Advanced Two-State Compressing Algorithm: A Versatile, Reliable and Low-Cost Computational Method for ECG Wireless Applications

Duong Trong Luong*, Nguyen Minh Duc, Nguyen Tuan Linh, Nguyen Thai Ha, Nguyen Duc Thuan

Department of Electronic Technology and Biomedical Engineering, Hanoi University of Science and Technology, Vietnam.

***Corresponding Author**

Duong Trong Luong

Department of Electronic Technology and Biomedical Engineering

Hanoi University of Science and Technology

Vietnam

Email: luong.duongtrong@hust.edu.vn

Abstract

Compressing the ECG signal is considered a feasible solution for supporting a system to manipulate the package size, a major factor leading to congestion in an ECG wireless network. Hence, this paper proposes a compression algorithm, called the advanced two-state algorithm, which achieves three necessary characteristics: a) flexibility towards all ECG signal conditions, b) the ability to adapt to each requirement of the package size and c) be simple enough. In this algorithm, the ECG pattern is divided into two categories: "complex" durations such as QRS complexes, are labeled as low-state durations, and "plain" durations such P or T waves, are labeled as high-state durations. Each duration type can be compressed at different compression ratios, and Piecewise Cubic Spline can be used for reconstructing the signal. For evaluation, the algorithm was applied to 48 records of the MIT-BIH arrhythmia database (clear PQRST complexes) and 9 records of the CU ventricular tachyarrhythmia database (unclear PQRST complexes). Parameters including Compression Ratio (CR), Percentage Root mean square Difference (PRD), Percentage Root mean square Difference, Normalized (PRDN), root mean square (RMS), Signal-to-noise Ratio (SNR) and a new proposed index called Peak Maximum Absolute Error (PMAE) were used to comprehensively evaluate the performance of the algorithm. Eventually, the results obtained were positive with low PRD, PRDN and PMAE at different compression ratios compared to many other loss-type compressing methods, proving the high efficiency of the proposed algorithm. All in all, with its extremely low-cost computation, versatility and good-quality reconstruction, this algorithm could be applied to a number of wireless applications to control package size and overcome congested situations.

Keywords: ECG compression, Telemedicine, ECG pattern classification, adaptive package size

1. Introduction

ECG telemedicine is being developed rapidly and is widely used for a variety of medical purposes, such as improving access to medical services, monitoring patients with chronic and cardiovascular diseases or in ambulatory applications [1,2]. Nevertheless, to guarantee the quality of the transmitted ECG signal, a medical network often faces congestion problems that lead to high Bit Error Rate (BER) and high package loss rate, where the size of the transmitted data is a major contributing factor [3-5]. In low bit rate wireless environments, such as GPRS or HSCSD, different package lengths could cause significant changes in transport delay and jitter, possibly leading to package errors [3]. A larger package size will also increase the number of retransmissions that, as a consequence, will increase the package loss rate due to a higher possibility of packages being discarded [4]. However, continuously reducing the package size does not always produce better performance, since transmission intervals reduce proportionally, and the channels will be extremely busy at a certain level [5]. Therefore, optimizing package size for ECG devices could be an effective solution to maintain performance and utilize channels in a medical wireless network. The sampling rate for digitalizing ECG is always selected to be at least 250 samples/second for portable applications, and up to 1000 samples/second for fully functional monitoring systems in hospitals. Hence, it is difficult to ensure that quality is maintained and there is sufficient channel bandwidth to transmit all the raw data with such large package sizes from different systems. In such a scenario, compressing the ECG signal would be beneficial for transmitting smaller packages without proportionally reducing the interval of transmission. In order to adapt to various applications and clinical situations, the compression algorithm must have three characteristics:

1) It must be flexible for applying to the different shapes of ECG signals without depending on detecting any physiological features, such as P and T wave, QRS complex or R peak.

2) Immediately satisfy every adjustment of the package size to guarantee low delay in critical situations.

3) Have a low computational cost at both compression and decompression stages to allow the system to undertake further processing.

A detailed classification of previous works can be found in the Introduction part of Ref. [6]. There are more than 50 compression methods that could be divided into two major sections: 1-D methods and 2-D methods. In 1-D methods, there are also four sub-groups including *direct-time domain compression methods* (DTD), *model based compression methods* (MB), *transform domain compression methods* (TD) and *hybrid compression methods* (H). Except for DTD methods[7-10], which can achieve all three characteristics mentioned above, the other groups have their own disadvantages preventing their widespread use in different applications. MB methods need to detect QRS complexes or R peaks to capture different shapes of beats for storage in their codebooks [11-14], or for learning mechanism and compression in case of using Vector Quantization technique (VQ) [15-18].TD methods [6], [19-39] which use different transformations such as Wavelet transform, discrete cosine transform, etc., hardly satisfy the change of compressed data size without affecting the quality of reconstruction, since they depend on the size of processing block. Besides that, although the reconstruction were extremely good at very high compression ratio due to various modifications in transformation techniques or error minimization mechanisms, the considerable computational cost causes TD methods to be hardly applied in a network with multiple ECG devices. Likewise, H[40-42] and 2-D methods[43-48] are even more computationally complex and are difficult for implementing in wireless applications as a step. DTD methods, such as turning point (TP) [7], amplitude zone time epoch coding (AZTEC) [8], the coordinate reduction time encoding (CORTES) [9]and scan along polygonal approximation (SAPA) [10], are the most flexible ones compared to others, since

they are simple enough and independent of ECG features (these algorithms actually only detect slopes in general, not P and T waves or QRS complex). Nevertheless, almost all of them except SAPA cannot re-produce a reliable ECG signal. A comprehensive review about these algorithms was done in Ref. [49]. Therefore, this paper aims to add a novel, extremely simple, versatile and enough reliable compression algorithm to the DTD group, called *the advanced two-state algorithm*, using two different compression ratios to compress two types of durations in the ECG signal: *complex durations* and *plain durations*, and apply Piecewise Cubic Spline, a basic interpolation algorithm, for decompressing the signal. Details of the proposed method are given in section 2. In section 3, we survey the performance of the algorithm with two types of ECG signals: signals with clear PQRST complexes (BIH-MIT arrhythmia database [50]) and signals with unclear PQRST complexes (CU ventricular tachyarrhythmia [51]). We discuss our results in section 4 and, our conclusions are provided in the last section.

2. Two-state compressing algorithm

2.1 Principle and overview of the two-state compressing algorithm

Many compressing methods share the same idea of separating QRS complexes containing high frequency components, from P and T waves, which only consist of low frequency components. However, almost algorithms used in those methods tend to detect exactly R peaks or QRS complexes that can reduce their versatility and flexibility in case of irregular ECG signals as well as increase the cost of computation. To overcome this problem, the proposed algorithm tends to distinguish between *complex durations* in general, in which QRS complexes are particular examples, and *plain durations* in general, which include P and T waves, by a simpler method of using two thresholds in the first derivative of the signal (Figure 1). The first derivative of the ECG signal is calculated as below:

$$y_i' = \frac{y_{i+1} - y_i}{\Delta x} = y_{i+1} - y_i \qquad (1)$$
$$\text{with } \Delta x = 1 \text{ and } i = 0,1..,n-1$$

Where, n is the number of ECG samples, y_i and y_i' are the ith ECG's sample and the ith first derivative sample. As clearly seen, y_i' is in fact the difference between y_i and its previous sample, thus it can help distinguish the pattern as a low- or high-frequency duration. Considering a short period of record number 103 of MIT-BIH arrhythmia (Figure 1), which has clear PQRST shapes, the P and T waves exhibit a moderately flat pattern in the first derivative, expressing their slow changing curves, which could be classified easily by a threshold *Thr1*. If a sample is equal to or larger than *Thr1*, it would indicate a possible upcoming *complex duration* like QRS complexes. To capture sufficient *complex durations* in the first derivative, a smaller threshold *Thr2* is used. By continuously finding samples smaller than *Thr2*, the end of QRS will be defined, and the threshold is switched back to *Thr1*. As a result, *plain durations* and *complex durations* could be eventually separated by this extremely low-cost computational mechanism. After classification, both *complex durations* and *plain durations* are compressed simply by a downsampling process, which decreases the sampling frequency of the signal by just removing the samples:

$$\tilde{y}_i = y_{i*k} \text{ with } i = 0,1..,m-1 \qquad (2)$$

Wherein, h, $\tilde{y}_i$ is the ith sample of the compressed signal, m is the number of samples after compressing, k is the *downsample factor (DF)* and in this case, it is also the *compression ratio (CR)* of that duration. Henceforth, we will use the term CR instead of DF throughout the manuscript to be more precise in terms of the compressing data. The classification mechanism and the downsampling process above form the **principle** of the proposed *two-state algorithm*: the ECG pattern will be divided into two types: (i) *plain durations* like P and T waves (low frequency components), which could be downsampled at a higher CR (*hCR*) and are labelled as *high-state*, and (ii) *complex durations* like QRS (high frequency components), which

could be downsampled at a lower CR (*lCR*) and are labelled as *low-state*. As a result, a more optimized overall compression ratio (*oCR*) could be achieved for the signal. In this algorithm, the values of *hCR* and *lCR* have to satisfy:

$$hCR = n * lCR$$ with n being an interger and n $\geq$ 1, which will be further explained in the next section.

To keep consistency while presenting the method and evaluating the results, the terms "*plain*" and "*complex*" in this section, which were first propounded by Kim. et.al. [34] will be used along with *hCR*, *lCR*,*oCR*, *Thr1* and *Thr2* terminologies in this paper.
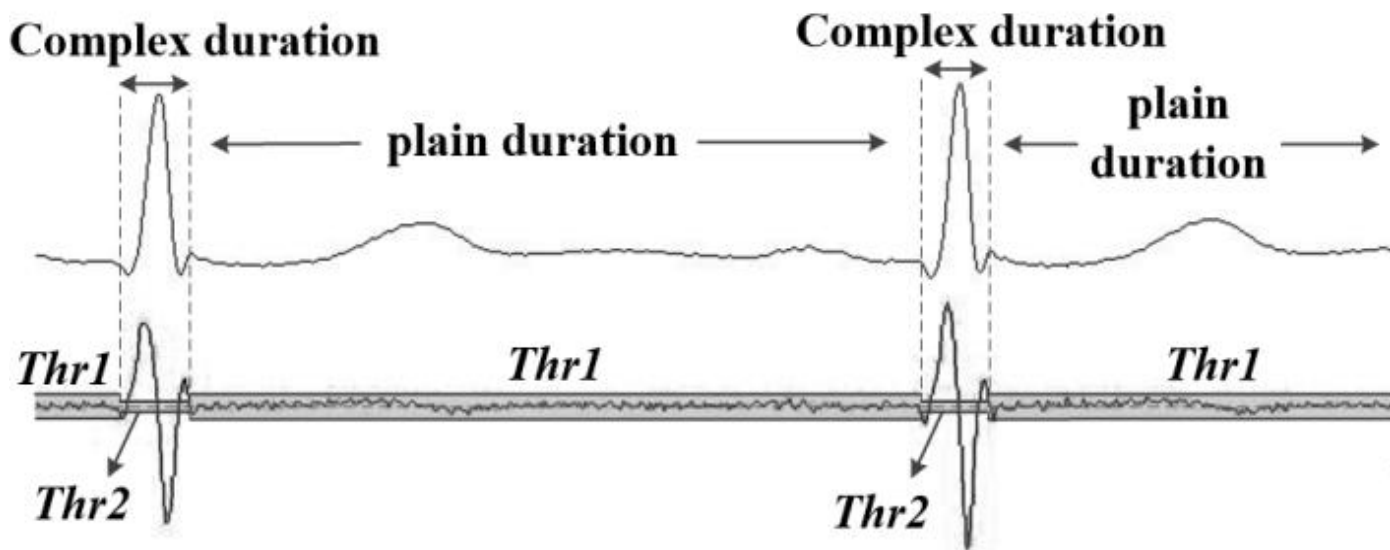

Figure 1. Record 103 of MIT-BIH arrhythmia database (above), its first derivative (below).Tthe complex durations and plain durations are distinguished by two thresholds in the first derivative signal

An overview of the proposed two-*state* algorithm is presented in Figure 2. There are four major compressing steps and three major decompressing steps. For the compressing steps, a block with the length of **L = hCR** samples is continuously scanned throughout the first derivative of the signal (Figure 1). The block is first classified as a *low-state* or *high-state* block (procedure 1), then compressed with **hCR** or **lCR** based on its *state*, but storing the *backward differences* instead of the ECG samples (procedure 2). Next, some special samples, called *state-changed-markers*, are added to mark a change of *state* if available(procedure 3). This finally, represents the *backward differences* to

improve the overall CR (procedure 4). At the end of the process, this block will be compressed to only one sample in case of *high-state* or n = **hCR/lCR** samples in case of *low-state* before moving to the next block. This kind of sample-unit process can help the system to control the size of the package easily and continuously in extremely short time.

