of the SDSS data that are relevant for this paper. This is followed in § 3 by an outline

of the cluster selection algorithm, details of which are presented in a companion paper (Koester et al. 2007). Overall properties of the derived cluster catalog are presented in § 4. Basic tests of the completeness and purity of cluster selection based on mock catalogs are described in § 5. Tests of the quality of redshift estimates, the importance of projection effects, the relationship between cluster richness measures and velocity dispersion, and the space density of clusters are outlined in § 6. As an additional test, a comparison of this catalog to existing X-ray–selected cluster catalogs is provided in § 7. We conclude in § 8. Where needed, we assume a standard Λ CDM cosmology with $\Omega_M = 0.3$, $\Omega_\Lambda = 0.7$, and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2. DATA

Data for this study are drawn from the Sloan Digital Sky Survey,¹⁷ a combined imaging and spectroscopic survey of 10^4 deg^2 in the north Galactic cap and a smaller region in the south. The imaging survey was carried out using a specially designed 2.5 m telescope (Gunn et al. 2006) in drift-scan mode in five SDSS filters (u , g , r , i , and z) to a limiting magnitude of $r < 22.5$ (Fukugita et al. 1996; Gunn et al. 1998; Lupton et al. 1999; Hogg et al. 2001; Smith et al. 2002). Photometric errors are typically limited at bright magnitudes by systematic uncertainties at the $\leq 3\%$ level (Ivezić et al. 2004). Astrometric errors are typically smaller than 50 mas per coordinate (Pier et al. 2003). The spectroscopic survey targets both a “main” sample of galaxies with $r < 17.8$ and a median redshift of $z \sim 0.1$ (Strauss et al. 2002; Blanton et al. 2003a) and a “luminous red galaxy” sample (Eisenstein et al. 2001) that is approximately volume-limited out to $z = 0.38$. For more details of early and more recent SDSS data releases, see Stoughton et al. (2002) and Adelman-McCarthy et al. (2006).

Two catalogs are extracted from the SDSS data for use in this paper. The first is a photometric galaxy catalog, used as input to the cluster finder. This catalog is generated using the same criteria applied in Scranton et al. (2002) to create the input catalog for measurements of galaxy clustering, including use of an optimized star-galaxy separator. The input catalog includes galaxy positions and `cmode1` magnitudes in each of the SDSS bands. These magnitudes are constructed from a weighted combination of Petrosian and model magnitudes, with the weights determined by the quality of individual fits of de Vaucouleurs and exponential profiles to the surface brightness profile of each galaxy. All magnitudes are corrected for Galactic extinction using the extinction maps of Schlegel et al. (1998). The resulting input catalog contains 2.3×10^7 galaxies. The distribution of these galaxies in $g-r$ color and i magnitude is shown in Figure 1.

The galaxies in our imaging catalogs include a wide range of objects with various colors, magnitudes, and morphologies. Only a subset of these have colors and magnitudes consistent with E/S0 ridgeline galaxies in the target redshift range. Imposing broad color cuts to exclude galaxies too red, blue, or faint to be bright cluster members substantially reduces the size of the input catalog with no loss in cluster-finding efficiency. The colors and magnitudes appropriate for E/S0 galaxies in the redshift range $0.1 < z < 0.3$ are extracted using the color-magnitude-redshift model described in Koester et al. (2007). We focus on this redshift range for reasons explained in more detail in § 4. These model parameters are turned into color-magnitude cuts in the following way: at an assumed redshift, we note the $g-r$ and $r-i$ colors and the $0.4L_*$ i -band magnitude prescribed by the

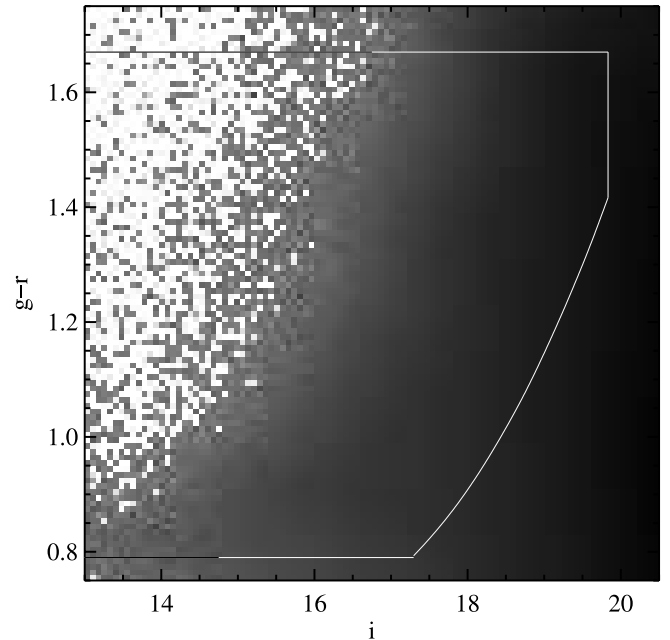


FIG. 1.—Distribution of galaxies in $g-r$ color and i magnitude in the input galaxy catalog. Overlaid on the figure are the cuts used to extract a sample of potential E/S0 ridgeline galaxies in the search redshift region. The gray scale is linear in the number of galaxies at each color and magnitude.

model. We include in the search catalog all candidate galaxies whose colors $(g-r)_{\text{cand}}$ and $(r-i)_{\text{cand}}$ pass the following criteria anywhere in the search redshift range:

$$\begin{aligned} (g-r)z_{\text{model}} - e_1 &< (g-r)_{\text{cand}} < (g-r)z_{\text{model}} + e_1, \\ (r-i)z_{\text{model}} - e_2 &< (r-i)_{\text{cand}} < (r-i)z_{\text{model}} + e_2, \\ i_{\text{cand}} &< 0.4L_*z_{\text{model}}, \\ e_1 &= \sqrt{\sigma_{\text{err}}^2 + 0.15^2}, \quad e_2 = \sqrt{\sigma_{\text{err}}^2 + 0.18^2}. \end{aligned} \quad (1)$$

Here the σ_{err}^2 are the color errors of the objects, measured using the methods described in Scranton et al. (2005). The factors of 0.15 and 0.18 each correspond to 3 times the intrinsic width of the E/S0 ridgeline in $g-r$ and $r-i$, respectively. At the same redshift, a magnitude constraint selects objects whose i -band magnitudes indicate that they are $0.4L_*$ or brighter at the current redshift. Running these selection criteria for the chosen redshift range reduces the total number of input galaxies to 4,689,495, or about one-fifth of the input galaxy catalog (see Fig. 1 for the range of these cuts in $g-r$ vs. i , excluding color errors). These galaxies are all treated as potential centers of groups or clusters by the maxBCG cluster finder described below. We note that this will bias the cluster search against completely blue, low-redshift clusters and groups (§ 3). Most of these input galaxies (a total of 1,389,858) are ultimately absorbed as centers or members of maxBCG groups and clusters.

The second input catalog is drawn from the SDSS spectroscopic data, including all available spectroscopic targets identified as galaxies with confidently measured redshifts. The catalog used here contains 567,486 galaxies with typical radial velocity errors of about $\pm 30 \text{ km s}^{-1}$. This spectroscopic catalog is not used in the detection of clusters, but provides vital data for testing the fidelity of photometric redshift estimation. Spectroscopic data also allow us to determine the relationship between measured cluster richness and velocity dispersion. The $g-r$ color as

¹⁷ See <http://www.sdss.org>.

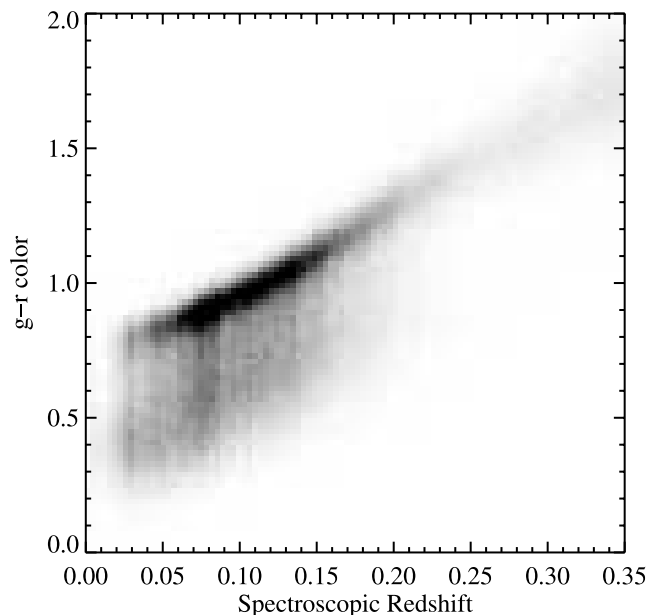


Fig. 2.—Distribution of galaxies in the input spectroscopic catalog in $g-r$ color and redshift. The close correspondence between redshift and $g-r$ color for the E/S0 galaxies is apparent in the strong sequence along the red edge of the distribution. This forms the basis for the excellent photometric redshifts obtained for maxBCG clusters. The gray scale is linear in the number of galaxies at each color and redshift.

a function of redshift for this spectroscopic catalog is shown in Figure 2.

3. DESCRIPTION OF THE CLUSTER DETECTION ALGORITHM

Galaxy cluster detection within the SDSS has been presented in several previous works. Initial efforts at photometric selection of clusters were presented in Goto et al. (2002) and Bahcall et al. (2003). The latter compared the results of two different selection methods, a hybrid matched-filter method (Kim et al. 2002) and an earlier version of the maxBCG method presented here (Annis et al. 1999). A photometrically selected catalog of compact groups has also been assembled (Lee et al. 2004). In addition to these photometrically selected catalogs, several group and cluster catalogs have been assembled from spectroscopic data, such as those of Miller et al. (2005), Berlind et al. (2006), and Weinmann et al. (2006). These spectroscopic catalogs are quite robust, but limited in volume by the flux-limited nature of the SDSS spectroscopy. Previously detected clusters have also been studied using SDSS optical data. Popesso and collaborators have published a series of papers relating X-ray and optical properties of Abell clusters (Popesso et al. 2004, 2005, 2007). Studies have also been conducted of the galaxy populations (Hansen et al. 2005) and lensing masses (Sheldon et al. 2001) of an earlier generation of maxBCG objects. Luminosity functions for photometrically selected clusters were considered in Goto et al. (2003).

The maxBCG galaxy cluster selection algorithm applied to the input galaxy catalog is described in more detail in a companion paper (Koester et al. 2007). Briefly, the algorithm exploits two well-known features of rich galaxy clusters. First, the bright end of the cluster luminosity function is dominated by galaxies occupying a narrow region of color-magnitude space (the E/S0 ridgeline). These galaxies are sometimes referred to as red-sequence galaxies. Second, clusters contain a brightest cluster galaxy (BCG) that is located near the center of the galaxy dis-

tribution. This BCG is often distinctly brighter than other cluster members (Hansen et al. 2005; Loh & Strauss 2006), and is nearly at rest relative to the cluster's center of mass (Oegerle & Hill 2001). While these criteria are not universal for all groups and clusters, they become increasingly common among the optically richest clusters.

For every galaxy in the input catalog, the algorithm measures two independent likelihoods. The first is the likelihood that a galaxy is spatially located in an overdensity of E/S0 ridgeline galaxies with similar $g-r$ and $r-i$ colors, and the second is the likelihood that it has the color and magnitude properties of a typical BCG. Both likelihoods are evaluated for every input SDSS galaxy at a grid of redshifts. The redshift that maximizes the product of these likelihoods is then found for each galaxy. This corresponding maximum likelihood redshift provides a first estimate of the cluster redshift and is used in the following steps.

Next a list of member galaxies for each potential center is assembled. The number of galaxies projected within $1 h^{-1}$ Mpc of this potential center that are brighter than $0.4L_*$, fainter than the potential center, and have colors matching its E/S0 ridgeline is counted. This number, which we call N_{gal} , provides a first estimate of the cluster richness. This initial richness estimate is then used to estimate the cluster size R_{200} , defined here as the radius within which the density of galaxies with $-24 \leq M_r \leq -16$ is 200 times the mean density of such galaxies. The value of R_{200} is determined using the relation between N_{gal} and R_{200} derived in Hansen et al. (2005). This richness-size relation was determined for a somewhat different, earlier version of the maxBCG cluster finder. While the normalization of the richness-size relation may differ slightly in this new catalog, we expect the overall scaling to remain the same.

