

## A Systematic Review on Mathematical Language Learning Using PRISMA in Scopus Database

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### Abstract

Through a search executed on Scopus database with general keywords such as 'mathematical language' and related terms, this study reveals the analysis of previous published articles based on PRISMA's procedure where it guides researchers' self-regulated learning on online platform. This review exhibits both inclusion and exclusion criteria in the publication distribution. Whilst, all included documents are articles in English language; the excluded articles are those from medicine subject area. The distribution of articles published specifically by years, subject areas, authors, countries and authors' affiliated universities were examined. The varied of findings show Scopus database provides essential information pertaining to mathematical language and approach carried out involving students from various level. The study also reveals there are wide-ranging articles related to mathematical language and technology approach in the database. Meanwhile, developing student's mathematical language learning using technology is one of the effective strategies. However, less attention has been given to such approach.

**Keywords:** mathematical language, PRISMA, Scopus, student, review

## INTRODUCTION

### Mathematical Language

Previous study revealed that there are at least three main sources of students' challenges using mathematical language which include mathematical language, image and notation (Alkhateeb, 2019), getting started on a proof, and conceptual understanding (Moore, 1994). First, the challenges with mathematical language are discussed in terms of mathematics register involving new meanings for everyday words (e.g. column, odd, prove), new words with specific meanings (e.g. hypotenuse), and modes of argument (Zack, 1999). For example, many children have limited understanding of 'more' and 'less' (Warren, 2006) and logical connectives such as 'because', 'but', and 'if...then' which are linked to generalizations to make arguments of mathematically strong (Zack, 1999).

Second, the challenges with proof understanding from Exist-All (EA) and All-Exist (AE) statements are presented. EA statements such as "There exists . . . for all . . ." convey various interpretations than AE statement

such as "For all . . . there exists...". It was found that students' proof skills for such statements modified their understanding of these statements. Moreover, confronted statement with EA and/or AE forms could help them determine the appropriate mathematical meanings. Therefore, the use of formal logic and knowledge of mathematical language structure are useful tools in proving mathematical statements (Piatek-Jimenez, 2010).

Third, the challenges with conceptual understanding could be interpreted via self-explaining process. The process commences as the students' attempt to describe targeted mathematical concepts regardless of the language type used, either formal or informal terms to explain reasoning. Besides, individual language abilities influence mathematics word problem solving achievement for most students at various levels (Walkington, Clinton, & Sparks, 2019).

Students who frequently practice using formal language would have greater procedural knowledge gains (McGinn & Booth, 2018). However, by evaluating only the procedural 'doing' of mathematics, it cannot be completely achieved without mathematical vocabulary

### Contribution to the literature

- This study demonstrates a step by step of PRISMA searching procedures (e.g., identification, screening, eligibility and inclusion) to enhance students' self-regulated learning through online platform.
- This study offers various educational level, methods and tools on the mathematical language usage among students employed in recent articles that may help teacher to identify strategies for teaching mathematics.
- This study identifies online learning environments as an important approach which engages students with mathematical language and transforms informal mathematical language to more formal one.

(and language) (Van Jaarsveld, 2018). Vocabulary was found to be a significant predictor for executive functioning (EF) which is defined as a process that controls thought and action; whereby mathematical language is related to the development of EF. Language complexity such as abstract vocabulary must be considered in exploring the factors contribute to EF development in the early years (Schmitt, Purpura, & Elicker, 2019).

Therefore, increasing children's exposure to mathematical language can positively affect their general mathematics skills (Purpura, Napoli, Wehrspann, & Gold, 2016), spatial mathematical skills (Medina Herrera, Castro Pérez, & Juárez Ordóñez, 2019) and numeracy skills (Hornburg, Schmitt, & Purpura, 2018). General mathematics skills refer to mathematical language that is highly content specific; whereby the use of this specific language affects children's mathematical knowledge (Purpura et al., 2016). Spatial mathematical skills are related to the utterance of spatial relations of which movement between objects is among significant considerations (Rudd, Lambert, Satterwhite, & Zaier, 2008). Important skill at the initial mathematical language utilization is numeracy skills. Understanding numerical skills involves number sense such as verbal counting, numeral identification, ordering numerals, comparisons of sets and/or numerals, cardinality, story problems and one to-one correspondence (Hornburg et al., 2018).

Previous studies indicate several different definitions for mathematical language. Generally, mathematical language or language of mathematics is defined as vocabulary, word order, syntax, and abbreviations unique to mathematics (Simpson & Cole, 2014). Definition from Bakhtin (1981) ideas more than just teaching vocabulary; mathematical language is understood through classroom interaction whereby situated dialogic relations exist between multiple discourses, voices and languages (Barwell, 2015). Therefore, interactions or communications emerged involve the use of mathematical language.

Many scholars define mathematical language in terms of utilization of mathematical language. Using mathematical language means understanding the language about one's own learning (O'Brian, Nocon, & Sands, 2010). Specifically, the use of language comprises

using correct or exact formal mathematics terminology (McGinn & Booth, 2018; Van Jaarsveld, 2016). Those include using mathematical language and notation in doing proof and using mathematical statements (Moore, 1994; Piatek-Jimenez, 2010). Thus, employing formal language regularly leads to higher procedural knowledge acquisition (Simpson & Cole, 2014).

