

1 A numerical investigation of isobaric combustion strategy in a compression ignition engine

2 Xinlei Liu^{1,*}, Hammam Aljabri¹, Balaji Mohan¹, Rafiq Babayev¹,

3 Jihad Badra², Bengt Johansson¹, Hong G. Im¹

4 ¹Clean Combustion Research Center (CCRC), King Abdullah University of Science and Technology

5 (KAUST), Thuwal, Saudi Arabia

6 ²Fuel Technology Division, R&DC, Saudi Aramco, Dhahran, Saudi Arabia

7 *Corresponding author: Xinlei Liu; Email: xinlei.liu@kaust.edu.sa

8 **Abstract**

9 Three-dimensional computational fluid dynamic simulations were conducted to study the means
10 to achieve isobaric combustion mode in a compression ignition engine, which is intended to be used in
11 the high-efficiency double compression-expansion engine (DCEE) concept. Compared to the
12 conventional diesel combustion mode, the isobaric combustion mode generated a significantly lower
13 peak combustion pressure, which was beneficial for the high load extension. For both combustion
14 modes, the ignition was triggered downstream of the nozzle, with the heat release dominated by
15 $\text{HCO} + \text{O}_2 = \text{CO} + \text{HO}_2$, while the injection-combustion duration for the isobaric combustion mode was
16 significantly longer. The effects of swirl ratio, spray angle, and piston geometries on the isobaric
17 combustion at various engine loads were also investigated. The higher swirl ratio resulted in a higher
18 heat transfer loss and thus lower thermal efficiency. Due to the higher air utilization rates and lower
19 heat transfer losses, cases with spray angles of 140° and 150° generated the higher thermal efficiencies.
20 The piston bowl geometry was found to have a significant impact on the mixing and combustion
21 processes, especially at high engine load conditions. For the conditions under study, the original piston
22 geometry with a swirl ratio of 0 and a spray angle of 140° demonstrated the highest thermal efficiency

23 for the isobaric combustion mode. The results of this work will provide guidance in the practical design
 24 and implementation of the DCEE concept.

25 **Keywords:** Isobaric combustion; Compression ignition; Double compression expansion engine;
 26 Thermal efficiency; Diesel

Nomenclature

AMR	Adaptive mesh refinement	LP	Low-pressure
C ₂ H ₄	Ethylene	LTC	Low-temperature combustion
CA ATDC	Crank angle after the top dead center	NO _x	Nitric oxides
CAC	Charge air cooler	PCCI	Premixed charge compression ignition
CDC	Conventional diesel combustion	ϕ	Equivalence ratio
CFD	Computational fluid dynamics	REXR	Representative exothermic reaction
CI	Compression ignition	ROI	Rate of injection
CO	Carbon monoxide	PPC	Partially premixed combustion
CR	Compression ratio	SA	Spray angle
DCEE	Double compression expansion engine	SI	Spark ignition
DI	Direct injection	SOI	Start of injection
EGR	Exhaust gas recirculation	SW	Swirl ratio
EVO	Exhaust valve opening	T	Temperature
GHG	Greenhouse gas	TDC	Top dead center
HP	High-pressure	THC	Total hydrocarbon
HRR	Heat release rate	TKE	Turbulent kinetic energy
HTR	Heat transfer rate	1D	One-dimensional
ICE	Internal combustion engine	3D	Three-dimensional
IVC	Intake valve closing		

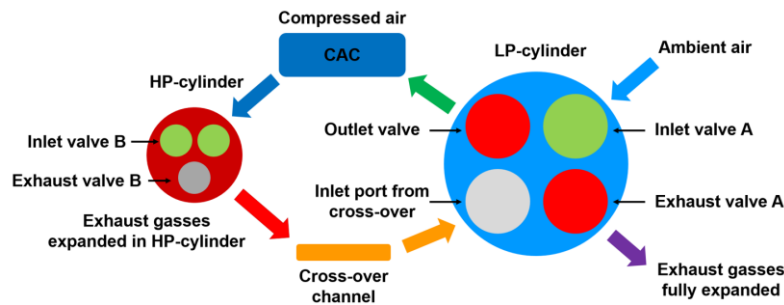
27 1. Introduction

28 The greenhouse gas (GHG) emissions from the utilization of petroleum-derived fuels are a major
 29 concern for regulatory authorities, who are enforcing stringent CO₂ and tailpipe emission regulations
 30 on the transportation sector. To fulfill the stringent CO₂ targets, the engine fuel economy, and hence, the
 31 thermal efficiency of internal combustion engines (ICE) need to be further improved [1-3].

32 Compared to the spark ignition (SI) engines whose compression ratio (CR) is limited by the
33 knocking issue and the intake throttle losses [4], the compression ignition (CI) engines can achieve
34 higher CR and efficiencies by employing non-premixed combustion using direct injection (DI)
35 strategies with variable injection timing. While the maximum CR is limited by the material, some large
36 marine engines operate at CR higher than 20, which extends their indicated thermal efficiency up to 55%
37 [5]. For land-use engines, however, it is too heavy and expensive to adopt such a large-size engine setup.
38 As such, improvements in thermal efficiency require systematic optimization in order to minimize
39 various losses associated with gas exchange, combustion, heat transfer, and mechanical friction [6, 7],
40 along with the reduction of pollutant emissions like nitric oxides (NO_x) and soot [8, 9]. Over the past
41 decades, various advanced combustion strategies were proposed, including the homogeneous charge
42 compression ignition (HCCI) [9], the premixed charge compression ignition (PCCI) [10], and partially
43 premixed combustion (PPC) [11, 12], all of which aim to achieve higher efficiency and lower emissions.
44 In fact, the HCCI, PCCI, and PPC concepts all belong to the category of low-temperature combustion
45 (LTC), which adopts exhaust gas recirculation (EGR) to control the combustion process [13-16]. The
46 primary difference for these three concepts is the different start of injection (SOI) timings, which will
47 lead to the different levels of charge stratification accordingly.

48 Considering that the CR is the primary factor that increases the thermodynamic efficiency, Lam et
49 al. [5] recently proposed the double compression expansion engine (DCEE) concept, which adopts two-
50 stage compression and expansion processes to achieve high thermal efficiency at a wider range of
51 operating conditions and more flexibility in optimization strategies. Figure 1 illustrates a schematic of
52 the DCEE concept [5]. It consists of two 4-stroke machines, a large-size low-pressure (LP) unit, and a
53 small-size high-pressure (HP) unit. The LP unit performs two tasks: 1. it inducts fresh air, compresses

54 it (for the first time), and transfers through the charge air cooler (CAC) into the HP unit; 2. it receives
 55 exhaust gas of the HP unit and performs the second expansion stage before discharging the gas into the
 56 atmosphere. The HP unit is essentially a combustion cylinder of a conventional diesel engine, where
 57 fresh air is compressed (for the second time) and combustion products and expanded (for the first time).
 58 Due to the small size of the HP unit, heat transfer and friction losses are both minimized. A one-
 59 dimensional (1D) modeling study revealed that the DCEE concept could potentially achieve brake
 60 thermal efficiency of 56 % [17].



61
 62 **Fig. 1. Schematic of the DCEE concept [5].**

63 Owing to the excessive pressure (up to 300 bar) in the HP unit, it is desirable for the DCEE concept
 64 to adopt an isobaric combustion strategy instead of a typically preferred isochoric combustion strategy
 65 [18, 19]. Okamoto and Uchida's work [20] has shown that it is possible to realize isobaric combustion
 66 using three injectors. More recently, Babayev et al. [21] reported that the isobaric combustion could be
 67 achieved using only a single high-pressure injector with multiple injection events. They also compared
 68 the combustion performance of the CDC mode and isobaric combustion mode, which demonstrated
 69 comparable thermal efficiencies. Note that the peak combustion pressure for the CDC mode was
 70 significantly higher than the isobaric combustion mode, suggesting lower friction losses for the latter.

71 The previous studies related to the isobaric combustion strategy are mostly focused on
 72 experimental or 1D simulation research [5, 18]. Therefore, this work intends to further enhance our

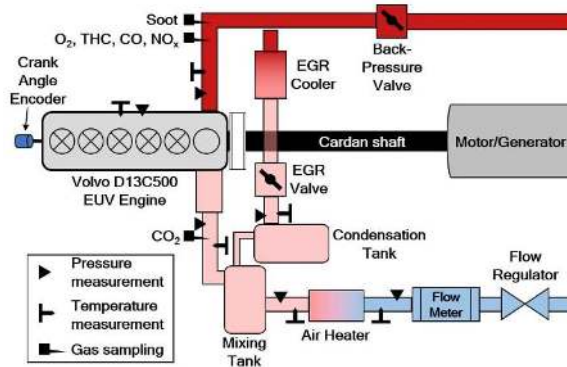
73 understanding of the isobaric combustion strategy using the three-dimensional (3D) computational
74 dynamics fluid (CFD) approach. A data-processing method developed by Liu et al. [22, 23] was also
75 adopted to compare the different heat release features of the isobaric and CDC combustion modes.
76 Following that, the effects of some significant engine design parameters, including swirl ratio, spray
77 angle, and piston geometries, on engine combustion performance and emissions at various engine load
78 conditions were investigated. This work will provide valuable guidance for the future development of
79 the practical applications of the DCEE concept.