Once the list of cluster center likelihoods is measured and lists of corresponding potential members are assembled, galaxy clusters are assembled, beginning with the richest and progressing down through a percolation procedure. The percolation begins with the highest likelihood potential center. This galaxy is declared a cluster BCG and assigned its maximum likelihood redshift. All galaxies within a projected separation R_{200} of the BCG, within $\pm 2\sigma$ of the E/S0 ridgeline in the space of $g-r$ color and i magnitude, and brighter than $0.4L_*$ in the i band are labeled as members of this cluster. Subsequent galaxies can be considered BCGs only if they are not already members of a higher likelihood center. We further eliminate any lower likelihood centers that fall within R_{200} and have a maximum likelihood redshift within ± 0.02 of a higher likelihood BCG. This latter step prevents the double counting that might occur if a real member of a rich cluster has slightly anomalous colors that prevent it from being selected as a cluster member. Note that this local suppression has important implications for the measurement of the spatial clustering of clusters. The observed clustering will be strongly affected by the cluster-finding algorithm on scales of less than a few Mpc. This process continues until all viable centers are either declared centers or have been otherwise absorbed as cluster members. Each object detected has a center defined as the BCG location, an estimated redshift, and a richness given by the number of E/S0 ridgeline members brighter than $0.4L_*$ and within R_{200} of the cluster center ($N_{\text{gal}}^{R_{200}}$).

Once the basic cluster-finding step is complete, we refine the measurement of cluster properties in several ways. First, redshift estimates are adjusted. A small empirical correction (≈ 0.004) is applied to the photometric redshifts, based on the comparison of spectroscopic to photometric redshifts described below. Information about the spectroscopic redshift of the cluster, where it

is available, is appended. The luminosity of the BCG and the summed luminosity of the BCG and all cluster members in the r and i bands is added. Luminosities are reported in units of $10^{10} L_{\odot}$, k -corrected to $z = 0.25$, the median redshift of the sample. The k -corrections are computed using the luminous red galaxy (LRG) template in version 4.1.4 of `kcorrect` (Blanton et al. 2003b), assuming the maxBCG photometric redshift. These k -corrections do not include an evolution correction. The final cluster catalog contains an array of measured properties, including location, photometric redshift, spectroscopic redshift (where available), and several richness and mass estimators, including N_{gal} , N_{gal}^{R200} , L_r^{BCG} , L_i^{BCG} , L_r^{memb} , and L_i^{memb} . Once the cluster catalog has been constructed, many more refined measures of cluster properties, including the overall richness, shape, concentration, and galaxy content can be made.

In concluding this description, it is worth noting that color cuts and the matched filter employed in maxBCG restrict detections of completely blue groups and clusters, especially those found at low redshifts (Goto et al. 2002). Furthermore, it assigns lower likelihoods to objects with less well defined ridgelines, unusual BCGs, or BCGs off-center from the cluster galaxy distribution. Although maxBCG may not miss such objects, they are of course penalized for their deviation from the model. More generally, since a perfect detection algorithm does not exist, understanding the selection function of any algorithm requires comparison to clusters detected by alternative approaches. In § 7, X-ray-selected clusters are compared to the maxBCG catalog, and simulations are used in § 5 and also in Koester et al. (2007) to address the robustness of the detection algorithm.

4. OVERALL PROPERTIES OF THE DERIVED CATALOG

The algorithm described above produces a catalog of all groups and clusters from $z = 0.05$ to 0.35 that contain bright red galaxies, a total of 2.18×10^6 objects. The resulting list spans a very broad mass range, from isolated elliptical galaxies and small groups through rich clusters. We focus here on only the more substantial clusters: those containing at least 10 E/S0 ridgeline galaxies brighter than $0.4L_*$ within a scaled aperture R_{200} . We focus on a restricted redshift range as well. SDSS photometric data are particularly well suited for the measurement of clusters at moderate redshifts. In the redshift range from 0.1 to 0.3, the relation between redshift and $g - r$ color is particularly simple, reflecting the gradual shift of the 4000 Å break from the blue to the red edge of the SDSS g filter (see Fig. 2). At the lowest redshifts (below $z = 0.1$), the approximately constant photometric redshift uncertainties of $\sigma_z \approx 0.01$ imply substantial fractional uncertainties in distance, causing correspondingly large uncertainties in derived parameters. Beyond $z = 0.1$, these uncertainties in distance fall below 10% and decrease with increasing distance. In addition, clusters present at these low redshifts can be more reliably selected using spectroscopic clustering algorithms (Miller et al. 2005). At redshifts beyond 0.3, the 4000 Å break begins to cross into the r filter, and for a range of redshift from $z = 0.32$ to $z = 0.37$, there is a significant increase in the photometric redshift uncertainty.

Focusing on the redshift range from 0.1 to 0.3 has another advantage. The cluster detection methods described here rely on identifying cluster members brighter than $0.4L_*$ at the cluster redshift. Our input galaxy catalog is essentially complete for these galaxies out to a redshift of 0.4, where they have i magnitudes of about 20.5. Cluster galaxies at redshifts less than 0.3 have photometric measurement errors in the essential g , r , and i bands that rarely exceed 10%. This combination allows our cluster selection across this redshift range to be remarkably uniform

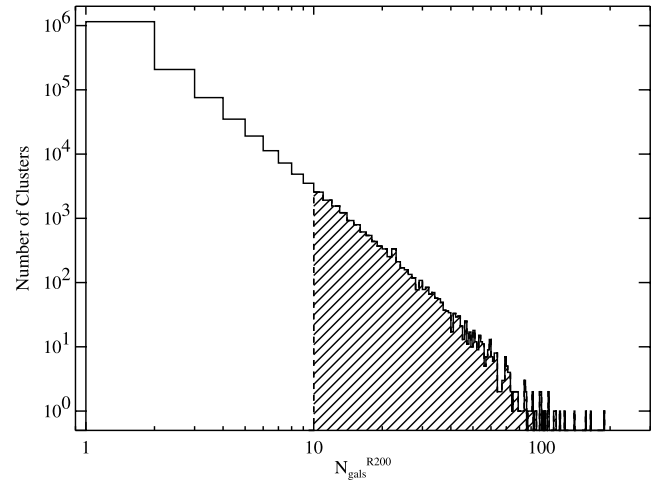


FIG. 3.—Differential number counts for clusters as a function of richness for the full maxBCG group and cluster catalog (solid line). The cluster catalog presented here includes all objects in the shaded region.

and allows us to assemble a catalog that is close to volume-limited. Residual uncertainty in the evolution of the cluster galaxy luminosity function from $z = 0.1$ to 0.3, which affects our definition of $0.4L_*$, is one of the principal remaining systematic errors at this point.

The catalog presented here includes 13,823 clusters with photometric redshifts $0.1 < z < 0.3$ and richnesses of $10 \leq N_{\text{gal}}^{R200} \leq 190$, 2891 of which have $N_{\text{gal}}^{R200} \geq 20$. The distribution of these clusters in scaled richness N_{gal}^{R200} is shown in Figure 3. As expected, smaller systems dominate the abundance function. The largest systems are often well-known Abell, Zwicky, or X-ray-selected clusters. The $N_{\text{gal}}^{R200} \geq 10$ objects contain 213,016 member galaxies, or a bit less than 1% of all input galaxies. Note that the input catalog is apparent magnitude-limited rather than volume-limited. Thus, these figures do not transparently reflect the probability that a galaxy will reside in a rich cluster.

Among these photometrically selected clusters, a total of 5413 (39%) have BCGs with measured spectroscopic redshifts. Only a small fraction, mostly at redshifts less than 0.15, have redshifts for more than five member galaxies. The lack of multiple redshifts per cluster at high redshifts is primarily due to the magnitude-limited nature of the SDSS spectroscopic survey. The photometric redshift distribution of these clusters is shown in Figure 4. Comparison to the expectation for a constant comoving density sample in the standard Λ CDM cosmology in this figure illustrates the approximately volume-limited nature of the catalog. A “pie diagram” for the clusters located in a 2.5° thick slice along the southern celestial equator is shown in Figure 5, and the volume-limited nature of the sample is again evident.

The full cluster catalog is available in machine-readable form as Table 1 in the online edition of this paper. A description of the information provided for each cluster in Table 1 is presented in Table 2.

5. TESTS OF CLUSTER SELECTION IN SIMULATED DATA

The quality of a cluster catalog is often explored in terms of its false-positive rate (purity) and its failure rate (completeness). Until recently, determining completeness and purity has only been possible through first-order techniques; for example, through random insertion of model clusters into real background data (Diaferio

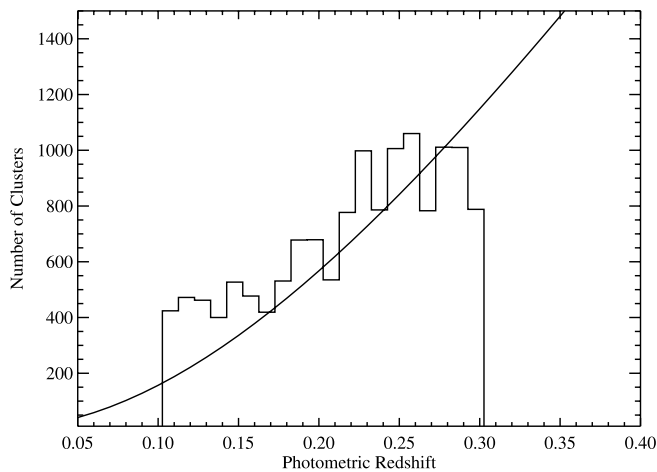


FIG. 4.—Number of clusters as a function of redshift for the maxBCG cluster catalog. The solid line shows the expectation for a volume-limited sample with a density of 2.3×10^{-5} clusters $h^3 \text{Mpc}^{-3}$ in a standard ΛCDM cosmology.

et al. 1999; Adami et al. 2000; Postman et al. 2002; Kim et al. 2002; Goto et al. 2002). Modern mock galaxy catalogs, in which the galaxy distribution is designed to represent the underlying dark matter distribution from N -body simulations, embed their galaxy clusters in their full environment of filaments and voids and provide realistic estimates of both the spatial and dynamical structure of the cluster galaxy population (White & Kochanek 2002; Kochanek et al. 2003; Eke et al. 2004; Miller et al. 2005; Yang et al. 2005; Gerke et al. 2005; R. Wechsler et al. 2007, in

preparation). These mock catalogs have enabled a deeper exploration of the purity and completeness of catalogs produced by a galaxy cluster finder. Since clusters of galaxies trace the underlying dark matter halo population in the universe, the mock galaxy catalogs can also help to reveal how well the objects that are found by the cluster finder relate to dark matter halos. In the end, it is the distribution of these halos in the real universe that we wish to uncover, and the extent to which this distribution is recovered from clusters in the mock catalogs is a strong indicator of the catalog's quality. This recovery rate also provides useful feedback for adjustments and corrections that need to be made to optimize cluster-finding algorithms.

To test the cluster finder described in this paper, we utilize the mock galaxy catalogs described by R. Wechsler et al. (2007, in preparation), which were largely designed for this purpose. The construction of these catalogs begins with an N -body realization of the large-scale structure in the nearby universe. Galaxies are then inserted into this simulation, adopting the locations and motions of dark matter particles, subject to a variety of empirical constraints. The first constraint simply determines the number and nature of the galaxies to be inserted. In this case, the number of galaxies and their distribution in r luminosity is taken from the measured SDSS galaxy luminosity function (Blanton et al. 2001, 2003c). Galaxies down to $0.4L_*$ in r are then assigned to particular dark matter particles according to a scheme that matches the observed luminosity-dependent two-point clustering of SDSS galaxies as measured by Zehavi et al. (2004). The assignment does not explicitly use any knowledge of the locations of dark matter halos, but produces a halo occupation that is in good

