

A MEAN VALUE MODEL FOR ESTIMATION OF LAMINAR AND TURBULENT FLAME SPEED IN SPARK-IGNITION ENGINE

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ABSTRACT

Flame velocity is the main parameter for determination of combustion propagation in a spark-ignition engine. The first part of combustion that consists of flame initiation and flame kernel growth has laminar velocity. For a certain radius of kernel growth, transition to turbulent flame occurs; afterwards, the flame can be described as turbulent. This paper investigates the relationship between fuel properties and engine operation parameters, their influence on flame velocity and their ability to calculate the time delay from ignition to 50% mass fraction burned (MFB) that is used for adjusting the spark advance. The GT-Power software is employed to simulate the combustion process of a spark-ignition (SI) engine. The flame speed mean value model is applied to determine the laminar flame speed under different amounts of unburned mixture, temperatures and pressures. The results show that mixture with less than the stoichiometric ratio has the greatest laminar flame speed. At higher temperature, the difference between poor and rich mixture is significant for laminar flame speed. On the other hand, the relationship between turbulence intensity and engine speed is almost linear. The cylinder pattern used to create turbulence during the intake and compression strokes defines the slope between the engine speed and turbulent flame speed. The mean value flame speed model was capable of determining the combustion phasing and predicting spark ignition in advance.

Keywords: Spark ignition engine; mean value model; laminar flame speed; turbulent flame speed; turbulence intensity; chamber geometry.

INTRODUCTION

The rate of flame travel in a spark-ignition engine cylinder is the main factor controlling the rate of pressure increase, and hence it has an important influence on engine performance [1]. The spark-ignition engine combustion rate is primarily dictated by the chamber geometry, the turbulent flame entrainment rate, and the laminar flame speed of mixture burn-up [2, 3]. The combustion flame propagation, distribution and disappearance can be simplified by a parametric model. Various flame structure models are applied in combustion calculations [4]. The mean flame front models are the ones that follow the simplest structure, where the turbulent flame is represented by its mean location. This approach works together with a flame geometry model in quasidimensional engine cycle simulations. The flame structure model accounts for the laminar flame speed, turbulent flame speed, and transition between these two. The flame speed model used in the flame structure model should provide values for those three quantities. The flame structure model may incorporate a model for the flame kernel initiation and development process [5-7]. The flame initiation and flame kernel growth during combustion are laminar. Transition to turbulent flame occurs until the flame has a radius of about 5 mm; afterwards, the flame can be described as turbulent [8, 9]. The flame structure model may apply different models for the laminar flame speed and turbulent flame speed, with the transition from laminar to turbulent being determined by a flame development angle [10, 11]. Otherwise, the flame structure model may incorporate a single model that calculates the flame speed at all stages, laminar, transition and turbulent [12]. Existing turbulent flame speed models are often a function of the laminar flame speed, the turbulence intensity and other scaling parameters. These models are generally the result of a correlation between experimental data and the scaling parameters. The scaling parameters are not always easily determined by ordinary instrumentation, and may be a limiting factor in the utilization of such models [13]. Combustion is initiated considering the product volume to be a very small percentage of the cylinder volume. The flame structure model previously assumed a laminar flame speed at the beginning of combustion, with an abrupt transition to turbulent flame at a specified flame development angle. Afterwards, combustion was assumed to be fully turbulent, where the turbulent flame speed was given by the laminar flame speed multiplied by a factor. The turbulent flame continued until the end of combustion [14, 15].

Laminar flame speed is a function of the mixture equivalence ratio, pressure, temperature, and residual gas fraction [16]. In-cylinder turbulence and flow patterns are influenced by the mean piston speed, intake parameters such as valve timing and port geometry, the length of the compression stroke during which there is turbulence decay, and combustion. The combustion chamber geometry and spark plug location affect the burn rate by altering the flame front area, determined by the interaction of the spherical flame front and combustion chamber walls. An accurate combustion model must therefore account for at least the effects of chamber geometry, laminar flame speed and in-cylinder turbulence [17, 18]. Nowadays, spark-ignition (SI) engines work with a variety of fuel types with different properties. On the other hand, engine operation requires a simple and accurate model to account for fuel variation. While the laminar and turbulent flame speed uses a complex formulation, a mean value model is proposed for turbulent flame speed. Gasoline was selected as the fuel and the simulation was run with engine operation boundaries such as intake pressure, intake temperature and stoichiometric mixture. Simulink MATLAB[®] was used for calculation of the flame speed parameters and GT-Power software was employed to apply the model to the combustion simulation [19, 20]. A 1.6L 4-cylinder CAMPRO engine GT-Power model was used.

