



Acoustic Birefringence and Poisson's Ratio Determined by Ultrasound: Tools to Follow-Up Deformation by Cold Rolling and Recrystallization

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Poisson's ratio and birefringence, both measured by ultrasound, are used to follow the evolution of the anisotropy in ASTM A-36 steel plates cold-rolled between 5 and 50% deformation, and then subjected to recrystallization at 900 and 1000 °C. Times of flight of longitudinal and shear waves along the thickness of the plates were measured. As orthotropy increases, both birefringence and the difference between Poisson's ratios measured using a shear wave polarized along the length and another wave polarized along the width of the plate, are linearly related to the degree of deformation and cold-rolled hardness. In addition, the ultrasonic methods used clearly detected the complex changes in anisotropy produced by the austenization and recrystallization heat treatments. Thus, Birefringence or Poisson's ratio, measured by ultrasound, can be used to follow-up nondestructively changes in the anisotropy of rolled plates as a function of both, degree of deformation and recrystallization heat treatment.

Keywords: Ultrasound, Poisson's Ratio, Acoustic Birefringence, Cold Working, Recrystallization

1. Introduction

The use of ultrasound to measure second order elastic constants in multiphase or polycrystalline materials is based on the Christoffel equation, which relates them with the phase velocity of three non-dispersive ultrasonic waves with mutually perpendicular polarization directions (i.e., of displacement of the medium's particles), propagating in specified directions¹. This equation comes from considering that the passage of a wave through a body generates small elastic stresses and deformations, setting up a dynamic equilibrium described by the equations of motion, wherefrom the equation that governs wave propagation in a homogeneous elastic medium is obtained by considering the generalized form of Hooke's law. The Christoffel equation is finally obtained by assuming the propagation of harmonic elastic waves as a solution for the equation of motion:

$$(C_{ijkl} n_j n_k - \rho v^2 \delta_{il}) u_l = 0 \quad (1)$$

where C_{ijkl} are the second order elastic constants; (n_1, n_2, n_3) , the direction cosines of the normal to the wavefront, indicating, therefore, the direction of propagation of the wave; u_l is the displacement or polarization vector; ρ , the density of the medium, and δ_{il} , the Kronecker delta. The equation corresponds to three homogeneous equations from which, for every propagation direction considered, three different velocity values arise from the cubic equation in v^2 , obtained

by making the determinant of the coefficient matrix equal to zero. These three velocities correspond to three waves with mutually perpendicular polarization vectors.

The solution to the inverse problem of determining the elastic constants from experimental measurements of wave velocity is well established, and the measuring protocols are clearly defined in the literature¹. Most materials used in engineering either have isotropic symmetry, with two independent elastic constants, or orthotropic symmetry, with nine independent constants. The following relations are obtained for the isotropic case, where $C_{11} = C_{22} = C_{33}$, $C_{44} = C_{55} = C_{66} = \frac{1}{2}(C_{11} - C_{12})$:

$$\begin{aligned} C_{11} &= \rho v_{ii}^2 \equiv \rho v_L^2; & C_{44} &= \rho v_{ij}^2 \equiv \rho v_T^2; & C_{12} &= \rho (v_L^2 - 2v_T^2); \end{aligned} \quad (2)$$

with v_{ii} , the velocity of the longitudinal wave (longitudinally polarized to its direction of propagation i), and v_{ij} , with $i \neq j$, the velocity of the shear wave (polarized in the direction j , transverse to its direction of propagation i). Thus, the values of the elastic constants may be obtained just by measuring the velocities of a longitudinal wave and a shear wave in any direction of propagation. From the theory of elasticity², which for the isotropic case relates the elastic stiffness constants with Young's and shear moduli, and with Poisson's ratio ν , these parameters may be expressed in terms of the velocities

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of the longitudinal and shear waves³, as Equation (3) shows for Poisson's ratio:

$$\nu = \frac{(v_L/v_T)^2 - 2}{2[(v_L/v_T)^2 - 1]} \quad (3)$$

Since in an isotropic material v_L and v_T are independent of their directions of propagation and polarization, access to any one plane is enough to calculate its elastic properties.

