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A NEW ROBUST LOW-SCATTER X-RAY MASS INDICATOR FOR CLUSTERS OF GALAXIES

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ABSTRACT

We present a comparison of X-ray proxies for the total cluster mass, M_{500} , including the spectral temperature (T_X) , gas mass measured within r_{500} ($M_{g,500}$), and the new proxy, Y_X , which is a simple product of T_X and $M_{g,500}$ and is related to the total thermal energy of the ICM. We use mock *Chandra* images constructed for a sample of clusters simulated with the Eulerian *N*-body+gasdynamics adaptive mesh refinement ART code in the concordance Λ CDM cosmology. The simulations achieve high spatial and mass resolution and include radiative cooling, star formation, and other processes accompanying galaxy formation. Our analysis shows that simulated clusters exhibit a high degree of regularity and tight correlations between the considered observables and total mass. The normalizations of the M_{500} - T_X , $M_{g,500}$ - T_X , and M_{500} - Y_X relations agree to better than $\approx 10\%$ -15% with the current observational measurements of these relations. Our results show that Y_X is the best mass proxy with a remarkably low scatter of only $\approx 5\%$ -7% in M_{500} for a fixed Y_X , at both low and high redshifts and regardless of whether clusters are relaxed or not. In addition, we show that redshift evolution of the Y_X - M_{500} relation is close to the self-similar prediction, which makes Y_X a very attractive mass indicator for measurements of the cluster mass function from X-ray-selected samples.

Subject headings: cosmology: theory — galaxies: clusters: general — galaxies: evolution — methods: numerical — X-rays: galaxies: clusters

Online material: color figures

1. INTRODUCTION

The evolution of cluster abundance is one of the most sensitive probes of cosmology, which can constrain the power spectrum normalization, matter content, and the equation of state of the dark energy. The potential and importance of these constraints have motivated efforts to construct several large surveys of high-redshift clusters during the next several years. However, in order to realize the full statistical power of the upcoming cluster surveys, it is paramount that the relation between cluster mass and observables and any potential biases are well known.

Several cluster observables based on galaxy velocities, optical light, and X-ray observables, such as luminosity, temperature, mass of the intracluster medium (ICM), and Sunyaev-Zel'dovich (SZ) flux, have been proposed and used in the literature as proxies of the total cluster mass (for a recent comprehensive review see Voit 2005). In this study we focus on the mass indicators derived from cluster X-ray observables, which provide a handle on the properties of the hot ICM component. X-ray luminosity, $L_{\rm X}$, computed using the flux integrated within a certain radius or a range of radii, is expected to correlate with cluster mass (e.g., Kaiser 1986) and is the most straightforward mass indicator to measure observationally. L_X has been used for cosmological fits to the cluster samples from the Röntgensatellit (ROSAT) All-Sky Survey (Reiprich & Böhringer 2002; Allen et al. 2003) and Deep Cluster Survey (Borgani et al. 2001). However, L_X is also the least accurate (internally) of all proposed X-ray proxies for M_{tot} . L_X is

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dominated by cluster cores and thus is particularly susceptible to nongravitational processes in the ICM. Given the large scatter in the L_X - T_X relation (e.g., David et al. 1993; Markevitch 1998; Ikebe et al. 2002), the L_X -M relation for real clusters probably also has significant scatter (Stanek et al. 2006). The slope of the L_X -M relation deviates from the self-similar prediction (e.g., Allen et al. 2003). In addition, X-ray luminosity is notoriously difficult to reliably model in cosmological simulations (e.g., Anninos & Norman 1996; Lewis et al. 2000), a significant disadvantage given that simulations are often used to get a handle on the expected evolution of the mass versus proxy relations. These problems could potentially be alleviated with sufficient angular resolution by excising the emission from cluster cores, responsible for most of the scatter (Markevitch 1998).

The most common choice of a mass proxy used to measure a cluster number density and constrain cosmological parameters is X-ray temperature of the intracluster plasma (e.g., Henry & Arnaud 1991; Oukbir & Blanchard 1992; Markevitch 1998; Henry 2000; Seljak 2002; Ikebe et al. 2002; Pierpaoli et al. 2003). Until recently, there was a large apparent systematic uncertainty in the normalization of the M- T_X relation, as evidenced, for example, by a $\approx 30\%$ -50% discrepancy between observational measurements and cosmological simulations (e.g., Finoguenov et al. 2001; Pierpaoli et al. 2003). Over the last several years the $M-T_X$ normalization was revised in both simulations and observations due to (1) inclusion of more realistic physics in cosmological simulations (e.g., radiative cooling and star formation; Davé et al. 2002; Muanwong et al. 2002), (2) improved analyses of observed clusters using more realistic gas density profiles (e.g., Borgani et al. 2004; Vikhlinin et al. 2006), (3) more reliable measurements of cluster temperature profiles (Markevitch et al. 1998; Nevalainen et al. 2000; Arnaud et al. 2005; Vikhlinin et al. 2006), and (4) better understanding of the meaning of the mean spectral X-ray temperature, T_X , and the use of uniform definition of T_X in observations and in simulation analyses (Mazzotta et al. 2004; Rasia et al. 2005; Vikhlinin 2006). The current agreement between models and observations is $\approx 10\%$ (see below).

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The scatter in the M- T_X relation is significantly reduced compared to that in the L_X -M relation (the upper limit from observations is $\approx 15\%$ in M for fixed T for relaxed clusters; Vikhlinin et al. 2006). In general, existence of a tight relation such as M- T_X indicates that clusters are a regular population of objects with their global properties tightly related to their total mass (e.g., Mohr et al. 1999) and scatter caused by secondary effects such as substructure in the ICM, nongravitational processes, and mergers (O'Hara et al. 2006).

More recently, gas mass was used as a proxy for the total mass (Vikhlinin et al. 2003; Voevodkin & Vikhlinin 2004). The practical advantage of gas mass over temperature is that it can be measured robustly from the X-ray imaging alone. Also, the M_g -M relation in principle permits external calibration from cosmic microwave background measurements of the global baryon–to–dark matter ratio. Finally, M_g can be expected to be less sensitive to mergers, which should translate into smaller scatter in the M_g -M relation. The caveat is that trends of gas mass with cluster mass and evolution with redshift are not yet fully understood.

The use of clusters as efficient probes for precision cosmology puts stringent requirements on observable cluster mass proxies: (1) tight, low-scatter correlation between the proxies and mass; (2) with the scatter insensitive to mergers, as the frequency of mergers is expected to increase sharply with redshift (Gottlöber et al. 2001); (3) simple power-law relation and evolution that can be described by a small number of parameters and be as close as possible to the prediction of the self-similar model.

Point 3 is crucial to ensure that the self-calibration strategies for analyses of large cluster surveys (Levine et al. 2002; Hu 2003; Majumdar & Mohr 2003, 2004; Lima & Hu 2004, 2005; Wang et al. 2004) are successful. This is because self-calibration is powerful when cluster scaling relations and their evolution have a simple form that can be parameterized with a small number of parameters. Self-similarity of the relation, for example, is a desirable property because it implies a particular simple power-law form of the relation at different redshifts and a specific redshift evolution of its normalization. Also, behavior close to self-similar suggests that parameterization will not be sensitive to reasonable changes to cosmology. Small deviations from the self-similarity can then be taken into account with a small number of parameters. Finally, we note also that it is very important that the scatter in the observable-mass relation is small and well behaved (Lima & Hu 2005).

