Adaptive Synergies for the Design and Control of the Pisa/IIT SoftHand

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Abstract-In this paper we introduce the Pisa/IIT SoftHand, a novel robot hand prototype designed with the purpose of being robust and easy to control as an industrial gripper, while exhibiting high grasping versatility and an aspect similar to that of the human hand. In the paper we briefly review the main theoretical tools used to enable such simplification, i.e. the neuroscience-based notion of soft synergies. A discussion of several possible actuation schemes shows that a straightforward implementation of the soft synergy idea in an effective design is not trivial. The approach proposed in this paper, called *adaptive* synergy, rests on ideas coming from underactuated hand design. A synthesis method to realize a desired set of soft synergies through the principled design of adaptive synergy is discussed. This approach leads to the design of hands accommodating in principle an arbitrary number of soft synergies, as demonstrated in grasping and manipulation simulations and experiments with a prototype. As a particular instance of application of the synthesis method of adaptive synergies, the Pisa/IIT SoftHand is described in detail. The hand has 19 joints, but only uses one actuator to activate its adaptive synergy. Of particular relevance in its design is the very soft and safe, yet powerful and extremely robust structure, obtained through the use of innovative articulations and ligaments replacing conventional joint design. The design and implementation of the prototype hand are shown and its effectiveness demonstrated through grasping experiments, reported also in the multimedia extension 1.

I. INTRODUCTION

To get close to the richness and complexity of the sensory and motor functionalities of a human hand with a robust and economically reasonable robotic device remains one of the hardest challenges in robotics.

In this paper, we propose an integrated approach of mechanics and control co-design, which aims to achieve better results — in terms of performance and design simplicity — by embedding part of the control intelligence in the physical structure of the system itself. Neuroscientific studies, as for example [Santello et al., 1998], [Weiss and Flanders, 2004] and [Latash et al., 2005], suggest that the extremely high complexity of the the human hand sensori-motor system is tamed through a stratified set of motor primitives, or *synergies*, which render it manageable for the higher level cognitive functions as an organized and ordered ensemble. These are embodied at different levels, from the physical grouping of multiarticular muscles and tendons, to reflex arcs, up to the cerebellar and cortical synaptic circuitry. By virtue of this organization, particular patterns of neuro-muscular



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Fig. 1. Skeleton of the Pisa/IIT SoftHand advanced anthropomorphic hand prototype implementing one adaptive synergy. The prototype dimensions are comparable to those of the hand of an adult human.

activities form a base set, analogous to the concept of *basis* in theory of vector spaces [Easton, 1972]: a minimal number of linearly independent elements that under specific operations generate all members of a given set, in this case, the set of all movements. Such basis are sometimes referred to as the space of *postural synergies*, or the eigengrasp space [Ciocarlie et al., 2007].

Recently, different approaches in robotics tried to take advantage from the idea of synergies, aiming to reproduce a similar "coordinated and ordered ensemble" of human hand motions. To transfer part of the embodied intelligence, typical of the human hand, into a robotic counterpart, a promising possibility is the re-creation of synergy patterns as a feature of the mechatronic hand system. This approach has already been tried in recent literature (see next section for a short review), although a purely kinematic model of synergies leads to inconsistent grasp force distribution models. To solve such problems, the concept of *soft synergies* was introduced [Gabiccini et al., 2011], [Bicchi et al., 2011], which provides a model of how synergies may generate and control the internal forces needed to hold an object.

In this paper, partly based on [Catalano et al., 2012], we

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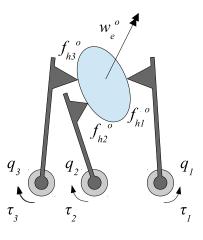


Fig. 2. Full Actuation. Conceptual schematics of a simple bi-dimensional fully actuated hand grasping an object.

exploit the soft synergy idea to build robot hands that can grasp a large variety of objects in a stable way, while remaning very simple and robust. Our approach to the principled simplification of hand design can be summarized as follows. From statistical observations of human grasping, we derive the hand postures most often used in the grasp approach phase (aka synergies) and design the hand mechanism so that similar approach motions are obtained. Indeed, human-like hand movement has great influence in the possibility of successfully achieving a large number of grasps belonging to the sphere of activities of daily living (ADL). The actual realization of the hand mechanics is not however a straightforward implementation of the soft synergy model. Indeed, to achieve a simple and compact design and better robustness, we recur to the technology of underactuated hands [Birglen et al., 2008], complementing it with innovative joint and ligament design. One of the main contributions of this paper is to show how the design parameters of an underactuated hand can be chosen so that its motion replicates a given set of synergies, in a sense allowing the translation of the concept of *soft synergies* into adaptive synergies.

The result of our design method is the Pisa/IIT SoftHand (see fig. 1), a 19-joints hand with anthropomorphic features, which grasps objects of rather general shape by using only a single actuator, and employing an innovative design of articulations and ligaments, which provides a high degree of compliance to external solicitations.

The paper is organized as follows: section II introduces the problem and presents a review of possible hand actuation patterns, before concentrating on the soft and adaptive synergies approaches. Section III presents a proof-of-concept design, after which the Pisa/IIT SoftHand prototype is built, as Section IV describes in detail. Section V presents the grasping results experimentally obtained. Finally, conclusions are drawn in section VI.

Notation	Definition	
δx	variation of variable x	
$ar{x}$	value of x in the reference configuration	
$\sharp x$	dimension of vector x	
$w_e^o \in \mathbb{R}^6$	external wrench acting on the object	
$u\in\mathbb{R}^6$	pose of the object frame	
$f_h^{c^o} \in \mathbb{R}^c$	contact forces exerted by the hand on the object	
c c	number of contact constraints	
$ au \in \mathbb{R}^{\sharp q}$	joint torque	
$q \in \mathbb{R}^{\sharp q}$	joint configuration	
$q_r \in \mathbb{R}^{\sharp q}$	reference joint configuration	
$\sigma \in \mathbb{R}^{\sharp \sigma}$	soft synergy configuration	
$\varepsilon \in \mathbb{R}^{\sharp \sigma}$	soft synergy forces	
$z \in \mathbb{R}^{\sharp z}$	adaptive synergy displacements	
$\eta \in \mathbb{R}^{\sharp z}$	adaptive synergy forces	
$^{o}G \in \mathbb{R}^{6 \times c}$	grasp matrix in object frame	
${}^{c^{o}}\!J \in \mathbb{R}^{c \times \sharp q}$	hand Jacobian matrix in object frame	
$S \in \mathbb{R}^{\sharp q \times \sharp \sigma}$	soft synergy matrix	
$R \in \mathbb{R}^{\sharp z \times \sharp q}$	adaptive synergy matrix	
TABLE I		

NOTATION FOR GRASP ANALYSIS.

