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A PROOF OF TWO CONJECTURES OF CHAO–PING CHEN FOR INVERSE TRIGONOMETRIC FUNCTIONS

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Abstract. In this paper we prove two conjectures stated by Chao-Ping Chen in [Int. Trans. Spec. Funct. 23:12 (2012), 865–873], using a method for proving inequalities of mixed trigonometric polynomial functions.

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