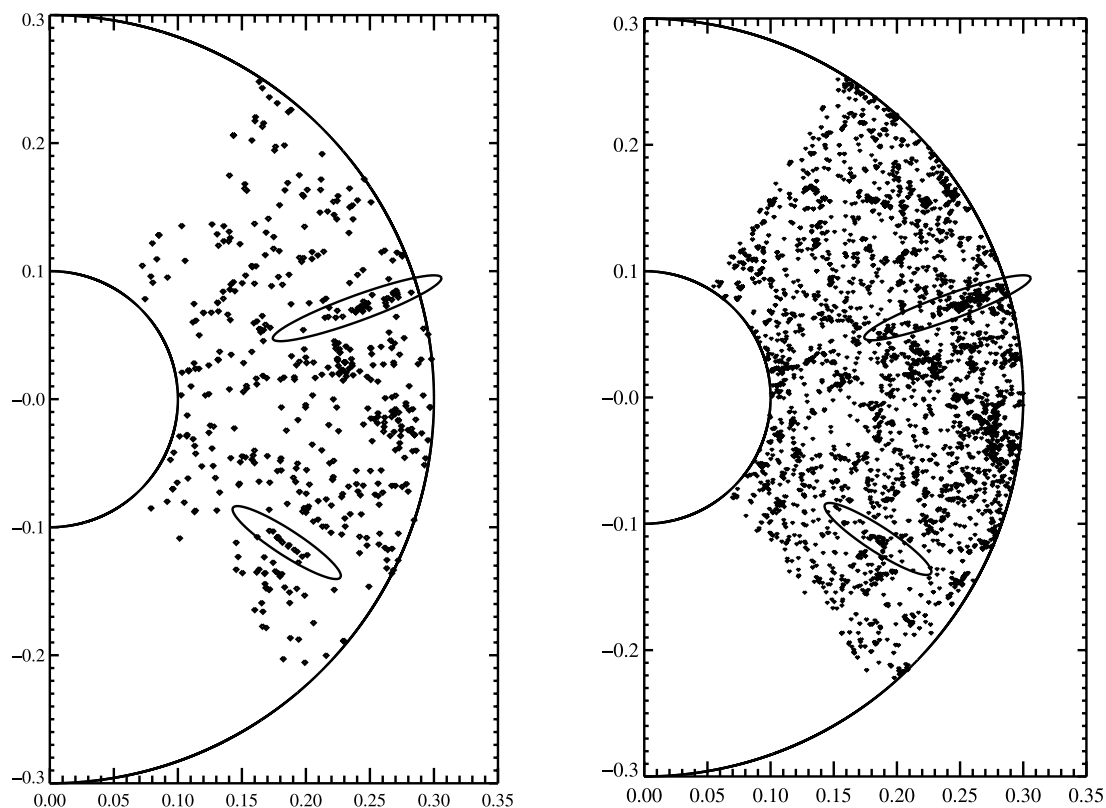


FIG. 5.—SDSS data in the region of the SDSS southern equatorial stripe, with $-1.25^\circ \leq \text{decl.} \leq 1.25^\circ$ and with $\text{R.A.} < 100^\circ$ or $\text{R.A.} > 300^\circ$. The left panel shows the locations in right ascension and photometric redshift of the maxBCG cluster centers. The right panel shows the right ascension and spectroscopic redshift of SDSS luminous red galaxies (LRGs). This slice contains 492 clusters, about 3.5% of the total catalog. Circles drawn at $z = 0.1$ and 0.3 show the boundaries of the maxBCG catalog redshift range. The approximately volume-limited nature of the cluster catalog is apparent. There are several features that look like “fingers of God.” These are partly generated by the ± 0.01 uncertainties in the photometric redshifts. Their appearance is exaggerated when they enhance real features in the galaxy distribution, as in the two examples outlined by the ellipses added to both panels.

TABLE 1
CLUSTER CATALOG

R.A. (deg)	Decl. (deg)	z	BCGspecz	L_r^{BCG} ($10^{10} L_\odot$)	L_i^{BCG} ($10^{10} L_\odot$)	L_r^{memb} ($10^{10} L_\odot$)	L_i^{memb} ($10^{10} L_\odot$)	N_{gal}	N_{gal}^{R200}
239.58334.....	27.233419	0.102650	0.0907943	8.67289	10.7264	274.706	343.396	95	188
140.10742.....	30.494063	0.291650	-1.00000	19.2961	23.9976	245.728	300.698	69	126
198.77182.....	51.817380	0.286250	-1.00000	16.1223	19.9630	166.088	201.767	62	87
126.37104.....	47.133478	0.135050	0.128977	19.0209	24.4289	152.746	192.101	68	99
203.16008.....	50.559919	0.283550	-1.00000	11.5153	14.6633	229.600	277.906	67	114
354.41554.....	0.27138263	0.286250	0.277195	11.6860	14.3761	145.190	177.315	59	88
213.78496.....	-0.49324716	0.135050	0.138936	10.6901	13.8037	152.922	192.425	55	115
189.24684.....	63.186584	0.294350	-1.00000	26.5106	32.3937	179.030	222.360	57	89
216.48612.....	37.816455	0.167450	0.170008	12.2946	15.4804	130.867	163.989	58	98
187.70363.....	10.546381	0.167450	0.170512	14.8285	18.5403	115.761	142.613	51	70

NOTE.—Table 1 is presented in its entirety in the electronic edition of the *Astrophysical Journal*. A portion is shown here for guidance regarding its form and content.

agreement with methods that constrain it directly. It has the advantage that it provides a way to naturally include the dim background population necessary for comparison to photometric data with less resolution than would be required for a method that populated dark matter halos directly.

Once a location and an r -band luminosity are chosen for each galaxy, appropriate galaxy colors are assigned by selecting a real SDSS galaxy with the same luminosity and measured local density. This process ensures that the simulated galaxy colors and their relation to their local galaxy density accurately reflect those found in the data. This is essential if the mock catalogs are to be useful for testing an E/S0 ridgeline-based cluster finder. If the dark matter particle on which a galaxy is placed is within R_{200} of the center of a dark matter halo, the galaxy is considered a member galaxy of that halo.

The most serious flaw of this process is that it includes no explicit mechanism for creating the brightest cluster galaxies, which we know often rest in the center of a dark matter halo. In a naive effort to fix this, the brightest galaxy in each halo is, as a final step, moved to the center of the halo and assigned the mean halo redshift. It may be possible to solve this problem by explicitly associating galaxies with resolved dark matter substructures within halos, as has been done in recent high-resolution simulations (Nagai & Kravtsov 2005; Conroy et al. 2006), although it is difficult to do this in simulations with the volume necessary for photometric cluster studies.

Straightforward techniques are employed to quantify the purity and completeness. Clusters in the mock catalog are identi-

fied using the same code that is run on the data. To understand the false-positive rate (purity), the halo membership of galaxies identified as red-sequence cluster members is used to determine the cluster-halo correspondence. In this comparison, it is important to recall that galaxies identified as cluster members by the cluster finder *must* be red-sequence members. As such, they are only a subset of the actual halo members, some of which fall outside the E/S0 ridgeline. This fact affects the matching process, guaranteeing that no perfect one-to-one match of cluster and halo members will be found.

To measure purity, we look to see whether each identified cluster corresponds to any real dark matter halo. For each cluster, the halo containing the maximum fraction of a cluster's members is located. If this fraction is less than some threshold, f_c , there is no halo to which this cluster clearly corresponds, and the cluster is called a false positive. The exact choice of f_c is arbitrary and may be driven by the science questions that the catalog is designed to answer. The purity results, presented in Figure 6, are based on two possible choices, $f_c = 0.3$ and 0.5 . At $f_c = 0.3$, the catalog is $>90\%$ pure for $N_{\text{gal}}^{R200} > 10$ and 95% – 100% pure for $N_{\text{gal}}^{R200} > 20$. Tightening f_c to 0.5 reveals a degraded purity, which is approximately constant at 90% across the full richness range.

To evaluate the completeness, the matching process is reversed. For each halo, we identify the cluster that contains the largest fraction of its members. If this fraction is less than some threshold, f_h , the halo has been missed. Because the member galaxies in the mock halos are red *and* blue (and the cluster finder only identifies the red ones as cluster members), this is a rather strict test. Figure 7 shows the results of these schemes, in which $f_h = 0.3$ and 0.5 , respectively. The sample is $>90\%$ complete above $\approx 2 \times 10^{14} h^{-1} M_\odot$ in the $f_h = 0.3$ test and is 95% – 100% complete for objects more massive than $3 \times 10^{14} h^{-1} M_\odot$. Notably, both choices of f_h yield nearly 100% completeness at values greater than $8 \times 10^{14} h^{-1} M_\odot$, with the completeness degrading more rapidly in the larger f_h fraction. In this more stringent test, 90% completeness is not reached until $\approx 3 \times 10^{14} h^{-1} M_\odot$.

Insight into the cluster-halo correspondence can be gained from considering the meaning of f_c and f_h (Gerke et al. 2005). In measurements of purity, we seek a halo that contains a substantial fraction ($f_c \geq 0.3$) of the cluster's members. When this fraction is small, the cluster finder has merged one or more additional halos with this best match, a failure we might describe as overmerging. The cluster members beyond those in the matched halo are actually members of other, nearby halos. If a cluster finder were tuned to maximize purity alone, it would endeavor to include as many members of the matching halo as possible,

TABLE 2
INFORMATION AVAILABLE IN THE ONLINE CLUSTER CATALOG

Column Name	Data Type	Unit	Description
R.A.	Floating point	Degree	BCG right ascension (J2000.0)
Decl.	Floating point	Degree	BCG declination (J2000.0)
z	Floating point	...	Photometric redshift
BCGspecz.....	Floating point	...	Spectroscopic BCG redshift
L_r^{BCG}	Floating point	$10^{10} L_\odot$	BCG r -band luminosity
L_i^{BCG}	Floating point	$10^{10} L_\odot$	BCG i -band luminosity
L_r^{memb}	Floating point	$10^{10} L_\odot$	Total r -band luminosity
L_i^{memb}	Floating point	$10^{10} L_\odot$	Total i -band luminosity
N_{gal}	Integer	...	Detection richness
N_{gal}^{R200}	Integer	...	Scaled richness

NOTE.—This table describes the information provided for each cluster in the online catalog.

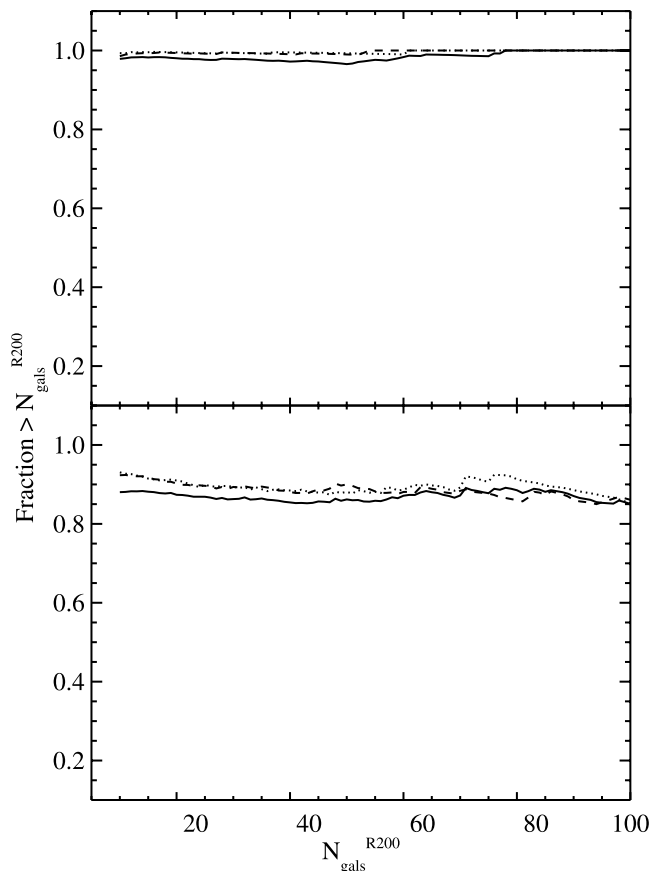


FIG. 6.—Basic results of purity tests based on mock catalog studies. In each plot the solid line represents the full mock catalog, the dotted line represents halos of $0.1 < z < 0.2$, and the dashed line represents halos at $0.2 < z < 0.3$. The top panel is a purity plot for cluster matching fractions $f_c = 0.3$, and the bottom is the same, but for $f_c = 0.5$. In each case a cluster is called “real” if a fraction of at least f_c of its E/S0 ridgeline members is contained within R_{200} of a single dark matter halo.

and in the process would be more likely to merge galaxies from neighboring halos. Increasing the value of f_c required for matching ensures that a halo becomes more dominant in the cluster, and that the cluster is not a conglomeration of many smaller halos, until $f_c \simeq 1$. At this point it is possible that the *cluster* is only part of a much larger *halo*, and there may in fact be several clusters for which this halo is a best match. Similar flexibility in the choice and meaning of matching parameters affects completeness measures. In these, a matching cluster must contain a substantial fraction ($f_h \geq 0.3$) of the halo’s total member list. The other halo galaxies may be distributed among other clusters, in which case the cluster finder has fragmented the halo into several objects. Letting this fraction approach 1 reduces the incidence of fragmentation, but is likely to cause overmerging. A more extensive discussion of these issues is presented in the companion algorithm paper (Koester et al. 2007).