The use of mathematical language involves the interpretation of mathematical meaning (Warren, 2006) through students' reflection on their classroom assessment performance and their explanation on the ways they attain correct and incorrect answers; then setting specific goals to improve their learning in future (O'Brian, Nocon, & Sands, 2010). Interpretation on symbolic mathematical language is also used in formal language of other fields such as physics (De Lozano & Cardenas, 2002) and computer systems (Zinn, 2006).

The interpretation of meaning does not merely depend on knowledge of key words or concepts (Hornburg et al., 2018), but also relies on understanding the key words used in mathematics (Purpura et al., 2016). Understanding the keywords refers to students' capability of using appropriate mathematical vocabulary (Barwell, 2015; Caniglia, Borgerding, & Meadows, 2017; Firmender, Gavin, & McCoach, 2014) including the ability to discriminate mathematical vocabulary usage to promote academic outcomes (Van Jaarsveld, 2016). This can be known through students' spoken words that transform from everyday language to more formal mathematical language (Simpson & Cole, 2014). The connection between informal and formal mathematical languages represents the beauty of word pattern (Serder & Jakobsson, 2015). Therefore, from previous definitions, mathematical language can be defined as specific focus on vocabulary to help students in connecting informal and formal mathematical languages using linguistic and communicative resources to obtain information (Caniglia et al., 2017).

Test, tasks, assessments, courses, project and assignments are various typical resources used in previous studies to examine student's mathematical language development (Hornburg et al., 2018; Moore, 1994; Piatek-Jimenez, 2010; Schmitt et al., 2019; Van Jaarsveld, 2016; Zack, 1999). However, different fields can benefit from the utilization of various technology tools and internet software which transforms

conventional learning into more interactive and engaging environment in the classroom. In language area, online tools such as Barrier game or Desmos®/ Polygraph program are developed for transforming informal language into formal language. Such online tools facilitate students' construction of mathematical knowledge through learning and application process to be more authentic (Caniglia et al., 2017). Additionally, language games are also used in small groups for science intervention (Serder & Jakobsson, 2015). In mathematics education, virtual environments such as 3D tools and 3D printing are adapted in developing spatial mathematical skills in higher education (Medina Herrera et al., 2019). Meanwhile in lower and middle grades; online problem-solving environment is utilized to examine the effects of individual language features on word problem solving performance (Simpson & Cole, 2014). Therefore, there are three main dimensions for the mathematical language learning, namely knowledge of the meaning of mathematical words, application of discourse, reading and writing of mathematical language in the classroom and ability to understand word problems (Warren, 2016).

The purpose of this study is to review previous published articles on mathematical language learning. This study will help researchers in obtaining information about the experts in mathematical language including country of origin and affiliation, subject areas and the focus of recent research on mathematical language studies. From educators' perspectives, this review may assist in improving their understanding on how mathematics is used specifically to discover deficiencies that require modification or supplementary materials in the classroom.

Furthermore, the information gathered from content analysis review enables them to evaluate their own teaching methods, use appropriate mathematical language in their learning, associate and develop new ideas into their own study and implement desired instructional processes. This analysis will also benefit policy makers, textbook's writers, education leaders, researchers and teachers to the extent of which researches to date on mathematical language are analysed and clarified. The results can help allocating existing materials and resources needed and making organization to guide future research.

## PRISMA

Preferred Reporting Items for Systematic reviews and Meta-Analyses (PRISMA) statement was developed in 2005 and was regularly reported by David Moher and the team in their published medical article (Moher et al., 2009). PRISMA statement consist of four steps, namely, identification, screening, eligibility and inclusion criteria. Identification is the process to enrich main keywords using several steps so that articles from the

database could be retrieved as wider as possible. The second phase is screening, a process to include or exclude articles base on criteria decided by authors and generated using database. Exclude articles means to remove unnecessary articles according to the types of articles. The third phase is eligibility, all articles were examined by reading through the title, abstract, method, result and discussion to ensure they meet the inclusion criteria and parallel with the current research objectives. The final phase, inclusion criteria where the articles left and fulfil the requirement to be analysed.

PRISMA can also be used as the foundation for reporting systematic review and benefits various fields (Moher et al., 2009). At least three major benefits of using PRISMA as guidance procedure in online training environment specifically for students, teachers, researchers or other readers. First, PRISMA procedure provides systematic searching procedures (e.g., identification, screening, eligibility and inclusion) to enhance students' self-regulated learning through online platform. Second, a step-by step procedure may be used by post graduate students or researchers as useful guidance to support their comprehensive searching to attain the required articles. Third, the PISMA procedures provide readers with clear comprehension of the process, easy observation of the connection between information and its sources via systematic reviews recording and straightforward evaluation of reported systematic reviews.

Based on the discussion of PRISMA procedure presented, explicit aspects of mathematical language learning are better supported. However, limited reviews on mathematical language learning researches in Scopus database utilizing PRISMA procedure as the guideline for documents search were discovered, not to mention reviews on content analysis. For example, content analysis reviews by Voronina, Tretyakova, Krivonozhkina, Buslaev, and Sidorenko (2019), Aydin (2019), Genç, Masalimova, Platonova, Sizova, and Popova (2019), Odabasi, Uzunboylu, Popova, Kosarenko, and Ishmuradova (2019), Ozcinar, Zakirova, Kurbanov, and Belyalova Simpson and Cole (2019) and Zack (1999) in Scopus database definitely do not apply PRISMA procedure. Therefore, extensive content analysis is needed to better understand the researches conducted on knowledge and understanding of mathematical language and how to apply them. This study utilizes PRISMA procedure to guide self-regulated learning on online platform.

