



Aerosol water parameterisation: a single parameter framework

Swen Metzger^{1,2,3}, Benedikt Steil², Mohamed Abdelkader², Klaus Klingmüller², Li Xu⁴, Joyce E. Penner⁵, Christos Fountoukis^{5,1}, Athanasios Nenes^{6,7,8}, and Jos Lelieveld^{1,2}

¹The Cyprus Institute, Nicosia, Cyprus

²Max Planck Institute for Chemistry, Mainz, Germany

³Eco-Serve, Freiburg, Germany

⁴Department of Earth System Science, University of California, Irvine, USA

⁵Atmospheric Science, University of Michigan, Ann Arbor, Michigan, USA

⁶Institute of Chemical Engineering Sciences, Foundation for Research and Technology Hellas, Patras, Greece

⁷Schools of Earth and Atmospheric Sciences and Chemical and Biomolecular Engineering, Georgia Institute of Technology, Atlanta, GA, USA

⁸Institute of Environmental Research and Sustainable Development, National Observatory of Athens, Palea Penteli, Greece

Correspondence to: Swen Metzger (s.metzger@cyi.ac.cy)

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Abstract. We introduce a framework to efficiently parameterise the aerosol water uptake for mixtures of semi-volatile and non-volatile compounds, based on the coefficient, ν_i . This solute-specific coefficient was introduced in Metzger et al. (2012) to accurately parameterise the single solution hygroscopic growth, considering the Kelvin effect – accounting for the water uptake of concentrated nanometer-sized particles up to dilute solutions, i.e. from the compounds relative humidity of deliquescence (RHD) up to supersaturation (Köhler theory). Here we extend the ν_i parameterisation from single to mixed solutions. We evaluate our framework at various levels of complexity, by considering the full gas–liquid–solid partitioning for a comprehensive comparison with reference calculations using the E-AIM, EQUISOLV II and ISORROPIA II models as well as textbook examples. We apply our parameterisation in the EQUilibrium Simplified Aerosol Model V4 (EQSAM4clim) for climate simulations, implemented in a box model and in the global chemistry–climate model EMAC. Our results show (i) that the ν_i approach enables one to analytically solve the entire gas–liquid–solid partitioning and the mixed solution water uptake with sufficient accuracy, (ii) that ammonium sulfate mixtures can be solved with a simple method, e.g. pure ammonium nitrate and mixed ammonium nitrate and (iii) that the aerosol optical depth (AOD) simulations are

in close agreement with remote sensing observations for the year 2005. Long-term evaluation of the EMAC results based on EQSAM4clim and ISORROPIA II will be presented separately.

1 Introduction

The most comprehensive description of aerosol composition and hygroscopic growth is provided by models that calculate the full gas–liquid–solid partitioning, i.e. the composition and state of the ion-pairs over the wide range of temperatures and relative humidities from the surface in the tropics to the winter polar stratosphere. Since thermodynamic equilibrium is the final state of kinetic processes, many modelling approaches assume equilibrium, which is reasonable if the atmospheric processes that lead toward it are fast compared to those that lead away from it (Wexler and Potukuchi, 1998).

To calculate the multiphase partitioning, composition and associated water uptake of multicomponent atmospheric aerosols, various equilibrium models (EQMs) have been developed over the past decades including: EQUIL (Bassett and Seinfeld, 1983), KEQUIL (Bassett and Seinfeld, 1984), MARS (Saxena et al., 1986), MARS-A (Binkowski and Shankar, 1995), SEQUI-

LIB (Pilinis and Seinfeld, 1987), AIM (Wexler and Seinfeld, 1991), SCAPE (Kim et al., 1993a, b; Kim and Seinfeld, 1995), SCAPE2 (Meng et al., 1995), EQUISOLV (Jacobson et al., 1996), ISORROPIA (Nenes et al., 1998, 1999), EQUISOLV II (Jacobson, 1999), GFEMN (Ansari and Pandis, 1999, 2000), EQSAM (Metzger et al., 2002a, b), AIM2 and E-AIM (Wexler and Clegg, 2002), HETV (Makar et al., 2003), ADDEM (Topping et al., 2005a, b), MESA (Zaveri, 2005), EQSAM2 (Metzger et al., 2006), UHAERO (Amundson et al., 2006), ISORROPIA II (Fountoukis and Nenes, 2007), EQSAM3 (Metzger and Lelieveld, 2007), UCD (Zhang and Wexler, 2008), AIOMFAC (Zuend et al., 2011) and EQSAM4clim (this work).

These EQMs are often embedded in aerosol dynamical models (e.g. Pilinis et al., 2000), but the gas–aerosol partitioning and especially the associated water uptake controls the aerosol size distribution, if treated explicitly, which makes the development of EQMs most critical. As a consequence, EQMs vary in the degree of complexity and computational approaches, while almost all EQMs are computationally expensive, due to the complexity of the underlying multicomponent and multiphase thermodynamics. Either numerical accuracy has higher priority than computational efficiency (i.e. iterations to reach equilibrium are extensive), or the computational approaches are comprehensive, often both apply. Despite the large efforts, computational efficiency, especially if combined with accuracy and flexibility regarding the number of chemical compounds that can be considered, remains a challenge, which is especially relevant for global atmospheric aerosol–chemistry and climate modelling.

To meet this challenge we introduce in Sect. 2 an unique single parameter framework, which is subsequently applied in Sect. 3. Our framework allows one to efficiently parameterise the aerosol water uptake for mixtures of semi-volatile and non-volatile compounds, being entirely based on the single solute-specific coefficient introduced in Metzger et al. (2012). Additional results and textbook examples of Seinfeld and Pandis (2006) are presented in the Supplement. We conclude with Sect. 4.

2 Mixed solution parameterisation framework

We introduce a mixed solution parameterisation framework to efficiently calculate the aerosol water uptake for mixtures of semi-volatile and non-volatile compounds with the constraint of using only one parameter, i.e. ν_i . The solute-specific coefficient ν_i was introduced in Metzger et al. (2012) – referred to in the following as M2012 – to accurately parameterise the single solution hygroscopic growth, also considering the Kelvin effect. M2012 have shown that the ν_i approach is valid for a wide range of atmospheric conditions. To investigate the potential of the ν_i approach with respect to mixtures of salt compounds, we extend in this work the ν_i parameterisations from single to mixed solutions. Since

computational efficiency is a requirement for our parameterisation framework, we minimise the overall computational burden by a set of key-constraints:

1. Solving the multicomponent and multiphase partitioning analytically, by using a consistent set of equations, based on one compound-specific single solute coefficient, ν_i [–]. This set of equations includes the solute molality, μ_s [mol(solute) kg⁻¹(H₂O)], and its equivalent expression in terms of the mass fraction solubility, χ_s [–]. Both are the essential thermodynamic properties in our framework and only depend on ν_i ; the temperature (T), relative humidity (RH) and the particle dry diameter (D_s) are given;
2. Breaking down the complexity of aerosol thermodynamics as much as possible, without the loss of crucial information and critical numerical accuracy, by using chemical domains with a neutralisation order for all salt compounds listed in Table 1;
3. Minimising the dependencies on the required thermodynamic data by using a pre-determined ν_i coefficient for each electrolyte listed in Table 1;
4. Assuming ν_i , constant for the entire range of water activity, a_w .

The relevant single solute equations (of M2012) are summarised in Appendix A. The mixed solution parameterisation framework has been determined by a multi-functional fitting, limited to one parameter per compound, to match the results of ISORROPIA II. The multiphase and multicomponent thermodynamic system has an analytical solution when our consistent set of analytical equations and the ν_i coefficient of M2012 are used. Consequently, our parameterisation framework has a similar applicability as ISORROPIA II.

2.1 Pre-determined ν_i

M2012 have detailed that a (unitless) single solute coefficient, i.e. ν_i [–], can be accurately deduced from one reference data pair of solute molality, μ_s , and the corresponding water activity, a_w [–]. We use a data pair at solute saturation to pre-determine ν_i , since measurements are available for all major salt compounds that are of interest in atmospheric aerosol modelling. For the salt compounds listed in Table 1 we use the mass fraction solubility, w_s [–], which is an equivalent expression of the saturation molality, $\mu_{s,\text{sat}}$. For the corresponding a_w , we use the available relative humidity of deliquescence (RHD) values and obtain ν_i by solving Eq. (5b) of M2012 with a root finding method (bisection). To be consistent with ISORROPIA II, here we determine ν_i from w_s and RHD data at temperature $T_0 = 298$ [K]. The water activity data used by ISORROPIA II (and other EQMs) are tabulated only for room temperature. We therefore do not consider the T dependency of ν_i in this work.

Table 1. Thermodynamic data (Sect. 2.1): stoichiometric coefficient ν_s [–], the ion-pair charge Z_s [–], the single solute parameter ν_i [–], the mass fraction solubility in percent W_s [%] ($w_s = W_s/100$), the molar masses M_s [kg mol^{-1}], the densities D_s [kg m^{-3}], $\text{RHD}(T_0)$ [–] at reference temperature $T_0 = 298.15$ [K], and the corresponding temperature coefficients, $T_{\text{coef}}(\text{RHD})$ [–]. The ν_i values have been obtained from the RHD and W_s values (at $T_0 = 298$ [K]) following the method described in Metzger et al. (2012). The RHD values are taken from Fountoukis and Nenes (2007); the W_s and all other values are taken from the *Handbook of Chemistry and Physics* (Lide, 2005).

Species 01–05	H ₂ O	H ₂ SO ₄	HNO ₃	HCl	NH ₃
$\nu_s Z_s$	2 1	3 2	2 1	2 1	1 1
ν_i	–	–	–	–	–
W_s	–	–	–	–	–
M_s	0.018020	0.098090	0.063020	0.036460	0.017040
D_s	997	1830	1513	1490	696
RHD	–	–	–	–	–
T_{coef}	–	–	–	–	–
Species 06–10	(NH ₄) ₃ H(SO ₄) ₂	(NH ₄) ₂ SO ₄	NH ₄ HSO ₄	NH ₄ NO ₃	NH ₄ Cl
$\nu_s Z_s$	5 3	3 2	2 1	2 1	2 1
ν_i	1.616356	1.274822	1.253573	1.051480	1.243054
W_s	53.30	43.31	76.00	68.05	28.34
M_s	0.247300	0.132170	0.115130	0.080060	0.053500
D_s	1775	1770	1780	1720	1519
RHD	0.6900	0.7997	0.4000	0.6183	0.7710
T_{coef}	186.00	80.00	384.00	852.00	239.00
Species 11–15	Na ₃ H(SO ₄) ₂	Na ₂ SO ₄	NaHSO ₄	NaNO ₃	NaCl
$\nu_s Z_s$	5 3	3 2	2 1	2 1	2 1
ν_i	–	1.278762	1.293906	1.160345	1.358377
W_s	–	21.94	66.18	47.70	26.47
M_s	0.262120	0.142050	0.120070	0.085000	0.058440
D_s	2565	2700	2430	2260	2170
RHD	–	0.9300	0.5200	0.7379	0.7528
T_{coef}	–	80.00	–45.00	304.00	25.00
Species 16–20	K ₃ H(SO ₄) ₂	K ₂ SO ₄	KHSO ₄	KNO ₃	KCl
$\nu_s Z_s$	5 3	3 2	2 1	2 1	2 1
ν_i	–	1.286445	1.308499	1.014102	1.256989
W_s	–	10.71	33.60	27.69	26.23
M_s	0.310444	0.174266	0.136178	0.101108	0.074548
D_s	2490	2660	2320	2110	1988
RHD	–	0.9750	0.8600	0.9248	0.8426
T_{coef}	–	35.60	0	0	159.00
Species 21–25	n/a	CaSO ₄	n/a	Ca(NO ₃) ₂	Ca(Cl) ₂
$\nu_s Z_s$	– / –	2 2	– / –	3 2	3 2
ν_i	–	1.271828	–	1.586562	2.024869
W_s	–	0.21	–	59.02	44.84
M_s	–	0.136150	–	0.164100	0.110980
D_s	–	2960	–	2500	2150
RHD	–	0.9900	–	0.4906	0.2830
T_{coef}	–	0	–	509.40	551.10
Species 25–30	n/a	MgSO ₄	n/a	Mg(NO ₃) ₂	Mg(Cl) ₂
$\nu_s Z_s$	– / –	2 2	– / –	3 2	3 2
ν_i	–	1.435281	–	1.878693	2.107772
W_s	–	26.31	–	41.59	35.90
M_s	–	0.120375	–	0.148325	0.095205
D_s	–	2660	–	2300	2325
RHD	–	0.8613	–	0.5400	0.3284
T_{coef}	–	–714.45	–	230.20	42.23

Table 2. Chemical domains (introduced in Sect. 2.2).