Above $N_{\text{gal}}^{R200} = 10$ and $M = 2 \times 10^{14} h^{-1} M_{\odot}$, the catalog presented here is $\simeq 90\%$ pure and complete. At masses below $\simeq 1 \times 10^{14}$, the decline in completeness is not surprising. The mean number of real halo members within a three-dimensional R_{200} from mock catalogs at masses near $\simeq 1 \times 10^{14}$ is about 8, with a tail to higher richness. When the cluster finder is run on these halos, it typically increases this true member number by $\approx 20\%$ due to projection, pushing most $10^{14} M_{\odot}$ halos over the detection threshold. Note that the precise values of purity and completeness are sensitive both to how the matching is done and

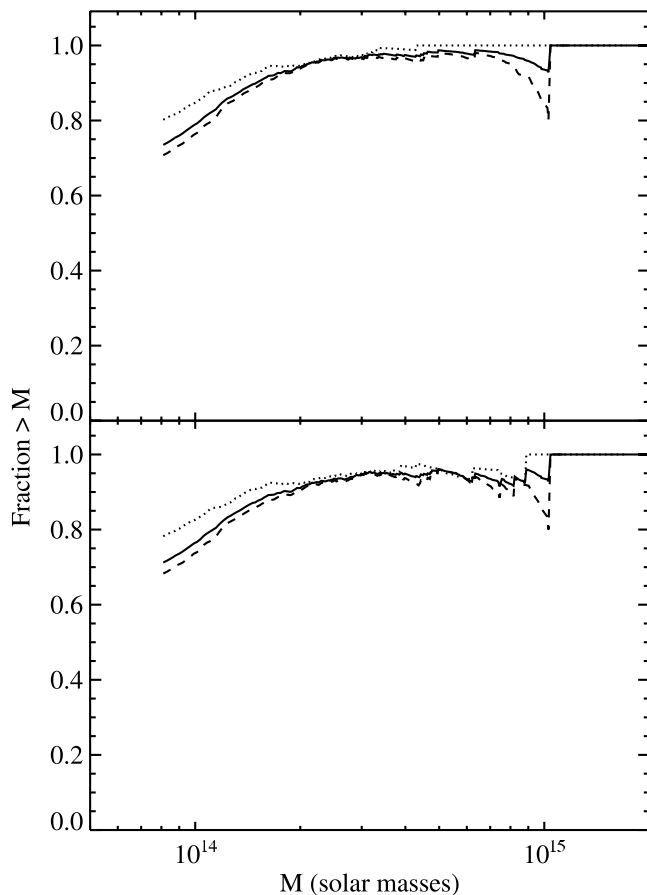


FIG. 7.—Basic results of completeness tests based on mock catalogs. In each plot the solid line represents the full mock catalog, the dotted line represents halos of $0.1 < z < 0.2$, and the dashed line represents halos at $0.2 < z < 0.3$. The top panel is a completeness plot for a halo matching fraction $f_h = 0.3$, and the bottom is the same, but for $f_h = 0.5$. In each case, a dark matter halo is considered “found” if a fraction f_h of its red-sequence members is found in a single identified cluster.

to how the limits of the catalog are defined. When completeness is defined without the explicit threshold and an exclusive matching scheme between halos and clusters is used, the catalog is $\simeq 95\%$ complete above $M = 1 \times 10^{14} h^{-1} M_{\odot}$ (E. Rozo et al. 2007, in preparation).

Halos at lower masses include a wide variety of galaxy groups. Some include clear red sequences and are easily detected. Others have larger blue fractions and are more difficult to identify by red-sequence techniques. There are indications from the radial profiles of these objects that low- N_{gal}^{R200} objects come from underdense regions of the universe (Hansen et al. 2005) and may be dominated by fossil groups. The mix of objects found by red-sequence methods at low values of N_{gal}^{R200} makes this an interesting area of future study, as do the objects missed by these means.

An important reason to assemble a cluster catalog is to determine the distribution of dark matter halos at different masses. Ideally, there would be a one-to-one correspondence between halos in the real universe and observed clusters of galaxies, with the correspondence encoded in a richness-mass relation such as $M(N_{\text{gal}}^{R200})$. Calibrating this relation would then allow extraction of the true halo distribution from the cluster abundance function. In fact, any cluster finder inevitably fragments some halos into sets of smaller clusters and merges some smaller halos into larger clusters. This complicates cluster-to-halo matching and illustrates the important role that studies of realistic mock catalogs must play: without such studies, reliable cosmological constraints from

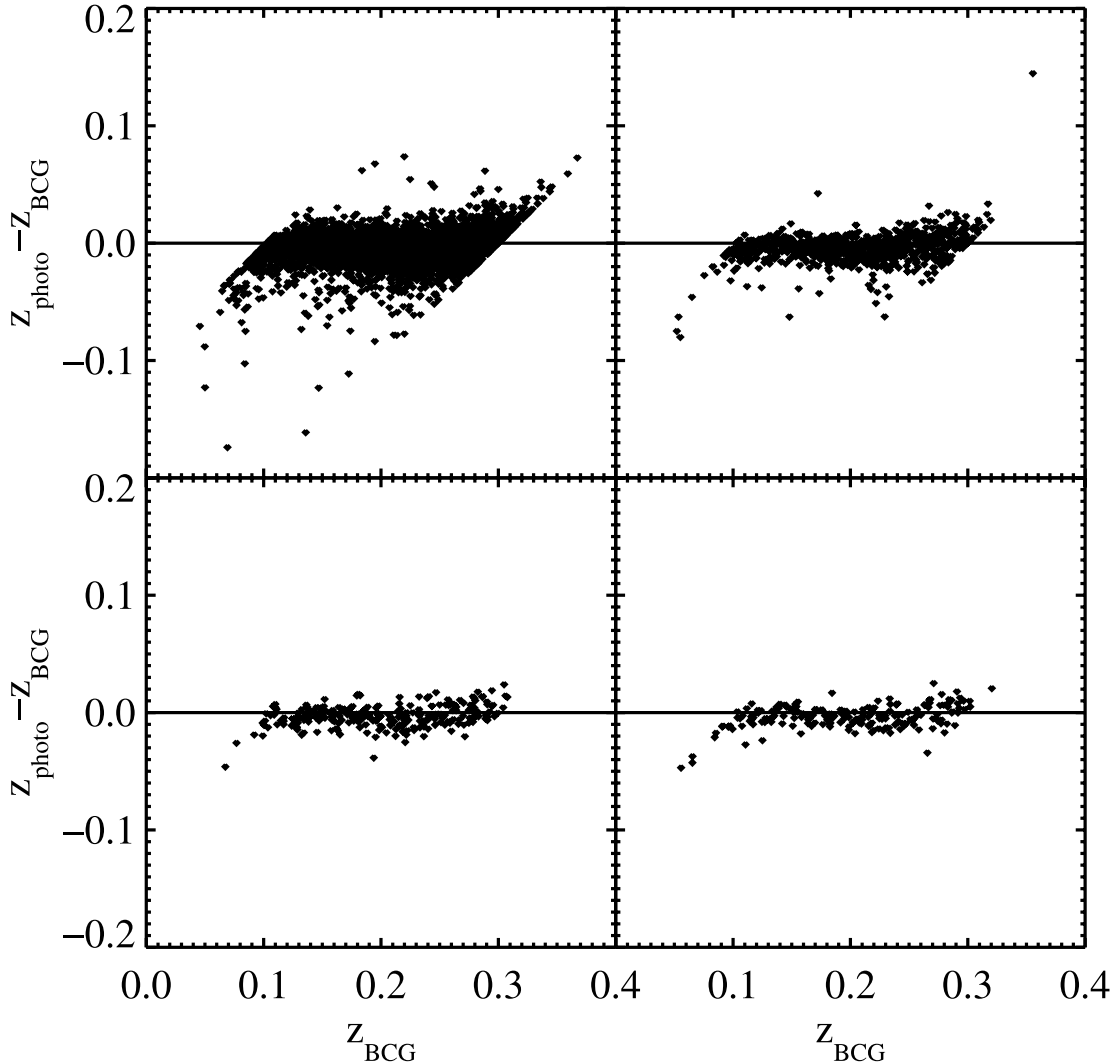


FIG. 8.—Comparison of BCG spectroscopic redshift, z_{BCG} , to cluster photometric redshift, z_{photo} , for 5413 objects, divided into several different richness N_{gal}^{R200} ranges: $10 < N_{\text{gal}}^{R200} < 20$ (top left), $20 < N_{\text{gal}}^{R200} < 30$ (top right), $30 < N_{\text{gal}}^{R200} < 40$ (bottom left), and $40 < N_{\text{gal}}^{R200}$ (bottom right). Note the one object in the top right panel that has a spectroscopic redshift ≈ 0.35 and a photometric redshift ≈ 0.21 . This is the BCG of a cluster actually at $z = 0.21$. The spectrum of the central galaxy (SDSS J075137.2+325447.4) shows a typical red galaxy spectrum with $z = 0.21$ overlaid with strong emission lines from a (possibly lensed) background object at $z = 0.355$. In this case, the photometric redshift in the cluster catalog is correct.

optically selected catalogs are likely to be impossible. A much more complete analysis of fragmentation, merging, and the richness-mass relations required to generate final estimates of the halo mass function will be presented in E. Rozo et al. (2007, in preparation).

6. TESTS OF DERIVED CLUSTER PARAMETERS

In this section we describe some tests of the quality of derived cluster properties, based in this case primarily on references to the SDSS spectroscopic data. The large spectroscopic catalog provided by the SDSS (Fig. 2) enables studies of the photometric redshift quality, the effects of projection on the cluster finder, and of the richness-velocity dispersion relation.

6.1. Tests of Photometric Redshifts

Determining the physical properties of observed clusters requires accurate photometric redshifts. To assess the quality of z_{photo} for a particular cluster, its true redshift z_{spec} must be known from spectroscopy. For this test of photometric redshifts, we use the clusters with BCG spectroscopic redshifts. Since the BCGs are bright, they are more likely to be targeted for spectroscopy than an average cluster galaxy. In addition, the SDSS LRG target

selection (Eisenstein et al. 2001) explicitly constructs a volume-limited sample of the brightest red galaxies, many of which are BCGs. The combination provides good statistics for the evaluation of z_{photo} . Figure 8 compares all available BCG spectroscopic redshifts (z_{BCG}) to cluster photometric redshifts (z_{photo}) for objects in four different N_{gal}^{R200} richness ranges. Figure 9 shows the comparison of z_{photo} to z_{spec} in a series of different redshift ranges. The dispersion in $z_{\text{spec}} - z_{\text{photo}}$ is $\simeq 0.01$, essentially independent of redshift. There is a small bias (≈ 0.004), in the sense that estimated redshifts are slightly higher than measured ones at all redshifts. We correct for this small bias in the photometric redshift estimates provided in the final catalog. The errors throughout are well represented by a Gaussian. Photometric redshifts for the richest half of the clusters are slightly better, with a typical dispersion in $z_{\text{spec}} - z_{\text{photo}}$ of about 0.008. This photometric redshift accuracy allows clusters separated by more than about $50 h^{-1}$ Mpc along the line of sight to be correctly identified.