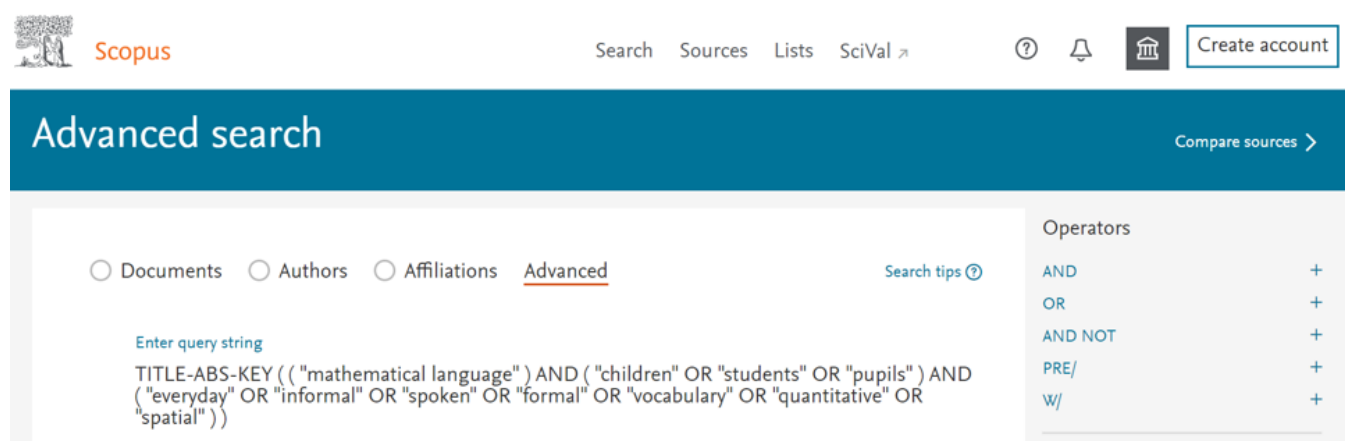
## The Objectives of the Study

The purpose of this study is to examine the researches on mathematical language learning using PRISMA in Scopus database. Under this general aim, the answers are searched for the following research questions (RQ):

RQ1: How are the articles distributed over the years?

**Table 1.** The search string

Database	Search String
Scopus	TITLE-ABS-KEY ( ("mathematical language" ) AND ( "children" OR "students" OR "pupils" ) AND ( "everyday" OR "informal" OR "spoken" OR "formal" OR "vocabulary" OR "quantitative" OR "spatial" ) )



**Figure 1.** Advanced menu to enter search string

- RQ2: What is the distribution of subject areas in the articles?
- RQ3: What is the distribution of authors in the articles?
- RQ4: What is the distribution of authors' country of origin in the articles?
- RQ5: What is the distribution of authors' affiliation in the articles?
- RQ6: What is the distribution of 'what', 'who' and 'how' associated with mathematical language and learning approach in the articles?

over 14000 journals for numerous fields including social sciences and mathematics.

### Limitations of Study

This research is limited to the selected articles in Scopus database, accessed via Universiti Sains Malaysia database, one of Malaysia public universities. Content analysis of the articles is limited to six themes specified in RQ1 to RQ6; whereby themes in RQ6 is limited to three categories. In addition, using single database exclusively has its shortcomings since it does not cover all languages, all fields and all journals in the world (Falagas, Pitsouni, Malietzis, & Pappas, 2008). Hence, this study only utilized this database to provide systematic and complete article searching procedure and analysis.

## METHODOLOGY

### The PRISMA Procedure

Titles and abstracts of 27 articles were filtered by the first author after inclusion and exclusion process which was automatically completed using database system (Table 2); and 25 articles were selected to be read in full text. The first author read full text of all articles. Whilst, the second author read full text of fifteen articles; the third author read subsequent ten articles. These three authors discussed the articles' relevancy to the study's research questions; then determined if it meets the inclusion criteria. When there was any doubt as to whether the article met the inclusion criteria, the second author conducted an independent evaluation. Finally, twenty articles were included. The selection process is shown in Figure 4.

### Scopus Database Resource

The present study utilized the most common database that is Scopus. Scopus has its own uniqueness as it is produced by reputable Elsevier Co and indexed

### The Systematic Review Processes

#### Identification

The first process involves the identification process whereby main keywords are enriched by identifying, searching and listing its synonyms so that articles from the database could be retrieved as many as possible. The researchers began to generate search strings using Scopus formatting in February 2020 (Table 1) through Universiti Sains Malaysia database.

Next, the search string was pasted on Enter query string in Advanced menu (Figure 1). As a result 49 documents were retrieved at the first phase (Figure 2).

