

A Novel Cylindrical Overlap-and-Fling Mechanism Used by Sea Butterflies

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Abstract

The clap-and-fling mechanism is a well-studied, unsteady lift generation mechanism widely used by flying insects and is considered obligatory for tiny insects flying at low to intermediate Re . However, some aquatic zooplankters including some pteropod (i.e. sea butterfly) and heteropod species swimming at low to intermediate Re also use the clap-and-fling mechanism. These marine snails have extremely flexible, actively deformed, muscular wings which they flap reciprocally to create propulsive force, and these wings may enable novel lift generation mechanisms not available to insects, which have less flexible, passively deformed wings. Using high-speed stereophotogrammetry and micro-particle image velocimetry, we describe a novel cylindrical overlap-and-fling mechanism used by the pteropod species *Cuvierina atlantica*. In this maneuver, the pteropod's wingtips overlap at the end of each half-stroke to sequentially form a downward-opening cone, a cylinder, and an upward-opening cone. The transition from downward-opening cone to cylinder produces a downward-directed jet at the trailing edges. Similarly, the transition from cylinder to upward-opening cone produces downward flow into the gap between the wings, a leading edge vortex ring, and a corresponding sharp increase in swimming speed. The ability of this pteropod species to perform the cylindrical overlap-and-fling maneuver twice during each stroke is enabled by its slender body and highly flexible wings. The cylindrical overlap-and-fling mechanism observed here may inspire the design of new soft robotic aquatic vehicles incorporating highly flexible propulsors to take advantage of this novel lift generation technique.

KEY WORDS: Leading edge vortex, pteropod, PIV, soft robotics, flexible, insect flight

Summary: Enabled by its highly flexible wings, the swimming pteropod *C. atlantica* generates thrust by using a novel cylindrical 'overlap-and-fling' maneuver twice during each wingstroke.

Running Title: Swimming of the pteropod *C. atlantica*

34 **Introduction**

35 The aerodynamics of flapping flight by insects, birds, and other organisms is highly
36 complex, and many unsteady lift-enhancing flow phenomena have been discovered (Weis-
37 Fogh, 1973; Dickinson et al., 1999; Bomphrey et al., 2017). The best known of these is the
38 clap-and-fling mechanism, originally described by Weis-Fogh (1973). The clap-and-fling
39 mechanism is widely used by insects and seems to be obligatory in the smallest insects
40 (Kolomenskiy et al., 2011; Sane, 2016; Cheng and Sun, 2018). In the clap-and-fling
41 mechanism, the wings closely approach each other at the end of the recovery stroke (the clap
42 phase) and force the flow in the gap between them downwards in a jet-like flow to enhance
43 lift generation. The wings then rotate apart from each other about their trailing edges (the
44 fling phase), creating a V-shaped gap into which air flows. In this way, insects overcome the
45 starting Wagner effect, create a low pressure region between the wings, and create enhanced
46 leading edge vortices.

47 The clap-and-fling mechanism has been widely studied since its discovery. Lighthill
48 (1973) performed theoretical analysis with simplifying assumptions, showing how the clap-
49 and-fling mechanism increases lift generation. Using a dynamically scaled laboratory model,
50 Maxworthy (1979) visualized the leading edge vortices formed in the fling phase and found
51 they comprise a large part of the force generated. Ellington (1984) reported variations of the
52 clap-and-fling maneuver, including the near-clap-and-fling and the clap-and-peel, in various
53 insect species. Lehmann et al. (2005) used dynamically scaled fruit fly wing models to find
54 that the clap-and-fling mechanism enhanced the resultant force by 17%. Kolomenskiy et al.
55 (2011) concluded from their theoretical and computational 2D model that viscosity enhances
56 lift generation in the ‘fling’ as compared to the inviscid case. Computational fluid dynamics
57 studies of the clap-and-fling mechanism have recently highlighted the importance of wing
58 flexibility and porosity in overcoming the large forces needed for tiny insects to clap their
59 wings together and fling them apart (Miller and Peskin, 2005; Miller and Peskin, 2009;
60 Santhanakrishnan et al., 2014) and have shown that flexible wings can reduce the drag force
61 generated during the fling by about 50% (Miller and Peskin, 2009).

62 Research by Satterlie et al (1985) and Borrell et al (2005) on the swimming of the
63 shell-less marine snail *Clione limacina* and its congener *Clione antarctica* suggested that the
64 clap-and-fling maneuver is not limited to aerial flight. Based on high speed filming of
65 tethered organisms, Chang and Yen (2012) showed that the tiny (~2 mm) shelled pteropod
66 *Limacina helicina* similarly uses a version of the clap-and-fling maneuver with its pair of

67 highly flexible, wing-like appendages (called parapodia) formed from a modified foot
68 structure. Murphy et al (2016) used volumetric particle image velocimetry to measure the
69 kinematics and flows generated by *L. helicina* performing its clap-and-fling mechanism,
70 findings which were verified by Adhikari et al. (2016) in *Limacina helicina antarctica*.
71 Similarly, Karakas et al. (2018) found that the heteropod *Atlanta selvagensis* performs a clap-
72 and-fling maneuver using its one flexible appendage and its rigid, coiled shell. Here we report
73 a novel variation of the clap-and-fling mechanism used by another sea butterfly species,
74 *Cuvierina atlantica*, which we call a cylindrical overlap-and-fling.

75

76 **Materials and methods**

77 **Species and environment**

78 A variety of shelled pteropod species including *C. atlantica*, *Hyalocylis striata*,
79 *Heliconoides inflatus*, and *Limacina bulimoides* were collected from offshore of Bermuda
80 using a Reeve net with 150 μm mesh size and a specialized 20 l cod end. Specimens were
81 collected during a nighttime cruise, kept in collected seawater, and brought back to a
82 temperature-controlled chamber at the Bermuda Institute of Ocean Sciences (BIOS) in May
83 2017. The zooplankton were sorted and visually identified under a stereomicroscope and
84 were then stored in filtered sea water at an *in situ* temperature of 21 °C. To ensure that
85 specimens were healthy, experiments were conducted immediately upon return from the
86 cruise and, since the pteropods did not live long after capture, experiments were completed
87 within 36 hours of collection. This mixed assemblage of pteropod species was placed
88 together in the experimental systems described below. At least two *C. atlantica* individuals
89 were included in this assemblage, and these could be differentiated in the recordings based on
90 shell length.

