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A Short ID-based Proxy Signature Scheme

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Abstract. The notion of identity-based proxy signature with message recovery feature has been proposed to shorten identity-based proxy signatures and improve their communication overhead since signed messages are not transmitted with these kinds of signatures. There are a few schemes for this notion: Singh and Verma’s scheme and Yoon et al.’s scheme. Unfortunately, Tian et al. by presenting two forgery attacks show that Singh and Verma’s scheme is not secure, and also Yoon et al.’s scheme does not support provable security. The contributions of this paper are twofold. First, we review Yoon et al.’s scheme and discuss why it does not have message recovery property, and consequently it is not short. Second, we propose a short identity-based proxy signature scheme with the help of message recovery property, and show that it is secure under CDH assumption in the random oracle model. Furthermore, our scheme is more efficient than (as efficient as) previous identity-based proxy signatures.

Keywords: identity-based signature, identity-based signature with message recovery, identity-based proxy signature, CDH assumption, random oracle model.

1 Introduction

The possibility to implement digital signatures is one of the most important achievements of modern cryptography. Digital signatures are widely deployed around the world and have the backing of significant international legislation to support their use in electronic business. Businesses need to be flexible about the way that they employ signatures and so there is a need for digital signature algorithms to support typical business practices. One such flexible type of signature is the *proxy signature* which permits the common business practice of delegating signing authority in a flexible manner. We are interested in exploring proxy signatures in the identity-based setting.

IDENTITY-BASED CRYPTOGRAPHY. Public-key cryptography has many different applications, but in its basic format requires extensive public-key infrastructure for practical use [1]. In order to provide more flexible management of public keys the notion of identity-based cryptography was introduced by Shamir [2]. The main feature of identity-based cryptosystems is to remove the requirement of certification of the public keys. The public key of each entity is obtained from its public identity, such as the IP address or email address, which uniquely identifies it. Since Shamir introduced this notion [2], different identity-based signature schemes [3–5] are proposed. Identity-based signatures with message recovery feature are proposed to minimize the size of signed messages and consequently size of these kinds of signatures. Therefore, these primitives are helpful when an organization intends to reduce the required bandwidth in transmission, or when it is necessary that small messages should be signed. In 2005, Zhang et al. presented the first identity-based signature with message recovery feature [6] for shortening signatures’ length, subsequently, Tso et al. [7] presented a revision to Zhang et al.’s scheme, and proposed a construction more efficient than Zhang et al.’s scheme in 2007.

PROXY SIGNATURES. Proxy signatures for the first time were introduced by Mambo et al. [8] in 1996. In a proxy signature scheme, an original signer, Alice, can delegate her signing right for signing messages to another signer, Bob, called the proxy signer. Since the notion of proxy signatures has been introduced, several variants of proxy signatures have been proposed. These include proxy signature schemes [9–17], identity-based proxy signature schemes based on the bilinear pairings [18–25], designated verifier signature

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schemes [26–28], (identity-based) multi-proxy signatures [23, 29–33], identity-based proxy multi-signatures [30, 34–37], (identity-based) multi-proxy multi-signature schemes [30, 38–43], identity-based proxy signatures with message recovery [44, 45], a certificate-less proxy signature with message recovery and its security analysis [46, 47] and analysis of proxy signatures [48–50]. In this study, we focus on identity-based proxy signature schemes with message recovery property to shorten identity-based proxy signatures.

In identity-based proxy signature schemes with message recovery, a signed message is not required to be transmitted with the signature since the signed message has been inserted to the signature and can be retrieved from the signature by anyone. The main feature of these schemes is to shorten identity-based proxy signatures. This primitive is useful where bandwidth is one of the crucial concern [51, 52]. If original messages are transmitted with these signatures, it defeats the main purpose of an identity-based proxy signature with message recovery to save bandwidth. In order to save the bandwidth and provide more flexible management of public keys, two identity-based proxy signatures with message recovery [44, 45] have been proposed. The first one was proposed by Singh and Verma [44] in 2012. In 2013, Tian et al. [48] show that Singh and Verma’s scheme is insecure by presenting two forgery attacks. Next, Yoon et al. proposed a secure identity-based proxy signature scheme with message recovery [45] to solve the problem of Singh and Verma’s scheme. Unfortunately, Yoon et al.’s scheme [45] does not support provable security, and also we show that it is not actually a scheme with message recovery property. Then, we present a short identity-based proxy signature scheme with employing message recovery property, which is based on the identity-based signature scheme [4] and the technique employed in [7] to achieve message recovery property, and show that it is secure under CDH assumption in the random oracle model.

1.1 Organization of the paper

The rest of this paper is organized as follows. Section 2 presents bilinear pairings and the CDH complexity assumption employed as the signature foundation, the outline of identity-based proxy signature schemes with message recovery and its security security model. Review and security drawback of Yoon et al.’s identity-based proxy signature with message recovery [45] are given in Section 3. Our proposed scheme and its formal security proof are presented in Section 4. Section 5 and 6 present the comparison and conclusion, respectively.

2 Background

In this section, we review several fundamental backgrounds employed in this research, including bilinear pairings and Computational Diffie-Hellman complexity assumption.

2.1 Bilinear pairings

Let $(\mathbb{G}, +)$ and (\mathbb{G}_T, \cdot) be two cyclic groups of the same prime order q ; furthermore, let P be a generator of \mathbb{G} . The map $e : \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}_T$ is said to be an admissible bilinear pairing if the following conditions hold true.

1. e is bilinear which means that $e(cP, dP) = e(P, P)^{cd}$ for all c and $d \in \mathbb{Z}_q^*$
2. e is non-degenerate which means that $e(P, P) \neq 1_{\mathbb{G}_T}$
3. e is efficiently computable.

2.2 Complexity assumptions

Definition 1. Computational Diffie-Hellman (CDH) problem. Given $(P, cP, dP \in \mathbb{G})$ for some unknown c and $d \in \mathbb{Z}_q^*$, output $cdP \in \mathbb{G}$.

Definition 2. The advantage of B , which is a polynomial bounded algorithm with a security parameter l , in solving the CDH problem in group \mathbb{G} is

$$Adv_B^{CDH}(l) = \Pr [cdP \leftarrow B(P, cP, dP) \mid c, d \in \mathbb{Z}_q^*]. \quad (1)$$

The probability is taken over the choice of c, d and B ’s coin tosses. An algorithm $B(t, \epsilon)$ -breaks CDH problem on \mathbb{G} if it runs in time at most t , and $Adv_B^{CDH}(l)$ is at least ϵ . The CDH assumption states that the CDH problem on \mathbb{G} is (t, ϵ) -hard if there is no algorithm $B(t, \epsilon)$ -breaks the CDH problem.