METHODS AND MATERIALS

Formulation for Turbulent Flame Speed

The turbulent flame speed model uses all the fundamentals related to spark-ignition engine combustion variables. The first assumption is that the flame structure model does not employ the flame development angle. The correlation between laminar and turbulent flame speed during a whole combustion event is described by Eq. (1). The model covers the combustion process from the initially laminar flame to the fully turbulent flame.

$$\frac{S_T}{S_L} = 1 + \left(\frac{CR}{8}\right)^a \left(\frac{\rho_u}{\rho_b}\right)^{\phi_1} \left(\frac{p}{p_{ig}}\right)^{\phi_2} \left(0.5\frac{\overline{S}_P}{S_L}\right)^b \left(1 - exp\left(-\frac{R_f}{cD}\right)\right)$$
(1)

where S_T is turbulent flame speed (m/s), S_L is laminar flame speed and (m/s), *CR* is compression ratio, ρ_u and ρ_b are density of the unburned and burned charge ahead of the flame, p_{ig} and p are cylinder pressure at the time of ignition and cylinder pressure (bar), \overline{S}_P is mean piston speed (m/s), R_f is flame radius (m), a,b and c are constant coefficients, *D* is cylinder bore (m) and ϕ_1 and ϕ_2 are fuel coefficients. By simplifying the engine running and cylinder geometrical parameters in Eq. (1) into *C* as a coefficient, Eq. (2) is generated. The turbulence intensity of Eq. (2) has been defined as half of the mean piston speed in Eq. (1) [13].

$$\frac{S_T}{S_L} = 1 + C(\frac{\rho_u}{\rho_b})^{\frac{1}{2}} (\frac{u'}{S_L})^b (1 - \exp(-\frac{R_f}{r_c}))$$
(2)

The turbulence integral scale r_c was assumed to correlate with the cylinder bore. The coefficients of Eq. (1) are set according to experiments. ϕ_1 and ϕ_2 are functions of the mixture equivalence ratio:

$$\phi_l = d + e(\phi - 1) \tag{3}$$

$$\phi_2 = f + g(\phi - 1) \tag{4}$$

The constant coefficients d, e, f and g are also adjusted by conducting the fuel experiments procedure.

Laminar Flame Speed

The laminar flame speed in Eq. (1) is calculated from the expression developed by [21]:

$$S_L = S_{L,0} \left(\frac{T_u}{T_0}\right)^{\alpha} \left(\frac{p}{p_0}\right)^{\beta} \left(1 - 2.06 F_R^{0.77}\right)$$
(5)

where T_u is unburned mixture temperature (K), T_0 and p_0 are reference temperature (298 °K) and pressure (1 atm), $S_{L,0}$ is reference laminar speed, α and β are temperature and pressure exponents for a given fuel. The last term in Eq. (5) is the correction to take into account the effects of the residual gas mass fraction. The values used for gasoline as the constant coefficients in Eqs. (1), (3) and (4) for the simulation were the following: a = 1.1, b = 0.7, c = 1.7, d = 0.611, e = 1.4, f = 1.152 and g = -1.5. These values were determined in such a way that the measured and calculated peak pressure coincide in value and take place at the same crank angle.

Eq. (6) is used for reference flame speed correction according to equivalence ratio variations [22].

$$S_{L,0} = B_m + B_\phi (\phi - \phi_m)^2$$
(6)

where B_m , B_{ϕ} and ϕ_m are the fuel constants, ϕ and ϕ_m are the equivalence ratio and the equivalence ratio at which maximum flame speed occurs for the selected fuel [23].