91 **3D Kinematics setup**

92 A photogrammetry system comprising two synchronized high-speed monochrome
93 Edgertronic cameras (Sanstreak Corp., San Jose, CA, USA) was used to measure the three-
94 dimensional swimming kinematics of the pteropods at high magnification. The cameras,
95 lights, and aquarium were mounted on optical rails and a breadboard to rigidly support the
96 system. The two cameras were arranged perpendicular to each other and were equipped with
97 200 mm Nikon macro lenses with apertures set to f/32 to maximize the depth of the field
98 (~12 mm). Both cameras filmed at 600 Hz with a resolution of 1024×912 pixels and viewed a

99 glass aquarium with $30 \times 30 \times 30 \text{ mm}^3$ ($W \times D \times H$) inner dimensions and 2.5 mm wall
100 thickness, which was filled with $0.2 \text{ }\mu\text{m}$ filtered seawater collected with the pteropods to a
101 depth of 28 mm. The field of view of each camera was at least 10 mm above the tank bottom
102 such that only actively swimming pteropods were recorded. The focal planes of the cameras
103 were set to the middle of the aquarium so that only freely swimming pteropods not
104 interacting with the walls would be recorded. The spatial resolution of the cameras was 14.3
105 $\mu\text{m pixel}^{-1}$. Collimated backlighting for each camera was provided by an LED fiber optic
106 illuminator with a dual arm gooseneck (Dolan-Jenner Industries, Lawrence, MA, USA). The
107 camera system was spatially calibrated prior to the experiments using the direct linear
108 transform technique (Abdel-Aziz and Karara, 1971; Hedrick, 2008). Briefly, a scaled
109 microscope slide held vertically and oriented 45° to both cameras was positioned at 25
110 predefined locations within the common field of view within the filled aquarium using a
111 microtranslator (PT3/M, Thorlabs, Newton, New Jersey, USA). Three points on the slide
112 imaged at these 25 locations provided 75 calibration points covering the measurement
113 volume. These points provided the calibration coefficients mapping the 2D camera
114 coordinates into the 3D world coordinates using DLTdv5 (Hedrick, 2008). Up to
115 approximately 10 pteropods of diverse sizes and species were selected for the experiments
116 and were carefully transferred to the test aquarium. Little interference was observed between
117 swimming animals since swimming bouts were intermittent and alternated with periods of
118 lying on the tank bottom. The camera system was manually triggered when a pteropod swam
119 into the field of view common to both cameras. Four videos of *C. atlantica* representing two
120 different individuals were collected. However, because of the high magnification, parts of the
121 pteropod were often outside the field of view of one camera for some part of these videos.
122 Thus, a 0.43 s segment from one recording event in which the animal swam upwards through
123 the field of view and in which both wings were fully visible for almost two complete wing
124 strokes was chosen for further analysis. As shown in Fig. 1, ten different points on the
125 pteropod were manually tracked in each frame using DLTdv5 in order to quantify the
126 pteropod wing and body kinematics (Hedrick, 2008). Kinematics data from one video in
127 which the pteropod swam upwards through the field of view are presented in the Results.

128 **PIV setup**

129 Brightfield back-illuminated 2D micro particle image velocimetry (μPIV) was applied
130 to quantify the flow structures and velocity fields around the freely swimming pteropods
131 (Gemmell et al., 2014). In this system, a $2 \times$ extra-long working distance (ELWD)

132 microscopic objective (#46-142, Mitutoyo) with an image-generating tube lens (#58-520,
133 Edmund Optics) provided a depth of field of 91 μm , resulting in a measurement plane width
134 (MPW) of approximately 250 μm (Koutsiaris, 2012). The advantage of this approach is its
135 ability to provide a narrow measurement plane width without the use of a laser. A high-speed
136 camera (Phantom VEO 640S) recorded at 1400 Hz with a spatial resolution of 2560×1600
137 pixels. The field of view was $12.43 \times 7.77 \text{ mm}^2$ (vertical \times horizontal) and was vertically and
138 horizontally centered within the tank in order to minimize wall and free surface effects. The
139 test tank was seeded with 2-3 μm mean diameter algae (*Nannochloropsis oculata*), which
140 work well as tracking particles because they are natural food items for pteropods (Thabet et
141 al., 2015) and because no light scattering by the particles is required. The test section was
142 illuminated with a telecentric backlight illuminator (#62-760, Edmund Optics). Similar to the
143 kinematics experiments, multiple pteropods were placed in the aquarium simultaneously.
144 Recordings were manually triggered when an animal swam through the focal plane. Six
145 videos of *C. atlantica* were recorded, but only in one video did this species perform a
146 complete stroke cycle while well positioned in the focal plane. This video, which recorded
147 the same individual for which kinematics data were analyzed, was chosen for further flow
148 analysis. Image processing was applied to the raw μPIV images to invert the images, apply
149 Gaussian filtering to remove out-of-focus particles, and algorithmically mask animals using
150 local intensity values. Velocity fields were calculated by applying multi-pass cross-
151 correlation using a 50% overlap, beginning with a 64×64 window size in the first pass and
152 decreasing to 32×32 window sizes in subsequent passes. Erroneous vectors were removed by
153 the universal outlier detection method. Particle seeding density was high, with about 20
154 particles distributed in each 64×64 interrogation window. The resulting vector fields
155 comprised 160×100 vectors with a vector grid spacing of 0.0766 mm.

156 **Results**

157 Fig. 1 shows a three-dimensional model of the shelled pteropod *C. atlantica* with the
158 tracked points labeled, including three points on the body (*c-e*), the wingtips (*a-b*), the
159 leading edges (*f* and *h*) and trailing edges (*g* and *i*) of the right and left wing chords, and a
160 point on the top edge of the shell (*j*, coinciding with the origin of the body-centered
161 coordinate system). A global (XYZ) coordinate system and a body-centered (X'Y'Z')
162 coordinate system, which translates and rotates with the animal, also are defined in Fig. 1. As
163 measured from the 3D coordinates taken from the processed kinematics videos, the adult
164 pteropod has a body length of $l_b = 9 \pm 0.03 \text{ mm}$ (a mean \pm standard deviation value measured

165 from point c to d over 116.7 ms), a wingspan of $l_s=9.4 \pm 0.1$ mm (a mean \pm standard
 166 deviation value measured between points a and b at the three time points in the recording
 167 when the wings are fully outstretched, as in Fig. 1A), and a chord length of $c=3.0 \pm 0.27$ mm
 168 (a mean \pm standard deviation value measured between points f and g over 408.3 ms). It is
 169 important to note that these mean and standard deviation values represent multiple
 170 measurements of the same animal taken at different time points within the same recording.
 171 The animal beats its wings at a mean frequency of $f=5$ Hz and has a mean swimming speed \bar{u}
 172 of 35 mm s^{-1} . These animals thus swim in an intermediate Reynolds number regime in which
 173 both inertial and viscous forces are important. A body-based Reynolds number $Re_b = \bar{u}l_b/\nu$
 174 and chordwise Reynolds number $Re_c = 2\varphi fl_f c/\nu$ are defined here, where l_f is the length of
 175 one wing, φ is wing stroke amplitude, and ν is the kinematic viscosity of the sea water at 21
 176 °C. Given that *C. atlantica* has a wing stroke amplitude of $\varphi = 160^\circ$, this pteropod species
 177 thus has a $Re_b = 300$ and $Re_c = 420$, placing its Re_c in the same order of magnitude as that
 178 of fruit flies (Vogel, 1966). As shown in Fig. 1B, the animal's pitching angle θ is defined as
 179 the angle between the Z and Z' axes. The wing bending angle β is defined for each wing
 180 using points on the wingtip, mid-wing chord, and body, as shown in Fig. 1C for the left wing.

