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A Modified Neutral-Point Balancing Space Vector Modulation for Three-Level Neutral Point Clamped Converters in High Speed Drives

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Abstract—This paper describes a high performance neutral point voltage balancing technique for a Neutral point clamped (NPC) Converter. Conventional neutral point voltage balancing methods do not function well under low power factor, low pulse ratio and near-unity modulation index operation conditions. These conditions are essentially dominant operation conditions for aircraft starter/generator systems. This paper introduces an alternative space vector modulation technique for three-level NPC converters in an aircraft starter generator system. The selection of voltage space vectors is optimized for high modulation index and low power factor operation. Disturbances caused by low pulse ratio is also compensated. The proposed method maintains neutral point voltage balance and ripple minimization over the full range of operating conditions. The paper also provides a detailed analysis into the sources of neutral point voltage imbalances and ripples in high speed drives with deep flux weakening. Simulation results obtained from a Simulink/PLECS model and experimental results obtained from a 45kVA, 32krpm aircraft starter generator test rig proves the proposed method eliminates the neutral point voltage imbalance and significantly reduces the neutral point voltage ripple.

Index Terms— Electric Starter Generator, More Electric Aircraft, Three Level, Neutral Point Balancing, High Speed Drives.

I. INTRODUCTION

SINCE the beginning of the More Electric Aircraft (MEA) concept, an increasing number of hydraulic, pneumatic and mechanical systems for large passenger aircraft have been replaced by their electrical equivalences to improve fuel efficiency and reduce emissions [1-3]. A key technology for

MEA is an electrical starter generator system which enables starting aircraft engines electrically and running as a generator when engines reach self-sustained speed [2]. A 45kVA, 32krpm aircraft electric starter generator system (ESG) has been presented in [5-6]. The ESG system consists of a Permanent Magnet Synchronous Machine [7-8] (PMSM) and a bi-directional power converter, as shown in Fig. 1. The machine is connected to the engine shaft and the converter operates as an interface between the ESG machine and a 270V DC bus. During the engine start-up process, the ESG accelerates the engine up to the ignition speed. In generation mode, the ESG extracts power from the engine shaft and supplies various onboard electrical loads through an AC/DC converter.

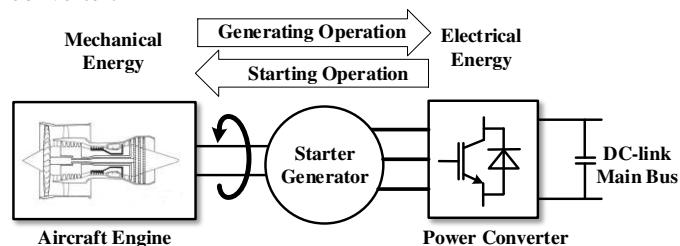


Fig. 1. Diagram of the target starter generator system

For the developed high-speed ESG, a three-level neutral point clamped (NPC) converter was chosen instead of a two-level topology due to its reduced switching loss and improved power quality[9-10]. Furthermore, each phase leg of the NPC converter can be seen as a single-pole three-throw switch as shown in Fig. 2[11]. This arrangement creates a total number of 27 voltage space vectors, allowing flexibility for the converter modulation.

However, one disadvantage of the topology is the potential voltage imbalance of two capacitors at the dc-link, i.e. neutral point (NP) voltage imbalance. The types of imbalance can be defined into two categories. One category is the continuous DC imbalance between the upper and lower capacitor voltages. This type of imbalance is typically induced by imperfections (i.e. capacitance mismatch, non-linear loads etc.) within the converter or/and the load [12]. On the DC side, such imbalance

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would significantly increase the voltage stress placed on capacitors. On the DC side, the increased voltage stress can potentially cause capacitor or semiconductor device failures. On the AC side, a continuous DC imbalance will result in even order current harmonics. These induced harmonics can potentially aggravate the voltage imbalance, reduce the power quality and machine performance.

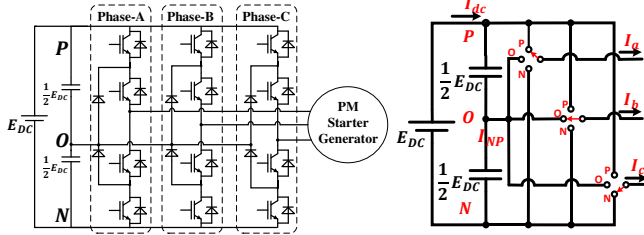


Fig. 2. Circuit diagram of a classic three-level NPC converter

The other category of NP voltage imbalance is the AC imbalance. This type of imbalance is essentially harmonic ripples (normally dominated by the third harmonic). This type of imbalance is an inherent property of the NPC converter using nearest-three-vector modulation (NTV)[13]. The amplitude of such ripple increases when the converter operates at low power factor and high modulation index conditions. To suppress this AC imbalance, larger capacitors are required. This is not ideal for aircraft applications as a larger capacitor means increased volume and weight of the overall system. The AC imbalance could cause distortion of converter output voltage and thus degrade performance of electrical machines.

Different solutions to eliminate these imbalances have been proposed recently. For the continuous DC imbalance, a classic family of solutions are based on common-mode voltage (CMV) injection[12]. Despite being simple, the performance of such method is weakened at lower power factor conditions. Its balancing capability also diminishes when the magnitude of fundamental current component is low. A six harmonic voltage injection is proposed in[14], where the dependency of power factor and fundamental current is addressed. However, the balancing capability at high power factors is reduced with this technique. Alternatively, the method proposed in [15] modifies the average NP current by injection of even-order harmonics [16] on the AC side. This method covers the gap in low power factor and low fundamental current operations. However, the drawback is an elevated AC side current THD.

To suppress the 3rd harmonic NP voltage ripple, carrier based pulse width modulation methods typically adopts variable common mode voltage injection [17-18] whereas nearest-three-vector (NTV) space vector modulation (SVM) methods tend to manipulate the redundant small vectors[11]. These methods work effectively at low to medium modulation index and high power factor operation conditions. However, their ripple suppression capabilities are limited when NPC operates at high modulation index and low power factor conditions. To address the dependency of modulation index and power factor, virtual space vector modulation method and its hybrids emerged[19-21]. This method creates a virtual vector by correlating duty cycles of adjacent small and medium vectors, thus achieving zero average NP current within each switching period. However, such method results in larger switching loss and increased common-mode noises. AC side

current THD is also increased at high modulation index. In addition, the zero neutral point current within each switching period is based on the assumption that the phase currents stays constant throughout each switching period, which would not be true under low pulse ratio condition.

For both types of imbalance, there are also hardware solutions such as adding extra balancing circuit[22], having two capacitors supplied by separate DC sources and back to back operation. With increased hardware component, the weight and volume will be increased as well as the cost.