D4	SULFURIC ACID ONLY	tCAT < MIN	AND	tHSO ₄ ≥ MIN
D3	SULFATE VERY RICH	tCAT ≥ MIN	AND	tCAT < tHSO ₄
D2	SULFATE RICH	tCAT ≥ tHSO ₄	AND	tCAT < tSO ₄
D1	SULFATE NEUTRAL	tCAT ≥ tSO ₄		

Table 1 lists the pre-calculated ν_i values for each salt compound considered, together with the required thermodynamic data: Stoichiometric coefficient ν_s [–], the ion-pair charge Z_s [–], the single solute parameter ν_i [–], the mass fraction solubility in percent W_s [%] ($w_s = W_s/100$), the molar masses M_s [kg mol^{–1}], the densities D_s [kg m^{–3}], $RHD(T_0)$ [–] at reference temperature $T_0 = 298.15$ [K] and the corresponding temperature coefficients, $T_{\text{coef}}(\text{RHD})$ [–]. The RHD values are taken from Fountoukis and Nenes (2007); the other values of Table 1 are taken from the Handbook of Chemistry and Physics (Lide, 2005).

2.2 Chemical domains

To break down the complexity of aerosol thermodynamics as much as possible, we minimise the number of chemical compounds and equilibrium reactions that have to be considered. Following the original EQSAM approach (Metzger et al., 2002a), we define chemical domains with a sub-set of neutralisation reactions that are considered for a given T , RH and input concentrations (total of aerosol cations/anions and precursor gases), with all concentration units in [mol m^{–3}(air)]. Our domain definition is listed in Table 2 and applied in our mixed solution framework with if-else logic and top-down approach. The potential aerosol neutralisation levels depend on the input concentration ratio of total cations, tCAT. The cations are balanced against the total sulfate anions, for which we consider, for sulfate-rich cases, the total sulfates as bi-sulfate, tHSO₄, or for sulfate-poor cases as total sulfate, tSO₄. In any case, these totals “t” need to exceed a threshold, MIN = 1×10^{-15} [mol m^{–3}(air)]; below the computations are neglected for a given domain. Our definition of totals is given by our domain classification (Table 2), implicitly taking into account the maximum neutralisation level that is theoretically possible for each domain:

$$\begin{aligned}
 - \text{tSO}_4 &= \sum(1 \cdot \text{HSO}_4^- + 2 \cdot \text{SO}_4^{2-}) \\
 - \text{tHSO}_4 &= \sum(1 \cdot \text{HSO}_4^- + 1 \cdot \text{SO}_4^{2-}) \\
 - \text{tCAT} &= \\
 &\sum(2 \cdot \text{Ca}^{2+} + 2 \cdot \text{Mg}^{2+} + 1 \cdot \text{Na}^+ + 1 \cdot \text{K}^+ + 1 \cdot \text{NH}_4^+).
 \end{aligned}$$

The domain definition (Table 2) is subsequently used to define the neutralisation reaction order (see Sect. 2.3). The two semi-volatile compounds listed in Table 1, NH₄NO₃ and NH₄Cl, are considered in our approach only in the sulfate neutral (D1) domain. On the other hand, bi-sulfate is taken into account only for the sulfate-rich (D2) and very-rich (D3)

cases, while free sulfuric acid is considered only for the un-neutralised sulfate case (D4).

2.3 Domain-dependent neutralisation reaction order

To avoid the numerical minimisation of the Gibbs free energy, which is required to obtain the equilibrium composition of mixed solutions (Seinfeld and Pandis, 2006), we define for each domain (Table 2) a neutralisation reaction order (NRO), which can practically be considered as the salting-out effect of salt solutes (Metzger and Lelieveld, 2007). For this work, we rank the cations and anions according to their preferred neutralisation reaction by

- Anions: SO₄^{2–} – HSO₄[–] – NO₃[–] – Cl[–]
- Cations: Ca²⁺ – Mg²⁺ – K⁺ – Na⁺ – NH₄⁺ – H⁺,

which yields the NRO listed in Table 3. The ordering is based on numerous modelling studies, both extensive box-modelling comparisons (Metzger et al., 2002a, 2006, 2012) and global applications (Metzger et al., 1999, 2002b; Metzger and Lelieveld, 2007). Note that we have constrained the ordering for this work to achieve the closest agreement with ISORROPIA II for two reasons: (1) ISORROPIA II is currently the only EQM that is widely applied in global modelling; (2) and it also considers the mineral cations Ca²⁺, Mg²⁺ and K⁺.

To solve the mixed solution framework we apply the NRO to balance cation–anion pairs that have a non-zero ion–ion product. Within a chemical domain (Table 2), the electrolyte compounds listed in Table 3 are subsequently formed for non-zero ion–ion product, until all cation–anion pairs are paired, or either all cations or anions are fully neutralised. To analytically solve the entire gas–liquid–solid partitioning, we consider at this stage all electrolytes in solution (computing totals of gas and ions). The gas–solid and gas–liquid partitioning of semi-volatile compounds, the liquid–solid partitioning and the water uptake are determined in that order in subsequent and independent computational steps (Sect. S2 in the Supplement).

2.4 Treatment of semi-volatile compounds

Table 1 includes two semi-volatile compounds that exhibit the gas–liquid–solid partitioning, i.e. ammonium nitrate, NH₄NO₃, and ammonium chloride, NH₄Cl. Both are allowed in our framework only in D1, provided that a surplus ammonium, NH₄⁺, is available. Our implicit assumption

Table 3. Neutralisation reaction order for Table 2 (introduced in Sect. 2.3).

D1	i.e. Sulfate neutral		
1. CaSO ₄	2. MgSO ₄	3. K ₂ SO ₄	
4. Na ₂ SO ₄	5. (NH ₄) ₂ SO ₄	6. Ca(NO ₃) ₂	
7. Mg(NO ₃) ₂	8. KNO ₃	9. NaNO ₃	
10. NH ₄ NO ₃	11. Ca(Cl) ₂	12. Mg(Cl) ₂	
13. KCl	14. NaCl	15. NH ₄ Cl	
D2	i.e. Sulfate rich		
1. CaSO ₄	2. MgSO ₄	3. K ₂ SO ₄	
4. KHSO ₄	5. Na ₂ SO ₄	6. NaHSO ₄	
7. (NH ₄) ₂ SO ₄	8. NH ₄ HSO ₄		
D3	i.e. Sulfate very rich		
1. CaSO ₄	2. MgSO ₄	3. KHSO ₄	
4. NaHSO ₄	5. NH ₄ HSO ₄	6. H–HSO ₄	
D4	i.e. Sulfuric acid		
1. H ₂ SO ₄			

is that all sulfates are neutralised first through the reactions with cations (Sect. 2.3). Only excess ammonium may further neutralise anions, nitrate, NO₃[−] and/or chloride, Cl[−]. Thus, semi-volatile compounds can only partition into the particles, if the concentration product exceeds a threshold that is given by the temperature- and humidity-dependent equilibrium dissociation constant, $K_p(T, RH)$. The equilibrium partitioning is detailed in Seinfeld and Pandis (2006) – hereafter referred to as SP2006 (Sect. 10.4.3 ff).

2.4.1 RH < RHD – pure and mixed compounds

When the RH is below the RHD and the partial pressure product of gaseous (g) ammonia, NH₃(g), and nitric acid, HNO₃(g), with units either in [ppbv] or [mol m^{−3}(air)], equals or exceeds the temperature-dependent equilibrium dissociation constant, $K_p(T)$, solid (s) ammonium nitrate (AN), NH₄NO₃(s), is assumed to be formed instantaneously:



$$\text{EQ: } [\text{NH}_3(\text{g})] \cdot [\text{HNO}_3(\text{g})] = K_{p,\text{AN}}(T).$$

For Reaction (R1) the equilibrium concentration of solid ammonium nitrate can be analytically computed from the gaseous concentrations by solving a quadratic equation – for our examples in the Supplement we use [ppbv]. We compute the temperature dependency of the equilibrium dissociation constants, $K_p(T)$, following Fountoukis and Nenes (2007):

$$K_p(T) = K_p^0 \times \exp[a \times (T_0/T - 1) + b \times (1 + \ln(T_0/T) - T_0/T)], \quad (1)$$

Table 4. Equilibrium dissociation constants [ppbv²] and T coefficients [−]; from Fountoukis and Nenes (2007).

NH ₄ NO ₃	$K_p^0 = 57.46$	$a = -74.38$	$b = 6.120$
NH ₄ Cl	$K_p^0 = 1.086$	$a = -71.00$	$b = 2.400$

where T and $T_0 = 298.15$ K, the ambient temperature and reference temperature, respectively. The $K_p^0(T_0)$ values are given in Table 4 in [ppbv²] for T_0 and reference pressure, $P_0 = 1$ [atm] = 101 325 [Pa], together with the dimensionless temperature coefficients, a and b [−]. For applications on a mole basis (e.g. for EQSAM4clim), $K_p(T)$ [ppbv²] can be converted to [(mol m^{−3}(air))²], using $K_{p,\text{mol}}(T) = K_p(T)/(R/P \times T)^2$, with $R = 8.314409$ [Pa m³ mol^{−1} K^{−1}] the gas constant and $P = 101 325$ [Pa] ($R/P_0 \times T_0 = 24.465$ [L mol^{−1}]).

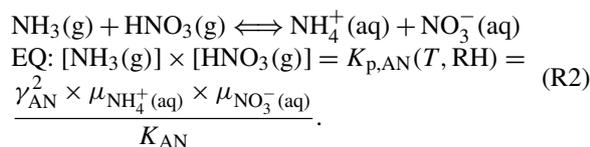
The equilibrium dissociation constant of NH₄NO₃ is sensitive to temperature changes and varies over more than 2 orders of magnitude for typical ambient conditions. This is illustrated in Fig. 10.19 of SP2006, which we recommend to the reader for a detailed discussion. For comparison, Fig. 1 shows the same $K_{p,\text{AN}}$ values as a function of T at $RH < RHD$ for the EQSAM4clim and ISORROPIA II applications. Although the results are similar, those of SP2006 are slightly lower since their values are obtained from a slightly different equation, i.e. $K_{p,\text{AN}}(T) = \exp(84.6 - 24 220/T - 6.1 \times \ln(T/T_0))$ – see Eq. (10.91) of SP2006 (respectively Eq. 9.91 and Fig. 9.19 of Seinfeld and Pandis, 1998).

Note that Reaction (R1) applies to the gas–aerosol partitioning over dry aerosols – pure NH₄NO₃(s), or any mixture of NH₄NO₃(s) with other dry salt compounds. An example is given in Sect. S1.1 in the Supplement.

