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## A phenomenological relative biological effectiveness (RBE) model for proton therapy based on all published in vitro cell survival data

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### Abstract

**Purpose**—Proton therapy treatments are currently planned and delivered using the assumption that the proton relative biological effectiveness (RBE) relative to photons is 1.1. This assumption ignores strong experimental evidence that suggests the RBE varies along the treatment field, i.e. with linear energy transfer (LET) and with tissue type. A recent review study collected over 70 experimental reports on proton RBE, providing a comprehensive dataset for predicting RBE for cell survival. Using this dataset we developed a model to predict proton RBE based on dose, LET and the ratio of the linear-quadratic model parameters for the reference radiation  $(\alpha/\beta)_x$ , as the tissue specific parameter.

**Methods and Materials**—The relationship of the RBE on dose, dose average LET ( $LET_d$ ) and  $(\alpha/\beta)_x$  was explored using 287 experimental data points. A RBE model based on the linear quadratic model was derived from a nonlinear regression fitting to the data.

**Results**—The proposed model predicts that the RBE increases with increasing  $LET_d$  and decreases with increasing  $(\alpha/\beta)_x$ . The model additionally predicts a decrease in RBE with increasing dose.

**Conclusions**—The proposed phenomenological RBE model is derived using the most comprehensive collection of proton RBE experimental data to date. The model agrees with previous theoretical predictions on the relationship between RBE,  $LET_d$  and  $(\alpha/\beta)_x$  and also makes predictions on the relationship between RBE and dose. The proposed model shows a relationship between both  $\alpha$  and  $\beta$  with  $LET_d$ . Previously published phenomenological models, based on a limited data set, may have to be revised.

### Keywords

relative biological effectiveness; proton therapy; cell survival; linear energy transfer

## 1. Introduction

The relative biological effectiveness (RBE) is defined as the ratio of the reference photon dose to the proton dose necessary to cause the same level of effect. Traditionally, dose in proton radiotherapy is prescribed by scaling the physical proton dose by 1.1, i.e. protons are assumed to be 10% more efficient than photons. This however assumes a spatially invariant

RBE within all treatment fields and disregards strong experimental evidence (mostly based on cell survival) that suggests the RBE varies. It has been suggested that using a variable RBE may help improve proton therapy outcomes as well as help interpret clinical results from proton therapy (Carabe *et al* 2013, Tilly *et al* 2005, Wedenberg and Toma-Dasu 2014, Paganetti 2015).

The RBE depends on the type of particle, the dose averaged linear energy transfer ( $LET_d$ ) as a reasonable approximation of macroscopic dosimetric parameters, the cell or tissue type defined by  $(\alpha/\beta)_x$  as well as the dose per fraction (Paganetti *et al* 2002). Previous experimental studies have shown a strong correlation between RBE and  $LET_d$ , suggesting RBE increases with increasing  $LET_d$  (Belli *et al* 1989, 1992, Folkard *et al* 1996, Perris *et al* 1986, Coutrakon *et al* 1997, Schettino *et al* 2001, Wouters *et al* 1996). This implies that the RBE around the distal edge of the spread out Bragg peak (SOBP) is larger than that in the plateau region since the increase in  $LET_d$  may soften the sharp decrease in dose at the distal edge. For this reason different studies have suggested a shift in the proton biological effective range by 1–2 mm (Robertson *et al* 1975, Paganetti and Goitein 2000). Generally, the RBE is expected to decrease with both increasing  $(\alpha/\beta)_x$  and increasing dose (Paganetti *et al* 2002, Gerweck and Kozin 1999), however, the experimental data from single experiments is unsatisfactory in showing a clear correlation between RBE and  $(\alpha/\beta)_x$  or dose. With the development of increasingly conformal proton therapy beam delivery systems, having a proper understanding of the RBE and the relevant treatment-scaling factor is essential for accurate calculation of the effective or biological dose in the patient as well as for efforts to reduce range margins.

A recent review study of the literature analyzed more than 70 reports to investigate the relationship of RBE with dose, biological endpoint and  $LET_d$  (Paganetti 2014), including a full analysis of RBE values for clonogenic cell survival. The analysis of the experimental data collected in this study suggested that the proton RBE increases with increasing  $LET_d$  as well as decreased with increasing  $(\alpha/\beta)_x$ . It was also shown that the RBE increased with decreasing dose. The comprehensive collection of data in Paganetti (2014) provides an unprecedented platform for the development and/or refinement of a biophysical model that predicts proton RBE.

In this study the experimental data presented in Paganetti (2014) was extracted and analyzed to parameterize the relationship of RBE versus dose,  $LET_d$  and  $(\alpha/\beta)_x$  for proton therapy. The derived model was compared with other published models. Note that, as in the review article, the  $LET_d$  values reported in this work are not absolute proton  $LET_d$  values but relative to the reference photon generated  $LET_d$  values (e.g.  $\sim 0.3$  keV/ $\mu$ m for 6-MV photon beams).

## 2. Methods and Materials

### 2.1. Experimental Data

Paganetti (2014) extracted experimental data from 76 different studies and analyzed the data in the framework of the linear-quadratic (LQ) model. Allowing the calculation of common quantities for each of the studies and making it possible to determine certain parameters that

the experiment may not have reported (e.g. RBE at a certain dose). In this study, the full collection of data presented in Paganetti (2014) was used to develop a new phenomenological model that predicts proton RBE. For each experimental data set, the following parameters relevant to the linear-quadratic model were extracted:  $\alpha_x$  and  $\beta_x$  which describe the tissue dose response to photons,  $\alpha$  and  $\beta$  describing the tissue dose response to protons and the dose averaged LET ( $LET_d$ ) at the position of the biological sample. Since the  $LET_d$  value at the measurement point was not reported in the majority of the studies, Paganetti (2014) inferred the  $LET_d$  values in these cases from either look-up tables or Monte Carlo simulations. Assuming the same level of effect compared to the reference radiation, the RBE for different proton doses ( $D_p$ ) was calculated using a RBE formalism based on the LQ model:

$$RBE \left[ D_p, \left( \frac{\alpha}{\beta} \right)_x, LET_d \right] = \frac{1}{2D_p} \left( \sqrt{\left( \frac{\alpha}{\beta} \right)_x^2 + 4 \left( \frac{\alpha}{\beta} \right)_x \frac{\alpha[LET_d]}{\alpha_x} D_p} + 4 \frac{\beta[LET_d]}{\beta_x} D_p^2 - \left( \frac{\alpha}{\beta} \right)_x \right). \quad (1)$$

The uncertainty in the RBE was calculated in Paganetti (2014) from the uncertainties reported in each of the individual published studies and used here to weigh the fitted data.

