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and extract certain statistics.

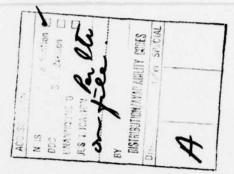
Synthesis of Independent Filtered Random Noise

The purpose of the first program was to produce several channels of independent filtered random noise with a specified spectral shape. The noise is produced by initially generating a series of independent and normally distributed random numbers and then "providing time correlation or dependence" with digital filtering techniques to produce the desired spectral characteristics for each channel.

The techniques used to generate independent but repeatable random numbers by a digital computer are detailed in an excellent survey paper by Chambers¹. Besides describing the history and application of random number generation by computers, a survey was made of current algorithms and their shortcomings. Chambers conclusion was that perhaps the best algorithm is the multiplicative congruental (power residue) method. This method involves multiphying two thirty-five bit numbers together (one of them always being the same) and taking the least significant thirty-five bits of the result as the random number generated. This number is also used as the next multiplier. The success of this method depends on the choice of the constant and on the choice of a starting random number. The method is extremely fast (about 8 μ s as coded by the author on a UNIVAC 1108) and will with proper normalization present numbers evenly distributed between 0 and 1 with negligible dependence from number to number.

The numbers are then transformed to a Gaussian or normal distribution with a zero mean and unit variance using a polynominal fit to the cumulative distribution curve.² These numbers are now equivalent to the numbers that would be obtained after sampling a bandlimited low pass noise spectrum of 1 volt RMS at twice the cutoff (Nyquist) frequency. The remaining task is to produce correlation between the numbers so that they look like numbers which were obtained from sampling a bandpass process at several times Nyquist. This is accomplished by some form of digital filtering.

The theory and application of digital filtering has been documented many places³⁻⁵ and is founded on Z-transform theory⁵. The most efficient method in terms of machine cycles is usually a filter of the recursive type. Such an algorithm works with future, present and past samples to properly filter the data. It was desired for the initial simulation to synthesize a bandpass filter in the frequency domain with rather steep skirts so a 5th order Butterworth design was used. Such a filter



has the response shown in Figure 2 and needs 17 multiply adds per data point. Using the above techniques the author has been able to produce over 50 channels of independent filtered noise about 20,000 samples long in under two minutes on the UNIVAC 1108.

Synthesis of Signals

This program is designed to create multi-channel signals with any desired characteristics to be added to the synthesized noise. Normally in sonar applications the signal is distinguished by its spatial distribution being a plane wave, and by some spectral shape. To properly form the signal a time delay structure is specified and a single channel of filtered noise, sinusoidal components, etc. is split and properly delayed into the correct number of channels. Since the signal is virtually formed on a sample by sample basis the type of signals formed may vary with time. This allows simulation of fading channels, transients, and echoes. The time delay structure for the array under simulation and the type of signal are data inputs to this program. The signal to noise ratios are controlled at the time the signal is added to the spatially correlated noise produced in the third program.

Synthesis of Hydrophone Inputs

It was desired to structure the signal and noise for this simulation to have a realistic acoustic spatial structure as well as temporal structure. In order to accomplish this a method for producing interhydrophone correlation for the noise field was necessary since some arrays7,8 are operating in such an environment. The technique for producing the interhydrophone correlation is detailed in a USL Report by Eby9 and will be reviewed for the reader in a simple form, as used by this program.

Let $e_1(t)$, $e_2(t)$, - - - , $e_N(t)$ represent the voltage at the N hydrophones in question, having a specified covariance matrix $R = (r_{ij})$ where $r_{ij} = \overline{e_i(t)e_j(t)}$. The results of the first program produced N independent channels of noise, which will be represented as x1(t),x2(t). The noise (uncorrelated between channels) covariance is $\overline{x_i(t)x_j(t)} = 0$ for all $i \neq j$. In order to introduce correlation between the channels an NXN matrix of real frequency independent weights A = (aij), which will be called the connection matrix, must be found. The specified covariance matrix may be expressed in terms of the connection matrix as: (1)

 $R = A A^T$

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It turns out there are many <u>A</u> matrices, (at least 2^N) which will satisfy (1) for a particular <u>R</u> matrix. A particular <u>A</u> matrix may be found by solving <u>R</u> for its <u>N</u> eigenvalues, denoted as λ_i , forming a diagonal matrix <u>D</u> whose main diagonal consists of the λ_i , and a matrix <u>C</u> whose ith row are the elements of the ith eigenvector associated with <u>R</u>. Then

$$\underline{\mathbf{A}} = \underline{\mathbf{D}}^{\underline{\mathbf{z}}}\underline{\mathbf{C}} \tag{2}$$

where $\underline{D}^{\frac{1}{2}}$ is the square root of the diagonal matrix \underline{D} .