80 **2. Experimental and modeling setup**

81 **2.1. Experimental setup**

82 Experimental work was performed by Babayev et al. [18] on a modified single-cylinder diesel
83 engine. Figure 2 depicts the schematic of the engine setup and Table 1 lists the engine specifications
84 and operating conditions [18]. Detailed descriptions of the engine setup can be found in [18, 21]. During
85 the experiment, the engine speed was kept at 1200 rpm. The intake pressure and temperature were fixed
86 at about 3.1 bar and 353 K, respectively. A solenoid-valve common-rail injector was used for fuel
87 injections with an injection pressure of 2300 bar. For the isobaric combustion mode, the target was to
88 achieve a constant compression pressure of 150 bar, [due to limitations of the air-intake system](#). Four
89 different injection strategies involving 2 to 5 injection events were tested, corresponding to the different
90 engine load conditions. For comparison, a CDC case was also tested under the engine load similar to
91 the 4-injection case. Table 2 shows the detailed information of the injected mass and the SOI timings.
92 The rate of injection (ROI) was measured by Babayev et al. [18] using a novel in-situ measurement
93 technique. The results are shown in Fig. 3, which were adopted as input parameters for the engine
94 combustion simulations.

95



96

Fig. 2. Schematic of the engine setup [18].

Table 1. Engine specification and operating condition.

Engine configuration	Single-cylinder, water-cooled
Number of valves	4
Bore/stroke (mm)	131/158
Connecting rod length (mm)	255
Displacement volume (L)	2.13
Geometric compression ratio	17:1
Swirl ratio	0
Intake valve close timing ($^{\circ}$ CA ATDC)	-160
Exhaust valve open timing ($^{\circ}$ CA ATDC)	140
Common-rail injector	7 holes, injection angle 150° , 0.225 mm nozzle
Engine speed (rpm)	1200
Intake air pressure (bar)	3.1
Intake air temperature (K)	353
EGR ratio (%)	0

97

Table 2. Injection details [18].

	2 inj.	3 inj.	4 inj.	5 inj.	CDC
Total injected mass (mg/cycle)	20.7	64.7	117.6	222.0	119.1
IMEP (bar)	1.3	5.9	11.1	19.7	11.3
SOI/Dur. 1 st inj. ($^{\circ}$ CA ATDC)	-3.0/2.4	-3.0/2.4	-3.0/2.4	-3.0/2.4	-1.5/8.4
SOI/Dur. 2 nd inj. ($^{\circ}$ CA ATDC)	0.5/2.4	0.5/2.6	0.5/2.2	0.5/2.4	-
SOI/Dur. 3 rd inj. ($^{\circ}$ CA ATDC)	-	4.5/3.4	4.5/3.4	4.5/3.2	-
SOI/Dur. 4 th inj. ($^{\circ}$ CA ATDC)	-	-	9.0/4.4	9.0/10.4 ^a	-
SOI/Dur. 5 th inj. ($^{\circ}$ CA ATDC)	-	-	-	12.7/10.4 ^a	-

^a Denotes the total duration for the 4th and 5th injections.

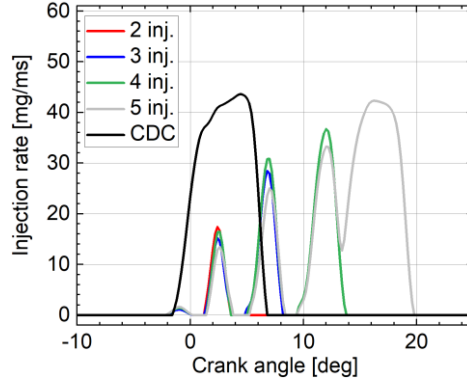


Fig. 3. Measured ROI profiles [18].

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100 2.2. Computational setup

101 2.2.1. Spray and combustion models

102 The 3D CFD modeling study was performed using the CONVERGE 2.4 package [24]. A
 103 Lagrangian-parcel method was utilized to describe the liquid spray dynamics [25]. The Kelvin-
 104 Helmholtz Rayleigh-Taylor model without a breakup length was adopted to predict the droplet breakup
 105 [26], the no-time-counter algorithm was adopted to predict the droplet collision [27], and the Frossling
 106 correlation approach was used to simulate droplet evaporation [28]. The SAGE detailed chemical
 107 kinetics solver [29] coupled with the reduced n-heptane mechanism developed by Wang et al. [30] was
 108 adopted for the diesel combustion simulation. Detailed descriptions of these modules can be found in
 109 [31].

110 2.2.2. Turbulence model

111 The renormalization group k- ϵ model was utilized to simulate the turbulence [32]. The modeled
 112 Reynolds stress is given by,

$$113 \quad \tau_{ij} = -\overline{\rho u'_i u'_j} = 2\mu_t S_{ij} - \frac{2}{3}\delta_{ij} \left(\rho k + \mu_t \frac{\partial \overline{u_i}}{\partial \overline{x_i}} \right) \quad (1)$$

114 in which the turbulent kinetic energy, turbulent viscosity, and mean strain rate tensor are respectively
 115 defined as,

116
$$k = \frac{1}{2} \widetilde{u'_i u'_i} \quad (2)$$

117
$$\mu_t = C_\mu \rho \frac{k^2}{\varepsilon} \quad (3)$$

118
$$S_{ij} = \frac{1}{2} \left(\frac{\partial \widetilde{\mu}_i}{\partial \widetilde{x}_j} + \frac{\partial \widetilde{\mu}_j}{\partial \widetilde{x}_i} \right) \quad (4)$$

119 In equation (3), C_μ is a model constant and ε is the dissipation of turbulent kinetic energy.

120 **2.2.3. Heat transfer model**

121 In our previous work, three different heat transfer models proposed by O'Rourke and Amsden [33],
122 Han and Reitz [34], and Angelberger [35] were adopted to simulate the isobaric engine combustion
123 process [36]. The results showed that the Angelberger model underpredicts the wall heat fluxes while
124 the Han and Reitz model overpredicts the wall heat fluxes. Therefore, this work adopted the O'Rourke
125 and Amsden model as the most accurate wall-function-based approach tested for predicting the heat
126 transfer process in engine applications.

127 **2.2.4. Computational mesh**

128 Figure 4 shows the schematic of the computational domain. Since the piston shape is axisymmetric
129 and the injector has 7 holes, a 51.4°-sector mesh was adopted to reduce computational expenses. Besides,
130 the adaptive mesh refinement (AMR) module was activated, with which a finer mesh is generated
131 dynamically where the computational field needs to be refined. A base mesh of 2.0 mm and an AMR
132 scale of 3.0 were adopted, which generated the minimum mesh size of 0.25 mm. Based on the previous
133 research [22, 37, 38], this mesh setup can achieve grid-convergence. The simulations started from the
134 intake valve closing (IVC) timing (-160° crank angle after the top dead center (CA ATDC)) and ended
135 at the exhaust valve opening (EVO) timing (140° CA ATDC), implying only closed-cycle modeling.

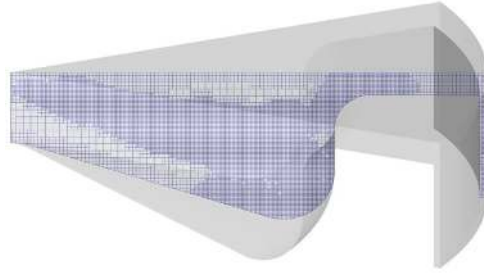


Fig. 4. Schematic of the computational domain.

2.2.5. Data-processing approach

A data-processing technique developed by Liu et al. [22, 23] was adopted to investigate the detailed chemical kinetics processes of the engine combustion heat release. In this method, the calculated 3D CFD results, together with the chemical kinetics mechanism, were taken as inputs. Instantaneous reactive source terms were computed by considering each cell as a perfectly stirred reactor [37, 39, 40]. For the analysis of the heat release features, the representative reaction which yielded the highest exothermic heat release rate (REXR) was used. [More details about the method can be referred to \[22, 23\].](#)

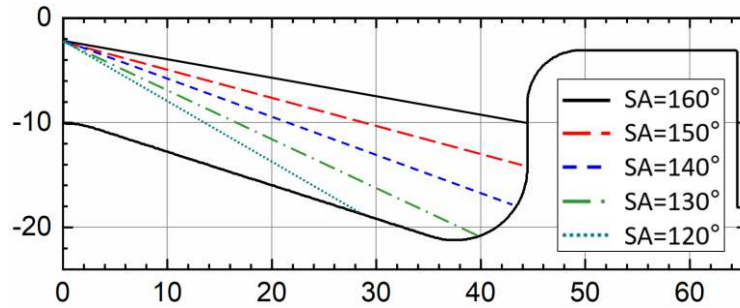
2.2.6. Parametric study cases

Swirl ratio (SW), spray angle (SA), and piston geometry are three of the most significant engine design parameters [41, 42]. As a result, a parametric modeling study was performed to analyze their effects on engine combustion performance and emissions, with the baseline case having the swirl ratio of 0, spray angle of 150° , and original piston geometry. Table 3 lists the parametric cases. For each studied parameter, the other parameters were the same as the baseline case. Figure 5(a) depicts the schematic of the five different spray angles, and Fig. 5(b) depicts the four different piston geometries, including the original (G1), shallow-type (G2), deep-type (G3), and toroidal-type (G4) geometries, respectively. Note that the chamber volume and squish height of the four geometries were kept the same

155 to maintain a constant compression ratio.

Table 3. Parametric cases.

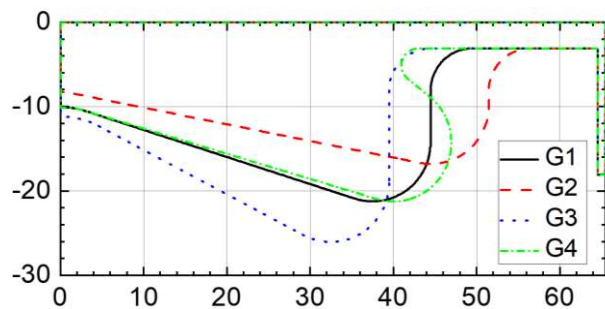
Parameter	Value
Swirl ratio	0, 1, 2, 3
Spray angle	160°, 150°, 140°, 130°, 120°
Geometry	G1, G2, G3, G4



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(a) Different spray angles.



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(b) Different piston geometries.