The primary data set extracted from Paganetti (2014) had a large range of  $LET_d$  and  $(\alpha/\beta)_x$  values, resulting in RBE values ranging from 0.02 to 7.4 for a dose of 2 Gy. To develop a biophysical model relevant to clinical proton therapy, restrictions were applied to the primary data set. Only data points with  $LET_d < 20$  keV/ $\mu$ m and  $(\alpha/\beta)_x < 30$  Gy were used in the fit. The exclusion criterion corresponds to the clinically relevant  $LET_d$  range, where the RBE is approximately linear with respect to  $LET_d$  (Paganetti 2014). These restrictions excluded 84 points from the original set of 369 data points. Data removed due to the restriction of  $(\alpha/\beta)_x < 30$  Gy included all the reported measurements in some studies (Ristic-Fira *et al* 2011, Petrović *et al* 2010, Antoccia *et al* 2009, Sakamoto *et al* 1980, Keta *et al* 2014) or the removal of selected data points (Belli *et al* 2000, Bettega *et al* 2000, Blomquist *et al* 1993, Grosse *et al* 2014, Baggio *et al* 2002, Schettino *et al* 2001, Urano *et al* 1980). The restriction of  $LET_d < 20$  keV/ $\mu$ m excluded another two studies (Goodhead *et al* 1992, Wéra *et al* 2011) as well as selected data points from other studies (Belli *et al* 1989, 1992, 1993, 1998, 2000, Bettega *et al* 1998, Chaudhary *et al* 2014, Fiorini *et al* 2011, Folkard *et al* 1989, Ogheri *et al* 1997, Prise *et al* 1990, Schettino *et al* 2001, Schuff *et al* 2002, Sgura *et al* 2000). The RBE was considered for proton doses ranging from 1 – 10 Gy, governed by the assumed validity of the linear-quadratic model. For this reason, a data point only valid for doses between 8–24 Gy was also eliminated from the data set (Ristić-Fira *et al* 2008). Additionally, one outlier, with  $(\alpha/\beta)_x = 25.5$  Gy,  $LET_d = 12.1$  keV/ $\mu$ m and  $RBE = 2.55$  for  $D_p = 2$  Gy, was excluded from the fit (Perris *et al* 1986). The other point reported in this study ( $(\alpha/\beta)_x = 25.5$ ,  $LET_d = 5.8$  and  $RBE = 1.62$ ) was not an outlier but was also removed for the sake of consistency.

## 2.2 The RBE Model

A LQ-based RBE model (equation (1)) was used to parameterize the dependence of proton RBE on  $LET_d$ ,  $(\alpha/\beta)_x$  and dose:

$$RBE \left[ D_p, \left( \frac{\alpha}{\beta} \right)_x, LET_d \right] = \frac{1}{2D_p} \left( \sqrt{\left( \frac{\alpha}{\beta} \right)_x^2 + 4D_p \left( \frac{\alpha}{\beta} \right)_x RBE_{\max} + 4RBE_{\min}^2 D_p^2 - \left( \frac{\alpha}{\beta} \right)_x} \right) \quad (2)$$

where  $RBE_{\max}$  and  $RBE_{\min}$  correspond to the asymptotic values of RBE at doses 0 and  $\infty$  Gy, respectively (Carabe-Fernandez *et al* 2007).  $RBE_{\max}$  and  $RBE_{\min}$  are quantified in terms of the following ratios:

$$\begin{aligned} RBE_{\max} [\alpha, \alpha_x, LET_d] &= \frac{\alpha[LET_d]}{\alpha_x} \\ RBE_{\min} [\beta, \beta_x, LET_d] &= \sqrt{\frac{\beta[LET_d]}{\beta_x}} \end{aligned} \quad (3)$$

Carabe *et al.* (2012) assumed that both  $RBE_{\min}$  and  $RBE_{\max}$  have a linear relationship with respect to  $LET_d$  as well as a dependence on  $(\alpha/\beta)_x$ . Here we make the same assumption for  $RBE_{\max}$  however we assume that  $RBE_{\min}$  has a dependence on  $\sqrt{(\alpha/\beta)_x}$  (Jones 2015),

$$\begin{aligned} RBE_{\max} [(\alpha/\beta)_x, LET_d] &= p_0 + \frac{p_1}{(\alpha/\beta)_x} LET_d \\ RBE_{\min} [(\alpha/\beta)_x, LET_d] &= p_2 + p_3 \sqrt{\left( \frac{\alpha}{\beta} \right)_x} LET_d \end{aligned} \quad (4)$$

where  $p_{0-3}$  are the fit parameters for our model. Both assumptions are in accordance with the LQ model. A fit to the extracted experimental data for the response parameter, RBE, was performed using a robust non-linear regression technique in Matlab (Mathwork Inc.) with predictor variables  $D_p$ ,  $LET_d$ , and  $(\alpha/\beta)_x$  with the model,

$$RBE \left[ D_p, \left( \frac{\alpha}{\beta} \right)_x, LET_d \right] = \frac{1}{2D_p} \left( \sqrt{\left( \frac{\alpha}{\beta} \right)_x^2 + 4D_p \left( \frac{\alpha}{\beta} \right)_x \left( p_0 + \frac{p_1}{(\alpha/\beta)_x} LET_d \right) + 4D_p^2 \left( p_2 + p_3 \sqrt{\left( \frac{\alpha}{\beta} \right)_x} LET_d \right)^2 - \left( \frac{\alpha}{\beta} \right)_x} \right) \quad (5)$$

The Matlab *NonLinearModel.fit* algorithm was used to estimate the fit coefficients ( $p_{0-3}$ ) using an iterative procedure. The experimental data is associated with considerable uncertainties as a result of stochastic variations in the radiation fields as well as variations in cell sensitivity within the same culture. Furthermore, systematic differences in the analysis of the experimental data are likely to occur, which different groups may estimate differently. The uncertainties calculated for the RBE from Paganetti (2014) were used to weigh the data in the fitting procedure. No uncertainty in  $LET_d$  and dose were considered but the reported uncertainties in  $\alpha_x$ ,  $\beta_x$ ,  $\alpha$  and  $\beta$  were used to calculate the error in RBE.

