



A network analysis of the Chinese stock market

Wei-Qiang Huang*, Xin-Tian Zhuang, Shuang Yao

School of Business Administration, Northeastern University, Shenyang, Liaoning 110004, China

ARTICLE INFO

Article history:

Received 7 December 2008

Available online 26 March 2009

Keywords:

Stock correlation network
Stock price fluctuations
Complex network theory
Topology structure
Scale-free degree distribution
Clustering coefficient
Component
Clique
Independent set
Topological stability
Portfolio investment

ABSTRACT

In many practical important cases, a massive dataset can be represented as a very large network with certain attributes associated with its vertices and edges. Stock markets generate huge amounts of data, which can be use for constructing the network reflecting the market's behavior. In this paper, we use a threshold method to construct China's stock correlation network and then study the network's structural properties and topological stability. We conduct a statistical analysis of this network and show that it follows a power-law model. We also detect components, cliques and independent sets in this network. These analyses allows one to apply a new data mining technique of classifying financial instruments based on stock price data, which provides a deeper insight into the internal structure of the stock market. Moreover, we test the topological stability of this network and find that it displays a topological robustness against random vertex failures, but it is also fragile to intentional attacks. Such a network stability property would be also useful for portfolio investment and risk management.

© 2009 Elsevier B.V. All rights reserved.

1. Introduction

In nature, a large number of complex systems can be described by complex networks [1–3].

In the network, the vertices are elements in the system, and two vertices are connected by an edge. After the innovative researches of small-world networks by Watts and Strogatz [4] and a scale-free network by Barabasi and Albert [5], people do extensive empirical researches on topology characteristics of actual networks from different domains, such as the WWW, the Internet, the movie actor collaboration networks, cell networks and telephone networks etc. These networks have a common topology character of being small-world and scale-free [2]. Traditional network models such as regular and stochastic networks cannot embody these characters. In recent years, many network modes are established such as small-world models [4,6,7] and dynamic evolvement scale-free models [5,8,9].

In essence, the stock market is a complex system [10]. The price fluctuations among vast stocks have complicated relationships. Lately, people have investigated stock markets by establishing the corresponding stock correlation networks, of which the vertices are stocks and edges between vertices are price fluctuation relationships of stocks [11–16]. From a different angle of view, people put forward much network construction arithmetic such as the minimum-cost spanning tree(MST) [11–13], the planar maximal filtering graph (PMFG) [14,15] and the correlation threshold method [16]. The research contents include basic topology characteristics and intrinsic hierarchical structures of stock correlation networks etc. Mantegna was the first [11] to construct networks based on stock price correlations. He investigated the portfolio of the stocks used to compute the Dow Jones Industrial Average (DJIA) index and the portfolio of stocks used to compute the Standard and Poor's 500 (S& P 500) index in the time period from July 1989 to October 1995. He found a hierarchical arrangement of stocks in the stock correlation network which was built by investigating the daily time series of the logarithm of the stock price. Onnela et al. [13] constructed a network called the asset graph according to the rank of 477 stock's

* Corresponding author.

E-mail address: hwqneu@hotmail.com (W.-Q. Huang).

correlation strength in the New York stock market. They studied its properties, such as topologically different growth types, number and size of clusters and the clustering coefficient. These properties, calculated from empirical data, are compared against those of a random graph. Tumminello et al. [15] investigated the planar maximally filtered graphs of the portfolio of the 300 most capitalized stocks traded at the New York Stock Exchange during the time period 2001–2003. Topological properties such as the average length of shortest paths, the betweenness and the degree were computed on different planar maximally filtered graphs generated by sampling the returns at different time horizons. Boginski et al. [16] constructed a stock market graph by analyzing daily fluctuations of 6546 financial instruments in the US stock markets during 500 consecutive trading days in 2000–2002. They conducted the statistical analysis of this graph and detected cliques and independent sets in this graph.