181 Fig. 2 shows a model of *C. atlantica* which illustrates the motion of its wings as the
 182 animal performs an idealized cylindrical overlap-and-fling maneuver as well as simplified
 183 schematics comparing the cylindrical overlap-and-fling maneuver to the classic clap-and-
 184 fling maneuver used by insects. High speed visualization, wingtip and body kinematics, and
 185 the resulting flow fields throughout one wing stroke are then presented in order to illustrate
 186 the principle of the cylindrical overlap-and-fling mechanism and how it is used by *C.*
 187 *atlantica*. Thus, Fig. 3 shows the *C. atlantica* wing stroke cycle from two synchronized
 188 orthogonal high speed cameras (Movie 1). Due to the highly flexible nature of the wings, the
 189 outer edge of the right wing in both perspectives is highlighted in red for clarity. Fig. 4 shows
 190 the time history of the right and left wingtip positions (in the body-centered coordinate
 191 system), body angle θ , instantaneous swimming speed U , and the wing bending angle $\bar{\beta}$
 192 averaged between the right and left wings. Fig. 5 shows flow fields recorded in a plane
 193 slightly offset from the pteropod's sagittal plane (Movie 2). The approximate location of this
 194 plane relative to the pteropod is shown in Fig. 2.

195 As shown in Fig. 2A and Fig. 3, at the beginning of the wingbeat cycle ($t' = 0$), the
 196 right and left wings are highly bent along their respective spans, with $\bar{\beta}$ up to 160° (Fig. 4B),
 197 and overlap each other to form a circular cylinder on the posterior side of the animal. This

198 wingtip overlap is reflected in the positive Y' position of the right wingtip and the negative Y'
199 position of the left wingtip in Fig. 4B. As the power stroke commences ($t' = 0.1$), the wings
200 separate from each other as the right and left wingtip Y' positions cross (Fig. 4B). As they
201 expand from their cylindrical configuration, $\bar{\beta}$ decreases (Fig. 4B), the X' wingtip positions
202 slightly decrease (Fig. 4A), and the Z' positions increase (Fig. 4C) as the wings elevate and
203 open away from the body simultaneously. As shown in Fig. 2B and Fig. 3, the leading edges
204 of the wings open from their cylindrical shape more quickly than the trailing edges, thus
205 transforming the cylinder into a conical shape with a larger opening on the top than on the
206 bottom. The result of this fling part of the cylindrical overlap-and-fling maneuver is that a
207 vortex ring seems to form on the wings' leading edges which feeds flow into the gap opening
208 between the wings, a concept illustrated in Fig. 2A-C. For example, Fig. 5 shows a clockwise
209 vortex developing on the right wing's leading edge at $t' = 0.12$ and strengthening as the wings
210 further separate at $t' = 0.15$ - 0.19 . This fling results in a strong downward flow adjacent to the
211 animal's shell, with flow speeds reaching a maximum of 121 mm s^{-1} at $t' = 0.19$. This
212 maneuver coincides with a sharp increase in swimming speed from 10 mm s^{-1} to 30 mm s^{-1} as
213 shown in Fig. 4D.

214 Subsequently, the X' wingtip positions continue to increase as the wing stroke
215 continues toward the anterior side of the animal (Fig. 4A). By $t' = 0.25$ in Fig. 3, the wings
216 are fully extended as the Y' wingtip coordinates reach their maximum negative and positive
217 values for the right and left wings, respectively (Fig. 4B). The wing bending angle $\bar{\beta}$
218 approaches zero and subsequently becomes negative as the fully extended wings cross to the
219 anterior side of the animal (Fig. 4B). As shown in Fig. 5 at $t' = 0.23$, a strong clockwise
220 vortex remains on the animal's posterior side and is transported downwards; no significant
221 flow around the wing is seen at this time because the view is obstructed by the other wing and
222 because the focal plane is near the root of the wing (Fig. 2C). As shown in Fig. 4D, this
223 anterior wing flapping coincides with an increase in θ as the top of the shell pitches
224 posteriorly and with the local maximum swimming speed of 50 mm s^{-1} at approximately $t' =$
225 0.26 . The flow field at $t' = 0.33$ in Fig. 5 show a tip vortex on the right wing; it is likely that
226 this vortex wraps around the animal to connect with the previously shed vortex on the
227 animal's posterior side.

228 At $t' = 0.4$ in Fig. 3, the wings have almost finished their respective power strokes and
229 have traveled to the anterior side of the animal, as shown by the Y' wingtip coordinates
230 converging in Fig. 4B. Here the wingtips overlap, as shown by the crossing traces of the

231 wingtip Y' positions and form a cone. This cone initially has a wider diameter on the bottom
232 than on the top but becomes cylindrical as the wings are pulled back towards the shell, as
233 illustrated in Fig. 2D-F. The local minima in the X' wingtip positions at approximately $t' =$
234 0.5 in Fig. 4A also illustrate how the wings must bend to close into a cylinder. The resulting
235 flow, a downward jet of fluid squeezed out from the cone between the wings, is shown at $t' =$
236 0.40 in Fig. 5. This jet has flow speeds of 78.5 mm s^{-1} , feeds into the existing tip vortex, and
237 rolls up to form what is likely a small vortex ring which travels downwards anterior to the
238 animal. This concept is illustrated in Fig. 2D-F. The weaker flow speeds generated by this
239 cylindrical overlap do not result in an increase in swimming speed as instead the animal
240 continues to decelerate during this time period (Fig. 4D). The downward jet thus may serve to
241 clear the previously generated vortex structures in preparation for the next half-stroke
242 (Dickinson, 1996).

243 At $t' = 0.53$ in Fig. 3 and $t' = 0.51$ in Fig. 5, the pteropod has finished its power stroke
244 and, with its wing bending angle (Fig. 4B) and swimming speed at a minimum, begins its
245 recovery stroke. The pteropod thus performs a second fling maneuver similar to that
246 performed during the power stroke. Specifically, the wings begin to unfold from their
247 cylindrical configuration in which the wingtips overlap with each other, evidenced by
248 increasing $\bar{\beta}$ (Fig. 4B). This unfolding also is shown by the increase in the X' wingtip
249 positions and crossing of the Y' wingtip traces in Fig. 4A and Fig. 4B, respectively. As the
250 wings unfold, the leading edges open before the trailing edges, again transforming the
251 cylinder into a cone, as shown in Fig. 2B and at $t' = 0.66$ in Fig. 3. This second fling
252 maneuver again causes a vortex to form around the wing's leading edges and fluid to flow
253 into the opening conical gap between the wings, resulting in a sharp increase in the
254 pteropod's swimming speed (Fig. 4D). This downward flow between the wings is shown at $t' =$
255 0.64 in Fig. 5 and has a maximum speed of 94 mm s^{-1} , slightly less than the maximum
256 speed measured during the power stroke's fling. This vortex and downward flow continue to
257 develop at $t' = 0.70$ in Fig. 5 as the pteropod continues with its recovery stroke ($t' = 0.75$ in
258 Fig. 3). The body angle reaches its minimum ($\theta = -7.4^\circ$) near the end of the recovery stroke
259 and subsequently begins to increase, as shown in Fig. 4D. At the end of the recovery stroke ($t' =$
260 0.92 in Fig. 3), the swimming speed decreases to 15 mm s^{-1} and the wings perform a second
261 overlap maneuver as they fold together to form a cone which transforms into a cylinder. The
262 wings are thus in position to perform the fling associated with the next power stroke.