For the decompression process, the recipient compressed signals will be reclassified based on the marking samples (procedure 5), followed by inversing the difference to get complete ECG samples (procedure 6) and reconstructed using Cubic Spline (procedure 7).
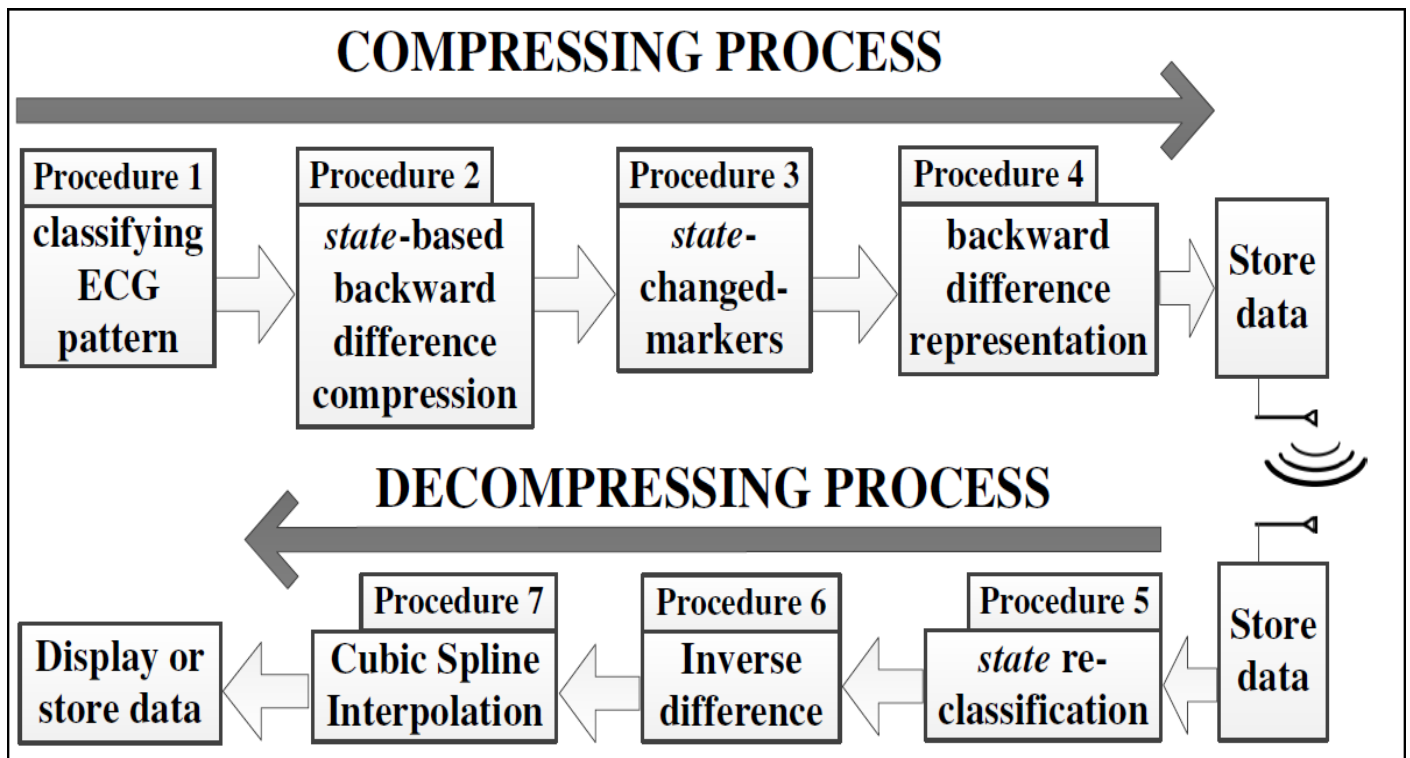
Figure 2. The overview of the advanced two-state algorithm.

2.2 Classification of ECG patterns (state-classifying).

As mentioned above, a block of $L = hCRy'$ samples (the first derivative samples) will be compared to two thresholds **Thr1** and **Thr2** before being labelled as a *low-state* or a *high-state* block. There are two main steps involved in this process, which is presented below (Figure 3):
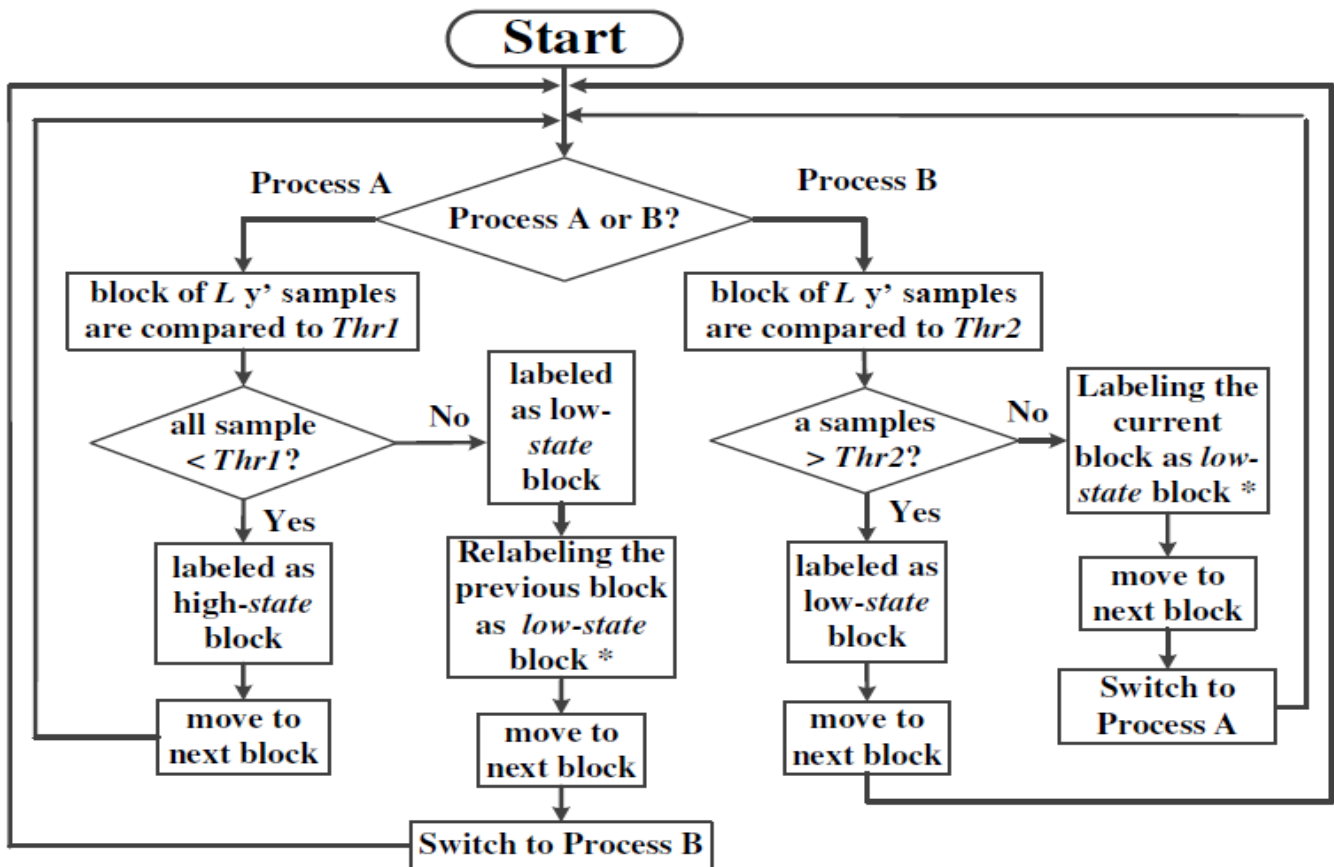
2.2.1 Process A (*high-state* classification)

First, a block of L consecutive y' samples are compared to **Thr1**. If all these samples satisfy the condition: $y'_i < Thr1$, with i = 0,1,...,L−1, then this block is classified as a *high-state* block since it only contains *plain* data. In contrast, if at least one component exceeds **Thr1**, this will be labelled as the first *low-state* block, marking an end of a *plain duration* and the program will switch to process B.

2.2.2 Process B (*low-state* classification)

Here, all the subsequent y' samples will be compared to the smaller value **Thr2**. If a block has at least one sample bigger than **Thr2**, it is still considered to be in *low-state duration*. In contrast, if all samples within a block are smaller than **Thr2**, then the previous block will be the final *low-state* block and the program is switched back to process A. Moreover, since **lCR** will be applied for these blocks, **lCR** must be a divisor of **hCR** to match the size of the block.

To guarantee a full capture, the *low-state duration* is extended by one block on each side. The structure of each block and the corresponding conditions are also presented in Figure 4.

Figure 3. Flowchart of the ECG pattern classification (state classification) procedure presenting two processes: Process A for high-state classification (left branch) and Process B for low-state classification (right branch).

Figure 4. The structure of classified blocks within each type of duration. Noting that the low-state durations are expanded to each side by 1 block which is originally a high-state block.

We also tested with all 48 records of MIT-BIH arrhythmia database to find suitable **Thr1** and **Thr2**, and we found that **Thr1 = 10** and **Thr2 = 0.3×Thr1** would be the best conditions to capture enough *complex durations*. Examples of classifying ECG patterns with $L = hCR = 8$ in records 102, 107, 119 and 123 are shown in Figure 5.
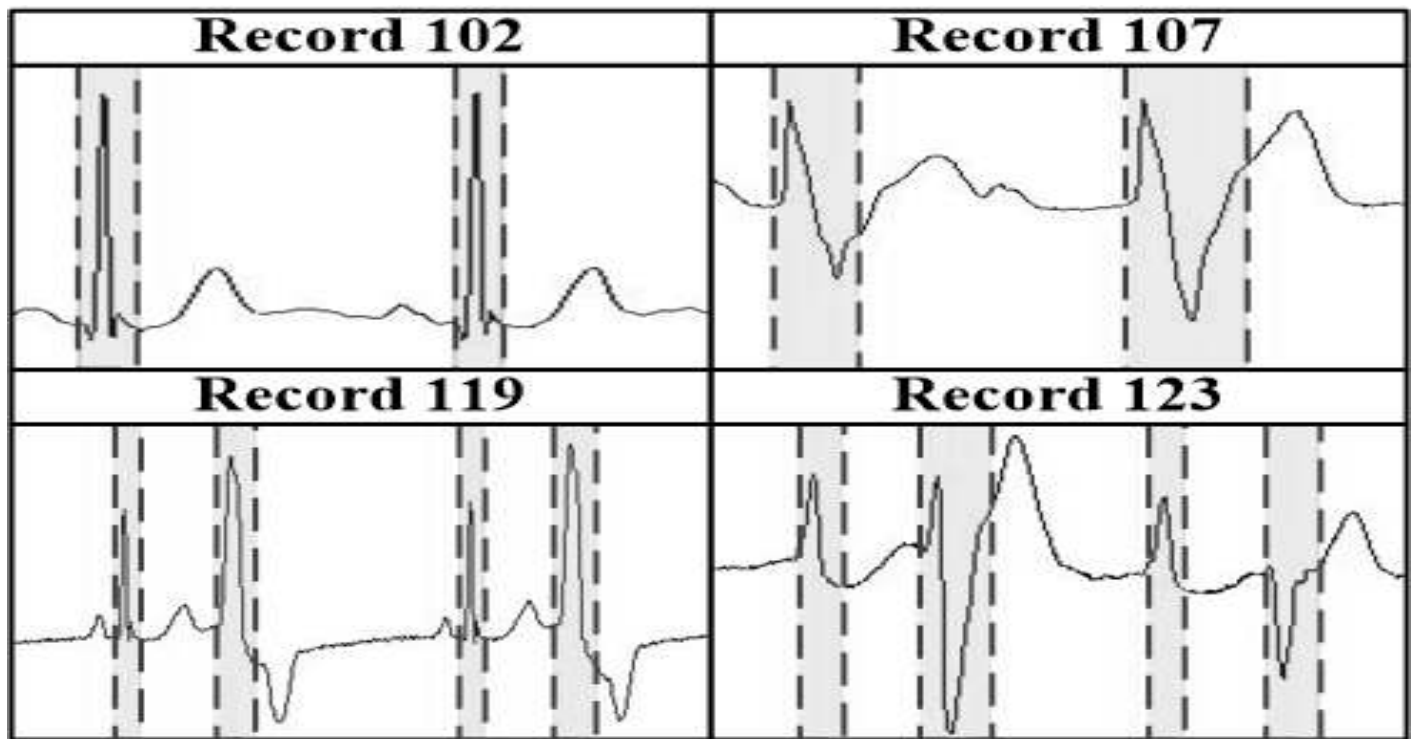
Figure 5. Examples of classifying ECG patterns(**hCR = 8**, **Thr1** = 10) in recordings 102, 107, 119 and 123 with grey durations representing the low-state durations.

