

A Static Phase Offset Reduction Technique for Multiplying Delay-Locked Loop

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Abstract

Static phase offset (SPO) in conventional multiplying delay-locked loops (MDLLs) dramatically degrades the deterministic jitter performance. To overcome the issue, this paper presents a new SPO reduction technique for MDLLs. The technique is based on the observation that the SPO of MDLL is mainly caused by the non-idealities on charge pump (e.g. sink and source current mismatch), and control line (e.g. gate leakage of loop filter and voltage controlled delay line (VCDL) control circuit). With a high gain stage inserting between phase detector/phase frequency detector (PD/PFD) and charge pump, the equivalent SPO has been decreased by a factor equal to the gain of the gain stage. The effectiveness of the proposed technique is validated by a Simulink model of MDLL. The equivalent SPO is measured by the power level of reference spur.

Keywords

Static Phase Offset, Multiplying Delay-Locked Loop, Deterministic Jitter, Reference Spur, PLL

1. Introduction

In high-speed data communication systems, on-chip clock multiplication plays a very important role. Phase-locked loops (PLLs) and multiplying delay locked loops (MDLLs) are widely employed to generate the accurate high-frequency on-chip timing signals from a low frequency, low jitter clock source. If a ring voltage controlled oscillator (VCO) is used in a PLL, the effect of accumulation of oscillator noise will be significant. VCO noise is mainly induced by the noise of power supply, substrate and the control line. Although a high-quality LC-tank oscillator can significantly reduce the effect of noise accumulation, it has a relatively small tuning range and occupies a large die area. This makes LC-tank VCO not the best candidate for data recovery and difficult to integrate. But an MDLL does not accumulate the noise over many cycles on VCDL. Most of the MDLLs are first-order systems; this means that it does not rely on a wide loop-bandwidth to correct for VCDL jitter; conse-

quently the jitter peaking is negligible [1] and the system is also unconditionally stable.

However, relatively high reference spur caused by SPO between the reference edge and its counterpart of MDLL output dramatically degrades its deterministic jitter performance. Different techniques of reducing SPO in MDLL have been reported [2]-[7].

[2] proposed a method to inject the clean reference edges with different phases into different delay stage of VCDL pseudo-randomly. So the SPO also pseudo-randomly showed up on different MDLL output cycle in one reference period. Theoretically the reference spur can be lowered by $20\log(N)$ dB, where N is the division ratio. In [3] a narrow bandwidth auxiliary loop is employed to compensate for the mismatch of charge pump current. Similar to [3], a digital method has been proposed in [4]. In [5] the MDLL output signal is firstly divided by 2, then the divided two parts are sampled by a high-resolution time to digital converter (TDC) separately and finally the results are compared to generate phase error control signal. Similar to [5], a 1-bit TDC and a low-bandwidth delay-tuning path has been employed. The low-bandwidth ensures to suppress the TDC quantization noise to be low enough. In [6], the design focused on positioning of control signal of MUX which selected the clean reference edge or the delay line output feedback signal and the design also focused on a highly matched charge pump (CP). [7] proposed a fractional-N MDLL. A digital to time (DTC) block has been proposed to generate fine-resolution varying reference edge to compensate for SPO.

Although the reference spur performance of MDLL has been improved with all the reported SPO reduction techniques, it still cannot compare with that of PLL. Research effort is still largely needed. To attempt to shorten the research gap, this work proposed a new SPO reduction technique that is inserting a gain stage between PD/PFD and charge pump to achieve lower equivalent SPO.

2. Background

2.1. Operation Principle of MDLL

Typically, MDLL can be divided into two types, edge combiner based and cyclic reference injection based. For the edge combiner based MDLL shown in **Figure 1(a)**, the frequency multiplication is realized by combining the reference edges propagating in the VCDL with equally spaced phases. Compared with the PLL based clock generator, this implementation is easier to design but multiplication ratio is fixed and the mismatches in the delay stages and edge-combining logic significantly contribute the output deterministic timing jitter.