2.4.2 RH ≥ RHD – pure compound

For the wet case, with RH above the compound RHD or mixed solution RHD (see below), the situation is more complicated. In contrast to the gas–solid partitioning described above, the gas–liquid equilibrium partitioning of, e.g. gaseous ammonia, NH₃(g) and nitric acid, HNO₃(g), is in equilibrium with aqueous ammonium nitrate, NH₄NO₃(aq), when the vapour pressure product of the gases exceeds its temperature and humidity-dependent equilibrium dissociation constant, $K_{p,\text{AN}}(T, RH)$. The salt compound formed is – when equilibrium is reached – additionally dissociated into a cation NH₄⁺(aq) and anion NO₃[−](aq) pair.

1. Following SP2006 (their Sect. 10.4.3), Reaction (R1) expands to



For Reaction (R2) the equilibrium partitioning dissociation constant is now a function of T and RH . In the notation of SP2006 (see their Eq. 10.99), $K_{\text{p,AN}}(T, \text{RH})$ is related to the temperature-dependent equilibrium constant K_{AN} . K_{AN} [$\text{mol}^2 \text{kg}^{-2} \text{atm}^{-2}$] depends on the ion molalities [$\text{mol kg}^{-1}(\text{H}_2\text{O})$] of ammonium and nitrate, i.e. $\mu_{\text{NH}_4^+(\text{aq})}$ and $\mu_{\text{NO}_3^-(\text{aq})}$, and on the corresponding mean molal binary activity coefficient of aqueous ammonium nitrate, i.e. γ_{AN}^2 , squared because of the cation–anion product. Solving Reaction (R2) requires iterations. To determine the aqueous phase concentration of all compounds that can exist in solution at given T and RH requires knowledge of the total aerosol water mass (see below), which in turn depends on the solute concentrations and according to Reaction (R2) on activity coefficients. Thus, since γ_{AN} is a function of the aqueous phase concentration, $K_{\text{p,AN}}(T, \text{RH})$ has no analytical solution. According to the thermodynamic literature, the standard treatment is therefore quite comprehensive and requires complex thermodynamic codes.

2. Here we express the product ($\gamma_{\text{AN}}^2 \times \mu_{\text{NH}_4^+(\text{aq})} \times \mu_{\text{NO}_3^-(\text{aq})}$) of Reaction (R2) to be only a function of ν_i and RH , which is motivated by M2012, since their μ_s is only a function of ν_i and RH . To be able to solve Reaction (R2) analytically, we parameterise $K_{\text{p,AN}}(T, \text{RH})$ by introducing a solute-specific correction term for Reaction (R1), which only depends on RH :

$$K_{\text{p}}(T, \text{RH}) = K_{\text{p}}(T) \times \text{COEF}(\text{RH}). \quad (2)$$

At given T and RH , $K_{\text{p}}(T, \text{RH})$ is then a priori known, if $\text{COEF}(\text{RH})$ is independent of the solute concentration and associated water mass. This can be achieved either by fitting data (Metzger et al., 1999, 2002a; Hauglustaine et al., 2014), or expressing $\text{COEF}(\text{RH})$ in terms of the ν_i and the RH -dependent solute molality parameterisation of M2012, using their Eq. (5a). With a further comparison to Eq. (A11) of M2012, we can express the solute molality in terms of the solute mass fraction, χ_s , and define $\text{COEF}(\text{RH})$ for pure $\text{NH}_4\text{NO}_3(\text{aq})$ solutions in terms of $\chi_s(\text{RH})$, i.e. for $\text{RH} \geq \text{RHD}$:

$$\text{COEF}(\text{RH}) := 2 \times \chi_s^2(\text{RH}), \quad (3)$$

where $\text{COEF}(\text{RH}) := 1$ for $\text{RH} < \text{RHD}$. Equation (3) has been empirically derived to approximate the results obtained by ISORROPIA II (see Sect. 3). $\chi_s(\text{RH})$

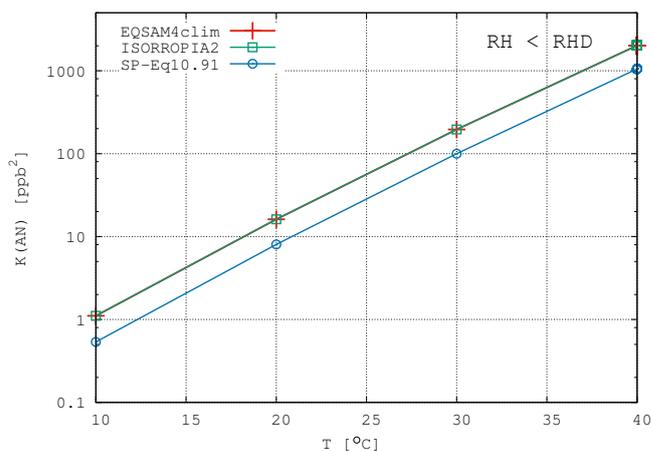


Figure 1. NH_4NO_3 equilibrium dissociation constant as function of T at $\text{RH} < \text{RH}(\text{AN})$. Red crosses show the values of EQSAM4clim, green squares refer to ISORROPIA II and the blue circles show Eq. (10.91) of Seinfeld and Pandis (2006); see their Fig. 10.19.

denotes the solute mass fraction, which requires in our mixed solution parameterisation framework only knowledge of RH and the solute-specific coefficient, ν_i . In accord with the dry case (Reaction R1), aqueous solutions (Reaction R2) can now be analogously solved. Using Eqs. (2) and (3) to obtain $K_{\text{p,AN}}(T, \text{RH})$ at a given T and RH , the quadratic equation, which has an analytical solution for the dry case, can now also be applied to pure $\text{NH}_4\text{NO}_3(\text{aq})$ solutions. The direct solution of Reaction (R2) by using Eqs. (2) and (3) is exemplified in the Supplement.

The T -dependent equilibrium dissociation constant of NH_4NO_3 , shown in Fig. 1, is also sensitive to changes in relative humidity and varies over orders of magnitude for typical ambient conditions. This is illustrated in Fig. 10.21 of SP2006, which we recommend to the reader for a detailed discussion. For comparison, Fig. 2 extends Fig. 1 showing the $K_{\text{p,AN}}(T, \text{RH})$ values as a function of RH at $T = 298.15$ [K] for the EQSAM4clim and ISORROPIA II applications. The line points, which refer to pure $\text{NH}_4\text{NO}_3(\text{aq})$ solutions, are relatively close for the EQSAM4clim and ISORROPIA II results, but both are (for $\text{RH} \leq \text{RHD}$) roughly a factor 2 higher than the corresponding values of SP2006 (see Fig. 1); the constant $K_{\text{p,AN}}(T)$ of SP2006 is included for reference (at $T = 298.15$ [K]). Note that with Eq. (2) and the quadratic form of Eq. (3) we can analytically approximate the solution of $K_{\text{p,AN}}(T, \text{RH})$ for $Y = 1.0$ (Fig. 2).

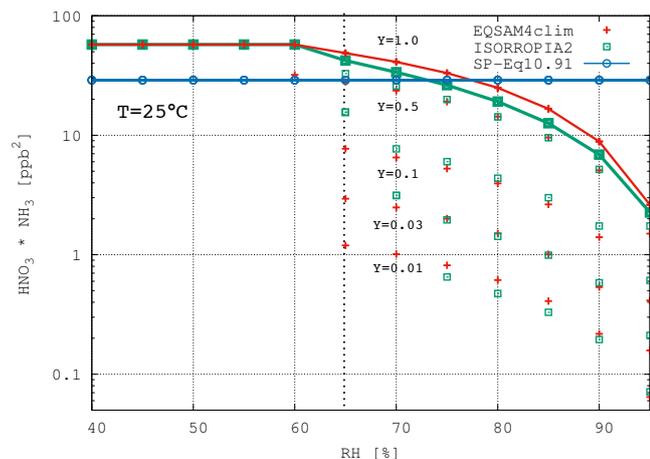


Figure 2. NH_4NO_3 equilibrium dissociation constant as function of RH (at $T = 298.15$ [K]) for various ionic strength factors (Y) defined in Seinfeld and Pandis (2006); see their Fig. 10.21. Red crosses show the results of EQSAM4clim, green squares those of ISORROPIA II. The line points refer to pure ammonium nitrate ($Y = 1$). The vertical line at $\text{RH} = 65$ [%] indicates the solid–liquid phase partitioning threshold for the mixed solution, shown in Seinfeld and Pandis (2006). The ordinate values refer to the product of $[\text{NH}_3]_{(\text{g,AN})} \times [\text{HNO}_3]_{(\text{g,AN})}$ that are obtained at end of the gas–liquid–solid NH_4NO_3 partitioning of ISORROPIA II, and by Eq. (9) for EQSAM4clim.

2.4.3 $\text{RH} \geq \text{RHD}$ – mixed compound

According to SP2006 (and references therein), Reaction (R2) needs to be extended for mixed aqueous solutions to include an ionic strength factor.

1. Following the notation of SP2006 (see their Eq. 10.100), the equilibrium concentration (either in [ppbv] or $[\text{mol m}^{-3}(\text{air})]$) of $[\text{NH}_4\text{NO}_3]$ in mixed aqueous solutions is controlled by the presence of ammonium sulfate, $[(\text{NH}_4)_2\text{SO}_4]$, and depends on a dimensionless ionic strength factor Y , which is defined by the ratio:

$$Y := \frac{[\text{NH}_4\text{NO}_3]}{[\text{NH}_4\text{NO}_3] + 3 \times [(\text{NH}_4)_2\text{SO}_4]} \quad (4)$$

To extend the calculation of the T and RH-dependent equilibrium dissociation constant to the case of multicomponent aqueous solutions of NH_4NO_3 , shown in Fig. 2, Eq. (4) needs to be considered such that $K_{\text{p,AN}}(T, \text{RH})$ becomes $K_{\text{p,AN}}(T, \text{RH}, Y)$.

2. To satisfy our key constraint (see Sect. 2) we avoid iterations in our mixed solution parameterisation. We therefore parameterise $K_{\text{p,AN}}(T, \text{RH}, Y)$ by expanding Eq. (2) to be additionally a function of Y (Eq. 4):

$$K_{\text{p}}(T, \text{RH}, Y) = K_{\text{p}}(T) \times \text{COEF}(\text{RH}, Y). \quad (5)$$

For Eq. (5), $\text{COEF}(\text{RH}, Y) := \text{COEF}(\text{RH}) \times Y^{0.8}$, where $\text{COEF}(\text{RH})$ is given by Eq. (3) and Y by Eq. (4), for which we use the concentration given by the NRO (Sect. 2.3), i.e. $Y := \frac{[\text{NH}_4\text{NO}_3]_{(\text{nro,max})}}{[\text{NH}_4\text{NO}_3]_{(\text{nro,max})} + 3 \times [(\text{NH}_4)_2\text{SO}_4]_{(\text{nro})}}$. The $Y^{0.8}$ term has been empirically determined to approximate the results of ISORROPIA II by keeping the initial NH_4NO_3 and $(\text{NH}_4)_2\text{SO}_4$ concentrations constant. Since we do not use at this computation step any dissociation constant, we obtain the maximum concentrations (NRO, max) directly from the NRO (see Sect. 2.3). Equation (5) and the quadratic equation can be solved non-iteratively. The solution is detailed below (Sect. 2.5); examples are given in Sect. S1 in the Supplement.