### 2.3 Comparison of models

The fitted model was compared to two previously published proton RBE models, both based on a parameterization of the LQ RBE model. Each model has a different assumption regarding the relationship between LET,  $\beta$ ,  $\alpha$  and  $(\alpha/\beta)_x$ . The Carabe *et al.* model (Carabe *et al* 2012) applies a linear relationship between  $RBE_{\min}$ ,  $RBE_{\max}$  and  $LET_d$  with a slope depending on  $(\alpha/\beta)_x$  (equation (2)) with

$$\begin{aligned} RBE_{max} \left[ LET_d, \left( \frac{\alpha}{\beta} \right)_x \right] &= 0.843 + 0.154 \frac{2.686}{(\alpha/\beta)_x} LET_d \\ RBE_{min} \left[ LET_d, \left( \frac{\alpha}{\beta} \right)_x \right] &= 1.09 + 0.006 \frac{2.686}{(\alpha/\beta)_x} LET_d. \end{aligned} \quad (6)$$

The Wedenberg *et al.* model (Wedenberg *et al* 2013) on the other hand is based on the assumption that there is a linear relationship between  $\alpha$  and  $LET_d$  with a slope depending on  $(\alpha/\beta)_x$ , while  $\beta$  is assumed to be independent of  $LET_d$  with

$$RBE \left[ D_p, \left( \frac{\alpha}{\beta} \right)_x, LET_d \right] = \frac{1}{2D_p} \left( \sqrt{\left( \frac{\alpha}{\beta} \right)_x^2 + 4D_p \left( \left( \frac{\alpha}{\beta} \right)_x + 0.434 LET_d \right) + 4D_p^2} - \left( \frac{\alpha}{\beta} \right)_x \right). \quad (7)$$

Both models are based on fits through a small subset of the data used in our study.

## 2.4 SOBP and Patient RBE Simulation

A SOBP with a range/modulation width of 25 cm/10 cm was generated in water using the TOPAS Monte Carlo simulation system (Perl *et al* 2012), which has been extensively validated for proton therapy (Testa *et al* 2013). The SOBP was generated with a detailed model of the Francis H Burr Proton Therapy Center at Massachusetts General Hospital (Paganetti *et al* 2004). TOPAS features a number of different scorers, a function called by the user to record a specific simulation property. Both dose and LET distribution scorers were used in the simulation with a step size of 1 mm. The dose and  $LET_d$  along the SOBP was scored and used to calculate the RBE with the three models described above.

TOPAS has previously been used to simulate both LET (Giantsoudi *et al* 2013, Sethi *et al* 2014, Grassberger *et al* 2011) and RBE distributions (Polster *et al* 2015) in patient environments. For this study, two patients were selected from the MGH clinical patient database, a pediatric head and neck patient as well as a prostate patient. The purpose was to demonstrate the clinical impact predicted by our model for targets with low  $(\alpha/\beta)_x$  (e.g. the prostate) and for treatment sites adjacent to organs at risk (e.g. the brainstem). An in-house Matlab-based script that links the treatment planning system to TOPAS was used to create all the input files for the simulation. The simulations were performed using the same steps as described elsewhere (Paganetti *et al* 2008, Schuemann *et al* 2014, Schümann *et al* 2012). All simulations were performed on a research-computing cluster with 10 and 30 parallel simulations per SOBP and patient field, respectively, each with 250,000 protons starting at the entrance of the treatment head. Variance reduction techniques were employed increasing the statistical accuracy by a factor of 64 (Ramos-Méndez *et al* 2013). The fitted RBE model was implemented in TOPAS as a new extension and then used to simulate the RBE distributions in each patient case. Our goal was not to do a study on the clinical impact of RBE variations but rather show the use of the RBE model in a patient.

## 3. Results and Discussion

### 3.1 Fit Parameters

We found that the fitted model (Equation (4)) would extend to the complex plane when data points with  $(\alpha/\beta)_x \sim 0$  were included in the fit. In order to avoid this behavior, three

additional data points were removed from the primary data set. Two of these points had  $\alpha_x = 0$  Gy (Green *et al* 2001). The other point had  $(\alpha/\beta)_x = 6.2 \times 10^{-13}$  Gy (Hall *et al* 1978). The values of the fit coefficients in Equation (6) that best fit the experimental data, including the above mentioned restrictions, was found to be:  $p_0 = 0.99064$  (Standard Error (SE) 0.014125),  $p_1 = 0.35605$  (SE 0.015038),  $p_2 = 1.1012$  (SE 0.0059972) and  $p_3 = -0.0038703$  (SE 0.00091303) with a R-squared value of 0.255. From equation (4) we find,

$$RBE \left[ D_p, \left( \frac{\alpha}{\beta} \right)_x, LET_d \right] = \frac{1}{2D_p} \left( \sqrt{\left( \frac{\alpha}{\beta} \right)_x^2 + 4D_p \left( \frac{\alpha}{\beta} \right)_x \left( 0.999064 + \frac{0.35605}{(\alpha/\beta)_x} LET_d \right)} + 4D_p^2 \left( 1.1012 - 0.0038703 \sqrt{(\alpha/\beta)_x LET_d} \right)^2 - \left( \frac{\alpha}{\beta} \right)_x \right) \quad (7)$$

Figure 1 shows the dependence of the RBE for cell survival on  $LET_d$  and  $(\alpha/\beta)_x$  for a dose of 2 Gy (left panel) and 8 Gy (right panel) as predicted by our model. The experimental data used in the fit is also shown. The model predicts a decrease in RBE with increasing  $(\alpha/\beta)_x$  and an increase in RBE with increasing  $LET_d$ . As the dose increases, the model plane flattens and the RBE decreases. Figure 2 shows slices through the regression surface of our predicted model and plots the change in the response variable ( $D_p$ ,  $(\alpha/\beta)_x$  or  $LET_d$ ) as a function of RBE, when all other predictor values are constant. The red dashed curves show the 95% confidence bounds for the predicted response values. Figure 3 plots the predicted  $RBE_{max}$  and  $RBE_{min}$  for our model as a function of  $LET_d$  for two different values of  $(\alpha/\beta)_x$ . The experimental data is also plotted.

### 3.2 Model Comparison

**RBE as a function of LET**—Figure 4 plots the RBE as a function of  $LET_d$  predicted by three different biological models for different  $(\alpha/\beta)_x$  values and for a dose of 2 Gy. The horizontal grey dashed line represents a constant RBE of 1.1 and the vertical line a  $LET_d$  of 2.5 keV/ $\mu$ m ( $\sim$  average  $LET_d$  in the plateau region of the SOBP). For each of the models considered, the RBE increases with increasing  $LET_d$  with a somewhat linear relationship between RBE and  $LET_d$  (especially at large  $(\alpha/\beta)_x$ ). All models predict a positive slope of RBE as a function of  $LET_d$ , with a steeper slope occurring at low  $(\alpha/\beta)_x$ . This agrees with other theoretical studies which also find a linear relationship between RBE and  $LET_d$ , in the clinically relevant range of  $LET_d$  (Wilkins and Oelfke 2004, Chen and Ahmad 2012).