Despite many NP balancing methods have been reported[13][15][23], none of them can deliver desirable performance under stringent operating conditions of ESG. A tailored NP balancing modulation method is therefore required. In this paper, operating characteristics of the target ESG system are elaborated and light load condition with high modulation index and low power factor is identified as the most vulnerable condition for NP imbalance and ripple. An alternative SVM method is proposed, aiming at maintaining NP voltage balanced and ripple minimized at near-unity modulation index and full power factor range whilst supporting bi-directional power flow. The performance of the method is validated by detailed simulation and experiments

II. PRINCIPLES OF OPERATION

A. ESG system characteristics and control

For the electric starter generator system, a 6-pole 36-slot surface mount PMSM is selected and classic vector control structure with synchronous reference frame current regulators based on conventional PI controllers and space vector modulation is implemented as shown in Fig.3. Vector control approach is selected over direct torque control(DTC) for the PMSM as DTC lack of direct current regulation, which is required in the control of power flowing between the engine shaft and aircraft DC-bus. Modulated model predictive control is also developed for the project as a parallel option [24], and has been achieved on a two-level converter based drive. However, model predictive control techniques have poor tolerance against parameter variations, whereas the ESG sometimes operates at a temperature as low as -70 °C, which leads to significant parameter variation.

For the synchronous reference frame current regulation, when the machine is rotating beyond the base speed, flux weakening operation is activated and negative d-axis current is injected based on the error between the reference voltage and the voltage limit set by the inverter[25]. The q-axis current reference is set by the outer speed loop when the system operates in starter mode. During flight, the system operates in generation mode and the q-axis current reference is set by the DC-link current demands dictated by a droop control technique[26-27]. In such circumstances, both q-axis and d-axis currents are negative, a large negative d-axis current is constantly required for flux weakening. Therefore, the power factor is typically very low. In addition, the flux weakening operation requires almost full utilization of the DC-link voltage. Therefore, a near-unity modulation index is expected.

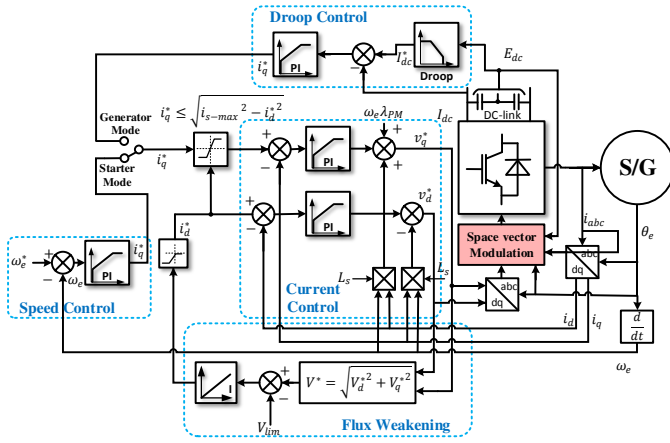


Fig. 3. Control structure for the target ESG system [28]

Based on the parameters of the machine given in table. II. in the appendix, the operational limits and trajectory of the ESG system is presented in Fig. 4. In the starter mode, the operation trajectory follows the maximum torque per amp (MTPA) line. When flux-weakening starts, the trajectory follows the current limit set by converter and voltage limit based on speed. After engine ignition at 10krpm, ESG is in standby mode and q-axis current falls to zero. Generation mode starts at 20krpm. At such speed, the fundamental electrical frequency is 1kHz. The control system sampling frequency and converter switching frequency are 16kHz, therefore a pulse ratio below 16:1 would be expected. This pulse ratio is significantly lower than typical drives. Furthermore, when the ESG is on standby or lightly loaded conditions, active power is fractional whilst reactive power is large due to flux weakening requirement. This makes the ESG working in a low power factor condition.

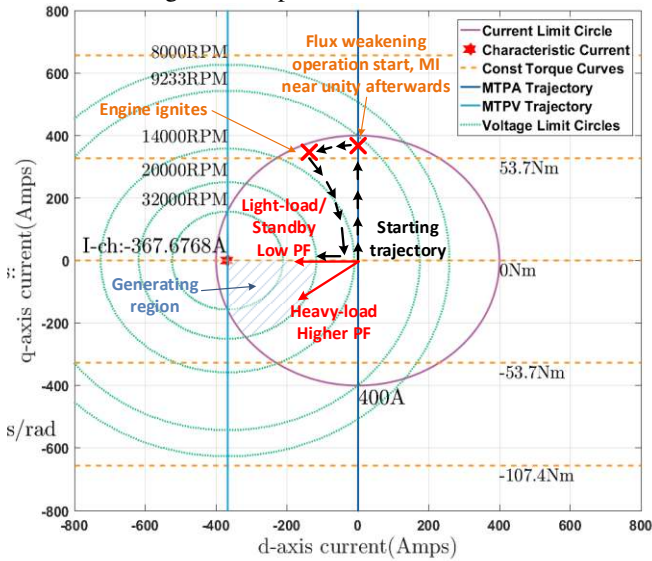


Fig. 4. Operating trajectory of the target system

B. Conventional SVM strategy

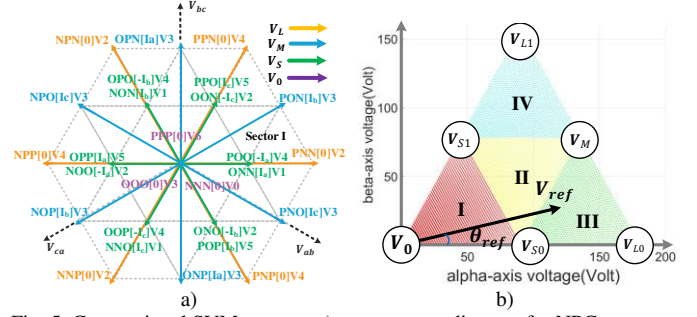


Fig. 5. Conventional SVM strategy a) space vector diagram for NPC converter b) space vector diagram in sector I

A total number of 27 switching states are available for a three-level NPC converter. As illustrated in Fig. 5, large vectors have magnitudes of $2V_{DC}/3$. When this vector applies, three phases are either connected to the positive or the negative rail. Thus, these vectors do not affect the NP voltage. For the null vectors, all three phases are connected to the same rail and thus do not affect the NP voltage either. For the medium vectors (with a magnitude of $\frac{\sqrt{3}}{3}V_{DC}$), the three phases are connected to the positive rail, the negative rail and the neutral point respectively. Take vector PNO for example. Phase C is connected to the neutral point. Therefore, the phase current i_c is flowing into the neutral point and thus affecting the neutral point potential. Small vectors are with magnitudes of $V_{DC}/3$. As they come in pairs with opposite polarity of NP current, they could be used to mitigate the NP voltage drift caused by the medium vectors[11].