2.3 State-based backward difference compression

After classification, the corresponding block will be compressed depending on its *state*. If it is a *high-state block*, only the first sample is stored while the remaining samples within that block will be removed (downsample factor = *hCR*). Conversely, in case of a *low-state block*,this block will be downsampled with a lower downsample factor = *lCR*, or in other words, there will be $\frac{hCR}{lCR}$samples within a *low-state block,* which will be saved into the compressed package.In addition, each compressed ECG samples except the first one will be immediately replaced by the difference between itself and its previous sample, called the *backward difference*: $\Delta\tilde{y}_i = \tilde{y}_{i+1} - \tilde{y}_i$, with $\tilde{y}_{i+1}$ and $\Delta\tilde{y}_i$ is the $(i+1)^{th}$ samples of the compressed package and its backwards difference. A full overview of this procedure is shown in Figure 6.

2.4 State-changed-markers

This procedure is an important part because it helps the receiver re-classify the pattern of the received package before reconstructing the signal.

Some special samples, called *state-changed-markers*, will be added into the intersections between *low-state durations* and *high-state durations*. Importantly, this procedure is only enabled when a switch from Process A to Process B (Procedure 1) or vice versa occurs, and the marking samples have to be unique in order to be recognized clearly. It is worth noting that these marking samples must have the same presentation as the ECG sample, and it is in 2-byte form in case of BIH-MIT arrhythmia database and CU ventricular tachyarrhythmia database.

Specifically, if a *high*-to-*low* transition occurs, then an *all-bit-1* sample, which has a decimal value of -32768 (signed form) in terms of 2-byte presentations, is added between the final *high-state* sample and the first *low-state* sample in the compressed package (Figure 6). In contrast, if a *low*-to-*high* happens, two marking samples will be inserted between the final *low-state* sample and the first *high-state* sample, including an *all-bit-1* sample and an *all-bit-0* sample (decimal value of 0) (Figure 6) to mark the end of a *low-state duration*.
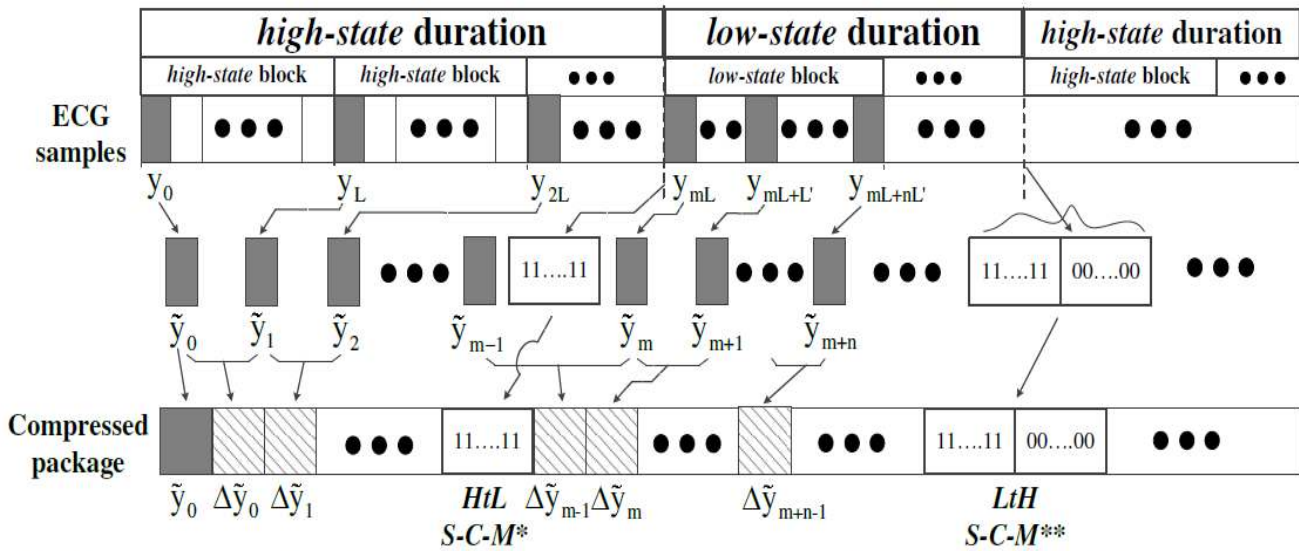
* **HtL S-C-M**: *state-changed-markers* indicate a transition from *high-state* to *low-state*, which is an *all-bit-1 sample* (= -32768 for 2-byte form)

** **LtH S-C-M**: *state-changed-markers* indicate a transition from *low-state* to *high-state*, which includes an *all-bit-1 sample* (= -32768) and an *all-bit-0 sample* (=0)

Figure 6. The compressed package structure. In a high-state block, only the first sample is reserved while in a low-state block, there will be n = hCR/lCR =L/L' samples are kept. Additionally, only the first sample is the ECG sample while the next samples are the backward differences: $\Delta\tilde{y}_i = \tilde{y}_{i+1} - \tilde{y}_i$, with $\tilde{y}_{i+1}$ and $\Delta\tilde{y}_i$ is the $(i+1)^{th}$ samples of the compressed package and its backwards difference.

2.5 Backward difference representation

This procedure will represent the compressed package, which possibly contains samples with 2-byte format, and convert samples into 1-byte format, if possible, to enhance the overall compression ratio (Figure 7). The backward differencesamples are considered subject to satisfying the condition: $-128 \le y_i' \le 127$. Samples that meet the demand could be shortened into 1-byte format without problems, while those that do not meet the criteria will be represented in 2-byte format, in which the first byte is -128 (if $y_i' < -128$) or 127 (if $y_i' > 127$), and the second byte stores the difference: $\Delta y' = |\Delta\tilde{y}| - 128$ (if $y_i' < -128$) or $\Delta y' = \Delta\tilde{y} - 127$ (if $y_i' > 127$). In case of *state-changed-markers*, *all-bit-1* sample will be reserved (2 bytes, each byte = -128), while *all-bit-0* sample will be shortened into 1 byte (1 byte = 0).

ECG sample (first sample)		Backward difference samples									
		Nor*	HtL**		< -128		Nor	> 127		LtH***		
2-byte		1-byte	2-byte		2-byte		1-byte	2-byte		2-byte		1-byte
Byte high	Byte low	$\Delta\tilde{y}$	-128	-128	-128	Res1[a]	$\Delta\tilde{y}$	127	Res2[b]	-128	-128	0

* **Normal**: $-128 \le y'$ sample ≤ 127

** **HtL**: *state-changed-markers* indicate a transition from *high-state* to *low-state*

*** **LtH**: *state-changed-markers* indicate a transition from *low-state* to *high-state*

[a]: Res1 $= |\Delta\tilde{y}| - 128$

[b]: Res2 $= \Delta\tilde{y} - 127$

Figure 7. The structure of backward difference representation.

2.6 State re-classification

After receiving a package, the receiver first checks the package to re-detect *complex durations* and *plain durations* based on *state-changed-markers*. The beginning of *complex duration* will be recognized by detecting two consecutive bytes of -128, while the end will be marked by two bytes of -128 and one byte of 0. Due to the fact that *state* changes alternatively, successfully re-classifying *complex durations* also lead to successfully re-detecting *plain durations*. The *state-changed-markers* are also simultaneously removed in this procedure.

2.7 Inverse difference

Before interpolating the compressed signal, the package needs to be reversed to ECG samples instead of samples of differences. Hence, each difference sample will be re-converted into 2-byte form and the corresponding ECG sample will be calculated based on the previous ECG sample and the difference, starting from the first ECG sample.

2.8 Cubic Spline Interpolation

Finally, the signal will be reconstructed using Cubic Spline noting that different durations will have different distances between samples.

3. Experiments and results

3.1 Indexes for evaluating compression algorithm

The performance of the proposed algorithm was evaluated by some common indexes presented below, which were also used by many other studies:

1) The compression ratio (CR):

$$CR = \frac{N_{origin}}{N_{comp}} \qquad (3)$$

N_{origin} is the original size and N_{comp} is the size of the compressed signal. The CR calculated here is the overall CR (*oCR*) after applying **hCR** and **lCR** to compress the whole signal.

2) Percentage RMS difference (PRD):

$$PRD(\%) = 100\% \times \sqrt{\frac{\sum_0^{N-1}(y_i - \hat{y}_i)^2}{\sum_0^{N-1}(y_i)^2}} \qquad (4)$$

This is also most commonly used to evaluate the performance of an ECG compression method.

3) Percentage RMS difference, normalized (PRDN):

$$PRDN(\%) = 100\% \times \sqrt{\frac{\sum_0^{N-1}(y_i - \hat{y}_i)^2}{\sum_0^{N-1}(y_i - \bar{y})^2}} \qquad (5)$$

$\bar{y}$ is the average of the original data.

4) Root mean square error (RMS):

$$RMS = \sqrt{\frac{\sum_0^{N-1}(y_i - \hat{y}_i)^2}{N-1}} \qquad (6)$$

5) Signal-to-noise ratio (SNR):

$$SNR = 10 \times \log\left(\frac{\sum_0^{N-1}(y_i - \bar{y})^2}{\sum_0^{N-1}(y_i - \hat{y}_i)^2}\right) \qquad (7)$$

6) Peak Maximum Absolute Error(PMAE):

Of note, we also proposed a new index to support the evaluation of the attenuation level of P, R and T peaks known as the *Peak Maximum Absolute Error* (PMAE) presented below:

$$PMAE = \frac{y_{peak} - \hat{y}_{peak}}{\Delta y_{max}} \times 100\% \qquad (8)$$

With: $\quad \Delta y_{max} = \max(y_i | i = n_1, .., n_2) - \min(y_i | i = n_1, .., n_2) \quad (8)$

y_{peak} is the P, R or T peak of the original data, $\hat{y}_{peak}$ is the P, R or T peak of the reconstructed data, n_1 and n_2 are the starting index and the final index of the corresponding duration containing this peak (P wave, QRS or T wave), respectively. Δy_{max} is the maximum difference of this wave from index n_1 to index n_2 of the original data. This index aims to compare each peak's attenuation level to the maximum difference of the wave holding that peak. Therefore, a high PMAE, about 10% and above, could lead to clear visibility of attenuation in shape and affect the outcome of the medical diagnosis.

3.2 Experiments with MIT-BIH arrhythmia database

The first lead of all 48 MIT-BIH arrhythmia records with values ranging from 0 to 2048 were compressed and decompressed by the *two-state* algorithm, in which 4 different ratios of **hCR / lCR** from 2 to 5 were tested. These included (**hCR-lCR**) 2-2, 4-2, 6-2, 8-2, 10-2, 6-3, 9-3, 12-3, 15-3, 8-4, 12-4, 16-4, 20-4, 10-5, 15-5, 20-5 and 25-5, and two thresholds **Thr1** = 10and **Thr2** = 0.3 x **Thr1** = 3. To evaluate the whole signal reconstruction, CR (overall compression ratio - **oCR**), PRD, PRDN, RMS and SNR were calculated for the full period of 30 minutes for each record. Moreover, to assess the influence of the selection of two compression ratios (**hCR** and **lCR**) in re-building the signal, 10 consecutive P waves, T waves and QRS of each recording were surveyed through PRD, and 10 consecutive P, R

and T peaks were assessed for their attenuation through PMAE. The overall performance of the algorithm in compressing and reconstructing all 48 arrythmia records is presented in Figure 8.