Another method for solving equation (1) due to Marsaglia¹⁰, provides an algorithm for finding the elements of a triangular matrix <u>A</u> in terms of the original covariance elements as follows:

$$a_{11} = \sqrt{r_{11}}$$
(3)

$$a_{1j} = r_{1j}/a_{11}$$
 (4)

$$a_{ii} = \sqrt{(r_{ii} - \sum_{m=1}^{i-1} a_{mi}^2)} \quad i > 1$$
 (5)

$$a_{ij} = \left\{ r_{ij} - \sum_{m=1}^{i-1} a_{mi} a_{mj} \right\} / a_{ii} \ j > i \ (6)$$

$$a_{ij} = 0, i > j$$
 (7)

Using either of these solutions a network such as the one in Figure 3, may be used so that a particular hydrophone voltage $e_i(t)$

$$\mathbf{e}_{i}(t) = \sum_{j=1}^{N} \mathbf{a}_{ij} \mathbf{x}_{j}(t) \qquad (8)$$

is in general a linear combination of the N uncorrelated channels.

Since the correlated noise field is formed on a sample by sample basis the interhydrophone correlation may be programmed as a function of time. In addition this method allows the study of arrays operating in acoustic noise fields that have unequal correlation, between equidistant hydrophones.

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The third program is also used to add the signals generated in the second program to the correlated noise at any desired S/N ratio at any phone. Multi-target situations are synthesized by the repeated addition of various signals, and time varying S/N ratios are produced by changing the S/N ratios as a function of time.

Forming of Multiple Beams

The fourth program is designed to form multiple beams from the noise and signals that have been synthesized in the first three programs. A pre-calculated time delay structure for the particular array geometry of interest is used to form any number of desired beams. In addition different non-linear operations may be performed on the data before beamforming so that different systems may be compared under identical noise and signal characteristics. The high order statistics at the beamformer output present considerable analytical difficulties for certain of the non-linear operations, but are of considerable interest in system design and performance, and may be estimated from this program.

Post Beamforming Processing

After beamforming a variety of algorithms exist for multibeam sonars that deal with normalization, detection, tracking and parameter estimation that are easily programmed. Simulations of these algorithms are not meaningful however if the high order statistics are unknown at the inputs, and what their relationship is to the input acoustic field. Therefore they must be an integral part of the total simulation. An example of the difficulties encountered is shown by considering the problem of trying to locate an echo on three adjacent beams. What is the probability of an echo being detected on two of the three adjacent beams? Do false alarms occur at the same time on all three beams? The problems are clearly of a multidimensional nature, where the efficiency of Monte Carlo techniques becomes competitive with theoretical methods.

Statistical Estimation and Utility Routines

The last main program is designed to provide estimates of the relevant statistics at various points in the algorithm or "system". Various plots and graphs are produced and summaries of each run. In addition, various routines are used for tape handling, since tapes are produced between each program so that different algorithms may be compared with the same inputs. Some of these routines have been

detailed in other USL Technical Memorandum11,12

Conclusions

Monte Carlo simulations can provide detailed knowledge of how major and minor changes in an algorithm (and the corresponding special purpose hardware used to implement the algorithm) effect certain sonar performance parameters, under identical and controllable input conditions. Because of this it provides a unique sonar design capability that may be effectively used in trade-off studies. In most cases the simulations run on a general purpose computer will not run as fast as the special purpose hardware, and therefore should not be used in a major data reduction program.