6.2. Tests of Projection

The projection of foreground and background galaxies onto the observed cluster population is a concern for all optical cluster

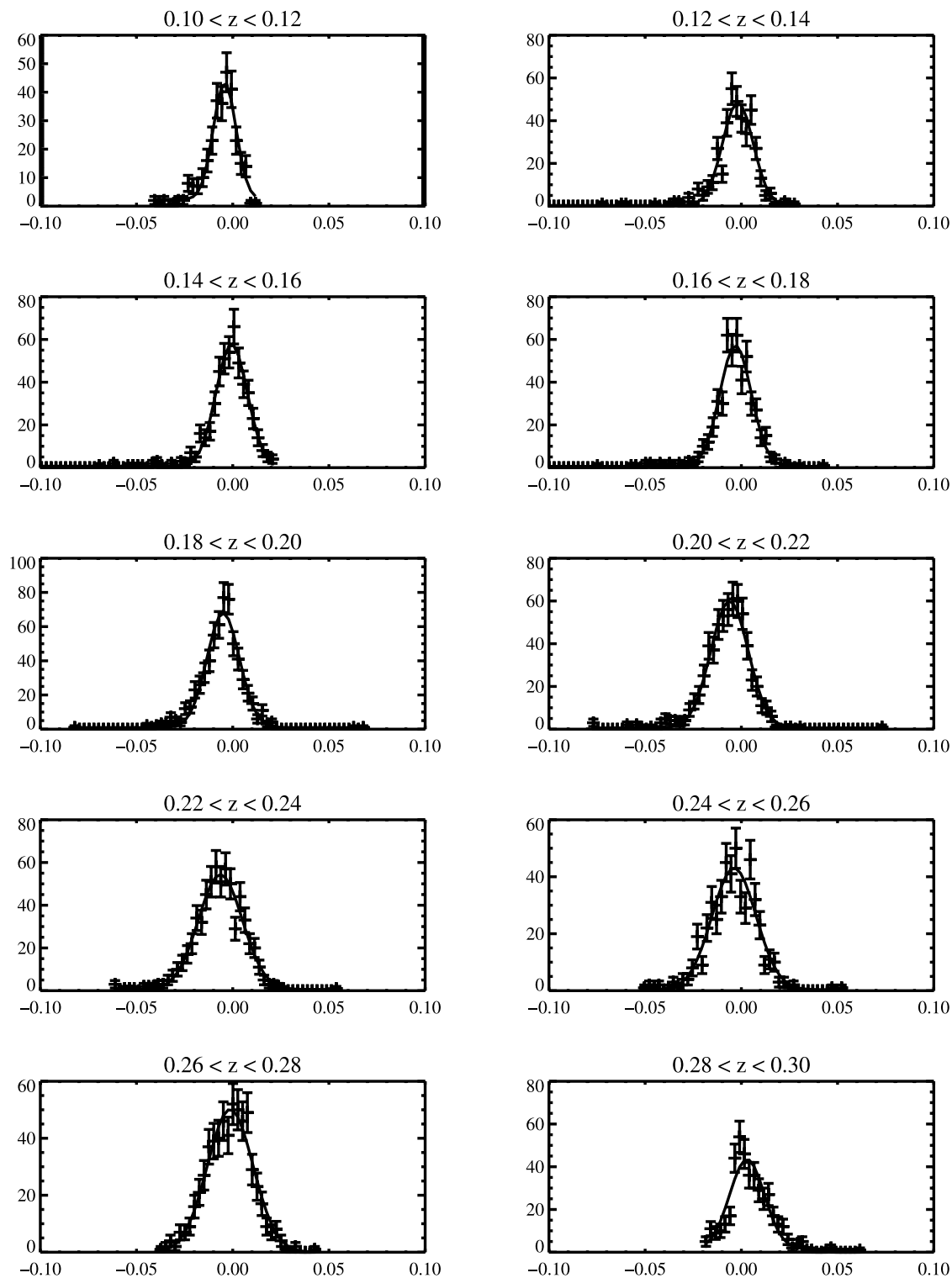


FIG. 9.—Difference between measured BCG spectroscopic redshift and cluster estimated photometric redshift for a total of 5413 clusters with $N_{\text{gal}}^{R200} \geq 10$ for which spectroscopic BCG redshifts exist. Each panel shows the difference between spectroscopic and photometric redshift for a small bin of spectroscopic redshifts. Gaussian fits to each distribution are overlaid. The fit dispersions range from $\sigma_z = 0.006$ to 0.011 . The small ($\Delta_z \approx 0.004$) average bias seen here is subtracted in the final catalog.

selection algorithms. There are two levels at which projection occurs. First, there is large-scale projection, in which galaxies that are more than a few tens of Mpc from a cluster and randomly projected on it are mistaken for cluster members. This large-scale projection can easily be tested for by using spectroscopic redshifts and is an effect one might aspire to completely avoid. Second, there is small-scale projection, in which galaxies near the

cluster, along infalling filaments for example, are thought to lie within the cluster. Spectroscopic information about cluster membership on these small scales is limited by redshift-space distortions. This kind of projection is best constrained using realistic simulations.

By relying on the tight clustering of E/S0 galaxies in color-magnitude space, the maxBCG cluster finder limits the influence

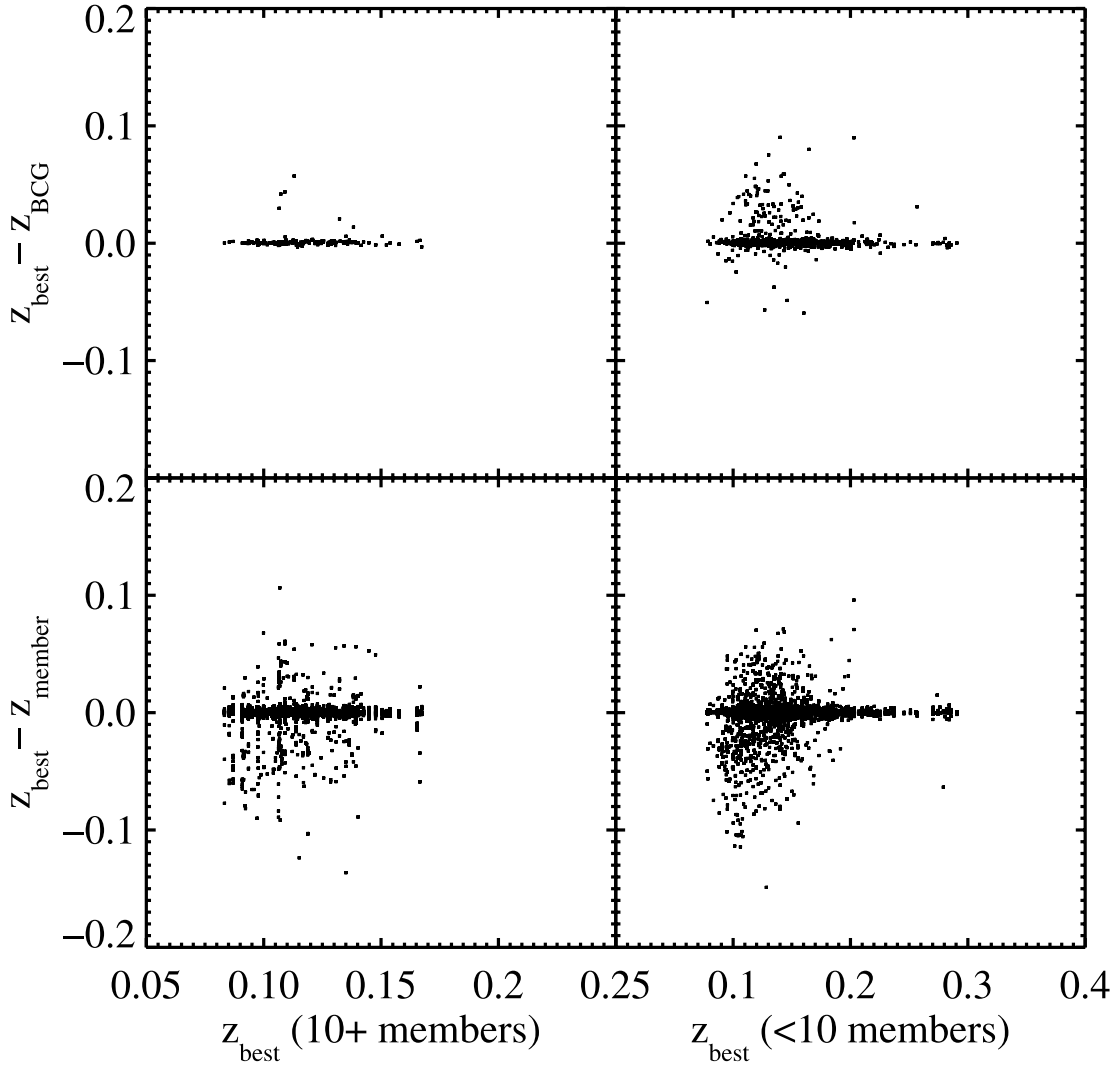


FIG. 10.—Residual plots of BCG (z_{BCG}) and member (z_{memb}) projection in maxBCG clusters. The top left panel compares BCG redshifts to median member redshifts, z_{best} , in the 143 cases where at least 10 member galaxies are found within $\pm 2000 \text{ km s}^{-1}$ of the median. Only 8 out of 143 (5.6%) of these BCGs are found with velocities differing from the median by $> 2000 \text{ km s}^{-1}$. The top right panel shows the same comparison for the remaining 2914 clusters, for which the apparent BCG projection fraction is 117 out of 910 (13%) (excluding those where $z_{\text{best}} = z_{\text{BCG}}$). The bottom panels show similar comparisons for all member galaxies with spectroscopic redshifts. The bottom left panel compares z_{memb} to z_{best} for the 143 well-measured clusters, while the bottom right panel does the same for the remaining clusters. A fraction of 427 out of 2701 (16%) of members are seen to be projected in the well-measured cases, and 829 out of 5068 (16%) in the remainder.

of projection, but it remains important to quantify this source of contamination. Direct study of projection also provides insight into the limitations of red-sequence cluster finding and may suggest algorithmic improvements.

To study the incidence of projection in this catalog, we take advantage of the large number of spectroscopic redshifts available for both BCGs and member galaxies identified by the algorithm. We begin by identifying the 3057 clusters that have spectroscopic redshifts for both the BCG and at least one member galaxy. The first step is to define a “best” redshift for each of these clusters, z_{best} . When a cluster has at least three member galaxy spectra, we take the median redshift of all the cluster member galaxies as z_{best} . If there are fewer than three member redshifts, we define z_{best} to be the BCG redshift. To test for projection, we then compare individual BCG and member spectroscopic redshifts to these estimates of z_{best} . Our determination of z_{best} is far from perfect; often it is measured from just a few member galaxy redshifts or from only the redshift of the BCG. Because of this, we further split the spectroscopic sample into the 143 clusters with at least 10 member galaxies located within $\pm 2000 \text{ km s}^{-1}$ of the median redshift

and the remaining 2914 clusters with fewer. Comparing the projection results obtained with these two samples provides a check on the influence of uncertainty in the determination of z_{best} on our conclusions.

We first measure the incidence of BCG projection. Since we require the BCG to be the brightest galaxy in a cluster, one might worry that we would occasionally select as a BCG a bright foreground galaxy projected onto the E/S0 ridgeline of a more distant cluster. To test for projection, we compare z_{BCG} to z_{best} in the top panels of Figure 10. The top left panel shows the comparison for the 143 clusters with the best-determined median member redshifts, while the top right panel shows the comparison for the remainder, including only those with between 3 and 10 member galaxies with spectra; those with $z_{\text{best}} = z_{\text{BCG}}$ are removed altogether. The fraction of BCGs with velocities differing from the median by more than 2000 km s^{-1} is 5.6% (8/143) for the best-measured set and 13% (117/910) for the remainder. While BCG projection does occasionally occur, it is not particularly common. When it does happen, it is most common to find an unusually red foreground galaxy projected onto a more distant

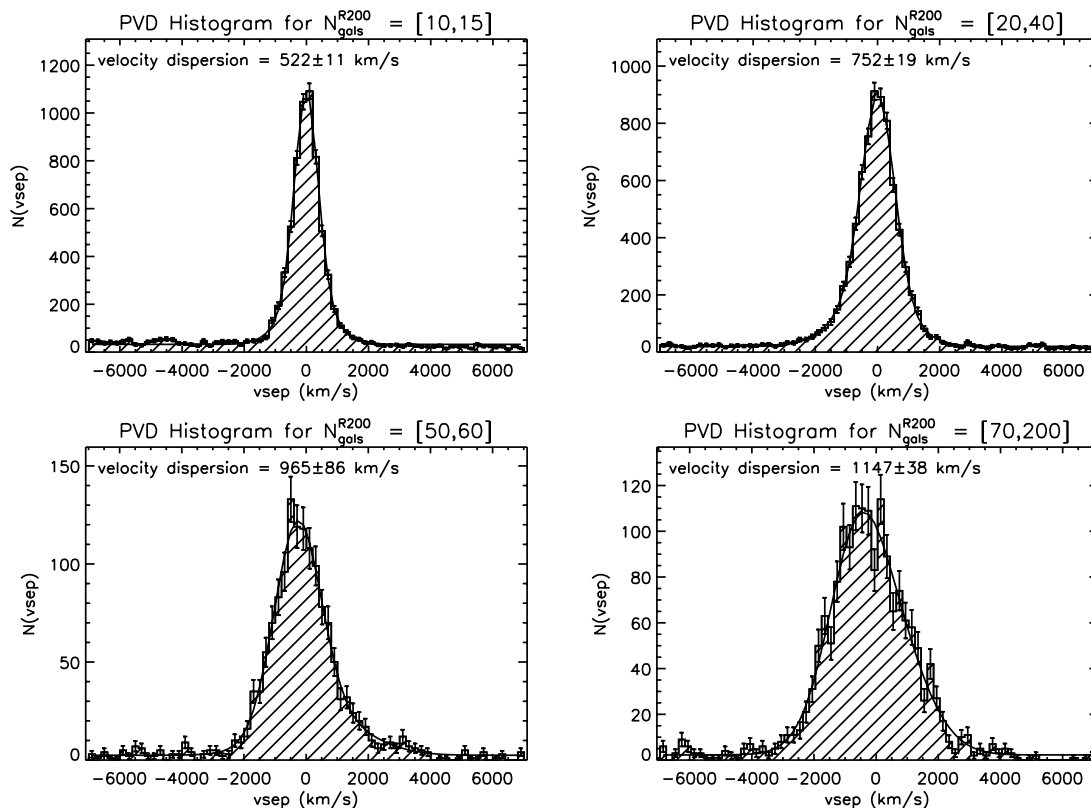


FIG. 11.—Examples of the velocity distribution seen relative to the BCGs in clusters with various values of N_{gal}^{R200} . While the distribution is approximately Gaussian, it is much better fitted by a combination of two Gaussians. The characteristic dispersions shown in the legends are the appropriately weighted averages of the two best-fit Gaussians.

cluster. BCG projection is also somewhat less likely as clusters increase in richness.