In terms of overall CR (**oCR**), although an increase in both **hCR** and **lCR** led to an increase in **oCR**, when **hCR** was large enough (**lCR** ≥ 15), the **oCR** showed no further signifcant improvements, such as in cases of **hCR-lCR** (**oCR**)16-4 (14.125) versus 20-4 (14.046), or 15-5 (15.556) versus 20-5 (15.932) versus 25-5 (15.559). Generally, the increase in the ratio **hCR/lCR** from 2 to 5 caused an increase on average by 0.6% in PRD, 1.5% in PRDN, 0.45 bit in RMS and a decrease on average by 2.75dB in SNR in all cases of **lCR**. Table 1 shows the detailed results of five indexes of each recording with two cases of **hCR-lCR** = 25-5.

hCR - lCR	4 - 2	6 - 2	8 - 2	10 - 2	6 - 3	9 - 3	12 - 3	15 - 3	8 - 4	12 - 4	16 - 4	20 - 4	10 - 5	15 - 5	20 - 5	25 - 5
CR*: Avr	6.384	8.068	9.037	9.512	9.052	11.028	11.909	12.129	11.439	13.478	14.125	14.046	13.597	15.556	15.932	15.559
(SD)	(0.321)	(0.722)	(1.108)	(1.428)	(0.532)	(1.126)	(1.646)	(2.033)	(0.769)	(1.534)	(2.148)	(2.544)	(1.007)	(1.914)	(2.566)	(2.879)
▬ PRD (%)**	0.124	0.157	0.184	0.195	0.180	0.207	0.224	0.232	0.258	0.274	0.288	0.306	0.362	0.373	0.393	0.420
▬ PRDN (%)**	3.797	4.781	5.560	5.876	5.454	6.246	6.736	6.946	7.763	8.230	8.611	9.149	10.818	11.125	11.693	12.499
▭ RMS(bit)**	1.227	1.557	1.818	1.924	1.782	2.050	2.211	2.291	2.556	2.713	2.848	3.031	3.581	3.692	3.884	4.149
▭ SNR(log₂₅)**	29.351	27.130	25.708	25.213	26.063	24.708	24.022	23.710	22.933	22.361	21.912	21.340	20.129	19.816	19.313	18.682

* Overall compression ratio of the data after applying two different ratios hCR and lCR

** PRD, PRDN, RMS and SNR in the table were the average values

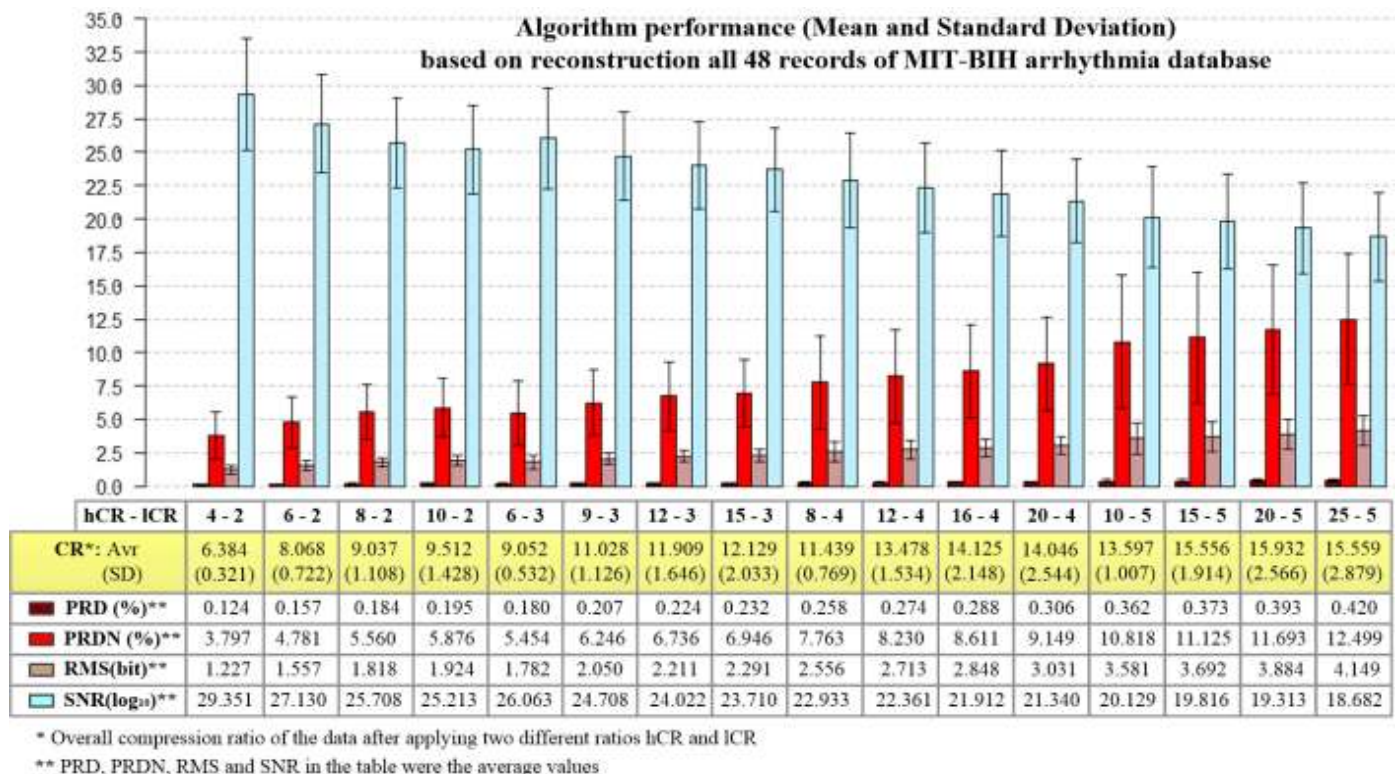**Figure 8.** The overall performance of the proposed algorithm through five evaluation indexes of all 48 records of MIT-BIH arrhythmia database

Refering to PRD boxplots of a total of 480 P waves, QRS complexes and T waves of all 48 records (Figure 9), it seemed that reconstructions

of QRS results were very stable among cases with the same **lCR**, but there were a big difference in both the median value and the data

range between *lCR* = 2, 3, 4 and 5. Except for some outliers, the PRD results of QRS were all smaller than 0.5% if *lCR* < 4 was selected and below 1% with *lCR* = 4.

With the highest *lCR* of 5, only 75% of all QRScomplexes were re-built with PRD below 1%, and this result will heavily affect medical diagnosis. In contrast, the PRD results of P waves and T waves expanded proportionally mostly to the rise in *hCR*, but not in *lCR*, and the level of the data's expansion was much lower in all cases with PRD being smaller than 0.75%, except for a very small number of outliers.

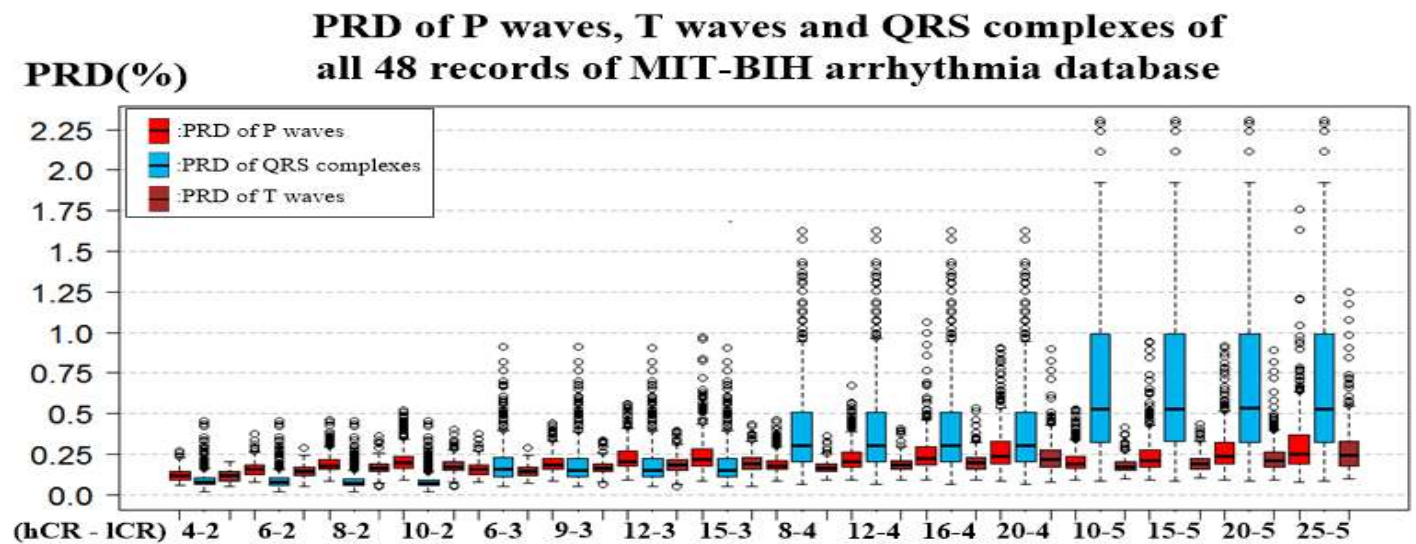

Figure 9. PRD of a total of 480 P waves, T waves and QRS complexes of all 48 records of MIT-BIH arrhythmia database
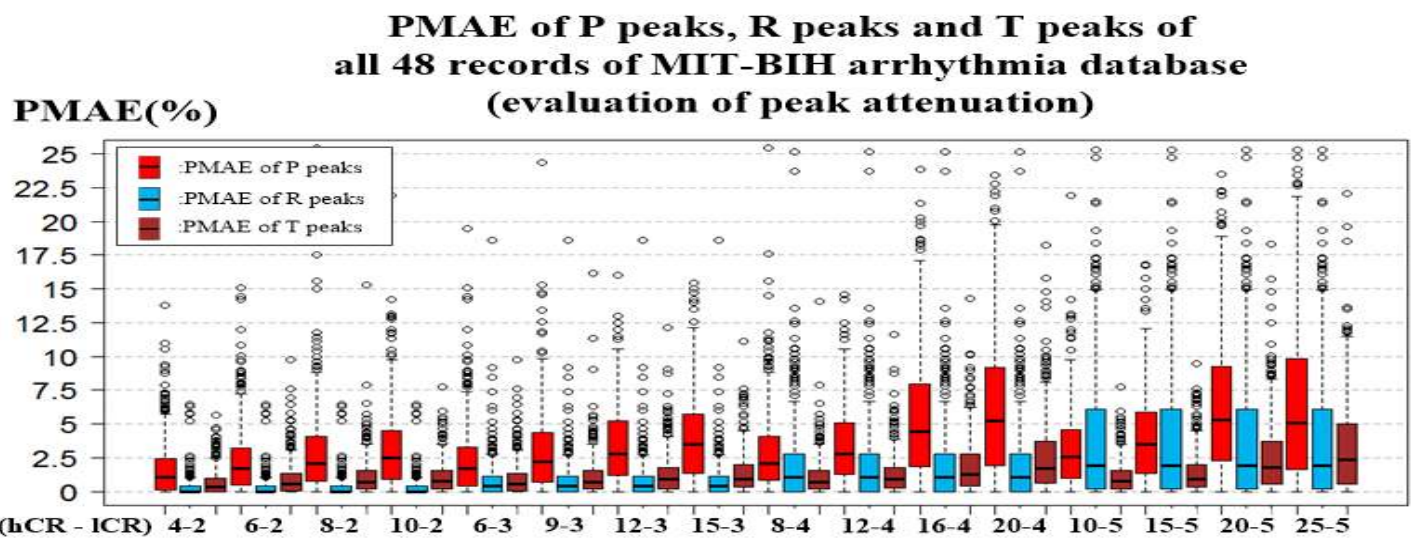

Figure 10. PMAE of a total of 480 P, R and T peaks of all 48 records of all 48 records of MIT- BIH arrhythmia database

In terms of attenuation of the peaks (Figure 10), the PMAE of R peaks were almost under 10% (a value that could lead to medical misintepretation) except for a very small number of outliers with *lCR* ≤ 4. In contrast, higher PMAE results of both the median value and the range were found in T peaks and especially in P peaks when compared to R peaks within the same cases. Nevertheless, with *lCR* ≤ 4 and *hCR* ≤ 10, all peaks could obtain less than 10% PMAE as shown in Figure 10.

Figure 11, 12, 13 and 14 respectively exhibit the reconstruction of record 113 (with worst PRD), record 117, record 119 and record 112 (with best PRD) after compression by the proposed algorithm with four *hCR- lCR* of 10-2, 15-3, 20-4 and 25-5. The differences became visually clear when **lCR**> 3 in record 113 however, no significant differences were seen between all 4 cases for other 3 records.