263 Discussion

264 The lift-enhancing clap-and-fling maneuver as used by most insects and some marine
265 snails consists of the close apposition of largely flat wings (Ellington, 1984; Murphy et al.,
266 2016; Karakas et al., 2018). Apposing and separating these flat wings in close proximity to
267 each other during the clap and fling phases, respectively, requires a large amount of power,
268 especially at $Re < 10$, though this drag-induced energetic expense is reduced somewhat by
269 increased wing flexibility and porosity (Miller and Peskin, 2005; Miller and Peskin, 2009;
270 Santhanakrishnan et al., 2014). In contrast, the pteropod species studied here uses its highly
271 flexible wings to sequentially form a downward-opening cone, a cylinder, and an upward-
272 opening cone at the end of each half stroke. We call this novel lift-enhancing technique the
273 cylindrical overlap-and-fling. Though serving the same function as in insects, the geometrical
274 configuration of the wings is dramatically different. This novel geometry allows this pteropod
275 species to take advantage of the lift enhancement offered by the clap-and-fling maneuver
276 without the necessity of wing apposition. The cylindrical overlap-and-fling maneuver may
277 thus offer the possibility of avoiding the large drag associated with the classic ‘planar’ clap-
278 and-fling maneuver. However, the Reynolds number at which *C. atlantica* uses the overlap-
279 and-fling ($Re_b=300$ and $Re_c=420$) is somewhat larger than the Reynolds number at which
280 most insects use the clap-and-fling. Indeed, the clap-and-fling maneuver is thought to be
281 obligatory for tiny insects flying at Reynolds numbers of 100 or less. However, large insects
282 also perform the clap-and-fling maneuver in high Re flight, especially to generate extra lift
283 (e.g. *Locusta migratoria* in climbing and turning flight (Cooter and Baker, 1977), the
284 butterfly *Vanessa atalanta* (Srygley and Thomas, 2002), and some other large insects
285 carrying loads (Marden, 1987)). Indeed, Marden (1987) showed that use of clap-and-fling by
286 various insects, small birds, and bats increases the lift per unit flight muscle mass by about
287 25% as compared to flight in the absence of the clap-and-fling maneuver, and Lehmann et al.
288 (2005) measured a 17% increase in lift generation in a dynamically scaled *Drosophila* wing
289 model ($Re \sim 100-200$) which performs a near-clap-and-fling maneuver. It is likely that
290 pteropods employing a version of the clap-and-fling at $Re_c=5-35$ (e.g. *L. helicina*; Murphy et
291 al., 2016) and the overlap-and-fling at higher Re (e.g. *C. atlantica*) enjoy similar lift
292 augmentation. However, it is unknown whether the cylindrical overlap-and-fling maneuver is
293 employed by smaller pteropod species or juvenile *C. atlantica* individuals swimming at Re
294 characteristic of tiny insect flight. The need for such extreme and complex wing deformation
295 may possibly limit use of the overlap-and-fling maneuver to somewhat larger wing sizes and
296 larger Re .

297 A second significant difference in the ways that pteropods and insects use this type of
298 clap-and-fling maneuver is that *C. atlantica* performs two complete overlap-and-fling
299 maneuvers in each wing stroke while all insects studied to date and some other pteropod
300 species (e.g. *L. helicina*) are only able to perform one. This ability in *C. atlantica* is enabled
301 by its highly flexible wings which may bend 160° in both anterior and posterior directions
302 and by the fact that its body and elongated shell, a more recent evolutionary shift in pteropod
303 morphology as compared to spiraled shell pteropods (Peijnenburg et al. in review; Janssen
304 and Peijnenburg, 2017), do not interfere with its wing motion. Insects, on the other hand,
305 have relatively less flexible wings, and clapping at the end of the power stroke has not been
306 reported, likely because the presence of their bodies prevents the wings from clapping at the
307 end of the power stroke (Lighthill, 1973; Wootton, 1981; Cheng and Sun, 2017). Similarly,
308 some other pteropod species, though they do have highly flexible wings, are prevented from
309 clapping twice during each stroke because of the presence of their spiral shaped shell (Chang
310 and Yen, 2012; Adhikari et al., 2016; Murphy et al., 2016). In contrast, enabled by its slender
311 body and extremely large stroke angle, the atlantiid heteropod *A. selvagensis* performs a
312 double clap-and-fling on each stroke without significant bending of its appendages (Karakas
313 et al., 2018). The ability to use the clap-and-fling maneuver twice during each stroke was
314 theoretically considered by Lighthill (1973) who hypothesized that this double use would
315 create a circular vortex ring on each half-stroke in the animal's wake, thereby maximizing
316 downward momentum per unit kinetic energy. Though volumetric velocity measurements are
317 needed for confirmation, it seems likely that its large wing stroke amplitude and low
318 wingbeat frequency enable *C. atlantica* to indeed create two independent vortex rings
319 throughout each stroke cycle. The wake in this scenario would represent a real life case of
320 Dickinson's (1996) idealized fish propelling itself via large amplitude pectoral fin strokes and
321 thus creating a series of disconnected vortex loops in its wake. Indeed, the separation between
322 the vortices created by the power and recovery strokes seen in Fig. 5 show that this is likely
323 the case. Regardless of the wake structure, the additional lift provided by using the overlap-
324 and-fling mechanism twice during each stroke is beneficial in supporting the heavy shell of
325 *C. atlantica* as it daily migrates at least 100 m upwards to the ocean surface to feed
326 (Wormuth, 1981).

