COMMUNICATION

A Recent History of the Production of Doctorates in Mathematics Education

Barbara Reys and Robert Reys

Institutions in the United States have been producing PhDs in mathematics education for more than a century. Teachers College at Columbia University and the University of Chicago produced the first graduates in mathematics education in 1906 and 1912, respectively [1]. In those institutions, doctoral students in mathematics education typically took courses along with doctoral students in mathematics. However, the dissertation research took a different direction as doctorates in mathematics education focused on issues related to mathematics learning, teaching, or curriculum. Over the past fifty years the nature of doctoral programs in mathematics education has taken many different paths [2], [3], [4], [5]. While some doctoral programs remain in mathematics departments, today the majority of doctoral programs in mathematics education are in colleges/schools of education. Some doctoral programs in mathematics education continue to require a substantial amount of mathematics, while others require very little graduate-level mathematics.

This article highlights the production of doctorates in mathematics education for the past fifty years.

Findings

Figure 1 shows the annual total number of doctoral graduates in mathematics education from the first Survey of Earned Doctorates (SED) in mathematics education in 1962 to the most recent data available from 2014 [6]. Figure 1 shows annual variability, with several valleys and peaks, ranging from a low of 14 doctoral graduates in mathematics education in 1962 to highs of 153 graduates (1972) and 161 graduates (2009). The steady increase in doctoral graduates in mathematics education during the latter 1960s and early 1970s coincided with the "modern mathematics era" and can likely be attributed to the number

Barbara Reys is Curators' Professor Emerita of Mathematics Education, University of Missouri-Columbia. Her email address is reysb@missouri.edu.

Robert Reys is Curators' Professor Emeritus of Mathematics Education, University of Missouri-Columbia. His email address is reysr@missouri.edu.

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Total doctorate recipients

Figure 1. Annual production of doctorates in mathematics education from 1962 to 2014 [6].

of Summer Institutes for K–12 mathematics teachers supported by the National Science Foundation at institutions of higher education throughout the United States during this period [7]. Many middle and secondary mathematics teachers took advantage of these opportunities to pursue a doctorate in mathematics education.

About twenty years later another steady increase occurred in the production of doctorates. This increase might be attributed to a surge in recruitment efforts due to an announced shortage of doctorates in mathematics education in institutions of higher education [8], [9]. In

2000 the National Science Foundation began funding several Centers for Learning and Teaching that were designed, among other things, to increase the production of doctorates in mathematics education. This likely contributed to the steady increase of doctoral graduates in mathematics education during the twenty-first century.

Table 1 provides additional detail regarding the data shown in Figure 1. An examination Since 1970 there has been a steady increase in the percentage of females earning a doctorate in mathematics education

Years	1962-64	1965-69	1970-74	1975-79	1980-84	1985-89	1990-94	1995-99	2000-04	2005-09	2010-14
Range of # of graduates during the 5-year period	14-36	56-111	104-153	57-108	50-74	56-74	62-74	92-115	80-91	89-161	114-144
Total # of graduates	81	413	651	444	312	336	343	501	429	607	681
Total # of females & percent	17 21.0%	64 15.5%	118 18.1%	149 33.6%	145 46.5%	176 52.8%	192 56.0%	313 64.5%	253 59.0%	381 62.8%	441 64.8%
Total # of minorities & percent	N/A	N/A	11 4.6%	50 11.3%	22 7.1%	33 9.8%	25 7.3%	50 10.0%	75 17.5%	87 14.3%	117 17.2%
# of different institutions graduating at least one	37	63	77	69	63	75	77	105	108	116	129

Table 1. Summary of total number of doctorates in mathematics education and the number of different institutions awarding the degrees [6].

by 5-year increments reveals several patterns, the most striking of which is the dramatic change in the gender of recipients of doctorates in mathematics education. Males represented the majority of graduates during the 1960s and 1970s. However, since 1970 there has been a steady increase in the percentage of females earning a doctorate in mathematics education. Beginning in 1987 over one half of the recipients of doctorates in mathematics education were female, and that pattern has continued for more than twenty-five years.

Table 1 also provides information on the number of minorities receiving doctorates in mathematics education. The SED identifies minorities as Asian, Black, Native American, or Hispanic but did not start collecting minority data until 1973. The 1975-79 period provides the first full 5-year increment reflecting ethnic status and shows that during the 1970s and 1980s, about 10 percent of the doctoral recipients were classified "minority." This percentage has increased significantly since 2000. Over this period African Americans represent nearly two-thirds of the minority recipients, Hispanics 20 percent, Asians 15 percent, and Native Americans 2 percent.

The increasing number of different institutions awarding doctorates is another pattern shown in Table 1. During the initial time period (1962–64) there were a total of 81 doctoral graduates, and they completed their degrees from thirty-seven different institutions. The number of different institutions awarding degrees has steadily increased over the years, with over one hundred different institutions graduating doctorates in mathematics education during each of the last four 5-year increments.