II. HAND ACTUATION, SYNERGIES AND ADAPTATION

A. Fully Actuated Hands

In this section we provide a description of design paradigms of hand motor systems found in robotic literature. Starting from the simplest case of fully actuated hand grasping an object, we also provide an analytical description of the different actuation methods. The nomenclature and notation used for grasping analysis are synthesized in Table I. Finally, we present a map between the human inspired soft synergy model and the adaptive synergy design, used in the Pisa/IIT SoftHand. More details about the mathematical description of grasping can be found in [Murray et al., 1994], [Gabiccini et al., 2012].

A quasi-static description of the problem of a hand grasping an object can be formalized by a system of three equations as

$$\delta w_e^o + {}^o G \delta f_h^{c^o} = 0, \tag{1}$$

$$\delta\tau = \bar{\Omega}\delta q + \bar{U}\delta u + {}^{c}\bar{J}^{T}\delta f_{h}^{c^{o}}, \qquad (2)$$

$$\delta f_h^{c^o} = K_c ({}^{c^o} \bar{J} \delta q - {}^o G^T \delta u). \tag{3}$$

Here, the object equilibrium equation (1) establishes a relationship between external disturbances acting on the object and contact forces that the hand exerts on the object, eq. (2) describes the joint torque variation required to compensate contact force variation and/or kinematic displacement of the system, and the contact constitutive equation (3) relates contact force variation with the mutual displacements of the hand and the object contact points.

More in detail, in equation (1), the symbol $w_e^o \in \mathbb{R}^6$ indicates the external wrench acting on the object, described in a local frame $\{O\}$, while $f_h^{c^o} \in \mathbb{R}^c$ are the forces that the hand exerts on the object, described in local contact frames, fixed to the object. The value of c, for the contact force vector, depends on the number and type of contact constraints. For example, an *hard finger* contact, allows the presence of three components of forces, thus it contributes three. Indeed, the *soft finger* contact, with respect to the hard one, adds the possibility to exert a moment around the normal vector to the contact surface, thus it contributes four. Through the introduction of the grasp matrix ${}^{o}G \in \mathbb{R}^{6 \times c}$, the object equilibrium condition is written as

$$w_e^o + {}^o G f_h^{c^o} = 0. (4)$$

Because the equation is written in a reference frame attached to the object, the grasp matrix is constant, hence by differentiating (4), (1) follows.

The hand equilibrium equation relates contact forces with joint torques, $\tau \in \mathbb{R}^{\sharp q}$, through the transpose of the hand Jacobian matrix ${}^{c}J^{T}(q, u) \in \mathbb{R}^{\sharp q \times c}$, as

$$\tau = {}^{c^o}\!J^T(q, u) f_h^{c^o}.$$
(5)

It is worth observing that the Jacobian matrix is here a function both of the hand configuration q and of the object configuration $u \in \mathbb{R}^6$. This is a consequence of the choice to describe the contact interaction in a local frame attached to the grasped object. From this fact it follows that, differentiating (5), (2) is obtained, where the terms $\Omega = \frac{\partial^{c^o} J^T f_h^{c^o}}{\partial q} \in \mathbb{R}^{\sharp q \times \sharp q}$ and $U = \frac{\partial^{c^o} J^T f_h^{c^o}}{\partial u} \in \mathbb{R}^{\sharp q \times 6}$ have to be considered. As described in [Bicchi, 1994], a rigid model of hand/object

As described in [Bicchi, 1994], a rigid model of hand/object interaction does not allow the computation of the contact force distribution. The problem can be simply solved by introducing a *virtual spring* at the contact points. One extreme of each virtual spring is attached to the hand and the other to the object, both in the nominal contact location. The virtual spring model generates a force variation corresponding to the local interpenetration of the hand and object parts. Correspondingly, a contact force variation is described in (3) through the introduction of the *contact stiffness* matrix $K_c \in \mathbb{R}^{c \times c}$.

The basic grasp equations (1), (2) and (3) can be rearranged in matrix form as

$$\begin{bmatrix} I_{\sharp w} & 0 & {}^{o}G & 0 & 0\\ 0 & I_{\sharp \tau} & -{}^{c^{o}}\bar{J}^{T} & -\bar{\Omega} & -\bar{U}\\ 0 & 0 & I_{\sharp f} & -K_{c}{}^{c^{o}}\bar{J} & K_{c}{}^{o}G^{T} \end{bmatrix} \begin{bmatrix} \delta w_{e}^{o}\\ \delta \tau\\ \delta f_{h}^{c^{o}}\\ \delta q\\ \delta u \end{bmatrix} = 0. \quad (6)$$

This is a linear homogeneous system of equations in the form $A\delta y = 0$, where $A \in \mathbb{R}^{r_a \times c_a}$ is the coefficient matrix, and $\delta y \in \mathbb{R}^{c_a}$ is the vector containing all system variables. From (6), we easily obtain that A is always full row rank, and its dimensions are

$$r_a = \sharp w + \sharp q + \sharp f,$$

$$c_a = 2\sharp w + 2\sharp q + \sharp f.$$
(7)

These facts imply that a basis for the solution space of the system has dimension $c_a - r_a = \#w + \#q$. Thus, a perturbed configuration of the system can be completely described knowing the values of the external wrench variation, δw_e^o , and the displacements of the joint configuration¹, δq . We will refer to these as the *independent variables* of the system. The *dependent variables* will be indicated as $\delta y_d = [\delta \tau^T, \delta f_h^{c^o T}, \delta u^T]^T$. Acting on the coefficient matrix of the system, it is possible to obtain a formal method to get an explicit expression of the dependent variables of the system, as a function of the independent ones. This result is achievable extending the *elementary Gauss operations*, defined for typical linear systems of equations, in order to act on a block partitioned matrix. A general algorithm to obtain the desired form starting from (6), called GEROME-B, was presented in [Gabiccini et al., 2012]. The final result of the procedure is a set of equations of the type

$$\delta y_d = W_d \,\delta w_e^o + Q_d \delta q. \tag{8}$$

In the rest of this paper, we will mostly focus on the study of the controllability of grasping with different hand actuation system, hence considering a null external wrench variation in (8). For the sake of completeness, we report here on the structure of this matrix, which can be partitioned as $Q_d = \begin{bmatrix} Q_{\tau}^T & Q_f^T & Q_u^T \end{bmatrix}^T$, with the following explicit formulae

$$Q_{\tau} = \bar{\Omega} + {}^{c^{o}}\bar{J}^{T}K_{c}{}^{c^{o}}\bar{J} + + (\bar{U} - {}^{c^{o}}\bar{J}^{T}K_{c}{}^{o}G^{T}) ({}^{o}GK_{c}{}^{o}G^{T})^{-1}{}^{o}GK_{c}{}^{c^{o}}\bar{J}, Q_{f} = K_{c}{}^{c^{o}}\bar{J} - K_{c}{}^{o}G^{T} ({}^{o}GK_{c}{}^{o}G^{T})^{-1}{}^{o}GK_{c}{}^{c^{o}}\bar{J}, Q_{u} = ({}^{o}GK_{c}{}^{o}G^{T})^{-1}{}^{o}GK_{c}{}^{c^{o}}\bar{J}.$$
(9)

