A Vector Voltage Modulator for a Dual Inverter with a Floating Bridge to Operate in Normal and Fault Tolerant Mode

V. Fernão Pires

Department of Electrical Engineering Sustain.RD, EST Setúbal, Instituto Politécnico Setúbal INESC-ID Lisboa Setúbal, Portugal vitor.pires@estsetubal.ips.pt

Armando Cordeiro

ADEEEA, LCEC ISEL, Instituto Politécnico de Lisboa INESC-ID Lisboa Lisboa, Portugal armando.cordeiro@isel.ipl.pt

Abstract—The dual inverter multilevel converter is characterized by a simple structure using two well-known threephase bridge inverters supplied by two independent DC sources. However, it can be supplied only by a single DC source if one of the bridges uses just a floating DC capacitor. In this case the control is more complex since it is also required to ensure the capacitor voltage regulation. Besides this, if a fault in one of the switches is also considered, the operation of the converter in fault operation mode becomes even more complex. This paper presents a vector voltage modulator that in addition to track the reference of the output AC voltages, also allows the capacitor voltage regulation of the floating bridge. The capability of this modulator to operate the converter in fault tolerant mode under an inverter open switch will also be analyzed. This analysis will allow to verify that the proposed control and modulation strategy presents inherent fault tolerant capability to open switch fault, since it does not require any fault detection algorithm or change in the control or modulation strategy. The capability and operation of the proposed vector voltage modulator will be verified through several simulation studies

Keywords— vector voltage modulator; dual inverter; floating bridge; open switch fault, fault tolerant

I. INTRODUCTION

Multilevel inverters are today an important solution for many applications. Indeed, they have been proposed for many applications, such as electric trains, high voltage transmission systems (HVDC), Flexible AC Transmission Systems FACTS, storage systems and renewable sources [1-5]. Initially, there was a first category of developed topologies, that have been designated as Diode Clamped Multilevel Inverter (NPC) [5,6], Flying Capacitors Multilevel Inverter [7,8] and Cascaded Hbridge Multilevel inverter [9,10]. These topologies have been applied to an important number of applications. Daniel Foito

Department of Electrical Engineering Sustain.RD, EST Setúbal, Instituto Politécnico Setúbal CTS/UNINOVA Setúbal, Portugal daniel.foito@estsetubal.ips.pt

> J. Fernando Silva Department of Electrical Engineering IST/University of Lisbon INESC-ID Lisboa Lisboa, Portugal fernando.alves@tecnico.ulisboa.pt

With the purpose to reduce the number of power semiconductors, introduce modularity or increase reliability, many new types of multilevel inverters have been proposed. One group of multilevel inverters that have been proposed and studied is the one associated to the modular topologies. These topologies use several well-known two-level voltage source inverters. One of these topologies is designated modular multilevel converter (MMC). The classical solution of this topology is based in the half-bridge inverter [11], but the MMC have also been used with the classical two level H-bridges [12]. However, for electrical drives this topology requires extra inductors and an important number of DC capacitors. Structures with classical two-level H-bridge but different from the MMC configurations were also proposed [13]. Other type of modular topologies that have been proposed uses classical two-level inverters but with four legs [14-17]. Multilevel topologies based in hybrid configurations employing single and three-phase two-level inverters were also proposed [18,19]. Another category of modular multilevel inverters with twolevel inverters uses only three-phase converters [20,21]. From these, the ones that have received more attention are the dual three-phase H-bridge voltage source multilevel inverters. Among the several topologies the designated dual inverter is the most studied [22-24]. This topology consists into two Hbridges voltage source inverters supplied by two independent voltage source inverters. Nevertheless, to avoid the usage of two floating DC power supplies, it was also proposed a topology in which a floating DC capacitor is used in one threephase-bridge [25,26]. However, its control is more complex since it is required to ensure the regulation of the capacitor voltage of the floating bridge.