327 Another significant difference between pteropods' overlap-and-fling and insects'
328 clap-and-fling is that *C. atlantica* actively bends its wings whereas the wings of insects are
329 passively deformed depending on the aerodynamic load (Wootton, 1981; Wootton, 1990;
330 Combes and Daniel, 2003a; Combes and Daniel, 2003b). Indeed, this pteropod is able to bend

331 its wings along the spanwise direction to such an extent that its wingtips overlap at the end of
332 each half stroke. The active flexibility of pteropod appendages is due to their unique
333 morphology and wing structure. Pteropod wings are modified from the molluscan foot
334 without any rigid support (Borrell et al., 2005), and these organisms have hydrostatic
335 skeletons which are supported by fluid pressure (Szymik and Satterlie, 2017). Further, the
336 wings of pteropods have layers of parallel muscles oriented at different angles across the
337 wing (Satterlie et al., 1985). This unique wing structure enables active spanwise wing
338 bending and high flexibility, with wing bending angle amplitudes up to 160° in *C. atlantica*
339 (Fig. 4B). In contrast, insects have exoskeletons and their wings, which are actuated at their
340 roots, have a complex network of veins with connecting membranes to support the forces on
341 the wings (Wootton, 1981). Active spanwise wing deformation is thus absent, and passive
342 wing deformation in insects is mostly limited to an amplitude of less than 40 degrees (Lucas
343 et al., 2014). Wing flexibility in insects has been shown to be beneficial with higher energetic
344 efficiency and aerodynamic performance (Vanella et al., 2009; Colin et al., 2012; Kodali et
345 al., 2017; Wong and Rival, 2017). Wong and Rival (2017) showed that passive spanwise
346 bending of $30\text{--}40^\circ$ stabilizes the leading edge vortex (LEV), thus providing augmented lift for
347 an extended period of time. In contrast, these researchers found that active spanwise bending
348 of the same magnitude generates a much stronger yet less stable LEV than that generated
349 either with passive bending or in the absence of bending, thus generating higher levels of
350 instantaneous lift. *Cuvierina atlantica* utilizes passive spanwise bending as the wings separate
351 after each overlap-and-fling. The mid-span of each convex-shaped wing thus leads during the
352 first part of each half-stroke. Midway through each stroke (i.e. leading into the overlap
353 phase), the convexity of the wing reverses as the tip begins to lead, thus changing into an
354 active spanwise bending configuration. This mechanism may provide an effective way to
355 actively control the strength and stability of the LEV over the wing stroke and thus to
356 manipulate the lift generation.

357 In addition to controlling spanwise bending, pteropods are also able to actively
358 control chordwise bending owing to their fluid-filled wings which have infinite degrees of
359 freedom in motion. This chordwise deformation is actively controlled by the fluid pressure
360 and by muscle fibers in the wing, with the control system based on complex feedback from
361 the surrounding flow conditions (Szymik and Satterlie, 2017). Active control over chordwise
362 flexibility likely enables *C. atlantica* to perform the overlap-and-fling maneuver as it moves
363 its overlapping wings from a cylindrical configuration to a conical configuration. Chordwise
364 wing flexibility similarly enables insects and micro aerial vehicles to generate greater lift-to-

365 drag ratios when performing the clap-and-fling or clap-and-peel maneuver. For example,
366 Miller and Peskin (2009) numerically showed a 50% decrease in peak drag in the fling due to
367 wing flexibility and an increase in lift force in some cases. Similarly, flow and force
368 measurements on a pair of flexible model wings performing clap-and-peel showed relatively
369 higher force generation as compared to rigid wings (Percin et al., 2017).

370 Though all pteropod species swim by flapping a pair of structurally similar highly
371 flexible parapodia, swimming kinematics may vary substantially among different species
372 based on size and shell morphology. The species studied here, *Cuvierina atlantica*, uses a
373 unique overlap-and-fling maneuver at the end of each half stroke and pitches its large,
374 elongated shell by approximately 20° while swimming. In contrast, the much smaller, coiled
375 shell thecosomes *L. helicina* (Chang and Yen, 2012; Murphy et al., 2016) and *L. helicina*
376 *antarctica* (Adhikari et al., 2016) use a modified version of the clap-and-fling maneuver only
377 at the end of the power stroke and flap their wings against the shell at the end of the recovery
378 stroke. In addition, these thecosomes pitch their shells to a much greater degree, by up to 60°
379 in *L. helicina* and up to 110° in *L. helicina antarctica*. These coiled shells possess much less
380 rotational drag and moment of inertia in comparison to the elongated shell of *C. atlantica*,
381 which retards such a large degree of pitching. In addition, the different Reynolds number
382 regimes in which the tiny coiled shell species and *C. atlantica* operate could contribute to
383 their different swimming kinematics. The coiled shell species generally operate in a highly
384 viscous regime at Reynolds numbers less than 100 whereas *C. atlantica*, with its elongated
385 shell, operates at a Reynolds number an order of magnitude higher ($Re=100-600$). The
386 relative importance of inertial and viscous forces may have thus led this species to adopt a
387 more streamlined shell in order to reduce the pressure drag, which would be important at this
388 larger Re . Finally, though it would be expected that the larger species would have a lower
389 wingbeat frequency, comparing the wingbeat frequency of *C. atlantica* with the tiny coiled
390 shell species is difficult because of ambient water temperature (and thus viscosity)
391 differences. *Cuvierina atlantica* lives at a water temperature of ~21° C (which has a viscosity
392 of $1.05 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$) and beats its wings at ~5 Hz. In contrast, *L. helicina* lives at ~12-16°C
393 and has a wingbeat frequency of 5-10 Hz, and *L. helicina antarctica* lives at ~0°C (which has
394 a higher viscosity of $1.83 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$) and has a lower wingbeat frequency of 2-3 Hz (Chang
395 and Yen, 2012; Adhikari et al., 2016; Murphy et al., 2016). The higher seawater viscosity at
396 colder temperatures thus corresponds to lower wingbeat frequencies, though temperature-
397 induced differences in metabolism may also play a role here (Pétavy et al., 1997).

398 The swimming of the thecosome species studied here also bears some similarity to
399 that of the shell-less gymnosomes *C. limacina* (Satterlie et al., 1985; Szymik and Satterlie,
400 2011) and *C. antarctica* (Borrell et al., 2005). *Cuvierina atlantica* and these gymnosomes
401 have a similar elongated shape, have approximately the same body length, and flap their
402 wings in similar, nearly horizontal stroke planes. However, compared to *C. atlantica*,
403 gymnosomes have relatively short, low aspect ratio wings, and this difference in wing
404 morphology affects their ability to perform a version of the overlap-and-fling maneuver.
405 During slow swimming, the wingtips of *C. limacina* approach but do not touch each other.
406 However, during fast swimming, it appears that *C. limacina* may perform a version of the
407 overlap-and-fling maneuver at the end of the downstroke as the wings fold over each other
408 close to the body (Szymik and Satterlie, 2011). Because the wings are shorter, the void
409 between them is compressed in comparison to the cylindrical void formed by the wings of *C.*
410 *atlantica*. However, similar to *C. atlantica*, gymnosome wings unfold in an upward-opening
411 cone, presumably in order to gain lift from a leading edge vortex. Another difference between
412 *C. atlantica* and gymnosomes is the wingbeat frequency. Gymnosomes living at an ambient
413 seawater temperature of 0°C flap their wings at ~1-3 Hz. This lower beat frequency may be
414 due to the higher viscosity of colder seawater, metabolic and physiologic constraints, and the
415 lack of a heavy calcareous shell. The lack of a shell in gymnosomes would result in a smaller
416 wing loading and thus allow a smaller wingbeat frequency for propulsion (Pétavy et al.,
417 1997). Further, the low aspect ratio wings of gymnosomes are not efficient for long periods
418 of swimming but are well suited for generating high forces necessary for maneuvering.
419 Correspondingly, gymnosomes swim slowly most of the time (at $Re < 100$) but swim very fast
420 ($Re > 1000$) for short periods of time when escaping or hunting. In contrast, *C. atlantica* has a
421 larger wing aspect ratio and is thus well suited to swim the long distances necessary for diel
422 vertical migration while benefiting from the double overlap-and-fling which aids in
423 generating the forces needed to carry the heavy shell.