B. Approaches to Simplification

In principle, fully independent actuation offers the widest possibilities, limited only by the hand kinematics. This comes with a cost in terms of design complication to accommodate for the large number of actuators. Even disregarding the hardware aspect, however, the exploitation of the potential of full independent actuation requires sophisticated programming and control of the hand to exploit the potentialities of the kinematic structure. Programming complexity turns often out to represent a major obstacle to usability and efficiency in real-world applications of robot hands.

One of the main directions recently followed is the under-parametrization of the hand postures, following the idea of synergies, so as to find a trade off between the full utilization of the hand capabilities and the simplicity in control. Neuroscience results, as for example those of [Weiss and Flanders, 2004], [Santello et al., 2013], [Castellini and van der Smagt, 2013], hinted that the brain controls the human hand not as a collection of independent articulations and muscles, but rather as an organized whole of coherent motion patterns or primitives. Particular muscular activation patterns give rise to strongly correlated movements, which form a base set [Easton, 1972], resembling the concept of basis of a vector space in linear algebra. Such basis is referred to as the space of *postural synergies*, or *eigengrasp* [Ciocarlie et al., 2007], [Prattichizzo et al., 2010], space [Wimboeck et al., 2012].

What makes the bio-aware synergy basis stand out among other possible choices for the basis to describe the hand configuration is the fact that most of the hand grasp posture variance, actually the 80%, is explained just by the first two synergies, and the 87% by the first three

¹From the previous considerations, it follows that other choices are possible. However, a complete discussion about these cases is out of the scope of this work.

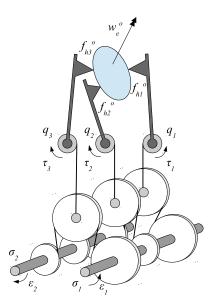


Fig. 3. Hard Synergy actuation scheme. Turning the shaft of a pulley train generates a joint motion pattern, which can be designed corresponding to a desired synergy vector.

[Santello et al., 1998]. This renders the synergy space a credible candidate as a basis for simplification.

The basic idea behind the use of synergies in robotics consists in specifying a suitable base for the joint space movements, called *synergy matrix*, $S \in \mathbb{R}^{\sharp q \times \sharp \sigma}$, where $\sharp \sigma \leq \\ \sharp q$ is the number of used synergies. A hand configuration can be described in the synergy space by the coordinate vector $\sigma \in \mathbb{R}^{\sharp \sigma}$ as in

$$q = S\sigma. \tag{10}$$

There already exist some applications in robotics which take advantage of the idea of synergies. For example in [Ciocarlie et al., 2007], the use of *software synergies* as simulated correlation patterns between joint movements of a fully actuated robotic hand was suggested to simplify control. Software synergies can substantially simplify the design phase of a grasp, by reducing the number of control variables (see also [Ficuciello et al., 2011]). However, software synergies clearly do not impact the simplification of the design of physical hands.

The possible applications of the synergy concept however are not limited to software. Robotic hand implementing hardware synergies can be build, reducing the number of motors, but preserving the ability to achieve most grasping tasks. The design proposed in [Brown and Asada, 2007], for instance, adopts a train of pulleys of different radii to transmit simultaneously different motions to each joint. Motions corresponding to two synergies can be superimposed via a mechanism with tendons and idle pulleys, as illustrated in the simplified scheme of fig. 3.

Both the software synergies [Ciocarlie et al., 2007], and the hard synergies [Brown and Asada, 2007] adopt a model of the hand with a number of independent actuators (or Degrees of Actuation, DoA) smaller than the number of joints (or degrees of Freedom, DoF). In both cases, this causes the hand to move of each finger when it comes in contact with the grasped object, while prosecuting motion of others, or introducing a complementary actuation system for modifying the shape of synergies. While these techniques can be considered to simplify the grasp approaching phase design, they do not benefit from synergies to control grasping forces.

C. Soft Synergies

To take advantage of synergistic approach both in the pre-grasp phase and in contact force control, the idea of *soft synergies* was introduced and discussed in [Bicchi et al., 2011]. In this model, synergy coordinates define the configuration of a *virtual hand*, toward which the real one is attracted by an elastic field. To describe this situation, we introduce a *reference configuration* vector $q_r \in \mathbb{R}^{\sharp q}$, describing the configuration of the virtual hand. In this model, the motion of the virtual hand is directly controlled in the synergy space as

$$\delta q_r = S \delta \sigma. \tag{11}$$

The difference between the real position of the hand and its reference configuration generates the joint torques, which, at equilibrium, balance the interaction forces between the real hand and the grasped object. In formulae, defining a *joint stiffness* matrix $K_q^s \in \mathbb{R}^{\sharp q \times \sharp q}$, the joint torques in the soft synergy model are given by

$$\delta \tau = K_a^s (\delta q_r - \delta q). \tag{12}$$

By kineto-static duality, introducing the generalized force in the synergy space $\delta \varepsilon \in \mathbb{R}^{\sharp \sigma}$, one has immediately that

$$\delta \varepsilon = S^T \delta \tau. \tag{13}$$

The soft synergy model can be used to control grasping forces by either commanding the virtual hand posture, as for example in [Gabiccini et al., 2011], or varying the joint stiffness matrix (see below (17)).

A implementation via software of this approach was demonstrated in [Wimboeck et al., 2006] on the DLR HAND II, a fully actuated hand with programmable gains, which can simulate variable joint stiffness. A hardware implementation of a fully variable stiffness hand, using an antagonist pair of actuators per each joint, as sketched in fig. 4, was presented in [Grebenstein et al., 2011]. Although this hand has the potential for unprecedented versatility and performance, it does not address the simplification goals of this paper.