The cyclic reference injection based MDLL shown in **Figure 1(b)** is very similar as a PLL except for the extra MUX and Select Logic blocks. With the MUX, the VCDL output is fed back to its input, and forms a ring VCO as MUX control signal Sel is 0. When Sel changes to 1, the rising edge of reference signal f_{ref} will inject and propagate in the VCDL. And the clean reference edge resets the phase noise accumulated in the previous $M-1$ cycles. The high-frequency signal generated from the VCO-like VCDL is divided by the divider and a pulse signal $last$ is generated at every M cycles. The $last$ signal triggers the select logic to generate Sel . The signal Sel also enables the phase detector to produce the phase difference between the rising edge of f_{ref} and its counterpart of f_{out} then feed it to charge pump to generate the VCDL control signal V_{ctrl} to adjust the delay of VCO-like VCDL. This type of MDLL can easily achieve frequency programmable multiplication. Another significant advantage over the edge combiner based MDLL is that the output frequency is less sensitive to the mismatch among the VCDL. Because each edge of the output passes through the same delay element, the fixed pattern jitter due to mismatch among delay stages is avoided.

2.2. Mechanisms of SPO

In PLL, SPO does not cause as much reference spur as MDLL does because in PLL the reference edge does not replace the counterpart of VCO output. SPO in PLL and MDLL is shown in **Figure 2**. It can be seen that although PLL output has SPO, the period of the N th cycle is almost the same as the average period of other cycles. However, comparing with PLL output, if MDLL output has SPO, the period of N th cycle is much different (either larger or smaller) from the average period of other cycles. SPO is mainly caused by the sink and source current mismatch in charge pump and the current leakage on the control line. The charge pump output current in locked state due to mismatch is shown in **Figure 3**. Please refer to [8] for more detailed analysis about charge pump current mismatch.

The SPO can be calculated in both phase and time domain [8] [9]. In the case with leakage current on control line,

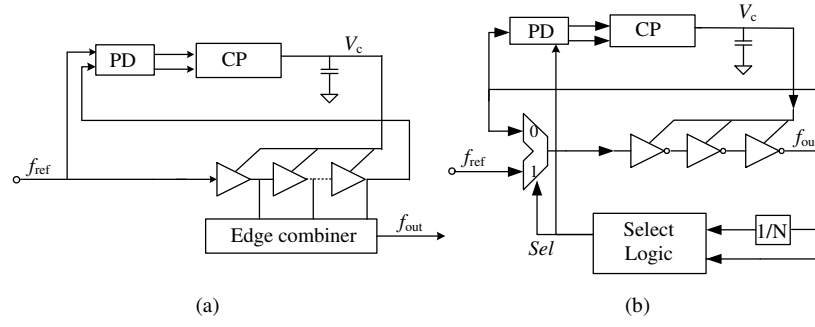


Figure 1. (a) Edge combiner based MDLL; (b) Cyclic reference injection based MDLL.

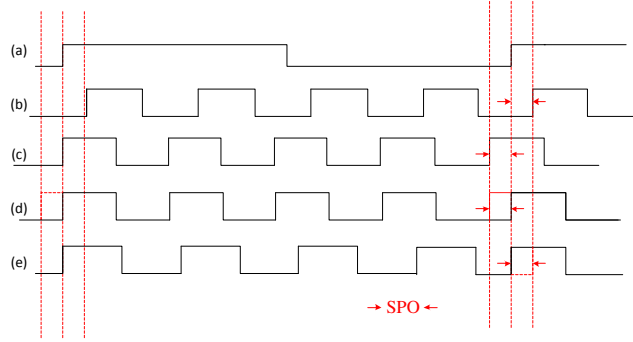


Figure 2. PLL/MDLL output signal in locked state; (a) PLL/MDLL reference signal; (b) PLL output with positive SPO; (c) PLL output with negative SPO; (d) MDLL output with positive SPO; (e) MDLL output with negative SPO.

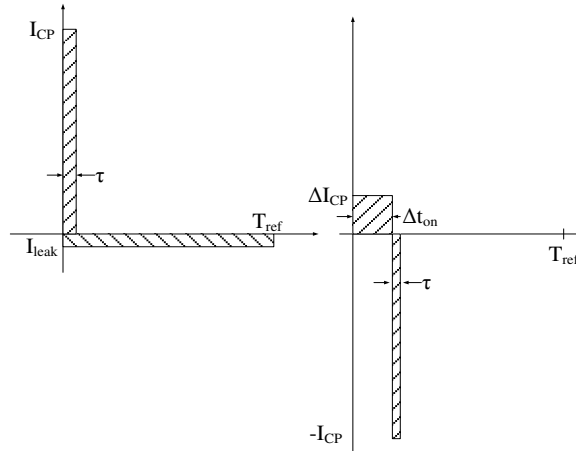


Figure 3. Charge pump output current in locked state due to mismatch [10].