Conventional SVM synthesize the reference voltage vector in the stationary reference frame based on the nearest three space vectors (NTV) [11] as in Fig. 6, where the triangle represents the Sector. I of the space vector hexagon in Fig. 5. Vector V_0 represents the null vector; vector V_{S0} & V_{S1} represents the small vectors; vector V_M represents the medium vector and vector V_{L0} & V_{L1} represents the large vector. The duty cycle of each vector is calculated based on voltage-time-area balance between the selected voltage space vectors and the reference vector, for example, a reference vector falls inside the region 3 in Fig 6 can be calculated from (1) and (2):

$$V_{ref} = d_{S0}V_{S0} + d_{L0}V_{L0} + d_MV_M \quad (1)$$

$$d_{S0} + d_{L0} + d_M = 1 \quad (2)$$

III. ANALYSIS OF NEUTRAL POINT IMBALANCE

A. Source of NP ripple and imbalance

With the modulation principles described in Section II.B, the neutral point is being charged or discharged by the current i_{NP} when the medium vectors or the small vectors are applied. For the upper capacitor and the lower capacitor, the difference of charge Q induced within each switching period is dependent on the neutral current i_{NP} . This charge difference Q is referred as current-time-area (ITA) and defined as:

$$Q = \int_0^{T_s} I_{NP} dt \quad (3)$$

Thus the variation of the neutral point voltage ΔV_{NP} can then be determined as:

$$\Delta V_{NP} = \frac{Q}{C} = \frac{ITA}{C} \quad (4)$$

where C represents the capacitance of the DC-link capacitor.

For the medium vector V_M and the small vectors V_{S0} and V_{S1} , their neutral point current-time-area within each switching period are:

$$\begin{aligned} ITA_M &= \int_0^{d_M T_s} I_{NP-M}(sector) dt \\ ITA_{S0} &= \int_0^{d_{S0} T_s} I_{NP-S0}(sector) dt \\ ITA_{S1} &= \int_0^{d_{S1} T_s} I_{NP-S1}(sector) dt \end{aligned} \quad (5)$$

where T_s represents the switching period, d_x represents the duty cycle for corresponding vectors, and the neutral point current during corresponding voltage states can be found in Table. I.

Table. I. Neutral point current for medium and small vectors

Sector	$I_{NP-M}(sector)$	$I_{NP-S0}(sector)$	$I_{NP-S1}(sector)$
I	i_b	$\pm i_a$	$\pm i_c$
II	i_a	$\pm i_c$	$\pm i_b$
III	i_c	$\pm i_b$	$\pm i_a$
IV	i_b	$\pm i_a$	$\pm i_c$
V	i_a	$\pm i_c$	$\pm i_b$
VI	i_c	$\pm i_b$	$\pm i_a$

Assuming the phase currents are perfectly sinusoidal, the neutral point potential drift induced by the small vectors and the medium vector over a line cycle with regards to modulation index and power factor angle can be mapped using (5) and Table. 1, as shown in Fig. 6. It should be noted that the high power factor region refers to the area where the power factor angle is close to 0 or $\pm\pi$, and low power factor region refers to where the power factor angle is close to $\pm 0.5\pi$.

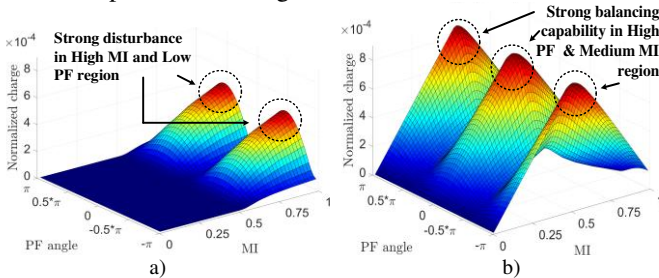


Fig. 6. Neutral point potential drift caused by a) V_M b) V_{S0} and V_{S1}

It can be seen that the medium vector places a large impact on the neutral point potential in high modulation index and low power factor range. The small vectors can be used to decrease the impact of medium vectors on the neutral point voltage. This counterbalance capability is reflected by the current-time-area of small vectors for one whole duty cycle. The balancing ability of small vectors is shown in Fig. 6. As can be seen, this capability is stronger when the system operates at medium modulation index and higher power factor conditions.

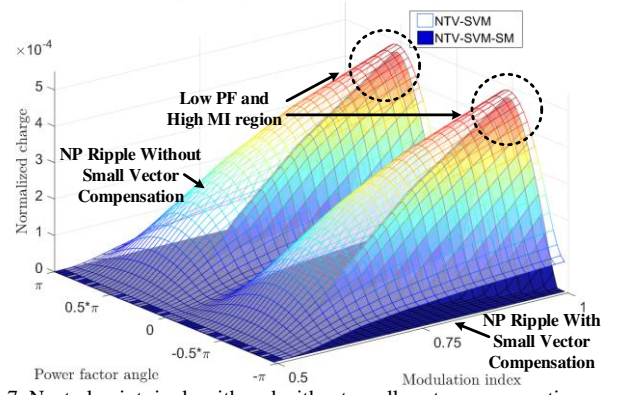


Fig. 7. Neutral point ripple with and without small vector compensation

Conventional NTV-SVM technique for NPC converter swap the polarity of the small vectors in alternate switching periods instead of manipulating them against the medium vector within each switching period[13].Such method can effectively cancel the impact of small vectors but leave the disturbance from the medium vector untouched. This method serves as a benchmark for various neutral point balancing modulation approaches. The extent of the 3rd harmonic neutral point potential ripple with and without manipulation of small vectors is presented in Fig. 7. It can be observed that the manipulation of small vectors can reduce the extent of the neutral point ripple. However, at very high modulation index and lower power factor, the ripple remains almost unchanged. This indicates that the NTV-SVM method with small vector manipulation (NTV-SVM-SM) has very poor balancing capability in this operating condition.

B. Issue with high fundamental frequency

Exploiting the redundancy of the small vectors to balance to the neutral point voltage requires feedback information of phase currents. Both quantities can be seen as constant at the presence of the 1.5 sample period delay in digital control systems, as long as the pulse ratio is high enough. However, as explained in section II, the pulse ratio of the target ESG system can be lower than 16:1 in the generating mode. Under this operation condition, there can be significant differences between the sampled phase currents and the phase currents when control actions are applied. Assuming the target ESG system is operating at 1kHz fundamental frequency, the movement of rotor electrical position θ_{adv} during 1.5 sample period can be obtained by:

$$\theta_{adv} = 1.5\omega_o T_s \quad (6)$$

Where T_s represents one sample period; ω_o represents the fundamental frequency. The calculated advance angle θ_{adv} is $\frac{3}{16}\pi$. Since the ESG uses a PMSM, the rotor flux and stator flux are synchronized. Therefore, such advance angle θ_{adv} can also be used to obtain the variation of phase currents in the 1.5 sample period in the steady state.