R. P. Gordon

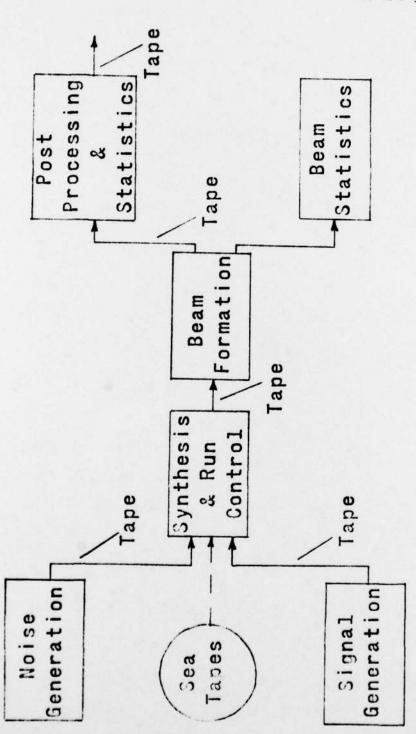
R. L. Gordon Electronic Research Engineer

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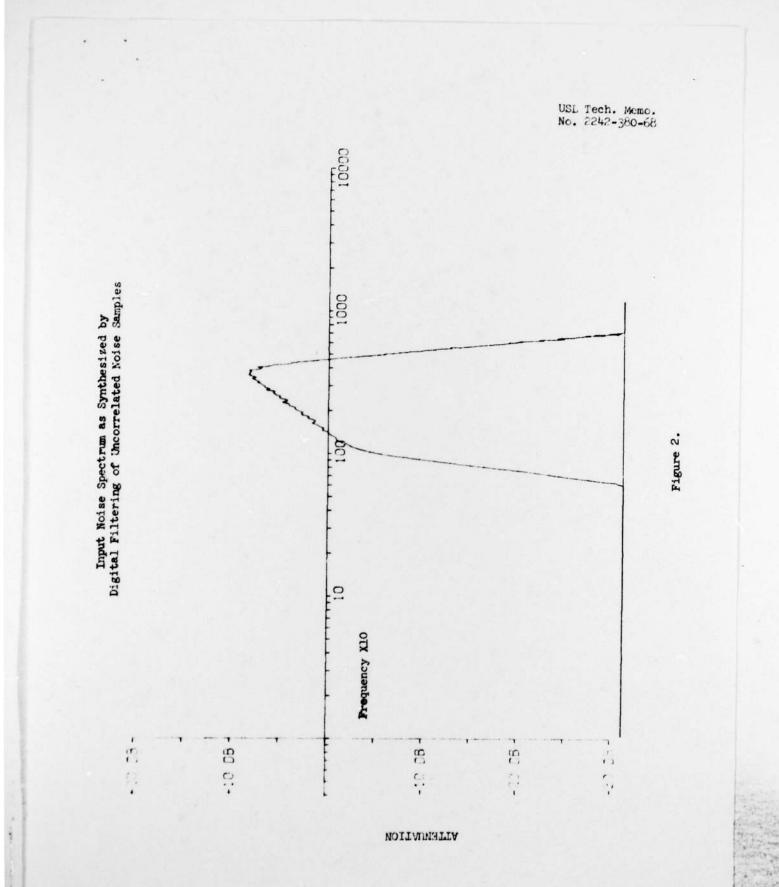
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Existing Software



USL Tech. Memo. No. 2242-380-68

Figure 1.

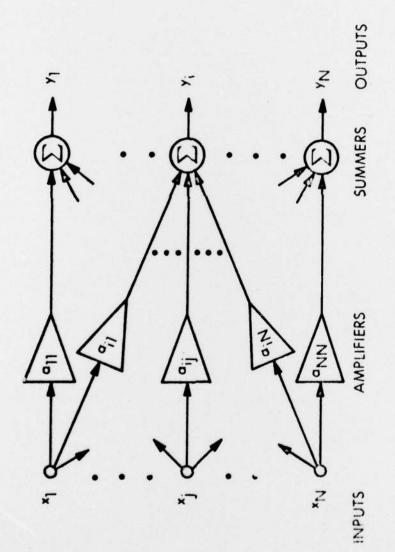


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Synthesis of Spatially Correlated Noise

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From E. S. Eby; USL Report 925