424 It is also worth noting that the cylindrical overlap-and-fling mechanism observed here
425 employs both suction- and jet-based propulsion mechanisms. Specifically, *C. atlantica*
426 manipulates its wing positions to generate a low pressure suction region on the upper wing
427 surface in the fling phase and to generate thrust by pushing the flow downward during the
428 overlap phase. It is likely that suction dominates in thrust generation because, as shown in
429 Figure 4d, the animal accelerates during the fling phase and decelerates during the overlap
430 phase. Many other efficient aquatic swimmers such as jellyfish and lampreys similarly rely
431 on suction for thrust generation (Gemmell et al., 2015). Indeed, the kinematics of the overlap-

432 and-fling mechanism bear some similarity to the bell kinematics of jellyfish medusae (Dabiri
433 et al., 2005; Gemmell et al., 2018) and jellyfish-inspired robots (Nawroth et al., 2012;
434 Ristroph and Childress, 2014; Ren et al., 2019). Finally, the swimming mechanisms of
435 marine molluscs in general (Borrell et al., 2005; Szymik and Satterlie, 2011; Chang and Yen,
436 2012; Adhikari et al., 2016; Murphy et al., 2016; Zhou and Mittal, 2017; Zhou and Mittal,
437 2018) and the cylindrical overlap-and-fling mechanism observed here in particular may serve
438 as bioinspiration for new soft robotic aquatic vehicles propelled by highly flexible propulsors
439 capable of taking advantage of this and other novel lift generation techniques.

440

441

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446

447 **Competing interests**

448 The authors declare no competing or financial interests.

449

450 **Author contributions**

451 F.K., D.W.M., and A.E.M conceived and designed the experiment. F.K. and D.W.M carried
452 out experimental work and data analysis. A.E.M. procured and identified the animals. F.K.,
453 D.W.M., and A.E.M. wrote the manuscript. All authors approved the final manuscript.

454

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461

462 **Supplementary movies**

463 **Movie 1. Visualization of swimming *C. atlantica* taken from two orthogonal high speed**
464 **cameras.** Movies acquired at 600 frames per second and played back at 25 frames per
465 second.

466 **Movie 2. Flow measurements of *C. atlantica* swimming.** Vectors indicate flow direction
467 and magnitude, and color contours represent vorticity. Recorded at 1400 frames per second
468 and played back at 25 frames per second.