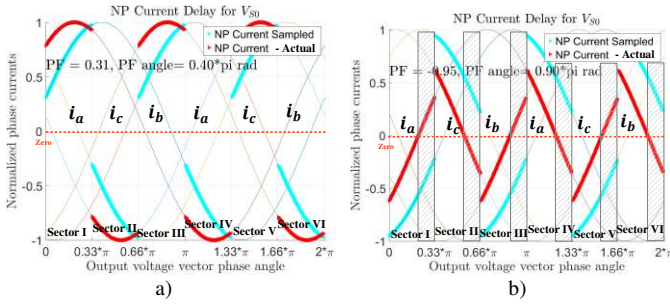


Fig. 8. Variation of NP current of V_{S0} a) before & b) after $1.5 T_s$ of sample delay. Blue line: the sampled current i_{NP} ; red line: the actual current when the control action applied

For the small vector V_{S0} , its corresponding neutral point current over a line cycle under the influence of the 1.5 sample delay with respect to different power factor angle is presented in Fig. 8. The term ‘NP current - actual’ refers to the neutral point current when the control actions are applied. When the power factor angle is 0.4π , both the sampled NP current and the actual NP current have the same polarity over a full line cycle. However, when the power factor angle is 0.9π , the sampled NP current and the advanced NP current (i.e. NP currents when control output applied) have the opposite polarity in the shaded region, during which erroneous would be selected if such effect is not compensated.

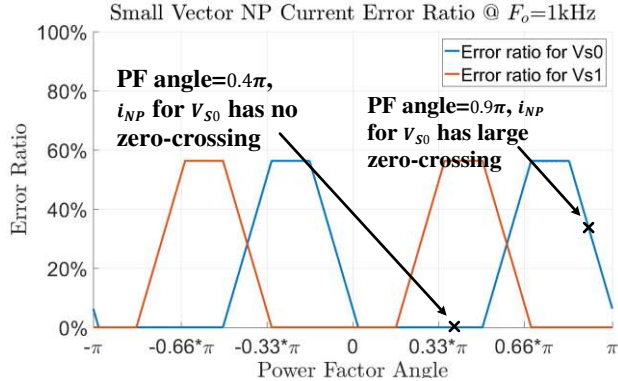


Fig. 9. NP current error ratio for small vectors

The error ratio, hence the possibility of erroneous neutral point current polarity being selected for small vectors over a full power factor range is presented in Fig. 9. Combining small vector V_{S0} and V_{S1} , the possibility of erroneous small vector being selected exceeds 50% over a significant power factor range, at which the NP balancing ability offered by small vector redundancy would completely diminish.

IV. THE PROPOSED MODULATION TECHNIQUE

A. Principle of operation

The proposed space vector modulation scheme suppresses neutral point imbalance and ripple by restricting the use of the medium vector at higher modulation index. The sectors are divided for sub-sectors as given in Fig. 10.

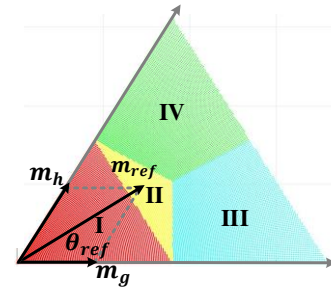


Fig. 10. Region division for the proposed SVM

The reference voltage region identification approach is presented in table. II. Where the indices V_{ref} and V_{ref} for a given reference voltage with a magnitude of V_{ref} and a phase angle of θ_{ref} can be obtained by:

$$\begin{bmatrix} m_g \\ m_h \end{bmatrix} = \frac{\sqrt{3}}{2V_{DC}} \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} V_{ref} \cos(\theta_{ref}) \\ V_{ref} \sin(\theta_{ref}) \end{bmatrix} \quad (7)$$

Table. II. Reference voltage region identification strategy

Region	Condition for m_g and m_h
I	$m_g + m_h \leq 0.5$
II	$m_g + m_h > 0.5$ && $m_g < 0.5$ && $m_h < 0.5$
III	$m_g > 0.5$ && $m_h > 0.5$ && $m_g \geq m_h$
IV	$m_g > 0.5$ && $m_h > 0.5$ && $m_g < m_h$

In region I given in Fig. 11, the reference vector is synthesized by a null vector and two small vectors. The duty cycles for each vector are given as:

$$\begin{aligned} d_{S0} &= 2 \cdot M \cdot \sin\left(\frac{\pi}{3} - \theta_{ref}\right) \\ d_{S1} &= 2 \cdot M \cdot \sin(\theta_{ref}) \\ d_0 &= 1 - d_{S0} - d_{S1} \end{aligned} \quad (8)$$

In the region II, the reference voltage vector is synthesized by the medium vector and the two small vectors.

The duty cycles for each vector are given in (9).

$$\begin{aligned} d_{S0} &= 1 - 2 \cdot M \cdot \sin(\theta_{ref}) \\ d_{S1} &= 1 + 2 \cdot M \cdot \sin\left(\theta_{ref} - \frac{\pi}{3}\right) \\ d_M &= 2 \cdot M \cdot \sin\left(\theta_{ref} + \frac{\pi}{3}\right) - 1 \end{aligned} \quad (9)$$

It should be emphasized that the target ESG system operates mostly in generating mode, where a high modulation index is constantly required due to the need of flux weakening. Therefore, the voltage space vector would mostly fall inside region III and IV. The region I and II would only be used for a short period in the starting mode when the ESG is running at low speed.

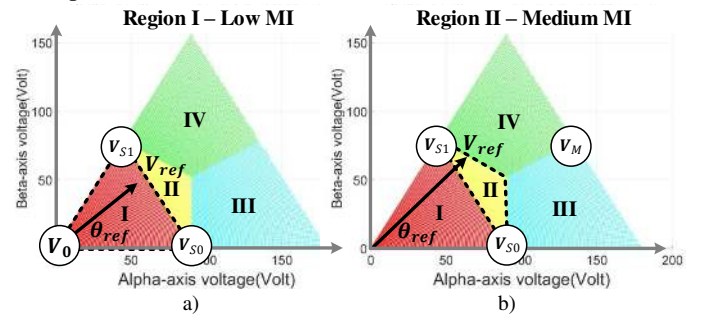


Fig. 11. Proposed SVM a) region 1 b) region 2

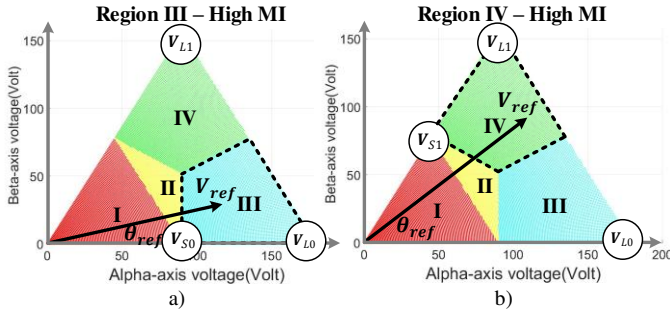


Fig. 12. Proposed SVM a) region 3 b) region 4

In the third and the fourth region, the modulation index is high. The reference voltage vector is synthesized by two large vectors and the adjacent small vector as shown in Fig. 12. The duty cycles for each vector are given in (10) and (11).