2.3 Notations

Throughout the paper, we will use the following notations.

- $y||x$: a concatenation of two strings y and x such that from $y||x$, y and x are effectively recoverable.
- \oplus : X-OR operation.
- $[y]_{10}$: the decimal representation of $y \in \{0, 1\}^*$.
- $[y]_2$: the binary representation of y .
- $l_2|y|$: the first left l_2 bits of y .
- $|y|_{l_1}$: the first right l_1 bits of y .
- $|y|$: the number of bits of y .
- $s \stackrel{\$}{\leftarrow} S$: the operation of assigning a uniformly random element of S to s .

2.4 Outline of identity-based proxy signature schemes with message recovery

An original signer with identity ID_o and a proxy signer with identity ID_p and a verifier are participants of an identity-based proxy signature with message recovery. An identity-based proxy signature scheme with message recovery consists of Setup, KeyExtract, DelGen, DeleVer, PSign and PVer/MR algorithms as follows [44].

- Setup: Given the system security parameter l , it outputs system's parameters $Para$ and the system's master key (msk, mpk) , i.e. $(Para, (msk, mpk)) \leftarrow Setup(l)$.
- KeyExtract: Given the system's parameter $Para$, master public key mpk , master secret key msk , and an identity ID_u , it outputs the corresponding secret key x_u , i.e. $x_u \leftarrow KeyExtract(Para, mpk, msk, ID_u)$.
- DelGen: Given the system's parameter $Para$, the master public key mpk , a warrant w , proxy signer's identity ID_p , the original signer's secret key x_o , it outputs the delegation σ_o after a number of interactions to delegate original signer's signing right on the warrant w to the identity ID_p , i.e. $\sigma_o \leftarrow DelGen(Para, mpk, w, ID_p, x_o)$.
- DelVer: Given the system's parameter $Para$, the master public key mpk , the original signer's identity ID_o , the warrant w and proxy signer's identity ID_p and the delegation σ_o , it outputs 1 if σ_o is a valid delegation of the warrant w for identity ID_p under the identity ID_o and outputs 0 otherwise, i.e. $\{0, 1\} \leftarrow DelVer(Para, mpk, ID_o, w, ID_p, \sigma_o)$.
- PSign: Given the system's parameter $Para$, the master public key mpk , original signer's identity ID_o , the proxy signer's identity ID_p , the warrant w , the delegation σ_o , secret key x_p of the proxy signer with identity ID_p and the message m to be signed, it outputs the identity-based proxy signature θ , i.e. $\theta \leftarrow PSign(Para, mpk, ID_o, ID_p, w, \sigma_o, x_p, m)$.
- PVer/MR: Given the system's parameter $Para$, the master public key mpk , the original signer's identity ID_o , the proxy signer's identity ID_p , the warrant w and the proxy signature θ , it first recovers the message m , and outputs 1 if θ is a valid identity-based proxy signature of the message m and outputs 0 otherwise, i.e. $(m, \{0, 1\}) \leftarrow PVer/MR(Para, mpk, ID_o, ID_p, w, \theta)$.

2.5 Security model of identity-based proxy signatures with message recovery

In a warrant-based identity-based proxy signature scheme with message recovery, the delegation is the original signer's standard signature on a proxy signer's identity ID_p and a warrant w which contains information regarding the period of validity and the restriction on the class of messages for which the warrant is valid. Therefore, the properties of strong identifiability, strong undeniability, verifiability, and prevention of misuse are satisfied naturally. Therefore, the signature scheme should be secure against existential forgery under an adaptive-chosen-message, an adaptive-chosen warrant and chosen identity attack. The adversary A can choose

the identities on which it wants to forge a proxy signature and can request the secret keys corresponding to them (corrupted users) except for the honest signer, and also A can make delegation and proxy signature queries on arbitrary warrants and messages under arbitrary identities including honest identity. To achieve existential unforgeability, three types of potential adversaries are considered. Adversaries of type I which only have identities of an original and a proxy signer, adversaries of type II which have the secret key of the proxy signer in addition to capabilities of adversaries of type I and adversaries of type III which have the secret key of the original signer in addition to identities of the original signer and the proxy signer.

Since an identity-based proxy signature scheme secure against type II (or type III) adversaries is also secure against type I adversaries we will henceforth only consider type II and type III adversaries. To have a formal definition for strong unforgeability, the adversary A and the challenger C should interact through the following game[44].

1. Setup: Algorithm C runs the Setup algorithm with a security parameter l to obtain system's parameter $para$ and the master key (mpk, msk) , then it sends $(mpk, para)$ to A .
2. The adversary A issues a polynomially bounded number of questions to the following oracles adaptively.
 - KeyExtract: The adversary A can ask for the secret key corresponding to ID_u , then C returns the private key x_u with running the KeyExtract algorithm.
 - DelGen: Adversary A can request the delegation algorithm under the designator's identity ID_u on the pair (w, ID_p) of its choice. Then, C returns $\sigma_u \leftarrow DelGen(Para, mpk, w, ID_p, x_u)$ to A .
 - PSign: Adversary A can request the proxy signature of m under proxy signer's identity ID_p , where m is in the warrant w . In addition, A provides a valid delegation σ_o which indicates that an original signer with identity ID_o delegates its signing right to the proxy signer with identity ID_p on the warrant w . In response, C firstly runs the KeyExtract algorithm to obtain the secret key x_p corresponding to the identity of the proxy signer with identity ID_p . Next, C runs PSign protocol to generate $\theta \leftarrow PSign(Para, mpk, ID_o, ID_p, w, \sigma_o, x_p, m)$. Then, C returns θ to the adversary A .
3. Eventually, A returns a valid signature (w^*, θ^*) w.r.t. an original signer's identity ID_o^* and a proxy signer's identity ID_p^* , and wins the game if the following conditions hold.
 1. For adversaries of type II, we have
 - E_0 : Identity of the original signer ID_o^* has not been requested to the KeyExtract oracle.
 - E_1 : The pair (w^*, ID_p^*) has not been requested to the DelGen oracle under the original signer's identity ID_o^* .
 2. For adversaries of type III, we have
 - E_0 : Identity of the proxy signer ID_p^* has not been requested to the KeyExtract oracle.
 - E_1 : The message m^* has not been requested to the PSign oracle under the proxy signer's identity ID_p^* .