In this paper a vector voltage modulator for the dual inverter with a floating capacitor bridge will be presented hereafter. Besides their capability to track the AC voltage

references this modulator will also ensure the voltage regulation of the capacitor associated to the floating bridge. Moreover, the capability to operate this converter in fault tolerant mode will be analyzed. Tests of this multilevel inverter with the proposed vector voltage modulator will also be presented.

II. DUAL INVERTER WITH A FLOATING BRIDGE

The multilevel dual inverter includes two H-bridge voltage source inverters supplied by two DC voltage sources. However, it is possible to avoid the second DC voltage source using a floating bridge, in which in the DC side of that bridge is replaced by a DC capacitor, as shown in Fig. 1.



Fig. 1. Topology of the dual inverter with a floating bridge

The dual inverter with the floating capacitor bridge can be modeled considering that the power semiconductors are ideal and associated to a variable γ that will be 1 or 0 respectively according to the *ON* or *OFF* state of the semiconductors. In agreement with this assumption, the output *AC* voltages of the multilevel inverter can be written by the following expression:

$$\begin{bmatrix} V_{o1} \\ V_{o2} \\ V_{o3} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix} \begin{bmatrix} V_{11} \\ V_{12} \\ V_{13} \end{bmatrix} - \frac{1}{3} \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix} \begin{bmatrix} V_{21} \\ V_{22} \\ V_{23} \end{bmatrix}$$
(1)

where

$$\begin{cases} V_{1j} = \gamma_{1j} V_{DC} \\ V_{2j} = \gamma_{2j} V_{C_0} \end{cases}$$
(2)

The previous three-phase AC voltages can be converted into a two phase orthogonal system through the application of the Clark-Concordia transformation. In this way, these voltages can also be written by the following new expression:

$$\begin{bmatrix} V_{o\alpha} \\ V_{o\beta} \end{bmatrix} = \begin{bmatrix} \sqrt{\frac{2}{3}} & -\frac{1}{\sqrt{6}} & -\frac{1}{\sqrt{6}} \\ 0 & \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{bmatrix} \begin{bmatrix} V_{11} \\ V_{12} \\ V_{13} \end{bmatrix} - \begin{bmatrix} \sqrt{\frac{2}{3}} & -\frac{1}{\sqrt{6}} & -\frac{1}{\sqrt{6}} \\ \end{bmatrix} \begin{bmatrix} V_{21} \\ V_{22} \\ V_{23} \end{bmatrix}$$
(3)

Analyzing the previous expression, considering all combinations of switches and assuming that the voltages of the DC source and capacitor are equal, it will be possible to see that in the alfa-beta reference plane 19 distinct vectors are obtained. However, if these voltages are different then the number of voltage vectors is increased. For example, considering that the voltage of the capacitor is half of the DC source, then 37 distinct vectors are obtained, as presented in Fig. 2. However, since the possible combinations of switches are higher (64), a higher number of voltage vectors also exist, although many of them are redundant. These redundant vectors are very important in this topology since they are used to ensure the voltage regulation of in the capacitor connected to the floating inverter, so that $V_{Co}=V_{DC}/2$.



Fig. 2. Voltage vectors in the alfa-beta plane considering that the voltage of of capacitor is half of the DC source

III. CONTROL OF THE DUAL INVERTER WITH A FLOATING CAPACITOR BRIDGE

With the purpose to ensure that the converter is able to control their AC voltages in a fast and robust way, it is proposed the use of a voltage sliding mode controller together with a vector voltage modulator. From (3) the strong relative degree of the AC voltages is zero [27]. This means the AC voltages are not state quantities. Furthermore, AC voltages being staircase waveforms cannot track sinusoidal references. Therefore, an auxiliary state variable is created using the AC voltages average value in a switching period. Moreover, the sliding surfaces will have to consider the switching period error averages expressed in (4). Thus, the development of the controller is achieved considering the average value of the error between the AC voltages $V_{0\alpha,\beta}$ in the alfa-beta coordinates and

their references $V_{0\alpha, \beta ref}$ during a switching period T(4).