Figure 2 shows that the results of EQSAM4clim and ISORROPIA II exhibit a similar dependency on Y for $K_{\text{p,AN}}(T, \text{RH}, Y)$, where the values decrease with decreasing Y according to the results and the discussion of SP2006 (see their Fig. 10.21). $K_{\text{p,AN}}(T, \text{RH}, Y)$ is given here by the product of the gaseous concentrations of ammonia, $[\text{NH}_3]_{(\text{g,AN})}$, and nitric acid, $[\text{HNO}_3]_{(\text{g,AN})}$, which are in equilibrium with either the solid $[\text{NH}_4\text{NO}_3(\text{s})]$ concentration, if $\text{RH} < \text{RHD}$, or in equilibrium with the aqueous $[\text{NH}_4\text{NO}_3(\text{aq})]$ concentration when $\text{RH} \geq \text{RHD}$ in case of pure $[\text{NH}_4\text{NO}_3]$ (zero $[(\text{NH}_4)_2\text{SO}_4]$, where $Y = 1$). Below the RHD, $K_{\text{p}}(T, \text{RH}, Y)$ reduces to $K_{\text{p}}(T)$ as given by Eq. (1) in Reaction (R1). Differences, which occur mainly in the mixed deliquescence humidity range, are discussed below (Sect. 2.6).

2.5 Solving NH_4NO_3 / NH_4Cl -thermodynamic equilibrium – this work

To analytically compute the equilibrium concentrations of the two semi-volatile compounds, NH_4NO_3 and NH_4Cl , for a given RH and T with our mixed solution parameterisation, we first solve all neutralisation reactions at once for the domain by using the NRO (Table 3, Sect. 2.3) and the totals (gas + aerosol) of the cation and anion input concentrations. Thus, we obtain the free ammonium $\text{TA} = [\text{NH}_4^+]_{(\text{nro,free})}$ and nitrate $\text{TN} = [\text{NO}_3^-]_{(\text{nro,free})}$, after all higher ranked cation–anion pairs are paired. To enable a non-iterative solution, we do not use at this computation step any dissociation constant, so that we directly obtain from [TA] and [TN] the corresponding maximum ammonium nitrate concentration $[\text{NH}_4\text{NO}_3(\text{nro,max})] = \text{MIN}([\text{TA}], [\text{TN}])$, which is possible for $K_{\text{p}}(T, \text{RH}, Y) = 1$ and the given input concentration, T and RH. Analogously, we compute the maximum ammonium chloride concentration from the final free ammonium and free chloride, $[\text{TC}] = [\text{Cl}^-]_{(\text{nro,free})}$, with $[\text{NH}_4\text{Cl}(\text{nro,max})] = \text{MIN}(\text{TA}, \text{TC})$.

With the initial (maximum) values of $[\text{NH}_4\text{NO}_3(\text{nro,max})]$ and $[(\text{NH}_4)_2\text{SO}_4(\text{nro,max})]$ we can solve Eq. (4). To obtain the final equilibrium concentrations, we compute the evaporative loss. For $[\text{NH}_4\text{NO}_3(\text{nro})]$, we compute the gaseous

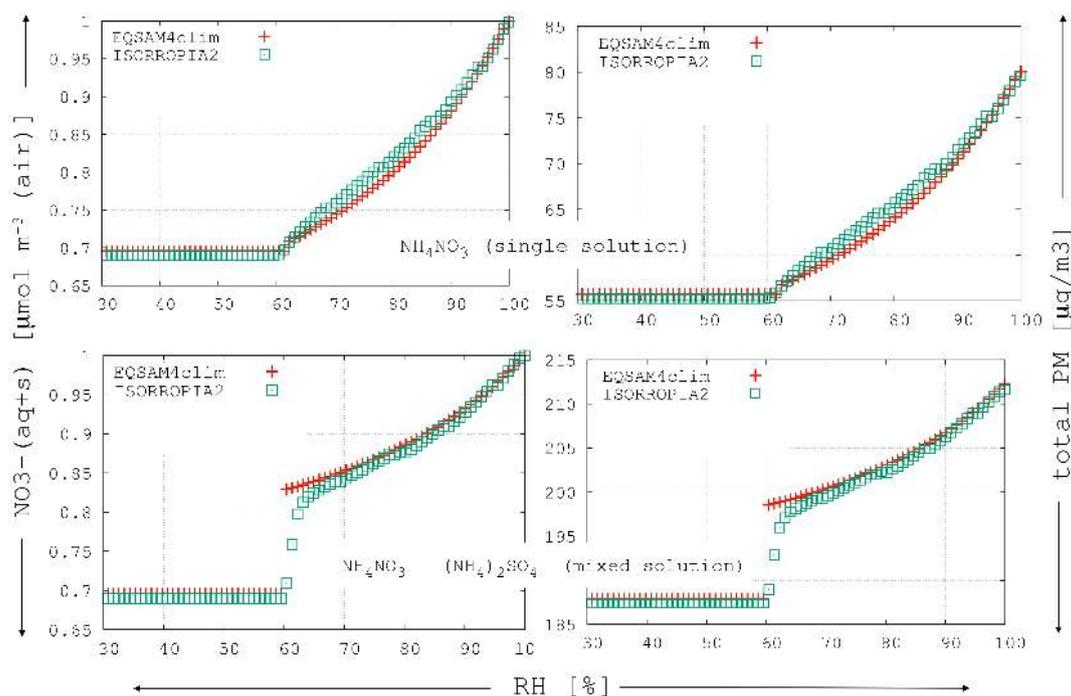


Figure 3. Results of EQSAM4clim (red crosses) and ISORROPIA II (green squares) for two idealised gas–liquid–solid partitioning examples: single solute (binary) solution of pure NH_4NO_3 (upper panels) and mixed solution of NH_4NO_3 and $(\text{NH}_4)_2\text{SO}_4$ with the concentration of each compound fixed to $1 \mu\text{mol m}^{-3}(\text{air})$ at $T = 298.15 \text{ K}$. The left panels show the NH_4NO_3 concentration in $[\mu\text{mol m}^{-3}(\text{air})]$, the right panels show the corresponding particulate mass $[\mu\text{g m}^{-3}(\text{air})]$. The mixed solution RHD described in Sect. 2.6 has been neglected for EQSAM4clim for this case, since this figure presents only an example for Sects. 2.4 and 2.5 (Sect. 2.6 is considered below).

ammonia, $[\text{NH}_3]_{(\text{g,AN})}$, and nitric acid, $[\text{HNO}_3]_{(\text{g,AN})}$ from $[\text{NH}_4\text{NO}_3]_{(\text{nro,max})}$:

$$[\text{TN}] = [\text{NO}_3^-]_{(\text{nro,free})}, \quad (6)$$

$$[\text{TA}] = [\text{NH}_4^+]_{(\text{nro,free})}, \quad (7)$$

$$[\text{X}] = \frac{1}{2} \times (-([\text{TA}] + [\text{TN}]) + \sqrt{([\text{TA}] + [\text{TN}])^2 + 4 \times K_p(T, \text{RH}, Y)/(RT)^2}), \quad (8)$$

where the variable $[\text{X}]$ is used to obtain

$$[\text{NH}_3]_{(\text{g,AN})} = [\text{HNO}_3]_{(\text{g,AN})} = \text{MIN}([\text{NH}_4\text{NO}_3]_{(\text{nro,max})}, [\text{X}]). \quad (9)$$

With Eq. (9) we compute the final gaseous concentrations of $\text{HNO}_3(\text{g})$ and $\text{NH}_3(\text{g})$ from

$$[\text{NH}_3]_{(\text{g})} = [\text{TA}] + [\text{NH}_3]_{(\text{g,AN})}, \quad (10)$$

$$[\text{HNO}_3]_{(\text{g})} = [\text{TN}] + [\text{HNO}_3]_{(\text{g,AN})}, \quad (11)$$

and the final ammonium nitrate equilibrium concentration from

$$[\text{NH}_4\text{NO}_3]_{(\text{nro})} = [\text{NH}_4\text{NO}_3]_{(\text{nro,max})} - [\text{HNO}_3]_{(\text{g,AN})}. \quad (12)$$

One can now solve with Eqs. (6)–(12) the quadratic equation for the dry, pure or mixed solution cases. But, in contrast to Seinfeld and Pandis (1998) (see their Eq. 9.103), we compute with Eq. (8) the evaporative losses of gaseous concentrations at equilibrium.

Figure 3 shows a comparison of idealised box model calculations of EQSAM4clim (see Appendix B) and ISORROPIA II (more comprehensive calculations are shown in Sect. 3). The upper panels show the gas–liquid–solid partitioning concentration of NH_4NO_3 for a binary solution with a fixed concentration of $1 \mu\text{mol m}^{-3}(\text{air})$ of pure NH_4NO_3 , while the lower panels show the same for a mixed solution with each $1 \mu\text{mol m}^{-3}(\text{air})$ of NH_4NO_3 and $(\text{NH}_4)_2\text{SO}_4$ (both at $T = 298.15 \text{ K}$). The left panels show NH_4NO_3 , the right the corresponding total mass loading. To solve the gas–solid and gas–liquid partitioning we have used the ν_i -based framework (Sect. 2) for EQSAM4clim, and for ISORROPIA II the option to iteratively calculate activity coefficients. A detailed calculation for this example is given in the Supplement (Sect. S1). Despite fundamental differences in both approaches, the comparison of these results is satisfactory for mixed solute concentration from which the aerosol water mass is derived in a subsequent calculation step – for EQSAM4clim without iterations.

2.6 Mixed solution RHD

To calculate the liquid–solid partitioning, we follow (Fountoukis and Nenes, 2007) and consider a mutual deliquescence RH range. In our framework, it depends on a minimum and maximum threshold: RHDMIN and RHDMAX, which are defined below. When the RH is below RHDMIN the aerosol is considered to be dry, while for RH above RHDMAX the aerosol is considered wet with all ionic compounds dissolved. In between a mixture can exist, with some compounds dissolved while other compounds are precipitated from the solution.

For mixed solutions (two or more compounds and water), only the amount that exists for $RH > RHDMIN$ is considered in solution and allowed to contribute to the mixed solution water uptake. Otherwise, the compounds are considered to be instantaneously solid and precipitated from the solution. For all non-precipitated compounds, a weighted solute concentration is computed from which subsequently all partial water masses are obtained. The sum of all partial water masses yields the total water for the given aerosol composition, size, T and RH (see Sect. 2.7).

However, comparing the water uptake calculation of EQSAM4clim with reference calculations of, e.g. ISORROPIA II and E-AIM is somewhat precarious. The reason is that for mixed solutions the calculated water mass mainly depends on the threshold at which the mixture is considered to take up water. The assumptions made to define the mixed solution RHD, or the mutual deliquescence RH range, are generally a major source of uncertainty in modelling the aerosol associated water uptake. First we discuss the procedure of Fountoukis and Nenes (2007), and then we describe our single parameter approach.

1. For ISORROPIA II, if the RH is within a mutual deliquescence RH range, the so-called MDRH region, the solution is assumed to be the sum of two weighted solutions; a “dry solution” (considering a pure dry case) and a “saturated liquid” solution (considering a pure liquid case). Then a numerical solution needs to be found based on a weighting factor (WF) for the dry and liquid solution that could be present in the given sub-domain (solute composition). The weighting factors are obtained from $(RHD - RH)/(RHD - MDRH)$ using prescribed MDRH values, which have been measured and tabulated for certain mixtures of salt solutes (see Fountoukis and Nenes, 2007). When the RH is below the MDRH, only a solid phase is possible. Otherwise a liquid and solid phase may coexist (with $MDRH < RH < RHD$). For the latter case the aqueous phase concentrations are determined by WF. The summation over all partial water masses then yields the total aerosol water mass. But the gas–liquid–solid partitioning is reiterated until the solution converges and the

concentrations do not change further (equilibrate). For details see Fountoukis and Nenes (2007).

2. Here we follow the idea of a weighted mixed solution approach of ISORROPIA II, but we approximately solve the liquid–solid partitioning by computing the weighting factor non-iteratively. We compute the liquid–solid partitioning after solving the NRO (Sect. 2.3) and the gas–liquid partitioning (Sect. 2.4). For each salt compound (j) we analytically obtain the solid concentration $n_{j(s)}$ from its aqueous $n_{j(nro)}$ concentration (determined in the previous computation steps). Analogously to Fountoukis and Nenes (2007), we use a mixed solution weighting factor, $WF_{j,mix}$:

$$n_{j(s)} = n_{j(nro)} \times WF_{j,mix}, \quad (13)$$

with

$$n_{j(aq)} = n_{j(nro)} - n_{j(s)}, \quad (14)$$

where $n_{j(nro)}$ denotes an aqueous concentration of, e.g. $[NH_4NO_3]_{(nro)}$ from Eq. (12).