In general, a mass proxy does not have to be a single cluster property, such as L_X , T_X , or $M_{g,500}$. Any physically motivated combination of these variables that is expected to be tightly related to cluster mass can be used to construct a valid mass indicator. A hint for a better X-ray mass proxy is provided by recent studies based on cosmological simulations of cluster formation (Motl et al. 2005; Nagai 2006), which show that integrated SZ flux, Y_{SZ} , proportional to the product of gas mass and temperature, is a good, robust mass indicator with low scatter in the Y_{SZ} -M relation, regardless of the dynamical state of a cluster. In addition, the Y_{SZ} -M relation exhibits a simple, nearly self-similar evolution with redshift (da Silva et al. 2004; Nagai 2006). The physical reason for the robustness of the SZ flux is straightforward: Y_{SZ} is directly related to the total thermal energy of the ICM and thus to the depth of the cluster potential well (see eq. [4] in § 2).

In this study we show that a similar robust, low-scatter mass indicator can be constructed using X-ray observables. The indicator, which is simply the product of the total ICM mass and X-ray spectroscopic temperature, $Y_X = M_g T_X$, correlates strongly with cluster mass with only $\approx 5\%-8\%$ intrinsic scatter. The scatter is robust to mergers, in a sense that even for disturbed unrelaxed systems it gives unbiased estimates of mass with the statistical uncertainty similar to that for relaxed systems. Thus, the scatter of the Y_X -M relation at higher redshift is similar to the scatter at z =0. In addition, we show that evolution of the slope and normalization of the Y_X -M relation is nearly self-similar. These properties make Y_X particularly useful for measurements of cluster mass function using X-ray surveys.

2. MASS PROXIES

Physical properties of virialized systems, such as clusters, are expected to correlate with their total mass. For example, in the selfsimilar model (Kaiser 1986, 1991) the cluster gas mass is expected to be simply proportional to the total mass:

$$M_{\Delta_c} = C_{M_g} M_{g,\Delta_c},\tag{1}$$

where masses are determined within a radius enclosing a certain overdensity Δ_c with respect to the critical density of the universe at the epoch of observation, $\rho_{crit}(z)$, and C_{M_g} is a constant independent of cluster mass and redshift. The self-similar relation between cluster mass and temperature is

$$E(z)M_{\Delta_c} = C_T T^{3/2}.$$
(2)

Here the function $E(z) \equiv H(z)/H_0$ for a flat cosmology with the cosmological constant assumed throughout this study is given by (e.g., Peebles 1993)

$$E(z) = \sqrt{\Omega_M (1+z)^3 + \Omega_\Lambda}, \qquad (3)$$

where Ω_M and Ω_Λ are the present-day density parameters for matter and cosmological constant, respectively.

The SZ flux integrated within a certain radius, Y_{SZ} , is proportional to the total thermal energy of the ICM gas and thus to the overall cluster potential, which makes it relatively insensitive to details of the ICM physics and merging:

$$Y_{\rm SZ} = \left(\frac{k_{\rm B}\sigma_{\rm T}}{m_e c^2}\right) \int_{r < r_{\Delta_c}} n_e T_e \, dV \propto M_{g,\Delta_c} T_m, \tag{4}$$

where $k_{\rm B}$, $\sigma_{\rm T}$, m_e , and c have their usual meaning, n_e and T_e are the electron number density and temperature of the gas, respectively, and T_m is the gas mass–weighted mean temperature of the ICM. Note that the gas mass M_{g,Δ_c} here has the same meaning as in equation (1), as we assume integration over volume within r_{Δ_c} . A combination of equations (1), (2), and (4) gives a self-similar prediction for the $Y_{\rm SZ}$ -M relation,

$$E(z)^{2/5}M_{\Delta_c} = C_{Y_{\rm SZ}}Y_{\rm SZ}^{3/5}.$$
 (5)

Cosmological simulations show that Y_{SZ} is a good cluster mass proxy with very small scatter and that Y_{SZ} -*M* relation form and evolution are close to the self-similar prediction (da Silva et al. 2004; Motl et al. 2005; Hallman et al. 2006; Nagai 2006). Given the good qualities of Y_{SZ} as a mass proxy, it is interesting whether a similar indicator can be constructed using X-ray observables, which could be used in studies of X-ray cluster abundances. The simplest X-ray analog of Y_{SZ} is

$$Y_{\rm X} = M_{q,\Delta_c} T_{\rm X},\tag{6}$$

where M_{g,Δ_c} is the gas mass derived from X-ray imaging data (it is measured within a radius enclosing overdensity Δ_c) and T_X is the mean X-ray *spectral* temperature (Mazzotta et al. 2004; Vikhlinin 2006). As we describe below in § 3, it is advantageous

TABLE 1 Simulated Cluster Sample at z = 0

Cluster ID	${M_{500} \over (10^{13} \ h^{-1} \ M_{\odot})}$	$M_{g,500} \ (10^{13} \ h^{-1} \ M_{\odot})$	$\langle T_{\rm X} \rangle$ (keV)
CL 101	90.8	8.17	8.7
CL 102	54.5	4.82	5.8
CL 103	57.1	4.91	4.8
CL 104	53.9	5.15	7.7
CL 105	48.6	4.71	6.2
CL 106	34.7	3.17	4.3
CL 107	25.7	2.17	3.9
CL 3	20.9	1.91	3.6
CL 5	13.1	1.06	2.4
CL 6	16.8	1.38	3.4
CL 7	14.1	1.21	2.9
CL 9	8.23	0.73	1.6
CL 10	6.72	0.43	1.9
CL 11	8.99	0.78	2.0
CL 14	7.69	0.62	1.8
CL 24	3.47	0.26	1.0

to measure T_X excluding central cluster regions, which can be achieved with moderate angular resolution X-ray telescopes ($\leq 15''$ FWHM). Excising the central regions is desirable because observed cluster temperature profiles show a greater degree of similarity outside the core (Vikhlinin et al. 2006) and also because this makes the spectral temperature closer to the gas mass–averaged T_m , which ideally should be used in equation (6).

3. MOCK *CHANDRA* IMAGES AND ANALYSES OF SIMULATED CLUSTERS

A detailed account of the simulations, mock image generation, and analysis will be presented elsewhere (D. Nagai et al. 2006, in preparation). Here we give a brief overview of the procedure and define how the observables used in this study are derived.

3.1. Simulated Cluster Sample

In this study we use high-resolution cosmological simulations of 16 cluster-sized systems in the "concordance" flat Λ CDM model: $\Omega_m = 1 - \Omega_{\Lambda} = 0.3$, $\Omega_b = 0.04286$, h = 0.7, and $\sigma_8 = 0.9$, where the Hubble constant is defined as $100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$ and σ_8 is the power spectrum normalization on the 8 h^{-1} Mpc scale. The simulations were done with the adaptive refinement tree (ART) *N*-body+gasdynamics code (Kravtsov 1999; Kravtsov et al. 2002), an Eulerian code that uses adaptive refinement in space and time and (nonadaptive) refinement in mass to reach the high dynamic range required to resolve cores of halos formed in self-consistent cosmological simulations.