Turbulence Intensity Modeling

The controls-oriented model is developed based upon the quasi-dimensional turbulent flame entrainment concept first introduced by [24] and refined by [25, 26] and finally propagated by [27]. The rate at which unburned mass is entrained by the flame front is described by Eq. (7). The flame is assumed to propagate through the unburned charge along Kolmogorov-scale vortices entraining turbulent eddies. The entrainment velocity is defined by the sum of a diffusive component, laminar flame speed, and a convective component, turbulence intensity. The flame front area is defined by the leading flame edge, not the total flame surface area enclosing the still unburned eddies. Of these parameters, the mass entrainment rate is most influenced by the turbulence intensity and flame front area [18]. Turbulence intensity is defined as the root-mean-squared velocity fluctuation within the cylinder [28], and is generally an order of magnitude larger than the laminar flame speed.

$$\frac{dm_e}{dt} = \rho_u A_f(u' + S_L) \tag{7}$$

where $m_e =$ mass entrained by the flame, $\rho_u =$ density of the unburned charge ahead of the flame, $A_f =$ total flame front area, u' = turbulence intensity and $S_L =$ laminar flame speed.

After the turbulent flame entrainment, the mass burn-up rate can be described by Eq. (8). The burn-up rate is proportional to the total unburned mass entrained behind the flame front. Entrained turbulent eddies are then assumed to burn up at the laminar flame speed since the length scale is small. The eddy size is approximated as the Taylor micro-scale, which is the assumed length scale over which laminar diffusion occurs, justifying the use of the laminar flame speed in this case [25]. The Taylor micro-scale is calculated using Eq. (9). It is important to note that the Taylor micro-scale is a function of turbulence intensity.

$$\frac{dm_b}{dt} = \frac{m_e - m_b}{\tau} \tag{8}$$

where m_b =total burned mass, $\tau = \frac{\lambda}{S_L}$, characteristic cell burn time and λ = Taylor micro-scale of turbulence.

$$\frac{\lambda_{S_{L}}}{S_{L}} = \left(\sqrt{\frac{15}{\xi}}\right) \left(\frac{u'L}{v}\right)^{-\frac{1}{2}}$$
(9)

where $\xi = 1$ (assumption made by [25]), L = integral length scale and v = kinematic viscosity.

Prior to ignition, the integral length scale is assumed equal to the instantaneous combustion chamber height [18]. After ignition, which is the period of interest here, unburned charge is compressed at such a rate that the rapid distortion theory (RDT) is assumed valid. The RDT is used when the timescale of the turbulence distortion rate is much shorter than the large eddy turnover or decay timescales [29]. The RDT assumes that angular momentum within the turbulent field is conserved, and that there is no interaction between turbulent eddies [30]. Rapid distortion theory defines the integral length scale during combustion by Eq. (10). The instantaneous chamber height at the time of the spark is calculated by dividing the cylinder volume by the bore area.

$$L = L_0 \left(\frac{\rho_{u0}}{\rho_u}\right)^{\frac{1}{3}}$$
(10)

where L_0 = chamber height at ignition, ρ_{u0} = unburned charge density at ignition, ρ_u = unburned charge density during combustion.

The flame front area at each crank angle is interpreted from a geometrically calculated table. The flame-area table is generated using engine-specific combustion chamber geometry. Spherical coordinates, originating at the spark plug, are used to calculate a flame front area and burned gas volume for a range of radii at each crank angle. Additional information, such as flame/wall interaction areas with the piston, cylinder walls, and cylinder head, is also generated. The cylinder volume V at any crank position θ is calculated by Eq. (11), where *s* is the distance between the crank axis and the piston pin axis generated from Eq. (12).

$$V = V_c + \frac{B^2}{4}(l + a - s)$$
(11)

$$s = a\cos\theta + (l^2 - a^2\sin^2\theta)^{1/2}$$
(12)

where V_c is compression volume, *B* is cylinder bore, *l* is connecting road length, *a* is crank radius [14]. Furthermore, the combustion chamber space simulated by using the engine cylinder head and piston drawing part are used for flame front area calculation. The inverse-model is derived from the quasi-dimensional turbulent flame entrainment model introduced in the previous section. Eqs. (7) to (10) are solved for the entrained intensity using the following methodology. First, Eq. (8) is solved for the entrained

mass (see Eq. (13)).