The formal definition of existential unforgeability for adversaries of type II (type III) is expressed in Definition 3.

Definition 3. An identity-based proxy signature is $(t, q_H, q_e, q_d, q_s, \epsilon)$ -existentially unforgeable against adaptive chosen message (chosen warrant) attack and chosen identity attack if there is no adversary which runs in time at most t , (makes at most q_H queries to hash functions), makes at most q_e KeyExtract queries, q_d DelGen queries and q_s PSign queries, can win the aforementioned game with probability at least ϵ .

3 An Identity-based proxy signature scheme with message recovery

In this section, first we review Yoon et al.'s identity-based proxy signature scheme [45] with message recovery, then, we show that it does not have message recovery property despite authors' claim.

3.1 Overview of Yoon et al.'s identity-based proxy signature scheme with message recovery

In 2013, Yoon et al. [45] proposed an identity-based proxy signature with message recovery to eliminate security problems [48] of Singh and Verma's identity-based proxy signature with message recovery [44] presented by Tian et al. in 2013. This scheme includes an original signer with identity ID_o and a proxy signer with identity ID_p . Their scheme consists of the following algorithms:

1. Setup: The system parameters are as follows. Let l_1 and $l_2 \in \mathbb{N}$, and let \mathbb{G} be an additive cyclic group of order q and \mathbb{G}_T be a multiplicative cyclic group of the same order q , where q is a prime and $P \in \mathbb{G}$ be a generator of \mathbb{G} . Let $H_0 : \{0, 1\}^* \rightarrow \mathbb{G}$, $H_1 : \mathbb{G}_T \rightarrow \mathbb{Z}_q^*$, $H : \{0, 1\}^* \rightarrow \mathbb{G}$, $F_1 : \{0, 1\}^{l_2} \rightarrow \{0, 1\}^{l_1}$, $F_2 : \{0, 1\}^{l_1} \rightarrow \{0, 1\}^{l_2}$ be random oracles, where $l_1 + l_2 = |q|$. It is assumed that x is a master secret key and $P_{pub} = xP$ is a master public key. Therefore, public parameters are $Para = \{\mathbb{G}, \mathbb{G}_T, H, H_0, H_1, F_1, F_2, e, P, P_{pub}, q, l_1, l_2\}$.
2. KeyExtract: On input a master secret key $msk = x$ and a user's identity ID_u , the key distribution center computes $x_u = xH(ID_u)$, and sends the user's secret key x_u over a secure and authenticated channel to the user with identity ID_u .
3. DelGen: The original signer with identity ID_o chooses $k_o \xleftarrow{\$} \mathbb{Z}_q^*$, computes $K_o = k_oP$, $h_w = H_0(ID_o, w, K_o)$ and $s = k_o h_w + x_o$, and outputs the delegation (w, K_o, s) in order to delegate its signing right on a warrant w to a proxy signer with the identity ID_p .
4. PKGen: If a delegation (w, K_o, s) is valid, the proxy signing key $d_p = s + x_p$ is generated by the proxy signer with identity ID_p .
5. PSign: The proxy signer with identity ID_p can sign a message m in the warrant w as follows. The proxy signer with identity ID_p chooses $k_p \xleftarrow{\$} \mathbb{Z}_q^*$, computes $K_p = k_pP$, $\beta = F_1(m) || F_2(F_1(m)) \oplus m$, $\alpha = [\beta]_{10}$, $h_m = H(ID_p, \alpha, K_p)$ and $U = k_p h_m + d_p$, and returns the proxy signature (w, K_o, K_p, U, α) .
6. PVer: Given identities ID_o and ID_p and a signature (w, K_o, K_p, U, α) , a verifier does as explained below:
 - Checks if ID_p is authorized by the identity ID_o in the warrant w , otherwise, it stops.
 - Accepts the proxy signature if and only if $H_1(e(U, P)e(H(ID_o) + H(ID_p), p_{pub})^{-1}) = H_1(e(h_m, K_p)e(h_w, K_o))$ holds, where $h_w = H_0(ID_o, w, K_o)$ and $h_m = H_0(ID_p, \alpha, K_p)$, and recovers the message by $\beta = [\alpha]_2$ and $m = F_2(l_1|\beta) \oplus |\beta|_{l_2}$.
 - Checks if the message m conforms to the warrant w , otherwise, it stops.

3.2 Why Yoon et al.'s scheme does not have message recovery property

Yoon et al.'s identity-based proxy signature scheme with message recovery [45] not only does not support provable security but also it does not have message recovery property despite its authors' claim. Hence, it is not short. The feature of message recovery in signatures is used to minimize the size of the signatures and the message can be recovered from the signature by everyone. The signature in this scheme is (w, K_o, K_p, U, α) , where the message m is recovered as follows: a verifier computes $\beta = [\alpha]_2$, and then $m = F_2(l_1|\beta) \oplus |\beta|_{l_2}$.

To show that Yoon et al.'s scheme does not have message recovery, we use the fact that there is a direct relation between α and m and everyone can extract the message m from α , and α is transmitted with the signature. Consider a scheme as a modified version of Yoon et al.'s scheme in which we transform α to m because of the aforementioned fact. In this case, the result signature is (w, K_o, K_p, U, m) , and the signature U can be generated on m instead of α . As a consequence, we obtain an ordinary identity-based proxy signature. These two schemes are equivalent in their signature size since α is equivalent to m , and α or equivalently m is transmitted with the signature. Therefore, Yoon et al.'s scheme does not support message recovery property to reduce the signature size.

4 Our identity-based proxy signature scheme with message recovery

In this section, we present an identity-based proxy signature scheme with message recovery based on the identity-based signature scheme [4] and the technique employed in [7] to achieve message recovery property. Then, we prove that it is secure under CDH assumption in the random oracle model.

4.1 Details of our identity-based proxy signature scheme with message recovery

In this section, we present the details of our identity-based proxy signature scheme with message recovery. There are three participants in the system, an original signer with identity ID_o , a proxy signer with identity ID_p and a verifier. Our scheme consists of seven algorithms as follows.