$$\begin{aligned} d_{S0} &= 2 - 2 \cdot M \cdot \sin(\theta_{ref} + \frac{\pi}{3}) \\ d_{L0} &= \sqrt{3} \cdot M \cdot \cos(\theta_{ref}) - 1 \\ d_{L1} &= M \cdot \sin(\theta_{ref}) \end{aligned} \quad (10)$$

$$\begin{aligned} d_{L0} &= M \cdot \sin(\theta_{ref} - \frac{\pi}{3}) \\ d_{L1} &= \sqrt{3} \sin(\theta_{ref} + \frac{\pi}{6}) - 1 \\ d_{S1} &= 2 - 2 \cdot M \cdot \sin(\theta_{ref} + \frac{\pi}{3}) \end{aligned} \quad (11)$$

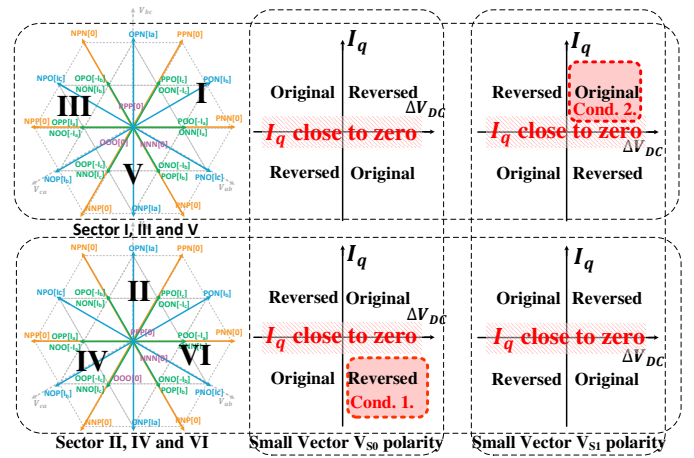
B. Small vector selection

Accurately manipulate the polarity of small vectors under high modulation index and high fundamental frequency is the key to neutral point balancing.

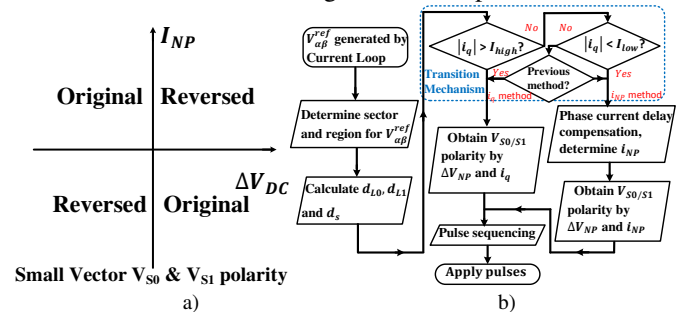
Based on the potential difference between the upper and the lower capacitors ΔV_{DC} , the q-axis current I_q , the small vectors for different sectors can be determined and are presented in Fig. 13. The potential difference ΔV_{DC} is defined as.

$$\Delta V_{DC} = V_{Cu} - V_{Cl} \quad (12)$$

Where V_{Cu} and V_{Cl} represent upper and lower capacitor voltages respectively. Among the required information, sector information and the polarity of I_q are already known in SVM duty cycle calculation and don't have to be calculated again. The only feedback required are the measurements of the capacitor voltages. Therefore, the approach can be conveniently implemented as a simple look-up table. For instance, assuming that the ESG system is generating (i.e. $I_q < 0A$), if the reference voltage vector falls inside sector II and the ΔV_{DC} term is positive (denoted as Cond. 1 in Fig. 13), the small vector V_{S0} should be selected such that the current i_{NP} is the inversed corresponding phase current (i.e. $-i_c$). Alternatively, if ESG is cranking the engine (i.e. $I_q > 0A$) and reference voltage vector falls in sector I, when the ΔV_{DC} term is positive (denoted as Cond. 2 in Fig. 13), small vector V_{S1} should be selected such that the current i_{NP} is the same as its corresponding phase current (i.e. i_c).


 Fig. 13. Small vector polarity selection – I_q method

Nevertheless, the above-mentioned method is prone to error when the ESG system is on standby mode or lightly loaded. Under these conditions, the q-axis current is very close to zero, in which case the control algorithm might generate erroneous demands under the effects of q-axis current zero-crossing. Therefore, an alternative method is required and shown in Fig. 14. a) This approach determines the polarity of the small vector based on the neutral point current i_{NP} and the imbalance of DC-link capacitor voltage ΔV_{DC} . The neutral point current i_{NP} is obtained by selecting from the corresponding phase current based on the information given in table. I. Therefore no additional sensors is required to obtain neutral point current i_{NP} . For both small vectors V_{S0} and V_{S1} , assuming its corresponding converter phase leg which connects to the neutral point has positive current flowing (phase current flows from converter to machine winding), and the ΔV_{DC} term is positive, the polarity of the small vectors should be selected such that its NP current is the inversed ones and discharge the neutral point.


 Fig. 14. Small vector polarity selection for the proposed SVM a) I_{NP} method b) Operating procedure for proposed SVM

The performance of the two presented methods are complementary. The second method is more suitable when there is active power flowing between the machine and the converter. The first method can deliver better performance when the system is operated in a standby mode and the power flowing within the starter-generator system is predominantly reactive. A simple hysteresis-based transition mechanism can thus be adopted to switch between these two schemes at different load levels. As presented in the flowchart Fig. 14. b), the proposed modulation takes the load level of the ESG system into account via q-axis current. If the absolute value of the q-axis current is below i_{low} , the I_{NP} method is used to select

small vector. If the absolute value is larger than i_{high} , the I_q method is used. The transition band is in between, and the boundary values i_{low} and i_{high} are defined based on experimental measurements.

C. Delay compensation & Pulse sequence

To compensate the high fundamental frequency induced delay issue discussed in section III.B, a simple solution is proposed in this section. The measured phase current vector i_s can be advanced by $1.5T_s$ with the fundamental frequency as in (13):

$$i_s^{adv} = i_s \cdot e^{-j \cdot 1.5\omega_o T_s} \quad (13)$$

The advanced phase current will then be used in the small vector polarity determination method described in Fig. 14. In practical implementation, the small vector polarity determination method described in Fig. 13 would not be affected as it does not need phase current information.

Pulse sequencing affects the switching loss, thus affecting the efficiency of the system. It is worth noting that with the restriction of medium usage described in section IV.A, more switching events are involved as sometimes the state of a phase leg has to commute between ‘P’ and ‘N’ state, hence taking two steps in one transition. To minimize such effect, the numbering system described in [11] is implemented (i.e. states P = 2, O=1 and N=0 and the vector number is the sum of states of three legs.). The selected vectors are applied in an ascending or descending sequence, so that the switching events within each region and the switching events between adjacent regions are minimized.