$$m_e = m_b + \tau (\frac{dm_b}{dt}) \tag{13}$$

The derivative of Eq. (13) is related to the rate of turbulent flame entrainment. The characteristic diffusive cell burn time, τ , is assumed constant during differentiation to simplify calculations.

$$\underbrace{\left(\frac{d\tau}{dt}\right)\left(\frac{dm_b}{dt}\right) + \tau\left(\frac{d^2m_b}{dt^2}\right) + \left(\frac{dm_b}{dt}\right) = \left(\frac{dm_e}{dt}\right) = \rho_{unburned}A_{flame}\left(u' + S_L\right)$$
(14)

To solve for Eq. (14), it is converted into a cubic polynomial (Eq. (15)). The cubic polynomial can be solved graphically or numerically. Only positive real roots of the polynomial are acceptable solutions for u'. The mass-fraction burned curve from a single-zone heat release model is used as the input for the derivative of the mass-burning rate. The flame front area, laminar flame speed, and unburned gas density and temperature are also calculated at each crank angle.

$$u'^{3} + 2(S_{L} - \frac{1}{\rho A} \frac{dm_{b}}{dt})u'^{2} + (S_{L}^{2} + \frac{1}{(\rho A)^{2}} (\frac{dm_{b}}{dt})^{2} + \frac{2S_{L}}{\rho A} \frac{dm_{b}}{dt})u' = \frac{15L\upsilon}{\xi(\rho A S_{L})^{2}} (\frac{d^{2}m_{b}}{dt^{2}})^{2}$$
(15)

Previous studies have demonstrated that the turbulence intensity scales linearly with the mean piston speed (MPS) [31]. The increase in turbulence intensity with engine speed occurs because the time duration of the intake stroke changes. For a given air and fuel mass, increasing engine speed will decrease the induction time and create high velocities at the intake valves. The slope of turbulence intensity with respect to mean piston speed varies with the engine design and operating condition. Typical slope values range from approximately 0.4 to 1.7.

The base turbulence intensity level is determined from the mean piston speed and valve overlap using

$$u' = c_I V_{MPS} \tag{16}$$

where c_1 = specific coefficient and V_{MPS} = mean piston speed (m/s). The relationship between the RPM and MPS is

$$V_{MPS} = \frac{2n}{60}.l\tag{17}$$

where l is piston stroke and n is engine speed (rpm). The standard fixed-cam engines generally have a period when both the intake and exhaust valves are open simultaneously, known as valve overlap. The valve overlap is designed into fixed-cam engines as a compromise that will allow function throughout the speed and load range of the engine. For this model, a 20° overlap is assumed for calculation [2].

RESULTS AND DISCUSSION

The model was simulated using the Simulink MATLAB[®] and GT-Power softwares. Eqs. (5)–(6) are employed for laminar flame speed determination and Eqs. (15)–(17) are utilized for turbulent flame speed estimation. All the initial values assumed for gasoline and running parameters are chosen in the domain of the SI engine operating range. Table 1 shows the fuel properties and engine operating parameters during the simulation process. Figure 1 shows the variation of the laminar flame speed with equivalence ratio, temperature, and pressure. The phenomena of the laminar flame speed have an inverse behavior in lean and rich air-to-fuel conditions. Laminar flame speed variation at low temperature (328 °K) is negligible; however, by increasing the in-cylinder temperature, the laminar flame speed increases for poor mixtures and decreases in rich conditions. At higher temperatures, the difference between the poor and rich mixtures for laminar flame speed was significant.