In order to obtain the independent constants of an orthotropic material, nine measurements are required. These are the velocities of longitudinal and shear waves in the three symmetry directions of the material, allowing to obtain C_{11} , C_{22} , C_{33} , C_{44} , C_{55} and C_{66} ; and the velocities of either quasi-longitudinal or quasi-shear waves in the three symmetry planes, but at an angle with respect to the axes, obtaining C_{12} , C_{13} and C_{23} . Now, using only normal incidence for propagation along the z-axis (Figure 1), the following relations are obtained:

$$C_{33} = \rho v_{33}^2; \quad C_{44} = \rho v_{32}^2; \quad C_{55} = \rho v_{31}^2 \quad (4)$$

That is, although to obtain all of the constants of an orthotropic material, three perpendicular planes must necessarily be accessed, variations in the degree of orthotropy may be studied by having access to only one plane and measuring the velocities of the shear waves v_{31} and v_{32} , thus determining the difference between the elastic constants C_{44} and C_{55} . This difference gives rise to the acoustic birefringence B , which is quantified as the ratio of the difference of velocities v_{31} and v_{32} to their average, as Equation 5 shows, so that for a perfectly isotropic material, $B = 0$:

$$B = \frac{v_{31} - v_{32}}{\frac{1}{2}(v_{31} + v_{32})} = \frac{t_{32} - t_{31}}{\frac{1}{2}(t_{32} + t_{31})} \quad (5)$$

where t_{ij} corresponds to the times of flight of the waves along the z-axis. The equation shows that birefringence can be quantified without measuring the distance, usually the thickness as in the case of rolled metal plates, of the material through which the wave travels, because the ratio of the velocities of two waves traveling the same distance becomes a ratio of the times of flight of those waves. Therefore, on the one hand, an important source of error in measurement is omitted, and on the other hand, it allows the study to be made under conditions in which it is difficult or impossible to measure the thickness⁴⁻⁷.

Notice that Equation (3) indicates that the thickness can also be omitted to calculate Poisson's ratio. This equation is valid for an isotropic material; for an orthotropic material, the difference between the elastic constants C_{44} and C_{55} should generate two values for Poisson's ratio, depending on the polarization direction of the shear wave, that is:

$$\nu_{31} = \frac{(v_{33}/v_{31})^2 - 2}{2[(v_{33}/v_{31})^2 - 1]} = \frac{(t_{31}/t_{33})^2 - 2}{2[(t_{31}/t_{33})^2 - 1]} \quad (6)$$

$$\nu_{32} = \frac{(v_{33}/v_{32})^2 - 2}{2[(v_{33}/v_{32})^2 - 1]} = \frac{(t_{32}/t_{33})^2 - 2}{2[(t_{32}/t_{33})^2 - 1]} \quad (7)$$

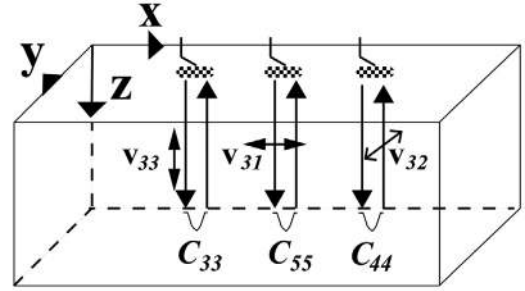


Figure 1. Waves for the determination of elastic constants, with longitudinal and shear waves propagating along z. The longitudinal wave is polarized along the z-axis, while the shear waves of velocities v_{31} and v_{32} are polarized along the x and y axes, respectively.

Therefore, it should be possible to relate Poisson's ratio with the effect of deformation processes and post deformation heat treatments on the anisotropy, without specifying the thickness of the material under study. There is no information in the literature with respect to the use of Poisson's ratio for this purpose. The objective of this paper is, then, to study the feasibility of relating Poisson's ratio and acoustic birefringence measured by ultrasound with the degree of cold-working and the temperature and time of austenization after cold deformation of an structural steel. For this research, the traditional contact ultrasonic technique was used (as Figure 1 suggests), which readily lends itself to some industrial use, though it might be a limitation when contact between transducers and the part becomes an issue. However, the method is suitable for any non-contact technique, such as Electromagnetic Acoustic Transducer (EMAT) and Laser Ultrasonic (LUS), as long as longitudinal and shear waves may be induced in the part.