To set up initial conditions, we first ran low-resolution simulations of two 80 h^{-1} Mpc boxes and seven 120 h^{-1} Mpc boxes, from which we selected 16 clusters with the virial masses ranging from $M_{\rm vir} \approx 7 \times 10^{13}$ to $2 \times 10^{15} h^{-1} M_{\odot}$ for resimulation at higher resolution. High-resolution simulations were run using the 128³ uniform grid and eight levels of mesh refinement in the computational boxes of 120 h^{-1} Mpc for CL 101–107 and 80 h^{-1} Mpc for CL 3–24. These simulations achieve the dynamic range of 128 × 2⁸ = 32,768 and peak formal resolution of \approx 3.66 and 2.44 h^{-1} kpc, corresponding to the actual resolution of \approx 7 and 5 h^{-1} kpc for 120 and 80 h^{-1} Mpc boxes, respectively. Only the region of \sim 3–10 h^{-1} Mpc around the cluster was adaptively refined; the rest of the volume was followed on the uniform 128³ grid. The mass resolution corresponds to the effective 512³ particles in the entire box, or the Nyquist wavelength $\lambda_{\rm Ny} = 0.469$ and

0.312 h^{-1} comoving Mpc for CL 101–107 and CL 3–24, respectively, or 0.018 and 0.006 h^{-1} Mpc in the physical units at the initial redshift of the simulations. The dark matter particle mass in the region around the cluster was $9.1 \times 10^8 h^{-1} M_{\odot}$ for CL 101–107 and $2.7 \times 10^8 h^{-1} M_{\odot}$ for CL 3–24, while other regions were simulated with lower mass resolution.

The cluster simulations used in this analysis include dissipationless dynamics of dark matter, gasdynamics, star formation, metal enrichment and thermal feedback due to Type II and Type Ia supernovae, self-consistent advection of metals, metallicity-dependent radiative cooling, and UV heating due to cosmological ionizing background (Haardt & Madau 1996). The cooling and heating rates take into account Compton heating and cooling of plasma, UV heating, and atomic and molecular cooling and are tabulated for the temperature range $10^2 \text{ K} < T < 10^9 \text{ K}$ and a grid of metallicities and UV intensities using the CLOUDY code (ver. 96b4; Ferland et al. 1998). The CLOUDY cooling and heating rates take into account metallicity of the gas, which is calculated selfconsistently in the simulation, so that the local cooling rates depend on the local metallicity of the gas.

Star formation in these simulations was implemented using the observationally motivated recipe (e.g., Kennicutt 1998): $\dot{\rho}_* = \rho_{gas}^{1.5} t_*^{-1}$, with $t_* = 4 \times 10^9$ yr. Stars are allowed to form in regions with temperature $T < 2 \times 10^4$ K and gas density n > 0.1 cm⁻³. No other criteria (like the collapse condition $\nabla \cdot v < 0$) are used. Comparison of the runs with different choices of the threshold for star formation, n = 10, 1, 0.1, and 0.01 cm⁻³, shows that the threshold affects gas fractions at small radii, $r/r_{vir} < 0.1$, but its effect is negligible at the radii we consider in this study. Further details about this simulated cluster sample will be presented in D. Nagai et al. (2006, in preparation).

The properties of the simulated cluster sample are summarized in Table 1. We list the total and hot ICM masses defined within a radius r_{500} enclosing the overdensity of 500 with respect to the critical density at z = 0. We also list the mean spectral temperature measured using mock *Chandra* spectra from the radial region of $(0.15-1)r_{500}$, as described in § 3.3. Although the simulated cluster sample is small, the objects cover more than an order of magnitude in mass and are simulated with very high resolution, which allows us to take into account effects of galaxy formation on the ICM.

In what follows, we use cluster total mass and observables measured within $r_{500} \approx (0.5-0.6)r_{vir}$, where r_{vir} is a traditional definition of cluster virial radius using the virial overdensity Δ_{vir} (\approx 337 at z = 0 for the cosmology adopted in our simulations) with respect to the mean density at z = 0. This choice of the outer radius is mainly motivated by the fact that clusters are more relaxed within r_{500} compared to the outer regions (Evrard et al. 1996; E. T. H. Lau et al. 2006, in preparation). Also, the analysis of real clusters is often limited to a similar radius because of a limited field of view and sensitivity.

3.2. Mock Chandra Images

In what follows, in discussing the X-ray mass indicators we use quantities as they would be derived from a realistic X-ray analysis of the *Chandra* data. To this end, we use mock *Chandra* X-ray images of the simulated clusters and employ analysis procedures closely matched to those used to analyze real *Chandra* observations. Our motivation is twofold. First, we are interested in evaluating realistic mass indicators involving actual observables, rather than theoretical three-dimensional quantities. Second, as we show below, part of the reason Y_X works so well is due to the fact that we use M_g and T_X as measured in observations. The low scatter of Y_X is due to a fortunate anticorrelation of deviations in gas mass and

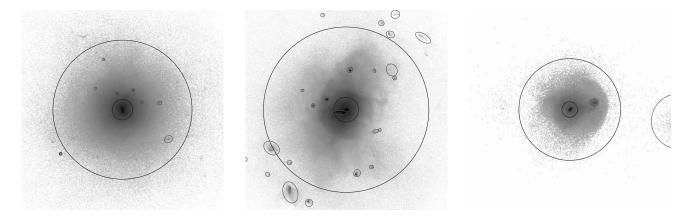


FIG. 1.—Mock X-ray 100 ks images of three clusters from our sample. Left to right: CL 104 at z = 0, CL 101 at z = 0, and CL 14 at z = 0.6. Image size is 4×4 Mpc for CL 101 and CL 104 and 2×2 Mpc for CL 14. CL 104 is classified as relaxed, while the other two clusters are classified as unrelaxed. Small ellipses show substructures detected by our automated software (see § 3.2). The outer and inner circles show the radii $r = r_{500}$ and $0.15r_{500}$, respectively. [See the electronic edition of the Journal for a color version of this figure.]

temperature. This anticorrelation is enhanced when Y_X is estimated using M_{q,Δ_c} and T_X estimated from the X-ray analysis (see § 4).

To generate mock data, we first create X-ray flux maps of the simulated clusters viewed along three orthogonal projections. The flux map is computed by projecting the X-ray emission arising from the computational cells within $3R_{vir}$ of the cluster along a given line of sight, taking into account the actual gas density, temperature, and metallicity of each cell in a simulation output. We compute the X-ray plasma emission, $\Lambda_E(T_i, Z_i, z)$, using the MEKAL code with the relative elemental abundance from Anders & Grevesse (1989) and assuming interstellar absorption with a hydrogen column density of $n_{\rm H} = 2.0 \times 10^{20} \text{ cm}^{-2}$. This provides expected emission spectra in the 0.1–10 keV energy range on a spatial grid 1024×1024 pixels with the size 4.88 h^{-1} kpc for CL 101–107 and 2.44 h^{-1} kpc for CL 3–24. The entire map is therefore 5.0 and 2.5 h^{-1} Mpc, respectively. In generating the spectral maps we assume that the redshift of cluster observation is $z_{obs} = 0.06$ for the simulation output at z = 0 and $z_{obs} = 0.6$ for the z = 0.6sample.