$$\frac{1}{T} \int_{0}^{T} V_{0\alpha,\beta\,ref} \, dt - \frac{1}{T} \int_{0}^{T} V_{0\alpha,\beta} \, dt = e_{V0\alpha,\beta} = 0 \qquad (4)$$

From (4), the two sliding surfaces of the controller will be defined by:

$$\begin{cases} S(e_{\alpha},t) = \frac{k_{\alpha}}{T} \int_{0}^{T} (V_{0\alpha ref} - V_{0\alpha}) dt = 0\\ S(e_{\beta},t) = \frac{k_{\beta}}{T} \int_{0}^{T} (V_{0\beta ref} - V_{0\beta}) dt = 0 \end{cases}$$
(5)

Where k_{α} k_{β} are positive constants that impose the switching frequency and ensure the control response speed in accordance with the conditions defined by the sliding surfaces described by (5). The sliding mode stability condition $S(e_{\alpha\beta},t)\dot{S}(e_{\alpha\beta},t) < 0$ [27-29] is ensured by choosing a vector so that if $S(e_{\alpha\beta},t) > 0$, then the chosen vector will cause $\dot{S}(e_{\alpha\beta},t) < 0$. Otherwise, if $S(e_{\alpha\beta},t) < 0$, then the chosen vector must cause $\dot{S}(e_{\alpha\beta},t) > 0$. This will be achieved through a voltage vector modulator. Taking into account that there are two sliding surfaces, the modulator will have two inputs. Between there inputs and the sliding surfaces there will be two hysteretic comparators with five levels each. The number of levels was defined taking into consideration the amplitude of the voltage vectors according alfa and beta axis. In this way, the implementation of the vector voltage modulator can be realized by a look up table, as shown in Table I.

TABLE I. LOOKUP TABLE USED FOR THE VECTOR VOLTAGE MODULATOR

λοβΙλοα	-2	-1	0	1	2
-2	26,28	27,25	31	29,32	30,33
-1	23,24	22	31	34	35,36
0	20,21	19	0	1	2,3
1	17,18	16	7	4	5,6
2	13,15	12,14	7	8,10	9,11

The regulation to the value $V_{DC}/2$ of the capacitor voltage associated to the floating bridge is ensured by the redundant voltage vectors. An example can be seen for the vector 4. Associated to this vector there are two more redundant vectors (the 3 vectors can be designated from 4A to 4C). Each vector presents different semiconductor switching combinations, although the amplitude in accordance with the alfa and beta axis is the same as shown in Table II. The choice of the redundant vector must also take into consideration the direction of the *AC* currents. For this, eight sectors are considered as shown in Fig. 3.

 TABLE II.
 REDUNDANT VOLTAGE VECTORS ASSOCIATED TO VECTOR 4

Vector	S ₁₁	S ₁₂	S ₁₃	S ₂₁	S ₂₂	S ₂₃	Voa	V _o β
4A	0	0	0	0	0	1	0,20 V _{DC}	$0,35 V_{DC}$
4B	1	1	0	1	1	1	0,20 V _{DC}	0,35 V _{DC}
4C	1	1	1	0	0	1	0,20 V _{DC}	0,35 V _{DC}



Fig. 3. AC currents and correspondet sectors

Another aspect is the operation of the system when there is an open switch fault. In this situation automatically several voltage vectors are not available. For example, let's consider that there is a fault in the switch S_{11} . In this case the voltage vectors 2, 3, 5, 6, 8, 9, 10, 11, 29, 30, 32, 33, 35 and 36 are not available anymore (Fig. 4). However, if for example the vector 6 is chosen, in reality, due to the fault the vector that will be applied will be vector 4 (the vector that has the same switching combination except the S_{11} that instead be 1 will be 0). However, this vector still maintains in the same quadrant of the chosen vector, although with less amplitude. So, if the required voltage reference is not at their maximum value, then the system will be able to operate in fault tolerant mode. It should be noticed that this change is automatic, requiring no fault detection algorithm. So, the proposed system inherently provides fault tolerance capability, despite not operating at its maximum voltage.



