

A new method of enhancing reliability for transmission expansion planning



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Abstract The reliability plays a significant role in power systems and it is an important objective or constraint in transmission expansion planning. Firstly, a DC optimization model was proposed to calculate the maximum arrival power at each load point. Compared to the network flow method, DC model is closer to the actual power flow and it is able to obtain more realistic reliability assessment results. Furthermore, a novel sensitivity index (SI) was also proposed to choose the most effective line so as to enhance the nodal and/or system reliability. The Monte Carlo simulation is used to simulate the system components state. This improved reliability evaluation method and SI can be used for transmission expansion planning or maintenance scheduling. Tests are performed using 6-bus system derived from the Garver's system and the IEEE 10-machine 39-bus system. The results show the effectiveness of the method.

Keywords Probabilistic reliability evaluation, Sensitivity analysis, Monte Carlo simulation, DC model

1 Introduction

Transmission system plays a significant role in electric power system. It is not only a linkage between the generation

and distribution, but also provides a non-discriminative and reliable environment for demanders and suppliers [1]. With the growth of load demand, the generation expansion planning (GEP) and transmission expansion planning (TEP) become more and more important. The main objective of TEP is to develop the system as economically as possible [2] due to the load growth, and it is subject to a set of economic, technical and reliability constraints [1, 3]. In the regulated market, GEP and TEP are sub-tasks of a power system planning process performed by a regulated power utility. However, in the deregulated market environment, TEP is usually performed separately by transmission network service providers, while GEP becomes the task of generation companies or investors [4]. In the conventional monopolistic market, the power utilities have the social obligations to provide a reliable electricity supply. In a competitive market, the reliability of service is one of the important factors for market competitiveness [5, 6]. Therefore, a reliability level is an important constraint for TEP process. In addition, at the time of preparation for maintenance scheduling, a certain level of supplying reliability must be guaranteed after some power system components which are in outage and maintenance state [7, 8]. Thus, reliability evaluation and reinforcement are very meaningful works both in the power system planning or maintenance scheduling.

Generally, power system reliability includes two aspects: adequacy and security. Adequacy measures the generation and transmission capacities of the system under static conditions, without considering system disturbances [3]. In this paper, the reliability means adequacy. It is not only restricted by the capacities of the generators and transmission lines, but also subjected to the availabilities of them. The reliability analysis is carried out before stability and fault analyses in conventional TEP [9]. Thus, reliability evaluation should be incorporated in TEP. Otherwise there is no guarantee to have a trustworthy supply for demands [3].

CrossCheck date: 13 November 2014

Received: 29 August 2014 / Accepted: 13 November 2014 / Published online: 12 December 2014

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Generally, TEP problem can be formulated as an optimization problem. Reliability is generally treated as a constraint [10] or a part of objective function to deal with [11]. The common reliability of the system is often assumed to be guaranteed via the demand constraints. That is, these constraints enforce that line capacities exceed the line loads based on an assumed demand profile [12]. In [11], the probabilistic load curtailment loss was handled as a part of objective function and a TEP approach considering the load and wind power generation uncertainties was proposed. The different reliability indices such as loss of load expectation (LOLE) [13], loss of load probability (LOLP) [14], hierarchical reliability assessment [15], loss of load cost (LOLC) [16] and expected energy not supplied (EENS) [17] have been used to investigate TEP. Among them, LOLE and EENS are two common reliability indices and they are easily obtained from the load duration curve (LDC). An extended effective load model, considering the capacities and uncertainties of generators and transmission lines, has been proposed [5, 6]. Then an extended nodal ELDC based on this extended effective load model can be obtained. Thus, the indices LOLE and EENS can be calculated.

