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A PULSED POWER SUPPLY FOR INJECTION BUMP MAGNETS

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A PULSED POWER SUPPLY FOR INJECTION BUMP MAGNETS\*

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Summary

A very precise and relatively inexpensive charging circuit for an energy storage capacitor bank feeds an efficient thyristor-controlled pulse-forming discharge circuit. These circuits, which generate magnet pulses of 300 joules at a rate of 30 per second, are analyzed in this paper.

Introduction

For injection of  $H^-$  ions at 50 MeV into a synchrotron at Argonne National Laboratory, three injection bump magnets must be pulsed 30 times per second. Figure 1 shows the orbit deformation produced by the magnets during injection.

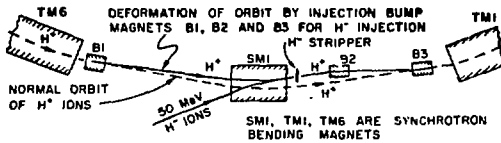


Fig. 1.  $H^-$  injection at 50 MeV into a 500 MeV synchrotron.

Figure 2 shows the desired current pulse and associated magnet voltage for the series-connected magnets. The current rises sinusoidally to its peak value of 3 kA in 500  $\mu$ s. After the current has passed its peak, it decays exponentially during the beam-injection time. At the end of injection, the current must be turned off within 125  $\mu$ s because the magnetic field would interfere with beam acceleration. The current shape during turnoff is unimportant and, for this reason, is shown as a straight line in Fig. 2. Different modes of injection require that the time constant of the injection field be adjustable between 1.2 ms (solid waveforms in Fig. 2) and 0.45 ms (dotted waveforms in Fig. 2). No commutation spikes may appear in the current waveform.

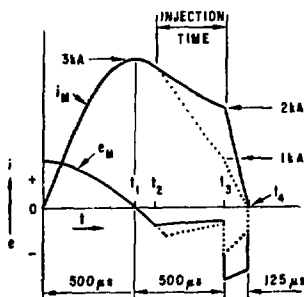


Fig. 2. Desired current and voltage for beam bump magnets.

\*Work supported by the U. S. Energy Research and Development Administration.

A Pulsed Power Supply With Limited Energy Recovery

Figure 3 is a schematic diagram of a charging circuit to store energy in capacitor  $C_1$  and of a discharge circuit which generates the desired magnet pulse with a minimum number of circuit components.

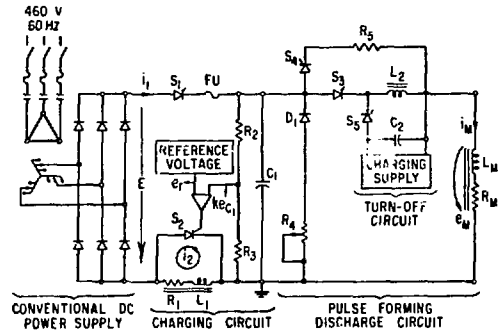


Fig. 3. Power supply for beam bump magnets.

A Controlled Charging-Choke Circuit with Energy Recovery

When thyristor  $S_1$  is turned on, the unregulated voltage  $E$  of a conventional dc power supply is applied to a charging circuit comprising  $L_1$ ,  $C_1$ , and  $R_1$ . As shown in Fig. 4, voltage  $E$  drives a sinusoidal current  $i_1$ . Between times  $t_1$  and  $t_2$ , the decaying current generates a voltage  $L_1 di_1/dt$ , which adds the supply voltage  $E$  to charge capacitor  $C_1$  to a voltage greater than  $E$ . When  $R_1 \rightarrow 0$ , this voltage would be, at time  $t_2$ ,  $e_{C_1} = 2E$ .

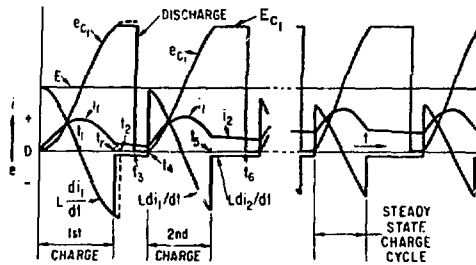


Fig. 4. Currents and Voltages of the Charging Circuit of Figure 3.

With thyristor  $S_2$  across the charging choke  $L_1$ , we can terminate the charging cycle at any instant between times  $t_1$  and  $t_2$ . The charging circuit compares a fraction of the capacitor voltage  $ke_C$  with a reference voltage  $e_r$ . At time  $t_r$ , when these voltages are equal, a pulse is generated which turns  $S_2$  on.

With  $S_2$  conducting, the driving voltage  $L_1 di_1/dt$  is removed from the circuit, and with the capacitor voltage  $e_{C_1}$  larger than the power-supply voltage  $E$ , thyristor  $S_1$  is back biased and turns off, thereby stopping the charging current  $i_1$ . Thus capacitor  $C_1$  is charged to a very precisely controlled voltage  $E_{C_1}$  (error  $\pm 0.1\%$ ) from a poorly regulated ( $\pm 2\%$ ) dc power supply.