Table 2 identifies the ten institutions producing the most doctoral graduates for each of the last five decades. An examination of Table 2 shows that Teachers College, Columbia University, has been the highest producer of doctoral graduates in mathematics education, ranking number one in five of the six time periods. Ohio State University has also been among the top ten each period.

Further examination of Table 2 shows that some institutions, such as Illinois State University, have developed into large producers of doctoral graduates in mathematics education during the last two decades, whereas some high producers in earlier decades, such as Wayne State University, are no longer present.

Of further interest is that over one half of the largest producers average less than two doctoral graduates a year, and about one fourth of them average less than one graduate a year over a decade. The SED data reveal that one hundred eighty different institutions graduated at least one doctorate in mathematics education from 2000 to 2014. Further examination showed that about forty-one of these institutions graduated a total of one doctorate in mathematics education, and over one half (55 percent) of the institutions graduated a total of five or fewer doctorates during this 15-year period.

Some Takeaway Points for Doctoral Graduates

- The number of doctoral graduates in mathematics education has been increasing each decade, with dramatic increases in the last ten years.
- The number of doctoral graduates in mathematics education varies annually but has averaged about 120 during each of the last ten years.
- The majority—over 60 percent—of doctoral graduates in mathematics education are female.
- The percent of minority doctoral graduates in mathematics education has ranged from 5 to 17 percent across the five decades, with African Americans comprising about two-thirds of the minority graduates.

Some Takeaway Points for Institutions

- The number of different institutions awarding doctorates in mathematics education has been increasing each decade.
- Two institutions (Ohio State University and Teachers College, Columbia University) have consistently ranked among the top ten producers of doctorates in mathematics education in each decade.
- During the last fifteen years (2000–2014) there were one hundred eighty institutions that graduated at least one doctorate in mathematics education. Nearly 40 percent of the institutions graduated just one or two doctorates in mathematics education.

Closing Comments

This brief history of the production of doctorates in mathematics education documents the changing nature of the doctoral graduates as well as the increasing number of institutions that produce them. Unfortunately, these data do not provide insight into the academic content of the doctoral programs or the nature of the additional

Table 2. Top 10 (and ties) of institutions producing doctoral graduates in mathematics education for five and one half decades (6). For a listing of the 40 largest producers of doctoral graduates in mathematics education from 1962 to 2004, See Metry 97 institutions producing soctoral graduates in mathematics education for five and one-half decades (6)

Rank	1962-1969	1970-1979	1980-1989	1990-1999	2000-2009	2010-2014
1	Oklahoma State University(43)	Teachers College- Columbia University(64)	Teachers College Columbia University(52)	Teachers College- Columbia University(70)	Teachers College, Columbia University(74)	Teachers College- Columbia University(64)
2	Teachers College- Columbia University(35)	Ohio State University(55)	New York University(33)	University of Georgia(56)	University of Georgia(59)	University of Georgia(43)
3	Ohio State	Florida State	University of	University of	Illinois State	Rutgers
	University(34)	University(53)	Georgia(33)	Texas(49)	University(41)	University(21)
4	University of	New York	University of	Ohio State	University of	Georgia State
	Michigan(33)	University(51)	Texas(33)	University(38)	Texas(32)	University(17)
5	University of Illinois(25)	University of Northern Colorado(50)	Georgia State University(25)	Georgia State University(33)	Florida State University(31)	North Carolina State University(17)
6	New York	Indiana	Ohio State	Florida State	Rutgers	University of
	University(23)	University(49)	University(25)	University(26)	University(31)	Missouri(17)
7	University of	University of	Temple	Rutgers	North Carolina State	Illinois State
	Wisconsin(21)	Texas(49)	University(21)	University(21)	University(25)	University(15)
8	Florida State	University of	University of	American	Oregon State	Michigan State
	University(19)	Georgia(46)	Maryland(21)	University(19)	University(23)	University(15)
9	University of	University of	Florida State	University of	University of	University of
	Virginia(14)	Illinois(41)	University(19)	Wisconsin(18)	Maryland(22)	Michigan(14)
10	University of Northern Colorado(14)	University of Maryland(38)	Boston University(18)	University of Oklahoma(18)	Ohio State University(21)	Ohio State University(13)

experiences that ultimately shape the preparation of doctoral graduates in mathematics education.

While it is safe to say that every PhD in mathematics has successfully completed graduate-level courses in advanced calculus and analysis, it is not possible to identify any specific course(s) with certainty that all doctoral graduates in mathematics education have completed. Additional research into the overall nature of doctoral programs in mathematics education across a wide variety of institutions of higher education is sorely needed.

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ABOUT THE AUTHORS

Barbara likes to hike and watch after her new grandchild.

Robert enjoys playing tennis and officiates collegiate-level tennis matches.



Barbara and Robert Reys

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