Through reliability evaluation, if the system reliability indices do not satisfy the prescribed criteria, there is a reasonable question: where to add a transmission line is the most effective to improve the reliability indices. In [14], a method was developed for analyzing the reliability of composite power systems under the constraints of emissions. Some reliability indices are expressed by the function of the relevant factors such as the element forced outage rates (FOR) and the element capacities. Then their sensitivity with respect to various relevant factors are obtained by calculating the partial derivative of the reliability indices [14, 18–20]. A sensitivity index (SI) based constructive heuristic algorithm (CHA) has been applied for TEP [21, 22]. At each step of CHA, a component (circuit) of the feasible solutions must be added to the system. The choice of this component is determined by SI. The SI is based on the greatest active power flow of circuits, which is obtained from the solution to relaxing the integrality of DC investment model [21]. As an improvement, SI comes from the greatest apparent power flow of circuits, which is obtained from the solution to relaxing the integrality of AC investment model [22].

Following the previous work, this paper proposed a method to evaluate the composite power system reliability considering the FOR of the generators as well as the transmission lines. The Monte Carlo method is used to simulate the random behavior of the availability of the system components (generator or branch). A DC power flow model, instead of the network flow method [5, 6], is used to obtain more accurate maximum arrival power at load point. With

the reliability evaluation process, an implicit sensitivity index based optimization method can be obtained, which can help to choose the most effective component so as to improve the system or bus reliability.

There are two main contributions of this paper. One is that the DC model optimization was used to improve the accuracy of maximum arrival power at each load point. The other one is that a novel SI based optimization method was presented to choose the most effective line so as to enhance the reliability.

The remainder of this paper is organized as follows. A DC model based reliability evaluation model of composite power system is presented in Section 2. Section 3 proposes the process of obtaining the ELDC using the Monte Carlo simulation and provides a sensitivity analysis index. Case studies are presented in Section 4. Finally, the paper is concluded in Section 5.

2 Reliability evaluation model of composite power system

The traditional ELDC considers only the FOR of the units, without the FOR of the transmission lines [5]. Firstly, a composite ELDC and the reliability indices LOLE and EENS [5, 6] are briefly introduced. Then, an optimization model of obtaining minimum outage power (i.e. maximum arrival power) at load point is presented, which is a DC constraint model.

2.1 Model of reliability evaluation in composite power system

The reliability indices, such as LOLE and EENS, can be assessed using a composite ELDC (CMELDC) based on the effective load model at the load point [5, 6]. When a load point curtails a certain amount of load due to outages of generator unit and/or transmission line, it is equivalent to the case because the same amount of probabilistic loads is added to the load point but no components outage [5, 6, 23]. Base on this concept, the effective inverted load duration curve can be obtained at load point k .

$$\Phi_i^k(x_e) = \Phi_{i-1}^k(x_e) \otimes f_{oi}^k(x_{oi}) = \int \Phi_{i-1}^k(x_e - x_{oi}) f_{oi}^k(x_{oi}) dx_{oi} \quad (1)$$

where \otimes is the operator, indicating the convolution integral; k is the load point number; x_e is the random variable of the effective load; x_{oi} is the random variable of the probabilistic load caused by the forced outage of component i ; $\Phi_i^k(x_e)$ is the effective inverted load duration curve caused by the forced outage of components 1 to i at load

point k ; $\Phi_{i-1}^k(x_e)$ is the effective inverted load duration curve caused by the forced outage of components 1 to $i - 1$ at load point k ; $f_{oi}^k(x_{oi})$ is the probability density function (PDF) of the outage capacities caused by the forced outage of component i at load point k .

From (1), it is important to note that $\Phi_i^k(x_e)$ is calculated by iterative manner. If the total probability density function of the outage capacities caused by the forced outage of components 1 to i at load point k is determined, $\Phi_i^k(x_e)$ can be obtained by (2).

$$\Phi_i^k(x_e) = \Phi_0^k(x_e) \otimes f_{osi}^k(x_{osi}) = \int \Phi_0^k(x_e - x_{osi}) f_{osi}^k(x_{osi}) dx_{osi} \tag{2}$$

where x_{osi} is the random variable of the synthesized fictitious probabilistic load caused by the forced outage of components 1 to i ; $\Phi_0^k(x_e)$ is the original inverted load duration curve at load point k ; $f_{osi}^k(x_{osi})$ is the total probability density function of the outage capacities caused by the forced outage of components 1 to i at load point k .