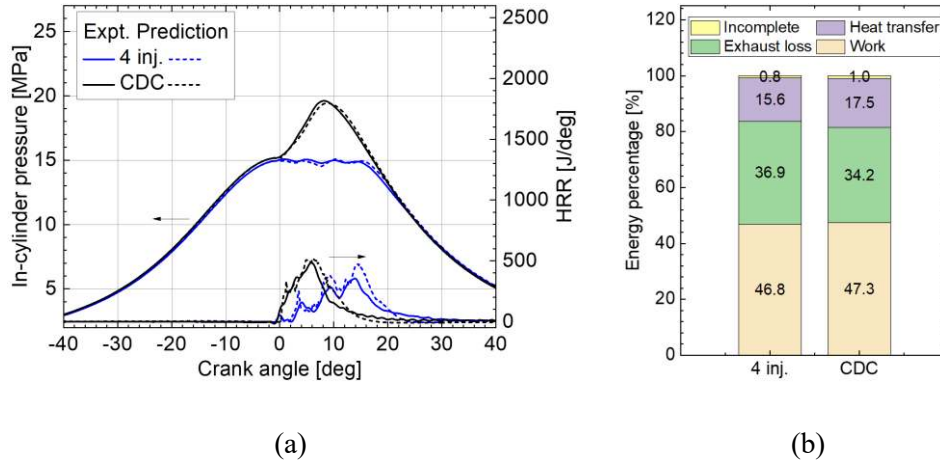
160 **Fig. 5.** Schematics of the different (a) spray angles and (b) piston geometries. Axis unit: mm.

161 3. Results and discussions

162 3.1. Comparison of the CDC and isobaric combustion

163 Figures 6(a) shows the experimental and predicted pressure and HRR profiles, while Fig. 6(b)
164 shows the predicted energy distribution for the CDC and the 4-injection isobaric cases. Table 4
165 summarizes the experimental and predicted indicated thermal efficiency (ITE) and emissions. The
166 simulated cases are able to predict the experimental results for both the CDC and isobaric combustion

167 cases reasonably well. Only the THC and CO emissions are underpredicted, which may be attributed to
 168 the uncertainties in the adopted chemical kinetic mechanism and wall heat losses in the crevice region.
 169 Also, this work adopted n-heptane only to represent diesel combustion chemistry, which could also lead
 170 to the discrepancy. Note that, compared to the isobaric combustion mode, the CDC produces a
 171 significantly higher peak pressure. As a consequence, it is preferable to adopt the isobaric combustion
 172 mode for the DCEE concept from the durability and mechanical efficiency standpoints. Although the
 173 4-injection isobaric case has a slightly lower ITE with its intrinsically late combustion phasing, the
 174 unused energy leaves the HP unit as an exhaust loss. The heat transfer loss, on the other hand, is reduced
 175 with the isobaric cycle. Recall that, unlike the heat transfer loss, the HP unit's exhaust energy can be
 176 further recovered by the LP unit of the DCEE, which should yield an overall higher thermal efficiency
 177 [19].



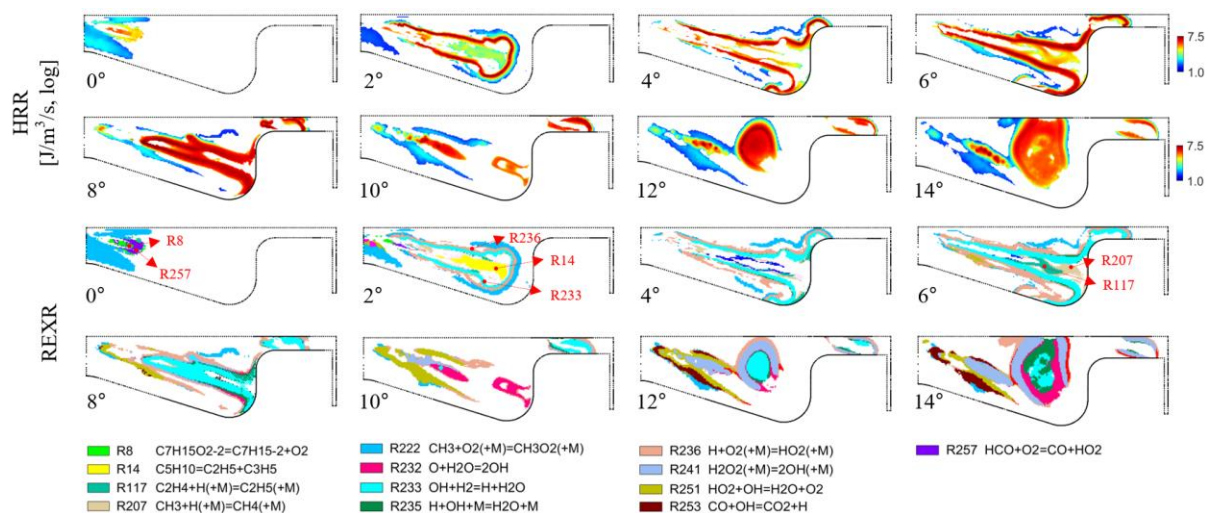
178
 179
 180 **Fig. 6.** Comparison of the (a) experimental and predicted pressure and HRR profiles and (b) predicted
 181 energy distributions for the CDC and 4 inj. cases.

Table 4. Experimental and predicted ITE and emissions for the CDC and 4 inj. cases.

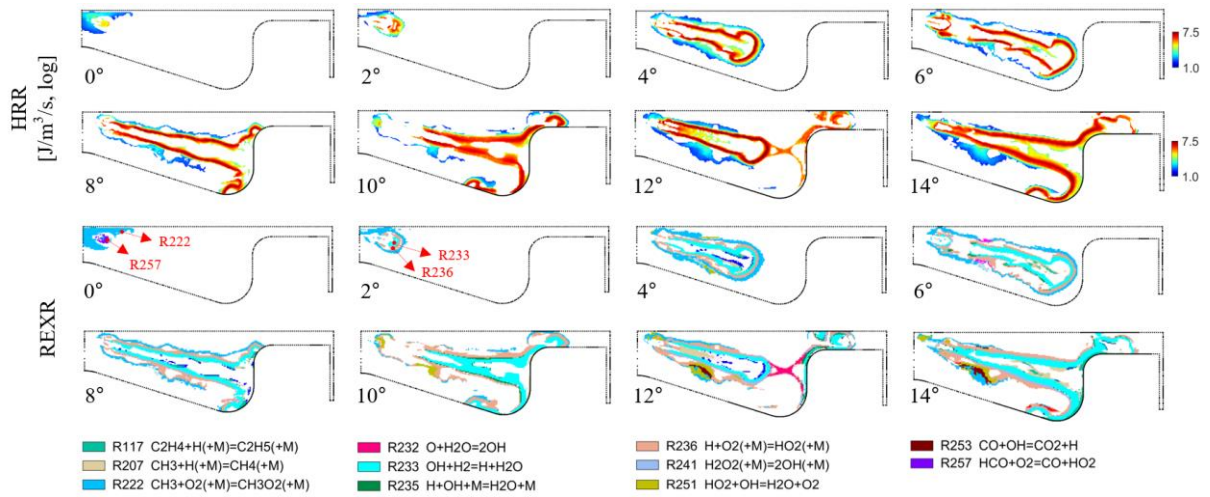
Parameters	Expt. (4 inj.)	Prediction (4 inj.)	Expt. (CDC)	Prediction (CDC)
ITE (%)	47.0	46.8	47.2	47.3
NOx (g/kW-h)	16.0	13.8	29.1	18.7

Soot (mg/kW-h)	0.49	0.58	0.71	0.60
CO (g/kW-h)	0.165	0.048	0.116	0.041
THC (g/kW-h)	0.166	0.0166	0.142	0.009

182 To further compare the heat release features between the CDC and isobaric combustion modes, Fig.
183 7 shows the predicted distributions of the HRR and the corresponding REXR regions for the CDC case
184 and the 4-injection isobaric case, respectively. For both cases, the chemical ignitions (when the peak
185 temperature reaches $(T_{ini} + T_{peak})/2$ [43]) are initiated just downstream of the injector tip, with the
186 heat release dominated by the reaction R257 ($\text{HCO} + \text{O}_2 = \text{CO} + \text{HO}_2$). At 2°CA ATDC, substantial heat is
187 released at the peripheries of the fuel jet, where the reactions R233 ($\text{OH} + \text{H}_2 = \text{H} + \text{H}_2\text{O}$) and R236
188 ($\text{H} + \text{O}_2(+\text{M}) = \text{HO}_2(+\text{M})$) dominate. Note that until 6°CA ATDC, significant heat release is caused by the
189 reactions R117 ($\text{C}_2\text{H}_4 + \text{H}(+\text{M}) = \text{C}_2\text{H}_5(+\text{M})$) and R207 ($\text{CH}_3 + \text{H}(+\text{M}) = \text{CH}_4(+\text{M})$) which occur inside the
190 intensely reacting jet peripheries of the CDC case. This inhibits the rapid consumption of fuel and
191 promotes the formation of soot precursors like acetylene [23, 44].



(a) CDC case.

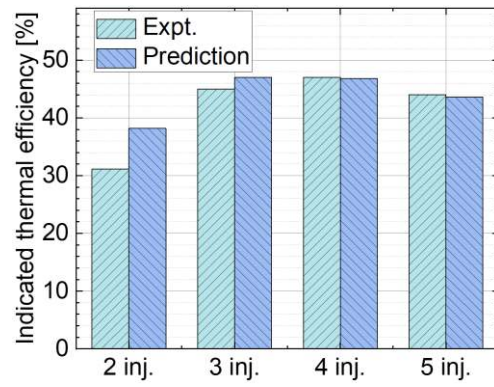
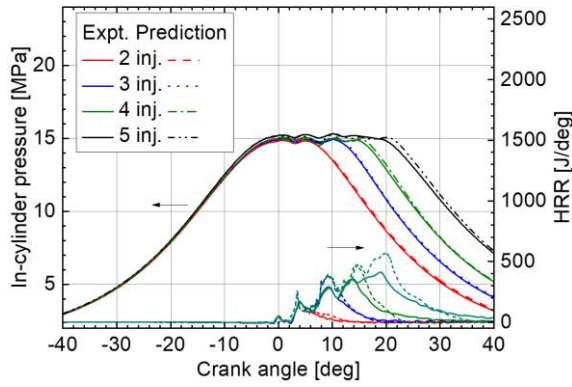


(b) 4 inj. case.