At low  $(\alpha/\beta)_x$  values (less than  $\sim 5$  Gy), our model predicts RBE values lower than the Carabe *et al.* and Wedenberg *et al.* models for  $LET_d \gtrsim 5$  keV/ $\mu$ m. At an  $(\alpha/\beta)_x$  of 1.22 Gy our model is  $\sim 8\%$  lower than the Wedenberg *et al.* model and  $\sim 13\%$  lower than Carabe *et al.* model for  $LET_d > 5$  keV/ $\mu$ m. Our model however predicts slightly higher RBE values at  $LET_d \lesssim 5$  keV/ $\mu$ m. For high  $(\alpha/\beta)_x$  values ( $\geq 10$  Gy), our model agrees better with the Wedenberg *et al.* model for low  $LET_d$  values. However at high  $LET_d$ , our model is similar to the Carabe *et al.* model. The discrepancy most likely reflects the limited data selected for the fits in both the Wedenberg *et al.* and Carabe *et al.* models.

To test the predictability of our model, we also include new experimental data on RBE as a function of  $LET_d$  (Guan *et al* 2015) for an  $(\alpha/\beta)_x$  of 1.22 Gy and 3.49 Gy, published after

Paganetti (2014). The reported  $\alpha$ ,  $\beta$ ,  $\alpha_x$ ,  $\beta_x$  and  $LET_d$  were extracted from the study and the RBE for 2 Gy was calculated for each data point. At low  $LET_d$ , most of the experimental data points fall in the region where all three of the models agree relatively well (within ~4%). At higher  $LET_d$  values, the experimental data agrees better with our model, within the uncertainties of the experiment. However the experimental data at very high  $LET_d$  values ( $LET_d = 18.7$  keV/ $\mu$ m) show RBE values much higher than those predicted by any of the three models. One reason for this discrepancy could be due to the assumption in all of the models that  $\alpha$  and  $\beta$  are linear functions of  $LET_d$ , whereas this experimental data seems to suggest an increase in slope as  $LET_d$  increases. This behavior is however not supported by our fit through all the experimental data.

**RBE as a function of  $(\alpha/\beta)_x$** —Figure 5 shows the RBE for cell survival as a function of  $(\alpha/\beta)_x$  for four different  $LET_d$  values and for a dose of 2 Gy, predicted with the same models as Figure 4. The RBE decreases with increasing  $(\alpha/\beta)_x$  for all three models. The decrease in RBE with increasing  $(\alpha/\beta)_x$  is most significant at low  $(\alpha/\beta)_x$  values, especially at large  $LET_d$  values, where the model curves are steeper.

Our model has closer agreement with the Wedenberg *et al.* model, especially at low  $LET_d$  values ( $\leq 5$  keV/ $\mu$ m). The Carabe *et al.* model predicts higher RBE values at low  $(\alpha/\beta)_x$  values ( $< 2$  Gy) than both other models but predicts much lower RBE values for  $(\alpha/\beta)_x$  values greater than ~5 Gy (up to 14% less in the case of  $LET_d = 2$  keV/ $\mu$ m).

In order to assess the predictive power of the model, experimental data published after the 2014 review (Paganetti 2014) are also shown in figure 5. The data were obtained in vitro using lung cancer cell lines for a  $LET_d$  of 1.31 and 1.89 keV/ $\mu$ m, relative to the reference photon radiation (Liu *et al* 2015). At a  $LET_d$  of 1.31 keV/ $\mu$ m, the majority of the experimental data predicts RBE values less than ~1.1. The experimental data however doesn't favor one particular model. At a  $LET_d$  of 1.89 keV/ $\mu$ m, most of the RBE data values are larger than 1.1, which all three models underestimate. The large spread in the experimental data demonstrates not only the challenge in measuring RBE but also the difficulty in determining an effective model from this data.

**RBE as a function of dose**—Figure 6 shows the RBE for cell survival as a function of dose for different  $(\alpha/\beta)_x$  values and for an  $LET_d$  of 2.5 keV/ $\mu$ m. The  $LET_d$  was chosen as an approximate value of the  $LET_d$  in the plateau region of a SOBP (~2–3 keV/ $\mu$ m). The RBE decreases with increasing dose for  $(\alpha/\beta)_x \leq 2$  Gy for all models. For large  $(\alpha/\beta)_x$ , the RBE in the Carabe *et al.* model increases with increasing dose. The Wedenberg *et al.* model however predicts a decrease in RBE with increasing dose for all  $(\alpha/\beta)_x$  values considered. For high  $(\alpha/\beta)_x$ , the slope of our model converges to zero with RBE ~ 1.08 and 1.05 for  $(\alpha/\beta)_x = 10$  and 15 Gy, respectively.

Most experiments predict an increase of RBE as dose decreases, however some experimental data indicate the opposite behavior (Paganetti 2014). Overall, the fitted model has better agreement with the Carabe *et al.* model at low  $(\alpha/\beta)_x$ , predicting RBE values ~7% higher than the Wedenberg *et al.* model for  $(\alpha/\beta)_x = 2$  Gy. However at high  $(\alpha/\beta)_x$ , the fitted model predicts RBE values up to ~11% higher than the Carabe *et al.* model.

In the Carabe *et al.* models, the trend of increasing RBE with increasing dose is due to the fact that  $RBE_{\min}$  (RBE as  $D \rightarrow \infty$  Gy) is larger than  $RBE_{\max}$  (RBE as  $D \rightarrow 0$  Gy) for high  $(\alpha/\beta)_x$  values (and low  $LET_d$  values). This trend is not observed in some other models which predict a decrease in RBE for increasing dose for all  $(\alpha/\beta)_x$  and  $LET_d$  values (Wedenberg *et al.* 2013, Elsässer *et al.* 2010, Wilkens and Oelfke 2004, Jones 2015). This is discussed further in (Grün *et al.* 2013). An increase of RBE with dose is also not observed in our model.

### Spread out Bragg Peak (SOBP) simulation

The RBE values calculated by our, Wedenberg *et al.* and Carabe *et al.* models using the  $LET_d$  and dose values of the simulated SOBP are shown in Figure 7. The simulated SOBP had a modulation width of 10 cm and range of 25 cm with an average  $LET_d$  of  $\sim 3$  keV/ $\mu\text{m}$  in the plateau region of the SOBP. The  $LET_d$  in the middle of the plateau region of the SOBP (depth  $\sim 160 - 220$  cm) ranged from 1.4 – 3.1 keV/ $\mu\text{m}$  and from  $\sim 1.4 - 10$  keV/ $\mu\text{m}$  over the entire plateau region.

Each of the considered RBE models predict an increase in the biological dose at the distal edge of the SOBP as a result of the increase in  $LET_d$  ( $\sim 7$  keV/ $\mu\text{m}$  at 90% dose in the distal falloff) combined with a sharp drop in dose. At  $(\alpha/\beta)_x = 1$  Gy, the Carabe *et al.* model predicts the highest biological dose in the SOBP. At 90% dose in the distal falloff, the Carabe *et al.* model predicts a biological dose  $\sim 9\%$  higher than our model. At the same point in the distal falloff, our model has a biological dose 28% higher than the dose scaled by 1.1, which is generally used in clinical treatment planning. The three models have the best agreement at an  $(\alpha/\beta)_x$  of 2 Gy, especially in the plateau region of the SOBP. At 90% dose in the distal falloff, the Carabe *et al.* and Wedenberg *et al.* models both predict  $\sim 5\%$  more biological dose than our model.