Next, we simulate a photon map by convolving the spectrum from each image pixel with the on-axis response of the Chandra ACIS-I camera and drawing the number of photons in each spectral channel from the Poisson distribution. We simulate two sets of mock Chandra photon maps. In the first set we assume a 100 ks Chandra exposure, which is fairly typical for real deep observations. From this set, we generate cluster images in the 0.7–2 keV band. We then add a uniform Poisson background with the intensity typical for ACIS-I data (Markevitch et al. 2003). These images are used to identify and mask out from the further analysis all detectable small-scale clumps (see Fig. 1), as routinely done by observers. These clumps contain a small fraction of gas mass and do not bias gas mass estimates. They can, however, bias temperature measurement significantly. Our clump detection is fully automatic and based on the wavelet decomposition algorithm described in Vikhlinin et al. (1998).

All further analysis is performed using the second set of photon maps generated for very long exposures, 10^6 s for the z = 0 sample and 10^8 s exposure for the z = 0.6 sample. Here the exposure time is chosen to ensure $\approx 10^6 - 10^7$ photons outside the cluster core region for all simulated clusters. This second set of data is used in our analysis to derive gas mass and mean spectroscopic temperature of the ICM. The exposures are artificially large by design as we are interested in the intrinsic scatter of the X-ray observablemass relation, not the statistical errors due to photon noise in a particular choice of short exposure. Also, we ignore further complications present in reduction of real *Chandra* data, including background subtraction and spatial variations of the effective area (i.e., we assume that accurate corrections for these effects can be applied to the real data and any associated uncertainties are included in the reported measurement errors).

3.3. Analysis of Mock Chandra Data

We analyze the mock data of the simulated clusters employing techniques and tools used in analyses of the real Chandra cluster observations, as described in detail by Vikhlinin et al. (2006). After masking out detectable substructures (see above), we fit the X-ray spectra in concentric annuli to measure projected temperature and metallicity profiles. Next, we measure an X-ray surface brightness profile in the 0.7-2 keV band (used in the real data analysis because it provides the optimal signal-to-noise ratio). Using the effective area as a function of energy and observed projected temperature and metallicity at each radius, we convert the observed brightness from units of count rate to the projected emission measure, EM = $\int n_e n_p \, dl$. The derived projected emission measure profile is fitted to a three-dimensional model of $\rho_{gas}(r)$ that has great functional freedom and can independently describe the gas density slopes at both $r \gtrsim r_{500}$ and at smaller radii and in the very inner region. The best-fit model directly provides the gas mass profile, $M_{\text{gas}}(r)$.

We also measure the average X-ray spectral temperature, T_X , from a single-temperature fit to the spectrum integrated within r_{500} , excluding the central region strongly affected by radiative cooling. The inner cut is set at a fixed fraction of r_{500} , $r_{in} = 0.15r_{500}$. Note that we choose to cut out central regions defined using a fixed fraction of r_{500} rather than a fixed metric radius of 70 kpc as in Vikhlinin et al. (2006). This new definition for T_X results in only a small correction (-3% on average) of the T_X values reported in Vikhlinin et al. (2006), who used notation of T_{spec} instead of T_X . We choose the specific value of $r_{in} = 0.15r_{500}$ because beyond this radius the observed temperature profiles of clusters are approximately self-similar, while at smaller radii the profiles show a large scatter. The choice of r_{in} thus should maximize the selfsimilarity of the relation between mass and T_X .

In our analysis below we distinguish unrelaxed clusters from relaxed systems to test the sensitivity of the mass proxies to mergers and substructure. Specifically, as is usually done to classify observed clusters, we visually examine mock 100 ks *Chandra* images for *x*, *y*, and *z* projections of each cluster and classify as "relaxed" clusters that have regular X-ray morphology and no secondary maxima

Sample ^a	Quantity ^b	M_{500} - $T_{\rm X}$	M_{500} - $M_{g,500}$	M_{500} - $Y_{\rm X}$	$M_{500}\text{-}Y_{\mathrm{SZ}}^{\mathrm{3D}}$
All z, all clusters	$\log_{10}C$	14.41 ± 0.014	14.35 ± 0.008	14.27 ± 0.006	14.27 ± 0.005
	α	1.521 ± 0.062	0.921 ± 0.023	0.581 ± 0.009	0.585 ± 0.010
	Scatter	0.195	0.107	0.071	0.067
	$\log_{10}C_{\rm ss}$	14.41 ± 0.014	14.35 ± 0.010	14.27 ± 0.006	14.27 ± 0.006
All <i>z</i> , relaxed	$\log_{10}C$	14.36 ± 0.017	14.36 ± 0.015	14.26 ± 0.008	14.26 ± 0.009
	α	1.533 ± 0.103	0.898 ± 0.051	0.579 ± 0.012	0.564 ± 0.014
	Scatter	0.136	0.115	0.053	0.058
	$\log_{10}C_{\rm ss}$	14.36 ± 0.016	14.36 ± 0.019	14.26 ± 0.009	14.26 ± 0.010
All z, unrelaxed	$\log_{10}C$	14.44 ± 0.018	14.34 ± 0.010	14.28 ± 0.008	14.27 ± 0.006
	α	1.553 ± 0.063	0.931 ± 0.029	0.589 ± 0.010	0.600 ± 0.010
	Scatter	0.186	0.095	0.072	0.059
	$\log_{10}C_{\rm ss}$	14.44 ± 0.018	14.35 ± 0.011	14.28 ± 0.007	14.27 ± 0.006
z = 0, all clusters	$\log_{10}C$	14.39 ± 0.019	14.37 ± 0.012	14.27 ± 0.007	14.28 ± 0.008
	α	1.524 ± 0.070	0.917 ± 0.028	0.583 ± 0.010	0.584 ± 0.013
	Scatter	0.219	0.090	0.064	0.075
	$\log_{10}C_{\rm ss}$	14.39 ± 0.020	14.37 ± 0.013	14.27 ± 0.007	14.27 ± 0.008
z = 0.6, all clusters	$\log_{10}C$	14.44 ± 0.018	14.31 ± 0.009	14.27 ± 0.008	14.26 ± 0.007
	α	1.590 ± 0.086	0.871 ± 0.033	0.571 ± 0.016	0.577 ± 0.012
	Scatter	0.157	0.077	0.075	0.051
	$\log_{10}C_{\rm ss}$	14.43 ± 0.017	14.34 ± 0.015	14.27 ± 0.009	14.26 ± 0.007

TABLE 2 Power-Law $M_{500} = CX^{\alpha}$ Best-Fit Parameters and Scatter

^a Power-law fits were performed for different subsets of our cluster sample, split in redshift and/or dynamical state. In addition to the fits in which both normalization and slope of the power-law relations were fitted simultaneously, we provide the best-fit normalizations, C_{ss} , for each relation when fitted with the slopes fixed to their self-similar values: 1.5, 1.0, and 0.6 for the M_{500} - T_X , M_{500} - $M_{g,500}$, and M_{500} - Y_X relations, respectively.