Fig. 7. Predicted distributions of the HRR and REXR regions for the (a) CDC and (b) 4 inj. cases.

3.2. Isobaric combustion at various engine loads

Figures 8(a) compares the experimental and predicted pressure and HRR profiles, whereas Fig. 8(b) compares the ITEs. To maintain constant combustion pressure, more fuel is injected in the later injection events. The simulations are able to capture the experimental results at various engine loads reasonably well, except that the thermal efficiency for the 2-injection isobaric case is over-predicted by about 6.5% points. This is due to the earlier combustion phasing and higher peak HRR predicted by the simulations. Note that at low engine loads (as in 2-injection case), the discrepancies between the experimental and predicted ITEs become amplified because of the normalization process involved; the pressure trace and HRR still show a very good match. With the increase of engine load, the thermal efficiency first grows, and then reduces. Peak thermal efficiencies are obtained with the 3- and 4-injection cases.



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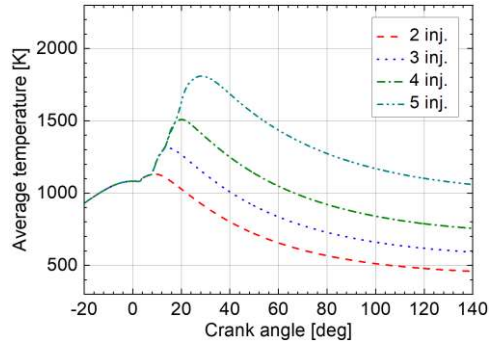
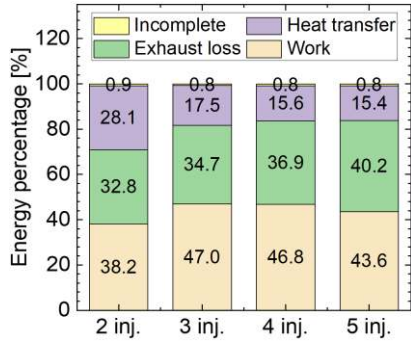
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(a) In-cylinder pressure and HRR.

(b) Indicated thermal efficiency.

210 **Fig. 8.** Comparison of the experimental and predicted (a) pressure and HRR profiles and (b) indicated
 211 thermal efficiency at various engine loads.

212 Figures 9(a) and 9(b) compare the predicted energy distributions and average temperature profiles
 213 at various engine loads, respectively. At a higher engine load, the average temperature is increased due
 214 to the larger energy input, which results in higher exhaust temperature and a higher proportion of
 215 exhaust loss. Despite the higher average temperature at the higher engine load, the proportion of heat
 216 transfer loss is still reduced. The proportion of the exhaust loss, on the other hand, tends to increase
 217 with a higher load. The competition between heat transfer loss and exhaust loss leads to the initially
 218 increasing and later decreasing trend in thermal efficiency. Compared to the exhaust and heat transfer
 219 losses, the incomplete combustion loss remains at a low level (below 1%). Note that for the 5-injection
 220 isobaric case, the exhaust loss fraction is comparable to the useful work fraction. This emphasizes the
 221 importance of the use of exhaust energy recovery systems in modern engine concepts, such as the LP
 222 unit of the DCEE.



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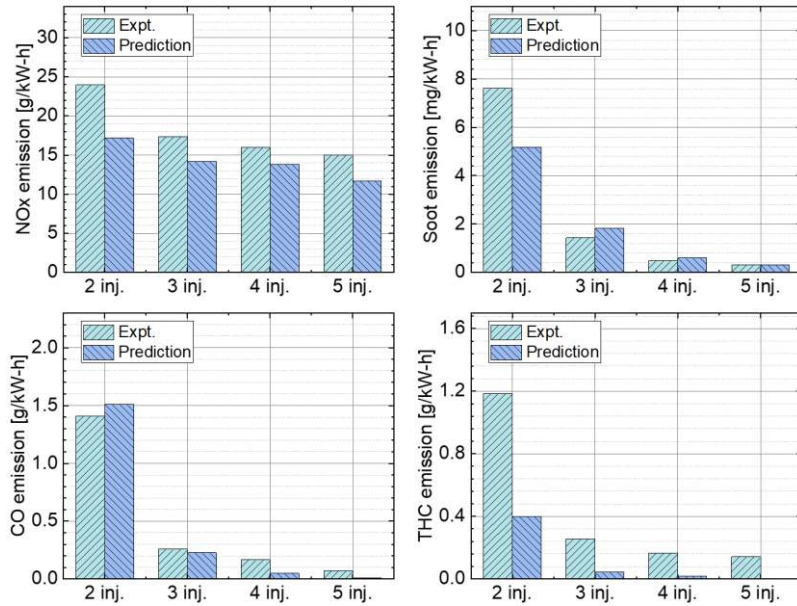
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(a) Energy distributions.

(b) Average temperature profiles.

225 **Fig. 9.** Comparison of the predicted (a) energy distributions and (b) average temperature profiles at
 226 various engine loads.

227 Figures 10 compares the experimental and predicted NO_x, soot, CO, and THC emissions at various
 228 engine loads. Despite discrepancies in low-load cases, the trends are reasonably captured by the
 229 simulations. Note that the emissions are in a unit of g/kW-h, all of which show a declining trend with a
 230 higher load. The reductions of soot, CO, and THC emissions are primarily due to the higher combustion
 231 temperatures that enhance oxidation, while the declining of NO_x in g/kW-h is due to the isobaric
 232 combustion restriction so that the injection timing must be delayed significantly. However, the absolute
 233 amount of NO_x in volume fraction (ppm) grows with a higher load, owing to the longer combustion
 234 duration and larger high-temperature reaction zones. Therefore, the NO_x/soot trade-off still exists when
 235 we adopt the units of ppm and g/m³ for NO_x and soot emissions, respectively.



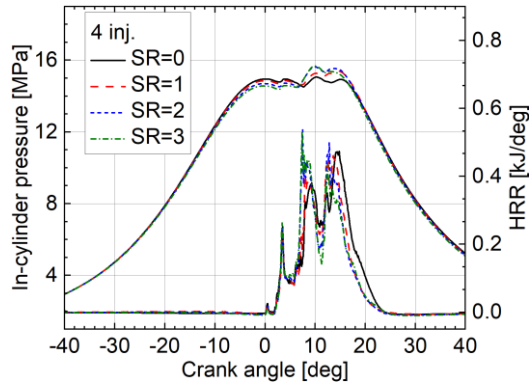
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237 **Fig. 10.** Comparison of the predicted and experimental NO_x, soot, CO, and THC emissions at various
 238 engine loads.

239 3.3. Parametric study on the isobaric combustion

240 3.3.1. Effect of swirl ratio

241 Figure 11 compares the predicted pressure and HRR profiles with different swirl ratios (SR) for
 242 the 4-injection isobaric cases. With a higher swirl ratio, in-cylinder pressure is lower before the top
 243 dead center (TDC), but higher after the second-injection combustion event. Figures 12(a) and 12(b)
 244 compare the average temperatures and air utilization profiles at different swirl ratios, respectively.
 245 Note that the lower percentage of $\phi > 1.5$ regions indicates better air utilization. It shows that a higher
 246 swirl ratio leads to a better air utilization rate. Therefore, the premixed HRR is higher with a higher
 247 swirl ratio, as shown in Fig. 11, which is especially apparent during the 3rd-and 4th-injection
 248 combustion events.

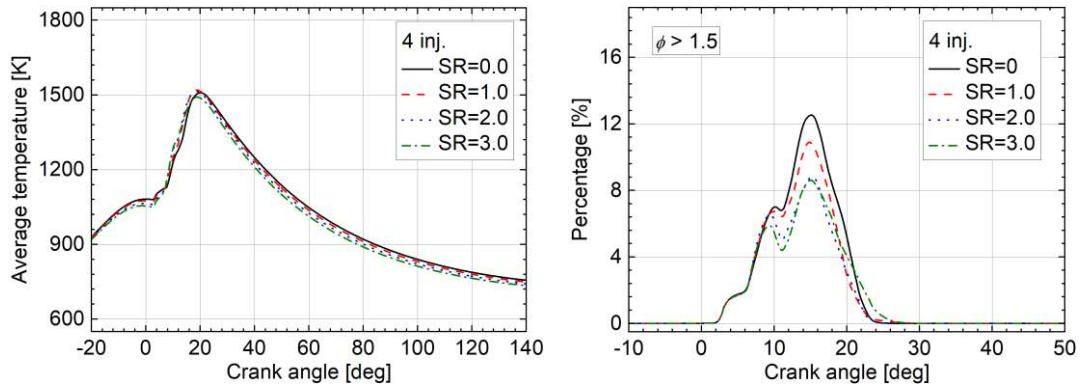


249

250 **Fig. 11.** Comparison of the predicted pressure and HRR results with different swirl ratios for the 4 inj.

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cases.



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(a) Average temperature.

(b) Air utilization profile.

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254 **Fig. 12.** Comparison of the predicted (a) average temperature and (b) air utilization profiles with

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different swirl ratios.