To study the importance of projection for cluster member galaxies, we compare individual member redshifts, z_{memb} , to the best estimate of the cluster redshift, z_{best} . Again, we conduct the comparison both for the clusters with the best-determined value z_{best} and also for the remainder, including only those with between 3 and 10 member galaxies with spectra. These comparisons are shown in the bottom panels of Figure 10. In the best-measured clusters, 16% (427/2701) of member galaxies are found to have velocities differing from the median by more than 2000 km s^{-1} . For the less well measured clusters, 16% (829/5068) have velocities differing from the median by more than 2000 km s^{-1} . Since the determination of z_{best} is not especially robust for these clusters, this represents an upper bound on the degree of member projection.

This test demonstrates the relative insensitivity of red-sequence methods to large-scale projection effects. No more than 13% of BCGs and 16% of the galaxies identified as cluster members according to color and spatial location are actually observed in projection. The majority of projected members lie behind the cluster; they are intrinsically bluer galaxies at higher redshift. Narrowing the color window for membership can reduce the incidence of projection, but, as shown in the accompanying algorithm paper (Koester et al. 2007), it also increases the fragmentation of dark matter halos.

The conclusions drawn here are restricted somewhat by the realities of the SDSS spectroscopic selection. Galaxies for which spectra are obtained are preferentially bright cluster members, and there is a small fiber-collision bias against the measurement of galaxies in the densest regions. Since the member galaxies selected here are all brighter than $0.4L_*$ and the probability of

cluster membership is highest in the densest regions, the effect of these limitations on our conclusions should be minimal, but they complicate measurements such as the radial dependence of member projection (T. A. McKay et al. 2007, in preparation).

6.3. Relating Richness and Velocity Dispersion

In addition to their usefulness in confirming cluster redshifts, spectroscopic samples of galaxies can be applied to understand the relation between richness and cluster velocity dispersion. In the current catalog, the number of E/S0 ridgeline galaxies, N_{gal}^{R200} is a basic indicator of cluster richness. To understand the relationship between this cluster richness and the velocity dispersion, we begin with a list of clusters for which a spectroscopic redshift for the BCG is known. Around each such BCG, we search for any other galaxies with measured spectroscopic redshifts and define spectroscopic “pairs,” each of which includes a BCG and a nearby tracer of the velocity field. For this study we keep all pairs in which the neighboring galaxy lies within a projected distance R_{200} of the BCG and within $\pm 7000 \text{ km s}^{-1}$ of the BCG velocity, irrespective of whether the neighboring galaxy is a member of the E/S0 ridgeline; this value of R_{200} is the same as that derived from Hansen et al. (2005) for photometric data. In many cases, a cluster will contribute only a few pairs, making the determination of individual velocity dispersions impractical. As a result, we gather together all pairs for clusters of similar richness and hence measure the average pairwise velocity difference (PVD) structure around a class of similar clusters. This *stacking* approach is analogous to that applied in the study of halo masses in isolated galaxies by McKay et al. (2002) and Prada et al. (2003).

Examples of the velocity structure seen around these clusters in several N_{gal}^{R200} bins are shown in Figure 11. These PVD

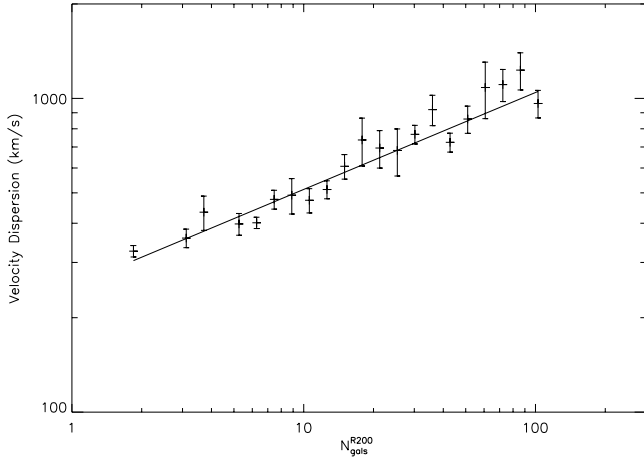


FIG. 12.—Dependence of stacked velocity dispersion on scaled richness N_{gal}^{R200} . The steady increase of the stacked velocity dispersion with richness illustrates the connection between N_{gal}^{R200} and mass. The best-fit power law for these data is $\ln \sigma = (5.52 \pm 0.04) + (0.31 \pm 0.01) \ln N_{\text{gal}}^{R200}$. At the $N_{\text{gal}}^{R200} \geq 10$ threshold for this cluster catalog, the typical velocity dispersion is $\approx 500 \text{ km s}^{-1}$.

histograms are approximately Gaussian, but show clear evidence for components both narrower and broader than the average. This probably arises from the imperfect mapping between N_{gal}^{R200} and mass. If all clusters in a narrow bin of N_{gal}^{R200} had the same mass, we would expect a very nearly Gaussian PVD. If, however, the bin contains a mix of both lower and higher mass objects, the PVD will include a mix of narrower and broader components (Scoccimarro 2004). To determine the typical velocity dispersions in each bin, we fit two Gaussians plus a constant to the PVD histogram. The constant is shown by Wojtak et al. (2006) to adequately account for unbound particles in simulations (see also T. A. McKay et al. 2007, in preparation). The dispersion is then the square root of the weighted average of the variances of the two Gaussians. The weights of each Gaussian are determined in the fitting procedure (the expectation maximization algorithm; see Connolly et al. 2000). Two Gaussians are used in the fit as a more convenient and stable parametric fit to the PVD histogram. They allow us to fully measure the second moment of the PVD histograms and, more importantly, to measure their kurtosis. The kurtosis is an important parameter that allows one to constrain mass mixing in these PVD histograms.

Median velocity dispersions for clusters binned by N_{gal}^{R200} are shown in Figure 12. There is a clear increase in measured velocity dispersion with richness N_{gal}^{R200} . This increasing velocity dispersion is related to the increasing mass of the sample, reinforcing the idea that N_{gal}^{R200} is a useful proxy for mass. This richness measure is simple: just a count of the number of bright E/S0 ridgeline galaxies in a cluster. A variety of refined richness measures can be derived from these data, including matched filter likelihoods, member galaxy luminosities, and total optical luminosities. It is likely that combinations of luminosity and concentration measures will provide useful mass estimators for clusters, just as they do for individual elliptical galaxies (Zaritsky et al. 2006). It should also be useful to include measures of the diffuse optical light in the clusters, as this may include as much as 40% of the total optical light (Zibetti et al. 2005; Gonzalez et al. 2005; Krick et al. 2006). A more detailed description of these richness-dispersion scaling relations, along with their extension to cluster mass and mass scatter estimates, is given in a companion paper (T. A. McKay et al. 2007, in preparation). Additional information about the masses of clusters detected in

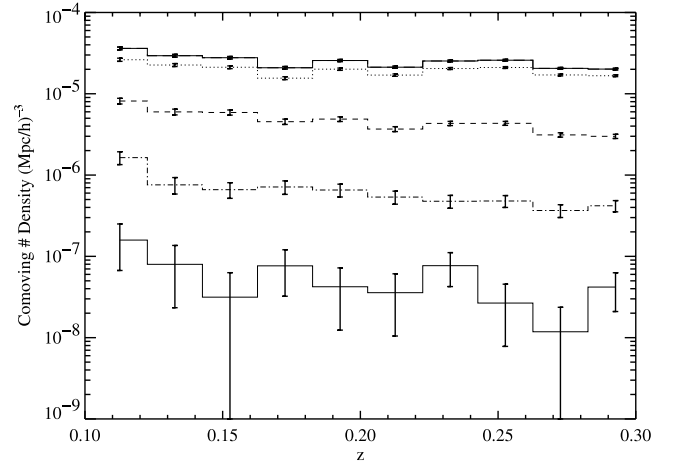


FIG. 13.—Comoving number density of objects of varying richness. The solid top line represents the space density for the full catalog. The lines below it represent the space density in ranges of richness. From top to bottom, these ranges are $10 < N_{\text{gal}}^{R200} < 20$, $20 < N_{\text{gal}}^{R200} < 43$, $43 < N_{\text{gal}}^{R200} < 91$, and $91 < N_{\text{gal}}^{R200} < 189$. Poisson error bars are overlotted.

the SDSS can be provided by weak-lensing measurements, as was done for a much smaller cluster sample in Sheldon et al. (2001). The combination of lensing and dynamical mass calibration will provide the input needed for estimation of the cluster mass function.

6.4. Measurements of Space Density

Λ CDM simulations reveal that the space density of dark matter halos is nearly constant out to $z \sim 0.3$, with only a small increase in the number of objects at the high end of the mass function at late times. In Figure 13, the comoving number density of clusters in a given N_{gal}^{R200} bin is plotted as a function of redshift. No correction for purity or completeness is applied. It is approximately flat in all bins, as predicted by theory. This is a simple demonstration of the roughly volume-limited nature of the catalog. Measurements on simulations indicate that the slight decrease seen in the highest N_{gal}^{R200} bin is due to evolution in the mass- N_{gal}^{R200} relation or a redshift-dependent bias in the definition of $0.4L_*$ and not to incompleteness at high redshift. Before proceeding to use this measurement as a tool to constrain cosmology, careful calibration must be made of the richness-mass relation and especially of any possible dependence of this relation on redshift. The details of this mass calibration will be presented in future papers on dynamical and weak-lensing mass estimators.

7. COMPARISON TO KNOWN X-RAY-SELECTED CLUSTERS

An important test of any cluster finder is the extent to which it identifies those clusters found by other means. Optically selected catalogs generated by alternative codes with measurements, sky, and redshift coverage similar to the current catalog are not yet available, but will in the future be invaluable in understanding selection biases in maxBCG. X-ray surveys are attractive for this purpose, in that they are dependent on different cluster physics, have mass proxies, accurate redshifts, and large sky coverage. Just as with comparisons of optically identified clusters to mock catalog halos, some care must be taken. Optical and X-ray methods may identify different cluster centers, and while optical richness and X-ray luminosity are clearly coupled (Lin et al. 2004;

Popesso et al. 2005), there is significant scatter in this relation. Nevertheless, we expect that in the field of X-ray–bright clusters there should be some significant overdensity of galaxies that is approximately centered on the X-ray peak. With this in mind, we investigate the extent to which known X-ray clusters were identified in this catalog. Because the maxBCG cluster finder centers clusters according to the BCG location, we compare our BCG location to the X-ray peak location.

Comparison of optical and X-ray catalogs is complicated by several factors. First, the central galaxies in clusters are also not always perfectly coincident with peaks in the X-ray emission, and the identification of a single cluster BCG in merging systems is often ambiguous. The X-ray–brightest clusters are also especially likely to contain BCGs exhibiting unusual colors, often due to cooling flows with accompanying star formation or AGN activity (Crawford 2004). In addition, the optically selected sample presented here extends to much lower mass objects than existing large-area X-ray catalogs include. For these reasons, we do not use the X-ray sample to quantify the purity of the optical sample, but merely use it as a check of our ability to locate most previously identified clusters.

We conduct our comparison to the combined NORAS (Northern *ROSAT* All-Sky; Böhringer et al. 2000) and REFLEX (*ROSAT*-ESO Flux-Limited X-ray; Böhringer et al. 2004) catalogs. These catalogs are purely X-ray–selected, are flux-limited to about 3×10^{-12} ergs cm $^{-2}$ s $^{-1}$ at energies 0.1–2.4 keV, and, when combined, cover both the northern and southern Galactic caps. Within the redshift limits of this maxBCG catalog ($0.1 < z < 0.3$) and its sky coverage, the combined NORAS and REFLEX catalogs contain 99 X-ray clusters. It is important to note that the NORAS catalog was based on early selection of extended sources and as a result is not as complete or pure as the later REFLEX catalog. A new generation of the NORAS catalog is under construction (H. Böhringer 2006, private communication).