Table 1. Overall CR, PRD, PRDN, RMS, SNR of 48 records of MIT-BIH arrhythmia after decompressing with hCR/lCR = 25-5

| Rec.	CR	PRD	PRDN	RMS	SNR	Rec.	CR	PRD	PRDN	RMS	SNR
100	17.538	0.418	21.023	4.154	13.545	201	19.456	0.239	12.126	2.409	18.325
101	18.600	0.410	15.273	4.083	16.321	202	17.018	0.270	8.927	2.719	20.985
102	15.881	0.491	25.145	4.903	11.989	203	11.444	0.440	8.743	4.435	21.166
103	17.353	0.423	12.859	4.236	17.815	205	15.872	0.340	16.810	3.384	15.488
104	14.667	0.642	25.078	6.428	12.013	207	17.503	0.337	9.366	3.395	20.568
105	14.225	0.410	9.916	4.113	20.072	208	12.299	0.447	9.126	4.506	20.793
106	15.063	0.469	12.549	4.725	18.027	209	12.136	0.486	17.869	4.903	14.957
107	10.393	0.543	6.215	5.458	24.130	210	15.220	0.271	10.226	2.733	19.805
108	16.339	0.427	13.875	4.274	17.155	212	11.277	0.585	17.414	5.901	15.181
109	13.945	0.305	5.990	3.058	24.450	213	10.402	0.435	6.361	4.370	23.929
111	15.813	0.304	11.667	3.070	18.660	214	13.650	0.344	7.214	3.472	22.835
112	15.859	0.301	7.235	1.655	22.811	215	10.355	0.378	13.205	3.812	17.584
113	17.297	0.718	17.148	7.241	15.315	217	11.624	0.481	7.699	4.854	22.270
114	18.825	0.340	19.563	3.431	14.170	219	16.678	0.456	7.807	4.406	22.149
115	17.925	0.519	13.607	5.060	17.324	220	17.502	0.628	18.682	6.090	14.571
116	13.231	0.671	9.183	6.245	20.740	221	15.326	0.301	9.838	3.029	20.141
117	21.069	0.331	12.679	3.102	17.938	222	15.969	0.394	20.925	3.977	13.586
118	12.408	0.593	12.680	5.555	17.937	223	15.062	0.353	8.238	3.431	21.682
119	15.946	0.551	9.427	5.167	20.512	228	16.001	0.354	10.093	3.577	19.919
121	20.662	0.416	12.703	3.919	17.921	230	16.060	0.370	10.284	3.732	19.756
122	14.504	0.375	9.408	3.523	20.529	231	19.985	0.438	15.888	4.422	15.978
123	20.465	0.443	14.045	4.176	17.049	232	18.739	0.306	18.256	3.087	14.771
124	19.561	0.281	5.599	2.647	25.037	233	12.244	0.373	6.771	3.767	23.386
200	12.586	0.398	10.387	4.041	19.669	234	14.836	0.313	9.138	3.157	20.782
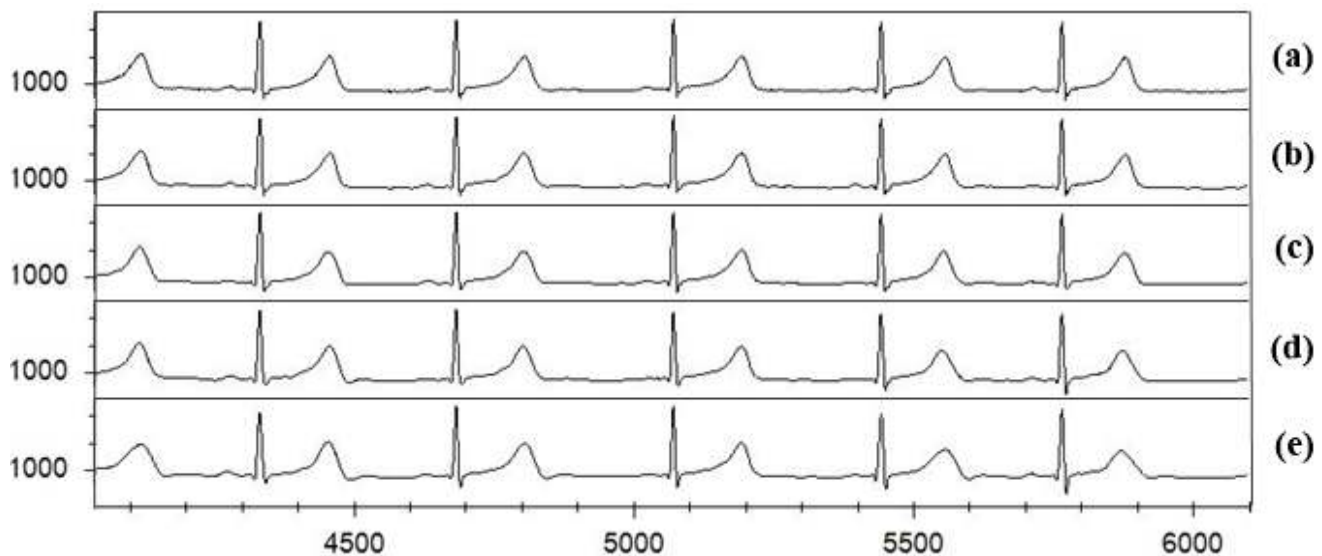
Figure 11. Reconstruction of record 113 (worst PRD) at different compression ratios. (a) Original data, (b) **hCR/lCR** = 10-2, CR = 10.72, PRD = 0.179%, (c) **hCR/lCR** = 15-3, CR = 13.73, PRD = 0.264% (d) **hCR/lCR** = 20-4, CR = 15.86, PRD = 0.453% (e) **hCr/lCR** = 25-5, CR = 17.29, PRD = 0.718%.
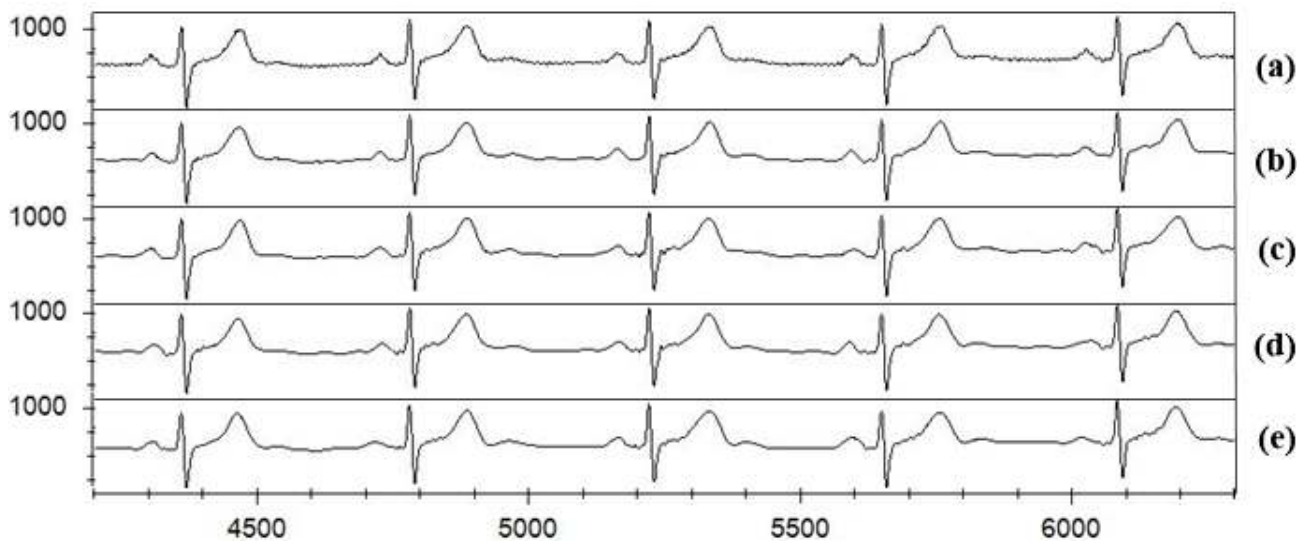

Figure 12. Reconstruction of record 117 at different compression ratios. (a) Original data, (b) **hCR/lCR** = 10-2, CR = 11.86, PRD = 0.213%, (c) **hCR/lCR** = 15-3, CR = 15.78, PRD = 0.225% (d) **hCR/lCR** = 20-4, CR = 18.82, PRD = 0.254% (e) **hCr/lCR** = 25-5, CR = 21.06, PRD = 0.331%.

3.3 Experiments with CU ventricular tachyarrhythmia database

A period of 1-minute of each record in 9 ventricular tachyarrhythmia records (CU04, CU06, CU07, CU10, CU12, CU16, CU20, CU22, CU24), which do not have clear PQRST shapes and have values ranging from 0 to 4095, was extracted, compressed and decompressed by our algorithm with the same parameters used in MIT-BIH arrythmia database. For evaluation, the overall CR, PRD, PRDN, RMS and SNR were chosen.

It can be seen that there were minor variances (small standard deviations) in all five indexes with all values of *lCR* ranging from 2 to 5 in 9 records. Moreover, all recordings experienced the same tendency of continous increase in PRD (an average of ~0.12%) , PRDN (~ 2%) and RMS (~ 6 bits), and a decrease of SNR (~ 6dB) when increasing *lCR* by 1, except for CU04 and CU20

whose indexes were relatively consistent when changing *lCR.*

There were also examples of the reconstruction of CU04 (best PRD) (Figure 15) and CU12 (worst PRD) (Figure 16) with *hCR-lCR* = 10-2, 15-3, 20-4 and 25-5. It is difficult to visually recognize the real differences in the reconstruction in all five cases, including record CU12 although its PRD was 3.914% at the highest compression ratios (when *hCR-lCR* = 25-5).
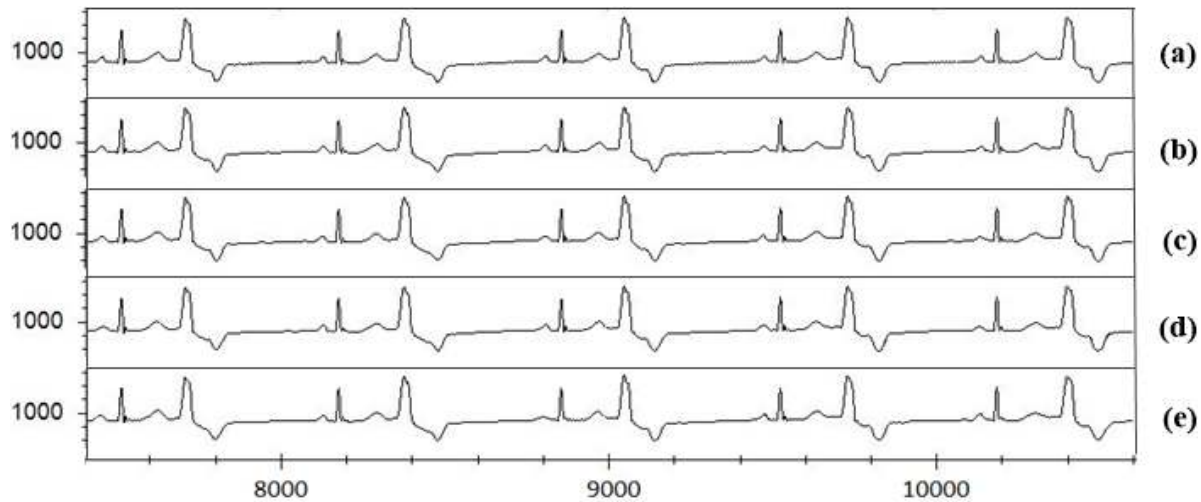
Figure 13. Reconstruction of record 119 at different compression ratios. (a) Original data, (b) **hCR/lCR** = 10-2, CR = 10.08, PRD = 0.226%, (c) **hCR/lCR** = 15-3, CR = 12.81, PRD = 0.282% (d) **hCR/lCR** = 20-4, CR = 14.56, PRD = 0.390% (e) **hCr/lCR** = 25-5, CR = 15.94, PRD = 0.551%.