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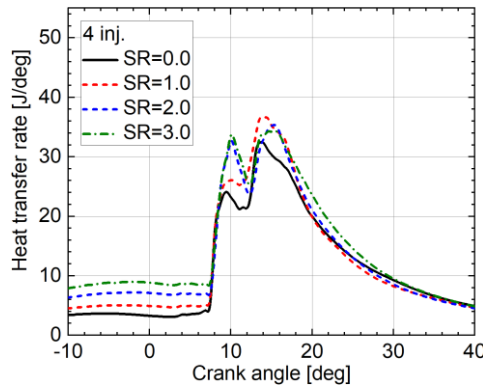
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The higher swirl ratio also significantly affects the heat transfer process. Figure 13 compares the predicted evolutions of the heat transfer rate with different swirl ratios. A higher swirl ratio significantly enhances the heat transfer rate even before ignition. To further clarify this, Fig. 14 compares the predicted distributions of turbulent kinetic energy (TKE), temperature (T), and ϕ at different swirl ratios before the injection event (-4°CA ATDC). Note that a higher swirl ratio leads to a more tilting spray/flame plume. Besides, the higher swirl ratio increases the TKE, which leads to a higher heat transfer rate. Therefore, the more intense convection heat transfer process results in the lower near-wall

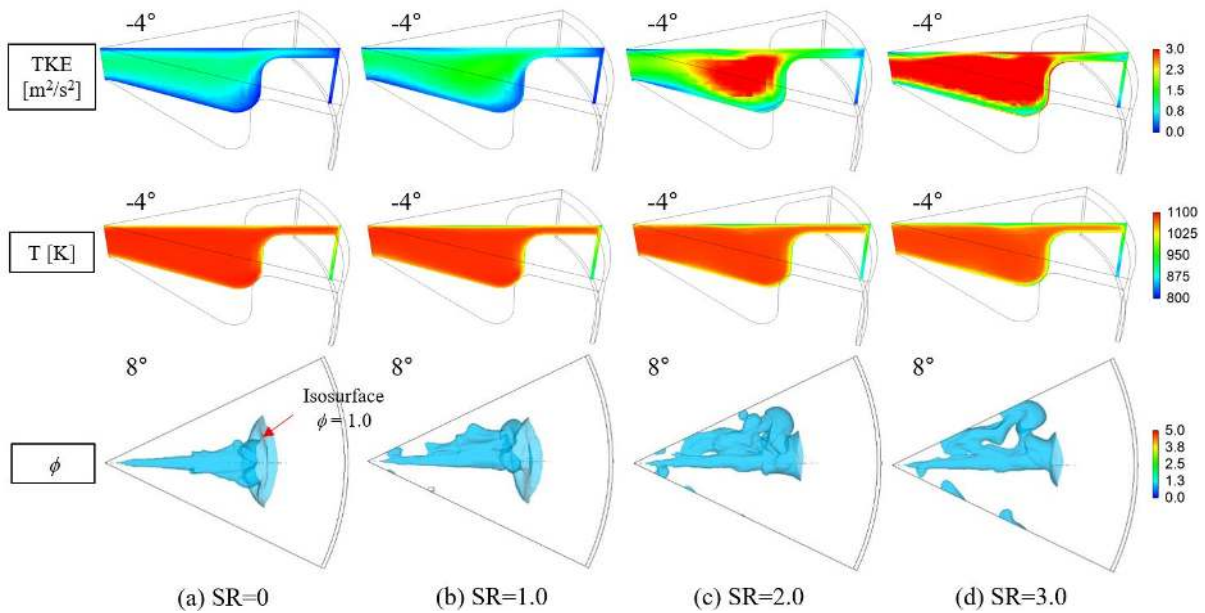
263 and average temperatures before ignition.



264

265 **Fig. 13.** Comparison of the predicted evolutions of heat transfer rate at different swirl ratios.

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268 **Fig. 14.** Comparison of the predicted distributions of turbulent kinetic energy (TKE), temperature (T),

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phi at different swirl ratios.

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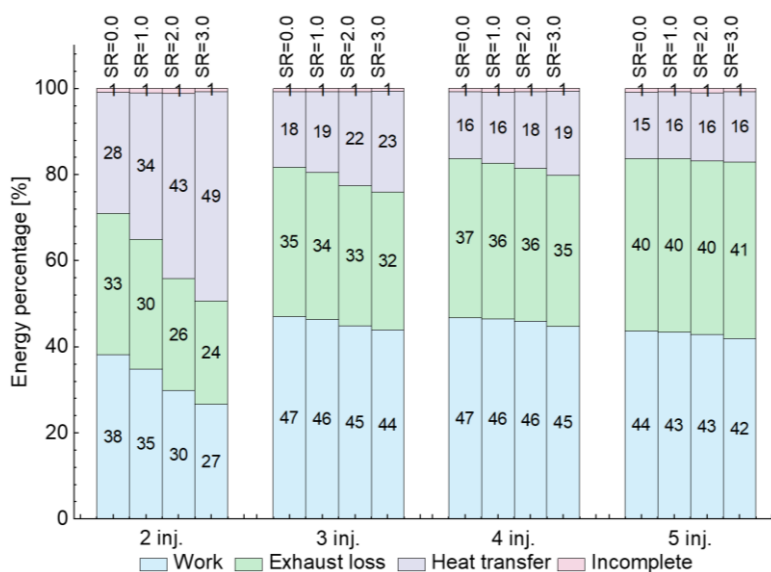
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Figure 15 compares the predicted energy distributions at various engine loads with different swirl ratios. A higher swirl ratio leads to a lower thermal efficiency, which is primarily due to the enhanced heat transfer loss. Besides, at different engine loads except the 5-injection case, exhaust loss fraction generally demonstrates a declining trend with a higher swirl ratio, which is owing to the faster combustion process and thus lower exhaust temperature as depicted in Fig. 12(a). Comparatively, the

275 incomplete combustion loss fraction remains at a stably low level of about 1%.



276

277 **Fig. 15** Comparison of the predicted energy distributions with different swirl ratios.

278 Figure 16 compares the predicted emissions at various engine loads with different swirl ratios.

279 With each swirl ratio, generally similar trends in the change of the emissions with different engine loads

280 are observed, except that the soot, CO, and THC emissions are significantly higher for the 5-injection

281 case at the swirl ratio of 3.0. This is primarily owing to the late combustion. Since a high swirl ratio

282 stirs up the combustion region further from the upstream combustible fuel-air mixture, it delays the

283 combustion and results in lower combustion temperature, as indicated by Fig. 12(a). Therefore, the

284 oxidation rate is lower at this condition, which increases the soot, CO, and THC emissions.

285 For the 2-injection cases, all of the emissions in g/kW-h show a growing trend with a higher swirl

286 ratio, owing to the joint effect of the lower work output and the premixed combustion process. For NOx

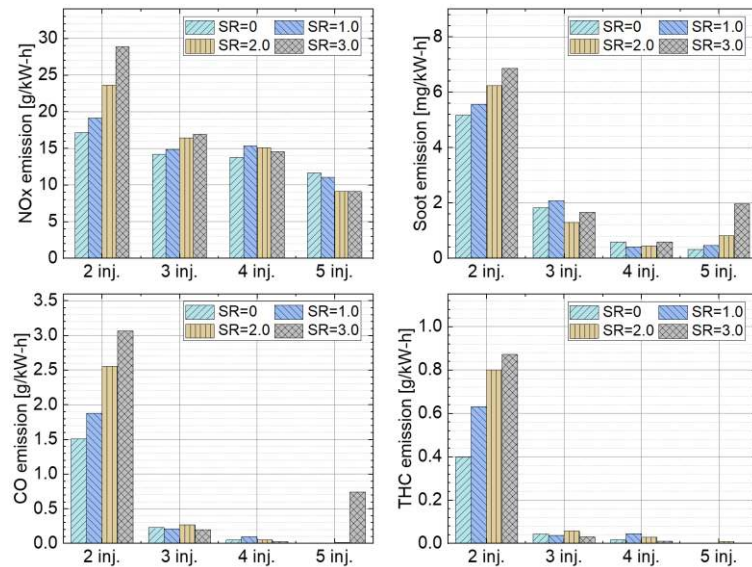
287 emission, the 3-injection cases continue exhibiting a growing trend with a higher swirl ratio, but the

288 higher-load cases demonstrate an overall declining trend, due to the lower temperature during the post-

289 combustion period as depicted in Fig. 12 (a). For the other three kinds of emissions, the 3-and 4-

290 injection cases both show a comparatively weak response to the higher swirl ratio. However, the 5-

291 injection cases show a growing trend since the higher swirl ratio has a more significant effect on the
 292 5th-injection combustion period, which leads to a lower post-combustion temperature and thus lower
 293 oxidation rates of soot, CO, and HCs.