$$\phi_{\text{SPO}} = 2\pi(I_{\text{leak}}/I_{\text{CP}}) \text{ or } \tau = T_{\text{ref}}(I_{\text{leak}}/I_{\text{CP}}) \quad (1)$$

where ϕ_{SPO} and τ are the phase and time domain static phase offset, T_{ref} is the period of reference signal, I_{leak} is the leakage current on control line and I_{CP} is the average charge pump current. In the case of sink and source current mismatch in charge pump,

$$\phi_{\text{SPO}} = 2\pi \frac{\Delta t_{\text{on}}}{T_{\text{ref}}} \frac{I_{\text{UP}} - I_{\text{DN}}}{I_{\text{DN}}} = 2\pi \frac{\Delta t_{\text{on}}}{T_{\text{ref}}} \frac{\Delta I_{\text{CP}}}{I_{\text{DN}}} \text{ or } \tau = \Delta t_{\text{on}} (I_{\text{UP}} - I_{\text{DN}}) / I_{\text{DN}} = \Delta t_{\text{on}} \Delta I_{\text{CP}} / I_{\text{DN}} \quad (2)$$

where T_{reset} is the reset time of tri-state phase frequency detector (PFD), I_{UP} and I_{DN} are the source and sink current

of charge pump. Here I_{UP} is assumed to be larger than I_{DN} . If I_{DN} is larger than I_{UP} , Equation (2) can be expressed as

$$\phi_{SPO} = 2\pi \frac{\Delta t_{on}}{T_{ref}} \frac{\Delta I_{CP}}{I_{UP}} \quad \text{or} \quad \tau = \Delta t_{on} \Delta I_{CP} / I_{UP} \quad (3)$$

3. Proposed SPO Reduced MDLL

3.1. Concept of the Proposed SPO Reduction Technique

The concept of block diagram of the proposed SPO reduction technique is shown in **Figure 4**. **Figure 4(a)** shows the S-domain model of cyclic reference injection based MDLL. To model the edge combiner based MDLL, the only requirement is to change the division ratio to “1” because the loop (shown in **Figure 1(a)**) essentially is a DLL. The SPO shown in **Figure 2(c)-(d)** is modeled as phase error $\Delta\theta$ shown in **Figure 4(b)**. Because the charge pump current mismatch and leakage current on the control line are not proportional to charge pump current value, if a high gain stage with gain of G is inserted between PD/PFD and charge pump shown in **Figure 4(c)**, at the same time decrease the charge pump current by a factor of G , the loop characteristic is not changed but the equivalent SPO has been decreased to $\Delta\theta/G$ shown in **Figure 4(d)**.

3.2. Proposed SPO Reduced MDLL

To achieve a gain stage between the PD/PFD and charge pump, one possible way is to employ time amplifiers to amplify the UP and DN pulses width of tri-state PFD. Another way is to convert the time domain signal, VCDL output phase signal, to a voltage signal. Because to process a voltage-domain signal is much easier than to process a time-domain signal this work adopted the second method. **Figure 5(a)** shows the proposed MDLL. Comparing with the conventional one shown in **Figure 1(b)**, the PD of this MDLL shown in **Figure 5(b)** has only one input which is the output of VCDL. The architecture can dramatically reduce the error caused by path mismatch due to avoiding comparison of two different edge signals as conventional PFD does. The PD consists of a period to voltage converter and a delta modulator. As shown in **Figure 4(c)-(d)**, the first $N-1$ cycles of MDLL output waveforms have evenly distributed in-lock error and the N th cycle has either larger or smaller period. The operation principle of PD is: firstly the VCDL output f_{out} is converted to a voltage signal based on each period through a period to voltage converter then the converted voltage signal of N th cycle is sampled by *Sel1* to produce V_{inst} . The converted voltage signal of the first $N-1$ cycles is sampled by *Sel2* and goes into a delta modulator to generate the period average signal V_{ave} . The simplified timing diagram of PD is shown in **Figure 6**. The delta modulator provides a highly accurate average period of the first $N-1$ cycles of VCDL output. V_{inst} subtracts V_{ave} through V/I circuit shown in **Figure 5(c)** to extract SPO information and this information is converted to the VCDL control voltage V_c .