1. **Setup:** The system parameters are as follows. Let l_1 and $l_2 \in \mathbb{N}$, and let \mathbb{G} be an additive cyclic group of order q and \mathbb{G}_T be a multiplicative cyclic group of the same order q , where q is a prime and $P \in \mathbb{G}$ be a generator of \mathbb{G} . Let $H_0 : \{0, 1\}^* \times \mathbb{G}_T \rightarrow \mathbb{Z}_q^*$, $H_1 : \mathbb{G}_T \rightarrow \{0, 1\}^{|q|}$, $H : \{0, 1\}^* \rightarrow \mathbb{G}$, $F_1 : \{0, 1\}^{l_2} \rightarrow \{0, 1\}^{l_1}$, $F_2 : \{0, 1\}^{l_1} \rightarrow \{0, 1\}^{l_2}$ be random oracles, where $l_1 + l_2 = |q|$. It is assumed that $x \in_R \mathbb{Z}_q^*$ is a master secret key and $P_{pub} = xP$ is a master public key. Therefore, public parameters are $Para = \{\mathbb{G}, \mathbb{G}_T, H, H_0, H_1, F_1, F_2, e, P, P_{pub}, q, l_1, l_2\}$.
2. **KeyExtract:** Given $Para$, master secret key $msk = x$ and the user identity ID_u , the key distribution center computes $x_u = xH(ID_u)$, and sends the user's secret key x_u over a secure and authenticated channel to the user with identity ID_u .
3. **DelGen:** Let w be a warrant for that an original signer with identity ID_o who wants to delegate its signing right a proxy signer with identity ID_p , the delegation σ_o is generated as follows: the original signer with identity ID_o selects $k_o \in \mathbb{Z}_q^*$, computes $K_o = e(H(ID_o), P_{pub})^{k_o}$, $h_0 = H_0(w||ID_p, K_o)$ and $U_o = (h_0 + k_o)x_o$, and outputs the delegation (w, K_o, U_o) .
4. **DelVer:** Given original signer's identity ID_o and the delegation (w, K_o, U_o) , a verifier checks if $e(U_o, P) = K_o e(H(ID_o), P_{pub})^{h_0}$ holds, where $h_0 = H_0(w||ID_p, K_o)$.
5. **PSign:** The proxy signer with identity ID_p can sign a message m such that $|m| = l_2$ under the warrant w with having a valid delegation $\sigma_o = (w, K_o, U_o)$. To do so, the proxy signer chooses $k_p \in_R \mathbb{Z}_q^*$, computes $K_p = K_o \cdot e(H(ID_p), P_{pub})^{k_p}$, $h_1 = H_1(K_p)$, $\beta = F_1(m)||F_2(F_1(m)) \oplus m$, $\alpha = [\beta \oplus h_1]_{10}$ and $U = U_o + (\alpha + k_p)x_p$. The proxy signature θ on the message m is (w, U, α, K_o) .
6. **PVer/MR:** Given identities ID_o and ID_p and a signature $\theta = (w, U, \alpha, K_o)$, a verifier does as explained below:
 - Checks if ID_p is authorized by the identity ID_o in the warrant w , otherwise, it stops.
 - Computes $h_1 = H_1(e(U, P)e(H(ID_o), P_{pub})^{-h_0}e(H(ID_p), P_{pub})^{-\alpha})$, $\beta \leftarrow [\alpha]_2 \oplus h_1$, and then recover the message $m = |\beta|_{l_2} \oplus F_2(|\beta|)$, and accepts the signature θ on the message m if and only if $|\beta|_{l_1} = F_1(m)$ holds, where $h_0 = H_0(w||ID_p, K_o)$, otherwise, it stops.
 - Checks if the message m conforms to the warrant w , otherwise, it stops.

4.2 Analysis of the proposed scheme

In this subsection, we verify the correctness and prove existential unforgeability of the new identity-based proxy signature scheme with message recovery in the random oracle model (see [53] for the background). In order to prove unforgeability of the proposed scheme, we need to show that it is unforgeable against adversaries of types II and III (as defined in Section 2.5). Since our security proofs are quite similar for two types of adversaries, we have parametrized these proofs to prevent unnecessary repetitions of arguments. Hence, just for notational settings, we refer to the adversary as $A_{(1-k)II+kIII}$ in which the parameter $k \in \{0, 1\}$ makes the difference between adversaries of types II and III (i.e. notationally we assume that we have an adversary

of type II, A_{II} , when $k = 0$ and an adversary of type III, A_{III} , when $k = 1$). Note that, the proofs for different values of k are independent since different types of adversaries are independent.

To prove the security of our proposed scheme, and by contradiction, assuming an adversary $A_{(1-k)II+kIII}$, we show that there is a solver (algorithm B) that can solve a random instance of the CDH problem with a non-negligible probability. Our main result on the security of the proposed scheme is summarized in Theorem 1, where the parameter k is used to code the result for both adversaries of types II and III. To start let us verify the correctness of the proposed scheme, and we use $e(U_o, P) = K_o e(H(ID_o), P_{pub})^{h_o}$ in what follows.

$$\begin{aligned}
& e(U, P) e(H(ID_o), P_{pub})^{-h_o} e(H(ID_p), P_{pub})^{-\alpha} \\
&= e(U_o + (\alpha + k_p)x_p, P) e(H(ID_o), P_{pub})^{-h_o} e(H(ID_p), P_{pub})^{-\alpha} \\
&= e(U_o, P) e(\alpha x_p, P) e(k_p x_p, P) e(H(ID_o), P_{pub})^{-h_o} e(H(ID_p), P_{pub})^{-\alpha} \\
&= e(U_o, P) e(H(ID_p), P_{pub})^\alpha e(H(ID_p), P_{pub})^{k_p} e(H(ID_o), P_{pub})^{-h_o} e(H(ID_p), P_{pub})^{-\alpha} \\
&= K_o e(H(ID_o), P_{pub})^{h_o} e(H(ID_p), P_{pub})^{k_p} e(H(ID_o), P_{pub})^{-h_o} \\
&= K_o e(H(ID_p), P_{pub})^{k_p} = K_p.
\end{aligned} \tag{2}$$

If θ is a valid signature, $H_1(e(U, P) e(H(ID_o), P_{pub})^{-h_o} e(H(ID_p), P_{pub})^{-\alpha} = K_p) = h_1$, and we have $F_1(m) || F_2(F_1(m)) \oplus m = \beta = [\alpha]_2 \oplus h_1$. Hence, the message is recovered as $m = |\beta|_{l_2} \oplus F_2(l_1 |\beta|)$ and integrity of the message is checked by $F_1(m) = l_1 |m|$.