#### Screening

The second phase is called the screening process whereby articles are included or excluded based on the criteria decided by the researchers and generated using

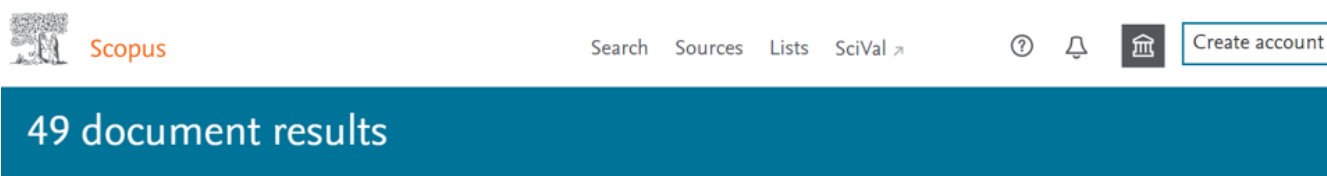


Figure 2. The number of documents accessed on Scopus database using search string

Table 2. The included and excluded criteria

Criteria	Inclusion	Exclusion
Type of articles	Journal (research articles)	conference proceeding, systematic review articles, book series, chapter in book and books
Language	English	Non-English
Timeline	until February 2020	-
Field	Other than medicine	Medicine

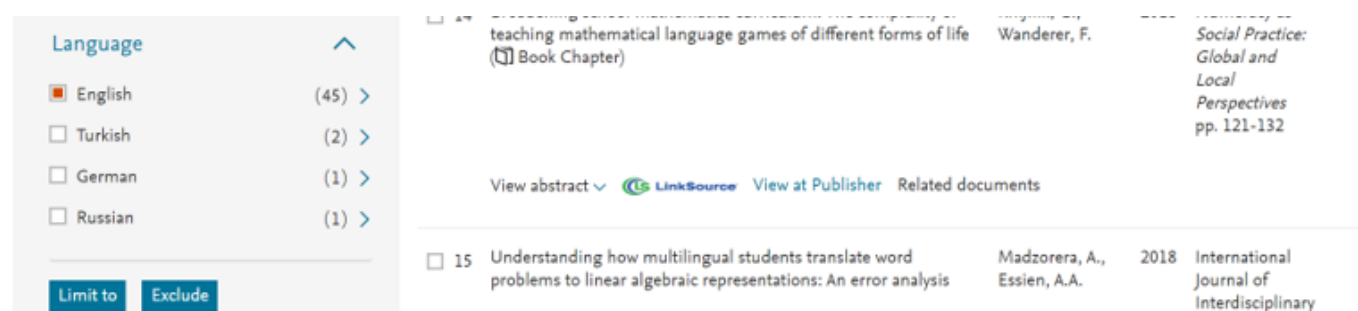


Figure 3. The procedure to include and exclude the access documents

database. Whilst, the term ‘included articles’ refers to the articles that meet the required criteria; the ‘excluded articles’ refers to the unnecessary articles that are removed according to its’ types. The included and excluded criteria are summarised in Table 2.

The researchers continued the process by selecting the types of document in the database for ‘article’ and those that are in ‘English Language’. The procedure to include the types was carried out by clicking on left side box of the website interface and chose the Limit to button at the bottom of the tick boxes. Then, subject area of Medicine was excluded by pressing Exclude button at the bottom of the tick boxes (Figure 3). Consequently, the screening process produced 27 articles. Later, the researchers examined the distribution of articles published specifically by years, subject areas, authors, countries and authors’ affiliated universities. Out of 27 articles, two articles were excluded as the researchers failed to obtain full-text articles. Furthermore, the abstracts lack information required especially full result and whole picture of the topic.

### Eligibility

Therefore, 25 articles were included in the third phase known as the eligibility process. All articles were examined by reading through the titles, abstract, method, result and discussion to ensure they met the inclusion criteria and parallel with current research

objectives. It was discovered that five articles needed to be rejected based on two criteria; one is they did not involve students and two is type of the article. Finally, only 20 articles left and fulfilled the requirements to be analyzed (Figure 4).

### RESULTS

Two steps were carried out to examine the articles and obtain the data for the study. Firstly, the researchers investigated PRISMA’s Screening phase (Figure 4); whereby 27 articles were obtained as filtering process automatically took place using Scopus database. It is important to note that a total of 5 categories: years, subject areas, authors, authors’ country of origin and authors affiliation, were examined to answer the first to the fifth sub-objective. Secondly, the researchers investigated PRISMA’s Included phase (Figure 4); whereby 20 articles were selected via researchers’ manual filtering process and 3 categories: ‘what’, ‘who’ and ‘how’, were examined to answer the sixth sub-objective.