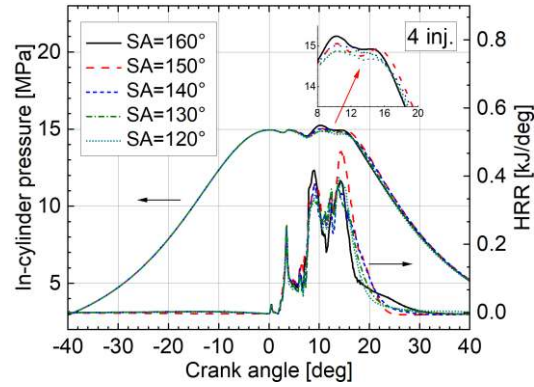


294

295 *Fig. 16. Comparison of the predicted NOx, soot, CO, and THC emissions with different swirl ratios.*

296 3.3.2. Effect of spray angle

297 Figure 17 compares the predicted pressure and HRR profiles with the different spray angles for the
 298 4-injection isobaric cases. During the first and second injection events, combustion heat release is
 299 similar for all the cases. This is due to the low amount of injected fuel mass and thus a shorter spray
 300 penetration. As a result, the combustion is primarily confined within the chamber. However, different
 301 spray angles have a significant effect on the 3rd- and the 4th-injection combustion processes, owing to
 302 the significantly longer spray penetrations, hence more intense flame-wall interactions, **which is clearly**
 303 **shown in Fig. 18.** Note that a spray angle of 150° generates the highest combustion pressure during the
 304 4th-injection combustion period, while spray angles of 160° and 120° generate the lowest combustion
 305 pressures. **As seen in Fig. 18, cases with spray angles of 160° and 120° generate more combustion**
 306 **regions within the squish, which impairs the effective engine work and enhances the heat transfer loss.**

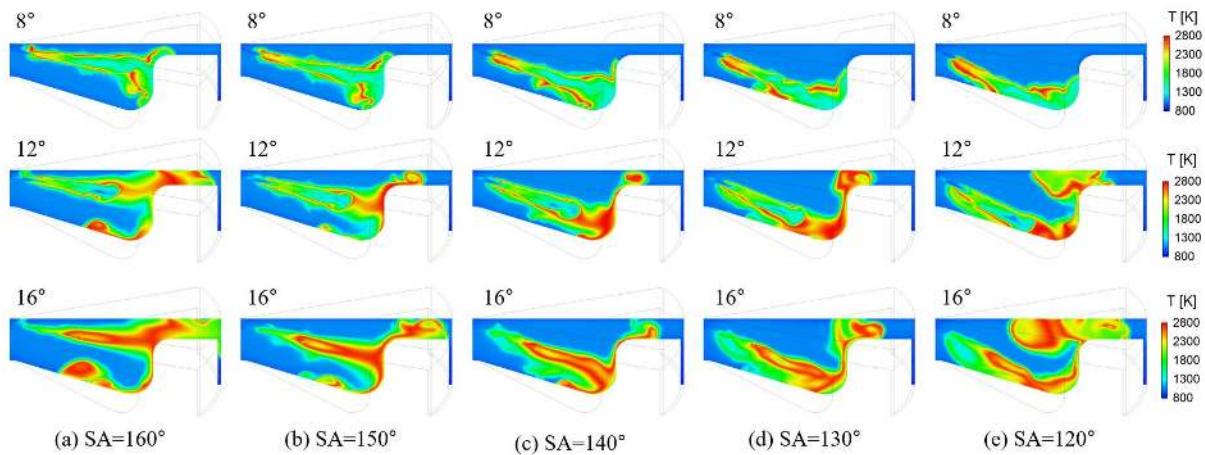


307

308 **Fig. 17.** Comparison of the predicted pressure and HRR profiles with different spray angles for the 4

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inj. cases.



310

311 **Fig. 18.** Comparison of the predicted distributions of T for the 4 inj. cases with different spray angles.

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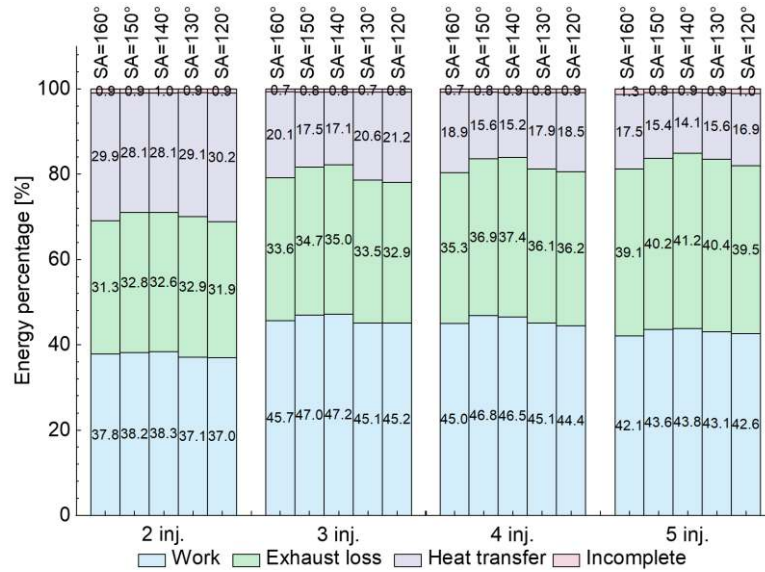
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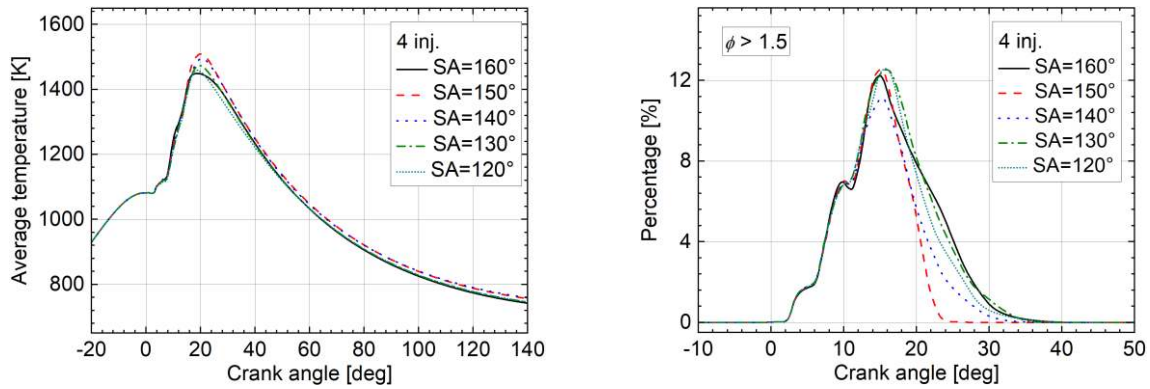
Figure 19 compares the predicted energy distributions at various engine loads with different spray angles. As with the swirl ratio, the thermal efficiency follows the same trend with respect to the spray angle at different engine load conditions. An obvious firstly growing and then declining trend of thermal efficiency is observed as the spray angle is reduced from 160° to 120° . Peak thermal efficiencies are obtained with a spray angle of either 150° or 140° , primarily due to the more efficient combustion processes and lower heat transfer losses. Figures 20(a) and 20(b), respectively, compare the predicted average temperature and air utilization profiles for the 4-injection isobaric cases with different spray angles. The cases with spray angles of 150° and 140° yield the highest air utilization rates and combustion temperatures, which explain their higher thermal efficiencies.



321

322

Fig. 19. Comparison of the predicted energy distributions with different spray angles.



323

324

(a) Average temperature.

(b) Air utilization profile.

Fig. 20. Comparison of the predicted (a) average temperature and (b) air utilization profiles with

326

different spray angles.

327 Figure 21 compares the predicted evolutions of the total heat transfer rate (HTR) and HTRs through

328 the piston, cylinder head, and liner for the 4-injection isobaric cases with different spray angles. Clearly,

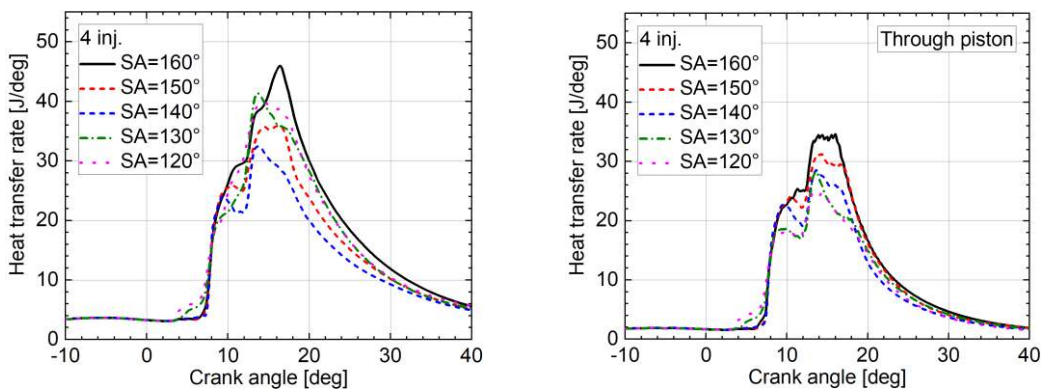
329 the SA=140° case generates the lowest heat transfer loss, although it has a comparatively high average

330 temperature, as seen in Fig. 20(a). Figures 21(b-d) show that the SA=140° case generates the lowest

331 heat transfer loss through the liner, which means the combustion is well confined within the cylinder

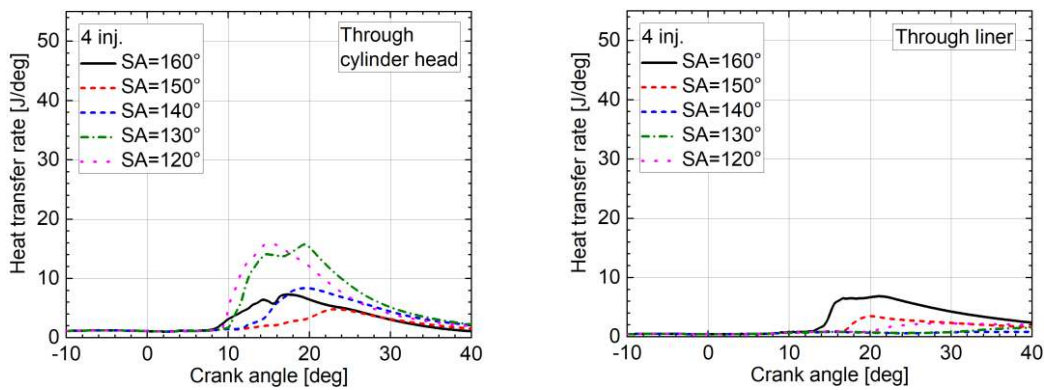
332 and squish regions, as seen in Fig. 18. Besides, it also generates comparatively low heat transfer losses

333 through the piston and cylinder head simultaneously. These factors lead to the lowest heat transfer loss
 334 for the SA=140° case.



335
 336 (a) Total HTR.