Also, in what follows we will be needing the following Splitting lemma.

Lemma 1. [54] *Let $S \subset X \times Y$ such that $\Pr[(x, y) \in S] \geq \delta$. For any $\gamma < \delta$, define $\Omega = \{(x, y) \in X \times Y \mid \Pr_{y' \in Y}[(x, y') \in S] \geq \delta - \gamma\}$ and $\bar{\Omega} = (X \times Y) \setminus \Omega$, then the following statements hold:*

- $\Pr[\Omega] \geq \gamma$
- $\forall (x, y) \in \Omega, \Pr_{y' \in Y}[(x, y') \in S] \geq \delta - \gamma$
- $\Pr[\Omega | S] \geq \frac{\gamma}{\delta}$.

Theorem 1. *If the CDH problem is (t', ϵ') -hard, then the proposed scheme is $(t, q_H, q_{H_0}, q_{H_1}, q_e, q_d, q_s, \epsilon)$ -secure against the adversary $A_{(1-k)II+kIII}$ for a constant $k \in \{0, 1\}$ such that*

$$\begin{aligned}
\epsilon' &\geq \frac{(\epsilon_1 - 2^{-|q|+1})^2 (1 - 2^{-|q|})}{4(q_{H_k} + (1-k)q_d + kq_s)}, \\
t' &\leq 2(t + q_e(t_m) + q_d(t_m + t_p + t_e) + q_s(1t_p + 2t_e + 2t_{m_T})),
\end{aligned} \tag{3}$$

where $\epsilon_1 \geq \frac{\epsilon}{q_H} - ((1-k)q_d(2q_d + q_{H_0})2^{-|G_T|} - kq_s(2q_s + q_{H_1})2^{-|G_T|})$, and t_e, t_m, t_{m_T} and t_p are the time of an exponentiation in \mathbb{G}_T , a scalar multiplication in \mathbb{G} and \mathbb{G}_T and the time of a pairing computation, respectively. In addition, $q_H, q_{H_0}, q_{H_1}, q_e, q_d$ and q_s are the number of queries to oracles $H, H_0, H_1, \text{KeyExtract}, \text{DelGen}$ and PSign , respectively.

Proof. It is supposed that there is an adversary $A_{(1-k)II+kIII}$ against unforgeability of the scheme with success probability ϵ . We construct another algorithm B to solve CDH problem with success probability ϵ' . Given a random instance of the CDH problem $(\mathbb{G}, q, P, aP, bP)$ output by the challenger C , B plans to find abP .

The algorithm B runs Setup on a security parameter l , and gets $(\mathbb{G}, q, P, aP, bP)$ to generate the public parameter $Para = \{\mathbb{G}, \mathbb{G}_T, H, H_0, H_1, F_1, F_2, e, P, P_{pub} = aP, q, l_1, l_2\}$ and sets $i \leftarrow 1$, and invokes the adversary $A_{(1-k)II+kIII}$ on it. The adversary $A_{(1-k)II+kIII}$ runs in time at most t , makes q_H queries to the random oracle H , q_{H_0} queries to the random oracle H_0 , q_{H_1} queries to the random oracle H_1 , q_e queries to the KeyExtract, q_d queries to the DelGen and q_s queries to the PSign algorithm, and can win the unforgeability game with probability at least ϵ . Algorithm B answers $A_{(1-k)II+kIII}$'s oracle queries as described below.

- $H_0(\cdot, \cdot)$ queries: If $T_0[\cdot, \cdot]$ is defined for query $(w || ID_p, K_o)$, then, B returns its value, otherwise B chooses $T_0[w || ID_p, K_o] \xleftarrow{\$} \mathbb{Z}_q$, and returns $T_0[w || ID_p, K_o]$ to $A_{(1-k)II+kIII}$.
- $H_1(\cdot)$ queries: If $T_1[\cdot]$ is defined for query K_p , then, B returns its value, otherwise B chooses $T_1[K_p] \xleftarrow{\$} \{0, 1\}^{|q|}$, and returns $T_1[K_p]$ to $A_{(1-k)II+kIII}$.

- $H(\cdot)$ queries: If $T[ID_i]$ for query ID_u is defined, then, B returns X_i as X_u . If this entry is not yet defined, it sets $ID_i \leftarrow ID_u$, $i \leftarrow i + 1$, and sets $T[ID_i] = (0, X_i = bP)$ if $i = t$. If $i \neq t$, $x_i \xleftarrow{\$} \mathbb{Z}_q$, and sets $T[ID_i] = (x_i, X_i = x_iP)$. Then, B returns X_i to $A_{(1-k)II+kIII}$.
- KeyExtract queries for ID_u : The algorithm B looks up $T[ID_i]$, if $i = t$, it sets $bad_{KE} \leftarrow true$ and aborts the execution of $A_{(1-k)II+kIII}$. Otherwise, B computes $x_u = x_iP_{pub}$, and returns x_u to $A_{(1-k)II+kIII}$. If $T[ID_i]$ for query ID_u is not yet defined, it makes $H(\cdot)$ query for ID_u .
- DelGen queries for (w, ID_p) under an identity ID_o : If $ID_o \neq ID_t$, the algorithm B uses x_o to generate the delegation following the real DelGen algorithm. If $ID_o = ID_t$, B chooses $h_0 \xleftarrow{\$} \mathbb{Z}_q$ and $U_o \xleftarrow{\$} \mathbb{G}$, and computes $K_o = e(U_o, P)e(H(ID_o), P_{pub})^{-h_0}$. If $T_0[w||ID_p, K_o]$ has already been defined, then B sets $bad_{DG} \leftarrow true$ and halts; otherwise, it sets $T_0[w||ID_p, K_o] \leftarrow h_0$. Then, B returns the delegation (w, K_o, U_o, h_0) to the adversary $A_{(1-k)II+kIII}$.
- PSign queries for a message m under proxy signer's identity ID_p : The algorithm B receives the delegation (w, K_o, U_o, h_0) from $A_{(1-k)II+kIII}$. Next, B checks if the delegation is valid for proxy signer's identity ID_p and the warrant w , if m conforms to the warrant w and if $|m| = l_2$. If all conditions hold and $ID_p \neq ID_t$, B generates a valid signature following the real PSign algorithm. If $ID_p = ID_t$, B chooses $\alpha \xleftarrow{\$} \mathbb{Z}$ and $U \xleftarrow{\$} \mathbb{G}$, and computes $\beta = F_1(m)||F_2(F_1(m)) \oplus m$ and $K_p = e(U, P)e(H(ID_o), P_{pub})^{-h_0}e(H(ID_p), P_{pub})^{-\alpha}$. If $T_1[K_p]$ has already been defined, then, B sets $bad_{PS} \leftarrow true$ and halts; otherwise, it computes $h_1 = \beta \oplus [\alpha]_2$, and sets $T_1[K_p] \leftarrow h_1$. Hence, the signature on the message m w.r.t. ID_o and ID_p is $\theta = (w, U, \alpha, K_o, h_0)$.
- Finally, $A_{(1-k)II+kIII}$ outputs a forged identity-based proxy signature θ with original signer's identity ID_o and proxy signer's identity ID_p . The forgery is non-trivial if $ID_o = ID_t$, and A_{II} has not made KeyExtract query on input ID_o and DelGen query on input (w, ID_p) under identity ID_o , or similarly, if $ID_p = ID_t$, and A_{III} has not made KeyExtract query on input ID_p and PSign query on input m under identity ID_p .