After obtaining the effective inverted load duration curve at load point, the reliability indices $LOLE_k$ and $EENS_k$ can be calculated at load point k .

$$LOLE_k = \Phi_{NE}^k(x) | x = AP_k \tag{3}$$

$$EENS_k = \int_{AP_k}^{AP_k + L_{Pk}} \Phi_{NE}^k(x) dx \tag{4}$$

where NE is the number of total elements (including generating units, transformer and transmission lines); AP_k is the maximum arrival power at load point k ; L_{Pk} is the peak load at load point k .

The EENS of the entire system is equal to the summation of $EENS_k$ at all load points, as shown in (5). However, the approach of calculating LOLE is completely different from the EENS. The expected load curtailed (ELC) at the load point k must be calculated. Then, the ELC of the entire system can be obtained. Thus, the entire system LOLE index can be calculated.

$$EENS = \sum_{k=1}^{ND} EENS_k \tag{5}$$

$$ELC_k = EENS_k / LOLE_k \tag{6}$$

$$ELC = \sum_{k=1}^{ND} ELC_k \tag{7}$$

$$LOLE = EENS / ELC \tag{8}$$

where ND represents the number of load demand points.

2.2 Minimum outage power using DC model

To obtain the probability density function of the outage capacities caused by the forced outage of components, the load point outage power must be calculated first of all. There are several possible solutions when calculating the load point outage power for each component state. This problem can be formulated as an optimization model. The objective function for minimum outage power can be set up and an optimal solution can be obtained by the network flow method [5]. The network flow method takes into account Kirchhoff's current law (KCL) [24] at all nodes but neglecting Kirchhoff's voltage law (KVL) [25]. Thus, its accuracy is low. In this paper, transmission network is characterized by a simplified lossless DC load flow model. It not only satisfies KCL but also obeys Ohm's law. Thus, KVL is implicitly taken into account. Therefore, DC load flow model is more close to the actual situation and can improve the accuracy.

To minimize the outage power at load point, the mathematical model used to minimize the outage power at load point can be formulated as follows.

$$\sum_{i=1}^{ND} (L_{pi} - P_{Li}) / L_{pi} \tag{9.1}$$

where L_{pi} is the peak load at bus i ; P_{Li} is the decision variable meaning effective supplied power at bus i (therefore, they represent the arrival power at load point i).

Subject to

- 1) Power balance constraint at each node

$$P_{Gi} - P_{Li} = \sum_{j=1}^n P_{ij} \tag{9.2}$$

where P_{Gi} is the generation capacity at bus i ; P_{ij} is the power flow between bus i and j ; n is the number of transmission lines connected to bus i .

- 2) Constraint of line power

$$P_{ij} = b_{ij}(\theta_i - \theta_j) \tag{9.3}$$

where b_{ij} is the susceptance of the transmission lines between bus i and j ; θ_i is the phase angle at bus i .

- 3) Limitation constraint of peak load

$$0 \leq P_{Li} \leq L_{Pi} \tag{9.4}$$

- 4) Limitation constraint of generation capacity

$$0 \leq P_{Gi} \leq P_{Gi}^{\max} \tag{9.5}$$

where P_{Gi}^{\max} is the maximum capacity of generation at bus i .

- 5) Limitation constraint of transmission capacity

$$-P_{ij}^{\max} \leq P_{ij} \leq P_{ij}^{\max} \tag{9.6}$$



where P_{ij}^{\max} is the maximum transmission capacity between bus i and j .

3 Probabilistic reliability evaluation and sensitivity analysis

3.1 State probability calculation

There are two fundamental methods for probabilistic reliability evaluation: state enumeration and Monte Carlo simulation [2, 26]. Generally, if the outage probabilities of most of the components are very small (i.e. the system is reliable) or the number of components is very small, state enumeration method is usually more efficient. When the complex operating conditions are concerned or outage probabilities of most of the components cannot be ignored, it is almost impossible to enumerate all the system states. Thus, Monte Carlo simulation is an effective alternative to obtain all the approximate system states.