(b) HTR through piston.



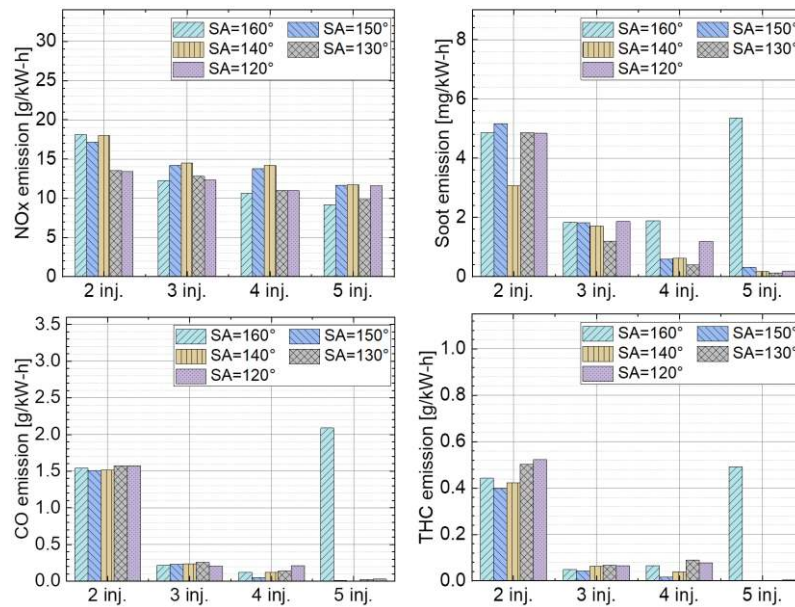
337
 338 (c) HTR through cylinder head.

(d) HTR through liner.

339 **Fig. 21.** Predicted evolutions of the (a) total HTR and HTR through (b) piston, (c) cylinder head, and
 340 (d) liner with different spray angles.

341 Figure 22 compares the predicted NO_x, soot, CO, and THC emissions at various engine loads with
 342 different spray angles. With each spray angle, different emissions generally show a declining trend with
 343 a higher load. Owing to the higher combustion temperature and air utilization rate (see Fig. 20), the
 344 cases with spray angles of 140° and 150° tend to generate higher NO_x emissions and lower CO and
 345 THC emissions. Note that among the 5-injection isobaric cases, the case with a spray angle of 160°
 346 generates a significantly higher amount of soot, CO, and THC emissions. This is because a lot of fuel

347 is injected into the squish region during the 5th injection event, which leads to poor air-fuel mixing
 348 characteristics and, hence, low oxidation rates of the pollutant species during the post-combustion
 349 period.

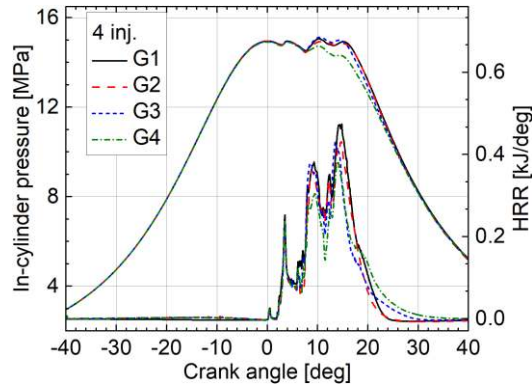


350

351 **Fig. 22.** Comparison of the predicted NOx, soot, CO, and THC emissions with different spray angles.

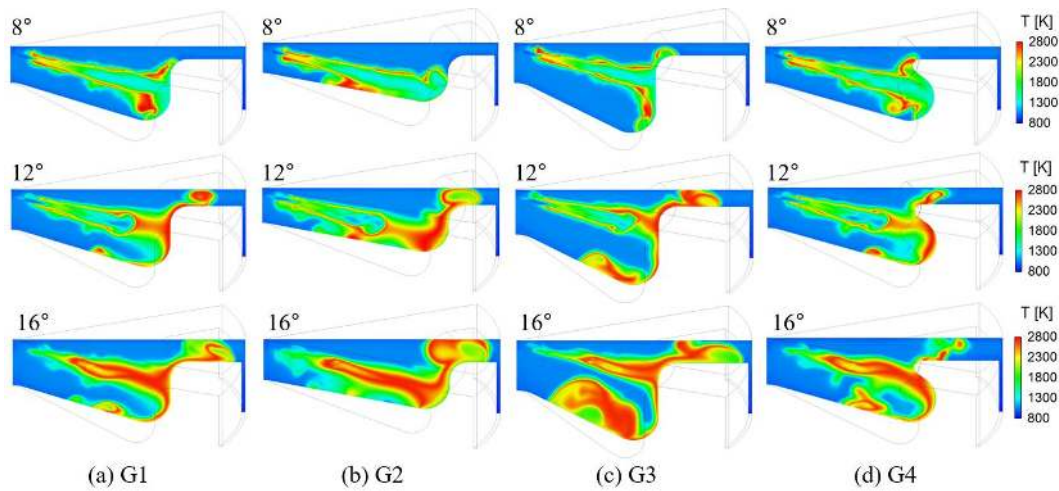
352 3.3.3. Effect of piston geometry

353 Figure 23 compares the predicted pressure and HRR profiles with the four different piston
 354 geometries for the 4-injection isobaric case. Comparatively, G1 and G2 show overall higher combustion
 355 pressures and HRRs, followed by G3, and then G4. For the 1st- and the 2nd-injection combustion events,
 356 different piston geometries have a negligible effect on the combustion process; however, there is a
 357 significant effect on the 3rd- and the 4th-injection combustion events, which is clearly shown in Fig. 24.
 358 Comparatively, G2 generates the longest spray-flame plume due to the longest inner piston radius; G3
 359 generates the most combustion regions within the piston due to the deeper piston design; while G4
 360 generates a spray-flame plume that is primarily confined within the combustion chamber, which,
 361 however, leads to the overall lower combustion temperature.



362

363 **Fig. 23.** Comparison of the predicted pressure and HRR profiles with four piston geometries for the 4
 364 inj. cases.



365

366 **Fig. 24.** Comparison of the predicted distributions of T with four piston geometries.

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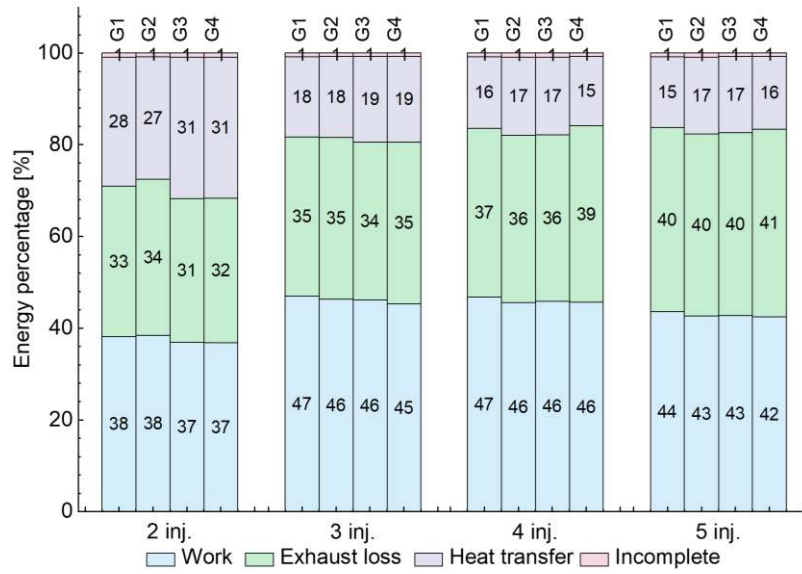
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Figure 25 compares the predicted energy distributions at various engine loads with different piston geometries. With each piston geometry, thermal efficiency at a higher load demonstrates a firstly growing and then declining trend. For the 2-injection isobaric cases, G2 generates the highest thermal efficiencies among four piston geometries, primarily due to the lowest heat transfer loss. For the 3-, 4-, and 5-injection isobaric cases, however, G1 generates the highest thermal efficiencies, owing to the low heat transfer and exhaust losses together.



373

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Fig. 25. Comparison of the predicted energy distributions with four piston geometries.

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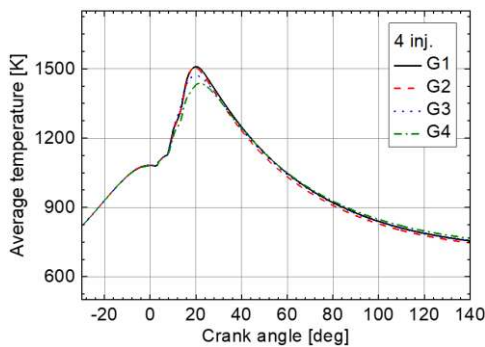
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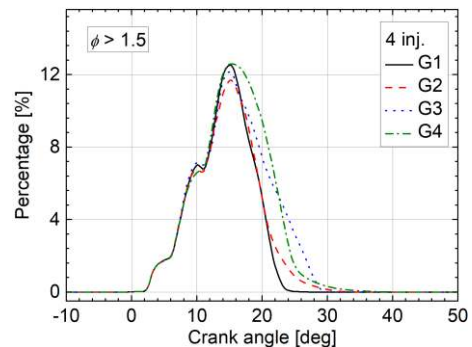
Note that for the 4- and 5-injection isobaric cases, although G4 yields a significantly lower combustion pressure during the 3rd- and the 4th-injection combustion periods, it eventually generates similar thermal efficiencies as G2 and G3. To clarify this, Figs. 26(a) and 26(b) compare the predicted average temperature and air utilization profiles for the 4-injection isobaric cases. It reveals that the lower HRR in the G4 case is primarily due to the lower air-utilization during the 4th-injection combustion period. Therefore, G4 yields a lower average temperature, which results in a lower heat transfer loss. This explains its comparable thermal efficiency with G2 and G3.