The current  $i_2$  flowing in choke  $L_1$  at time  $t_r$  will decay with a time constant of  $L_1/R_1$ . At time  $t_3$ , capacitor  $C_1$  discharges into the magnet load. Thyristor  $S_2$  remains turned on by the circulating current  $i_2$  until time  $t_4$ , when the next charging cycle is initiated by turning on  $S_1$ .

With  $S_1$  conducting, the supply voltage  $E$  is back-biasing  $S_2$  and thereby turning it off. This returns the choke to the charging circuit, and the above cycle repeats. The current  $i_2$  flowing in the choke when  $S_2$  is turned off will aid in charging capacitor  $C_1$ . The energy  $0.5 L_1 i_2^2$  is returned to the circuit. This makes the charging circuit not only a very precise voltage regulator, but also very efficient.

The range of the capacitor voltage  $E_{C_1} = e_r/k$  is controlled by selecting the appropriate taps on the rectifier transformer for a choice of supply voltage  $E$ . By adjusting the reference voltage  $e_r$ , we can obtain any voltage value  $E_{C_1}$  within a given range. Table 1 shows the three overlapping ranges that cover voltages  $E_{C_1}$  from 200 to 800 V.

Table 1. Ranges of Capacitor Voltage  $E_{C_1}$

Power Supply Voltage $E$	Range of $E_{C_1}$ Controlled by Setting of $e_r$
Tap 1: 187 V	200-365 V
Tap 2: 271 V	290-529 V
Tap 3: 410 V	439-800 V

As shown in Fig. 4, it takes several charging cycles with increasing peak currents to reach the steady-state waveform. When  $S_1$  is turned on, the charging current  $i_1$  and the capacitor voltage  $e_{C_1}$  follow the equations

$$i_1 = I_0 e^{-\alpha t} \cos \omega t + \frac{E - I_0 R_1/2}{\omega L_1} e^{-\alpha t} \sin \omega t, \quad (1)$$

and

$$e_{C_1} = I_0 L_1 \left[ \alpha e^{-\alpha t} (\alpha \cos \omega t - \omega \sin \omega t) \right] + (E - I_0 R_1/2) \left[ 1 - e^{-\alpha t} \left( \frac{\alpha}{\omega} \sin \omega t + \cos \omega t \right) \right], \quad (2)$$

where

$I_0$  = current circulating in  $L_1$  at  $t_0$ ,

$\alpha = R_1/2L_1$ ,

$\omega = (1/L_1 C_1 - \alpha^2)^{1/2}$ ,

and

$E$  = Power-supply voltage.

The waveshapes illustrated in Fig. 4 are shown in detail in Fig. 5 for a desired capacitor voltage of  $E_{C_1} = 800$  V. The first charge cycle takes  $t_r = 23.1$  ms and ends at time  $t_r$  with a choke current of  $i_2 t_r = 15.2$  A. The current then circulates through  $L_1$  for 10.2 ms, during which time it decays to

$$i_2 t_4 = i_2 t_r e^{-\frac{R_1}{L_1}(t_4 - t_r)} = 15.2 \text{ A } e^{-\frac{0.1}{0.038} 0.0102} = 14.8 \text{ A}. \quad (3)$$

The second charge cycle begins at  $t_4$  with  $i_2 = 14.8$  A and lasts for 21 ms, ending at time  $t_5$  with a current of  $i_2 t_5 = 22$  A. After a few more cycles, a steady-state condition is reached with current and voltage waveforms as shown in Fig. 5.

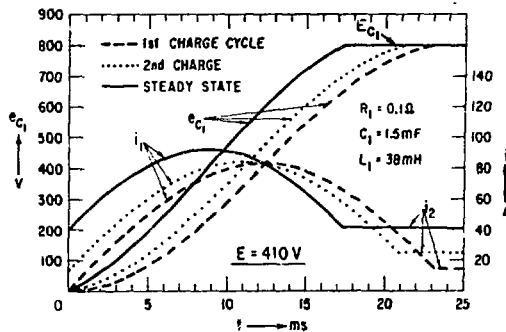


Fig. 5. Current, and voltages of the charging circuit of Figure 3 for  $E = 410$  V.