Monte Carlo simulation method treats the problem as a series of experiments. Generally, generator states are modeled using multiple state random variables. In this paper, for simplicity, the generating units are taken into account and their states are modeled using two-state (up and down) random variables as well as transmission circuit states. It is assumed that component outages are mutually independent events. Therefore, transmission line and generating unit outages are simulated by separate random numbers.

In a planning context, the probability is a measure of the likelihood that the power system will be in a given situation at a random time in the future, and it is also a function of the availability of every piece of equipment in the power system. This relationship can be represented as follows [27].

$$PRO = \prod_{i \in \mathbf{U}} u(c_i) \prod_{j \in \mathbf{A}} a(c_j) = \underbrace{u(c_1)u(c_2) \dots u(c_n)}_{\text{Unavailable}} \underbrace{a(c_1)a(c_2) \dots a(c_m)}_{\text{Available}} \quad (10)$$

where \mathbf{U} is the set of unavailable components; \mathbf{A} is the set of available components.

Forced outage rate (FOR) of power system elements can be obtained through the historical data statistical method. Suppose that there are NE elements including such as generation units, transmission lines, transformers. The random number generation method can generate a series of random numbers $y_i (i = 1, 2, \dots, NE)$ distributed uniformly under $\{0, 1\}$. s_i is the state of component i and FOR_i is its forced outage rate. s_i is expressed as (11).

$$s_i = \begin{cases} 0 & (\text{normal state, } y_i > FOR_i) \\ 1 & (\text{abnormal state, } 0 \leq y_i \leq FOR_i) \end{cases} \quad (11)$$

The state of all components can be formulated by a vector \mathbf{S} as (12).

$$\mathbf{S} = [s_1, s_2, \dots, s_i, \dots, s_{NE}] \quad (12)$$

The probability of component i appearing the state s_i can be expressed as follows.

$$PRO(s_i) = s_i FOR_i + (1 - s_i)(1 - FOR_i) \quad (13)$$

According to (10), the probability of the state vector \mathbf{S} , $PRO(\mathbf{S})$, is calculated as (14).

$$PRO(\mathbf{S}) = \prod_{i=1}^{NE} P(s_i) \quad (14)$$

It is assumed that the system states are sampled N times. If N is large enough, the state combinations of all the system components can be sampled. The component state vector \mathbf{S} may be the same in the N times samples. After removing duplicate state \mathbf{S} , a state set $U(\mathbf{S})$ of all the system components and the corresponding probability values can be obtained.

3.2 Sensitivity index

The reliability indices are not only associated with the capacity of each component, but also related to the FOR. The sensitivity index (SI) based DC model [21] or AC model [22] does not consider the FOR of the component. The indices LOLE and EENS are strongly associated with the arrival power at load point. Therefore, based on the Monte Carlo simulation and the optimization model shown as (9), an implicit sensitivity index is presented.

Generally, at the initial stage of planning, human knowledge is needed to ensure rationality of the candidate line selection with practical engineering and management concerns [28]. The main focus of this paper is on the reliability evaluation and its sensitivity analysis. Therefore, it is assumed that the feasible candidate pool of transmission lines has been obtained properly. Assuming the candidate pool is expressed as follows.

$$\mathbf{X} = \{x_1, x_2, \dots, x_{NC}\} \quad (15)$$

where NC is the number of candidate transmission lines.

The state of all components can be expressed as a vector \mathbf{S} , and its corresponding probability can be calculated, shown as (12) and (14), respectively. Under the state \mathbf{S} , the arrival power vector $\mathbf{AP}_k (k = 1, 2, \dots, ND)$ at each load point can be obtained using the model (9) first of all. Next, assuming that one candidate line $x_i (i = 1, 2, \dots, NC)$ is added to the power grid and then the corresponding arrival power vector \mathbf{AP}_k^i at each load point can be obtained using

the model (9) again. Thus, the incremental vector of the arrival power at each load point, caused by adding the line x_i , can be easily calculated as (16).

$$\Delta AP_k^i = AP_k^i - AP_k \tag{16}$$

Due to the fact that the different system state has different probability, the above ΔAP_k^i should be taken into account with its system state probability. The incremental of the arrival power under the state probability, denoted as ΔP_k^i , can be expressed as (17).