^b For each observable $X = T_X, M_{g,500}, Y_X, Y_{SZ}^{3D}$, we fit a power-law relation of the form $M_{500} = C(X/X_0)^{\alpha}$, with $X_0 = 3.0$ keV, $2 \times 10^{13} M_{\odot}, 4 \times 10^{13}$ keV M_{\odot} , and 5×10^{-6} Mpc² for $T_X, M_{g,500}, Y_X, Y_{SZ}$, respectively. Note that at z = 0.6, the masses M_{500} are corrected for the expected self-similar evolution appropriate for each scaling relation, as described in § 2.

and minimal deviations from the elliptical symmetry. "Unrelaxed" clusters are those with secondary maxima, filamentary X-ray structures, or significant isophotal centroid shifts. As an illustration, Figure 1 shows X-ray images of three simulated clusters: one classified as relaxed and two as unrelaxed.

4. COMPARISON OF MASS INDICATORS

In this section we compare four indicators of cluster mass: X-ray spectral temperature T_X , gas mass $M_{g,500}$, integrated SZ flux Y_{SZ} , and its X-ray analog $Y_X \equiv M_{g,500}T_X$.

Figures 2–4 show the M_{500} - T_X , M_{500} - $M_{g,500}$, and M_{500} - Y_X relations, respectively. We present correlations at redshifts z = 0.0 and 0.6, classifying clusters into relaxed and unrelaxed based on their X-ray image morphology, as described in § 3.3. We performed power-law fits to these relations and present best-fit values of parameters, as well as the amount of scatter around the best-fit relation for different subsets of the clusters in Table 2. The table shows best-fit values for the case when both normalization and slopes were allowed to vary and the best-fit power-law normalizations, C_{ss} , for the fits with the values of slope for each relation fixed to the value predicted by the self-similar model. The latter are useful in evaluating trends in normalization between different subsamples (e.g., relaxed vs. unrelaxed trend in the M_{500} - T_X relation) or judging how close is the evolution of each relation to the self-similar expectation.

For comparison, we also include fits to the M_{500} - Y_{SZ} relation, where Y_{SZ} is the three-dimensional integrated SZ flux measured within r_{500} (Nagai 2006). The power-law fits were performed for each projection (i.e., x, y, and z) separately. We estimate the uncertainties in the best-fit parameters by generating 10,000 bootstrap samples (Press et al. 1992) and calculating a dispersion of the best-fit power-law normalization and slope among the samples. Figure 2 and Table 2 show that the slope and evolution of the M_{500} - T_X relation are quite close to the self-similar model. There is a ~20% scatter in M_{500} around the mean relation, and much of the scatter is due to unrelaxed clusters. Note also that the normalization of the M_{500} - T_X relation for unrelaxed systems is somewhat biased with respect to that for the unrelaxed subsample. Unrelaxed clusters have somewhat lower temperatures for a given mass (see best-fit normalizations in Table 2). This may seem counterintuitive at first, given that one can expect that shocks can boost the ICM temperature during mergers. However, in practice the effect of shocks is relatively small (e.g., O'Hara et al. 2006). The main source of the bias is that during advanced mergers the mass of the system already increased but only a fraction of the kinetic energy of merging systems is converted into the thermal energy of the ICM (see, e.g., Mathiesen & Evrard 2001).

The M_{500} - $M_{g,500}$ relation (Fig. 3) has a somewhat smaller scatter ($\approx 10\%-12\%$) around the best-fit power-law relation than the M_{500} - $T_{\rm X}$, but its slope is significantly different from the self-similar prediction: we find $M_{500} \propto M_{g,500}^{0.88-0.92}$ compared to the expected $M_{500} \propto M_{g,500}$. This is due to the trend of gas fraction with cluster mass, $f_{\rm gas} \equiv M_{g,500}/M_{500} \propto M_{500}^{0.1-0.2}$, present for both the simulated clusters in our sample (see Kravtsov et al. 2005) and the observed clusters (Vikhlinin et al. 2006). The normalization of the M_{500} - $M_{g,500}$ relation, on the other hand, evolves only weakly between z = 0.6 and 0 (yet, statistically significant evolution is present; see Table 2), reflecting slow evolution of the gas fraction with time (Kravtsov et al. 2005).

The M_{500} - Y_X relation (Fig. 4) has the smallest scatter of only $\approx 5\%$ -7%. Note that this value of scatter includes clusters at both low and high redshifts and both relaxed and unrelaxed systems. In fact, the scatter in M_{500} - Y_X for relaxed and unrelaxed systems is indistinguishable within the errors (see Table 2). Note also that

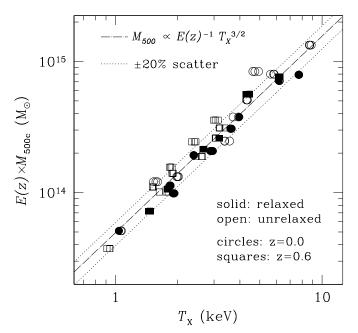


FIG. 2.— Relation between the X-ray spectral temperature, T_X , and total mass, M_{500} . T_X is measured within the radial range $(0.15-1)r_{500}$. Separate symbols indicate relaxed and unrelaxed clusters, and also z = 0 and 0.6 samples. The dashed line shows the power-law relation with the self-similar slope fitted to the entire sample, and the dotted lines indicate 20% scatter. [See the electronic edition of the Journal for a color version of this figure.]

the figures include points corresponding to three projections of each cluster. Figure 4 shows that the dispersion in the projected values of Y_X for each given cluster is very small, which means that Y_X is not very sensitive to asphericity of clusters. Remarkably, the scatter of the M_{500} - Y_X relation, which involves direct X-ray observables, is as small as that in the M_{500} - Y_{SZ} relation (see Table 2), which is computed using three-dimensional density and temperature information from the simulations.

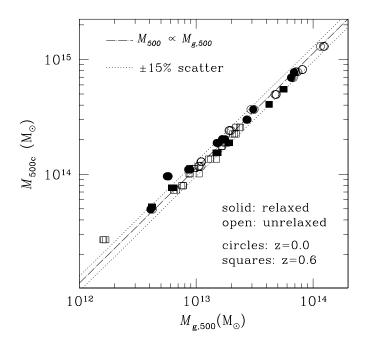


FIG. 3.—Correlation between gas mass and total mass of the clusters. Both masses are measured within r_{500} . The meaning of the symbols and lines is the same as in Fig. 2. The dotted lines indicate 15% scatter. [See the electronic edition of the Journal for a color version of this figure.]

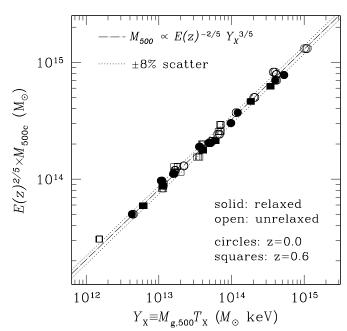


FIG. 4.— Y_X - M_{500} correlation. The meaning of the symbols and lines is the same as in Fig. 2. The dotted lines indicate 8% scatter. [See the electronic edition of the Journal for a color version of this figure.]

The comparison of the mass proxies clearly shows that Y_X , the product of gas mass and X-ray spectral temperature, is a more robust and self-similar mass indicator than either of these X-ray observables. Why is the product better than its parts? Figure 5 shows that the answer lies in the anticorrelation of the residuals of temperature and gas mass from their respective relations with total cluster mass. We plot residuals from the best-fit power laws with the slope value fixed to the self-similar value (i.e., using normalizations given by the values of C_{ss} in Table 2) to illustrate both random scatter and systematic deviations from self-similar behavior.