4. Simulation Results

The proposed MDLL described above was verified by a behavioral model built in Simulink shown in **Figure 7**. It mainly consists of a VCDL modeled with a *Variable Delay Line*, a divider with division ratio of 10, a block of *Extract period value* extracting each cycle period value from VCDL output f_{out} waveform and a block of *PD + V/I* shown in **Figure 8** extracting SPO. Loop filter capacitor is modeled with *Integrator1*. *Loop Gain1* is the product of factor of period to voltage conversion, factor of voltage to current conversion, loop filter gain and VCDL gain. T_n in **Figure 8** is the n -th output period, $G1$ is the gain of period to voltage converter equivalent to the gain of the gain stage in **Figure 4**. $(G1*G2)$ is equivalent to the gain of the integrator in **Figure 5(b)**. The N th period is deducted by the integrated value to extract the period error value which is integrated again to generate a new average period value. This procedure will be repeated as long as the circuit operates. Since the main in-lock error appears in the last period within one reference cycle, this error detection is controlled by *Sel1*. Then the error value is sent to loop filter to generate a control voltage to tune the VCDL delay. Non-idealities caused SPO is modeled as an additive constant which is labeled as “SPO” shown in **Figure 8**. This “SPO” has the unit of time.

The reference signal f_{ref} is 100MHz, division ratio is 10 and the *Initial propagation delay* is 480 ps. *Loop Gain1* = 1.28 e4 and *TransPOrt Delay2* = 2.5 ns. Simulation results of the MDLL output signal spectra are shown in **Figure 9**. The center frequencies in all of the spectra plots are 1 GHz. In **Figure 9(a)**, the SPO and $G1$ are set to 0 and 1 respectively, the spectrum plot shows that the reference spur has similar power to noise floor. In **Figure 9(b)**,

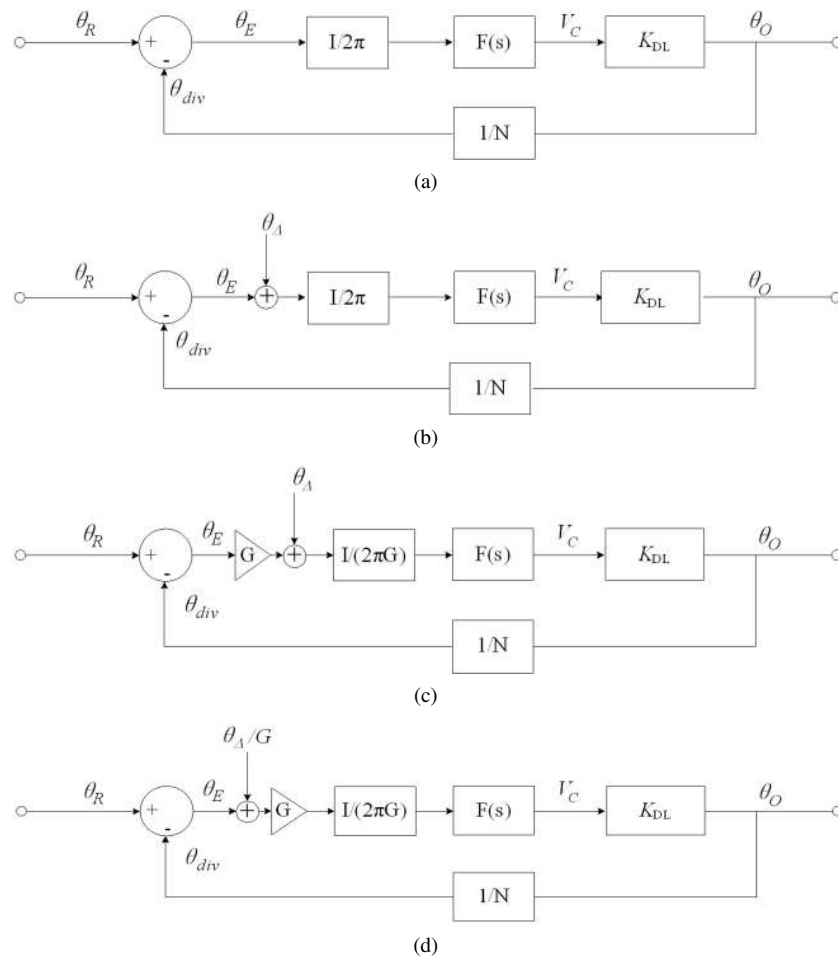


Figure 4. Concept of block diagram of the proposed SPO reduction technique; (a) S-domain model of MDLL; (b) S-domain model of MDLL with SPO $\Delta\theta$; (c) S-domain model of MDLL with SPO $\Delta\theta$; and a gain stage insertion; (d) Equivalent SPO becoming $\Delta\theta/G$ after a gain stage insertion.