At an  $(\alpha/\beta)_x$  value of 10 Gy, our model and the Wedenberg *et al.* model closely agree within  $\sim 1-2\%$ , predicting RBE values between the physical and constant biological dose. At the distal edge, both models predict RBE values slightly larger than the constant RBE = 1.1 case ( $\sim 4\%$  higher). The Carabe *et al.* model predicts values lower than the physical dose in these regions except for at the distal edge, where the Carabe *et al.* model is approximately equal to the constant biological dose. This is a result of the Carabe *et al.* model predicting RBE values below 1.0 for low  $LET_d$  values (see Figure 5).

Two different proton treatment plans were simulated; a prostate and pediatric head and neck case, to demonstrate the RBE model predictions in a patient. The prostate case consisted of two transverse beams. We assume a prostate  $(\alpha/\beta)_x$  value of 1.5 Gy with  $\alpha_x = 0.036$  Gy $^{-1}$  and  $\beta_x = 0.024$  Gy $^{-2}$  (Brenner and Hall 1999). The rectum as well as the surrounding tissue  $(\alpha/\beta)_x$  value was set to 3.1 Gy with  $\alpha_x = 0.0890$  Gy $^{-1}$  and  $\beta_x = 0.0287$  Gy $^{-2}$  (Terry and Denekamp 1984). The head and neck treatment plan consisted of 10 beams. The  $(\alpha/\beta)_x$  value of the target volume was set to 11 Gy with  $\alpha_x = 0.55$  Gy $^{-1}$  and  $\beta_x = 0.019$  Gy $^{-2}$  (Steele et al. 1991). The  $(\alpha/\beta)_x$  value of the rest of the brain was set to 2.1 Gy with  $\alpha_x = 0.0499$  Gy $^{-1}$  and  $\beta_x = 0.0238$  Gy $^{-2}$  (Meeks *et al.* 2000). For each case, the different  $(\alpha/\beta)_x$  values were assigned to the relevant contours in the patient plan (e.g. 1.5 Gy to the prostate PTV and 3.1 Gy to all others). The left and right panels of figure 8 show both the prostate and the head



and neck cases, combining all treatment fields for a total prescribed dose of 1.8 Gy per fraction. The biological dose with RBE assumed to be 1.1 is shown in (a) and (d) for each case. The biological dose with the RBE calculated from the proposed model is shown in (b) and (e) for each case. The difference between the biological dose with constant RBE and that calculated with the proposed model is shown in (c) and (f).

In the case of the prostate treatment plan, two beams are delivered transversely and the distal edges of each SOBP have a higher RBE value than that of the plateau region of the SOBP. The plateau region coincides with the primary target volume (PTV). In this case, the areas that receive a higher biological dose as predicted by our model do not coincide with any critical structure (e.g. the rectum, represented by the black contour). The elevated RBE is mainly driven by the low value of the  $(\alpha/\beta)_x$  value in the prostate. The actual RBE values calculated within the prostate target were  $\sim 1.2$ , while the RBE values occurring in the regions adjacent to the target region were  $\sim 1.3$ , instead of the assumed constant RBE of 1.1. Thus, the prescribed dose to the target would be exceeded by  $\sim 9\%$  based on our model calculations, which could impact the interpretation of clinical trials comparing tumor control for proton versus photon therapy.

In the case of the head and neck treatment plan, the proposed model predicts that the region just outside the target volume receives a biological dose significantly higher than assumed by the current clinical practice using an RBE of 1.1. In this particular case, this region does coincide with a critical structure, the brainstem. The RBE values within the target were  $\sim 1.1$  but those occurring within the sensitive brainstem were  $\sim 36\%$  higher (RBE  $\sim 1.5$ ). It has been suggested that in cases where proton fields stop in the brainstem, elevated RBE values could lead to brainstem toxicity. A recent study did not find statistically significant evidence to support this claim (Giantsoudi et al. 2015).

Figure 8 is shown to demonstrate how the use of our model might impact the RBE-weighted dose in proton therapy. Since this paper focuses on the model parameterization, an extended discussion about the clinical impact is beyond the scope of the manuscript. Note that the majority of published RBE values are based on clonogenic cell survival in vitro, which sheds some light on RBE variations in patients with respect to tumor control probability (TCP). Our model, as well as the majority of models previously published is based on clonogenic cell survival. The relevance of this data to define an RBE for normal tissue complications probabilities (NTCP) is controversial (Paganetti 2014, 2015). Due to lack of sufficient experimental data, RBE variations deduced from cell survival data may have to be considered not only for TCP but also for NTCP considerations.

## Conclusion

We present a phenomenological model based on the well-know LQ model, to determine proton RBE as a function of dose averaged LET, the tissue specific  $(\alpha/\beta)_x$  parameter and dose. Our model makes the assumptions of an inverse linear relationship of  $RBE_{\max}$  to  $(\alpha/\beta)_x$  and a linear relationship of  $RBE_{\min}$  to  $\sqrt{(\alpha/\beta)_x}$  as supported by the LQ model.

The model was derived using a non-linear regression fit to all published RBE experimental measurements before September 2014. The fitted model incorporates experimental data from a range of different  $(\alpha/\beta)_x$  values (cell lines) as well as LET values for different doses, simultaneously. All previously published phenomenological models were based on limited experimental data sets.

The proposed model predicts an increase in RBE with increasing  $LET_d$  and a decrease in RBE with increasing  $(\alpha/\beta)_x$ . These relationships agree with observations from previous studies and with other theoretical predictions (Wedenberg *et al* 2013, Carabe *et al* 2012). The proposed model predicts a dose dependence on the RBE that depends on the  $LET_d$  and  $(\alpha/\beta)_x$  values. For low  $(\alpha/\beta)_x$  values, the RBE decreases with increasing dose. However for low  $LET_d$  and high  $(\alpha/\beta)_x$  values, the RBE has very little dependence on dose. The proposed model assumes a linear relationship between  $\alpha$  and  $LET_d$  as well as between  $\beta$  and  $LET_d$ . Some other models predict a constant  $\beta$  ( $\beta = \beta_x$ ) (Wedenberg *et al* 2013, Chen and Ahmad 2012, Wilkens and Oelfke 2004), while the model by Carabe *et al.* uses a linear relationship between  $RBE_{min}$  and  $LET_d$  with a positive slope dependent on the inverse of  $(\alpha/\beta)_x$ . Our model predicts a linear relationship between  $RBE_{min}$  and  $LET_d$  but with a small negative slope dependent on the square root of  $(\alpha/\beta)_x$ .