Figure 5 shows that the clusters with temperatures lower than the mean temperature for a given total mass tend to have gas mass higher than the mean and vice versa. Note also that there is some redshift evolution between z = 0 and 0.6: more clusters have negative deviations of temperature and positive deviations of measured gas mass at z = 0.6 compared to z = 0. This redshift evolution is thus in the opposite direction for the gas mass and temperature deviations. The measured $M_{g,500}$ systematically increases at higher z for a fixed total mass because high-z clusters are less relaxed on average. For unrelaxed clusters, the ICM density distribution is nonuniform, which results in overestimation of $M_{g,500}$ from X-ray data (Mathiesen et al. 1999). Some of the decrease of $M_{g,500}$ at lower z may be due to continuing cooling of the ICM, which decreases the mass of hot X-ray–emitting gas.

The anticorrelation of residuals and opposite evolution with redshift for gas mass and temperature is the reason why the behavior of their product, on average, has smaller scatter and is closer to the self-similar expectation in both the slope and evolution. We discuss the origin of this behavior further in \S 6.

5. PRACTICAL ALGORITHM FOR ESTIMATING CLUSTER MASS USING Y_X

Suppose we have the Y_X-M_{500} relation precalibrated by some external means, $M_{500} = CE(z)^{\gamma}Y_X^{\alpha}$, and we would like to use it to estimate M_{500} . The precalibration can be done using a well-observed sample of relaxed clusters or simulations. Note that the definition of Y_X includes spectral temperature and gas mass within

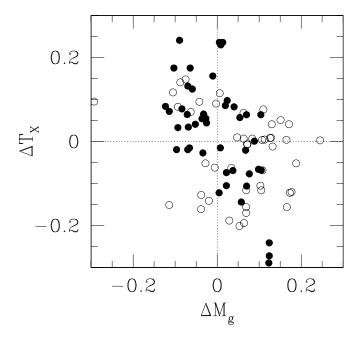


FIG. 5.—Fractional deviations in temperature and gas mass for fixed M_{500} relative to their respective best-fit self-similar relations, $M_{500} \propto T_X^{1.5}$ and $M_{500} \propto M_{g,500}$. The fit includes all systems, at both z = 0 (*filled circles*) and z = 0.6 (*open circles*). Note that the deviations for gas mass and temperature are generally anticorrelated: clusters with large positive (negative) deviations in $M_{g,500}$ tend to have negative (positive) deviations in T_X . A similar anticorrelation exists in the trend with redshift (compare the distribution of points for z = 0 and 0.6). [See the electronic edition of the Journal for a color version of this figure.]

 r_{500} . In practice, however, when we want to use Y_X to estimate M_{500} we do not know the value of r_{500} a priori. The measurement of gas mass will depend quite sensitively on the adopted outer radius because the profile $M_g(r)$ does not converge at large r. In practice, therefore, we have to solve for r_{500} simultaneously with estimating M_{500} , which can be done with the following iterative algorithm. An initial value for T_X can be obtained by using the integrated temperature (including the center) to estimate an approximate value of r_{500} through a crude mass-temperature relation and then remeasuring the spectrum in the radial range $(0.15-1)r_{500}$. Then, using identity $M_{500} = (4/3)\pi 500\rho_c(z)r_{500}^3$, we can rewrite the Y_X -M relation as

$$\frac{4}{3}\pi 500\rho_c(z)r_{500}^3 = CE(z)^{\gamma}[Y_{\rm X}(r_{500})]^{\alpha},\tag{7}$$

where $Y_{\rm X}(r) \equiv T_{\rm X}M_{g,500}(r)$ and the constant *C* is from the precalibrated $Y_{\rm X}$ - M_{500} relation. Equation (7) is used to solve for r_{500} . A second iteration can then be done using $T_{\rm X}$ remeasured in the newly estimated radial range $(0.15-1)r_{500}$, continuing the procedure until convergence. Once r_{500} is determined, $M_{500} =$ $(4/3)\pi 500\rho_c(z)r_{500}^3$.

It is useful to know how the observational calibration of the normalization constant *C* in equation (7) scales with the assumed value of the Hubble constant. Cluster masses determined dynamically or through gravitational lensing scale as $M \propto h^{-1}$. This implies that the angular size that corresponds to r_{500} is *h* independent. The gas mass derived from X-ray data for a fixed angular radius scales as $M_g \propto h^{-5/2}$. Therefore, the observed normalization of the Y_X -M relation with a slope close to self-similar scales as $C \propto h^{1/2}$.

6. DISCUSSION AND CONCLUSIONS

In this paper we presented comparisons of several X-ray proxies for the cluster mass: the spectral temperature and gas mass

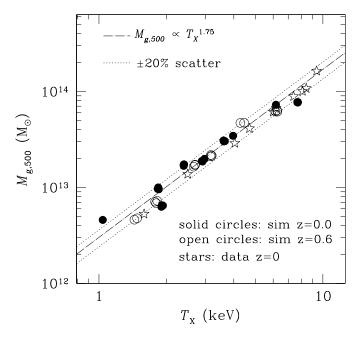


Fig. 6.— Relation between X-ray spectral temperature and gas mass for the relaxed subsample of simulated clusters (*circles*) and for a sample of relaxed *Chandra* clusters of Vikhlinin et al. (2006; *stars*). Both gas mass and temperature are the quantities derived from analysis of real and mock X-ray data. The error bars in the *Chandra* measurements are comparable to the symbol size and are not shown for clarity. The gas masses for the simulated clusters are rescaled by a factor of 0.17/ 0.143 = 1.19 to reflect the difference between the universal baryon fractions adopted in the simulation and the value measured by *WMAP*. The dot-dashed line shows the best-fit power-law relation with the slope 1.75. [See the electronic edition of the *Journal for a color version of this figure.*]

measured within r_{500} and the new proxy, Y_X , defined as a simple product of T_X and $M_{g,500}$. Analogously to the integrated Sunyaev-Zel'dovich flux, Y_X is related to the total thermal energy of the ICM. To test these mass proxies, we use a sample of clusters simulated in the concordance Λ CDM cosmology. The simulations achieve high spatial resolution and include radiative cooling, star formation, and other processes accompanying galaxy formation. We construct mock *Chandra* images for the simulated clusters and derive the X-ray proxies from a procedure essentially identical to that used in real data analysis.

The main result of this study is that Y_X is a robust mass indicator with remarkably low scatter of only $\approx 5\%-7\%$ in M_{500} for fixed Y_X , regardless of whether the clusters are relaxed or not. In addition, we show that the redshift evolution of the Y_X - M_{500} relation is close to the self-similar prediction given by equation (5), which makes this indicator a very attractive observable for studies of cluster mass function with X-ray–selected samples. This is because self-similar behavior suggests well-motivated, simple parameterization for the scaling relations and their redshift evolution for a reasonably wide range of underlying cosmologies.

The T_X - M_{500} relation has the largest scatter ($\approx 20\%$), most of which is due to unrelaxed clusters. The unrelaxed clusters have temperatures biased low for a given mass. This is likely because during mergers, the mass of the system has already increased but only a fraction of the kinetic energy of merging systems is converted into the thermal energy of gas, due to incomplete relaxation.