The probability of B in returning a forged signature (w, U, α, K_o, h_0) is $\epsilon_1 = \Pr[E_1] \Pr[E_2|E_1]$ which is computed as follows. First of all, we define events E_1 and E_2 .

- E_1 : Algorithm B does not abort as a result of signature simulation (as a result of KeyExtract and DelGen queries for A_{II} and as a result of KeyExtract and PSign queries for A_{III}).
- E_2 : Adversary $A_{(1-k)II+kIII}$ returns a non-trivial forgery.

To lower-bound the probability of B , $\Pr[E_1]$, we need to compute the probability that B does not abort in signature simulation; $\eta = \Pr[E_1] = \Pr[\neg bad_{KE}]((1-k)\Pr[\neg bad_{DG}|\neg bad_{KE}] + k\Pr[\neg bad_{PS}|\neg bad_{KE}])$, where events bad_{KE} , bad_{DG} and bad_{PS} indicate that B aborts in signature simulation as a result of any of $A_{(1-k)II+kIII}$'s KeyExtract, DelGen and PSign queries, respectively. These probabilities are computed as follows.

Claim 1. $\Pr[\neg bad_{KE}] \geq \frac{1}{q_H}$.

Proof. $\Pr[\neg bad_{KE}]$ is the probability that B does not abort as a result of $A_{(1-k)II+kIII}$'s KeyExtract queries. The algorithm B does not abort at answering to KeyExtract queries when $H(ID_o) = bP$ for A_{II} which means that $ID_o = ID_t$ (when $H(ID_p) = bP$ for A_{III} which means that $ID_p = ID_t$), and the probability of this event is at least $\frac{1}{q_H}$.

Claim 2. $\Pr[\neg bad_{DG}|\neg bad_{KE}] \geq 1 - q_d((q_d + q_{H_0})2^{-|\mathbb{G}_T|}) - q_d^2 2^{-|\mathbb{G}_T|}$.

Proof. Events $\neg bad_{KE}$ and $\neg bad_{DG}$ are independent, so $\Pr[\neg bad_{DG}|\neg bad_{KE}] = \Pr[\neg bad_{DG}]$. The value of $\Pr[\neg bad_{DG}]$ is the probability that B does not abort as a result of DelGen queries. The algorithm B aborts at answering to a DelGen query if bad_{DG} is set to true which means that there is a conflict

in the table $T_0[.,.]$. The probability of finding a conflict in $T_0[.,.]$ for one DelGen query (w, ID_p) equals the probability that $(w||ID_p, K_o)$ generated in a DelGen simulation has been occurred by chance in a previous query to the oracle $H_0(.,.)$. Since there are at most $q_{H_0} + q_d$ entries in the table $T_0[.,.]$ and the number of K_o , uniformly distributed in \mathbb{G}_T , is $2^{|\mathbb{G}_T|}$, the probability of this event for one DelGen query is at most $(q_{H_0} + q_d)2^{-|\mathbb{G}_T|}$. Hence, the probability of this event for q_d queries is at most $q_d(q_{H_0} + q_d)2^{-|\mathbb{G}_T|}$. In addition, this probability includes the probability that B previously used the same randomness K_o , uniformly distributed in \mathbb{G}_T , in one DelGen simulation. Since there are at most q_d DelGen simulations, this probability is at most $q_d 2^{-|\mathbb{G}_T|}$. Therefore, for q_d DelGen queries the probability of this event is at most $q_d^2 2^{-|\mathbb{G}_T|}$.

Claim 3. $\Pr[\neg bad_{PS} | \neg bad_{KE}] \geq 1 - q_s((q_s + q_{H_1})2^{-|\mathbb{G}_T|}) - q_s^2 2^{-|\mathbb{G}_T|}$.

Proof. Events $\neg bad_{KE}$ and $\neg bad_{PS}$ are independent, so $\Pr[\neg bad_{PS} | \neg bad_{KE}] = \Pr[\neg bad_{PS}]$. The value of $\Pr[\neg bad_{PS}]$ is the probability that B does not abort as a result of PSign queries. The algorithm B aborts at answering to a PSign query if bad_{PS} is set to true which means that there is a conflict in the table $T_1[.]$. The probability of finding a conflict in $T_1[.]$ for one PSign query K_p equals the probability that K_p generated in a PSign simulation has been occurred by chance in a previous query to the oracle $H_1(.,.)$. Since there are at most $q_{H_1} + q_s$ entries in the table $T_1[.]$ and the number of K_p , uniformly distributed in \mathbb{G}_T , is $2^{|\mathbb{G}_T|}$, the probability of this event for one PSign query is at most $(q_{H_1} + q_s)2^{-|\mathbb{G}_T|}$. Hence, the probability of this event for q_s queries is at most $q_s(q_{H_1} + q_s)2^{-|\mathbb{G}_T|}$. In addition, this probability includes the probability that B previously used the same randomness K_p , uniformly distributed in \mathbb{G}_T , in one PSign simulation. Since there are at most q_s PSign simulations, this probability is at most $q_s 2^{-|\mathbb{G}_T|}$. Therefore, for q_s PSign queries the probability of this event is at most $q_s^2 2^{-|\mathbb{G}_T|}$.