One important aspect of the soft synergy model, which can be observed in the comparison between (10) and (11), is that a soft synergy hand can reduce the number of DoA while retaining all its kinematic DOFs, leaving the fine adjustment of the $\sharp q - \sharp \sigma$ remaining movements to the compliance model. A conceptual hardware implementation of this idea is shown in fig. 5, where springs are used in series with a mechanism similar to that of fig. 3. Such a reduced-DoA soft synergy

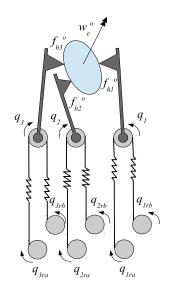


Fig. 4. Full Variable Stiffness Actuation. Schematics of a hand with same kinematics as in fig. 2, where each joint is powered by variable stiffness agonist-antagonist actuators.

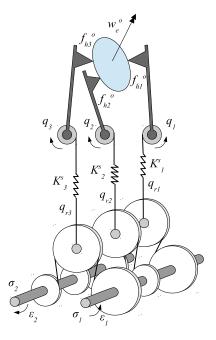


Fig. 5. Soft Synergy Actuation. Schematics of a hand with same kinematics as in fig. 2, where all the joints are moved according to soft synergy actuation system.

hand can be easily modeled by considering (11), (12) and (13), along with the grasp equation (8). In particular, for zero external wrenches on the object, for the joint torques it holds

$$\delta \tau = Q_\tau \delta q, \tag{14}$$

where $Q_{\tau} \in \mathbb{R}^{\sharp q \times \sharp q}$ was described in (9). Substituting (14) in (12), taking into account (11), we obtain

$$\delta q = \left(K_q^s + Q_\tau\right)^{-1} K_q^s S \delta \sigma. \tag{15}$$

Defining the matrix

$$H^{s} = \left(K_{q}^{s} + Q_{\tau}\right)^{-1} \in \mathbb{R}^{\sharp q \times \sharp q},\tag{16}$$

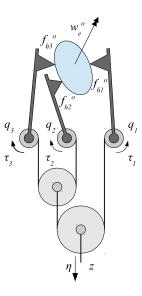


Fig. 6. Shape-Adaptive Underactuation. Schematics of a hand with same kinematics as in fig. 2, where all the joints are powered by an Adaptive Under-Actuated distribution system.

from (8), it immediately follows that

$$\delta y_d = Q_d H^s K^s_a S \delta \sigma. \tag{17}$$

Equation (17) give us a complete description of the variation of the hand/object configuration as a consequence of the synergistic displacements.

Applying (17) to (13), we can further evaluate the corresponding generalized force to be applied at the synergy actuator as

$$\delta \varepsilon = S^T Q_\tau H^s K^s_a S \delta \sigma. \tag{18}$$

Inverting this result, we arrive to

$$\delta\sigma = \left(S^T Q_\tau H^s K^s_q S\right)^{-1} \delta\varepsilon. \tag{19}$$

Substituting (19) in (15), the hand joint displacement becomes

$$\delta q = H^s K^s_q S \left(S^T Q_\tau H^s K^s_q S \right)^{-1} \delta \varepsilon.$$
⁽²⁰⁾

Therefore, substituting (20) in (8), the complete system variation, depending on the soft synergy forces, is finally obtained.

Although the idea of soft synergy actuation sketched in fig. 5 appears to provide an elegant solution to the problem of simple hand design, merging the natural motion inherited from the postural synergy approach with adaptivity due to compliance, its implementation in a mechanical design unfortunately turned out not to be very easy or practical, at least in our attempts.

D. Adaptive Synergies

A distinct thread of research work has addressed the design of simple robot hands via the use of a small number of actuators without decreasing the number of DOF. This approach, authoritatively described in [Birglen et al., 2008], is referred to as *underactuation* and has produced a number of interesting hands since the earliest times of robotics. For further details the reader can refer

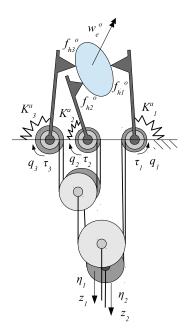


Fig. 7. Adaptive Synergies. Schematics of a hand with same kinematics as in fig. 2, where all the joints are controlled by two adaptive synergies.

to [Tomovic and Boni, 1962], [Hirose and Umetani, 1978], [Rovetta, 1981], and also to [Laliberté and Gosselin, 1998], [Carrozza et al., 2004], [Gosselin et al., 2008] and [Dollar and Howe, 2010].

The basic idea enabling shape adaptation in underactuated hands is that of a differential transmission, the well-known mechanism used to distribute motion of a prime mover to two or more DOFs. Differentials can be realized in various forms, e.g. with gears [Laliberte et al., 2002], closed-chain mechanisms [Laliberte et al., 2002], or tendons and pulleys [Hirose, 1985], and concatenated so as to distribute motion of a small number of motors to all finger joints q. Letting the vector $z \in \mathbb{R}^{\sharp z}$, with $\sharp z \leq \sharp q$, denote the position of the prime movers, a general differential mechanism is described by the kinematic equation

$$R\delta q = \delta z, \tag{21}$$

where $R \in \mathbb{R}^{\sharp z \times \sharp q}$ is the transmission matrix, whose element R_{ij} is the transmission ratio between the *i*th actuator to the *j*th joint. Fig. 6 conceptually illustrates a tendon-pulley differential mechanism with a single motor actuating three joints. By kineto-static duality, the relationship between the actuation force vector $\eta \in \mathbb{R}^{\sharp z}$ and the joint torques is

$$\delta \tau = R^T \delta \eta. \tag{22}$$

The kinematic model (21) highlights the non-uniqueness of the position attained by an underactuated hand. Indeed, being the transmission matrix R a rectangular fat matrix, an infinity of possible hand postures δq exist which satisfy (21) for a given actuator position δz , their difference belonging to the kernel of R.

While it is exactly these kernel motions that provide underactuated hands with the desirable feature of *shape adaptivity*, in practice these hands associate to differential mechanisms the use of passive elements such as mechanical limits, clutches, and springs [Birglen et al., 2008]. Reasons for adding passive elements are manifold, including avoiding tendon slackness and ensuring the uniqueness of the position of the hand when not in contact with the object.