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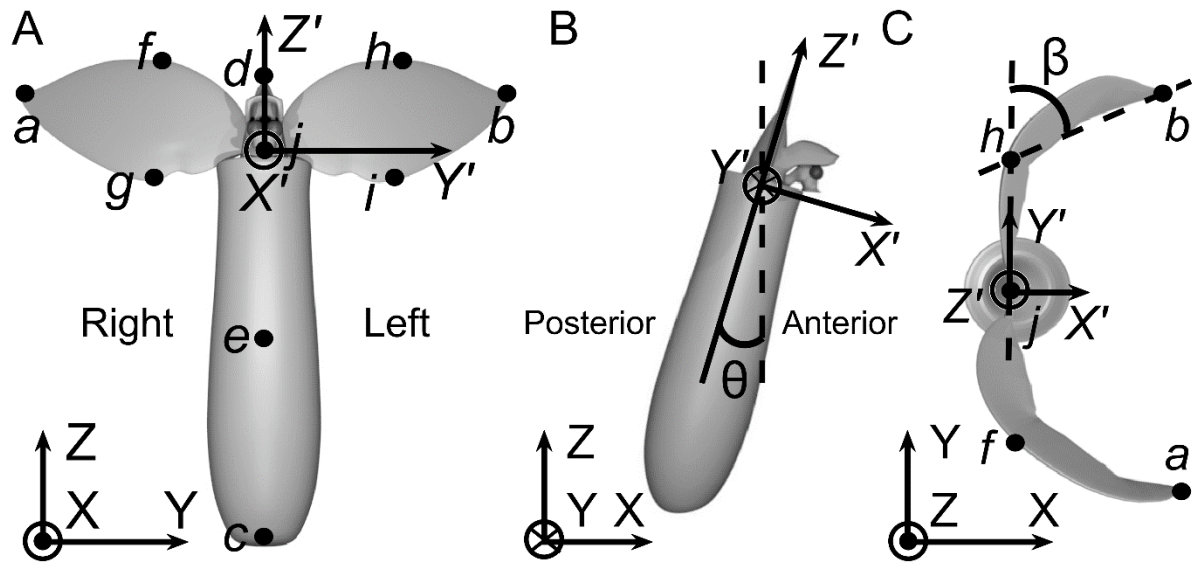
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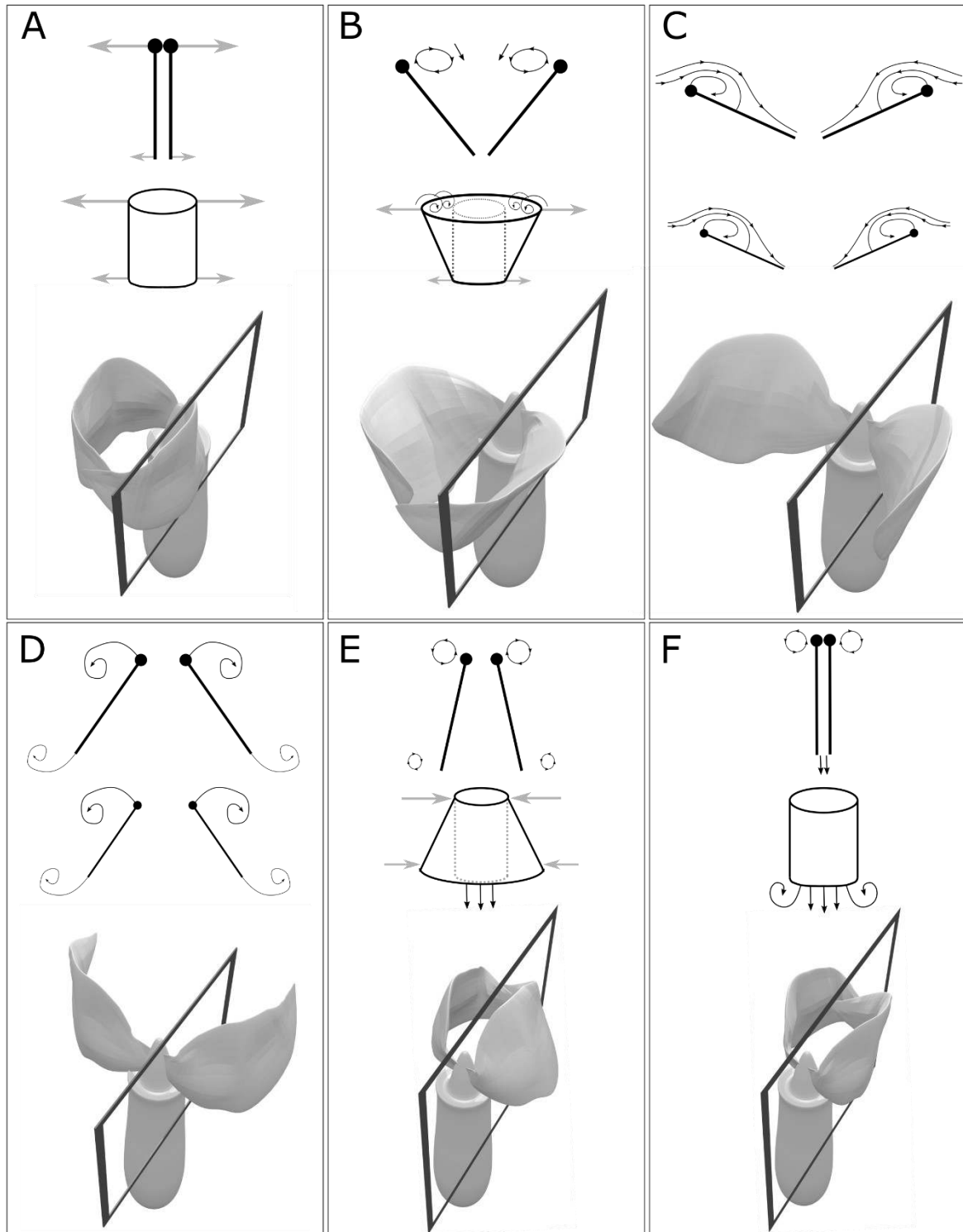
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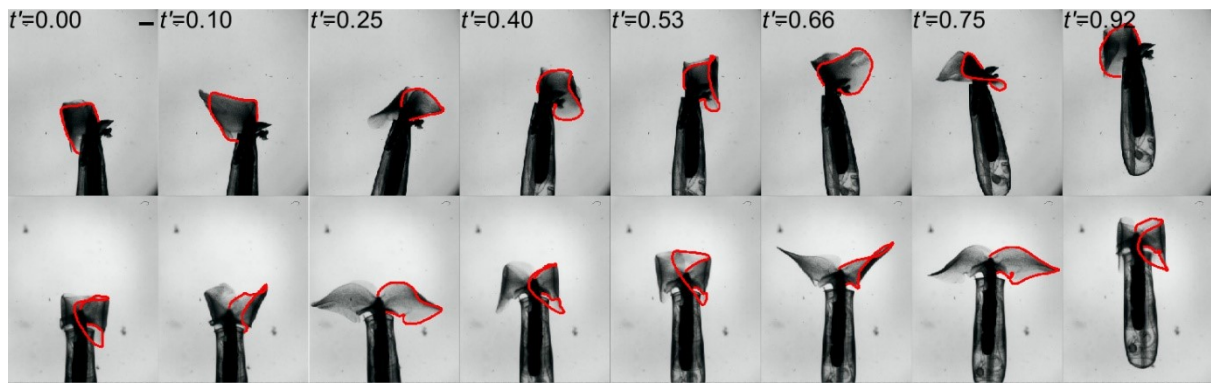
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Fig. 1. *Cuvierina atlantica* morphology and coordinate systems. (A) Front view, (B) side view, and (C) top view showing the locations of the tracked points (*a-j*), the definition of the body angle θ , the definition of the wing bending angle β for the left wing, the global coordinate system (XYZ), and the body-centered (X'Y'Z') coordinate system. The origin of the X'Y'Z' coordinate system is located at point *j*. The wing bending angle for the right wing is similarly calculated using points *f* and *a*.



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Fig. 2. Schematic of model pteropod wings performing the cylindrical overlap-and-fling maneuver as compared to planar wings performing the clap-and-fling maneuver. (A-C) Illustration of flow into opening cylinder during the fling. Wing orientation during fling at (A) $t'=0$, (B) $t'=0.1$, and (C) $t'=0.25$. (D-F) Illustration of flow exiting cylinder during the overlap. Wing orientation at (D) $t'=0.35$, (E) $t'=0.4$, and (F) $t'=0.53$. Within each panel, the top, middle, and bottom figures represents the traditional clap-and-fling maneuver, the overlap-and-fling maneuver, and a 3D rendering of the wing positions of *C. atlantica* performing the overlap-and-fling maneuver, respectively. The rectangle in each 3D rendering represents the location of the flow measurement focal plane relative to the animal in Fig. 5.