D. Difference with respect to previous methods

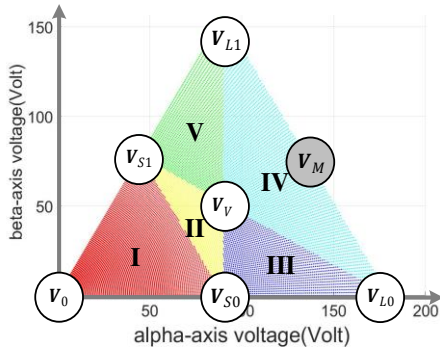


Fig. 15. NTVV-SVM

As mentioned in the introduction, a seemingly similar modulation technique namely the nearest three virtual space vector modulation (NTVV-SVM) was introduced to suppress the third harmonic voltage ripple at the DC-link neutral point. The essence of the NTVV-SVM is to suppress the usage of the medium vector V_M by replacing it with a virtual voltage space vector V_V which is shown in Fig. 15. Its formulation is given in the following equation, where d_V is the calculated virtual vector duty cycle.

$$V_V = \frac{1}{3} d_V V_{S0} + \frac{1}{3} d_V V_{S1} + \frac{1}{3} d_V V_M \quad (14)$$

Based on Table. I and Fig. 5. a), the implementation of the virtual vector V_V can be manipulated in such a way that all three

phase currents are connected to the DC-link neutral point for the same amount of time. Assuming the three phase currents stay constant in one switching period and ignoring all common-mode noises, then the following condition would apply:

$$i_{NP-V} = \frac{1}{3} i_a + \frac{1}{3} i_b + \frac{1}{3} i_c = 0 \quad (15)$$

Hence the virtual vector neutral point current i_{NP-V} is zero, and it is independent of the power factor.

The original NTVV-SVM technique aims at suppressing low frequency neutral point voltage ripple so that the size of DC-link capacitors wouldn't have to be significantly increased to allow low power factor operation. Many improved NTVV-SVM techniques and hybrid solutions have been introduced subsequently. However, for a neutral point clamped converter installed in an aircraft electric starter generator, the NTVV-SVM methods may not be entirely suitable. Illustrated in chapter. II, the ESG features high modulation index, low pulse ratio and full power factor range.

Presented in chapter. III. B, under a low pulse ratio, the assumption of three phase currents stay constant during a switching period hence (15) is no longer valid. Therefore, the use of the virtual vector neutral point current can not make the neutral point current zero and the neutral point will not be balanced.

At high modulation indices, both the NTVV-SVM and the proposed method would allocate the majority of duty cycle to large vectors. Furthermore, the use of NTVV-SVM method may result in higher number of switching at medium to high modulation index operation. The NTVV-SVM presented in [29] contains an optimized pulse pattern which reduces its number of commutations to the minimum.

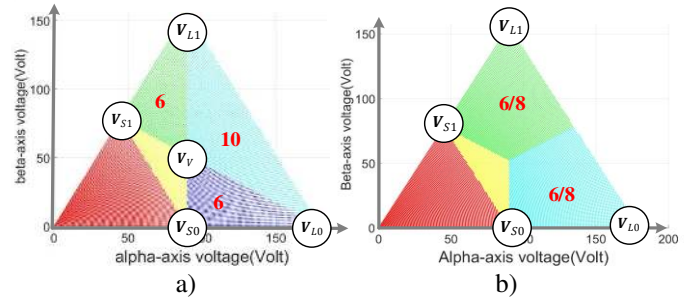


Fig. 16. Number of commutations per switching period for a) NTVV-SVM method b) the proposed method in medium to high modulation region

As the converter in the ESG operates at high modulation index for more 99% of time, the number of commutations in medium to high modulation index region for both NTVV-SVM method and the proposed method are analysed and presented in Fig.18, detailed pulse pattern is given in table. IV and table. V respectively in the appendix. Seen from Fig. 16, the optimized NTVV-SVM pulse pattern requires 6 switching actions per switching period for region III and V and 10 switching actions for region IV. The proposed method requires 6 or 8 switching actions depending on which particularly small vector is selected. Assuming the instantaneous voltage of the upper capacitor V_{Cu} is 50% of the time larger than that of lower capacitor V_{Cl} , and 50% of the lower. Weighting the number of switching actions with respect to the size of the corresponding region, the NTVV-SVM method requires 8 switching actions at

medium to high modulation index region, whereas the proposed method requires 7. Therefore, for more than 99% of ESG operation time, the NTVV-SVM requires 14.3% more commutations than the proposed method.

V. SIMULATIONS

A simulation model for the target ESG system is built within the PLECS/Simulink environment, the parameters are given in Section II. Both the conventional SVM method and the posed SVM method are evaluated. In simulation, the target ESG system initially operates in starting mode, and flux weakening operation starts at approximately 0.45s. Followed by engine ignition, the engine accelerates to 20krpm and the ESG system is switched to generating mode. The droop control takes over the DC-link voltage regulation, generating q-axis current references to the inner current controller. A 15kw resistive load is connected to the DC-link at 1.1s, resulting in a drop of the overall DC-link voltage and a step increase of negative q-axis current.

It should be emphasized that a typical engine start process takes more than 60s. In our simulation, the starting process is significantly scaled down to save simulation time and computational resource.

Denoted in Fig. 17, a large negative d-axis current is constantly required for flux weakening in generating mode. This indicates the system constantly operates at low power factor conditions with near unity modulation index. This working condition also pushes the converter into the ripple-prone region (denoted in red in Fig. 8).

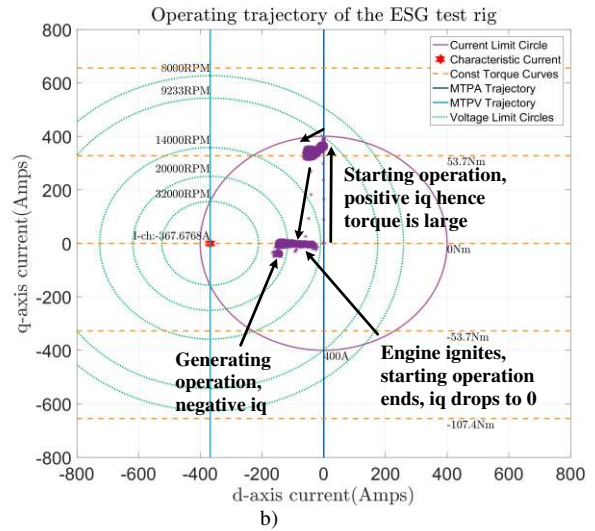
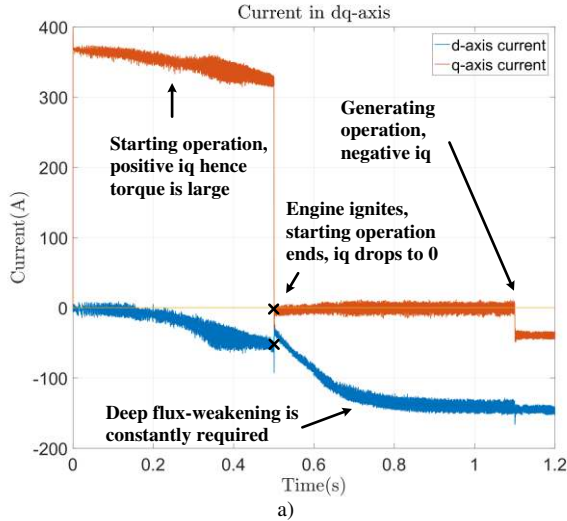