The $M_{g,500}$ - M_{500} relation shows an intermediate level of scatter, $\approx 10\%$ -12%. This relation does not appear to be sensitive to mergers. It does, however, exhibit significant deviations from the selfsimilarity in its slope, which is due to the dependence of gas fraction within r_{500} on the cluster mass (Kravtsov et al. 2005). A similar dependence exists for observed clusters (Vikhlinin et al. 2006),

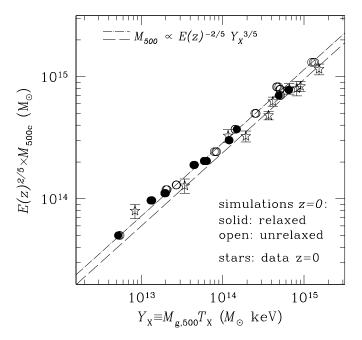


FIG. 7.— Y_X - M_{500} relation for the z = 0 sample of the simulated clusters (*circles*) and for a sample of relaxed *Chandra* clusters of Vikhlinin et al. (2006; *stars*). The gas masses for the simulated clusters are appropriately rescaled (see caption to Fig. 6). The dot-dashed line shows the best-fit power-law relation for the simulated clusters with the slope fixed to the self-similar value of $\frac{3}{5}$. The dashed line shows the same best-fit power law, but with the normalization scaled down by 15%. [See the electronic edition of the Journal for a color version of this figure.]

and we can thus expect similar trends in the $M_{g,500}$ - M_{500} relation for real clusters.

Generally, all of the observable-mass relations we tested demonstrate a remarkable degree of regularity of galaxy clusters as a population. T_X , $M_{g,500}$, and Y_X all exhibit correlations with M_{500} that are close to the expectation of the self-similar model, in both their slope and evolution with time, within the uncertainties provided by our sample. The only exception is the slope of the $M_{g,500}$ - M_{500} relation.

Given that our analysis relies on cosmological simulations, it is reasonable to ask whether the simulated clusters are realistic. Although simulations certainly do not reproduce all of the observed properties of clusters, especially in their core regions, the ICM properties outside the cores in simulations and observations agree quite well. We illustrate this in Figure 6, which shows the $M_{q,500}$ - $T_{\rm X}$ relations for simulated and observed clusters (the sample of relaxed clusters at $z \approx 0$ from Vikhlinin et al. 2006). For this comparison we use only those clusters from simulations that appear regular and relaxed in their X-ray surface brightness image. Clearly, both simulated and observed clusters exhibit tight correlations between $M_{q,500}$ and T_X (see also Mohr et al. 1999; Voevodkin et al. 2002), which agree remarkably in their slope $(M_a \propto T^{1.75})$ and normalization.⁶ The normalizations derived from simulated and real clusters agree to $\approx 10\%$, while slopes are indistinguishable and both deviate significantly from the expected selfsimilar value of 1.5. This is a consequence of significant trends in the gas fraction with cluster mass, $M_{g,500}/M_{500} \propto M_{500}^{0.2-0.25}$, for both simulated (Kravtsov et al. 2005) and observed clusters (Vikhlinin et al. 2006). The deviations from the self-similar model also manifest themselves in the absence of any noticeable evolution with redshift.⁷ Interestingly, the real clusters show a similarly weak evolution in the $M_{g,500}$ - T_X relation (Vikhlinin et al. 2002). Figure 5 shows that a likely explanation is that the clusters at z = 0.6 tend to be colder for the fixed M_{tot} but have higher estimated $M_{g,500}$ than their counterparts at z = 0 because they are less relaxed.

A similar level of agreement between the simulations and latest *Chandra* measurements exists also for the total mass versus temperature relation, M_{500} - T_X . In fact, the normalization for our simulated sample (Table 2) agrees with the observational results of Vikhlinin et al. (2006) to $\approx 10\%$. This is a considerable improvement given that significant disagreements existed just several years ago (see § 1). The residual systematic 10% difference in the normalization is likely caused by nonthermal pressure support from bulk gas motions (Faltenbacher et al. 2005; Rasia et al. 2006; E. T. H. Lau et al. 2006, in preparation), which is unaccounted for in X-ray hydrostatic mass estimates.

In Figure 7 we compare the Y_X - M_{500} relation for the simulated clusters⁸ and for the *Chandra* sample of Vikhlinin et al. (2006). The observed clusters show a tight correlation with a slope close to the self-similar value. There is a $\approx 15\%$ difference in normalization, likely explained also by the turbulent pressure support not accounted for in the *Chandra* hydrostatic mass estimates.

The excellent agreement of simulations and observations in terms of the relation between the two X-ray observables used to compute Y_X ($M_{g,500}$ - T_X) and a relatively good agreement in the T_X - M_{500} and Y_X - M_{500} relations gives us confidence that the results presented in this paper are sufficiently realistic. One can ask whether the real clusters show the same trend of decreasing scatter when $M_{g,500}$ and Y_X are used as mass indicators instead of T_X . Unfortunately, the existing data cannot answer this question because the mass measurement uncertainties for individual clusters are of order or larger than the expected scatter for relaxed clusters.

Our results show that Y_X is clearly the most robust and the most self-similar X-ray cluster mass indicator. Biases existing in mass estimates based on $M_{g,500}$ and T_X anticorrelate both for a given redshift and in terms of evolutionary trends (see Fig. 5). This explains why their product, Y_X , is a better mass indicator than T_X and $M_{g,500}$ individually. The quality of Y_X compares well to that for the actual three-dimensional integral of the ICM thermal energy (proportional to Y_{SZ}) in terms of its low scatter and self-similarity (see Table 2). Y_X may prove to be an even better mass proxy than Y_{SZ} , given that we use ideal three-dimensional measurement of the latter while reproducing the actual data analysis for the former.

Note that Y_X is also an attractive mass proxy from the data analysis point of view. First, it reduces observational statistical noise by combining the two independently measured quantities, $M_{g,500}$ and T_X , into a single quantity. Consider for example how mass estimates are affected by T_X , a parameter that is the most difficult to derive from the data. A 10% measurement uncertainty in T_X translates into a ~15% mass uncertainty through the M- T_X relation and only a 6% uncertainty through the Y_X -M relation. Y_X is also less sensitive to any errors in the absolute calibration of X-ray telescopes. For example, a miscalibration of the low-energy effective area typically translates into T_X and $M_{g,500}$ measurement errors of the opposite sign, $\delta T/T \approx -2\delta M_g/M_g$. These errors partially cancel in Y_X , $\delta Y/Y \approx 0.5\delta T/T$, and are further reduced in the mass

⁶ For this comparison, the gas masses of simulated clusters are rescaled by a factor of 0.17/0.143 = 1.19 to reflect a difference between the universal baryon fractions adopted in the simulation and the value measured by *WMAP* (Spergel et al. 2003; Tegmark et al. 2004).

⁷ Note that $M_{g,500}$ in Fig. 6 is not multiplied by the E(z) factor unlike the total mass in Figs. 2 and 4.

³ Where we appropriately rescaled gas masses; see footnote 6.

estimate: $\delta M/M = 0.6\delta Y/Y \approx 0.3\delta T/T$. The error in mass is larger when other proxies are used, $\delta M/M = \delta M_g/M_g \approx 0.5\delta T/T$ for the M_g -M relation and $\delta M/M = 1.5\delta T/T$ for the M-T relation.