2. Experimental Procedure

Seven samples measuring 505 mm x 54 mm x 15 mm were cut for cold rolling from a hot-rolled ASTM A-36 steel plate. Their surfaces were adequately prepared to readily accommodate the transducers and propagate the ultrasonic waves. Before rolling each sample, 21 points were identified along the central line of the top surface, separated by 10 mm each. The thickness at every point was measured with a micrometer. Then, the seven samples were rolled each at a different degree of deformation. Afterwards, the seven rolled samples were each cut into four equal parts, all of which were heat-treated in a 20-kW Lindberg model 56667-E furnace,

previously heated at the required temperature as shown in Table 1. Thus, four heat treatments were performed for each degree of deformation.

Table 1. Time and temperature for heat treatment of rolled samples.

Temp. °C	900	900	1000	1000
Time, min.	15	30	15	30

To determine birefringence and Poisson’s ratio, normal incidence from longitudinal and shear contact piezoelectric transducers and pulse-echo technique were used. Ultrasonic tests were carried out before and after each deformation and after each heat treatment in the 21 locations corresponding to the marked points. The waves propagated from the top surface (xy plane in Figure 1) and along the thickness of the samples (z-axis in Figure 1). Naturally, longitudinal waves were always polarized along the z-axis. On the other hand, by alternatively placing the shear wave transducer on the surface with its polarization direction perpendicular to and along the rolling direction, shear waves polarized along the principal axes (x and y axes in Figure 1) of the samples were propagated. The ultrasonic system consisted of a Panametrics 5077PR pulser-receiver, on pulse-echo mode; 5-MHz, 11 mm in diameter Panametrics contact transducers for longitudinal and shear waves; and an HS805 TiePie oscilloscope emulator plate to obtain and store the echoes for later processing.

To relate results to standard techniques, metallographic samples were prepared by common procedures, and Rockwell B hardness was measured before and after deforming the samples, and after the heat treatments. Five measures were taken on each sample for averaging.

3. Results and Discussion

3.1 Effect of cold rolling on wave velocities

After obtaining and storing the ultrasonic signals, the times of flight of the waves were measured, quantified as the difference between the times of the maxima of the first two echoes.

Table 2 shows the propagation velocity values before and after rolling the samples; each value corresponds to the average of the measurements for each of the 21 points marked along the samples before deformation.

The longitudinal velocity v_{33} , whose polarization vector is perpendicular to the rolling direction, has a decreasing trend as the degree of deformation increases beyond 17.9%, reaching, at 42%, a maximum difference of 46 m/s (0.78%) compared to its original average value without cold deformation. On the other hand, it is observed that for the original non-cold rolled sample, the difference between the average values of velocities of the perpendicularly polarized shear waves, v_{31} and v_{32} , is barely 3 m/s. From Equation 4, this gives rise to a difference of a mere 0.18% between C_{44} and C_{55} , rendering the sample nearly isotropic. As cold deformation increases, the shear wave velocity v_{31} , polarized parallel to the rolling direction, increases constantly from its original average value, so that the velocity is 2 m/s higher (0.06%), at $\epsilon = 5.4\%$ and 28 m/s higher (0.86%) at $\epsilon = 49.7\%$; meanwhile, v_{32} (perpendicularly polarized to the rolling direction) decreases between 5 and 86 m/s (0.15% and 2.65%), relative to its respective original value. Following Equation 4, this implies that C_{55} increases and C_{44} decreases because of the deformation, while the effect on C_{33} is more complex, although it clearly tends to decrease.

3.2 Effect of cold rolling on poisson’s ratio and birefringence

According to Equations 5, 6 and 7, the changes in the elastic constants modify B and ν . To illustrate the effect of cold rolling, Figure 2a compares Poisson’s ratios at the 21 locations of a sample before and after cold rolled to 12.3% deformation, and Figure 2b does the same for the sample rolled to 42%. On the non-rolled samples of Figure 2, the average values of Poisson’s ratios determined from Equations 6 and 7 are $\bar{\nu}_{31} = 0.2817$ and $\bar{\nu}_{32} = 0.2810$, respectively. Figure 2 also shows that the individual values of ν_{31} and ν_{32} before deformation slightly fluctuate around their respective mean values, with a maximum difference between ν_{31} and ν_{32} of 0.0019 at locations 4 and 10. On the other hand, when the samples are rolled, fluctuations around the respective averages increase somehow, but more importantly, as the deformation increases, ν_{31} decreases while ν_{32} increases at every location. Hence, the difference between the mean values for the sample rolled to 12.3% grows to $\bar{\nu}_{31} - \bar{\nu}_{32} = 0.0042$, while for the one rolled to 42%, climbs to $\bar{\nu}_{31} - \bar{\nu}_{32} = 0.0168$, that is, more than an order of magnitude greater than $\bar{\nu}_{31} - \bar{\nu}_{32} = -0.0007$, the difference between the mean values for the non-rolled samples. The effect of cold deformation, from 0 to 49.7%,