Consider the model of an underactuated hand with elastic springs depicted in fig. 7, that we will call, henceforth, *adaptive synergy* actuation. Notice that springs are arranged in parallel with the actuation and transmission mechanism, as opposed to the soft synergy model in fig. 5 where they are in series. Defining a joint stiffness matrix as $K_q^a \in \mathbb{R}^{\sharp q \times \sharp q}$, the balance equation (22) is rewritten as

$$\delta \tau = R^T \delta \eta - K^a_a \delta q. \tag{23}$$

Considering (23) and (14), it immediately follows that

$$\delta q = \left(K_q^a + Q_\tau\right)^{-1} R^T \delta \eta. \tag{24}$$

Thus, substituting this in (8), we obtain a description of the hand/object equilibria caused by the application of given actuator forces.

If instead actuators are modeled as position sources, defining the matrix

$$H^{a} = \left(K_{q}^{a} + Q_{\tau}\right)^{-1} \in \mathbb{R}^{\sharp q \times \sharp q},\tag{25}$$

and by substituting equation (24) in (21) and inverting, we find

$$\delta\eta = \left(RH^a R^T\right)^{-1} \delta z. \tag{26}$$

Substituing this in (24), we then obtain

$$\delta q = H^a R^T \left(R H^a R^T \right)^{-1} \delta z. \tag{27}$$

Finally, a complete system description in the case of actuator position control is given by substituting (27) in (8).

E. From Soft to Adaptive Synergies

Summarizing the discussion so far, we have seen that two design techniques for multiarticulated hands with simple mechanics stand out for different reasons. The method of soft synergies provides a sound theoretical basis for the design of anthropomorphic hands with a principled way to compose multiple motion primitives and a well understood neuroscientific rationale, but not an effective technological implementation. On the other hand, underactuated hands have desirable adaptivity to shapes, and can be effectively implemented with simple differential and elastic elements. In this section, we show how an underactuated hand can be indeed designed so as to realize a soft-synergy model.

Assuming that a desired soft synergy model is assigned trough its synergy and stiffness matrices, S and K_q^s respectively, our goal is to find a corresponding adaptive synergy model, identified by a transmission matrix R and a joint stiffness K_q^a , which exhibits the same behavior, at least locally around an equilibrium configuration.

As shown in the previous sections, the behavior of the hand/object system is slightly different if the hand is position controlled or force controlled. This holds true for both soft and adaptive synergy model. Nevertheless, in all of the cases, the system is described as a linear map from an independent variable δy_i , that can be one of $\{\delta\sigma, \delta\epsilon, \delta z, \delta\eta\}$, and the joint displacement as $\delta q = A_i \delta y_i$, where A_i is taken from one of (15), (20), (24) or (27), respectively. By means of (8), the joint displacement describes the variation of the dependent variables at the hand/object level.

The map can be also defined in the opposite direction, starting from a given adaptive synergy, to obtain a corresponding soft synergy. The total amount of possible maps is eight, considering both the case of position and force control.

We will describe now the procedure to find one of such mappings, from a given position controlled soft synergy model to the corresponding position controlled adaptive synergy hand. All the other maps can be found with similar procedures, and the results will be discuss later.

The hand/object behavior for a position controlled soft synergy hand is defined by (15), while the behavior of an adaptive underactuated hand is controlled by (27). To match them means to impose

$$H^{s}K_{q}^{s}S\,\delta\sigma = H^{a}R^{T}\left(RH^{a}R^{T}\right)^{-1}\delta z.$$
(28)

Looking at the span of the second term of the previous equation, it is possible to see that

$$\operatorname{span}\left\{H^{a}R^{T}\left(RH^{a}R^{T}\right)^{-1}\right\} = \operatorname{span}\left\{H^{a}R^{T}\right\},\qquad(29)$$

since the term $(RH^aR^T)^{-1}$ is a square full rank matrix. As a consequence, the span of the two terms in (28) can be matched by imposing

$$H^a R^T = H^s K^s_q SM, (30)$$

where matrix M can be any full rank square matrix of suitable dimensions, which can be used as design parameter and accounts also for measurement units harmonization. To complete the map, a relationship has to be defined from $\delta\sigma$ to δz . Given the choice on (30), a suitable relationship is

$$\delta z = \left(R H^a R^T \right) M^{-1} \delta \sigma. \tag{31}$$

With similar consideration, it is possible to prove that, even considering all the other possible actuation combinations, the map between soft and adaptive synergies can always be written as in (30). It is worthwhile noting that, by the choice $K_q^a = K_q^s = K_q$, remembering the definitions in (16) and (25), the map in (30) can be simplified to

$$R^T = K_q S M, (32)$$

in accordance with the results shown in [Grioli et al., 2012].

With some computation, a control map, similar to (31), can be found for any actuation combination. Without going into the details, we only report that in the "position controlled soft synergy – force controlled adaptive synergy" case, the control laws can be translated by the simple relation

$$\delta \eta = M^{-1} \delta \sigma \text{ or } \delta \sigma = M \delta \eta.$$
 (33)

It is important nothing that (33) abstracts from the knowledge of Q_{τ} , that is from the knowledge of the object being grasped. In other words this means that this case allows to design a force controlled adaptive synergy hand which behaves, with respect to the grasped object, as a position controlled soft synergy hand.

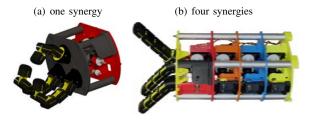


Fig. 8. A modular hand prototype with adaptive synergies. Left: an assembly with two 4-phalanges fingers, a 2-phalanges thumb, and a single adaptive synergy. Right: a prototype with three equal fingers and four adaptive synergies.

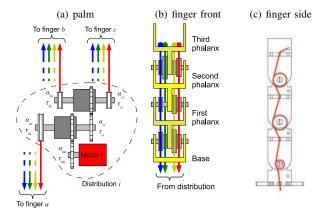


Fig. 9. Arrangement of the differential transmission to implement four adaptive synergies. Notice that the pulleys mounted on the finger (panel b) are idle, to allow a differential effect: the total tendon displacement is proportional to the weighted sum of the joint angles where the weights are the pulley radii. This implies that a given tendon displacement is compatible with different joint configurations, implementing a differential relationship.

III. A MODULAR HAND WITH FOUR ADAPTIVE SYNERGIES

To validate the approach of adaptive synergies and to demonstrate and analyse the effectiveness of the integration of multiple synergies in a single device, a proof-of-concept, rapidly prototyped hand was realized. The hand is conceived as a modular platform, which can accommodate for different numbers of phalanges, fingers, and synergies (see fig. 8). As the hand is not anthropomorphic, the choice of postural synergies from a human grasp database would make no sense. In order to test our design concepts, therefore, we chose the four synergies heuristically. However, we did implement the constraint on these artificial synergies to be orthogonal.