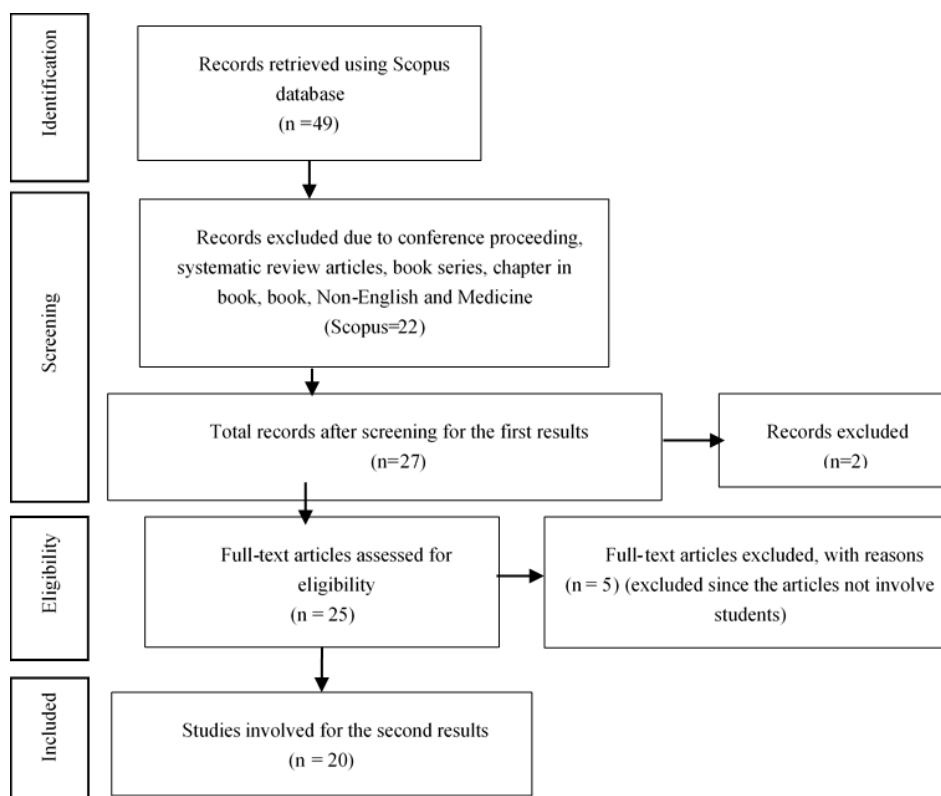


Figure 4. PRISMA's flow map

Table 3. Distribution of articles by years

Years	F
2019	3
2018	4
2017	2
2016	4
2015	1
2014	1
2012	2
2010	2
2008	1
2007	1
2006	2
2002	1
1999	1
1994	1
1991	1

Table 4. Distribution of articles by subject areas

Subject area	f
Social Sciences	23
Mathematics	10
Psychology	6
Engineering	3
Arts and Humanities	2
Computer Science	1
Physics and Astronomy	1

publication increases gradually within the last five years from 2014 to 2019 of which 14 articles were published. It shows that current researchers are getting more interested to study the field of mathematical language.

**RQ2: What is the Distribution of Subject Areas in the Articles?**

Within the scope of current research from Scopus database, number of scientific articles executed in different research fields investigated and its results are presented in Table 4. The distribution of subject areas in the articles shows that most studies were conducted in Social Sciences with 23 articles; followed by Mathematics with 10 articles. However, publication frequency related to mathematical language is extremely lacking in two areas: Computer Science and Physics and Astronomy. It shows that scholars from Social Sciences and Mathematics are those who were interested in mathematical language studies. It also reveals that researchers from Computer Science area were also

**RQ1: How are the Articles Distributed over the Years?**

As shown in article distribution according to its publication year in Table 3, no article publication is available in one group of two consecutive year in 1992 and 1993, two groups of three consecutive year in 2011, 2012, 2013 and 2003, 2004, 2005. It was also noticed that there is no article published for one group in four consecutive year between 1995 to 1998; and the biggest gap is for one group in five consecutive year from 2001 to 2005. Therefore, there were not many article publications in mathematical language from 1991 to 2014; of which total number of article publications available within these 24 years period is only 13 articles. However, article

**Table 5.** Distribution of articles by authors

Authors	f	Authors	f	Authors	f	Authors	f
Purpura, D.J.	3	Elicker, J.G.	1	Madzorera, A.	1	Sands, D.I.	1
Schmitt, S.A.	2	Essien, A. A.	1	McCoach, D.B.	1	Sanger, M.	1
Van Jaarsveld, P.	2	Firmender, J.M.	1	McGinn, K.M.	1	Satterwhite, M.	1
Arcavi, A.	1	Gavin, M.K.	1	McLeman, L.	1	Serder, M.	1
Barwell, R.	1	Giddings, M.M.	1	Meadows, M.	1	Simpson, A.	1
Booth, J.L.	1	Gold, Z.S.	1	Medina Herrera, L.	1	Sparks, A.	1
Borgerding, L.	1	Hadas, N.	1	Moore, R.C.	1	Walkington, C.	1
Caniglia, J.	1	Hornburg, C.B.	1	Napoli, A. R.	1	Warren, E.	1
Cardenas, M	1	Jaafar, R.	1	Nocon, H.	1	Wehrspann, E.A.	2
Castro Perez, J.	1	Jakobsson, A.	1	O'Brian, J.R.O.	1	Zack, V.	1
Clinton, V.	1	Juarez Ordonez, S.	1	Piatek-Jimenez, K.	1	Zaier, A.	1
Cole, M.W.	1	Karsenty, R.	1	Pirie, S.	1	Zinn, C	1
De Lozano, S.R.	1	Lambert, M.C.	1	Rudd, L.C.	1		

**Table 6.** Distribution of articles by authors' country of origin

Countries/ Area	f
United States	15
South Africa	3
Canada	2
United Kingdom	2
Argentina	1
Australia	1
Israel	1
Mexico	1
Sweden	1

interested in studies related to mathematical language as presented in [Table 4](#).