$$\Delta P_k^i = PRO(S)\Delta AP_k^i \tag{17}$$

Next, each of candidate lines is in turn added to the grid to get the corresponding incremental vector of the arrival power under the state probability. Then, the incremental arrival power matrix ΔP under the current system state due to adding each of candidate lines to the grid is shown in (18).

$$\Delta P = \begin{bmatrix} \Delta P_k^1 \\ \vdots \\ \Delta P_k^{NC} \end{bmatrix} = \begin{bmatrix} \Delta P_1^1 & \cdots & \Delta P_{ND}^1 \\ \vdots & \vdots & \vdots \\ \Delta P_1^{NC} & \cdots & \Delta P_{ND}^{NC} \end{bmatrix} \tag{18}$$

For each state in the state set $U(S)$, the above calculating process of obtaining ΔP is repeated. Every time, the obtained incremental arrival power matrix ΔP is accumulated.

Finally, the sensitivity index for the entire system and for load point k can be calculated using (19) and (20), respectively.

$$SI_{sys} = \max \left\{ SI_{x_i} = \sum_{k=1}^{ND} \Delta P_k^i, (i = 1, 2, \dots, NC) \right\} \tag{19}$$

$$SI_{Bus}^k = \max \left\{ SI_{x_i}^k = \Delta P_k^i, (i = 1, 2, \dots, NC) \right\} (k = 1, 2, \dots, ND) \tag{20}$$

3.3 The main procedure of reliability evaluation

As discussed above, reliability evaluation starts with Monte Carlo simulation to obtain the system components state set $U(S)$. Then, for a state S , the arrival power at each load point can be obtained using the DC constraint optimization algorithm. At the same time, the incremental arrival power matrix ΔP due to in turn adding one candidate line into grid can be gained too. Next, this calculating procedure is repeated until each state in state set $U(S)$ has been dealt with. Then, the probability density function of the outage power at each load point and the accumulated matrix ΔP are obtained. Thus, the effective LDC at each load point can be achieved by calculating the convolution of the original inverted duration curve at load point and the pdf of the outage

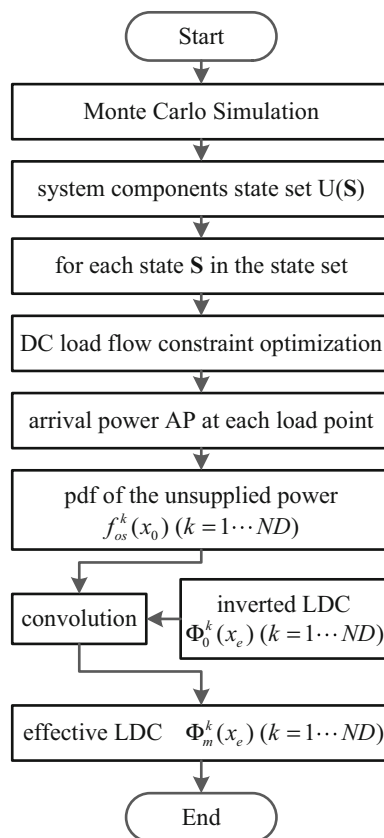


Fig. 1 Main procedure of obtaining the effective LDC

capacities. The main procedure of obtaining the effective LDC is shown in Fig. 1.

Next, the load bus reliability indices can be calculated according to (3) and (4), and the system reliability indices can be calculated according to (5)-(8). Moreover, the system and bus reliability indices can be augmented by adding the grid each time a line which is based on rules (19) and (20), respectively.

4 Case studies

The proposed method is tested on Garver’s 6-bus system and IEEE 39-bus model system. The algorithm was implemented in Matlab 8.2, using a PC with Core i7-4770 CPU clocking at 3.4 GHz and 32 GB of RAM. The DC constraint optimization is solved using the YAMIP environment [29]. In the two cases, it is assumed that the inverted LDC of load point is a polyline, shown as in Fig. 2.