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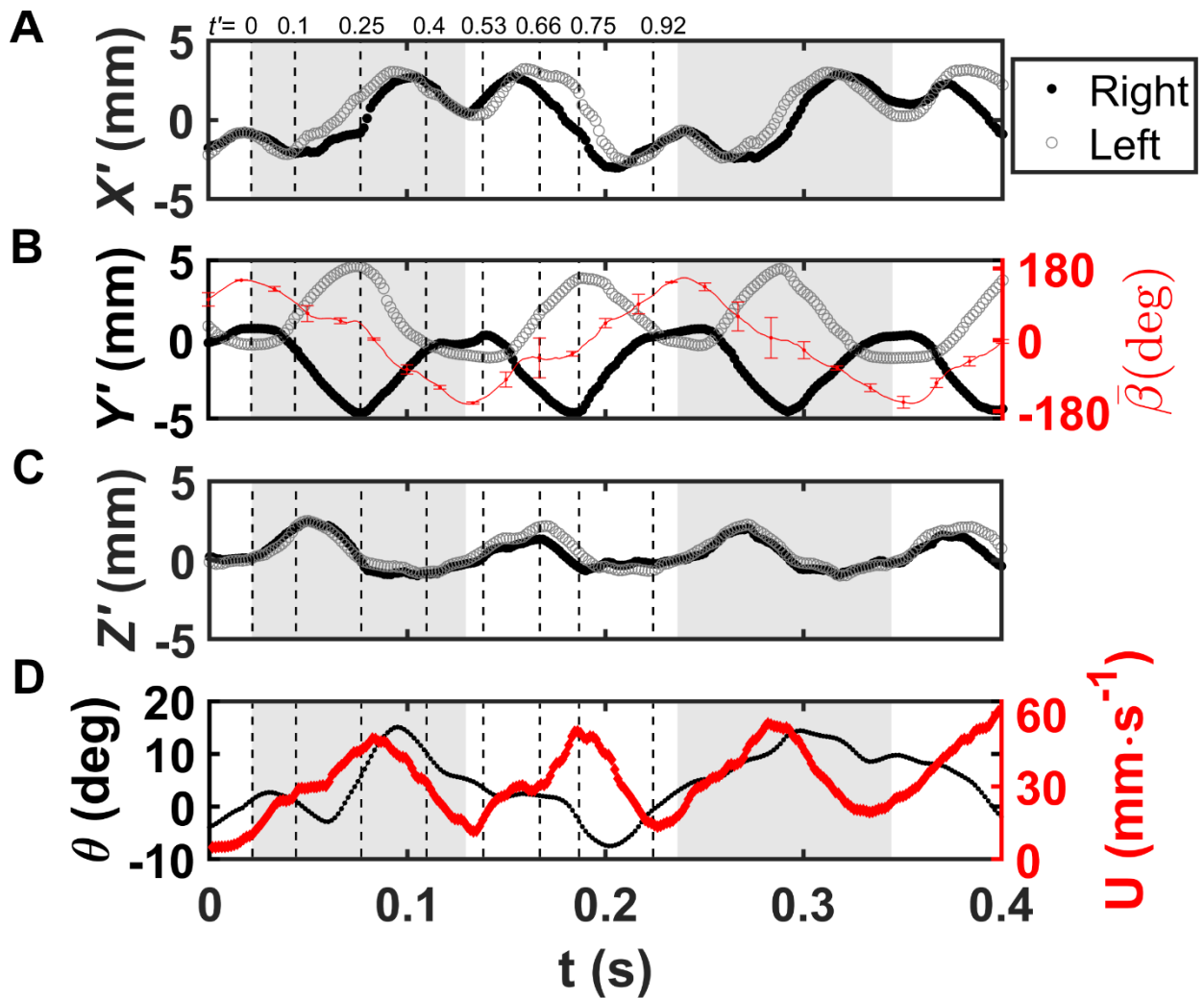
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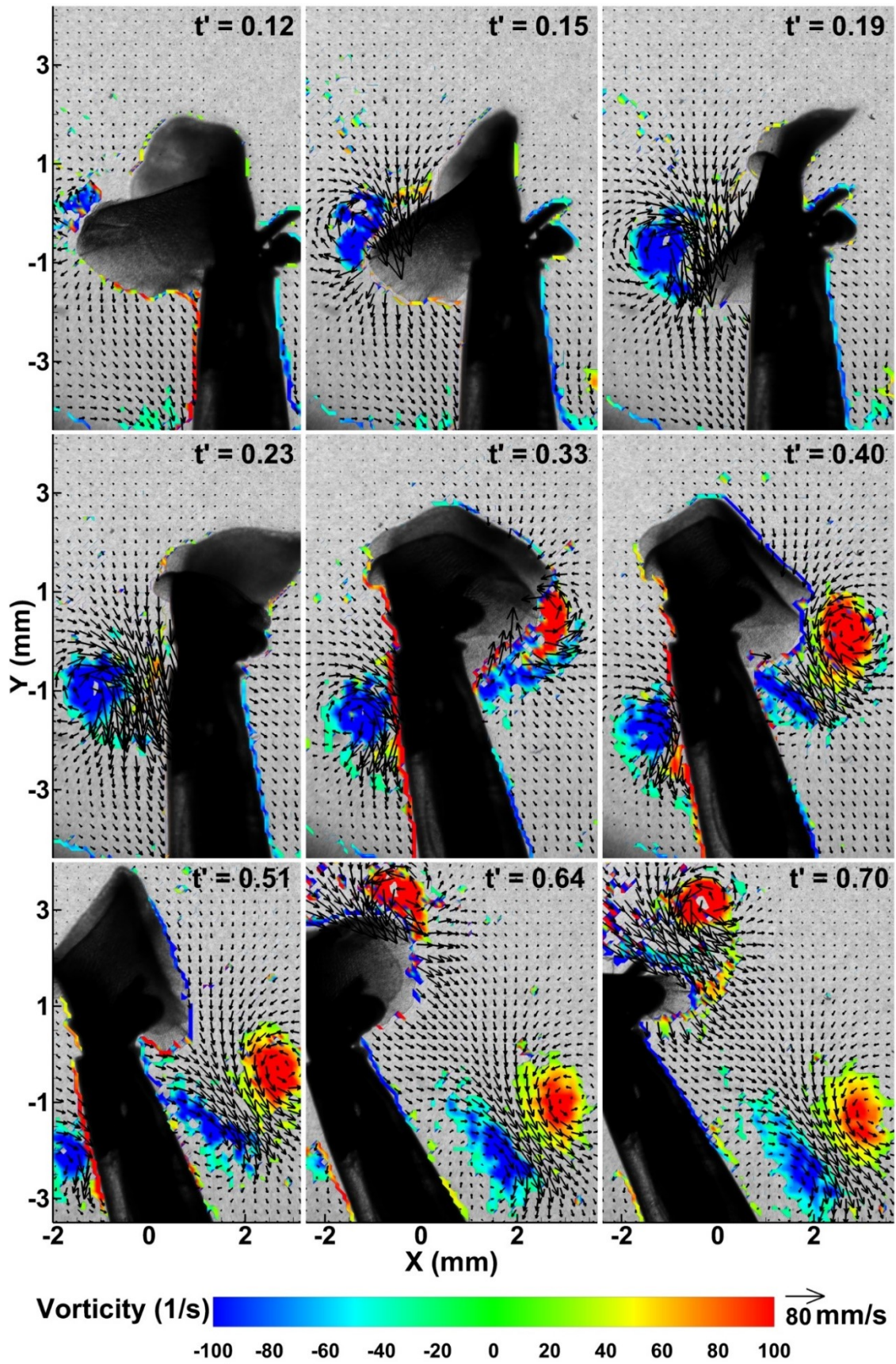
Fig. 3. Pteropod wing stroke. Sequence of synchronized images acquired from two orthogonal perspectives illustrating one stroke cycle. The top row views the animal from its right side, and the bottom row views the animal from its posterior. The variable t' is time normalized by the stroke period (200 ms). The scale bar represents 1 mm. The right wing of the animal is outlined in both views.



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 617 **Fig. 4. Pteropod wing and body kinematics.** Wing and body kinematics of *C. atlantica* over
 618 slightly less than two stroke cycles. (A-C) Right and left wingtip trajectories in the body-
 619 centered coordinate system. (B) mean and standard deviation of wing bending angle $\bar{\beta}$
 620 averaged between the left and right wings. (D) Body angle θ and swimming speed U . The
 621 power stroke is shaded gray. Dashed vertical lines correspond to non-dimensionalized times
 622 shown in Fig. 3.

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Fig. 5. Flow field. Time sequence of the velocity and vorticity fields generated as *C. atlantica* performs a cylindrical overlap-and-fling maneuver. Color contours represent the z-component of vorticity, and vectors indicate flow direction and magnitude. The measurement

629 plane intersects the animal as shown in Fig. 2. The variable t' is time normalized by the stroke
630 period (200 ms).