**RQ3: What is the Distribution of Authors in the Articles?**

[Table 5](#) indicates that 51 authors have significant works published in mathematical language. Out of 51, Purpura has three publications; meanwhile, Schmitt, Van Jaarsveld and Wehrspann have two publications each. The trend for the other authors remains constant with one publication each. Thus, it can be observed that prominent scholar in mathematical language is Purpura with the highest number of articles published; followed by Schmitt, Van Jaarsveld and Wehrspann.

**RQ4: What is the Distribution of Authors' Country of Origin in the Articles?**

Top nine countries published the most mathematical language related articles in Scopus database is presented in [Table 6](#). The results illustrate that the United States has the most scientific works executed and published in mathematical language with 15 articles. This value is far different compared to South Africa at the second rank with only three article publications. Meanwhile, Canada and United Kingdom are at the third rank with two article publications each. Five other countries such as Argentina, Australia, Israel, Mexico and Sweeden have the least article published one article each. Hence, it is evidence that western countries produce the highest number of article publications in mathematical

**Table 7.** Distribution of articles by authors' affiliation

Affiliation	f	Affiliation	f
Purdue University	3	Southern Methodist University	1
University of Witwatersrand	3	Weizmann Institute of Science Israel	1
Tiffin University	1	Texas Tech University at Lubbock	1
St. George's Elementary School	1	University of Michigan-Flint	1
Southern College of Seventh-Day Adventists	1	University of Connecticut	1
Valdosta State University	1	University of Dakota	1
Saint Joseph's University, United States	1	Clemson University	1
City University of New York	1	University of Oxford	1
Malmo Hogskola	1	University of Edinburgh	1
Technologico de Monterrey	1	University of Ottawa, Canada	1
Central Michigan University	1	Kent State University	1
University of Colorado at Denver	1	Temple University	1
Australian Catholic University	1	College of Health and Human Sciences	1

language. This proves that western researchers paid serious attention on mathematical language issues.

**RQ5: What is the Distribution of Authors' Affiliation in the Articles?**

[Table 7](#) shows the distribution of authors' affiliation pertaining to mathematical language article publications. Out of 26 institutions, two with the most number of article publications are Purdue University and University of Witwatersrand with three publications each. The publication frequency remains constant for 24 other institutions with one article publication each.

**Table 8.** Distribution of ‘what’, ‘who’ and ‘how’

Authors	Year	What tools/ approach?	Who involve?	How?
Medina Herrera, J. Castro Pérez and S. Juárez Ordóñez (2019)	2019	virtual environments, team working	University students	Test
C. Walkington, V. Clinton, and A. Sparks (2019)	2019	online problem-solving environment	Grade 6 <sup>th</sup> -12 <sup>th</sup>	Assignment
S.A. Schmitt, D.J. Purpura, and J.G. Elicker (2019)	2019	Vocabulary task, Mathematical language assessment, Executive Functioning (EF) task, behavioral assessment, children’s inhibitory control task and early mathematics skills task.	Preschool children	Assessments and Task
B.C. Hornburg, S.A. Schmitt, and D.J. Purpura (2018)	2018	Mathematical language and specific numeracy skills (e.g., cardinality, numeral comparison).	Preschool children	Assessments
P. Van Jaarsveld (2018)	2018	Students were required to write, in language suitable for teaching, a description of the procedure which led to a solution. On-line methods were used to obtain data	Trainee teacher	Writing task
K.N. McGinn, and J.L. Booth (2018)	2018	Self-explanation prompts (questions) and students’ self-explaining	Secondary school students	Assignments
D.J. Purpura, A. R. Napoli, E.A. Wehrspann, and Z. S. Gold (2016)	2016	Course of eight weeks, interventionists implemented a dialogic reading intervention focused on quantitative and spatial mathematical language.	Preschool children	Assessment
J. Caniglia, L. Borgerding, and M. Meadows (2017)	2017	Online tools (graphing calculator Desmos®’ <i>Polygraph</i> program) for transforming informal language into formal language similar to a Barrier Game.	Secondary school students	Online task
R. Barwell (2015)	2015	3 weeks lesson observe whole-class interaction and group interaction.	Grades 5–6	Classroom discussion
M. Serder, and A. Jakobsson (2016)	2016	Language games in the small groups of students discussed and collaboratively solved Programme for International Student Assessment (PISA) science test items.	Secondary school students	Assessment
R. Jaafar (2016)	2016	Several writing-to-learn activities (WTL) assignments with checklist (prompt questions), classroom discussion	College students	Assignments
J.M. Firmender, M. K. Gavin, and D.B. McCoach (2014)	2014	Instructional practices: engaging students in verbal communication in mathematics and encouraging the use of appropriate mathematical vocabulary	Kindergarten and Grades 1 and 2.	Assessments
J.R.O. O’Brian, Nocon and Sands (2010)	2010	Students and their teachers engaged in a collaborative dialogic inquiry process (data-driven dialogue) to co-construct meaning	Grade 5	Assessment
K. Piatek-Jimenez (2010)	2010	The course and individual task-based interviews	Undergraduate students	Courses and task
L.C. Rudd, M.C. Lambert, M. Satterwhite, and A. Zaier (2008)	2008	Observe classroom interactions using Noldus Observer XT software loaded on Hewlett-Packard iPAQ handheld computers employ the touch screen of a handheld computer to record event data	Kindergarten	Classroom interactions
R. Karsenty, A. Arcavi, and N. Hadas (2007)	2007	Ad-hoc strategies, mental calculations, idiosyncratic ideas, everyday rather than mathematical language, non-symbolic explanations, visual justifications and common-sense based reasoning	Secondary school students	Mathematical task
E. Warren (2006)	2006	The written tests in small groups consisted of a common structure same over the 3-year period. Each took up to 40 minutes to complete. Word problems involving Year 5 multiplication is more complicated	Elementary school students	Written test
S.R. De Lozano, and M. Cardenas (2002)	2002	Explicit instruction when the discourse is analyzed or formalized.	University students	Physics courses
R.C. Moore (1994)	1994	Observation of class, tutorial sessions with the students, and interviews with the professor and the students	University students	Mathematics courses
S. Pirie (1991)	1991	Classroom mathematical discourse discussed	Primary classroom pupils	Pupil-pupil discussion