A schematic of a single stage is shown in fig. 9(a), containing a servomotor and two differential gears used to transmit the torque from the motors to the tendons routed through fingers. From each stage three tendons (one for each finger) go up to the palm. Fig. 9(b) shows how actuation tendons of each synergy are put together and managed inside each finger. Each tendon is routed through each finger in a way similar to the solution shown in fig. 9(c).

Some experimental tests were performed to demonstrate the main characteristics of the hand prototype. In the experiments reported, some simple grasp tests were performed to show the hand adaptiveness during grasp of objects (a sphere, a cylinder,

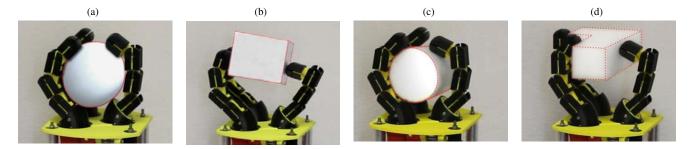


Fig. 10. Hand prototype during the execution of some simple grasps. Only one synergy is used to grasp four test objects. Despite this, depending by the actuation variable, grasped object shape, contact point positions and internal forces, different grasp configurations can be achieved.

a box and a L-shaped polyhedron). Pictures of the resulting grasp positions are shown in fig. 10, showing the adaptivity allowed by the use of differential transmission.

IV. THE PISA/IIT SOFTHAND

In this section we apply the adaptive synergy design approach of fig. 7 to the design of a humanoid hand. The hand was designed according to few specifications. On the functional side, requirements are to grasp as wide a variety of objects and tools as possible, among those commonly used by humans in everyday tasks. The hand should be primarily able to effect a *whole hand grasp* of tools, properly and strongly enough to operate them under arm and wrist control, but also be able to achieve *tip grasps*. No in–hand dexterous manipulation is required for this prototype. The main nonfunctional requirements are resilience against force, overexertion and impacts, and safety in interactions with humans. The hand should be lightweight and self-contained, to avoid encumbering the forearm and wrist with motors, batteries and cabling, along with cost effectiveness.

To meet the first functional requirement, the hand was designed anthropomorphically, with 19 DOFs arranged in four fingers and an opposable thumb (fig. 11). To maximize simplicity and usability, however, the hand uses only one actuator. According to our design approach, the motor actuates the adaptive synergy as derived from a human postural database [Santello et al., 1998]. The mechanical implementation of the first soft synergy through shapeadaptive underactuation was obtained via the numerical evaluation of the corresponding transmission matrix R and joint stiffness matrix K_q^a appearing in (21) and (23). The addition of further degrees of actuation, for example in-hand manipulation capabilities, is possible in principle, following the design approach illustrated in the previous section, but is left for future work. The hand assembly design is shown in fig. 12. Each finger has four phalanges, while the thumb has three. The hand palm is connected to a flange, to be fixed at the forearm, through a compliant wrist allowing for three passively compliant DOFs.

The wrist of the SoftHand is composed by two curved surfaces, able to roll one on the other. The contact between them is guaranteed by the use of elastic ligaments, arranged along the perimeter of the wrist. When relative motion of the surfaces arises, for example caused by an external load, a set

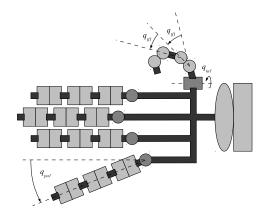


Fig. 11. Kinematics of the Pisa/IIT SoftHand. Revolute joints are in dark gray, while rolling-contact joints are in light gray.

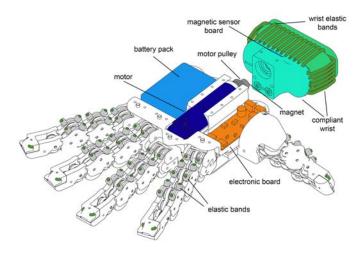


Fig. 12. A three–dimensional view of the Pisa/IIT SoftHand. Main components (the motor, the battery pack and the electronic control board), joints and wrist architecture are highlighted.

of elastic forces appears. The wrist comes back to the original configuration when the external load is removed.

In rest position, with fingers stretched out and at a relative angle of about 15° in the dorsal plane, the hand spans approximately 230 mm from thumb to little finger tip, is 235 mm long from the wrist basis to the middle finger tip and has 40 mm maximum thickness at the palm. The requirement on power grasp implies that the hand is able to generate a high enough grasping force, and to distribute it evenly through all contacts, be them at the fingertips, the inner phalanges, or the palm. These goals are naturally facilitated by the shape adaptivity of the soft synergy approach, yet they also require strong enough actuation and, very importantly, low friction in the joints and transmission mechanisms.

The requirement on resilience and safety was one of the most exacting demands we set out for our design, as we believe these to be crucial features that robots must possess to be of real use in interaction with, and assistance to, humans. This is only more true for hands, the body part primarily devoted to physical interaction with the environment for exploration and manipulation. To achieve this goal, we adopted a non-conventional "soft robotics" design of the mechanics of the hand, that fully exploits the potential of modern material deposition techniques to build a rather sophisticated design with rolling joints and elastic ligaments at very low cost. A first departure form conventional design is the use of rolling contact articulations to replace standard revolute joints. Our design is inspired to a class of joints known as COmpliant Rolling-contact Elements (CORE) [Cannon and Howell, 2005], [Jeanneau et al., 2004], aka "Rolamite" or "XRjoints" joints [Cadman, 1970] (see fig. 13). Among these, Hillberry's design of a rolling joint [Hillberry and Hall Jr, 1976] is particularly interesting to our purposes. A Hillberry joint consists of a pair of cylinders

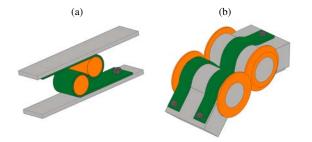


Fig. 13. Schematic illustration of two examples of COmpliant Rollingcontacts Elements (CORE): a Rolamite joint (a) and a Hillberry joint (b).