To determine if an X-ray cluster was “found” in our maxBCG catalog, a cylinder centered on the X-ray peak with a $2 h^{-1}$ Mpc radius and a depth $|z_{\text{X-ray}} - z_{\text{photo}}| < 0.05$ is searched for optical clusters. For 94 of the 99 X-ray clusters a single, quite rich object and occasionally a few lower richness objects are found within these boundaries. The best match is defined by combining the richness of the optical object and the proximity to the center of the X-ray cluster. Despite the fact that a relatively deep redshift box is used for this match, the matches identified in this way have redshifts that agree with those given in NORAS and REFLEX with a dispersion of $\sigma_z \approx 0.003$, so they are clearly physically related. Because this exercise is automated, it differs from that in some previous comparisons of X-ray and optical properties. Here we compare optical centers identified with an automatic algorithm with X-ray centers, rather than visually examining each cluster and manually identifying BCGs. It shows that in many cases, the center selected by the automatic algorithm agrees with the BCG that would have been manually selected. For 76 of these 94 matches, the offsets between X-ray and BCG centers are less than $250 h^{-1}$ kpc. For these objects, the distribution of offsets has a median of $58 h^{-1}$ kpc and a standard deviation of $57 h^{-1}$ kpc. An additional 15 matches have offsets between $250 h^{-1}$ kpc and $1 h^{-1}$ Mpc. The remaining three matches have very large separations, between 1 and 2 Mpc. The separations larger than $250 h^{-1}$ kpc occur for a variety of reasons, and each of these cases, along with the five not matched, is described individually below.

The X-ray matching is summarized in Figure 14. The top left panel in this figure shows the close correspondence between X-ray redshift and maxBCG photometric redshift. The top right

panel compares the overall richness distribution of the maxBCG catalog to the richness distribution of the X-ray–matched clusters. While it is clear that they are drawn preferentially from high-richness objects, the effect is diluted by the flux-limited nature of the X-ray catalogs. The bottom left panel compares the projected separation between X-ray and BCG centers to the cluster redshift. The tightly clustered group of matches with separations $\leq 250 h^{-1}$ kpc is clear, along with the smaller number of large separation matches. The bottom right panel compares the optical richness N_{gal}^{R200} to the X-ray luminosity for these clusters, drawing a distinction between the close matches and those that are more distant. The correlation is poor and will be undertaken in a future study. Point-source contamination and the chosen physical scale are among the complicating factors.

A case-by-case comparison was undertaken for each match separated by 250 – $2000 h^{-1}$ kpc. The full details of this comparison are reserved for a future work that examines the relationship between optical and X-ray properties of clusters. The 23 clusters for which the maxBCG cluster location differs from the NORAS/REFLEX X-ray center by 250 – $2000 h^{-1}$ kpc fall into several categories: complications in centering the X-ray flux due to point-source contamination and mergers, maxBCG centering complications due to the lack of a dominant BCG, BCGs with evidence of cooling flows that produce rather blue colors, and matched maxBCG clusters with richnesses below the N_{gal}^{R200} threshold. In these cases, the X-ray cluster is not missed; the centers chosen by optical and X-ray means disagree.

A final concern in this matching exercise is the incidence of matches by chance. The large-radius matches (250 – $2000 h^{-1}$ kpc) of maxBCG clusters to X-ray clusters may be the most subject to chance projections. To investigate this, we place 13,823 random points in the SDSS footprint with redshifts drawn from the maxBCG redshift distribution and positions noncoincident with maxBCG clusters within a projected $2 h^{-1}$ Mpc. The same matching routine is run to match these points to the NORAS/REFLEX X-ray catalog. Of the 99 NORAS/REFLEX X-ray clusters, we find 0 matches between $250 h^{-1}$ and $1000 h^{-1}$ kpc and 6 between $1000 h^{-1}$ and $2000 h^{-1}$ kpc. In the same ranges for the maxBCG clusters, we find 18 between $250 h^{-1}$ and $1000 h^{-1}$ kpc and 5 between $1000 h^{-1}$ and $2000 h^{-1}$ kpc. This simple test indicates that outside $1 h^{-1}$ Mpc, our matches are more subject to chance projections with the NORAS/REFLEX X-ray sample.

This simple matching exercise shows that in the catalog presented here, we are $\simeq 80\%$ successful at automatically identifying the BCGs selected manually by visual selection in bright X-ray clusters. This comparison also highlights some of the difficulties encountered in optical X-ray comparisons. Many X-ray–bright clusters have emission-line BCGs (perhaps 25%; Crawford et al. 1999) at their centers. Cluster finders that search for red-sequence BCGs may miss these centers. Future cluster-finding algorithms based on the red sequence may choose to account for this by searching for BCGs with unusually blue colors, although doing so invites contamination by foreground galaxies. In addition, there are examples in the X-ray catalogs of clusters without a single unambiguous BCG, and of clusters where the visually apparent BCG does not coincide well with the peak of X-ray emission. In some cases this may be due to contamination of the X-ray signal by cluster galaxy AGN emission. Unrelaxed clusters or those undergoing mergers are especially prone to this. The cases in which the optical cluster finder did not automatically identify the visually selected BCGs come from a mix of these issues. They are a combination of the algorithm used for

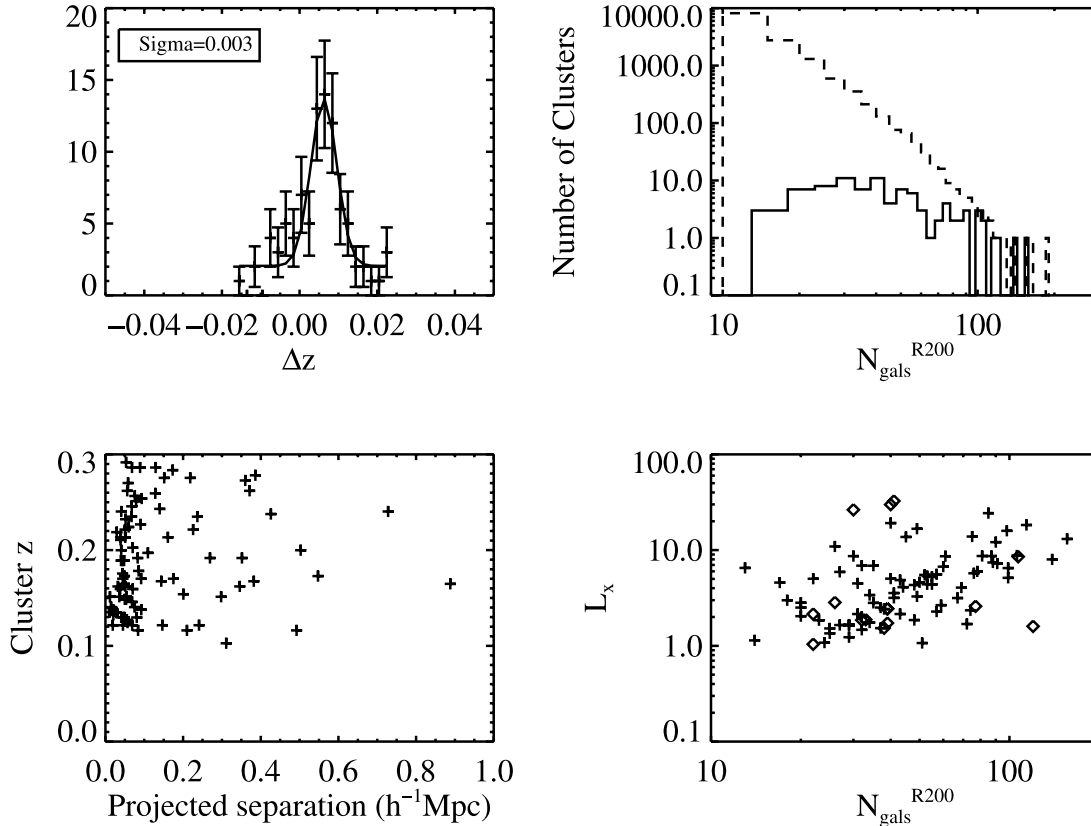


FIG. 14.—Summary of the results of comparisons of the maxBCG catalog to the combined NORAS and REFLEX catalogs. The top left panel shows the difference between NORAS/REFLEX spectroscopic cluster redshifts and the matching maxBCG photometric redshifts. The dispersion of the best-fit Gaussian (shown overlaid) is $\sigma_z = 0.003$. The top right panel shows the richness distribution of the full maxBCG catalog compared to the richness distribution for the clusters that match NORAS/REFLEX sources. The bottom left panel shows the projected separations between X-ray and optical centers as a function of redshift. The bottom right panel compares X-ray luminosity (in units of 10^{43} ergs s^{-1}) from NORAS/REFLEX to the N_{gal}^{R200} optical richness. Plus signs indicate the 73 clusters with X-ray optical offsets $\leq 250 h^{-1}$ kpc, and diamonds indicate the 14 clusters with offsets from 250 to $1000 h^{-1}$ kpc.

cluster finding and the complex cluster physics that determine the BCG location, spectrum, the optical galaxy membership, and the X-ray signal.

8. DISCUSSION

We have presented a new catalog of clusters of galaxies selected from SDSS photometric data using the maxBCG technique, which represents the largest galaxy cluster catalog assembled to date. This technique uses the clustering of galaxies on the sky, in magnitude, and in color to identify groups and clusters of bright E/S0 ridgeline galaxies. It identifies objects ranging in size from single isolated elliptical galaxies to the richest galaxy clusters. We have extracted from this very large list a sample of 13,823 clusters containing at least 10 E/S0 ridgeline galaxies brighter than $0.4L_*$. Running this cluster finder on realistic mock galaxy catalogs allows us to show that this cluster sample is more than 90% pure and more than 90% complete for halos with masses $\geq 2 \times 10^{14} h^{-1} M_\odot$. Comparison between maxBCG photometric redshifts and SDSS spectroscopic redshifts for BCGs demonstrates the precision and accuracy of the derived cluster redshifts. The large volume of SDSS spectroscopic data also allows, in a somewhat limited way, an examination of the effect of projection on both our identification of the brightest cluster galaxies and on our determination of cluster membership. In both cases we show that large-scale projection plays only a small role in red-sequence cluster detection.

We have shown that the basic richness measure presented here, the scaled number of bright E/S0 ridgeline galaxies N_{gal}^{R200} ,

is strongly correlated with cluster velocity dispersion. Comparison of this optically selected catalog with the existing NORAS and REFLEX X-ray-selected cluster catalogs reveals that nearly all of these relatively X-ray-luminous objects are detected among the richest of the optical clusters found here. As comparable wide-angle imaging cluster catalogs with accurate redshifts become available, these comparisons will be extended to catalogs selected by alternate optical algorithms as well. Further aspects of this cluster catalog, including galaxy populations and profiles, mass calibration by both dynamical and lensing measurements, diffuse light measurements, and the cosmological constraints it can place will be examined in future papers.

Funding for the SDSS and SDSS-II has been provided by the Alfred P. Sloan Foundation, the Participating Institutions, the National Science Foundation, the US Department of Energy, the National Aeronautics and Space Administration, the Japanese Monbukagakusho, the Max Planck Society, and the Higher Education Funding Council for England. The SDSS Web site is <http://www.sdss.org/>. T. A. M., A. E., and B. P. K. gratefully acknowledge support from NSF grant AST 04-4327. R. H. W. is supported by NASA through Hubble Fellowship grant HST-HF-01168.01-A awarded by the Space Telescope Science Institute. We are also grateful for the repeated hospitality of the Aspen Center for Physics and the Michigan Center for Theoretical Physics.

The SDSS is managed by the Astrophysical Research Consortium for the Participating Institutions. The Participating Institutions are the American Museum of Natural History, the Astrophysical Institute Potsdam, the University of Basel, Cambridge University, Case Western Reserve University, the University of Chicago, Drexel University, Fermilab, the Institute for Advanced Study, the Japan Participation Group, Johns Hopkins University, the Joint Institute for Nuclear Astrophysics, the Kavli

Institute for Particle Astrophysics and Cosmology, the Korean Scientist Group, the Chinese Academy of Sciences (LAMOST), Los Alamos National Laboratory, the Max-Planck-Institute for Astronomy (MPIA), the Max-Planck-Institute for Astrophysics (MPA), New Mexico State University, Ohio State University, the University of Pittsburgh, the University of Portsmouth, Princeton University, the United States Naval Observatory, and the University of Washington.