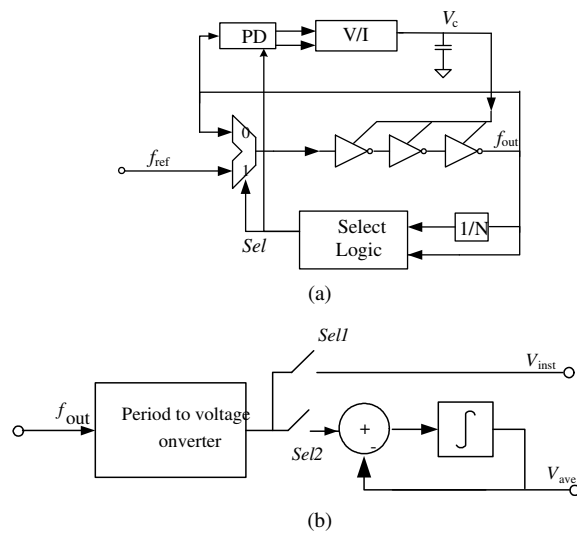


Figure 5. (a) Block diagram of proposed MDLL; (b) Block diagram of PD; (c) Schematic of V/I.

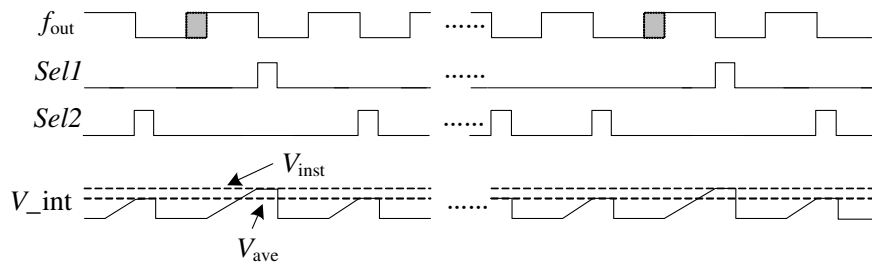


Figure 6. Simplified timing diagram of PD.

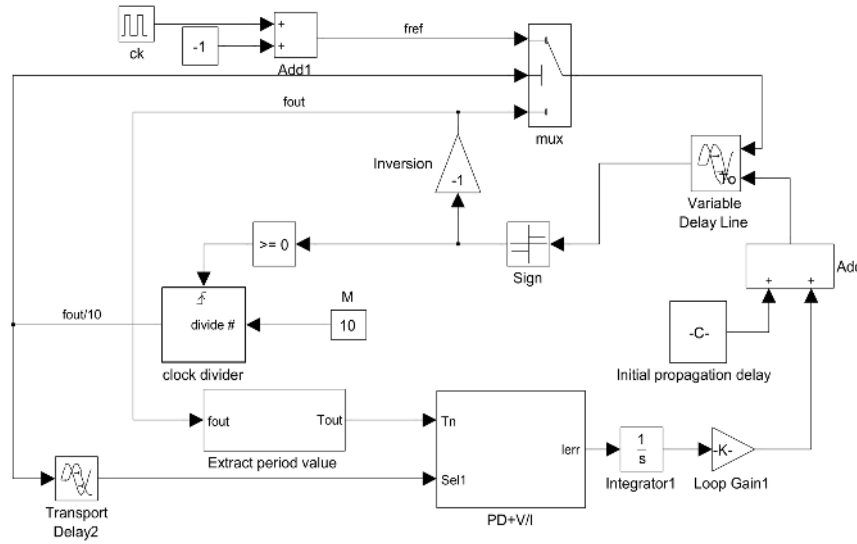


Figure 7. Simulink model of proposed MDLL.