in rolling contact on each other, held together by metallic bands, which wrap around the cylinders on opposite sides as schematically shown in fig. 13. In Hillberry joints, the band arrangement results in a compliant behavior in flexion but rigid in traction. The joint forms a higher kinematic pair, whose motion is defined by the profile of the cylinders, and exhibits very low friction and abrasive wear. The joint behaves more similarly to the human articulation than simple revolute joint, and for this reason was originally proposed for knee prostheses [Hillberry and Hall Jr, 1976]. Hillberry joints have been used in few robotic applications before, including robot hands [Ruoff, 1985]. Fig. 11 shows how we used CORE joints in the design of the Pisa/IIT SoftHand. In particular, we adopted CORE joints for all the interphalangeal, flexion/extension articulations. Conversely, conventional revolute joints was used for metacarpophalangeal, abduction/adduction articulations. Our design introduces a few important modifications of existing rollingcontact joints, which are illustrated in fig. 14. Firstly, metallic bands were replaced by elastic ligaments, realized

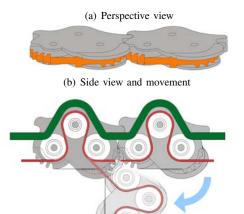


Fig. 14. Design of the compliant rolling–contact joint used in the interphalangeal joints of the Pisa/IIT SofHands: (a) perspective view with rolling cylinders with matching multi-stable profile; (b) lateral view, showing the arrangement of ligaments and tendons.

a polyurethane rubber able to withstand large deformations and fatigue, and are fixed across the joint with an offset in the dorsal direction. Suitable pretensioning of the ligaments, together with a carefully designed profile of the two cylinders, introduce a desirable passive stability behaviour, with an attractive equilibrium at the rest configuration with fingers stretched. The elastic ligaments are polyurethane rubber segments of 2mm diameter, characterized by 88 Shore A hardness. The rest length of the ligaments is 10mm. Some pre-tensioning is applied with a stretch in the range between 2 to 5 mm. All the long fingers proximal flexion joints have lower values of pre-tensioning, with respect to all the other joints, such to guarantee a hand motion similar to the first human synergy, as explained in section II.

The coupled rolling cam profiles are designed on a circular primitive with radius 6.5mm. The actuation tendon is wrapped around pulleys with radius 3.5mm. All the radii are the same for all the rolling profiles and the pulleys, in order to obtain a modular design. The rolling cam profile is realized on cylinder portions flanked by lateral walls on both sides, whose slope is about 80° (see fig. 14 and fig. 16). When two phalanges are assembled, such walls are housed in a fitting recess of the matching phalanx. These features of our design are particularly important for the system to behave softly and safely in contact, and to recover from force overexertion, due e.g. to impacts or jamming of the hand, making the hand automatically return to its correct assembly configuration. The joint can withstand severe disarticulations (cf. fig. 16) and violent impacts (fig. 17).

The design of interphalangeal joints does not require the use of screws, shafts, bearings or gears. As can be seen in fig. 14, a few teeth of an involute gear of vanishing height are indeed integrated in the cam shape, to better support tangential loads at the joint.

Actuation of the hand is effected through a single Dyneema tendon routed through all joints using passive anti-derailment pulleys. The tendon action flexes and adducts fingers and thumb, counteracting the elastic force of ligaments, and implementing adaptive underactuation without the need for

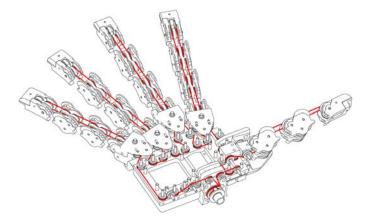


Fig. 15. Partially exploded line sketch of the Pisa/IIT SoftHand. The tendon routing distributes the motion to all joints.

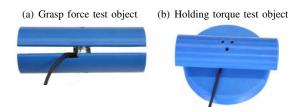


Fig. 18. Sensorized object for force measurements (a), sensorized object for torque measurements (b).

differential gears (fig. 15).

V. EXPERIMENTAL RESULTS

The prototype of the Pisa/IIT SoftHand (fig. 1) was built to perform experimentally tests. The actuator powering the hand is a 6 W Maxon motor RE-max21 with a reduction ratio of 84:1 equipped with a 12 bit magnetic encoder (Austrian Microsystems AS5045) with a resolution of 0.0875° .

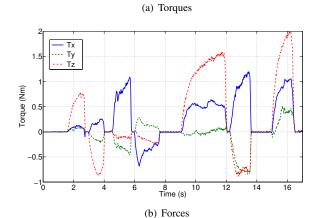
The embedded electronic unit hosting sensor processing, motor control and communication is located in the hand back, along with the battery pack. The opening/closing of the hand is controlled via a single set point reference, communicated via one of the available buses (SPI and RS-485).

During experiments the hand worn an off-the-shelf working glove with padded rubber surfaces, supplying contact compliance and grip.

A. Force and torque measurements

An ATI nano 17 F/T sensor with UDP interface was used to measure holding force and torque of the robotic hand. In the first case, a split cylinders, represented in fig. 18(a), was used to measure the grasp force. The cylinder is 120 mm high and has a diameter of 45 mm. The disk to measure maximum holding torque is represented in fig. 18(b). The disk is 20 mm high and has a diameter of 95 mm.

In fig. 19(b) we report force acquisitions during sensorized object grasp. It is possible to notice how forces increased when fingers get in contact with the sensorized cylinder (step behavior of the lines in fig. 19(b)). We achieved a maximum holding torque of 2 Nm and maximum holding force of about



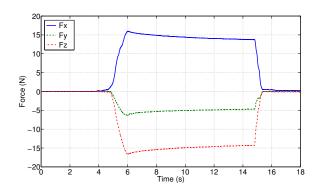


Fig. 19. Torques and forces of the robotic hand during grasp task.

20 N along the z axis. These limits appear to be dictated by the motor size rather than by the hand construction. Although we did not go through an exhaustive analysis, in an occasional experiment with a stronger motor a holding torque of 3.5 Nm and holding force of 28N were obtained. For more details on the performed experiments, pls. see also the accompanying multimedia extension 1.

B. Grasp Experiments

To test the adaptiveness of the robotic hand, the grasp of several objects of daily use in a domestic or lab environment were performed. Grasp experiments were performed in three different conditions: 1) the hand wrist fixed on a table and the object placed in the grasp; 2) the object placed on a table and the hand mounted on a robot arm, and 3) the hand wrist fixed to the forearm of a human operator.

Some examples of grasps achieved in the first condition are reported in fig. 20.