Figure 14. Reconstruction of record 201 (best PRD) at different compression ratios. (a) Original data, (b) **hCR/lCR** = 10-2, CR = 11.33, PRD = 0.129%, (c) **hCR/lCR** = 15-3, CR = 14.75, PRD = 0.152% (d) **hCR/lCR** = 20-4, CR = 17.37, PRD = 0.188% (e) **hCr/lCR** = 25-5, CR = 19.45, PRD = 0.239%

Figure 15. Reconstruction of record CU04 (best PRD) at different compression ratios. (a) Original data, (b) **hCR-lCR** = 10-2, CR = 3.99, PRD = 0.022%, (c) **hCR-lCR** = 15-3, CR = 5.98, PRD = 0.034%, (d) **hCR-lCR** = 20-4, CR = 7.91, PRD = 0.048%, (e) **hCR-lCR** = 25-5.
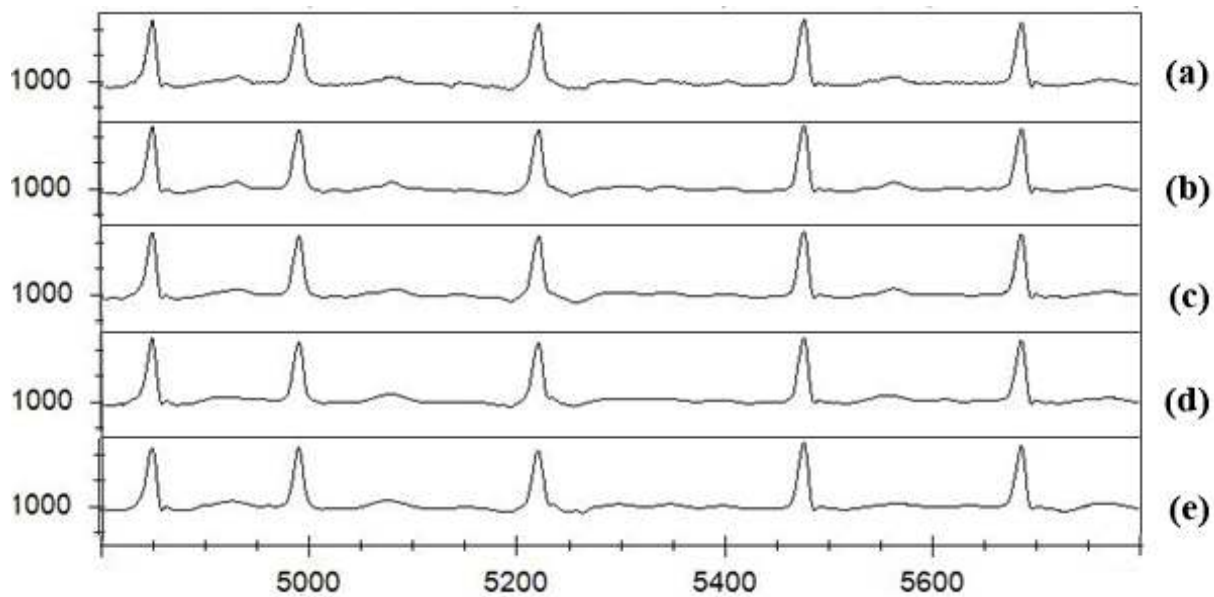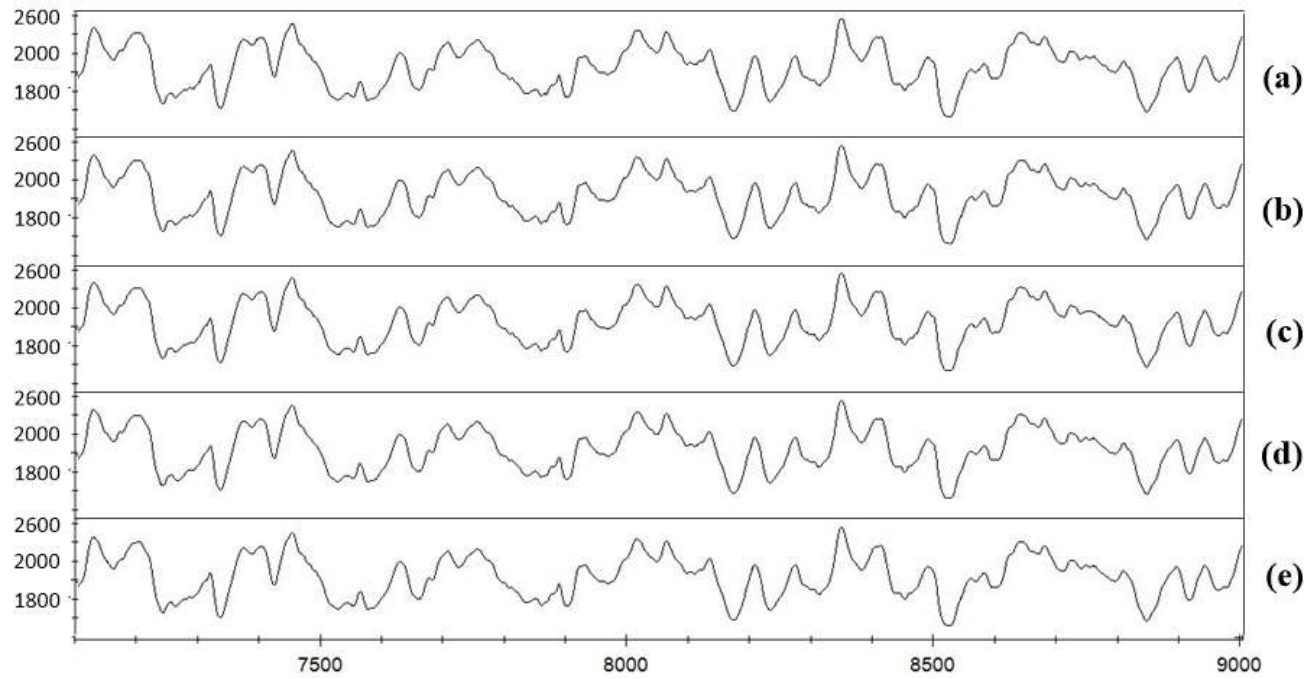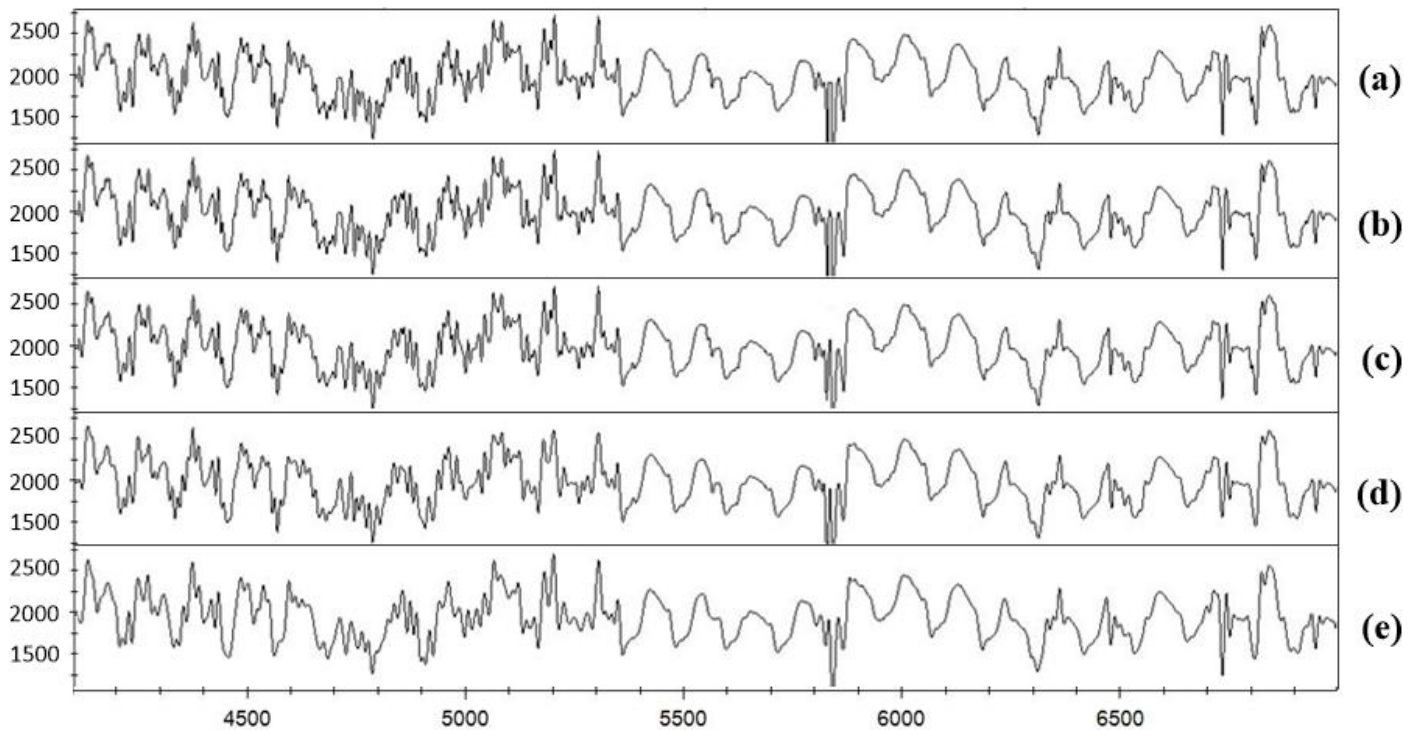

Figure 16. Reconstruction of record CU12 (worst PRD) at different compression ratios. (a) Original data, (b) hCR-lCR = 10-2, CR = 3.37, PRD = 0.938%, (c) hCR-lCR = 15-3, CR = 4.783, PRD = 1.542%, (d) hCR-lCR = 20-4, CR = 6.09, PRD = 2.803%, (e) hCR-lCR = 25-5, CR = 7.24, PRD = 3.914%.

Table 2. Overall CR, PRD, PRDN, RMS and SNR of 10 reconstructed records (CU ventricular tachyarrhythmia database). Results of cases having the same lCR were grouped in one group expressed by mean value and standard deviation.

Rec.	lCR	CR		PRD		PRDN		RMS		SNR	
		M	*SD*	*M*	*SD*	*M*	*SD*	*M*	*SD*	*M*	*SD*
CU04	2[a]	3.953	0.065	0.023	0.002	0.441	0.046	0.949	0.100	47.16	0.936
	3[b]	5.948	0.057	0.031	0.005	0.595	0.009	1.282	0.193	44.58	1.277
	4[c]	7.900	0.036	0.046	0.004	0.875	0.074	1.885	0.160	41.18	0.720
	5[d]	9.625	0.012	0.067	0.001	1.280	0.016	2.759	0.036	37.85	0.112
CU06	2	3.916	0.010	0.065	0.001	0.949	0.001	2.693	0.001	40.46	0.004
	3	5.492	0.012	0.153	0.001	2.213	0.001	6.281	0.001	33.10	0.001
	4	6.769	0.008	0.295	0.001	4.279	0.001	12.15	0.001	27.37	0.001
	5	7.888	0.009	0.426	0.001	6.183	0.001	17.55	0.001	24.17	0.001
CU07	2	3.862	0.071	0.068	0.001	1.147	0.014	1.407	0.018	38.81	0.110
	3	5.481	0.071	0.156	0.001	2.620	0.022	3.125	0.026	31.63	0.071
	4	6.931	0.024	0.367	0.001	6.157	0.005	7.554	0.006	24.21	0.007
	5	8.279	0.004	0.792	0.003	13.29	0.043	16.30	0.052	17.53	0.028
CU10	2	3.736	0.001	0.112	0.001	1.002	0.003	2.640	0.010	39.98	0.029
	3	5.084	0.001	0.481	0.001	3.963	0.001	10.44	0.001	28.04	0.001
	4	6.258	0.001	0.978	0.001	8.049	0.001	21.23	0.001	21.89	0.001
	5	7.358	0.001	1.581	0.001	13.01	0.001	34.33	0.001	17.71	0.001
CU12	2	3.372	0.003	0.938	0.001	4.221	0.001	20.69	0.001	27.49	0.001
	3	4.785	0.003	1.542	0.001	6.937	0.001	34.01	0.001	23.18	0.001
	4	6.092	0.002	2.803	0.001	12.61	0.001	61.82	0.001	17.99	0.001
	5	7.239	0.001	3.914	0.001	16.80	0.001	82.37	0.001	15.50	0.001
CU16	2	2.797	0.001	0.356	0.001	1.266	0.001	7.592	0.001	37.95	0.001
	3	3.737	0.001	1.073	0.001	3.817	0.001	22.90	0.001	28.36	0.001
	4	4.711	0.001	1.862	0.001	6.625	0.001	39.74	0.001	23.58	0.001
	5	5.708	0.001	2.895	0.001	10.12	0.001	61.66	0.001	19.74	0.001
CU20	2	4.193	0.052	0079	0.004	0.399	0.022	1.634	0.009	48.00	0.474
	3	5.876	0.034	0.129	0.006	0.655	0.031	2.687	0.129	43.88	0.415
	4	7.535	0.049	0.222	0.007	1.125	0.036	4.612	0.147	38.98	0.275
	5	9.011	0.081	0.292	0.007	1.478	0.033	6.057	0.138	36.61	0.196
CU22	2	3.778	0.009	0.964	0.001	6.893	0.001	20.30	0.002	23.23	0.001
	3	5.163	0.007	1.658	0.001	11.79	0.001	34.90	0.002	18.52	0.001
	4	6.316	0.007	1.787	0.010	12.54	0.003	37.72	0.010	18.03	0.002
	5	7.363	0.009	2.418	0.001	16.97	0.001	51.02	0.008	15.41	0.001
CU24	2	3.933	0.101	0.606	0.001	5.033	0.001	12.69	0.001	25.95	0.001
	3	5.398	0.118	1.162	0.001	9.665	0.001	24.33	0.001	20.30	0.001
	4	6.749	0.135	1.636	0.010	13.59	0.001	34.26	0.001	17.34	0.001
	5	8.081	0.152	1.923	0.001	15.98	0.001	40.29	0.001	15.93	0.001

[a]: Group of cases having *lCR* = 2: 2/2, 4/2, 6/2, 8/2, 10/2.
[b]: Group of cases having *lCR* = 3: 6/3, 9/3, 12/3, 15/3.
[c]: Group of cases having *lCR* = 4: 8/4, 12/4, 16/4, 20/4.
[d]: Group of cases having *lCR* = 5: 10/5, 15/5, 20/5, 25/5.