Table 2. Averages of the wave velocities and hardness in the rolled samples.

Sample	Original	1	2	3	4	5	6	7
Deformation ϵ (%)	0.0	5.4	12.3	17.9	21.2	30.8	42.0	49.7
v_{33} (m/s)	5882	5905	5884	5890	5866	5843	5836	5859
v_{31} (m/s)	3243	3245	3247	3251	3254	3250	3261	3271
v_{32} (m/s)	3246	3241	3225	3215	3206	3194	3174	3160
H (HRB)	82	90	92	93	94	95	98	101

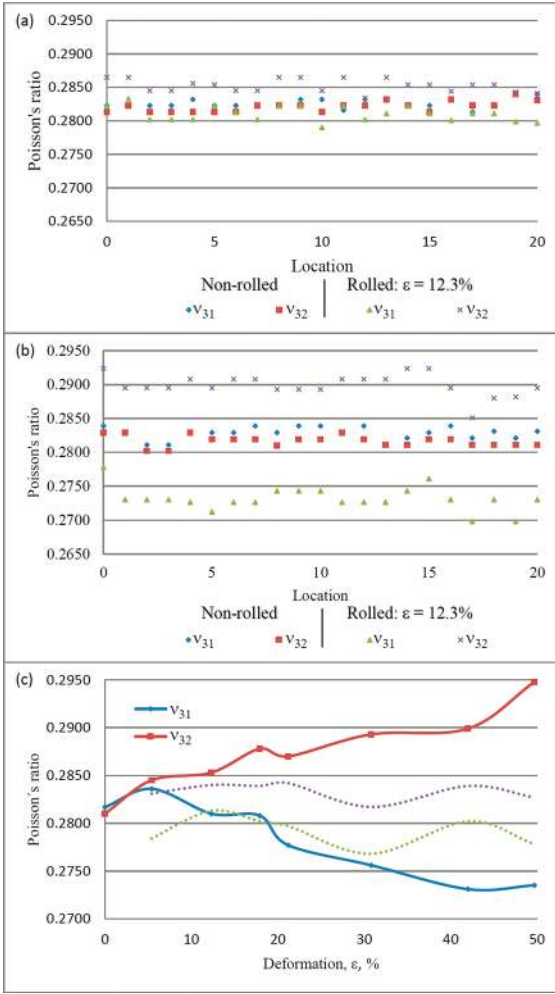


Figure 2. Poisson's ratios measured at 21 locations on samples; (a) non-cold rolled and rolled to $\epsilon = 12.3\%$; (b) non-cold rolled and rolled to $\epsilon = 42\%$. (c) Average of Poisson's ratios ν_{31} and ν_{32} versus cold deformation (dotted lines indicate the range of fluctuation of values of ν_{31} and ν_{32} before rolling).

on the average values of ν_{31} and ν_{32} is shown in Figure 2c. For comparison, the dotted lines also shown indicate the range of fluctuation of the individual values of ν_{31} and ν_{32} along the 21 points measured on each of the seven samples before rolling.

Figure 3 summarizes the effect of cold rolling on the difference between average values of Poisson's ratios (that is, the difference between the curves of Figure 2c), and on birefringence. It is seen that $\Delta\nu = (\bar{\nu}_{31} - \bar{\nu}_{32})$ increases linearly with deformation from -0.0007 to 0.0213. Likewise, the average birefringence B , which is barely -0.0011 in the hot rolled condition, reflecting its nearly isotropic behavior, increases linearly with cold deformation to 0.0346. Equations (8) and (9) give the respective relations:

$$\Delta\nu = (\bar{\nu}_{31} - \bar{\nu}_{32}) = 0.0004\epsilon - 0.0009 \quad r^2 = 0.9932 \quad (8)$$

$$B = 0.0007\epsilon - 0.0017 \quad r^2 = 0.9871 \quad (9)$$

Thus, it is possible to establish a linear relation between the difference of Poisson's ratios and birefringence. Such relation is given by:

$$\Delta\nu = (\bar{\nu}_{31} - \bar{\nu}_{32}) = 0.6215B + 0.0004 \quad r^2 = 0.9761 \quad (10)$$