The proposed model predicts the RBE for cell survival and is thus not necessarily applicable to other endpoints. While our model suffers from considerable uncertainties due to the spread of the underlying data, it can serve as a guideline when comparing proton and photon therapy results on tumor control and toxicities. The implications of experimental RBE values for tumor control probabilities and normal tissue complication probabilities have been discussed elsewhere (Paganetti 2014).

## Acknowledgments

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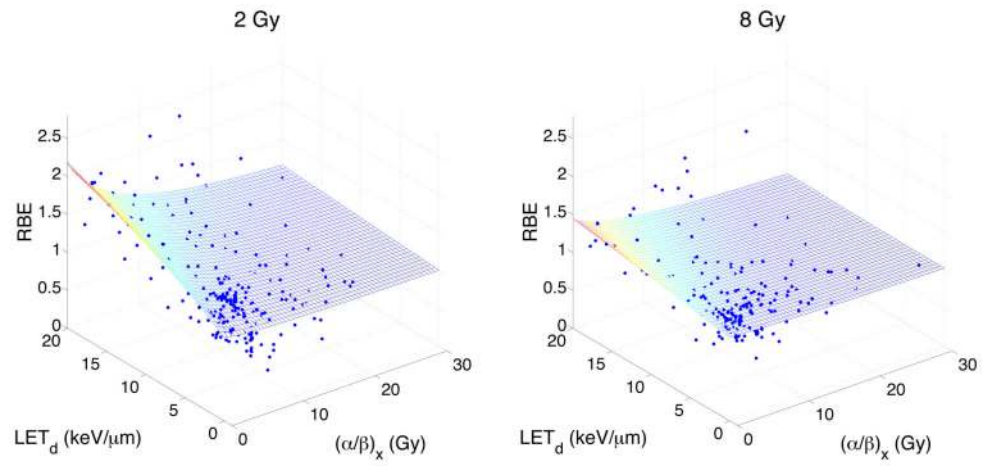
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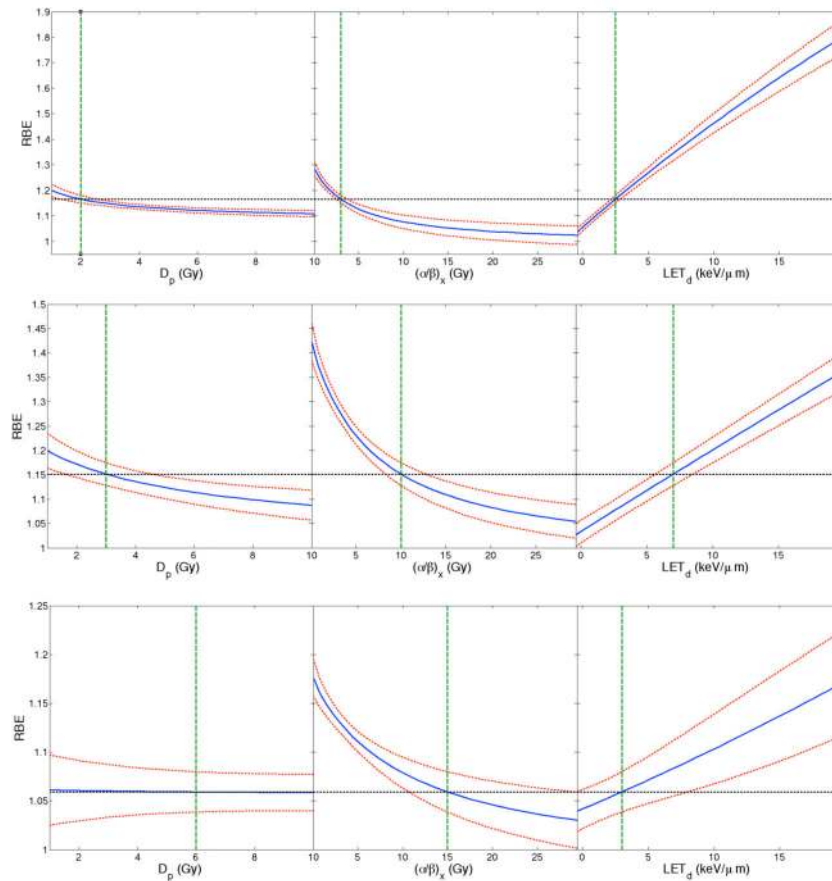
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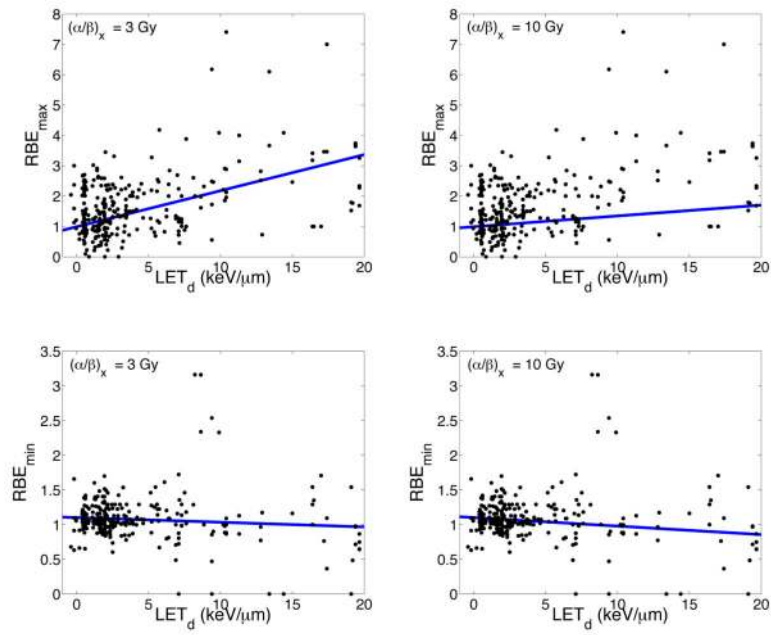
**Figure 1.** The RBE for cell survival as a function of LET<sub>d</sub> and  $(\alpha/\beta)_x$  for a dose of 2 Gy (left panel) and 8 Gy (right panel) as predicted by our model. The experimental data used in the fit is also plotted. The LET<sub>d</sub> is given relative to the reference photon radiation.