$WF_{j,mix}$ is defined for each compound (the j th salt solute in Table 3) by

$$WF_{j,mix} := \frac{(RHDMAX_j - RH)}{(RHDMAX_j - RHDMIN)} \quad (15)$$

always with a positive sign: $RHDMIN < RHDMAX_j$ and $RH < RHDMAX_j$. $RHDMIN$ and $RHDMAX_j$ are defined below. For $RH \geq RHDMAX_j$, $WF_{j,mix} = 0$; $RH \leq RHDMIN$, $WF_{j,mix} = 1$. Note that we use a different notation of $RHDMIN$ and $RHDMAX_j$ (instead of the MDRH and RHD used by Fountoukis and Nenes, 2007) to indicate that we are using different values and underlying mixed solution calculations, which do not necessarily have to yield the same results despite our constraint that the overall liquid–solid partitioning aims to be comparable.

To solve the liquid–solid partitioning analytically, i.e. without iteration, we modify the approach of Fountoukis and Nenes (2007). Each binary concentration $n_{j(nro)}$ is weighted by the total solute concentration, $n_{s,sum(nro)} = \sum_{j=1, N_{max}} n_{j(nro)}$ with all concentration units in $[mol\ m^{-3}(air)]$. But in our framework, $n_{s,sum(nro)}$ is directly obtained from the sum of all single solute concentrations that are formed by solving the neutralisation reaction order (Sect. 2.3). In case a semi-volatile compound has been initially neutralised, e.g. $[NH_4NO_3]_{(nro,max)}$, we additionally solve Eqs. (6)–(12) to obtain $n_{j(nro)} = [NH_4NO_3]_{(nro)}$ (Sect. 2.4), before we obtain a solute-specific weighting factor, WF_j , from:

$$WF_j := \frac{n_{j(nro)}}{n_{s,sum(nro)}} = \frac{n_{j(nro)}}{\sum_{j=1, N_{max}} n_{j(nro)}}. \quad (16)$$

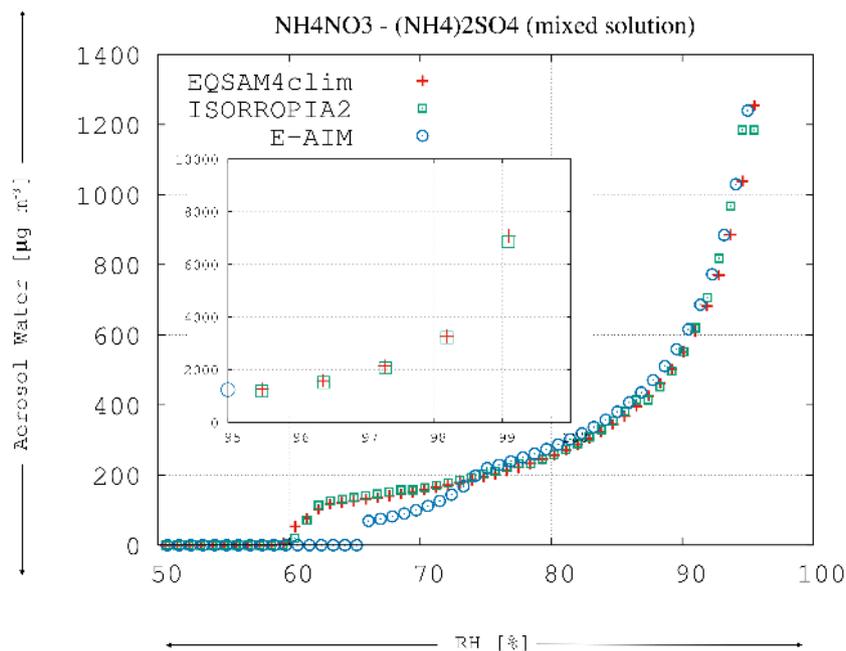


Figure 4. Results of EQSAM4clim (red crosses) and ISORROPIA II (green squares) for the total aerosol water mass $m_{w,mix}$ [$\text{kg m}^{-3}(\text{air})$] obtained by Eq. (22) for the mixed solution of NH_4NO_3 and $(\text{NH}_4)_2\text{SO}_4$ shown in Fig. 3 (lower panels). The results are shown for $\text{RH} = 50\text{--}97\%$ (large panels) and for the $\text{RH} = 95\text{--}99.5\%$ (small panel). The results of E-AIM (web version) (blue circles) are included for comparison. The mixed solution RHD has been obtained for EQSAM4clim from Eqs. (13)–(22) and are based on measured MDRH values for ISORROPIA II. The mutual deliquescence range of EQSAM4clim and ISORROPIA II (described in Sect. 2.6) differs from those of E-AIM (web version: <http://www.aim.env.uea.ac.uk/aim/aim.php>). This figure is extended by Fig. S3.

The maximum value of N_{\max} is limited by the domain-dependent NRO (see Table 3). It refers to aqueous solutes at this stage. The liquid–solid partitioning is computed below.

The concentration-weighted maximum RHD_j (upper threshold), which normally needs to be computed iteratively for each compound, is here directly obtained using WF_j :

$$\text{RHDMAX}_j := \text{RHDMIN} \times \text{WF}_j^{0.25} + \text{RHD}_j \times (1 - \text{WF}_j^{0.25}). \quad (17)$$

In case of mixed solutions, Eq. (17) is used to obtain the upper RH threshold, otherwise the compound's RHD_j given in Table 1 are used, while RHDMIN is computed here directly for $n_{s,\text{sum}(\text{nro})}$ only from v_i (see below). WF_j is introduced here with an exponent (empirically derived) to parameterise the results of ISORROPIA II, which uses iterations to solve the liquid–solid partitioning using MDRH measurements as the lower RH-threshold in Eq. (17).

To adhere to our key-constraints (Sect. 2, i.e. to minimise the dependency on the required thermodynamic data), we compute the RHDMIN from Eq. (5b) of M2012 (or Eq. A6 of the Appendix), by using the

mixed solution values for μ_s and v_i that correspond to $n_{s,\text{sum}(\text{nro})}$ (Eq. 16). Assuming $K_e = 1$, $A = 1$ and $B = 0$, the single RHDMIN value can be obtained from

$$\text{RHDMIN} := \left(1 + \mu_s^0 \times M_w \times v_{i,\text{mix}} \times \left(\frac{1}{\mu_s^0} \times \mu_{s,\text{sat,mix}} \right)^{v_{i,\text{mix}}} \right)^{-1}. \quad (18)$$

$\mu_{s,\text{sat,mix}}$ is the saturation solute molality and $v_{i,\text{mix}}$ the solute-specific constant of the mixed solution. $\mu_{s,\text{sat,mix}}$ and $v_{i,\text{mix}}$ are introduced here. $\mu_s^0 = 1$ [mol kg^{-1}] is the reference molality to match units. M_w [kg mol^{-1}] is the molar mass of water.

Due to a lack of experimental data, we approximate $\mu_{s,\text{sat,mix}}$ from the summation over all single solute molalities, $\mu_{s,\text{sat,single}}$ [mol kg^{-1}], using the relation to the mass fraction solubility (see, e.g., Eq. A11 of M2012). We therefore obtain $\mu_{s,\text{sat,mix}}$ from

$$\mu_{s,\text{sat,mix}} := \sum_{j=1, N_{\max}} \left[\frac{1}{M_{j(\text{single})} \times (100/W_{j(\text{single})} - 1)} \right]. \quad (19)$$

$M_{j(\text{single})}$ [kg mol^{-1}] is the single solute molar mass, $W_{j(\text{single})}$ [%] its mass fraction solubility. The data are

given in Table 1 for all compounds considered in this work.

With the mixed solution molality, $\mu_{s,\text{sat,mix}}$, we can directly compute the mixed solution solubility, $w_{s,\text{mix}}$, if we use as the corresponding total molar mass the sum of the molar masses over all (N_{max}) compounds that can dissolve in the mixed solution, i.e. $M_{s,\text{mix}} = \sum_{j=1,N_{\text{max}}} M_{j(\text{single})}$ (same compounds and N_{max} as in Eq. 16):

$$w_{s,\text{mix}} := \frac{1}{(\mu_{s,\text{sat,mix}} \times M_{s,\text{mix}})^{-1} + 1}, \quad (20)$$

where $0.1 < w_{s,\text{mix}} < 1$. Finally, we can obtain with Eq. (20) the solute-specific constant that corresponds to the mixed solution, $v_{i,\text{mix}}$, using an empirical equation that approximates $v_{i,\text{mix}}$ from the corresponding mixed solution solubility $w_{s,\text{mix}}$:

$$v_{i,\text{mix}} := (0.25 \times \ln(w_{s,\text{mix}}) + 1)^{-1}. \quad (21)$$

Thus, with Eq. (19) we solve Eq. (20) and with Eq. (20) we solve Eq. (21). With Eqs. (21) and (19) we solve Eq. (18) to obtain RHDMIN. Furthermore, with Eq. (16) we solve Eq. (17) to obtain RHDMAX_{*j*}. Together with RHDMIN we solve Eq. (15) to obtain $WF_{j,\text{mix}}$. $WF_{j,\text{mix}}$ is then used to compute the liquid–solid partitioning from Eqs. (13)–(14) after solving the NRO (Sect. 2.3) and the gas–liquid partitioning (Sect. 2.4), in case of semi-volatile compounds. Finally, the aerosol water uptake is computed for each salt compound that exists in the aqueous phase at the given T and RH from $n_{j(\text{aq})}$ (Eq. 14). See Figure S2.2 in the Supplement for a flow chart of the calculation.

2.7 Aerosol water uptake

To calculate the mixed solution aerosol water uptake, the standard procedure employs the widely used ZSR-mixing rule (see, e.g., SP2006, Eq. 10.98). Assuming that solute concentrations are in equilibrium with the ambient air, the total aerosol water mass, $m_{w(\text{mix})}$ [$\text{kg m}^{-3}(\text{air})$], can be directly obtained from the sum of all pure compound partial aerosol water masses in the case of a mixed solution (N compounds dissolved):

$$m_{w,\text{mix}} = \sum_{j=1,N} m_{w,j} = \sum_{j=1,N} \frac{n_{j(\text{aq})}}{\mu_{j(\text{aq})}}. \quad (22)$$

Here we follow the standard procedure, while the liquid–solid partitioning and the N compounds in the aqueous phase are solved non-iteratively with Sect. 2.6. N can differ from N_{max} considered in Eq. (16), because certain salt solutes may precipitate from the mixed solution during the