4.1 Garver’s 6-bus system

This system has 6 buses and a demand of 760 MW [24]. The line data in [24] are remained unchanged. The load



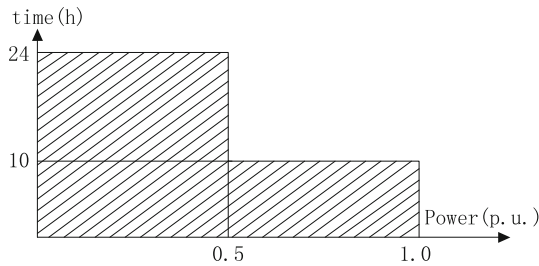


Fig. 2 Inverted load duration curve at load point

Table 1 Load and generation data for 6-bus system

Bus number	Load (MW)	Units (MW)
1	80	50
2	245	0
3	40	3 × 85
4	160	0
5	235	0
6	0	7 × 100

data and generator data are provided in Table 1. The generator is expressed using units due to the request for considering the FOR of the components. To exclude the impact on the reliability due to generator outage, the generator capacities are expanded.

The current system structure is shown in Fig. 3. For simplicity, FORs of all transmission lines and generating units are set to 0.5% and 1%, respectively.

Monte Carlo simulation method is used for state simulation. The reliability indices at the load points are evaluated using the proposed method and the results are shown in Table 2. Thus, the system reliability indices EENS and LOLE are calculated by (5) and (8), respectively. The system reliability indices are shown in Table 2 at last row.

Suppose that the candidate pool of transmission lines consists of the current transmission corridors, which have 8 right-of-way lines, shown in Table 3.

The incremental arrival power matrix ΔP by adding each candidate line is as follows.

$$\Delta P = \begin{bmatrix} 0 & -1.3212 & 0 & 0.6705 & 42.3723 \\ 0 & 2.3933 & 0 & -7.2632 & -7.3073 \\ 0 & 0.0351 & 0 & -2.3649 & 33.1669 \\ 0 & -0.9488 & 0 & -1.5299 & -25.3088 \\ 0 & 0.0457 & 0 & 13.6963 & 4.6497 \\ 0 & 3.1280 & 0 & 13.9975 & 1.7246 \\ 0 & -0.5101 & 0 & -3.8953 & 113.4931 \\ 0 & 1.6323 & 0 & 48.5670 & 38.5338 \end{bmatrix} \quad (21)$$

According to Table 2, the load point with the maximum EENS and LOLE is the bus 5. From (21), it can be found that the bus sensitivity index at bus 5 is $SI_{Bus}^5 =$

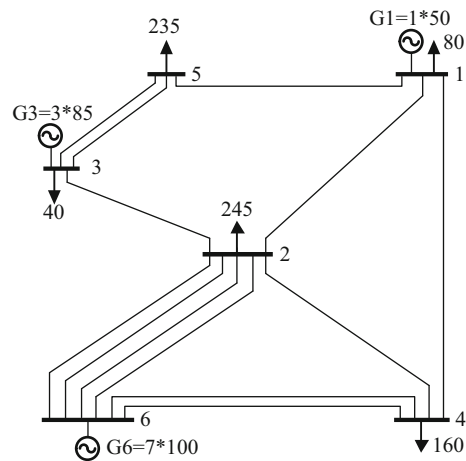


Fig. 3 The 6-bus system derived from the Garver's system

Table 2 Reliability indices of the base case

Load bus number	EENS (MWh/year)	LOLE (h/year)	ELC (MW/year)
1	0	0	0
2	120.7	2.5827	46.73
3	0	0	0
4	1777.1	38.72	45.90
5	4243.6	143.91	29.49
System	6141.4	50.29	122.12

$(SI)_{x7}^5 = 113.4931$, and the corresponding candidate line is line 7 (line₃₋₅). The system sensitivity index is $SI_{sys} = SI_{x7} = 109.1877$ and the corresponding candidate line is also line 7.

The line 7 (line₃₋₅) is added to the grid and the reliability indices are evaluated again using the proposed method. The evaluation results are shown in Table 4.

From Table 4, it can be seen that the reliability indices of system and bus 5 have been greatly improved, after adding line₃₋₅ to the grid.