#### A Discharge Circuit Without Energy Recovery.

With  $C_1$  charged to  $E_{C_1}$ , a magnet pulse as illustrated in Fig. 6 is initiated with the circuit of Fig. 3 by turning on thyristor  $S_3$ . Capacitor voltage  $E_{C_1}$  drives a sinusoidally rising current of

$$i_M = \frac{E_{C_1}}{\omega_1 L} e^{-\alpha_1 t} \sin \omega_1 t, \quad (4)$$

where

$$L = L_M + L_2 = 60 \mu\text{H} + 7 \mu\text{H} = 67 \mu\text{H},$$

$$\alpha_1 = R/2L,$$

$$\omega_1 = (1/LC_1 - \alpha_1^2)^{1/2},$$

and

$$R = \text{total effective circuit resistance.}$$

The current reaches its peak at time

$$t_1 = \frac{1}{\omega_1} \tan^{-1} \frac{\omega_1}{\alpha_1}. \quad (5)$$

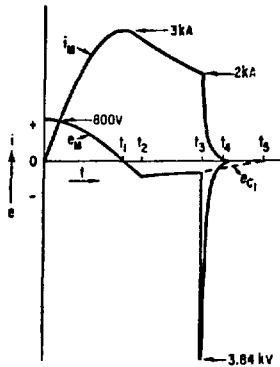


Fig. 6.  
Magnet pulse generated by the discharge circuit of Figure 3.

After the current has reached its peak, the voltage on  $C_1$  reverses its polarity and the current begins to transfer into the crowbar consisting of adjustable resistor  $R_4$  and diode  $D_1$ ;  $D_1$  was back-biased by  $e_{C_1}$  during the current rise. This current transfer takes place between times  $t_1$  and  $t_2$ . For oscillatory circuit conditions, the current and voltage shapes during transfer are

$$i_{C_1} = i_{t_1} e^{-\alpha_2 t} \left( \cos \omega_2 t - \frac{\alpha_2}{\omega_2} \sin \omega_2 t \right), \quad (6)$$

$$e_{C_1} = \frac{i_{t_1}}{C_1} \frac{\alpha_2}{\alpha_2^2 + \omega_2^2} \left\{ \left[ 1 - e^{-\alpha_2 t} \left( \cos \omega_2 t - \frac{\omega_2}{\alpha_2} \sin \omega_2 t \right) \right] - \left[ 1 - e^{-\alpha_2 t} \left( \frac{\alpha_2}{\omega_2} \sin \omega_2 t + \cos \omega_2 t \right) \right] \right\}, \quad (7)$$

$$i_{R_4} = \frac{i_{t_1}}{\omega_2 C_1 R_4} e^{-\alpha_2 t} \sin \omega_2 t, \quad (8)$$

and

$$e_{R_4} = e_{C_1} = \frac{i_{t_1}}{\omega_2 C_1} e^{-\alpha_2 t} \sin \omega_2 t, \quad (9)$$

where

$$\alpha_2 = \frac{R_4 R_M C_1 + L}{2LC_1 R_4},$$

$$\omega_2 = \left( \frac{R_4 + R_M}{LC_1 R_4} - \alpha_2^2 \right)^{1/2},$$

$$L = L_M + L_2,$$

and

$$t = \text{time after } t_1 \text{ in Fig. 6.}$$

If the crowbar resistor overdamps the circuit,

$\alpha_2^2 > (R_4 + R_M)/LC_1 R_4$ , the above equations change to

$$i_{C_1} = i_{t_1} e^{-\alpha_2 t} \left( \cosh \omega_3 t - \frac{\alpha_2}{\omega_3} \sinh \omega_3 t \right), \quad (10)$$

$$e_{C_1} = \frac{i_{t_1}}{C_1} \frac{\alpha_2}{\alpha_2^2 - \omega_3^2} \left\{ \left[ 1 - e^{-\alpha_2 t} \left( \cosh \omega_3 t + \frac{\omega_3}{\alpha_2} \sinh \omega_3 t \right) \right] - \left[ 1 - e^{-\alpha_2 t} \left( \frac{\alpha_2}{\omega_3} \sinh \omega_3 t + \cosh \omega_3 t \right) \right] \right\}, \quad (11)$$

$$i_{R_4} = \frac{i_{t_1}}{\omega_3 R_4 C_1} e^{-\alpha_2 t} \sinh \omega_3 t, \quad (12)$$

and

$$e_{R_4} = \frac{i_{t_1}}{\omega_3 C_1} e^{-\alpha_2 t} \sinh \omega_3 t, \quad (13)$$

where

$$\omega_3 = \left( \alpha_2^2 - \frac{R_4 + R_M}{LC_1 R_4} \right)^{1/2}.$$

At time  $t_2$ , the current transfer is completed. Figure 7 shows voltage and current shapes during the transfer time for various values of  $R_4$ .

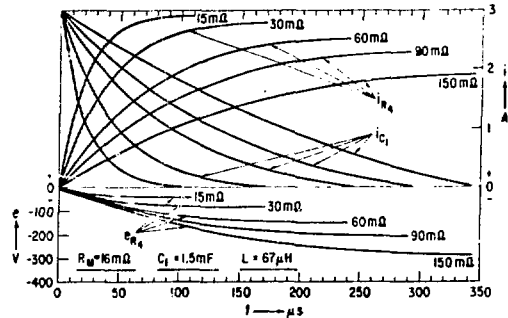


Fig. 7. Currents and voltages during transfer of current into crowbar.