Claim 4. $\Pr[E_2 | E_1] \geq \epsilon$.

Proof. The value of $\Pr[E_2 | E_1]$ is the probability that $A_{(1-k)II+kIII}$ returns a valid forgery provided that B does not abort as a result of $A_{(1-k)II+kIII}$'s KeyExtract, DelGen and PSign queries. If B did not abort as a result of $A_{(1-k)II+kIII}$'s queries, all its responses to those queries are valid. Therefore, by hypothesis $A_{(1-k)II+kIII}$ will produce a non-trivial forgery with probability at least ϵ .

Therefore, the probability that B returns (w, U, α, K_o, h_0) is at least $\epsilon_1 \geq \frac{\epsilon}{q_H}(1 - kq_s((q_s + q_{H_1})2^{-|\mathbb{G}_T|}) - kq_s^2 2^{-|\mathbb{G}_T|})(1 - (1 - k)q_d((q_d + q_{H_0})2^{-|\mathbb{G}_T|}) - (1 - k)q_d^2 2^{-|\mathbb{G}_T|}) \geq \frac{\epsilon}{q_H} - ((1 - k)q_d((2q_d + q_{H_0})2^{-|\mathbb{G}_T|}) - kq_s(2q_s + q_{H_1})2^{-|\mathbb{G}_T|})$. Since H_k is a random oracle for $k \in \{0, 1\}$, the probability of the event that $h_k = H_k(kK_P + (1 - k)(w||ID_p, K_o))$ for $k \in \{0, 1\}$ is less than $2^{-|q|+1}$, unless they are asked during the attack. Hence, in what follows it is likely that queries $kK_P + (1 - k)(w||ID_p, K_o)$ for $k \in \{0, 1\}$ are asked during a successful attack. The lower bound of probability of producing a non-trivial forgery after making queries to H_0 and H_1 oracles is $\epsilon_2 \geq \epsilon_1 - 2^{-|q|+1}$. Then, B uses the oracle replay technique [54] to solve the CDH problem.

Algorithm B employs two copies of $A_{(1-k)II+kIII}$, guesses a fixed index $1 \leq j \leq (q_{H_k} + (1 - k)q_d + kq_s)$ and hopes that j be the index of query $kK_P + (1 - k)(w||ID_p, K_o)$ to oracle H_k for which $A_{(1-k)II+kIII}$ forges a proxy signature, and the probability of a good guess by chance is $\frac{1}{(q_{H_k} + (1 - k)q_d + kq_s)}$. Algorithm B gives the same system parameters, the same identities and the same sequence of random bits to the two copies of $A_{(1-k)II+kIII}$, and responds with the same random answers to their queries for the oracles until they ask the oracle H_k for j th query. At that point (the j th query to the oracle H_k), B gives two random answers h_k and h'_k such that $h_k \neq h'_k$ to the hash queries H_k (forking). Hence, B obtains two proxy signatures (w, U, α, K_o, h_0) and $(w, U', \alpha', K_o, h'_0)$ after $A_{(1-k)II+kIII}$ asks the same query $kK_P + (1 - k)(w||ID_p, K_o)$ from H_k . We employ Splitting Lemma to compute the probability of B in returning these two valid forgeries.

It is assumed that S denotes the set of successful executions of $A_{(1-k)II+kIII}$ when B simulates the signature scheme, and the success probability of $A_{(1-k)II+kIII}$ in returning a non-trivial forgery is taken over the space (X, Y_k) , where X is the set of random bits and random oracle responses that $A_{(1-k)II+kIII}$ takes up except for randomness related to the oracle H_k , and Y_k is the set of random oracle responses to the oracle

H_k . Hence, we have $\Pr[(X, Y_k) \in S] = \epsilon_2$. With Splitting Lemma, we split the randomness Y_k related to H_k to (Y'_k, h_k) , where Y'_k is the set of all random responses to different queries of H_k except for j th query whose answer is denoted as h_k . The Splitting Lemma ensures the existence of a subset of executions Ω such that $\Pr[\Omega|S] \geq \frac{\gamma}{\delta} = \frac{1}{2}$, and for each $(X, Y_k) \in S$, $\Pr_{h'_k}[(X, Y'_k, h'_k) \in S] \geq \delta - \gamma = \frac{\epsilon_2}{2(q_{H_k} + (1-k)q_d + kq_s)}$. If B replays the attack with fixed (X, Y'_k) and a randomly chosen $h'_k \in \{0, 1\}^{|q|}$, it gets another successful pair $((X, Y'_k), h'_k)$ such that $h_k \neq h'_k$ with probability $\frac{\epsilon_2(1-2^{-|q|})}{4(q_{H_k} + (1-k)q_d + kq_s)}$.

After two successful executions of $A_{(1-k)II+kIII}$, B obtains $((X, Y'_k), h_k)$ and $((X, Y'_k), h'_k)$, $h_k \neq h'_k$ which means that it obtains two valid forgeries (w, U, α, K_o, h_0) and $(w, U', \alpha', K_o, h'_0)$ with probability $\epsilon' \geq \frac{\epsilon_2^2(1-2^{-|q|})}{4(q_{H_k} + (1-k)q_d + kq_s)}$, where $\epsilon_2 \geq \epsilon_1 - 2^{-|q|+1}$.

From valid forgeries (w, U, α, K_o, h_0) and $(w, U', \alpha', K_o, h'_0)$, B computes abP as $abP = \frac{U-U'}{\alpha-\alpha'}$ if $k = 1$. In this case, we have the adversary A_{III} and since $h_1 \neq h'_1$ and $\alpha = [\beta \oplus h_1]_{10}$, we have $\alpha \neq \alpha'$, while other random values especially (x_p, x_o, k_o, k_p) are the same and $h_0 = h'_0$. If $k = 0$, B computes abP as $abP = \frac{U-U'}{h_0-h'_0}$. In this case, we have the adversary A_{II} and $h_0 \neq h'_0$, while other random values especially (x_p, x_o, k_o, k_p) are the same and $h_1 = h'_1$ or equivalently $\alpha = \alpha'$.