The topological stability of a network against random failures and attacks is a very important research aspect of a complex network. The failures or attacks refer to removal of vertices or edges. The research results indicate that regular and random networks display comparative effects between error and attack tolerance. A small-world network is sensitive to long distance attacks [17]. Scale-free networks display a topological robustness against random node failures, but they are also fragile to intentional attacks [18]. The listed companies may have some extreme risks such as delisting or bankruptcy, to which corresponds removals of vertices in the stock correlation network. The removal of certain stocks will lead to topological changes of the holistic stock correlation network.

The study on such topological changes can help us understand correlation patterns among stocks, thus it can be a good guide for risk management of stock investment. Nowadays, a great number of different stocks are traded in the Shanghai and Shenzhen stock market in China. According to trading data of these stocks, we construct a corresponding stock correlation network with a correlation threshold method. We present a detailed study of the properties of this network, including the topology structures and topological stability against random failures and attacks. Different from other network construction arithmetic, the correlation threshold method is convenient for studying inherent relationships between network characteristics and correlation threshold. The rest of this article is organized as follows. In Section 2 we describe the process of network construction and topology statistical quantities of the network. Section 3 is the empirical study and results. In the last section we present a few conclusions.

2. Construction and structure of the stock correlation network

2.1. Constructing the network

Let $P_i(\tau)$ be the stock-price of a company $i (i = 1, \dots, N)$ at time τ . Then the return of the stock-price at a time interval Δt is defined as

$$r_i(\tau) = \ln P_i(\tau) - \ln P_i(\tau - \Delta t) \tag{1}$$

meaning the geometrical change of $P_i(\tau)$ during the interval Δt . We take Δt as one day in the following analysis throughout this paper. The cross-correlations between individual stocks are considered in terms of the matrix \mathbf{C} , whose elements are given by using the following formula

$$c_{i,j} \equiv \frac{\langle r_i r_j \rangle - \langle r_i \rangle \langle r_j \rangle}{\sqrt{(\langle r_i^2 \rangle - \langle r_i \rangle^2)(\langle r_j^2 \rangle - \langle r_j \rangle^2)}} \tag{2}$$

where the brackets mean a temporal average over the period we studied. Then $c_{i,j}$ can vary between $[-1, 1]$. The case of $c_{i,j} = 1(-1)$ means that two companies i and j are completely correlated (anti-correlated), while $c_{i,j} = 0$ means that they are uncorrelated.

The main idea of constructing the stock correlation network is as follows. Let the set of stocks represent the set of vertices of the network. Also, we specify a certain threshold value $\theta, -1 \leq \theta \leq 1$ and add an undirected edge connecting the vertices i and j if the correlation coefficient $c_{i,j}$ is great than or equal to θ . Obviously, different values of θ define the networks with the same set of vertices, but different sets of edges.

Let graph $G = (V, E)$ represent the stock correlation network, where V and E are the set of vertices edges respectively. E is defined as

$$E = \begin{cases} e_{ij} = 1, & i \neq j \text{ and } c_{ij} \geq \theta \\ e_{ij} = 0, & i = j. \end{cases} \tag{3}$$

2.2. Topology structure of the network

2.2.1. Degree distribution

The degree of vertex i is $k_i = \sum_{j \neq i} e_{ij}$ which denotes the vertex number connecting with i . The vertex degree distribution function P_k tells us the probability that a randomly selected vertex is connected with k edges. The results of many empirical studies on actual networks demonstrate that the vertex degree distribution obeys a power law [2]

$$P_k \propto k^{-\gamma} \tag{4}$$

متن کامل مقاله

دریافت فوری ←

ISIArticles

مرجع مقالات تخصصی ایران

- ✓ امکان دانلود نسخه تمام متن مقالات انگلیسی
- ✓ امکان دانلود نسخه ترجمه شده مقالات
- ✓ پذیرش سفارش ترجمه تخصصی
- ✓ امکان جستجو در آرشیو جامعی از صدها موضوع و هزاران مقاله
- ✓ امکان دانلود رایگان ۲ صفحه اول هر مقاله
- ✓ امکان پرداخت اینترنتی با کلیه کارت های عضو شتاب
- ✓ دانلود فوری مقاله پس از پرداخت آنلاین
- ✓ پشتیبانی کامل خرید با بهره مندی از سیستم هوشمند رهگیری سفارشات