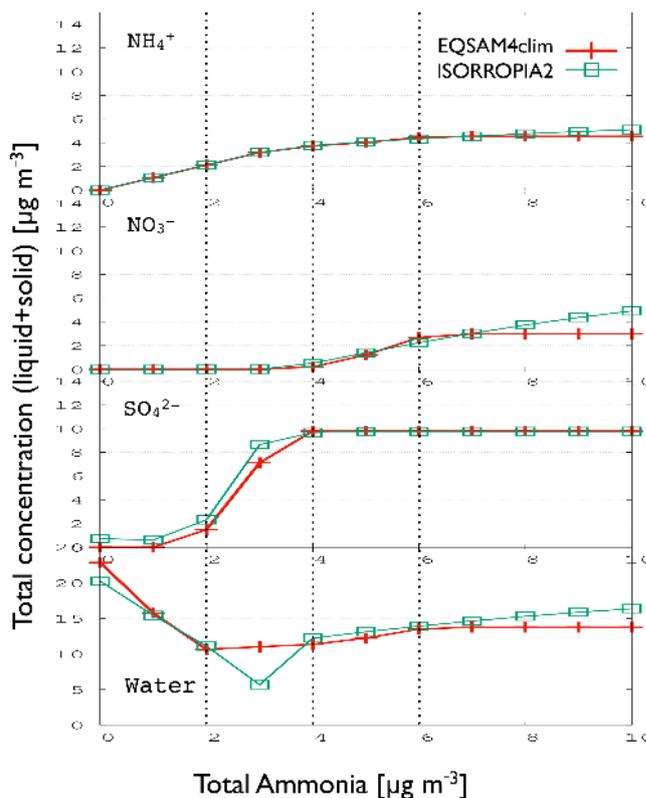


Figure 5. Mixed solution composition of NH_4NO_3 and $(\text{NH}_4)_2\text{SO}_4$ as a function of total ammonia at $T = 298.15$ [K] and $\text{RH} = 70$ [%], as defined in Seinfeld and Pandis (2006) for their Fig. 10.23. EQSAM4clim (red crosses) and ISORROPIA II (green squares) for $[\text{TS}] = [\text{TN}] = 10$ [$\mu\text{g m}^{-3}(\text{air})$]. Note that at zero ammonia, H_2SO_4 is at a maximum; shown in Fig. S4.

liquid–solid partitioning so that $N \leq N_{\text{max}}$. With increasing RH (from RHDMIN up to RHDMAX_{*j*}), an increasing number of compounds are considered for the water uptake calculations by Eq. (22). The partial aerosol water masses, $m_{w,j}$, which are associated with each binary solution (one compound and water), $n_{j(\text{aq})}$ [$\text{mol m}^{-3}(\text{air})$], can be directly obtained from tabulated single solute molalities, $\mu_{j(\text{aq})}$ [$\text{mol}(\text{solute}) \text{kg}^{-1}(\text{H}_2\text{O})$] (see Appendix A1), or parameterised based on Eq. (5a) of M2012 (Appendix A2, Eq. A3).

In case the RH is below the T -dependent RHD or the RHDMIN, we assume the compound to be dry and the partial aerosol water mass to be zero. Using the RH-dependent $\mu_{j(\text{aq})}$ parameterisation of M2012 (their Eq. 5a), we can solve Eq. (22) without iterations.

Our mixed solution framework is independent of the total aerosol water mass because

1. $n_{j(\text{aq})}$ is independent of $m_{w,\text{mix}}$, since it is directly given by our NRO (Sect. 2.3);

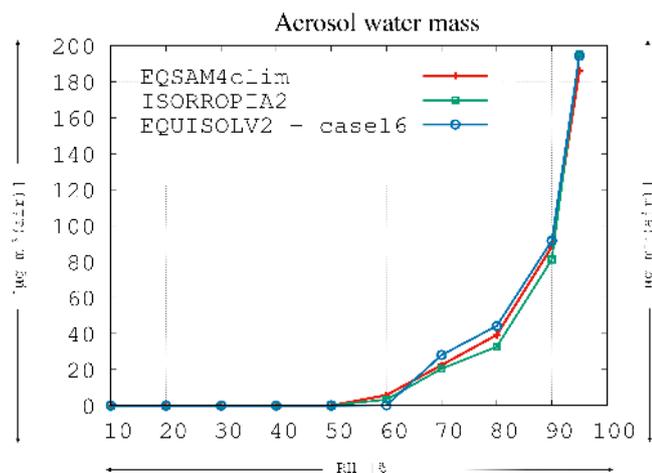


Figure 6. EQUISOLV II comparison – case 16. Bulk aerosol water mass as a function of RH for different sulfate molar ratios, fixed for the entire RH range (at constant $T = 298.15$ K). The dry concentration ratios of sulfate are $\frac{t_{\text{NH}_4}}{t_{\text{SO}_4}} = 2.0$, $\frac{t_{\text{NO}_3}}{t_{\text{SO}_4}} = 1.0$, $\frac{t_{\text{NaCl}}}{t_{\text{SO}_4}} = 0.5$, $\frac{t_{\text{K}}}{t_{\text{SO}_4}} = 0.04$, $\frac{t_{\text{Ca}}}{t_{\text{SO}_4}} = 0.02$, $\frac{t_{\text{Mg}}}{t_{\text{SO}_4}} = 0.01$ and corresponds to domain 1 of Table 2. This figure is extended to various (20 cases) sulfate molar ratios that are shown in Fig. S5 and correspond to Table 3 of Xu et al. (2009).

- $K_{p,AN}(T, \text{RH}, Y)$ is independent of $m_{w,\text{mix}}$, because of our $\chi_s(\text{RH})$ -based parameterisations of semi-volatile compounds, i.e. Eqs. (2)–(5) (Sect. 2.4)
- $\chi_s(\text{RH})$ is independent of $m_{w,\text{mix}}$, since it is directly given by $\mu_{j(\text{aq})}(\text{RH})$ (depending also only on v_i , and RH due to the relation Eq. A11 of M2012);
- $\mu_{j(\text{aq})}$ is independent of $m_{w,\text{mix}}$, since it only depends on v_i , and RH ($\mu_{j(\text{aq})}$ is based on Eq. 5a of M2012 and included with χ_s in Appendix A);
- Mixed solution RHDMIN is independent of $m_{w,\text{mix}}$, because of our mixed solution weighting factor, WF_{mix} , parameterisations, which also only depend on v_i , and RH.
- $m_{w,j}$ is independent of $m_{w,\text{mix}}$, because of the independence of points 1–5.

Finally, Eq. (22) is solved for diagnostic output only, since $m_{w,\text{mix}}$ does not need to be recalculated. Different from ISORROPIA II $m_{w,j}$ and $m_{w,\text{mix}}$ are not central in our gas–liquid–solid partitioning computations because of the v_i concept, which requires that the thermodynamic key-properties, $\mu_{j(\text{aq})}$ and χ_s , only depend on RH and v_i . Note that Eq. (22) can be equally used for so-called metastable aerosols, for which the formation of solid salts is generally not considered.

3 Application

We apply our parameterisation using EQSAM4clim. EQSAM4clim is entirely based on the mixed solution framework described in Sect. 2, which builds on the v_i approach of M2012. The underlying single solute parameterisation of solute molality, μ_s , and the relation to the solute mass fraction, χ_s , are summarised in Appendix A. The Appendix also includes a short description of EQSAM4clim (Sect. B), while the computational algorithm of EQSAM4clim is detailed in the Supplement (Sect. S2).

To evaluate EQSAM4clim we compare the single solute and mixed solution aerosol water uptake, as well as various other aerosol properties, against different reference models using box and global modelling calculations at various levels of complexity (see Table A1 for abbreviations):

- fixed solute concentrations (9 cases): ISORROPIA II and E-AIM (see also Sect. S3.1 in the Supplement);
- variable ammonia concentration: ISORROPIA II and SP2006 (see also Sect. S3.2 in the Supplement);
- variable solute concentrations (20 cases): ISORROPIA II and EQUISOLV II (see also Sect. S3.3 in the Supplement);
- field observations (MINOS campaign, 184 cases): ISORROPIA II (see also Sect. S3.4 in the Supplement);
- EMAC chemistry–climate model (year 2005): ISORROPIA II.

Selected results of each application case (1–5) are shown below, while the complete set of results are shown in the Supplement (Sect. S3). Throughout this work, all EQSAM4clim results will be primarily evaluated with respect to its ability to accurately simulate the water uptake of atmospheric aerosols, as this is a key process in climate modelling with our EMAC chemistry–climate model.

3.1 Fixed solute concentrations (9 cases): ISORROPIA II and E-AIM

Figure 4 shows the total aerosol water mass, $m_{w,\text{mix}}$ [$\text{kg m}^{-3}(\text{air})$] obtained by Eq. (22) for EQSAM4clim in comparison to the results of ISORROPIA II and E-AIM for the mixed solution case of NH_4NO_3 and $(\text{NH}_4)_2\text{SO}_4$ shown in Fig. 3 (lower panels). The results are based on the full gas–liquid–solid partitioning for EQSAM4clim in Sect. 2. This first example considers the simplest calculation case: dry compound concentration fixed to $1 [\mu\text{mol m}^{-3}(\text{air})]$. Figures 4 and S3 in the Supplement (see Supplement, Sect. 3.1)

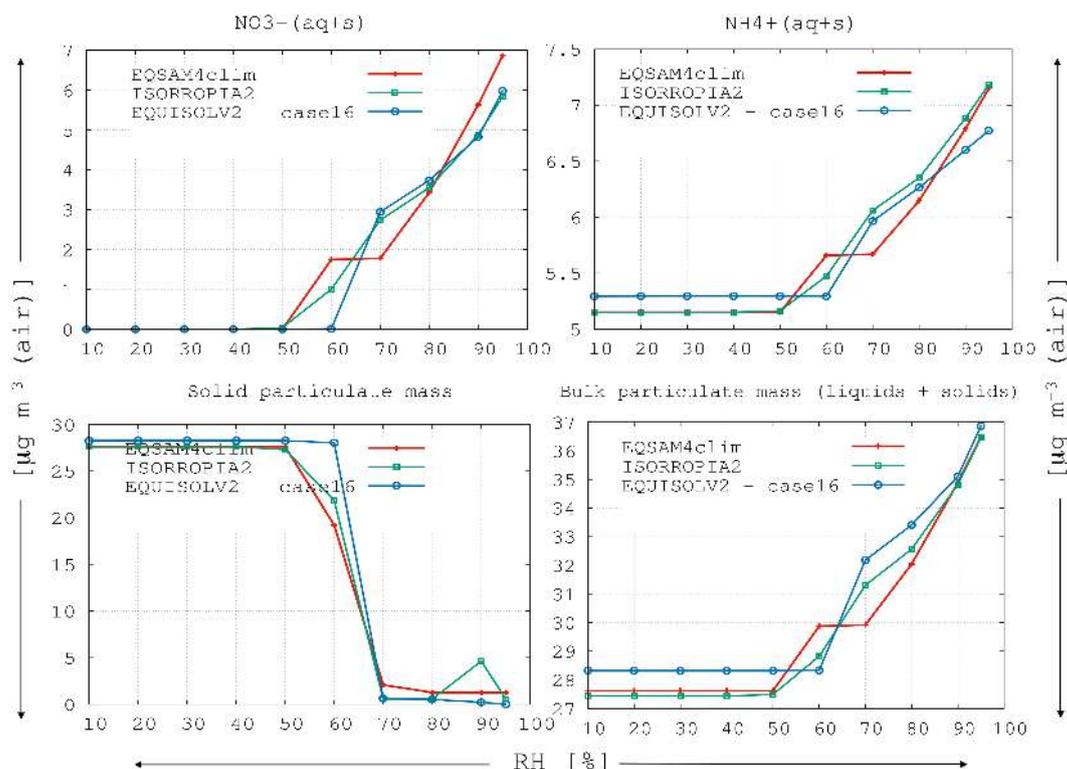


Figure 7. EQUISOLV II comparison – case 16. Bulk aerosol nitrate (ul), ammonium (ur), total solid PM (ll), liquid + solid PM (lr) as a function of RH for the sulfate molar ratios shown in Fig. 6. This figure is extended by Figs. S6 and S7.

show that the relatively largest differences occur for all cases in the (mutual) deliquescence range, while the general water uptake above this range is very similar for all three equilibrium models, despite the fundamental differences in the underlying approaches of the thermodynamic models.