**RQ6: What is the Distribution of ‘What’, ‘Who’ and ‘How’ Associated with Mathematical Language and Learning Approach in the Articles?**

The answers to ‘what’, ‘who’ and ‘how’ relating to mathematical language and learning approach are grouped into three categories which is summarized in Table 8 accordingly. First, the ‘what’ refers to what tool or approach applied by the scholars in their research e.g. online learning, questioning, reading, instructional practices or discussion. Second, the ‘who’ represents students’ level ranging from pre-school children, primary students, secondary students, university students or students in certain Grade. Finally, the ‘how’

refers to method to evaluate students’ progress or achievement e.g. test, task, assessment, course or even assignment. Detail explanations for the aforementioned three categories are as follow:

First category, the ‘what’ represents the approaches employed in the articles to encourage mathematical language usage among students. Out of 20 articles summarized, 3 current studies employed online learning environment (Caniglia et al., 2017; Medina Herrera et al., 2019; Walkington et al., 2019) and two studies utilized technology for data collection (Rudd et al., 2008; Van Jaarsveld, 2018). In the focus of current study, technology was not merely used by the researchers to collect data; but the students themselves applied



technology to improve knowledge, understanding and utilization of mathematical language in classroom learning.

The remaining 16 studies conducted typical approaches to encourage students' utilization and improve mathematical language in schools. Those include traditional strategy of proving the procedures (Van Jaarsveld, 2018), connecting mathematical language with numeracy skills (Hornburg et al., 2018), using vocabulary (Schmitt et al., 2019) and transitioning from informal to formal mathematical language (Caniglia et al., 2017). It shows that both typical and technological approaches have unique roles for students in mathematical language learning.

Second, the 'who' represents students' involved in the studies. The articles show mathematical language is embedded to each student level ranging from pre-school children (Firmender et al., 2014; Hornburg et al., 2018; Purpura et al., 2016; Rudd et al., 2008; Schmitt et al., 2019), primary school children (Barwell, 2015; Firmender et al., 2014; O' Brian, Nocon, & Sands, 2010; Pirie, 1991; Warren, 2006; Walkington et al., 2019), secondary school students (Caniglia et al., 2017; Karsenty, Arcavi, & Hadas, 2007; McGinn; & Booth, 2018; Serder & Jakobsson, 2016; Walkington et al., 2019) to higher level students (De Lozano & Cardenas, 2002; Jaafar, 2016; Medina Herrera et al., 2019; Moore, 1994; Piatek-Jimenez, 2010; Van Jaarsveld, 2018). The presented values include two studies involving two student levels such as Firmender et al. (2014) and Walkington et al. (2019). Whilst, six studies examined primary school children and higher-level students; only five studies investigated pre-school and secondary school students. This has shown that mathematical language emphasis was given more on primary and higher education levels. Therefore, future research pertaining to mathematical language learning should emphasize more on pre-school and secondary school students.

Third category, the 'how' represents the method examining students' mathematical language. It reveals that assessment (Firmender et al., 2014; Hornburg et al., 2018; O' Brian et al., 2010; Purpura et al., 2016; Schmitt et al., 2019; Serder & Jakobsson, 2015) was the highest number of methods used by previous researchers to evaluate students' mathematical language, followed by task (Caniglia et al., 2017; Karsenty et al., 2007; Piatek-Jimenez, 2010; Schmitt et al., 2019; Van Jaarsveld, 2018), courses (De Lozano & Cardenas, 2002; Moore, 1994; Piatek-Jimenez, 2010) and assignment (Jaafar, 2016; McGinn & Booth, 2018; Walkington et al., 2019), discussion (Barwell, 2015; Rudd et al., 2008; Pirie, 1991) and test (Medina Herrera et al., 2019; Warren, 2006). Assessment was the most selected method in the articles. It represents the emphasis given to the importance of students' active learning especially their engagement in mathematical language learning activities while promoting students' collaboration. Based on previous

studies, assessment was often applied to pre-school children; whereas task, assignment and test were frequently utilized for higher and elementary levels. Courses were popular for higher level students and discussion was mostly used for early years students.