4.2 39-bus system

In this case, the proposed method is tested on New-England 10-machine 39-bus system, shown as in Fig. 4. The system data, shown in Table 5 and Table 6, are taken from the open source software Matpower 4.1 [30]. In Table 5, NL represents the number of Line; FB and TB are from and to buses of the line, respectively; and X stands for the reactance of the line.

After Monte Carlo simulation sampling times of 10^5 , the load point ELDCs are obtained and the reliability indices are followed to be evaluated. For simplicity, the zero results are ignored and non-zero parts are shown in

Table 3 Candidate pool of transmission lines

Line number	From bus	To bus	Line number	From bus	To bus
1	1	2	5	2	4
2	1	4	6	2	6
3	1	5	7	3	5
4	2	3	8	4	6

Table 4 Reliability indices after adding line₃₋₅ to the grid

Load busnumber	EENS (MWh/year)	LOLE (hours/year)	ELC (MW/year)
1	0	0	0
2	139.3	3.28	42.51
3	0	0	0
4	1917.7	36.07	53.17
5	87.6	3.80	23.04
System	2147.6	18.06	118.73

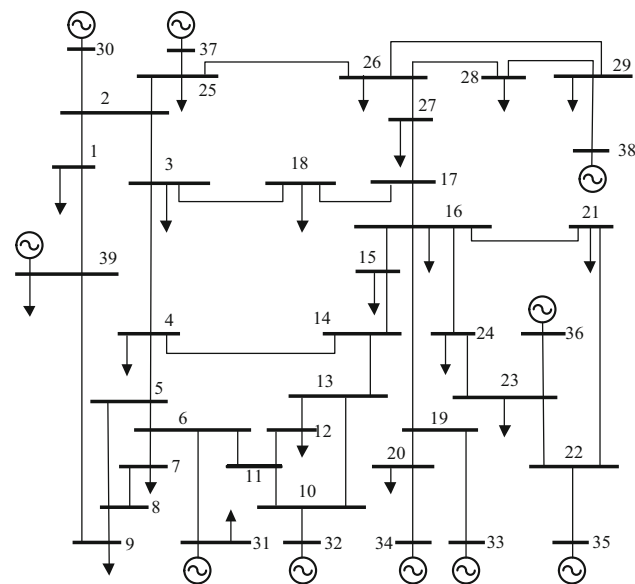


Fig. 4 The New-England 10-machine 39-bus system

Table 7. The corresponding sensitivity indices are calculated and shown in the last column of Table 7.

From Table 7, it can be seen that bus 39 has the maximum EENS and adding the line 1 (from bus 1 to bus 2) is the most effective for increasing the reliability of bus 39. However, adding the line 3 (from bus 2 to bus 3) is the most effective measures for increasing the system reliability. After adding the line 1, we can get the new reliability indices results, shown as in Table 8.

Table 5 Branch data for 39-bus system

NL	FB	TB	X (p.u.)	Pmax (MW)	NL	FB	TB	X (p.u.)	Pmax (MW)
1	1	2	0.0411	600	24	14	15	0.0217	600
2	1	39	0.0250	1000	25	15	16	0.0094	600
3	2	3	0.0151	500	26	16	17	0.0089	600
4	2	25	0.0086	500	27	16	19	0.0195	600
5	2	30	0.0181	900	28	16	21	0.0135	600
6	3	4	0.0213	500	29	16	24	0.0059	600
7	3	18	0.0133	500	30	17	18	0.0082	600
8	4	5	0.0128	600	31	17	27	0.0173	600
9	4	14	0.0129	500	32	19	20	0.0138	900
10	5	6	0.0026	1200	33	19	33	0.0142	900
11	5	8	0.0112	900	34	20	34	0.0180	900
12	6	7	0.0092	900	35	21	22	0.0140	900
13	6	11	0.0082	480	36	22	23	0.0096	600
14	6	31	0.0250	1800	37	22	35	0.0143	900
15	7	8	0.0046	900	38	23	24	0.0350	600
16	8	9	0.0363	900	39	23	36	0.0272	900
17	9	39	0.0250	900	40	25	26	0.0323	600
18	10	11	0.0043	600	41	25	37	0.0232	900
19	10	13	0.0043	600	42	26	27	0.0147	600
20	10	32	0.0200	900	43	26	28	0.0474	600
21	11	12	0.0435	500	44	26	29	0.0625	600
22	12	13	0.0435	500	45	28	29	0.0151	600
23	13	14	0.0101	600	46	29	38	0.0156	1200