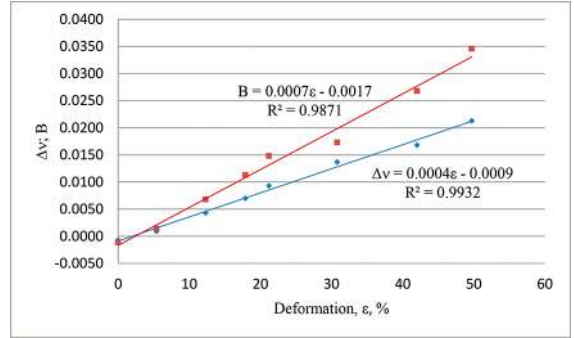


Figure 3. Effect of deformation on birefringence B and on the difference between Poisson's ratios $\Delta\nu = (\bar{\nu}_{31} - \bar{\nu}_{32})$.

3.2.1 Relationship to hardness

Average values of hardness for the samples are shown in Table 2. The average value for the original hot rolled plate was 82 (HRB). As expected, hardness increases with cold rolling, and from the data in Table 2 is seen that it does it linearly as deformation increases between 5.4 and 49.7%. The resultant relation is given by Equation (11), where, H stands for hardness.

$$H = 0.2302\epsilon + 88.8 \quad r^2 = 0.978 \quad (11)$$

As a consequence, both birefringence and the difference of Poisson's ratios are linearly related to hardness. The respective relations are given by:

$$B = 0.0031H - 0.2739 \quad r^2 = 0.9961 \quad (12)$$

$$\Delta\nu = (\bar{\nu}_{31} - \bar{\nu}_{32}) = 0.0019H - 0.1658 \quad r^2 = 0.9649 \quad (13)$$

Therefore, it is possible to estimate precisely the level of deformation as well as the hardness achieved by rolling from measurements of the time of flight of shear waves for birefringence, and of longitudinal and shear waves for Poisson's ratios.

3.3 Effect of heat treatment on poisson's ratio and birefringence

For high levels of deformation, Figures 4 and 5 show that the heat treatments to which the rolled samples were subjected tend to return the values of Poisson's ratio to the original values, which are shown by the dotted lines that indicate the range of fluctuation of the ratios, both ν_{31} and ν_{32} , considering the 21 points measured on each of the seven samples before rolling. However, at 900 °C (Figures 4a and 4b), it is seen that regardless of treatment time, between 17.9% and 30.8% deformations, the ν_{31} curves show a maximum, shifting even more from the original values. This implies that the material behaves more anisotropically after the heat treatment within that deformation range.

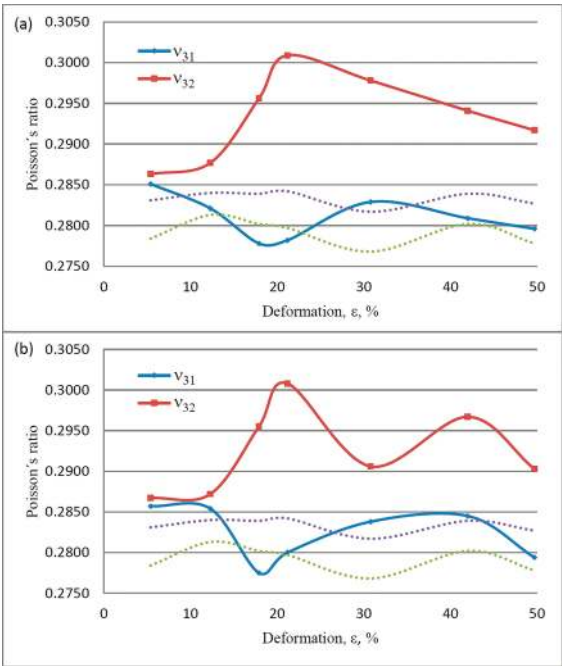


Figure 4. Effect of heat treatment on Poisson's ratio ν_{31} and ν_{32} in rolled samples. (a) 900 °C, 15 min.; (b) 900 °C, 30 min. (Dotted lines indicate the range of fluctuation of values of ν_{31} and ν_{32} before rolling).