Between times  $t_2$  and  $t_3$ , the exponentially decaying magnet current and voltage shown in Fig. 6 are given by

$$i_M = i_{t_2} e^{-\frac{R_4 + R_M}{L_2 + L_M} t}, \quad (14)$$

and

$$\hat{e}_M = \left[ R_M - \frac{L_M(R_4 + R_M)}{L_2 + L_M} \right] i_{t_2} e^{-\frac{R_4 + R_M}{L_2 + L_M} t} \quad (15)$$

Injection is terminated at time  $t_3$  when thyristors  $S_4$  and  $S_5$  are turned on. This causes the charge on capacitor  $C_2$  to discharge through  $L_2$  via  $S_5$  and through  $R_5$  via  $S_5$ ,  $S_3$ , and  $S_4$ . The reverse current through  $S_5$  and the reverse voltage provided by the voltage on  $C_2$  will turn off  $S_3$  in  $\leq 25 \mu s$ . Thyristor  $S_5$  turns off when the current in the oscillatory  $L_2 C_2$  circuit tries to reverse after  $C_2$  has reached its negative peak voltage. Figure 8 illustrates current and voltage waveforms of the turnoff circuit.

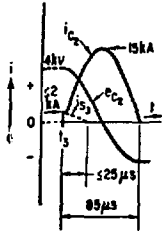


Fig. 8. Discharge of turnoff circuit of Figure 3.

When  $S_3$  turns off, the magnet discharges into  $R_4 + R_5$ . As shown in Fig. 6, the magnet coil is then exposed to a peak voltage of

$$\hat{e}_M = L_M \frac{di}{dt} \Big|_{t_3} - i_{t_3} R_M = i_{t_3} (R_4 + R_5) \quad (16)$$

At the end of the  $125 \mu s$  turnoff time, at time  $t_4$ , we can tolerate a current that is  $\leq 2\%$  of the current flowing at time  $t_3$ . This requires a time constant for the turnoff circuit of  $\tau \leq L_M / (R_4 + R_5) \leq 125 \mu s / 4 \leq 31.25 \mu s$ . With  $L_M = 60 \mu H$ , we require  $R_4 + R_5 \geq 60 / 31.25 \geq 1.92 \Omega$ ; almost all of this resistance value is provided by  $R_5$ . This forces a peak magnet driving voltage of  $\hat{e}_M \approx 1.92 \Omega \times 2 \text{ kA} = 3.84 \text{ kV}$ . The negative charge on  $C_1$  is dissipated in  $R_4$  between times  $t_3$  and  $t_5$ .

The relatively simple discharge circuit shown in Fig. 3 has the following very undesirable features:

- The magnet voltage at turnoff is  $\sim 3.8 \text{ kV}$ .
- The coil windings of the magnets and of inductor  $L_2$  must be rated for  $4 \text{ kV}$ .
- Thyristor assemblies  $S_3$ ,  $S_4$ , and  $S_5$  must be rated for  $4 \text{ kV}$ .
- The  $105 \mu F$  turnoff capacitor  $C_2$  must be rated for  $4 \text{ kV}$ .
- The turnoff circuit carries a peak current of  $15 \text{ kA}$ .
- The energies stored at the end of injection in the magnets and in  $C_1$  are lost. These energies, at  $2 \text{ kA}$  and  $R_4 = 50 \text{ m}\Omega$ , will amount to  $120 \text{ J}$  in the magnet and  $7.5 \text{ J}$  in  $C_1$ . They cause losses of  $3.83 \text{ kW}$  at a  $30 \text{ Hz}$  repetition rate.

(g) A  $4 \text{ kV}$  charging power supply is required for the turnoff circuit.

#### A Pulsed Power Supply With Optimum Energy Recovery

To avoid the shortcomings of the circuit of Fig. 3, we developed the more sophisticated circuit shown in Fig. 9. A typical magnet pulse generated by this circuit is shown in Fig. 10.

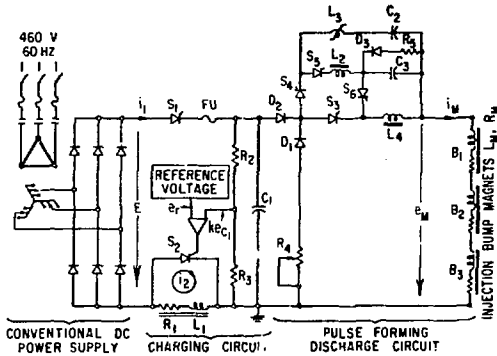


Fig. 9. Power supply with optimized energy recovery.

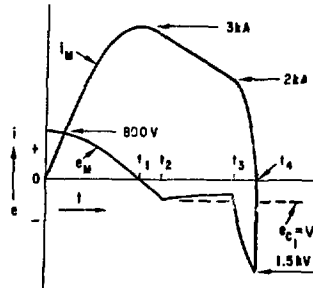


Fig. 10. Magnet pulse generated by the discharge circuit of Figure 9.