382

383

(a) Average temperature.



384

(b) Air utilization profile.

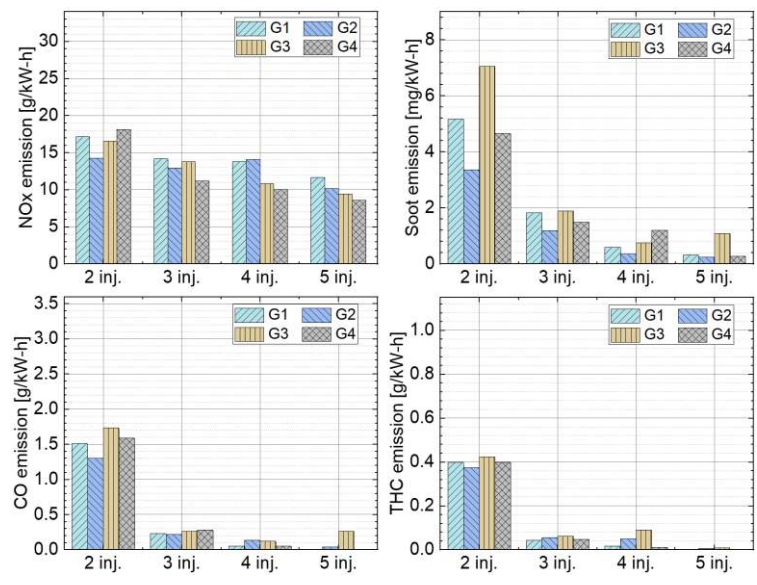
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Fig. 26. Comparison of the predicted (a) average temperature and (b) air utilization profiles with four

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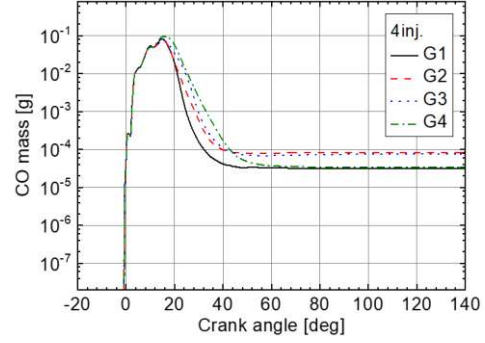
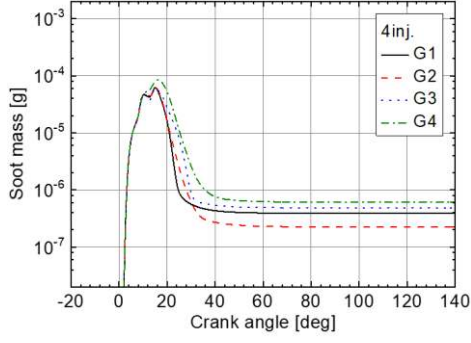
piston geometries.

386 Figure 27 compares the predicted NO_x, soot, CO, and THC emissions with different piston
 387 geometries. Still, with each piston geometry, each pollutant species demonstrates a declining trend with
 388 a higher engine load. Since the formation of NO_x is closely related to combustion temperature, G1 tends
 389 to generate higher NO_x emissions compared to the other piston geometries due to the generally higher
 390 combustion temperature, as seen in Fig. 26(a). Note that for the 3-, 4-, and 5-injection isobaric cases,
 391 there is a declining trend in NO_x emissions when changing the piston geometry from G2 to G4, owing
 392 to the declining trend in combustion temperature.



393
 394 **Fig. 27.** Comparison of the predicted NO_x, soot, CO, and THC emissions with four piston geometries.

395 Emissions of soot, CO, and THC at various engine loads demonstrate a more complicated behavior.
 396 Figure 28 compares the predicted evolutions for soot, CO, and C₂H₄ (ethylene) with different piston
 397 geometries. C₂H₄ is used because it is one of the primary compositions of THC emissions [45]. Note
 398 that before the 3rd-injection combustion periods, all pollutants show similar results regardless of the
 399 piston geometry. After that, significant discrepancies are observed, since different piston geometries
 400 start playing a more important role in the in-cylinder flow and fuel-air mixing processes.

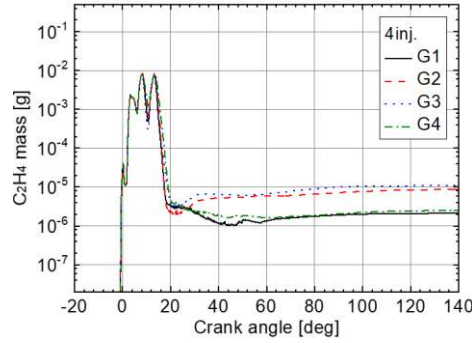


401

402

(a) Soot.

(b) CO.



403

404

(c) C₂H₄.

405 **Fig. 28.** Comparison of predicted evolutions of soot, CO, and C₂H₄ for the 4 inj. cases with four

406

piston geometries.

407 3.3.4. Summary

408 To summarize the effects of swirl ratio, spray angle, and piston geometry on the efficiency and

409 emissions of the isobaric combustion mode, two merit functions are defined with the baseline case

410 (SW=0, SA=150°, and G1) as a reference [46],

$$411 \quad Merit_{ITE} = 100 * \left(\frac{ITE}{ITE_{ori}} - 1 \right) \quad (5)$$

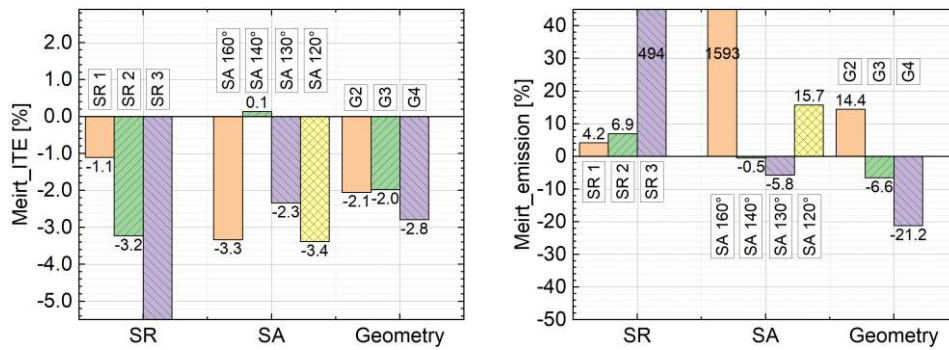
$$412 \quad Merit_{emission} = 100 * \left[\left(\frac{NO_x}{NO_{x,ori}} - 1 \right) + 0.1 * \left(\frac{SOOT}{SOOT_{ori}} + \frac{CO}{CO_{ori}} - 2 \right) + 0.01 * \left(\frac{THC}{THC_{ori}} - 1 \right) \right] \quad (6)$$

413 Besides, the merit value at each engine load is multiplied by a weight factor based on the total injected

414 mass and then summed up. The weight factor is calculated by,

$$415 \quad W_i = \frac{m_i}{\sum m_i} \quad (7)$$

416 Figures 29(a) and 29(b) summarize the calculated $Merit_{ITE}$ and $Merit_{emission}$ for the isobaric
 417 combustion cases. The adoption of a higher swirl ratio or a different piston geometry than the original
 418 one has a negative effect on the thermal efficiency, and hence, the fuel economy. A peak ITE is obtained
 419 with a spray angle of 140° , with a 0.1% improvement compared to the baseline case. On the other hand,
 420 a higher swirl ratio increases engine-out emissions, while spray angles of 140° and 130° and piston
 421 geometries of G3 and G4 all reduce engine-out emissions. In summary, considering both the fuel
 422 economy and emission factors, the original piston shape (G1) with a spray angle of 140° and a swirl
 423 ratio of 0 yields the best performance for the isobaric combustion mode.



424 (a) $Merit_{ITE}$.

425 (b) $Merit_{emission}$.

426 **Fig. 29.** Summary of the predicted (a) $Merit_{ITE}$ and (b) $Merit_{emission}$ for the isobaric combustion cases.

427 4. Conclusions and future work

428 This work numerically investigated the isobaric combustion mode using a three-dimensional
 429 modeling approach. An in-house data-processing method was utilized to understand and compare the
 430 detailed combustion features of the conventional diesel and isobaric combustion modes. Besides, the
 431 effects of swirl ratio, spray angle, and piston geometries on the engine combustion performance and
 432 emissions were investigated at various engine loads. The conclusions of this work are summarized as
 433 follows:

- 434 (1) The isobaric combustion mode generated a significantly lower peak pressure but a similar

435 thermal efficiency compared to the conventional diesel combustion mode, which is more preferable for
436 the double compression expansion engine concept.

437 (2) A higher swirl ratio led to the higher turbulent kinetic energy and air utilization rate, but it also
438 resulted in the higher heat transfer loss and thus the lower thermal efficiency.

439 (3) Cases with spray angles of 140° and 150° generated the higher thermal efficiencies owing to
440 the more efficient combustion processes and lower heat transfer losses.

441 (4) Different piston geometries demonstrated a significant impact on the post-combustion period
442 at a higher engine load, with original piston shape generally yielding the highest thermal efficiency.

443 (5) The original piston shape with a spray angle of 140° and a swirl ratio of 0 yields the best
444 performance for the isobaric combustion mode.

445 This work primarily focused on three parameters (swirl ratio, spray angle, and piston geometry)
446 with the start of injection timings unchanged. In the future, more studies will be performed by
447 optimizing the injector setup, injection strategy, and piston geometry simultaneously. Considering the
448 multiple-parameter target, the machine learning method may be necessary.

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452 Combustion for Advanced Engines) is a collaborative research undertaking between Saudi Aramco and
453 KAUST intended to address the fundamental aspects of hydrocarbon fuel combustion in engines, and
454 develop fuel/engine design tools suitable for advanced combustion modes. The computational
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