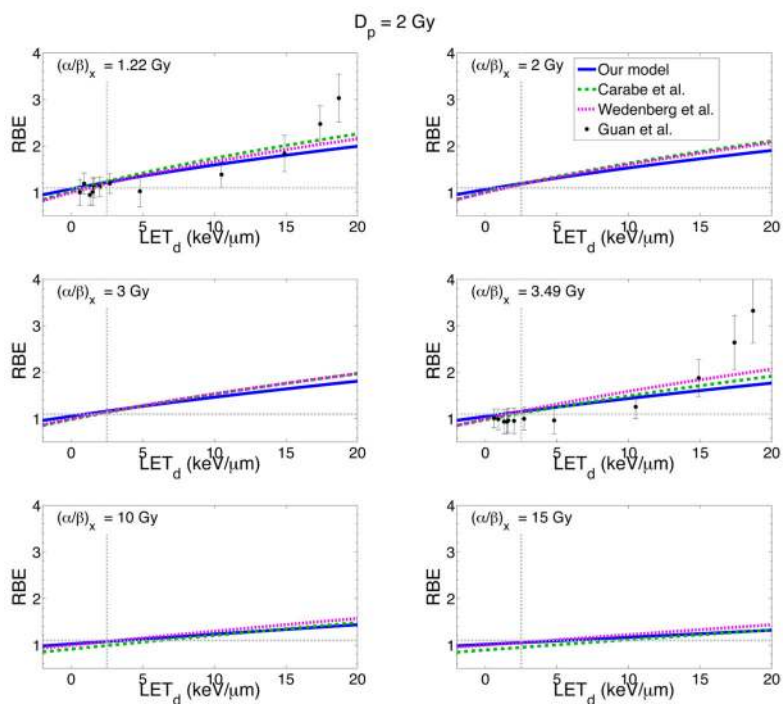
**Figure 2.**

Slices through the regression surface of our predicted model. The blue line in each row shows the change in the parameters ( $D_p$ ,  $(\alpha/\beta)_x$  or  $LET_d$ ) as a function of RBE when all other predictors are held constant. The horizontal dashed black line in each panel shows the predicted RBE for the specific values of the predictor variables corresponding to the dashed vertical green lines. The red curves in each panel show the 95% simultaneous confidence bounds for the predicted response values. The top panel represents the case where  $D_p = 2$  Gy,  $(\alpha/\beta)_x = 3$  Gy and  $LET_d = 2.5$  keV/ $\mu$ m, the middle row where  $D_p = 3$  Gy,  $(\alpha/\beta)_x = 15$  Gy and  $LET_d = 7$  keV/ $\mu$ m and the bottom row where  $D_p = 6$  Gy,  $(\alpha/\beta)_x = 15$  Gy and  $LET_d = 3$  keV/ $\mu$ m.



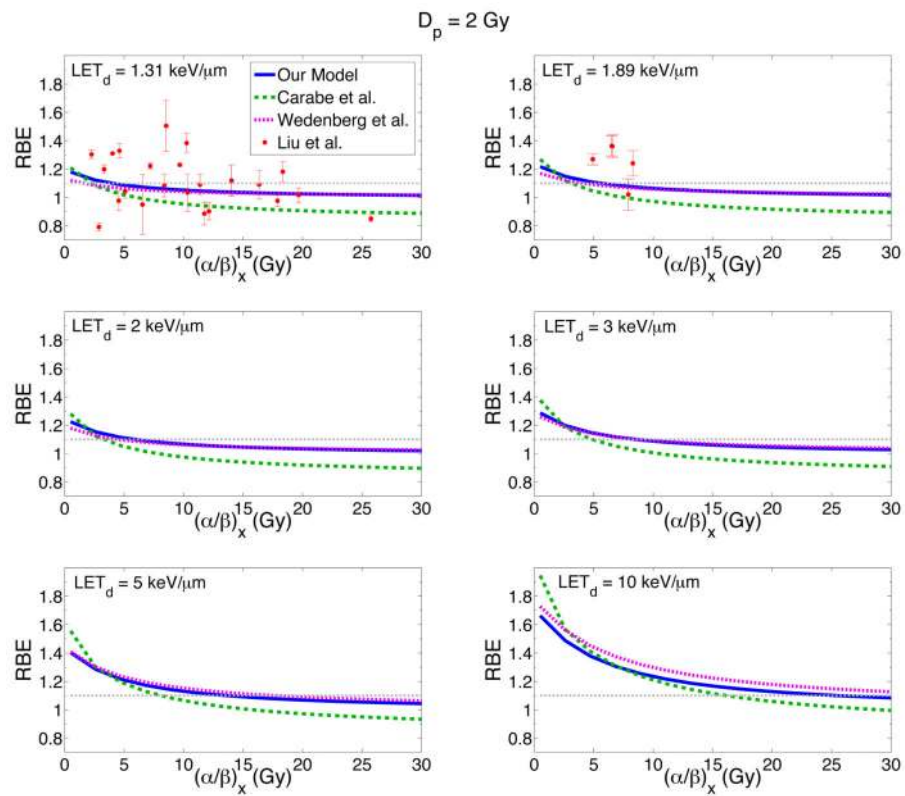


**Figure 3.**  $RBE_{max}$  and  $RBE_{min}$  as predicted by our model as a function of  $LET_d$  for an  $(\alpha/\beta)_x$  of 3 and 10 Gy. The experimental data is also included in the plots.



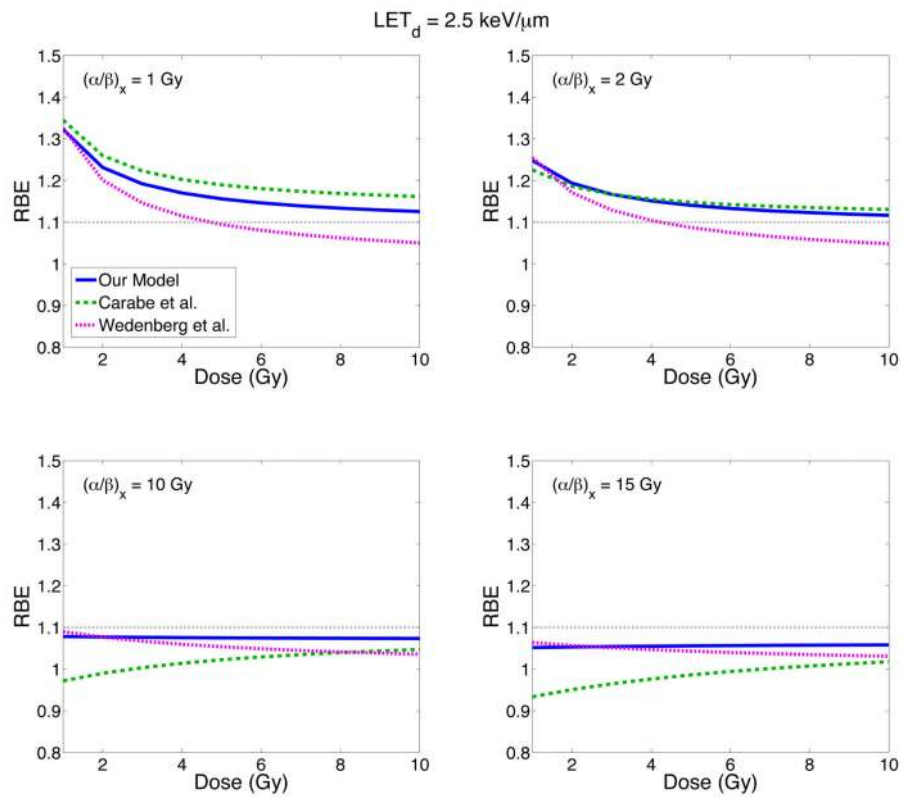
**Figure 4.**

RBE for cell survival as a function of  $\overline{LET}_d$  for six different  $(\alpha/\beta)_x$  values and a dose of 2 Gy. Three different models predict the RBE: our model (blue solid line), the Carabe *et al.* model (green dashed line) and the Wedenberg *et al.* model (pink dotted line). To test the predictability of the models, recently published experimental data for two different  $(\alpha/\beta)_x$  values is also included (Guan et al. 2015).