4. Discussion

4.1 The influence of choosing compression ratios on the algorithm's performance

As seen in Figure 8, the overall performance of the algorithm applied in MIT-BIH arrhythmia database showed its dependence on the selection of *hCR* and *lCR*. Although *lCR* had a greater impact on the overall results than *hCR*, their roles were determined more clearlywhen looking at the reconstruction of each feature including P wave, QRS complex, T wave and their peaks. While P and T waves were mostly affected by *hCR*, the peak of *lCR* completely influenced the reconstruction of QRS complexes. However, despite the fact that the R peaks were maintained very well at *lCR* = 4 with PAME < 10%, the shapes of QRS complexes were only reconstructed well with *lCR* < 4 with PRD < 0.75%. Therefore, based on the results, it seems that *lCR* = 3 should be the highest possible CR applied for *complex durations* to avoid any significant errors. Regarding *hCR*, although the shape of P and T waves were well preserved even at the highest *hCR* of 25 with PRD < 0.75% except for very few cases, the PMAE of P and T peaks started to exceed 10% at *hCR*> 10. However, it is important to note that because the 60Hz noises are still present in all records, many P and T peaks are not quite correctly detected and this could have affected the PMAE results. Hence, *hCR* could be expanded to 15 with most of the P peaks were attenuated by less than 12.5% of the waves maximum. Therefore, *lCR* = 3 and *hCR* = 15 corresponding with PMAE < 10%, PRD < 0.75% should be the limitations for the reconstruction of 11-bit ECG signals (value ranging from 0 to 2047). This is for critical applications that are needed to preserve the ECG signals well for diagnosis and critical treatment.

In CU ventricular tachyarrhythmia database, which offered more difficult curves with unclear PQRST, the role of *lCR* was shown to be dominant over *hCR* since all indexes were determined solely by *lCR*. Meanwhile, the change of *hCR* only created a very small variance. In addition, an increase by 1 unit in *lCR* also heavily affected the performance of the algorithm. It seemed that *lCR* = 3 should be a safe choice for such difficult conditions such as CU ventricular tachyarrhythmia.

4.2 The versatility of the algorithm

The proposed algorithm was proven to be applicable for different kinds of ECG without depending on detecting or extracting any features of ECG. The results obtained from the assessment of MIT-BIH arrhythmia and CU ventricular tachyarrhythmia databases were also very positive with an acceptable level of error at moderate compression ratios. Moreover, the algorithm also offers an extremely low-cost computational compressing and decompressing method. Specifically, with N being the size of original data and M being the size of compressed data, there are only N equations that need to be calculated in the compressing method for finding the first derivative of the signal, with only one operation (-) in each equation, and M equations in minimum to compress and store data. In the decompressing method, the time of calculation is nearly equal to the time of calculating the inverse difference (~2M equations) and executing Cubic Spline Interpolation (O(M) equations in minimum if using LU decomposition to solve), since the first procedure of re-classifying *state* consumes a very short time. This will provide redundant time for the system to implement other digital processing if needed. Besides that, the compressed package can stop at any size (number of bytes) due to its block-unit processing mechanism without affecting the reconstruction at the receiver. Therefore, the algorithm is very suitable for use in many wireless applications as a step, such as an optimization solution to handle congested network as seen in ECG data.

4.3 Performance comparison

The proposed *two-state* algorithm was compared to other loss-type methods, which were also applied in MIT-BIH arrhythmia database in cases of CR < 25 (table 3). Together, the results prove the great performance of our proposed algorithm with CR < 25 compared to many other methods, even including some TD methods which exhibited very promising results. However, as be seen in comparison with the Miaou et. al. algorithm[32] at CR > 18 which has far excellent

performance, the proposed algorithm cannot ensure the quality of reconstruction at high CR as perfectly as some TD methods or H methods containing error minimization mechanism embedded in. In exchange, those methods are much more complex compared to the proposed algorithm and cannot adapt various sizes of the compressed packages like the proposed algorithm does.

Table 3. Performance comparison of different loss-type ECG compression schemes in record 100, 117 and 119. In each record, the similarity of CR produced by different methods was grouped in 1 group and the order ranges from highest PRD (at the top of each group) to lowest PRD (at the bottom of the corresponding group). The proposed method was abbreviated as Proposed (hCR-lCR) and was highlighted in bold.

Record	Method	CR	PRD	Record	Method	CR	PRD
100	Husoy et. al.[27]	23.5:1	12	101	**Proposed (28-7)**	**23.7:1**	**16.19***
100	Lee et. al.[47]	24:1	8.10	101	Miaou et.al. ($\varepsilon = 5\%$) [32]	25.4:1	8.97*
100	Chou et. al. app.2 [46]	24:1	4.06	101	Miaou et.al. ($\varepsilon = 10\%$) [32]	24.8:1	8.89*
100	Filho et. al. app.3 [48]	24:1	3.95	101	**Proposed (32-4)**	**17.6:1**	**8.21***
100	SangJoon Lee et. al. [29]	23:1	1.94	101	Miaou et.al. ($\varepsilon = 5\%$)	19.3:1	5.98*
100	**Proposed (30-10)**	**24.5:1**	**1.29**	101	Miaou et.al. ($\varepsilon = 10\%$)	18.8:1	5.9*
100	Istepanian et. al. [30]	18.3:1	0.60	101	Miaou et.al. ($\varepsilon = 5\%$)	9.73:1	2.98*
100	**Proposed (18-6)**	**18.8:1**	**0.57**	101	Miaou et.al. ($\varepsilon = 10\%$)	9.33:1	2.98*
100	Kim et. al. [34][a]	15:1	0.46	101	**Proposed (8-2)**	**10.1:1**	**2.89***
100	**Proposed (10-5)[a]**	**14.4:1**	**0.37**	103	Kim. et. al.[a]	15:1	0.82
100	Filhoet. al. app.3	10:1	2.12	103	**Proposed (16-4)[a]**	**15.3:1**	**0.22**
100	SangJoon Lee et. al.	9.6:1	0.44	104	Kim. et. al.[a]	15:1	0.88
100	**Proposed (8-2)**	9.9:1	0.14	104	**Proposed (20-5)[a]**	**14.7:1**	**0.69**
100	Istepanian et. al.	8.1:1	0.58	107	Kim. et. al.[a]	15:1	1.42
100	**Proposed (6-2)**	**8.6:1**	**0.13**	107	**Proposed (24-8)[a]**	15:1	0.94
117	**Proposed (25-5)[b]**	**21.8:1**	**3.21***	109	**Proposed (18-6)[b]**	**16.9:1**	**5.11***
117	Hsieh-Wei Lee[37][b]	22.2:1	2.6*	109	Hsieh-Wei Lee[b]	17.4:1	4.53*
117	Gurkan[38]	17.9:1	2.46*	109	**Proposed (4-2)[b]**	**10.4:1**	**2.83***
117	**Proposed (12-3)**	**18.7:1**	**2.39***	109	Hsieh-Wei Lee[b]	10.7:1	2.76*

Record	Method	CR	PRD	Record	Method	CR	PRD
117	**Proposed (12-3)**[b]	**15.2:1**	**2.04***	109	**Proposed (4-2)**[b]	**6.4:1**	**1.95***
117	Hsieh-Wei Lee[b]	14.2:1	1.86*	109	Hsieh-Wei Lee[b]	6.5:1	1.67*
117	Chou et. al. app.2	13:1	1.18	111	Miaou et.al. (ε = 5%)	21.6:1	8.96*
117	Eddie B.L et. al. app.3	13:1	1.07	111	**Proposed (18-6)**	**20.5:1**	**8.9***
117	SangJoon Lee et. al.	12.6:1	0.43	111	Miaou et.al. (ε = 10%)	20.6:1	8.73*
117	**Proposed (9-3)**	**12.9:1**	**0.21**	111	Miaou et.al. (ε = 5%)	14.1:1	5.99*
117	Lu. et. al. [33]	10:1	2.96	111	Miaou et.al. (ε = 10%)	13.4:1	5.9*
117	Wel. el. al. [43]	10:1	1.18	111	**Proposed (15-3)**	**13.6:1**	**5.86***
117	Bilgin et. al. [44]	10:1	1.03	118	Gurkan	6.0:1	0.98*
117	Chou et. al. app.2	10:1	0.98	118	**Proposed (12-3)**	**6.0:1**	**0.96***
117	Filhoet. al. app.3	10:1	0.86	119	Bilgin et. al.	21.6:1	3.76
117	SangJoon Lee et. al.	10.4:1	0.42	119	Tai et. al. [45]	20:1	2.17
117	**Proposed (6-3)**	**9.9:1**	**0.14**	119	Chou et. al. app.2	20.9:1	1.81
117	Hilton [39]	8:1	2.6*	119	Filho et. al. app.3	20.9:1	1.92
117	Lu. et. al.	8:1	1.18*	119	SangJoon Lee et. al.	19.3:1	2.05
117	Ku. et.al.[35]	8:1	1.06*	119	**Proposed (21-7)**	**19.8:1**	**0.89**
117	**Proposed (4-2)**	**7.9:1**	**1.02***	119	Chou et. al. app.2	10:1	1.03
117	Hwang et.al. [31]	8:1	0.93*	119	Filhoet. al. app.3	10:1	0.93
117	Lu et.al.	8:1	1.18	119	SangJoon Lee et. al.	10.3:1	0.59
117	Bilgin et. al.	8:1	0.86	119	**Proposed (10-2)**	**10:1**	**0.23**
117	Filhoet. al. app.3	8:1	0.75	119	Filhoet. al. app.3	8:1	0.77
117	SangJoon Lee et. al.	7:1	0.34	119	SangJoon Lee et. al.	8.5:1	0.44
117	**Proposed (4-2)**	**7.8:1**	**0.09**	119	**Proposed (6-2)**	**8.3:1**	**0.15**

[a]: Test in a period of 5 minutes of the corresponding record

[b]: Test in a period of 10 minutes of the corresponding record

*: PRD of reconstructed samples with values ranging from -1024 to 1023

5. Conclusions

Compressing ECG data is an effective solution to reduce the size transmitted of packages, which help avoid the congestions as well as decrease BER and the package loss rate. In this study, an extremely low-cost computational, general-purposed ECG compression algorithm, called the advanced *two-state* algorithm, was proposed, which could: (i) adapt various ECG conditions including both regular and irregular ECG, (ii) satisfy every size of the compressed package without affecting the quality of reconstruction, and (iii) is quite simple to implement in any kinds of network. This algorithm aims to separate the ECG signal into two parts: *plain durations* (P and T wave), labelled as *high-state durations* and compressed at higher CR (*hCR*), and *complex durations* (QRS complex), labelled as *low-state durations* compressed at lower CR (*lCR*).In the experiments with all 48 records of MIT-BIH arrhythmia database and 9 records of CU ventricular tachyarrhythmia database, the performance result of the proposed algorithm were very promising at moderate CR. Almost the signals was reserved well at CR < 15. In the comparison with other loss-type methods even including some advanced methods like SPIHT or JPEG2000, the proposed method showed a superior result with lower PRD at the same CR despite of its simplicity in both compressing and decompressing process. Nevertheless, the proposed method cannot reach a higher CR without significantly damaging the signal like many other methods containing error minimization mechanism. In exchange, it can achieve many necessary requirements for a medical wireless network and, due to its dependence in physiological feature, the proposed algorithm can be used for other signals asides from ECG.