#### Controlled Charging-Choke Circuit with Energy Recovered from $C_1$

A negative charge is accumulated on  $C_1$  when the magnet is crowbarred by diode  $D_1$  with resistor  $R_4$  at time  $t_2$  in Fig. 10. Diode  $D_2$  prevents this charge from dissipating in  $R_4$ . This is shown as a dashed line  $e_{C_1} = V$  in Fig. 10 and has a profound effect on circuit efficiency. The energies stored in  $C_1$  and in  $L_1$  at the end of a magnet pulse will aid the dc power supply in charging  $C_1$  to  $V_{C_1}$  for the next magnet pulse.

As shown in Fig. 11, the very first charging pulse of the circuit of Fig. 9 is identical to the first one of the circuit of Fig. 3. However, in the circuit of Fig. 9, the negative charge on  $C_1$ , proportional to the trapped voltage  $V$ , will cause all subsequent charging pulses to have an energy boost proportional to  $V^2$ . This causes the charge time of subsequent pulses to decrease and the circulating current  $i_2$  in the charging choke to increase. This process continues until a steady-state condition is reached.

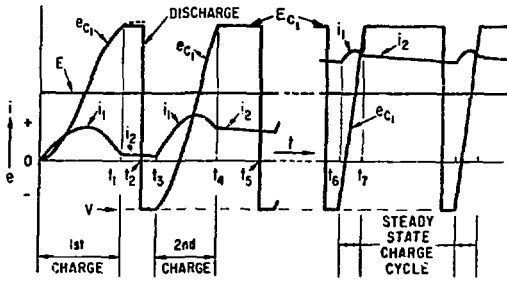


Fig. 11. Currents and voltages of the charging circuit of Figure 9.

For the circuit of Fig. 9, the charging current  $i_1$  and voltage  $e_{C_1}$  can be written

$$i_1 = I_0 e^{-\alpha t} \cos \omega t + \frac{E+V-I_0 R_1/2}{\omega L_1} e^{-\alpha t} \sin \omega t \quad (1')$$

and

$$e_{C_1} = I_0 L_1 \left[ \alpha - \epsilon^{-\alpha t} (\alpha \cos \omega t - \omega \sin \omega t) \right] + (E+V-I_0 R_1/2) \left[ 1 - \epsilon^{-\alpha t} \left( \frac{\alpha}{\omega} \sin \omega t + \cos \omega t \right) \right], \quad (2')$$

where

$V =$  negative voltage on  $C_1$  at  $t_0$ .

As illustrated in Fig. 12, with a power-supply voltage of  $E = 410$  V, the time for the initial charge to reach 800 V from zero is 23.1 ms, ending with a circulating current of 15.2 A. All subsequent pulses begin with  $V = -280$  V on capacitor  $C_1$ . The second charge has a duration of only  $\sim 17$  ms and ends with a circulating current of  $\sim 110$  A. Finally, a stable condition is reached with a charge time of  $\sim 6$  ms and a circulating current of  $\sim 270$  A. This high circulating current causes  $i^2 R$  losses of about 6.5 kW in the charging choke  $L_1$ .

Figure 13 is an oscilloscope picture of successive traces of capacitor voltage  $e_{C_1}$ . In this example, the time for the very first charge, starting from zero voltage, is 18 ms. It takes about six more charge cycles of ever-decreasing duration to reach a steady-state charge time of about 5 ms.

The operating conditions illustrated by Figs. 11-13 result in high losses in the charging-choke coil and therefore compare poorly with the ones shown in Fig. 5, for the circuit of Fig. 3. However, they can easily be corrected by operating the more efficient circuit of Fig. 9 from a lower supply voltage. Tapping the rectifier transformer back to a dc output voltage of  $E = 271$  V provides a steady-state capacitor voltage of 800 V with a charge pulse of 19 ms duration and a circulating current of  $i_2 = 41.2$  A, as shown in Fig. 14. Recovering the negative charge on capacitor  $C_1$  has reduced the power drawn from the line.

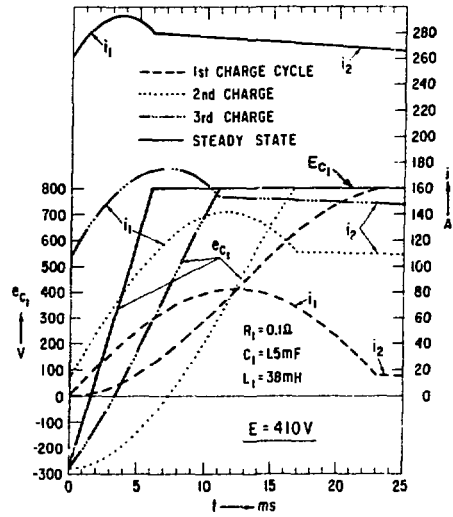


Fig. 12. Currents and voltages of the charging circuit of Figure 9 for  $E = 410$  V and  $E_{C_1} = 800$  V.