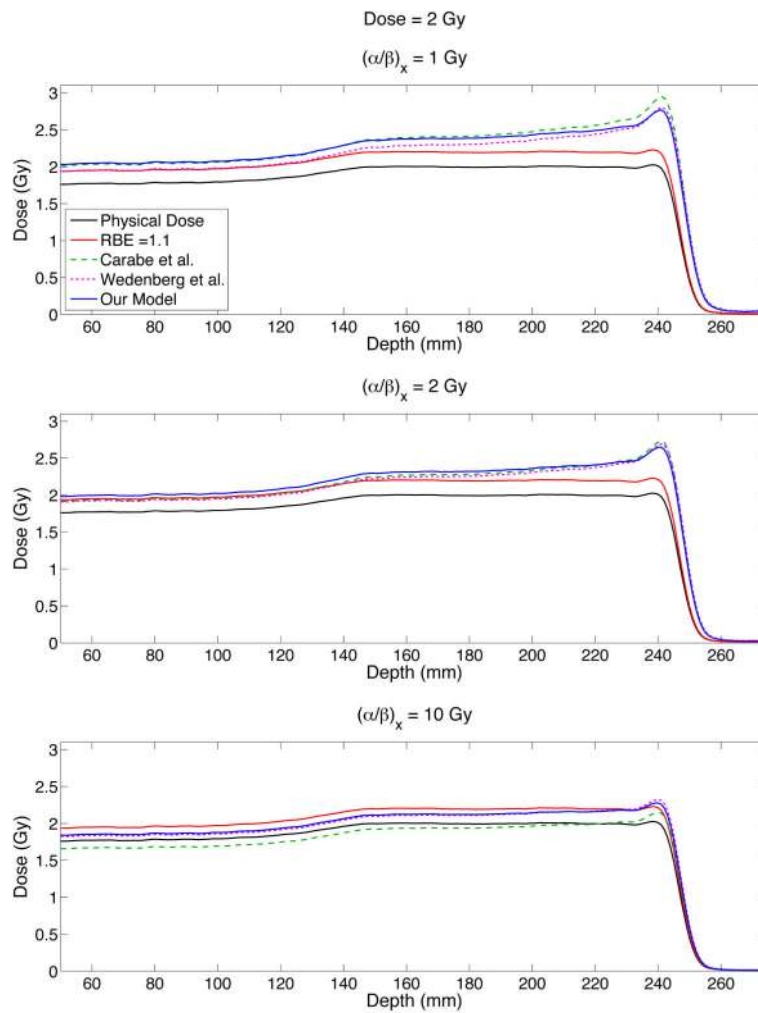


**Figure 5.**

RBE for cell survival as a function of  $(\alpha/\beta)_x$  for six different  $LET_d$  values and a dose of 2 Gy. Three different models predict the RBE: our model (blue solid line), the Carabe *et al.* model (green dashed line) and the Wedenberg *et al.* model (pink dotted line). To test the predictability of the models, recently published experimental data for  $LET_d$  values of 1.31 and 1.89 keV/ $\mu\text{m}$  is also included (Liu et al. 2015).

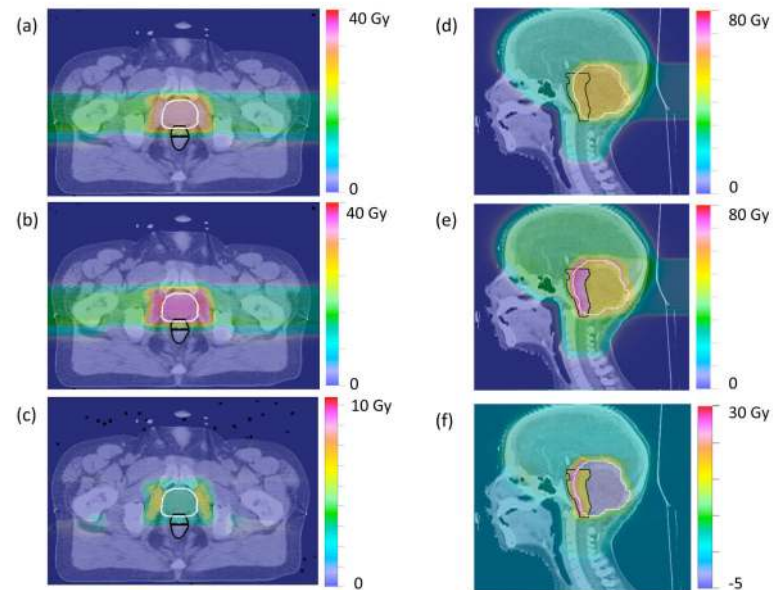


**Figure 6.** The RBE as a function of dose for different  $(\alpha/\beta)_x$  values. Three different models predict the RBE: our model (blue solid line), the Carabe *et al.* model (green dashed line) and the Wedenberg *et al.* model (pink dotted line).



**Figure 7.** Predicted biological doses for three different models: Carabe *et al.* model (green dashed curve), the Wedenberg *et al.* model (pink dotted curve) and our model (blue solid curve) for a simulated spread out Bragg peak (SOBP) with a modulation width of 10 cm and a range of 25 cm. The physical dose is shown by the black solid curve while the red curve shows the physical dose scaled by a constant value of 1.1.

## Patient Simulation

**Figure 8.**

Patient simulation studies of prostate (left panel) and head and neck (right panel) proton treatments. The biological dose with a constant RBE of 1.1 is plotted in (a) and (d) for the prostate and head and neck cases, respectively. The prescribed dose for the head and neck case was 55 Gy, while that for the prostate case was 35 Gy. The biological dose calculated with our proposed model is plotted in (b) and (e) for each case. The plots in (c) and (f) show the difference in biological dose between the RBE = 1.1 and the proposed model cases. The PTV is shown in white in both cases, while the rectum and brain stem (sensitive critical structures) are shown in black for each respective case.