The robustness and low scatter make Y_X an excellent mass indicator for observational measurements of cluster mass function at both z = 0 and higher redshifts. The necessary data, an X-ray brightness profile and a wide-beam spectrum excluding the core, are easily obtained with sufficiently deep observations with *Chandra*, *XMM-Newton*, and *Suzaku* (for low-redshift clusters). The small scatter and simple, nearly self-similar evolution of the Y_X -*M* relation hold promise for the self-calibration strategies for future large X-ray cluster surveys.

- Allen, S. W., Schmidt, R. W., Fabian, A. C., & Ebeling, H. 2003, MNRAS, 342, 287
- Anders, E., & Grevesse, N. 1989, Geochim. Cosmochim. Acta, 53, 197
- Anninos, P., & Norman, M. L. 1996, ApJ, 459, 12
- Arnaud, M., Pointecouteau, E., & Pratt, G. W. 2005, A&A, 441, 893
- Borgani, S., et al. 2001, ApJ, 561, 13
- _____. 2004, MNRAS, 348, 1078
- da Silva, A. C., Kay, S. T., Liddle, A. R., & Thomas, P. A. 2004, MNRAS, 348, 1401
- Davé, R., Katz, N., & Weinberg, D. H. 2002, ApJ, 579, 23
- David, L. P., Slyz, A., Jones, C., Forman, W., Vrtilek, S. D., & Arnaud, K. A. 1993, ApJ, 412, 479
- Evrard, A. E., Metzler, C. A., & Navarro, J. F. 1996, ApJ, 469, 494
- Faltenbacher, A., Kravtsov, A. V., Nagai, D., & Gottlöber, S. 2005, MNRAS, 358, 139
- Ferland, G. J., Korista, K. T., Verner, D. A., Ferguson, J. W., Kingdon, J. B., & Verner, E. M. 1998, PASP, 110, 761
- Finoguenov, A., Reiprich, T. H., & Böhringer, H. 2001, A&A, 368, 749
- Gottlöber, S., Klypin, A., & Kravtsov, A. V. 2001, ApJ, 546, 223
- Haardt, F., & Madau, P. 1996, ApJ, 461, 20
- Hallman, E. J., Motl, P. M., Burns, J. O., & Norman, M. L. 2006, ApJ, 648, 852
- Henry, J. P. 2000, ApJ, 534, 565
- Henry, J. P., & Arnaud, K. A. 1991, ApJ, 372, 410
- Hu, W. 2003, Phys. Rev. D, 67, 081304
- Ikebe, Y., Reiprich, T. H., Böhringer, H., Tanaka, Y., & Kitayama, T. 2002, A&A, 383, 773
- Kaiser, N. 1986, MNRAS, 222, 323
- ——. 1991, ApJ, 383, 104
- Kennicutt, R. C., Jr. 1998, ApJ, 498, 541
- Kravtsov, A. V. 1999, Ph.D. thesis, New Mexico State Univ.
- Kravtsov, A. V., Klypin, A., & Hoffman, Y. 2002, ApJ, 571, 563
- Kravtsov, A. V., Nagai, D., & Vikhlinin, A. A. 2005, ApJ, 625, 588
- Levine, E. S., Schulz, A. E., & White, M. 2002, ApJ, 577, 569
- Lewis, G. F., Babul, A., Katz, N., Quinn, T., Hernquist, L., & Weinberg, D. H. 2000, ApJ, 536, 623
- Lima, M., & Hu, W. 2004, Phys. Rev. D, 70, 043504
- ------. 2005, Phys. Rev. D, 72, 043006
- Majumdar, S., & Mohr, J. J. 2003, ApJ, 585, 603
- _____. 2004, ApJ, 613, 41
- Markevitch, M. 1998, ApJ, 504, 27
- Markevitch, M., Forman, W. R., Sarazin, C. L., & Vikhlinin, A. 1998, ApJ, 503, 77

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REFERENCES

- Markevitch, M., et al. 2003, ApJ, 583, 70
- Mathiesen, B., Evrard, A. E., & Mohr, J. J. 1999, ApJ, 520, L21
- Mathiesen, B. F., & Evrard, A. E. 2001, ApJ, 546, 100
- Mazzotta, P., Rasia, E., Moscardini, L., & Tormen, G. 2004, MNRAS, 354, 10 Mohr, J. J., Mathiesen, B., & Evrard, A. E. 1999, ApJ, 517, 627
- Motl, P. M., Hallman, E. J., Burns, J. O., & Norman, M. L. 2005, ApJ, 623, L63
- Muanwong, O., Thomas, P. A., Kay, S. T., & Pearce, F. R. 2002, MNRAS, 336, 527
- Nagai, D. 2006, ApJ, in press (astro-ph/0512208)
- Nevalainen, J., Markevitch, M., & Forman, W. 2000, ApJ, 532, 694
- O'Hara, T. B., Mohr, J. J., Bialek, J. J., & Evrard, A. E. 2006, ApJ, 639, 64
- Oukbir, J., & Blanchard, A. 1992, A&A, 262, L21
- Peebles, P. J. E. 1993, Principles of Physical Cosmology (Princeton: Princeton Univ. Press)
- Pierpaoli, E., Borgani, S., Scott, D., & White, M. 2003, MNRAS, 342, 163
- Press, W. H., Teukolsky, S. A., Vetterling, W. T., & Flannery, B. P. 1992, Numerical Recipes in FORTRAN (Cambridge: Cambridge Univ. Press)
- Rasia, E., Mazzotta, P., Borgani, S., Moscardini, L., Dolag, K., Tormen, G., Diaferio, A., & Murante, G. 2005, ApJ, 618, L1
- Rasia, E., et al. 2006, MNRAS, 369, 2013
- Reiprich, T. H., & Böhringer, H. 2002, ApJ, 567, 716
- Seljak, U. 2002, MNRAS, 337, 769
- Spergel, D. N., et al. 2003, ApJS, 148, 175
- Stanek, R., Evrard, A. E., Böhringer, H., Schuecker, P., & Nord, B. 2006, ApJ, 648, 956
- Tegmark, M., et al. 2004, Phys. Rev. D, 69, 103501
- Vikhlinin, A. 2006, ApJ, 640, 710
- Vikhlinin, A., Kravtsov, A., Forman, W., Jones, C., Markevitch, M., Murray, S., & Van Speybroeck, L. 2006, ApJ, 640, 691
- Vikhlinin, A., McNamara, B. R., Forman, W., Jones, C., Quintana, H., & Hornstrup, A. 1998, ApJ, 502, 558
- Vikhlinin, A., VanSpeybroeck, L., Markevitch, M., Forman, W. R., & Grego, L. 2002, ApJ, 578, L107
- Vikhlinin, A., et al. 2003, ApJ, 590, 15
- Voevodkin, A., & Vikhlinin, A. 2004, ApJ, 601, 610
- Voevodkin, A. A., Vikhlinin, A. A., & Pavlinsky, M. N. 2002, Astron. Lett., 28, 366
- Voit, G. M. 2005, Rev. Mod. Phys., 77, 207
- Wang, S., Khoury, J., Haiman, Z., & May, M. 2004, Phys. Rev. D, 70, 123008