The tests carried out at 1000 °C (Figures 5a and 5b) show a behavior similar to the previous one, but only for a time of 15 minutes of treatment (Figure 5a). It is also seen that for deformations lower than 17.9% and greater than 30.8%, ν_{31} and ν_{32} are practically identical.

Therefore, only for the treatment at 1000 °C for 30 minutes (Figure 5b), the samples, regardless of the degree of deformation to which they were subjected, return to a practically isotropic behavior.

Those results may be explained as follows: it would be expected that a cold-deformed ASTM A-36 steel sample, when heated above the upper critical temperature curve,

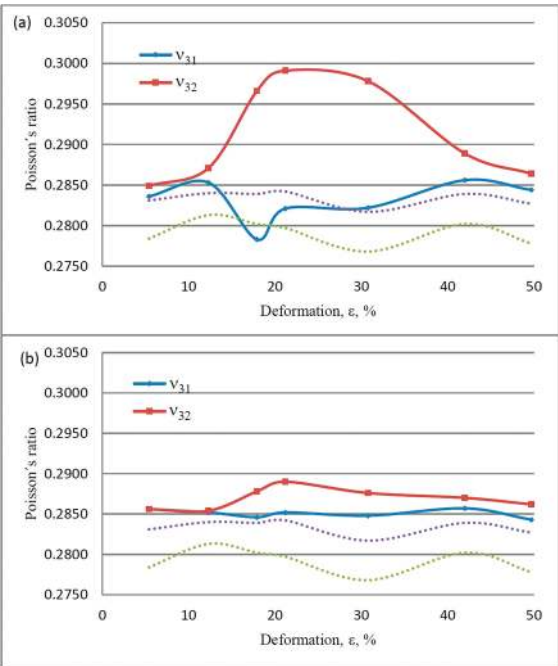


Figure 5. Effect of heat treatment on Poisson's ratio ν_{31} and ν_{32} in rolled samples. (a) 1000 °C, 15 min.; (b) 1000 °C, 30 min. (Dotted lines indicate the range of fluctuation of the individual values of ν_{31} and ν_{32} among the 21 points measured on each sample before rolling).

would recrystallize below curve A_1 , followed by a partial transformation above curve A_1 and a total transformation above curve A_3 . Then, on cooling the $\gamma \rightarrow \alpha$ and $\gamma \rightarrow \alpha +$ cementite transformations would occur. The onset of recrystallization and the recrystallized fraction depend on both the degree of deformation applied and the time at the recrystallization temperature. For low levels of deformation, the $\alpha \rightarrow \gamma \rightarrow \alpha$ transformations could take place without prior recrystallization. If so is the case, the deformed α structure (α_{DEF}) can be expected to be transformed into deformed γ (γ_{DEF}) upon heat treatment, and then on cooling it would transform back into α_{DEF} .

Then, graphs a and b of Figure 4 suggest that up to 21.2% deformation, at 900 °C the $\alpha_{DEF} \rightarrow \gamma_{DEF} \rightarrow \alpha_{DEF}$ transformation cycle may take place, whether the heat treatment lasts 15 or 30 minutes.

At 1000 °C, on the other hand, the $\alpha_{DEF} \rightarrow \gamma_{DEF} \rightarrow \alpha_{DEF}$ transformation cycle is valid only for 15 minutes of heat treatment. Apparently, as time at 1000 °C is increased all the γ grains would adopt a gray texture, giving rise to α grains without a preferred orientation. The same would happen with 30.8% deformation at the two heat treatment temperatures. The analysis suggests that for 42% deformation at 900 °C (Figures 4a and 4b) the $\alpha_{DEF} \rightarrow \gamma_{DEF} \rightarrow \alpha_{DEF}$ cycle still takes place in a time of 15 minutes, however, at a temperature of 1000 °C (Figures 5a and 5b) there would be recrystallization prior to the $\alpha \rightarrow \gamma$ transformation. A 49.70% deformation is

apparently sufficient to produce some degree of recrystallization prior to the $\alpha \rightarrow \gamma$ transformation, because it is seen that the values tend toward those of the isotropic material. This practically 100% isotropic symmetry is achieved after 30 minutes at 1000 °C for all degrees of deformation, as shown in Figure 5b, where Poisson's ratios tend to 0.286, a value slightly higher than the range of the original samples from the hot rolled material.