References

1. Mirza Mansoor Baig, Hamid Gholamhosseini. Smart health monitoring systems: an overview of design and modeling. J.Med. Syst. 37(2) (2013). doi: 10.1007/s10916-012-9898-z.
2. E.C. Kyriacou, C.S .Pattichis, M.S. Pattichis.An overview of recent health care support systems for eEmergency and mHealth applications. Conf. Proc. IEEE Eng. Med. Biol. Soc. 2009, 1246–1249. doi: 10.1109/IEMBS.2009.5333913.
3. J. Korhonen, Ye Wang.Effect of packet size on loss rate and delay in wireless links.Wireless Communications and Networking Conference, 2005 IEEE3, 1608–1613 (2005). doi: 10.1109/WCNC.2005.1424754.
4. N. Yaakob,I.Khalil, Hu Jiankun.Performance Analysis of Optimal Packet Size for Congestion Control in Wireless Sensor Networks.The 9th IEEE International Symposium on Network Computing and Applications (NCA), Cambridge, Massachusetts, 15-17 June 2010, 210–213. doi: 10.1109/NCA.2010.37.
5. Xuedong Liang, Ilangko Balasingham. Performance analysis of the IEEE 802.15.4 based ECG monitoring network. Proceedings of the Seventh IASTED international conferences: wireless and optical communications, Montreal, Quebec, Canada, 2007, 30 May - 1 June.
6. M.S. Manikandan﮲, S. Dandapat. Wavelet threshold based TDL and TDR algorithms for real-time ECG signal compression. Biomedical Signal Processing and Control3(1), 44–66 (2008). doi: doi:10.1016/j.bspc.2007.09.003.
7. W. Mueller. Arrhythmia detection program for an ambulatoryECG monitor. Biomed. Sci. Instrum 14,81–85 (1978).
8. J.R Cox, FM Nolle, A. Fozzard, G. Oliver. AZTEC, a preprocessingprogram forreal-timeECGrhythmanalysis.IEEE.Trans.Biomed.Eng.15(4), 128–129 (1968).
9. J.P. Abenstein, W.J. Tompkins. New data reduction algorithm for real-time ecg analysis. IEEE Trans Biomed Eng. 29(1), 43–48 (1982).

10. M. Ishijima, S.B. Shin, G.H.Hostetter, J. S.klansky. Scan-along polygon approximation for data compression of electrocardiograms. Med Biol Eng Comput. 30(11), 723–729 (1983).

11. Y. Zigel, A. Cohen, A. Katz. ECG signal compression using analysis by synthesis coding, IEEE Trans. Biomed. Eng. 47(10), 308–316 (2000).

12. G. Nave, A. Cohen. ECG compression using long term prediction. IEEE Trans. Biomed. Eng. 40(9), 877–885 (1993). doi: 10.1109/10.245608.

13. P.S. Hamilton, W.J. Tompkins. Compression of ambulatory ECG by average beat subtraction and residual differencing. IEEE Trans. Biomed. Eng.38(3), 253–259 (1991). doi: 10.1109/10.133206.

14. A. Cohen, Y. Zigel. Compression of multichannel ECG through multi-channel long-term prediction. IEEE Eng. Med. Biol. Mag. 16(4), 109–115 (1998). doi: 10.1109/51.646227.

15. A.Cohen,P.M.Poluta,R.Scott-Millar.CompressionofECGsignalsusing vector quantization. Proceedings of the IEEE-90 S. A Symposium of the Communications and Signal Processing, COMSIG-90, Johannesburg, 1990, 45–54.

16. C.P. Mammen, B. Ramamurthi.Vector quantization for compressionof multichannel ECG. IEEE Trans. Biomed. Eng. 37(9), 821–825 (1990). doi: 10.1109/10.58592.

17. S.G. Miaou, H.L. Yen.Multichannel ECG compression using multi-channel adaptive vector quantization. IEEE Trans. Biomed. Eng. 48(10), 1203–1207 (2001). doi: 10.1109/10.951524.

18. J. Cardenas-Barrera, J. Lorenzo-Ginori. Mean-shape vector quantization for ECG signal compression. IEEE Trans. Biomed. Eng. 46(1), 62–70 (1999). doi: 10.1109/10.736756.

19. W. Philips. ECG data compression with time-warped polynomials. IEEE Trans. Biomed. Eng. 40(11),1095–1101 (1993). doi:10.1109/10.245626.

20. L.V.Batista,E.U.K.Melcher,L.C.Carvalho. CompressionofECGsignals by optimized quantization of discrete cosine transform coefficients. Med. Eng.Phys.23(2), 127–134 (2001). doi: 10.1016/S1350-4533(01)00030-3.

21. M.E. Womble, J.S. Halliday, S.K. Mitter, M.C. Lancaster, J.H. Triebwasser. Data compression for storing and transmitting ECGs/VCG's. Proceeding of IEEE65(5), 702–706 (1977). doi: 10.1109/PROC.1977.10550.

22. B.R.S. Reddy, I.S.N. Murthy. ECG data compression using Fourier descriptors. IEEE Trans. Biomed. Eng. 33(4), 428–434 (1986). doi:10.1109/TBME.1986.325799.

23. W.S. Kuklinski. Fast Walsh transform data-compression algorithm: ECG applications. Med. Biol. Eng. Comput. 21(4), 465–472 (1983). doi: 10.1007/BF02442635.

24. E. Berti, F. Chiaraluce, N.E. Evans, J.J. McKee. Reduction of Walsh-transformed electrocardiograms by double logarithmic coding. Trans. Biomed. Eng. 47(11), 1543–1547 (2000). doi: 10.1109/10.880108.

25. A.G. Ramakrishnan, S. Saha. ECG compression by multirate processing of beats. Comput. Biomed. Res. 29(5), 407–409 (1996). doi: 10.1006/cbmr.1996.0030.

26. M. Blanco-Velasco.A low computational complexity algorithm forECG signal compression. Med. Eng. Phys. 26(7), 553–568 (2004).

27. J.H. Husoy, T. Gjerde. Computationally efficient sub-band coding of ECG signals. Med. Eng. Phys. 18(2), 132–142 (1996). doi: 10.1016/1350-4533(95)00028-3.

28. R.S.H.Istepanian,A.A.Petrosian.Optimalzo nalwavelet-basedECGdata compression for a mobile telecardiology system. IEEE Trans. Inf. Tech- nol.Biomed.4(3), 200–211 (2000). doi: 10.1109/4233.870030.

29. Sangjoon Lee, Jungkuk Kim, Jong-Ho Lee. A Real-Time ECG Data Compression and Transmission Algorithm for an e-Health Device. IEEE Trans. Biomed. Eng. 58(9), 2448–2455 (2011). doi: 10.1109/TBME.2011.2156794.

30. R.S.H. Istepanian, L.J. Hadjileontiadis, S.M. Panas. ECG data compression using wavelets and higher order statistics methods. IEEE Trans. Inf. Technol.Biomed.5(2),108–115 (2001). doi: 10.1109/4233.924801.

31. W.J. Hwang, C.F. Chine, K.J. Li. Scalable medical data compression and transmission using wavelet transform for telemedicine applications.IEEE Trans. Inf. Technol. Biomed. 7(1), 54–63 (2003). doi: 10.1109/TITB.2003.808499.

32. S.G. Miaou, H.L. Yen.A quality-on-demand algorithm for wavelet-based compression of electrocardiogram signals. IEEE Trans. Biomed. Eng. 49(3), 233–239 (2002).

33. Z.Lu,D.Y.Kim,W.A.Pearlman.Waveletcom pressionofECGsignalsby the set partitioning in hierarchical trees method. IEEE Trans. Biomed. Eng.47(7),849–856 (2000).

34. B.S. Kim, S.K. Yoo, M.H. Lee. Wavelet-based low-delay ECG compression algorithm for continuous ECG transmission. IEEE Trans. Inf. Tech- nol. Biomed. 10(1), 77–83 (2006). doi: 10.1109/TITB.2005.856854.

35. C.T. Ku, H.S. Wang, K.C. Hung, Y.S. Hung.A novel ECG data compressionmethodbasedonnonrecursivedi screteperiodizedwavelettransform.IEEE Trans. Biomed. Eng. 53(12), 2577–2583 (2006) (Part1).

36. K. Nagarajan, E. Kresch, S.S. Rao, Y. Kresh. Constrained ECG compressionusingbestadaptedwaveletpack etbases.IEEESignalProcess.Lett.3(10), 273–275 (1996). doi: 10.1109/97.540070.

37. Hsieh-Wei Lee, King-Chu Hung, Tsung-Ching Wu, Cheng-Tung Ku. A Modified Run-Length Coding towards the Realization of a RRO-NRDPWT-Based ECG Data Compression System.EURASIP Journal on Advances in Signal Processing 2011, 2011:703752. doi:10.1155/2011/703752.

38. Hakan Gurkan.Compression of ECG signals using variable-length classified vector sets and wavelet transforms.EURASIP Journal on Advances in Signal Processing 2012, 2012:119. doi:10.1186/1687-6180-2012-119.

39. M.L. Hilton.Wavelet and wavelet packet compression of electrocardiograms. IEEE Trans. Biomed. Eng. 44(5), 394–402 (1997). doi:10.1109/10.568915.

40. A. Alesanco, S. Olmos, R.S.H. Istepanian, J. Garcya. Enhanced real-time ECG coder for packetized telecardiology applications. IEEE Trans. Inf. Technol.Biomed.10(2),229–236 (2006). doi: 10.1109/TITB.2005.856853.

41. S.G. Miaou, H.L. Yen, C.L. Lin. Wavelet-based ECG compression using dynamic vector quantization with tree codevectors in single codebook.IEEE Trans. Biomed. Eng. 49(7), 671–680 (2002). doi: 10.1109/TBME.2002.1010850.

42. S.G. Miaou, S.N. Chao. Wavelet-based Lossy-to-Lossless ECG compression in a unified vector quantization framework. IEEE Trans. Biomed. Eng.52(3),539–543 (2005). doi: 10.1109/TBME.2004.842791.

43. J.J. Wei, C.J. Chang, N.K. Chou, G.J. Jan. ECG data compression using truncated singular value decomposition. IEEE Trans. Biomed. Eng. 5(4), 290–295 (2001). doi: 10.1109/4233.966104.

44. A. Bilgin, M.W. Marcellin, M.I. Altbach. Compression of electrocardiogram signals using JPEG2000. IEEE Trans. Consum. Electron. 49(4), 833–840 (2003). doi:10.1109/TCE.2003.1261162.

45. S.C. Tai, C.C. Sun, W.C. Tan.2-D ECG compression method based on wavelettransformandmodifiedSPIHT.IEE ETrans.Biomed.Eng.52(6), 999–1008 (2005). doi: 10.1109/TBME.2005.846727.

46. H.H. Chou, Y.J. Chen, Y.C. Shiau, T.S. Kuo. An Effective and Efficient Compression Algorithm for ECG Signals With Irregular Periods. IEEE Trans. Biomed. Eng. 53(6), 1198–1205 (2006). doi: 10.1109/TBME.2005.863961.

47. H. Lee, K.M. Buckley. ECG data compression using cut and align beats approach and 2-D transforms. IEEE

Trans. Biomed. Eng. 46(5) 556–565 (1999). doi: 10.1109/10.759056.

48. E.B.L. Filho, N.M.M.Rodrigues, E.A.B. da Silva, S.M.M. de Faria, V.M.M. da Silva, M.B.de Carvalho.ECG Signal Compression Based on Dc Equalization and Complexity Sorting. IEEE Trans. Biomed. Eng. 55(7), 1923–1926 (2008). doi: 10.1109/TBME.2008.919880.

49. S.M.S. Jalaleddine, C.G. Hutchens, R.D. Strattan, W.A. Coberly.Ecg data compression techniques–a unified approach. IEEE Trans Biomed Eng. 37(4), 329–343 (1990). doi:10.1109/10.52340.

50. http://physionet.org/physiobank/database/mitdb/

51. http://physionet.org/physiobank/database/cudb/