Fig. 17. Simulated ESG system dq-currents a) in a typical S/G process b) ESG system dq-currents trajectory(right)

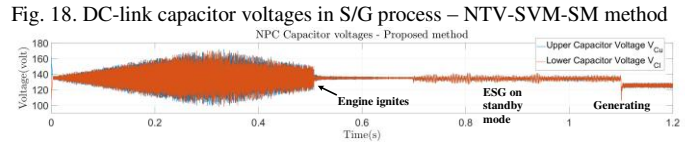
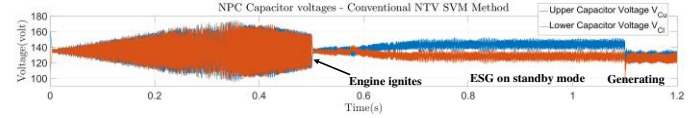


Fig. 18. DC-link capacitor voltages in S/G process – NTV-SVM-SM method

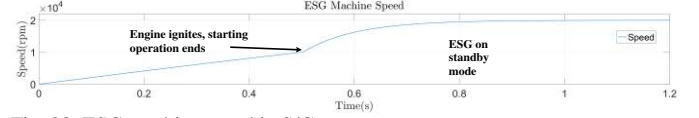


Fig. 19. DC-link capacitor voltages in S/G process – proposed method

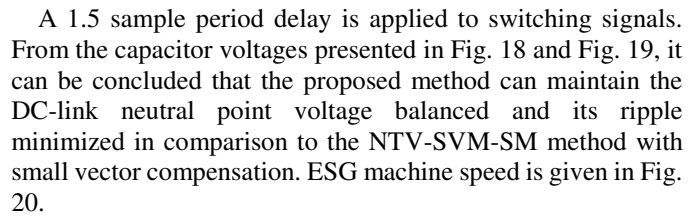


Fig. 20. ESG machine speed in S/G process

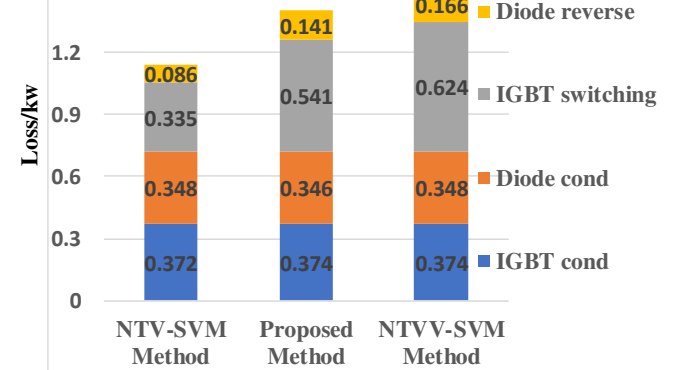


Fig. 21. Converter loss comparison when ESG is on standby mode at 20krpm

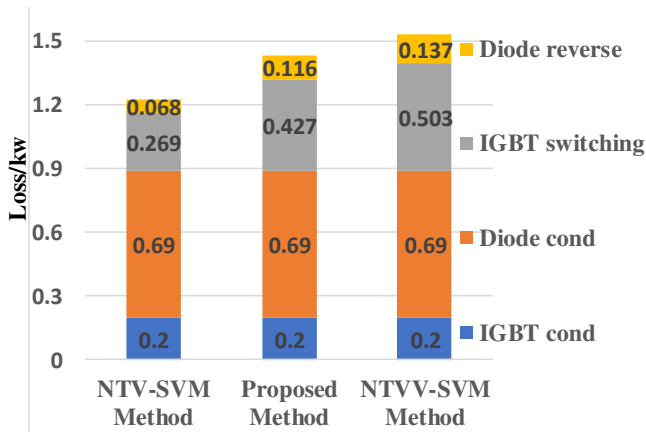


Fig. 22. Converter loss comparison when ESG is generating 30kw of active power at 20krpm

Further to the neutral point voltage balancing and ripple reduction. An accurate converter loss model is constructed within PLECS environment based on the switching characteristics of the power modules. The loss breakdown for the conventional NTV method, the proposed method and the NTVV method with optimized pulse pattern are presented in Fig. 21 and Fig. 22. When the ESG system is operating in generating mode at 20krpm of shaft speed, the converter losses for standby mode and 30kw of active power generation are presented respectively. The proposed method indeed causes a slight increase of the converter loss, but it is still lower than the seemingly similar NTVV modulation method even if the pulse pattern for NTVV method is optimized. From standby mode to generating mode, the combined converter loss tend not to vary significantly as a large reactive power is constantly flowing between the machine and the converter due to flux weakening.

VI. EXPERIMENTAL RESULTS

The proposed SVM method is verified with a 45kVA, 32krpm prototype of ESG system. The hardware structure is presented in Fig. 23. A 150kw prime mover and the homebrewed ESG machine are placed in an isolated room for safety consideration. The three-level NPC converter along with DSK6713/Actel a3p400 control platform, DC source, prime mover controller, host PC are placed outside of the high-speed room. The selected devices for the NPC converter are IGBT modules from Infineon. The prime mover emulates aircraft engine shaft, coupled with ESG machine. The NPC converter interfaces the ESG machine and the 270V DC-link. AC-side parameters are monitored by PPA5530 power analyzer.

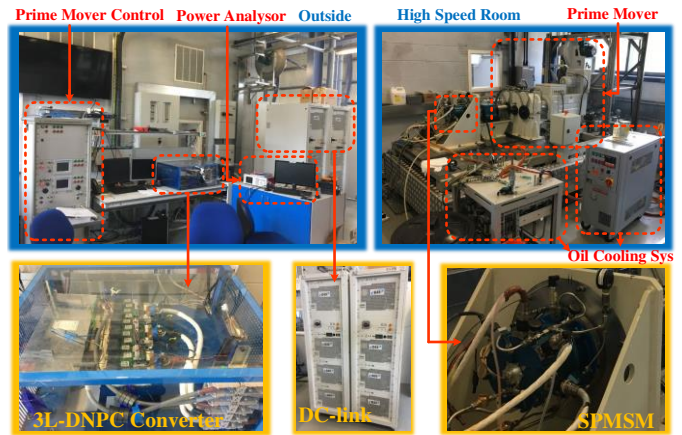


Fig. 23. ESG test rig setup

Experimental results presented in this section focus on the generation mode of the ESG system, and particularly the light load condition. This is because the neutral point balancing problem mainly occurs in such operating condition. The results when ESG system operates in starting mode are not presented as it accounts for less than 1% of the operation time and is out of the scope of this paper.