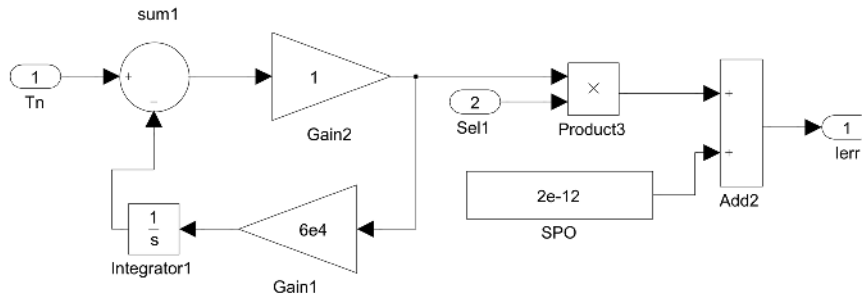
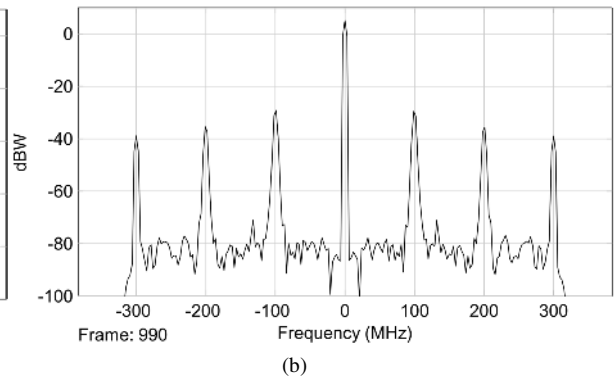
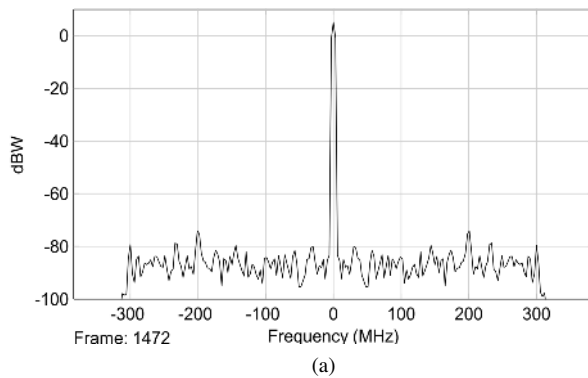


Figure 8. Model of PD + V/I.



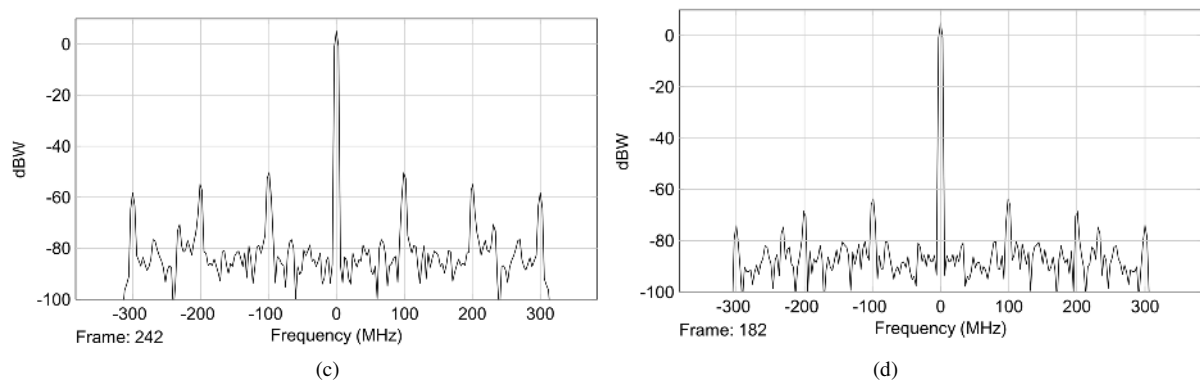


Figure 9. Spectral plots of VCDL output under different conditions (a) SPO = 0, G1 = 1; (b) SPO = $2e-12$, G1 = 1; (c) SPO = $2e-12$, G1 = 10; (d) SPO = $2e-12$, G1 = 50.

SPO = $2e-12$ and G1 = 1, the reference spur is about -30 dBc. In **Figure 9(c)**, SPO = $2e-12$ and G1 = 10, the reference spur is about -50 dBc. In **Figure 9(d)**, SPO = $2e-12$ and G1=50, the reference spur is about -64 dBc.

5. Conclusion

A concept of static phase offset reduction technique for MDLL has been proposed. The concept is also effective for PLL. A SPO reduction MDLL based on the concept has been proposed. It is verified by a behavioral simu-link model. The simulation results validated both the proposed concept and the SPO reduction MDLL. The reduced equivalent SPO is measured by the power of reference spur level.

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