3.2 Variable NH_3 concentration: ISORROPIA II and SP2006

To further evaluate the aerosol water uptake calculations of EQSAM4clim for variable concentrations, we first compare the mixed solution composition of NH_4NO_3 and $(\text{NH}_4)_2\text{SO}_4$ (at $T = 298.15\text{ K}$) as a function of total ammonia ($\text{NH}_3 + \text{NH}_4^+$), following SP2006; see their Fig. 10.23. Figure 5 shows the corresponding results in $[\mu\text{g m}^{-3}(\text{air})]$ of EQSAM4clim and ISORROPIA II – (from top to bottom) for ammonium, nitrate, sulfate and aerosol water, with bi-sulfate, sulfuric acid shown in the Supplement (Fig. S4). Overall, the results of EQSAM4clim and ISORROPIA II are close to those of Fig. 10.23 of SP2006. Minor differences in ammonium, nitrate and water occur at ammonia concentrations above $6\text{ }[\mu\text{g m}^{-3}(\text{air})]$, since the gaseous uptake of NH_3 and HNO_3 on saturated solutions is not considered for EQSAM4clim; see Supplement (Sect. S2). The EQSAM4clim results are for ammonia concentrations below $6\text{ }[\mu\text{g m}^{-3}(\text{air})]$ somewhat closer to those of SP2006 (see

their Fig. 10.23), while the opposite is true for higher ammonia concentrations.

3.3 Variable solute concentrations (20 cases): ISORROPIA II and EQUISOLV II

To scrutinise the differences between EQSAM4clim and ISORROPIA II, we further evaluate 20 variable mixed solution cases, following the comparison presented in Xu et al. (2009), using the corresponding sulfate molar ratios of their Table 3. Figures 6 and 7 show the modelling results for the following RHs: 10, 20, 30, 40, 50, 60, 70, 80, 90, 95 [%] in comparison to EQUISOLV II for case 16, which corresponds to domain D1 of Tables 2 and 3. The remaining cases are shown in Figs. S5–S7 in the Supplement. The aerosol composition is calculated from the full gas–liquid–solid equilibrium partitioning with the assumption that the aerosol lies on the deliquescence branch. Again, this comparison indicates that the relatively largest differences in the aerosol water mass calculations occur in the mutual deliquescence humidity range, while the general water uptake above this range is rather similar for all three equilibrium models (Fig. 6). This finding is also supported by the solid and total PM and confirmed by the total aerosol ammonium and nitrate comparison (Fig. 7). For all cases, the results of EQSAM4clim are

Table 5. MINOS aerosol statistics (see Figs. 8, 9 of Sect. 3.4; Appendix C for the evaluation metrics): EQSAM4clim (EQ4c) and ISORROPIA II (ISO2) versus MINOS observations (August 2001).

	Aerosol fine mode							
	HNO ₃		NH ₃		HCl		PM	
	EQ4c	ISO2	EQ4c	ISO2	EQ4c	ISO2	EQ4c	ISO2
Mean _m	19.86 ± 12.89	20.17 ± 13.05	74.16 ± 63.93	74.91 ± 63.41	69.86 ± 42.81	70.08 ± 42.55	0.13 ± 0.05	0.13 ± 0.10
Mean _o	19.56 ± 13.17	19.56 ± 13.17	41.13 ± 40.55	41.13 ± 40.55	78.26 ± 38.36	78.26 ± 38.36	0.17 ± 0.08	0.17 ± 0.08
r _m	16.81 ± 0.24	17.01 ± 0.25	37.35 ± 1.48	51.10 ± 0.43	44.75 ± 0.62	44.80 ± 0.62	0.13 ± 0.15	0.09 ± 0.46
r _o	16.15 ± 0.26	16.15 ± 0.26	32.33 ± 0.27	32.33 ± 0.27	69.89 ± 0.21	69.89 ± 0.21	0.15 ± 0.21	0.15 ± 0.21
RMSE	2.56	2.02	58.99	59.02	3.89	4.41	0.06	0.07
R	0.98	0.99	0.65	0.65	0.99	0.99	0.89	0.80
MBE	0.30	0.61	33.07	33.78	0.22	0.47	−0.03	−0.04
GFE	0.04	0.05	0.34	0.34	0.02	0.02	0.11	0.26
SS1	0.99	0.99	0.67	0.68	0.99	0.99	0.68	0.88
PF2	1.00	1.00	0.52	0.52	1.00	1.00	0.99	0.66
PF10	1.00	1.00	0.96	0.96	1.00	1.00	1.00	0.85
NPOINTS	124	124	122	122	110	110	124	124
	Aerosol coarse mode							
	HNO ₃		NH ₃		HCl		PM	
	EQ4c	ISO2	EQ4c	ISO2	EQ4c	ISO2	EQ4c	ISO2
Mean _m	13.39 ± 13.73	9.55 ± 12.34	43.57 ± 40.39	40.76 ± 41.05	57.58 ± 41.57	38.29 ± 41.11	0.23 ± 0.11	0.23 ± 0.14
Mean _o	19.56 ± 13.17	19.56 ± 13.17	41.13 ± 40.55	41.13 ± 40.55	78.26 ± 38.36	78.26 ± 38.36	0.19 ± 0.10	0.19 ± 0.10
r _m	5.79 ± 0.76	0.00 ± 12.54	35.09 ± 0.27	27.97 ± 0.46	39.17 ± 0.48	0.00 ± 11.11	0.20 ± 0.22	0.18 ± 0.36
r _o	16.15 ± 0.26	16.15 ± 0.26	32.33 ± 0.27	32.33 ± 0.27	69.89 ± 0.21	69.89 ± 0.21	0.17 ± 0.24	0.17 ± 0.24
RMSE	28.87	17.68	6.73	8.67	32.91	43.90	0.05	0.08
R	0.47	0.34	0.99	0.98	0.82	0.80	0.97	0.86
MBE	−2.09	−10.01	3.08	0.24	−20.58	−35.75	0.04	0.04
GFE	0.05	0.59	0.07	0.13	0.22	0.49	0.10	0.18
SS1	0.73	0.67	0.99	0.99	0.91	0.90	0.98	0.84
PF2	0.02	0.37	0.99	0.91	0.66	0.45	0.98	0.86
PF10	0.06	0.58	1.00	0.98	0.86	0.75	1.00	0.97
NPOINTS	124	124	122	122	110	110	124	124

close to the results of ISORROPIA II and EQUISOLV II (see also Supplement, Sect. S3.3).

The comparison of total nitrate and aerosol ammonium (Fig. 7) further reveals that also the semi-volatile compounds are rather well represented by EQSAM4clim, despite the underlying simplified analytical approach. Note that the lumped concentrations of the semi-volatile ions are shown only for the most complex cases, i.e. for the 10 sulfate neutral/poor cases (11–20). The common treatment among these EQMs is that both ammonium nitrate and ammonium chloride can be formed only when sulfate has been fully neutralised. A surplus of ammonia must exist to neutralise nitric acid and/or hydrochloric acid. Thus, their neutralisation also critically depends on the presence of the non-volatile, mineral cations, i.e. Ca²⁺, Mg²⁺, K⁺, Na⁺, which have been considered for certain cases (e.g. case 16). Depending on the sulfate loadings, these cations can practically determine the whole gas–liquid–solid partitioning and the water uptake (Metzger et al., 2006).

3.4 Field observations (MINOS campaign, 184 cases): ISORROPIA II

To scrutinise further mineral-rich cases and to extend our model inter-comparison to size-resolved aerosol observations, we further apply both gas–aerosol partitioning schemes to (184) field measurements of the Mediterranean INtensive Oxidant Study (MINOS) that were obtained during a campaign in Crete in the period of 27 July to 25 August 2001 (Lelieveld et al., 2002; Salisbury et al., 2003). Figures 8 and 9 compare the fine- and coarse-mode total particulate matter [$\mu\text{mol m}^{-3}(\text{air})$], the predicted associated water mass [$\mu\text{g m}^{-3}(\text{air})$] and the residual gases [$\mu\text{mol m}^{-3}(\text{air})$], i.e. [NH₃]_(g), [HNO₃]_(g), [HCl]_(g) obtained for EQSAM4clim from Eqs. (6)–(12) with the results of ISORROPIA II and the MINOS observations, following Metzger et al. (2006). For a general description of the measurements and the modelling set-up we refer to Metzger et al. (2006). Here we apply both gas–aerosol partitioning models at the same level of complexity by considering the ammonium–sulfate–nitrate–chloride–sodium–calcium–magnesium–potassium–water system, i.e. F4 and

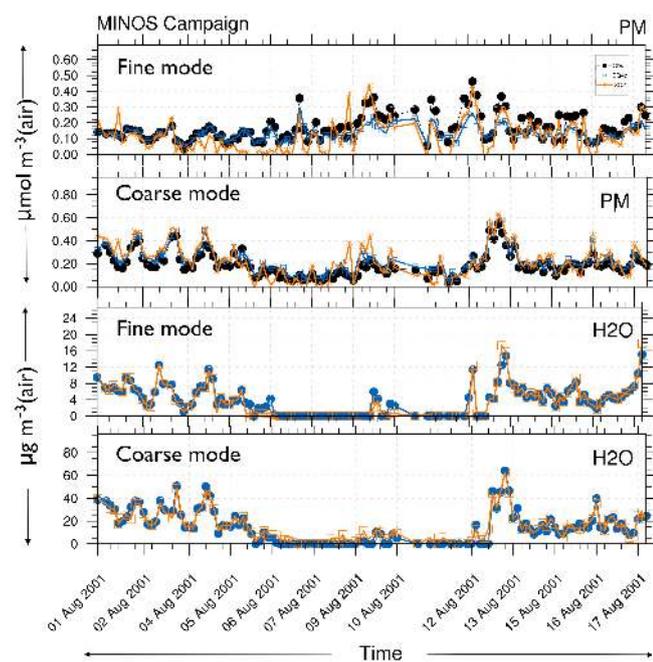


Figure 8. Observed and simulated total particulate matter [$\mu\text{mol m}^{-3}(\text{air})$] and the predicted associated water mass [$\mu\text{g m}^{-3}(\text{air})$] for the observed aerosol fine and coarse modes; EQSAM4clim (EQ4c), ISORROPIA II (ISO2), MINOS observations (black circles). This figure is extended to various other aerosol properties by Figs. S8 and S9 in the Supplement.

C4 in Table 1 of Metzger et al. (2006). Note that we omit here organic compounds for a consistent model inter-comparison, despite their relevance for the absolute comparison with observations. We refer to Metzger et al. (2006) for the influence of organic compounds on the ammonium partitioning during the MINOS campaign. Overall, also the size-resolved aerosol results of EQSAM4clim and ISORROPIA II are in close agreement with each other and reproduce field observations (see Table 5 for the statistics and Appendix C for the evaluation metrics and the additional comparison in the Supplement, Sect. S3.4).

3.5 EMAC vs. satellite and AERONET observations

To extend the model inter-comparison of EQSAM4clim and ISORROPIA II to global modelling applications, we use the atmospheric chemistry–climate model EMAC in a set-up following Abdelkader et al. (2015). Both gas–aerosol partitioning schemes are implemented in the GMXe aerosol microphysics submodule, as described in Pringle et al. (2010a, b) – fully coupled with the EMAC chemistry, transport and radiation schemes. EQSAM4clim and ISORROPIA II are embedded in EMAC in exactly the same way, so that a direct comparison of the global modelling results can be made. Deviations can be fully explained by differences in the gas–aerosol partitioning and water uptake calculation approach.