Based on the results of the systematic review, three dimensions are the focus of previous studies in the context of learning. It involve the knowledge of the meaning of words (De Lozano & Cardenas, 2002; Hornburg et al., 2018; McGinn & Booth, 2018; Schmitt et al., 2019; Van Jaarsveld, 2018; Warren, 2006), the application of discourse, reading and writing of mathematical language in the classroom (Barwell, 2015; Caniglia et al., 2017; Firmender et al., 2014; Jaafar, 2016; Karsenty et al., 2007; Medina Herrera et al., 2019; Moore, 1994; O' Brian et al., 2010; Piatek-Jimenez, 2010; Pirie, 1991; Purpura et al., 2016; Rudd et al., 2008; Serder & Jakobsson, 2016), and the ability to understand word problems (Walkington et al., 2019). The biggest focus is on the application of discourse, reading and writing of mathematical language in the classroom such as verbal communication, collaborative dialogic inquiry process, task-based interviews, and discussion. This involve the efforts to explore and use words requiring response and explanation from students.

## DISCUSSION AND CONCLUSION

This systematic review examined studies related to mathematical language published in Scopus. Results, first, revealed that the related articles presented from 1991 until 2019 show an increasing number; which represents the rising interest in mathematical language learning (RQ1). Second, both Social Sciences and Mathematics areas are those who were interested the most in mathematical language studies (RQ2). Third, Purpura is the prominent scholar in mathematical language (RQ3). Fourth, United States has the most scientific works executed and published in mathematical language (RQ4). Fifth, the greatest number of article publications are Purdue University and University of Witwatersrand (RQ5). Sixth, the 'what' revealed that the biggest focus is on familiarity with pattern of discourse, reading and writing mathematics which involve students' communication. The 'who' revealed that mathematical language emphasis was given more on primary and higher education levels. The 'how' revealed that assessment was the most selected method in the articles (RQ6).

Concerning familiarity with pattern of discourse, reading and writing mathematical language, this dimension involve communication between teachers and students. Through communication, teachers and students benefits in several aspects. From teachers' perspectives, it involves verbal communication which helps teachers to explore different aspects of students' perception pertaining to specific words as well as to

detect words that are still unclear for students. Besides, the shifts in roles of teacher and learners in learning production also occurred (O' Brian et al., 2010). In performing the role, teachers need to be concerned with factors that inhibit students' comprehension involving the unspoken and shared understandings while providing opportunity for students to communicate in group; although at the beginning of the discussion, students fail to generate any idea about the expected learning (Pirie, 1991).

From students' perspective, it is important to provide students with the opportunity to utilize words so that they can learn to speak mathematically and build their own meanings. Building meaning requires combination of several words since knowledge of words alone does not assure that students will be able to communicate. Therefore, providing students with building meaning experience through communication should be guided with questions and subsequent feedback that will enhance their knowledge of mathematical language.

In certain situation, communication involve interaction with technology. Technology is mediation tool not only essential for students' online skill development but also to enhance communication. During the last decade, instructional approach was found to be an effective strategy for mathematical language learning while exposing students to utilize digital platform; although, only few studies utilized online learning environments as mathematical language approaches. There is an increasing interest on online learning which engages students with mathematical language and transforms informal mathematical language to more formal one. Therefore, researchers or educational leaders should also place high priority on developing mathematical language among students using digital platform.

However, some challenges may occur to embed mathematical language through communication among students specifically dealing with students' misconception. Two-way communication during group collaboration between student and peer may lead to misinterpretation without proper guidance. One of major problems for the listener occurs when the shared meanings are in some way erroneous. The misuse of mathematical language emerges when student creates personal vocabularies based on incorrect previous knowledge or experience which possibly misconstrued. Therefore, speaker who shares experiences using inadequate vocabulary could be guided by using other linguistic strategies such as appropriate used of written symbolism.

With respect to utilize of PRISMA procedures, identification phase is the process of building keywords whereby understanding of the words are required. For example, in finding articles related to mathematical language in the study, the researchers listed different

words but within the same category for students, informal languages and formal languages. Those three categories are: a) students, pupils and children; b) informal language, everyday language, spoken language and c) formal language, vocabulary, quantitative language and spatial language. This first phase refers to the researcher's attempt to explain the meaning of words in context of mathematical language learning.

Meanwhile, the second phase is screening, and third phase is eligibility. Both require researchers to search Scopus database to obtain relevant articles before examining and analyzing the words category used in the acquired articles. Then, the relevance of articles are evaluated before the inclusion phase. This process involves the researchers' efforts in exploring the words related to mathematical language learning.

Besides, with the guidance of PRISMA procedure, self-regulated learning in online platform becomes easier and faster for researchers. Table 8 indicates a big number of articles focus on mathematical language learning among primary school and higher education students. This fact can provide further analysis on the reason for greater emphasis given at this different level.

## RECOMMENDATIONS

Current review provides significant evidence from traditional perspective on mathematical language to recent focus for various levels of students regarding study approach and data collection procedure. Considering the limitations, findings of the study offer researchers, trainee teachers or other educational practitioners' initial guidance on strategies to remedy current mathematical language shortcomings for students of all levels and prevent future mathematical difficulties. This study also gives important directions for future research to continue identifying effective mathematical language approaches that can be implemented at every student level setting.

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