REFERENCES

- Abell, G. O. 1958, *ApJS*, 3, 211
 Abell, G. O., Corwin, H. G., & Olowin, R. P. 1989, *ApJS*, 70, 1
 Adami, C., Ulmer, M. P., Romer, A. K., Nichol, R. C., Holden, B. P., & Pildis, R. A. 2000, *ApJS*, 131, 391
 Adelman-McCarthy, J. K., et al. 2006, *ApJS*, 162, 38
 Annis, J., et al. 1999, *BAAS*, 31, 1391
 Bahcall, N. A. 1999, *ApJ*, 525, 873
 Bahcall, N. A., & Soneira, R. M. 1983, *ApJ*, 270, 20
 Bahcall, N. A., et al. 2003, *ApJS*, 148, 243
 Berlind, A. A., et al. 2006, *ApJS*, 167, 1
 Biviano, A. 2000, in *Constructing the Universe with Clusters of Galaxies*, ed. F. Durret & D. Gerbal (Paris: IAP), 1
 Blanton, M. R., Lin, H., Lupton, R. H., Maley, F. M., Young, N., Zehavi, I., & Loveday, J. 2003a, *AJ*, 125, 2276
 Blanton, M. R., et al. 2001, *AJ*, 121, 2358
 ———. 2003b, *AJ*, 125, 2348
 ———. 2003c, *ApJ*, 594, 186
 Böhringer, H., et al. 2000, *ApJS*, 129, 435
 ———. 2004, *A&A*, 425, 367
 Bower, R. G., Lucey, J. R., & Ellis, R. S. 1992, *MNRAS*, 254, 601
 Carlstrom, J. E., Holder, G. P., & Reese, E. D. 2002, *ARA&A*, 40, 643
 Clowe, D., Trentham, N., & Tonry, J. 2001, *A&A*, 369, 16
 Collins, C. A., Guzzo, L., Nichol, R. C., & Lumsden, S. L. 1995, *MNRAS*, 274, 1071
 Connolly, A. J., Genovese, C., Moore, A. W., Nichol, R. C., Schneider, J., & Wasserman, L. 2000, preprint (astro-ph/0008187)
 Conroy, C., Wechsler, R., & Kravtsov, A. 2006, *ApJ*, 647, 201
 Crawford, C. S. 2004, in *Clusters of Galaxies: Probes of Cosmological Structure and Galaxy Evolution*, ed. J. S. Mulchaey, A. Dressler, & A. Oemler (Pasadena: Carnegie Obs.), 9
 Crawford, C. S., Allen, S. W., Ebeling, H., Edge, A. C., & Fabian, A. C. 1999, *MNRAS*, 306, 857
 Dahle, H., Pedersen, K., Lilje, P. B., Maddox, S. J., & Kaiser, N. 2003, *ApJ*, 591, 662
 Dalcanton, J. J. 1996, *ApJ*, 466, 92
 Dalton, G. B., Efstathiou, G., Maddox, S. J., & Sutherland, W. J. 1994, *MNRAS*, 269, 151
 de Putter, R., & White, M. 2005, *NewA*, 10, 676
 Diaferio, A., Geller, M. J., & Rines, K. J. 2005, *ApJ*, 628, L97
 Diaferio, A., Kauffmann, G., Colberg, J. M., & White, S. D. M. 1999, *MNRAS*, 307, 537
 Ebeling, H., Voges, W., Böhringer, H., Edge, A. C., Huchra, J. P., & Briel, U. G. 1996, *MNRAS*, 281, 799
 Eisenstein, D. J., et al. 2001, *AJ*, 122, 2267
 Eke, V. R., et al. 2004, *MNRAS*, 355, 769
 Erben, T., van Waerbeke, L., Mellier, Y., Schneider, P., Cuillandre, J.-C., Castander, F. J., & Dantel-Fort, M. 2000, *A&A*, 355, 23
 Evrard, A. E., et al. 2002, *ApJ*, 573, 7
 Fukugita, M., Ichikawa, T., Gunn, J. E., Doi, M., Shimasaku, K., & Schneider, D. P. 1996, *AJ*, 111, 1748
 Gal, R. R. 2006, preprint (astro-ph/0601195)
 Gal, R. R., de Carvalho, R. R., Lopes, P. A. A., Djorgovski, S. G., Brunner, R. J., Mahabal, A., & Odewahn, S. C. 2003, *AJ*, 125, 2064
 Gerke, B. F., et al. 2005, *ApJ*, 625, 6
 Gioia, I. M., & Luppino, G. A. 1994, *ApJS*, 94, 583
 Gladders, M. D., & Yee, H. K. C. 2000, *AJ*, 120, 2148
 ———. 2005, *ApJS*, 157, 1
 Gonzalez, A. H., Zabludoff, A. I., & Zaritsky, D. 2005, *ApJ*, 618, 195
 Gonzalez, A. H., Zaritsky, D., Dalcanton, J. J., & Nelson, A. 2001, *ApJS*, 137, 117
 Goto, T., et al. 2002, *AJ*, 123, 1807
 ———. 2003, *PASJ*, 55, 739
 Green, P. J., et al. 2004, *ApJS*, 150, 43
 Gunn, J. E., & Oke, J. B. 1975, *ApJ*, 195, 255
 Gunn, J. E., et al. 1998, *AJ*, 116, 3040
 ———. 2006, *AJ*, 131, 2332
 Hansen, S. M., McKay, T. A., Wechsler, R. H., Annis, J., Sheldon, E. S., & Kimball, A. 2005, *ApJ*, 633, 122
 Hogg, D. W., Finkbeiner, D. P., Schlegel, D. J., & Gunn, J. E. 2001, *AJ*, 122, 2129
 Ivezić, Ž., et al. 2004, *Astron. Nachr.*, 325, 583
 Johnston, D. E., Sheldon, E. S., Tasitsiomi, A., Frieman, J. A., Wechsler, R., & McKay, T. A. 2007, *ApJ*, 656, 27
 Katgert, P., Biviano, A., & Mazure, A. 2004, *ApJ*, 600, 657
 Kim, R. S. J., et al. 2002, *AJ*, 123, 20
 Kochanek, C. S., White, M., Huchra, J., Macri, L., Jarrett, T. H., Schneider, S. E., & Mader, J. 2003, *ApJ*, 585, 161
 Koester, B. P., et al. 2007, *ApJ*, 660, 221
 Kravtsov, A. V., Vikhlinin, A., & Nagai, D. 2006, *ApJ*, 650, 128
 Krick, J. E., Bernstein, R. A., & Pimbblet, K. A. 2006, *AJ*, 131, 168
 Lee, B. C., et al. 2004, *AJ*, 127, 1811
 Lin, Y.-T., Mohr, J. J., & Stanford, S. A. 2004, *ApJ*, 610, 745
 Loh, Y.-S., & Strauss, M. A. 2006, *MNRAS*, 366, 373
 Lucey, J. R. 1983, *MNRAS*, 204, 33
 Lumsden, S. L., Nichol, R. C., Collins, C. A., & Guzzo, L. 1992, *MNRAS*, 258, 1
 Lupton, R. H., Gunn, J. E., & Szalay, A. S. 1999, *AJ*, 118, 1406
 Majumdar, S., & Mohr, J. J. 2004, *ApJ*, 613, 41
 McKay, T. A., et al. 2002, *ApJ*, 571, L85
 Miller, C. J., Batuski, D. J., Slingsland, K. A., & Hill, J. M. 1999, *ApJ*, 523, 492
 Miller, C. J., et al. 2005, *AJ*, 130, 968
 Miralles, J.-M., et al. 2002, *A&A*, 388, 68
 Mullis, C. R., et al. 2003, *ApJ*, 594, 154
 Nagai, D., & Kravtsov, A. 2005, *ApJ*, 618, 557
 Oegerle, W. R., & Hill, J. M. 2001, *AJ*, 122, 2858
 Ostrander, E. J., Nichol, R. C., Ratnatunga, K. U., & Griffiths, R. E. 1998, *AJ*, 116, 2644
 Pier, J. R., Munn, J. A., Hindsley, R. B., Hennessy, G. S., Kent, S. M., Lupton, R. H., & Ivezić, Ž. 2003, *AJ*, 125, 1559
 Popesso, P., Biviano, A., Böhringer, H., & Romaniello, M. 2007, *A&A*, 461, 397
 Popesso, P., Biviano, A., Böhringer, H., Romaniello, M., & Voges, W. 2005, *A&A*, 433, 431
 Popesso, P., Böhringer, H., Brinkmann, J., Voges, W., & York, D. G. 2004, *A&A*, 423, 449
 Postman, M., Huchra, J. P., & Geller, M. J. 1992, *ApJ*, 384, 404
 Postman, M., & Lauer, T. R. 1995, *ApJ*, 440, 28
 Postman, M., Lauer, T. R., Oegerle, W., & Donahue, M. 2002, *ApJ*, 579, 93
 Postman, M., Lubin, L. M., Gunn, J. E., Oke, J. B., Hoessel, J. G., Schneider, D. P., & Christensen, J. A. 1996, *AJ*, 111, 615
 Prada, F., et al. 2003, *ApJ*, 598, 260
 Romano, P., Campana, S., Mignani, R. P., Moretti, A., Panzera, M. R., & Tagliaferri, G. 2004, *Mem. Soc. Astron. Italiana Suppl.*, 5, 343
 Romer, A. K., Viana, P. T. P., Liddle, A. R., & Mann, R. G. 2001, *ApJ*, 547, 594
 Romer, A. K., et al. 2000, *ApJS*, 126, 209
 Rosati, P., della Cecca, R., Norman, C., & Giacconi, R. 1998, *ApJ*, 492, L21
 Sadat, R., Blanchard, A., Kneib, J.-P., Mathez, G., Madore, B., & Mazzarella, J. M. 2004, *A&A*, 424, 1097
 Sandage, A., Kristian, J., & Westphal, J. A. 1976, *ApJ*, 205, 688
 Schlegel, D. J., Finkbeiner, D. P., & Davis, M. 1998, *ApJ*, 500, 525
 Scoccimarro, R. 2004, *Phys. Rev. D*, 70, 083007
 Scranton, R., Connolly, A. J., Szalay, A. S., Lupton, R. H., Johnston, D., Budavari, T., Brinkman, J., & Fukugita, M. 2005, *AJ*, submitted (astro-ph/0508564)
 Scranton, R., et al. 2002, *ApJ*, 579, 48
 Sheldon, E. S., et al. 2001, *ApJ*, 554, 881
 ———. 2006, *ApJ*, submitted
 Smith, J. A., et al. 2002, *AJ*, 123, 2121
 Springel, V., et al. 2005, *Nature*, 435, 629
 Stoughton, C., et al. 2002, *AJ*, 123, 485

- Strauss, M., et al. 2002, AJ, 124, 1810
Sutherland, W. 1988, MNRAS, 234, 159
Vikhlinin, A., Kravtsov, A., Forman, W., Jones, C., Markevitch, M., Murray, S. S., & Van Speybroeck, L. 2006, ApJ, 640, 691
Weinmann, S. M., van den Bosch, F. C., Yang, X., & Mo, H. J. 2006, MNRAS, 366, 2
White, M., & Kochanek, C. S. 2002, ApJ, 574, 24
White, M., van Waerbeke, L., & Mackey, J. 2002, ApJ, 575, 640
Wittman, D., Dell'Antonio, I. P., Hughes, J. P., Margoniner, V. E., Tyson, J. A., Cohen, J. G., & Norman, D. 2006, ApJ, 643, 128
Wittman, D., Margoniner, V. E., Tyson, J. A., Cohen, J. G., Becker, A. C., & Dell'Antonio, I. P. 2003, ApJ, 597, 218
Wittman, D., Tyson, J. A., Margoniner, V. E., Cohen, J. G., & Dell'Antonio, I. P. 2001, ApJ, 557, L89
Wojtak, R., Lokas, E. L., Mamon, G. A., Gottloeber, S., Prada, F., & Moles, M. 2006, A&A, submitted (astro-ph/0606579)
Yang, X., Mo, H. J., van den Bosch, F. C., & Jing, Y. P. 2005, MNRAS, 356, 1293
York, D. G., et al. 2000, AJ, 120, 1579
Zaritsky, D., Gonzalez, A. H., & Zabludoff, A. I. 2006, ApJ, 638, 725
Zaritsky, D., Nelson, A. E., Dalcanton, J. J., & Gonzalez, A. H. 1997, ApJ, 480, L91
Zehavi, I., et al. 2004, ApJ, 608, 16
Zibetti, S., White, S. D. M., Schneider, D. P., & Brinkmann, J. 2005, MNRAS, 358, 949
Zwicky, F. 1933, Helvetica Phys. Acta, 6, 110
———. 1937, ApJ, 86, 217
Zwicky, F., Herzog, E., & Wild, P. 1961, Catalogue of Galaxies and of Clusters of Galaxies (Pasadena: Caltech)