Table 6 Load and generation data for 39-bus system

Bus number	Load (MW)	Generation (MW)	Bus number	Load (MW)	Generation (MW)
1	97.6	0	21	274	0
2	0	0	22	0	0
3	322	0	23	247.5	0
4	500	0	24	308.6	0
5	0	0	25	224	0
6	0	0	26	139	0
7	233.8	0	27	281	0
8	522	0	28	206	0
9	6.5	0	29	283.5	0
10	0	0	30	0	1040
11	0	0	31	9.2	646
12	8.53	0	32	0	725
13	0	0	33	0	652
14	0	0	34	0	508
15	320	0	35	0	687
16	329	0	36	0	580
17	0	0	37	0	564
18	158	0	38	0	865
19	0	0	39	1104	1100
20	680	0			



Table 7 Reliability indices and SI of the 39-bus system (non-zero parts)

Load bus number	EENS (MWh/year)	LOLE (h/year)	ELC (MW/year)	SI
4	809.8	6.60	122.59	0.1806(line ₃)
8	73.5	0.74	98.84	0.0158(line ₃)
18	17.8	0.16	111.92	0.0029(line ₇)
20	27096.9	235.71	114.96	6.2797(line ₃)
25	86.1	0.96	89.45	0.0170(line ₄)
27	1.7	0.07	26.00	0.0050(line ₃₁)
29	31.7	0.16	199.79	0.0051(line ₄₆)
31	2.1	0.32	6.52	0.0030(line ₁₄)
39	47209.7	171.16	275.82	10.7070(line ₁)
System	75329.3	72.02	1045.89	15.6973(line ₃)

Table 8 Reliability indices and SI of the 39-bus system, after adding line₁ (non-zero parts)

Load bus number	EENS (MWh/year)	LOLE (h/year)	ELC (MW/year)	SI
4	7302.6	93.73	77.91	0.1806(line ₃)
8	6976.3	43.72	159.58	0.0158(line ₃)
18	17.7	0.16	111.92	0.0029(line ₇)
20	23806.7	193.88	122.79	6.2797(line ₃)
25	99.5	1.12	89.17	0.0170(line ₄)
27	6.9	0.26	26.00	0.0050(line ₃₁)
29	128.9	0.70	183.41	0.0051(line ₄₆)
39	12550.1	34.69	361.79	10.7070(line ₁)
System	50888.7	44.93	1132.57	15.6973(line ₃)

Comparing Table 8 with Table 7, it is interesting to note that adding line 1 greatly improves the reliability at the bus 39 and thus increases the system reliability, as well as decrease the reliability at some other buses (such as bus 4 and 8). The reason is that adding the line changes the system structure and then changes the power flow.

5 Conclusion

This paper addresses the reliability evaluation problem considering the forced outage rates of generators and transmission lines. Based on the works in [5, 6], the DC power flow model are used to obtain more accurate maximum arrival power for more accurate reliability indices. The system components states are simulated using Monte Carlo technique first of all. Next, the probability density functions of the outage capacities at load buses are obtained through calculating the maximum arrival power

using DC model based optimization under all possible system states. Then, the effective load duration curves at every load bus are obtained and the reliability indices can be calculated. With the reliability evaluation process, the implicit sensitivity indices of the reliability can be obtained, which help to choose the most effective component to improve the reliability of the system or a load bus. The work is an important step in preparing a transmission expansion plan or maintenance scheduling employing probabilistic reliability evaluation methods to ensure the reliability of the electric power grid.

Acknowledgments This work is supported by China Scholarship Council, as well as Young Teacher Scientific Research Foundation of Sichuan University (No. 2012SCU11003).

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