The NP balancing results for the proposed SVM method and the NTV-SVM-SM method are obtained when the ESG system is operated in generating mode at 20krpm in light load conditions. The q-axis current reference is -10A; the modulation index is above 0.9; the power factor is below 0.1. Line voltage and phase currents are presented in Fig. 24, where the distortions of phase currents originate from low machine inductance. DC-link capacitor voltages for NTV-SVM-SM method and the proposed SVM method during light load condition are given in Fig. 25. Due to limited balancing capability in such operating condition and small vector manipulation inaccuracies caused by low pulse ratio, a large continuous DC imbalance can be seen when NTV-SVM-SM method is used. Harmonic contents of NP voltage for both methods in the same condition are presented in Fig. 26, a large 3rd harmonic is observed, indicating a bigger pair of DC-link capacitors are required to absorb the ripple. Results shown the proposed SVM method maintains NP voltage balanced and ripple minimized under very low power factor (PF), near-unity modulation index (MI) and low pulse ratio.

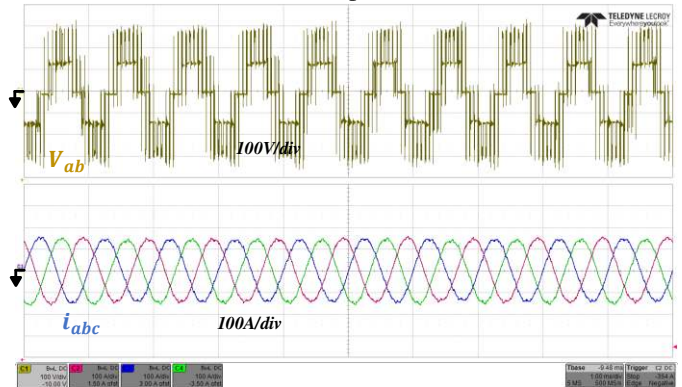


Fig. 24. Line-line voltage and phase currents for proposed SVM at light load($i_q = -1A$, Averaged MI = 0.905, Averaged PF = 0.012)

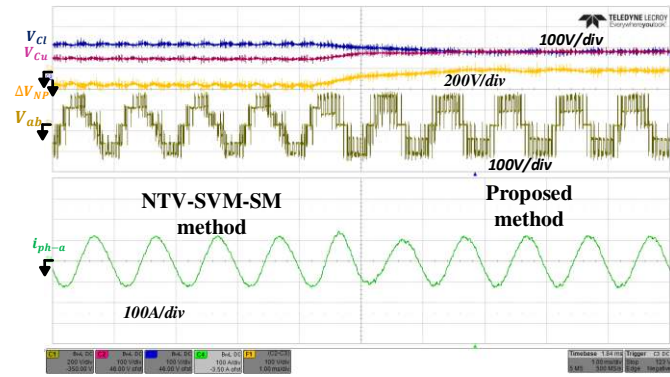


Fig. 25. Transition from NTV-SVM-SM to proposed SVM at light load ($i_q = -15A$, Averaged MI = 0.912, Averaged PF = 0.137)

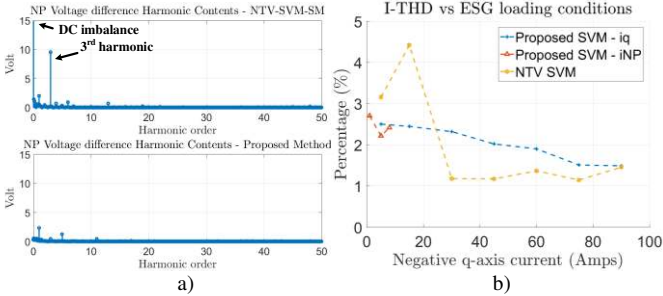


Fig. 26. Processed experimental results a) FFT of NP voltage difference for both methods b) AC-side current THD for NTV-SVM and proposed SVM

AC-side current THD is monitored by power analyzer from standby to heavy-load condition at 20krpm. The results are given in Fig. 26, proving the proposed method delivers better performance in light-load conditions.

VII. CONCLUSION

This paper presents a comprehensive study on the DC-link capacitor neutral point balancing for 3-level NPC converter in aircraft ESG systems, the conclusions are applicable to all 3-level NPC converter used in high speed drives. The operating characteristics of the ESG including bi-directional power flow, very low power factor, low pulse ratio and near unity modulation index is analyzed. Basic SVM principles for 3-level NPC converter is reviewed, and the source of neutral point ripple and imbalance under ESG operating conditions are elaborated. Further to the analysis, an alternative SVM technique is proposed, which is capable of suppressing neutral point voltage ripple and eliminate imbalance at light load condition. Two small vector polarity selection strategies are proposed so that the issues emerged due to low pulse ratio and load variation are addressed. Simulation and experimental results obtained from a ESG prototype demonstrate the proposed SVM technique delivers superior performance in terms of neutral point voltage ripple, balancing and output current THD under light load condition

APPENDIX

Table. III. Starter generator system parameters

Ld	99uH
Lq	99uH
Is-max	400A

Vdc	270V
PM flux	0.0364 Vs/rad
Pole pair	3
Base speed	8000rpm
Converter switching frequency	16kHz
Control system sampling frequency	16kHz
Fundamental frequency in generating	1~1.75kHz

Table. IV. Optimized NTVV-SVM pulse pattern in sector I in medium to high modulation index region

Region	Voltage imbalance	Pulse sequence
III	$V_{Cu} > V_{Cl}$	PNN-PON-POO-PPO-POO-PON-PNN
	$V_{Cu} < V_{Cl}$	PNN-ONN-ONN-ONN-ONN-ONN-PNN
IV	$V_{Cu} > V_{Cl}$	PNN-PPN-PPO-POO-PON-POO-PPO-PPN-PNN
	$V_{Cu} < V_{Cl}$	PPN-PNN-ONN-ONN-ONN-ONN-PNN-PPN
V	$V_{Cu} > V_{Cl}$	PPN-PPO-POO-PON-POO-PPO-PPN
	$V_{Cu} < V_{Cl}$	PPN-PON-ONN-ONN-ONN-ONN-PPN

Table. V. Pulse pattern in sector I in medium to high modulation index region for the proposed method

Region	Small vector	Pulse sequence
III	POO	PPN-PNN-POO-PNN-PPN
	ONN	PPN-PNN-ONN-PNN-PPN
IV	PPO	PNN-PPN-PPO-PPN-PNN
	ONN	PNN-PPN-ONN-PPN-PNN

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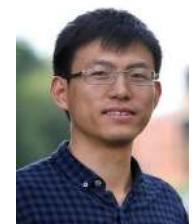
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