Fuel		Engine	
Property	Range	Parameter	Range
$S_{L,0}$	34–41 cm/s	speed	1000–6000 rpm
ϕ_m	1.21	intake temperature	328–428 °K
α (temperature exponent)	$2.4-0.27 l\phi^{3.51}$	cylinder pressure	4–10 bar
β (pressure exponent)	$-3.57+0.14\phi^{2.77}$	ϕ	0.9–1.1
B_m	35 cm/s	valve overlap	20 °CAD
B_{ϕ}	-54.9 cm/s	intake valve lifting	0.15 mm

Table 1. Fuel properties and engine operation parameters.

Figure 1(b) illustrates the relation between the laminar flame speed and the equivalence ratio at the time of ignition in a condition where the in-cylinder mixture temperature (350 °K) and pressure (1 bar) for gasoline (mean value model) and the experimental fuel are reported for a mixture of 80% iso-Octane plus 20% ethanol/ air [32]. Any increase in the cylinder pressure decreases the laminar flame speed. Different fuels have the same properties in very poor and very rich conditions, while the maximum laminar flame occurs around $\phi = 1$.

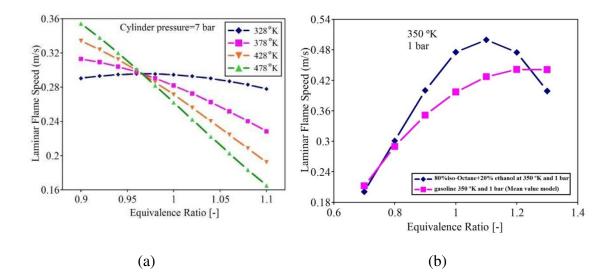


Figure 1. Laminar flame speed at different equivalence ratios with (a) cylinder temperatures; and (b) different fuels.

As a primary factor to determine the flame entrainment rate, turbulence intensity trends must be quantified throughout the engine operating range. A simple model for turbulence intensity prediction is also desirable for real-time spark timing prediction. Turbulence intensity predictions with respect to MPS follow a linear trend, as shown in Figure 2. The simulation was run at MBT timing, constant valve overlap, stoichiometric air-to-fuel ratio, and fixed engine load to isolate the influence of engine speed. The valve overlap has a direct influence on the slope between engine speed and turbulence intensity. As a result, each system that affects valve overlap – for instance, the variable

valve timing (VVT) system – is required to take into account the valve overlap parameter.

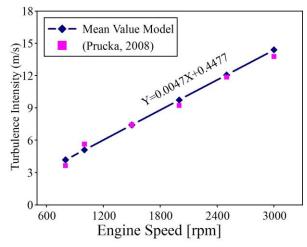


Figure 2. Relation between turbulence intensity and engine speed.

The location of 50% MFB was adjusted at 8° aTDC for optimum combustion efficiency. The ignition timing was set to keep the combustion phasing at the desired value. Figure 3 shows the result of applying the mean value model to the engine combustion model, and the engine brake torque and brake power are also illustrated.

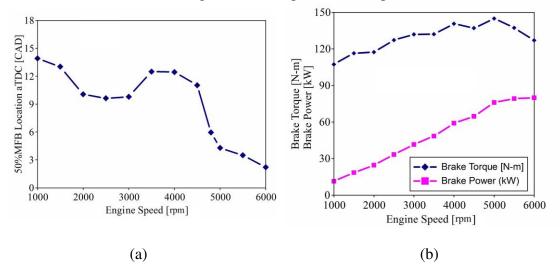


Figure 3. (a) The location of 50% MFB; (b) engine brake torque and power.

CONCLUSIONS

The SI combustion investigation was performed to evaluate the laminar and turbulent burning speed of near-to-stoichiometry gasoline/air flames. These formulations are based on easily determined engine geometric and running parameters. The cylinder pattern to create turbulence during the intake and compression strokes defines the slope between the engine speed and turbulent flame speed. By substituting the complex turbulent formulation with a mean value model, the engine management system is able to control the engine online. 50% MFB as the combustion phasing is accessible by utilizing this flame speed model. One goal of the mean value flame speed model is to

develop techniques to predict the flame speed. Later, the flame velocity will be used to determine the combustion delay between the spark and 50% MFB location. Therefore, the spark advance, as a most important control parameter that affects engine outputs such as torque, specific fuel consumption, and exhaust emissions, may be estimated.

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