Algorithm B 's run-time t' is twice of $A_{(1-k)II+kIII}$'s run-time, t , plus the time required to respond to hash queries, q_e KeyExtract, q_d DelGen and q_s PSign queries.

We assume that an exponentiation in \mathbb{G}_T takes time t_e , a scalar multiplication in \mathbb{G} and \mathbb{G}_T take time t_m and t_{m_T} , respectively, and a pairing computation takes time t_p , while other operations take zero time. Each random oracle or KeyExtract query takes time t_m , each DelGen simulation takes time $t_m + t_p + t_e$, and a proxy signature with message recovery simulation takes time $1t_p + 2t_e + 2t_{m_T}$, therefore B 's run-time is $t' \leq 2(t + q_e(t_m) + q_d(t_m + t_p + t_e) + q_s(1t_p + 2t_e + 2t_{m_T}))$. This completes the proof. \square

5 Comparison

The comparison for some short identity-based proxy signatures is summarized in Table 2. The comparison is in terms of DeleGen-Cost, DeleVer-Cost, PSign-Cost and PVer-Cost which are dominating computational cost in delegation generation, delegation verification, proxy signature generation and proxy signature verification, respectively. The computational cost for proxy secret key generation algorithm is ignored in the comparison. For the sake of comparison, we consider expensive operations, and we consider pre-computations in presenting the number of operations such that the same operations during generation and verification of different signatures are computed one time and before each algorithm. For example, terms $e(H(ID_o), P_{pub})$ and $e(H(ID_p), P_{pub})$ in our scheme are the same for different signatures, so, they can be computed before signature generation and verification. As a consequence, we ignore them when we present the number of operations in Table 2. Table 1 presents definitions of symbols used in comparison.

Symbols	Definitions
P	pairing evaluation
E_T	exponentiation in group \mathbb{G}_T
$m_{\mathbb{G}}$	scalar multiplication in \mathbb{G}
$m_{\mathbb{G}_T}$	scalar multiplication in \mathbb{G}_T
l_2	the number of bits of a message m
l_3	the number of bits of a warrant w

Table 1. Symbols' definitions in comparison

In Table 2, we do not consider two identity-based proxy signature schemes with message recovery [44, 45] since non of them is secure.

As shown in Table 2, if we consider just pairing computation, the most expensive operation [55], cost to simplify the computational cost comparison, our scheme is more efficient than those presented in [25, 20, 24, 22], and approximately as efficient as those presented in [19, 21].

Scheme	DeleGen Cost	DeleVer Cost	PSign Cost	PVer Cost	Signature Size
Our Scheme	$1E_T + 1m_{\mathbb{G}}$	$1P + 1E_T + 1m_{\mathbb{G}_T}$	$1E_T + 1m_{\mathbb{G}_T} + 1m_{\mathbb{G}}$	$1P + 2m_{\mathbb{G}_T} + 2E_T$	$2 \mathbb{G} + q + l_3$
Shim [25]	$3m_{\mathbb{G}} + 1P$	$3P + 1m_{\mathbb{G}}$	$3m_{\mathbb{G}}$	$3P + 2m_{\mathbb{G}}$	$3 \mathbb{G} + l_2 + l_3$
Wu et al. [20]	$2m_{\mathbb{G}}$	$2P$	$2m_{\mathbb{G}}$	$3P$	$3 \mathbb{G} + l_2 + l_3$
Ji et al. [22]	$2m_{\mathbb{G}}$	$2P + 1m_{\mathbb{G}}$	$2m_{\mathbb{G}}$	$1m_{\mathbb{G}} + 2P$	$3 \mathbb{G} + l_2 + l_3$
Xu, Zhang and Feng [24]	$2m_{\mathbb{G}}$	$2P$	$2m_{\mathbb{G}}$	$3P + 1E_T$	$3 \mathbb{G} + l_2 + l_3$
Zhang and Zou [19]	$2m_{\mathbb{G}} + 1E_T$	$1P + 1E_T$	$2m_{\mathbb{G}} + 1E_T$	$1P + 2E_T$	$1 \mathbb{G} + 2 \mathbb{G}_T + l_2 + l_3$
Gu and Zhu [21]	$1m_{\mathbb{G}} + 2E_T$ $+1m_{\mathbb{G}_T}$	$1P + 2E_T$ $+2m_{\mathbb{G}_T}$	$1m_{\mathbb{G}_T} + 2E_T$	$2m_{\mathbb{G}_T} + 2E_T$ $+1P$	$2 \mathbb{G}_T + \mathbb{G} $ $+l_2 + l_3$

Table 2. Comparison between our scheme and some existing schemes

As shown in Table 2, our scheme is shorter than all other existing identity based proxy signature schemes since l_2 , the number of bits of a signed message, is omitted in its size. To make it clearer, we write signature size of schemes in terms of bits in Table 3. In the following, let's assume that q be a 170-bit prime, and using any of the families of curves described in [56] to have security the same as the security of the standard 1024-bit RSA signature, each element of the group \mathbb{G} and \mathbb{G}_T will be 171 and 1024 bits, respectively.

Scheme	Actual Signature Size
Our Scheme	$512 + l_3$
Shim [25]	$513 + l_2 + l_3$
Wu et al. [20]	$513 + l_2 + l_3$
Ji et al. [22]	$513 + l_2 + l_3$
Xu, Zhang and Feng [24]	$513 + l_2 + l_3$
Zhang and Zou [19]	$2219 + l_2 + l_3$
Gu and Zhu [21]	$2219 + l_2 + l_3$

Table 3. Signature-size comparison (in bits)

As shown in Tables 3 and 2, our scheme is the shortest compared to all other existing identity based proxy signature schemes since the message m is not required to be transmitted with the signature.

6 Conclusion

In this paper, we showed that Yoon et al.'s identity-based proxy signature scheme with message recovery does not have message recovery property despite their authors' claim, therefore, it is not short. Hence, there was no provably secure short identity-based proxy signature. Then, we proposed a short identity-based proxy signature scheme with message recovery feature which is secure under CDH problem in the random oracle model. As shown in comparison, the size of our signature is reduced compared to identity-based proxy signatures since the original message is not transmitted with the signature. This primitive is useful where bandwidth is one of the crucial concern. Our scheme is designed for messages with fixed length and it can be modified to provide partial message recovery property with the technique presented by Tso et al. in [7]. Furthermore, our scheme is more efficient than (as efficient as) previous identity-based proxy signature schemes.

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