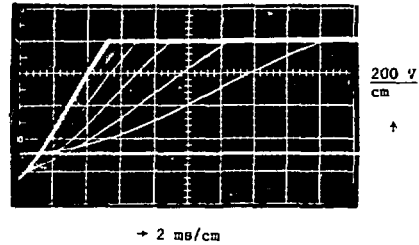


Fig. 13. Oscilloscope picture of capacitor voltage  $e_{C_1}$  during initial charging pulses.

**Startup of Charging-Choke Circuit.** In the circuit of Fig. 3, the peak voltage on capacitor  $C_1$  is always less than twice the supply voltage; that is,  $E_{C_1} < 2E$ . To start operation, the reference voltage is set for the desired operating voltage  $e_r = kE_{C_1}$  and the circuit will then perform as shown in Figs. 4 and 5. To operate the charging-choke circuit of Fig. 9 economically, the desired capacitor voltage must be larger than twice the supply voltage, that is  $E_{C_1} > 2E$ , as illustrated by the steady-state condition shown in Fig. 14. With this circuit, steady-state charging conditions can be reached in two different ways.

- a. The reference voltage  $e_r$  is set for the desired operating voltage  $e_r = kE_{C_1}$ . Since  $E_{C_1} > 2E$ , the first charging pulse will not reach  $E_{C_1}$ . As a consequence, thyristor  $S_2$  will not be turned on and the circuit operates during the first charge like an ordinary charging-choke circuit. For

example, with  $E = 271$  V and  $E_{C1} = 800$  V, capacitor  $C_1$  will be initially charged to  $e_{C1} \leq 542$  V. When the capacitor discharges, this voltage will drive a peak current of only 2 kA through the magnets. During the first discharge, a voltage of  $V = -190$  V is trapped on  $C_1$ . This voltage will aid in the second cycle to charge  $C_1$  to a higher voltage. In this way, the circuit reaches steady state after a few pulses.

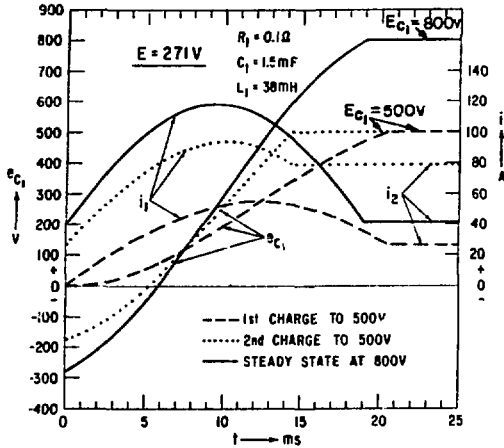


Fig. 14. Currents and voltages of the charging circuit of Figure 9 for  $E = 271$  V and  $E_{C1} = 500$  and  $800$  V.

- b. Another, perhaps less convenient, way of startup is as follows. The reference voltage is initially set for  $e_r/k < 2E$ . After the first pulse, energy will be stored in both  $C_1$  and  $L_1$ . The reference voltage can now be increased to the desired operating conditions. For example, with  $E = 271$  V and  $E_{C1} = 800$  V, one could initially set  $e_r/k = 500$  V. As shown in Fig. 14, after the first pulse of 20.5 ms duration, we have a circulating current of  $i_2 = 26$  A in  $L_1$ , and a voltage of  $V = -175$  V on  $C_1$ . These energies shorten the second pulse to 14.5 ms and leave  $V = -175$  V and  $i_2 = 79$  A stored. The reference voltage can now be increased to the desired value of  $e_r/k = E_{C1} = 800$  V. Stable operation will be obtained within a few pulses with a charge time of 19 ms and  $i_2 = 41.2$  A.

**Discharge Circuit with Energy Recovery.**

When the magnets are to be pulsed for the first time, the only component of the discharge circuit of Fig. 9 with stored energy is capacitor  $C_1$ . Therefore, the sequence of the operation is as follows:

1. In preparation for continuous operation, thyristor  $S_4$  is turned on at  $t_0$  as shown in Fig. 15. Thyristor  $S_4$  will stay on until capacitor  $C_2$  is charged from  $C_1$  through  $D_2$ ,  $L_3$ , and the injection bump magnets to a voltage  $e_{C2} \leq 2 E_{C1}$  at time  $t_1$ .

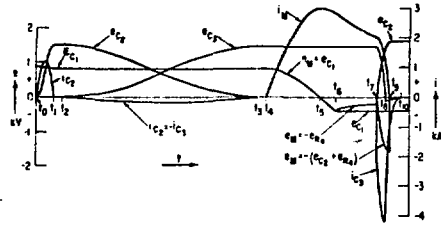


Fig. 15. Currents and voltages during first operation of the circuit of Figure 9.