To test usage of the Pisa/IIT SoftHand in a robotic scenario, the hand was mounted at the end-effector flange of a KUKA Light–Weight robot arm. Fig. 21 shows some of the grasps tested. Notice that the robot was manually programmed to reach an area were the object was approximately known to lie, and no grasp planning phase was executed. Rather, the hand was given a closure command by software. The closure time, as well as the robot trajectory, were preprogrammed in the examples shown, and were the same for each object lying roughly in the same area. Video sequences of the performed

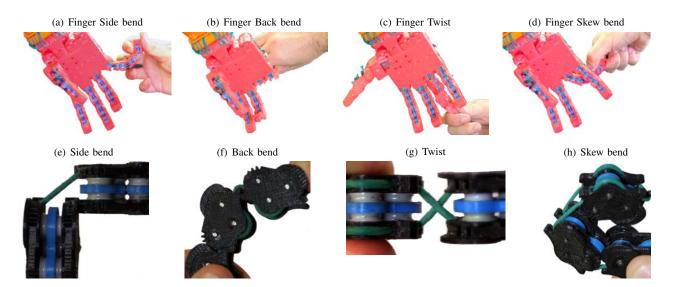


Fig. 16. The Pisa/IIT SoftHand joints can withstand severe force overexertion in all directions, automatically returning to the correct assembly configuration.

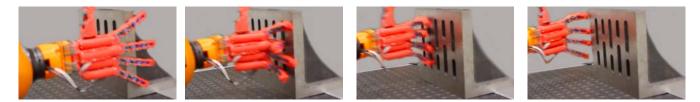


Fig. 17. A photo-sequence showing the PISA/IIT SoftHand during a violent impact with a stiff surface.

experiments can be seen on the multimedia extension 1, including one showing a simple application of grasp force control to first hold, and then operate a spray bottle, and one illustrating on-the-fly grabbing of a water bottle with the arm sweeping a table top at a speed of 1 m/s ca.

Finally, to test the capability of the Pisa/IIT Hand to acquire complex grasps of objects randomly placed in the environment, we developed a wearable mechanical interface (see fig. 22) allowing an operator to use our hand as a substitution of his/her own. The interface can be strapped on the operator's forearm and can be controlled by the operator acting on a lever with his/her real hand (see fig. 21(a)). In fig. 23 we report some grasps executed with the human interface (condition 2 above). Again, more results can be seen in the accompanying multimedia extension 1.

In summary, a total of 107 objects of different shape was successfully grasped, with a whole hand or a tip grasp, in all conditions previous considered, during our tests: bottle, reel, pincer, stapler, pen, phone handset, plier, teddy bear, cup, handle, spray, computer mice, hot–glue gun, human hand, cell phone, glass, screw–driver, hammer, file, book, coin, scotch tape holder, ball, tea bag, ketchup bottle, hamburger, camera, tripod stand, cutter, trash can, keyboard, torch, battery container, battery (AA), small cup, measuring tape, caliper, wrench, lighter, eraser, world map (globe), remote control, hex key, AC adapter, keyring, spoon, fork, knife, hand tissue box, liquid soap dispenser, corkscrew, rag, candy, calculator, slice of cake, rubber-stamp, spring, paper, cellphone case, rubber band,

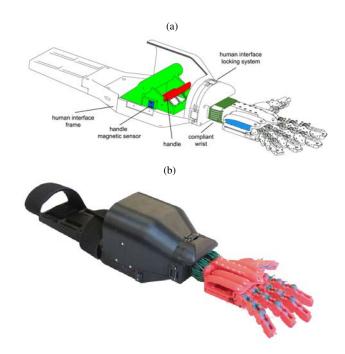


Fig. 22. (a) Components of the interface for human use of the Pisa/IIT SoftHand. The angle position of the lever is acquired by the electronics board and adopted as reference position to drive the actuator of the hand. (b) Appearance of the assembled human interface prototype.

bottle top, watch, umbrella, broom, garbage scoop, scarf, chair, schoolbag, USB cable, glue stick, wallet, credit card, sponge,



Fig. 20. Some experimental grasps performed with the Pisa/IIT hand, with the object placed in the hand by a human operator.

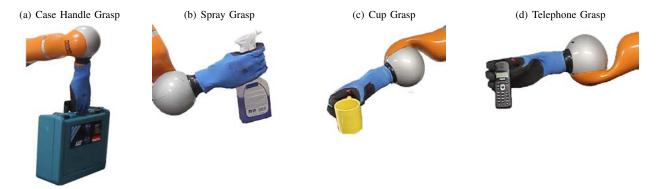


Fig. 21. Grasps executed with the Pisa/IIT SoftHand mounted on a Kuka Light Weight Robot: handbag (a), spray (b), cup(c) and telephone (d).



Fig. 23. Some examples of grasps executed with the robotic hand mounted on a wearable Human Interface: telephone (a), Teddy Bear (b), book (c), and strawberry (d)

pencil sharpener, straight edge, safety lock, mouse pad, hard disk, jacket, drill, chalk, notebook, blackboard eraser, door lock, square ruler, scissors, eyeglasses, deodorant, USB key, hat, headphones, cigarette, helmet, screw (M8), clamp, fridge magnet, drill bit, table calendar, saw, tape cassette, beauty case, bubble gum box, bubble gum, tissue pocket, dish, poster.

The more difficult situation is in grasping very thin objects. However, since grasp limitations of the prototype are also influenced by the operator training, it is not easy to quantify grasp limitations without resorting to further investigations, which are out of the scope of this paper.

One of the main lessons learned through these experiments is that, while all grasps could be easily achieved by the hand when operated by a human, programming the robot to achieve the same grasps was in some cases rather complex. One of the main reason for this is, in our understanding, that the human operator quickly learns how to exploit the intrinsic adaptivity of the hand, including the wrist compliance, to shape the hand before and during grasp. This is done with the help of object features and/or environmental constraints, notably the table top and walls. This observation hints that autonomous learning and planning for soft robot grasping might have to be focused on constraint–based motion rather than on free–space, multi-DOF hand shaping.

VI. CONCLUSION

This paper presented the design and implementation of the Pisa/IIT SoftHand, along with the theoretical framework behind that justifies the main design choices. The important aspect of the hand actuation pattern is considered first, reviewing various past and recent approaches, and finally considering adaptive synergies as preferred choice.

The first prototype of the Pisa/IIT SoftHand, a highly integrated robot hand characterized by a humanoid shape and good robustness and compliance, is presented and discussed. The hand is finally validated experimentally through extensive grasp cases and grasp force measurements. Results are also reported in an the multimedia extension 1.

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APPENDIX

The multimedia extensions to this article are at: http://www.ijrr.org.

Extension	Туре	Description
1	Video	The video shows the Pisa/IIT SoftHand performing many different grasps,
		in addition to robustness and grasp force tests.

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