Fig. 4. Voltage vectors in the alfa-beta plane considering an open switch fault $({\rm S}_{11})$

The proposed full control strategy for the dual inverter with the floating capacitor can be seen in Fig. 5. As shown by this figure, for the space vector modulator there are seven inputs since it depends of the sliding mode controller, capacitor voltage and AC current sectors.



Fig. 5. Full control system adopted for the dual inverter with the floating capacitor

IV. SIMULATION TESTS

Some simulation tests were performed using the *Matlab/Simulink* program. A 600 V DC voltage source was adopted and for the floating capacitor voltage was regulated to 300 V. Through Fig. 6 it is possible to see the time behavior of the output voltage of the dual inverter and ac currents. From this figure it is possible to confirm the multilevel operation of the dual inverter since the ac voltage of this converter presents 9 voltage levels. From Fig. 6 b) it is possible to confirm that the ac currents of the converter currents are almost sinusoidal. The capability of the controller and modulator to regulate the voltage of the floating capacitor can also be seen in Fig. 6 c).





Fig. 6. Waveforms of the a) AC output voltage, b) AC output currents and c) of the DC and floating capacitor voltages in heltly condition

The operation of the converter under an open switch fault was also tested. The results of a test in which the switch S_{21} (associated to the floating bridge) is in open fault can be seen in Figure 7. Through this figure it is possible to see that even in the situation of a fault in the floating bridge the AC currents still maintain with a low *THD* (although somewhat increased compared to the healthy condition value). In this situation the operation of the converter is practically not affected. The waveform of the voltage in the floating capacitor is shown in Fig. 7 c). From this figure is possible to see that higher ripple appears in this waveform. However, the voltage regulation is only slightly affected.





Fig. 7. Waveforms of the a) AC output voltage, b) AC output currents and c) of the DC and floating capacitor voltages for an open fault in switch S_{2l} .

A new test with the converter under an open switch fault, but in this case for the switch S_{12} that is associated with the other inverter (bridge connected to the *DC* voltage source) was also performed. The obtained results of this open fault can be seen in Figure 8. Through this figure it is possible to see that in this case the *AC* currents are much more affected, although the effect cannot be considered catastrophic. Regarding the capacitor voltage is also possible to verify that it is much more affected. Indeed, in this case the ripple is high (around 33%) and specially associated to under voltages that will affect the *AC* currents.



Fig. 8. Waveforms of the a) AC output currents and b) of the DC and floating capacitor voltages for an open fault in switch S_{12} .

An identical test in which the converter under an open switch fault for the switch S_{12} (that is associated to the bridge connected to the *DC* voltage source) but for a reduced output *AC* voltage (reduced power) was performed. Fig. 9 presents the obtained results for the *AC* output currents and *DC* and floating capacitor voltages. From this figure it is possible to conclude that with the reduction of the *AC* voltage the currents are practically not affected. The same happens for the capacitor voltage, since compared with the previous test the ripple presents an important reduction.



Fig. 9. Waveforms of the a) AC output currents and b) of the DC and floating capacitor voltages for an open fault in switch S_{12} .

An important factor that should be highlighted is that all the tests were realized without changing the control or modulation strategy. Thus, this indicates that the system shows fault tolerance capability for open switch fault with some output power limitations without requiring any fault detection algorithm or change in the control or modulation strategy.

V. CONCLUSIONS

This work presented a sliding mode vector control system for a voltage modulator of a dual inverter with a floating capacitor bridge. The controller was designed taking into consideration a sliding mode approach and sliding mode stablity. Associated to this controller, a vector voltage modulator was obtained. The design of the modulator took into consideration the regulation of the floating capacitor voltage. Another aspect that was studied was the capability of the system to operate under open switch faults. From this study it was possible to verify that the proposed control and modulation strategy presents inherent fault tolerant capability to open switch faults, as it does not require any fault detection algorithm or any change in the control or modulation strategy. With the purpose to verify the capability and characteristics of the proposed control system, several simulations were carried out. The obtained results showed the capability to control the converter, was well as, to maintain their operation with a fault in one of the switches.

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