2. At time  $t_2$ , thyristor  $S_5$  is turned on. With  $C_2 = C_3 = C$ , the total energy stored in  $C_2$  at time  $t_2$  is transferred to  $C_3$  at time  $t_3$ , except for losses, and  $S_5$  turns off. The inductance  $L_2$  never stores more than half the total energy during this transfer. The transfer current is

$$i_{C3} = -i_{C2} = \frac{E_{C2}}{\omega_3 L} e^{-\alpha_3 t} \sin \omega_4 t \quad (17)$$

and the voltage on  $C_3$  will be

$$e_{C3} = \frac{E_{C2}}{2} \left[ 1 - e^{-\alpha_3 t} \left( \frac{\alpha_3}{\omega_4} \sin \omega_4 t + \cos \omega_4 t \right) \right], \quad (18)$$

where

$$\alpha_3 = R_{L2} / 2L_2,$$

$$\omega_4 = \left( \frac{2}{L_2 C} - \alpha_3^2 \right)^{1/2},$$

$$E_{C2} = \text{voltage on } C_2 \text{ at } t_2.$$

and

$$R_{L2} = \text{resistance of the } C_2, L_2, L_3, C_3, \text{ and } S_5 \text{ circuit.}$$

3. The first magnet pulse is initiated at time  $t_4$  by turning on  $S_3$ . As described previously, the current will rise, pass its peak at time  $t_5$ , and transfer into the crowbar. A negative voltage is trapped on  $C_1$  at time  $t_6$  by diode  $D_2$  after the current has been transferred into the crowbar.
4. Injection is terminated at  $t_7$  when  $S_6$  and  $S_4$  are turned on. This provides discharge paths for  $C_3$  through  $L_4$  via  $S_6$  and through  $C_2$  via  $S_6, S_3, S_4,$  and  $L_3$ . Saturable inductor  $L_3$  keeps  $di/dt$  within the ratings of  $S_6$  and  $S_4$  during the first few microseconds of the  $C_3$  discharge. After  $\leq 25$   $\mu$ s,  $S_3$  has turned off. Thyristors  $S_6$  will stay on until the current in  $L_4$  has decayed to zero.

When  $S_3$  turns off, the magnet discharges into  $C_2$ . The current and voltage follow the equations,

$$i_M = i_{C2} = i_M e^{-\alpha_4 t} \left( \cos \omega_5 t - \frac{\alpha_4}{\omega_5} \sin \omega_5 t \right), \quad (19)$$



$$e_{C_2} = L_M i_M t_7 \left\{ \left[ \alpha_4 - e^{-\alpha_4 t} (\alpha_4 \cos \omega_5 t - \omega_5 \sin \omega_5 t) \right] - \alpha_4 \left[ 1 - e^{-\alpha_4 t} (\cos \omega_5 t + \frac{\alpha_4}{\omega_5} \sin \omega_5 t) \right] \right\}, \quad (20)$$

at time  $t_9$  with  $\omega t \approx \pi/2$  we have

$$e_{C_2} \approx \omega_5 L_M i_M t_7 e^{-\frac{\pi \alpha_4}{2 \omega_5}}, \quad (20')$$

where

$$\alpha_4 = (R_M + R_4) / 2L_M,$$

and

$$\omega_5 = \left( \frac{1}{L_M C_2} - \alpha_4^2 \right)^{1/2}.$$

The value of  $C_2$  has been chosen to resonate with the 60  $\mu\text{H}$  magnet at 2 kHz in order to bring the current to zero in 125  $\mu\text{s}$ . Diode  $D_3$  switches water-cooled resistor  $R_5$  in the turnoff circuit at time  $t_8$  when the current in  $L_4$  has passed its peak. Between times  $t_8$  and  $t_{10}$ , the energy in  $L_4$  dissipates mostly in  $R_5$  and very little in the high-Q inductor.

This completes the first discharge cycle with capacitor  $C_1$  having a negative charge and  $C_2$  having a positive charge. The circuit is now ready to be charged from the dc power supply in preparation for the next magnet pulse.

Important features of the circuit as compared to the circuit of Fig. 3 are:

- The magnet voltage at turnoff is  $\leq 1.5$  kV.
- The coil windings of the magnets and chokes must only be rated for 1.5 kV.
- All thyristor and diode assemblies must only be rated for 1.5 kV.
- Capacitors  $C_2$  and  $C_3$  are rated for only 1.5 kV.
- The turnoff circuit carries a peak current of only 5.2 kA.
- The energy trapped in  $C_1$  during discharge is used during the charge cycle. The energy recovered in  $C_2$  from the magnet is used to charge  $C_3$  and to terminate the next current pulse before it is dissipated in  $R_5$ .
- No separate turnoff power supply for charging  $C_3$  is required.