As could be expected, the behavior of birefringence to the heat treatments is similar to that of Poisson's ratio.

3.4 Hardness and metallographic analysis

The micrographs shown in this section were taken at a magnification of 500X. Figure 6a belongs to a material in its original state, showing an equiaxial ferrite plus pearlite microstructure, typical of an ASTM A-36 steel. Figure 6b shows a micrograph of a rolled sample at a medium degree of deformation, where, as expected, no significant change is seen in the orientation of the grains. As is well known, more sophisticated techniques, such as DRX and EBDS, are required to detect such changes. However, the results obtained by ultrasound clearly show that it is possible, in a nondestructive mode, to detect the increased orthotropy at even the lowest degrees of deformation.

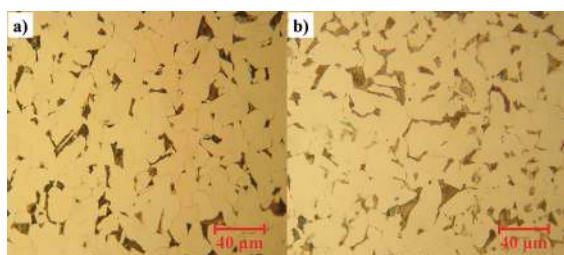


Figure 6. a) Material in its original state; b) sample rolled to 21.2%.

Figures 7a and 7b show that after the heat treatments there is a slight difference in ferritic grain size compared to the original sample (Figure 6a), and that in the sample treated at higher temperature there is the presence of colonies of thicker pearlite.

The hardness of all the heat-treated samples fluctuated randomly between 77 and 82 (HRB), with no relation to the temperature or time of treatment, showing a decrease of the hardness down to values lower in most cases than the average value obtained for the original plate.

The previous hardness results and the metallographic analysis show that those procedures do not allow following up the process of modification of anisotropy caused by the heat treatment applied to the cold-rolled samples. In contrast, the determination of birefringence or Poisson's ratio by ultrasonic methods allows these modifications to be distinguished precisely.

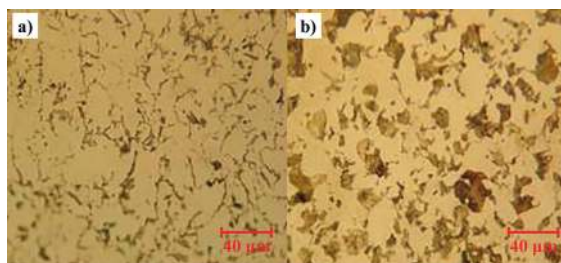


Figure 7. a) Sample rolled to 21.2%, and annealed at 900 °C, 30 min.; b) sample rolled to 49.7%, and annealed at 1000 °C, 30 min.

4. Conclusions

The main conclusions obtained from this work are the following:

- The mapping of Poisson's ratio on the ASTM A-36 steel showed it to be nearly isotropic.
- It was shown experimentally that the effect of deformation by cold rolling on wave velocity, birefringence, and Poisson's ratio is to shift the obtained data from their initial values in proportion to the degree of deformation applied.
- The above means that both birefringence and Poisson's ratio make it possible to determine the degree of cold deformation and the hardness of the materials studied by means of simple linear relationships.
- The effect of the heat treatment in the austenitic field on cold-rolled samples depends on the degree of deformation and on the temperature and time of treatment. Medium levels of deformation, low temperature and shorter austenization time tend to shift the values of birefringence and Poisson's ratio from the original values of the material before the deformation; high levels of deformation, high temperatures, and longer austenization tend to return those values to the original ones of the material before its deformation.

It can be concluded, therefore, that even though the times of flight of the waves measured in different positions show a random dispersion, it is feasible to use Poisson's ratio as well as birefringence, both measured by ultrasound, as a simple and nondestructive method to follow up the anisotropy changes in rolled plates due to cold rolling and to post rolling heat treatments.

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