Note that after  $S_3$  has been turned off, the magnet voltage increases gradually and is small as compared to the 3.8 kV step change in the circuit of Fig. 3. This helps considerably to keep  $S_3$  turned off. For example, operating with  $R_4 = 50 \text{ m}\Omega$ , we would have at the end of injection a magnet current  $i_M = 2 \text{ kA}$  and a voltage  $e_M \approx e_{R_4} = 100 \text{ V}$ . After  $\leq 25 \mu\text{s}$  required to turn off thyristor  $S_3$ , the potential on  $C_2$  is, from Fig. 10, only about  $e_{C_2} \approx 1500 \text{ V} \sin 18^\circ = 460 \text{ V}$ . In order to have at least that much potential across  $L_4$ , the initial voltage on  $C_3$  must be, from Figure 8,

$e_{C_3} > 460 \text{ V} \cos 54^\circ = 273 \text{ V}$ . For a magnet current of 2 kA, the circuit provides 1.3 kV on  $C_3$ .

The corresponding values, at the end of injection, when operating with  $R_4 = 150 \text{ m}\Omega$  are:

$$i_M = 1 \text{ kA}, \quad e_M \approx e_{R_4} = 150 \text{ V},$$

$$e_{C_3} \approx e_{C_2} \approx \omega_5 L_M i_M e^{-\frac{\pi \alpha_4}{2 \omega_5}} = 674 \text{ V},$$

at turnoff,  $e_{C_2} \approx 674 \text{ V} \sin 18^\circ = 208 \text{ V}$ ,

and at turnoff,  $e_{C_3} \approx 674 \text{ V} \cos 54^\circ = 396 \text{ V}$ .

The above examples illustrate how the circuit changes the turnoff energy accumulated on  $C_2$  automatically to match different values of magnet current. The current magnitude at the end of injection is determined by the injection time constant selected as shown by Eq. (14).

An oscilloscope picture of a typical magnet current pulse is shown in Fig. 16. At the end of the injection time, it can be noticed on the trace that the current decays for a very short time faster than described by Eq. (19). The reason for this is that, during the turnoff time of  $S_3$ , the magnet circuit is connected to  $C_3$ . This forces a rate of change of the magnet current

$$\frac{di}{dt} \Big|_{t_3} = \frac{e_{C_3} + e_{R_M} + e_{R_4}}{L_M} \quad (21)$$

during the turnoff time.

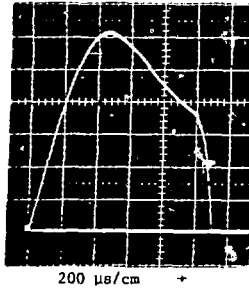


Fig. 16. Oscilloscope picture of typical magnet current generated by the circuit of Fig. 9.

The sequence of operation for subsequent magnet pulses is as described for the first pulse, with one exception. With capacitor  $C_2$  having a positive charge at the end of every magnet pulse, we no longer need to charge  $C_2$  from capacitor  $C_1$ . Time-delay inductor  $L_3$  is reset when the charge on  $C_2$  is transferred to  $C_3$ .

#### Circuit Components

The circuit of Fig. 9 was built from parts available commercially or fabricated in our shop. A few details of special components are given below.

#### Beam Bump Magnets.

The magnets are of the picture-frame type and have cores assembled from 12-mil-thick silicon steel laminations. The magnet coils are wound with copper bus bars having cross sections of  $1/8 \times 1 \text{ in.}$  Most of the

external connections between the power supply and the magnets are made with flat-strip transmission lines; the rest are made with cables. On account of eddy-current losses, mainly in the magnet windings and magnet core laminations, the value of resistance  $R_M$  is larger than the copper resistance. In addition, the value of  $R_M$  changes during the pulse as  $di_M/dt$  varies. The effective circuit resistance is  $\sim 62 \text{ m}\Omega$  during the rise time of the current and  $\sim 16 \text{ m}\Omega$  when the magnets are crowbarred.

#### Thyristors and Diodes.

For clarity, the solid-state components of the circuit of Fig. 9 are shown as single units. In reality, this is only true for thyristors  $S_1$  and  $S_2$ . All other components are made up by connecting two or more units in series. Voltage sharing between these units during steady-state and during transient conditions is achieved in the customary way with resistors and capacitors. The only thyristor assembly with stringent turnoff requirements is  $S_3$ . Here we use three matched thyristors in series, each having a reverse recovery charge of  $36 \pm 1 \text{ }\mu\text{C}$ .

#### Turnoff Inductor $L_4$ .

Inductor  $L_4$  carries both the load current and the turnoff current pulse. The sum of these currents has a maximum value of 741 A rms with operating conditions as shown in Fig. 10. The turnoff circuit resonates at 5.9 kHz. At this frequency, the skin depth of copper is  $\delta = 0.086 \text{ cm}$ . For the inductor to have low losses, it was wound with 80 insulated wires of #14 AWG in parallel. This wire has a diameter  $d = 2 \delta$ . The inductor has a C-core made from 12-mil laminations of grain oriented silicon steel with a cross section of  $65 \text{ cm}^2$ , an air gap of 4.2 cm and six turns.

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