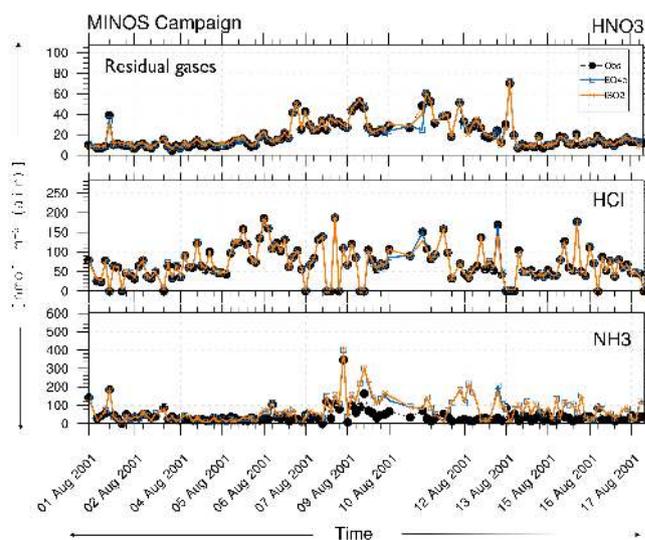


Figure 9. Residual gases [$\mu\text{mol m}^{-3}(\text{air})$] corresponding to Fig. 8.

To evaluate the EMAC results, we compare the aerosol optical depth (AOD) to three independent observational data sets, i.e. two satellites products, i.e. MODIS (MODerate resolution Imaging Spectroradiometer) and MISR (Multi-angle Imaging Spectro-Radiometer), and one ground-based product, i.e. from the AEROSOL ROBOTIC NETWORK (AERONET), <http://aeronet.gsfc.nasa.gov>. The AOD, or extinction coefficient, is a measure of radiation scattering and absorption at different wavelengths and sensitive to the gas–liquid–solid partitioning and aerosol hygroscopic growth. MODIS monitors the ambient AOD over the oceans and over a portion of the continents (see <http://modis-atmos.gsfc.nasa.gov/>). The MISR aerosol product is available globally. Both data products (and further information) are available from <http://disc.sci.gsfc.nasa.gov/giovanni>.

Figure 10 compares the model simulations and observations for the year 2005 (annual mean based on 5-hourly values). The upper left panel shows the EMAC results based on ISORROPIA II, the upper right panel shows the results based on EQSAM4clim; the results represent two independent simulations with an identical model set-up and spin-up. The AOD observations of MODIS and MISR are shown in the lower left and right panels, respectively. The qualitative comparison already shows that the differences between the two EMAC simulations and the satellite observations are larger than the differences between the two different EMAC simulations (despite the two distinct different gas–aerosol partitioning schemes). This result is supported by the AERONET observations, which are included in Fig. 10 as squares (with the same AOD colour scale). With respect to the observations, EMAC slightly underestimates the AOD, mainly over the open oceans, intense biomass burning and dust outbreaks, including the trans-Atlantic dust transport. Although the global dust belt seems to be captured rather well by the

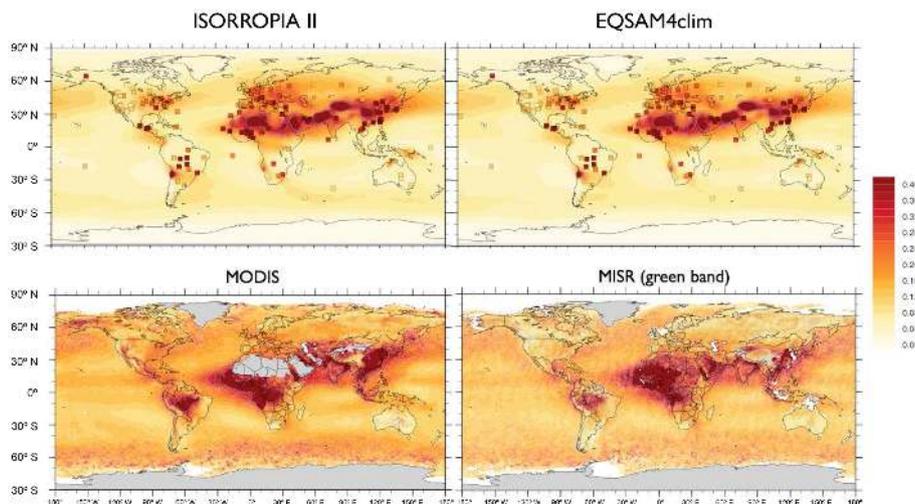


Figure 10. EMAC AOD vs. MODIS, MISR and AERONET (550 nm, annual mean 2005).

EMAC simulations, the current model set-up somewhat underestimates the AOD for the year 2005. The main reason is that we have limited the water uptake only to major inorganic salt compounds (those considered above in Sect. 3.4) for the sake of a consistent model inter-comparison of the two gas–aerosol partitioning schemes. A more complete set-up that includes the water uptake of, e.g., biomass burning and organic compounds, will be presented separately. Nonetheless, considering the differences between the observations and the uncertainty of the AOD products, also these EMAC model predictions of EQSAM4clim and ISORROPIA II seem reasonable.

4 Conclusions

We have successfully extended the ν_i parameterisations from single to mixed solutions. The novelty of our single parameter framework is given by the fact that only one coefficient per compound is required to solve the multicomponent gas–liquid–solid partitioning. Our results show that this approach is possible, since we use (i) a consistent set of equations that are all based on the mass fraction solubility χ_s (Eq. A1) and ν_i (Sect. 2), and (ii) since we can assume ν_i to be constant (Sect. 2.1 and A4) for the entire range of water activity, a_w (for the a_w parameterisation see Eq. 5a of M2012 and Eq. A3). For semi-volatile compounds, we (iii) parameterise the temperature- and humidity-dependent equilibrium dissociation constant, $K_{p,AN}(T, RH)$, by substituting required activity coefficients with a new equation that is also only based on χ_s and ν_i (Eqs. 1–5). The advantage is that ν_i can be accurately determined from one single data pair, i.e. the widely used solute’s mass fraction solubility and the corresponding a_w – for the latter we use in this work RHD measurements (Sects. 2.1 and A4). With M2012 we have demonstrated that the ν_i concept allows one to accurately determine the aerosol

water mass of binary solutions, $m_{w,j}$, for a given solute concentration $n_{j(aq)}$. With this work we have shown that this is also true for the total aerosol water mass of mixed solutions, $m_{w,mix}$ (Eq. 22), by using μ_s (Eq. A3). Differences to reference calculations are basically caused by the assumptions made on the mixed solution RHD (Sect. 2.6), i.e. the different assumptions on the mutual deliquescence humidity range. Examples that can be verified with a pocket calculator are presented in the Supplement (Sect. S1) – they support the various box and global modelling results of Sects. 3 and S3.

5 Data availability

The underlying research data is available on request.

Appendix A: Single solute solutions

A1 Solute mass fraction, χ_s , and solute molality, μ_s

The relation between solute mass fraction χ_s and solute molality μ_s is central in our mixed solution parameterisation framework (Sect. 2). Both can be expressed through each other (see, e.g., Eq. A11 of M2012). The solute mass fraction, χ_s [–], is defined as the mass [kg] of solute, $m_s = n_s \times M_s$, relative to the total mass [kg] of the solution composed out of the mass of solute m_s and water, $m_w = n_w \times M_w$:

$$\begin{aligned} \chi_s &:= \frac{m_s}{(m_s + m_w)} = \left(\frac{m_w}{m_s} + 1\right)^{-1} = \left(\frac{n_w \times M_w}{n_s \times M_s} + 1\right)^{-1} \\ &= \left(\frac{1}{M_s \times \mu_s} + 1\right)^{-1} \end{aligned} \quad (\text{A1})$$

n_s and n_w [mol] are the number of moles of solute and solvent (water), M_s and M_w [kg mol⁻¹] are the corresponding molar masses of the solute and water, respectively.

The solute molality is defined as the number of moles of solute per kilogram of water, i.e. μ_s [mol(solute) kg⁻¹(H₂O)]. It can be expressed in terms of the solute mass fraction by

$$\mu_s := \frac{n_s}{1 \text{ kg H}_2\text{O}} = \frac{n_s}{m_w} = \frac{n_s}{n_w \times M_w} = \frac{1}{M_s \times (1/\chi_s - 1)}. \quad (\text{A2})$$

μ_s measurements, tabulated as a function of water activity (a_w), are used in atmospheric modelling under the assumption that a_w equals RH to obtain the single solute (partial) aerosol water mass that is in equilibrium with a given amount of the single solute, n_s , at the given RH from Eq. (22); see Sect. 2.7. Under this assumption, μ_s is a function of RH, actually a_w , but in any case a function of the available water vapour mass, m_w , which is in equilibrium associated with the solute mass, m_s . This illustrated in Figs. A1 and A2 for several electrolytes used in this work; the solid lines refer to μ_s measurements, the dotted lines to a parameterisation; see Sect. A2. Since for atmospheric applications, the aerosol associated water mass depends on the available water vapour mass, M2012 have expressed the single solute molality as a function of RH and a solute-specific coefficient, v_i . The M2012 concept is summarised in the following and has been extended to mixed solutions in Sect. 2.

A2 Parameterisation of μ_s and χ_s

The representation of water activity (M2012) relates a_w to the solute molality μ_s through a single solute-specific constant, v_i . This is a major advantage compared to other parameterisations, because the number of unknowns is reduced to one. To extend the v_i approach to mixed solutions we use the parameterisation of solute molality

μ_s [mol(solute) kg⁻¹(H₂O)]. Inverting Eq. (5a) of M2012 allows one to express μ_s as a function of RH and v_i , with $a_w := \frac{\text{RH}}{K_e}$:

$$\mu_s = \mu_s^0 \times \left(\left[\frac{1}{\mu_s^0 \times M_w \times v_i} \times \left(\frac{K_e}{\text{RH}} - A \right) \right]^{\frac{1}{v_i}} - B \right) \quad (\text{A3})$$

The equivalent expression for χ_s [–] is given by inserting Eq. (A3) in Eq. (A1).

$\mu_s^0 = 1$ [mol kg⁻¹] denotes a reference to match units. M_w [kg mol⁻¹] is the molar mass of water and v_i a single solute-specific constant. K_e denotes the Kelvin term (see Sect. A5) and depends on the mass equivalent hygroscopic growth factor, GF (see Sect. A6). The terms A and B are defined by M2012; see their Eqs. (2) and (3) and are slightly revised (further simplified) in the following.

A3 Parameterisation of A and B terms

To break down the thermodynamics as much as possible, we use a simplified representation of the A and B terms compared to M2012. Throughout this work, we use a B term that has been empirically determined to be a function of v_i with the constraint that $A := 1$. Here, B is expressed in terms of the solute mass fraction χ_s and defined as

$$B := \chi_s^{\left[\frac{1}{1+v_i+\chi_s} \right]}. \quad (\text{A4})$$

To express χ_s in Eq. (A4), we use Eq. (A3) for μ_s (right term of Eq. A1).

A4 Relative humidity of deliquescence (RHD)

To pre-determine v_i for our mixed solutions framework we use RHD measurements at $T_0 = 298$ [K]; see Sects. 2.1 and 2.3 in M2012. To solve our mixed solution framework we calculate the temperature dependency from Wexler and Potukuchi (1998):

$$\text{RHD}(T) = \text{RHD}(T_0) \times \exp \left[T_{\text{coef}} \times \left(\frac{1}{T} - \frac{1}{T_0} \right) \right]. \quad (\text{A5})$$

The RHD measurements at $T_0 = 298$ and the corresponding temperature coefficients are taken from Fountoukis and Nenes (2007) and listed in Table 1.

To determine v_i , we solve Eq. (5b) of M2012, which we include here for completeness:

$$\text{RHD} = \quad (\text{A6})$$

$$\frac{K_e}{\left(A + \mu_s^0 \times M_w \times v_i \times \left[\frac{1}{\mu_s^0} \times \frac{1}{M_s \times (1/w_s - 1)} + B \right]^{v_i} \right)}.$$

The RHD [–] describes the point of water activity, a_w [–], where a solution is saturated. Any excess of solute leads to solute precipitation and co-existence of a solid and liquid

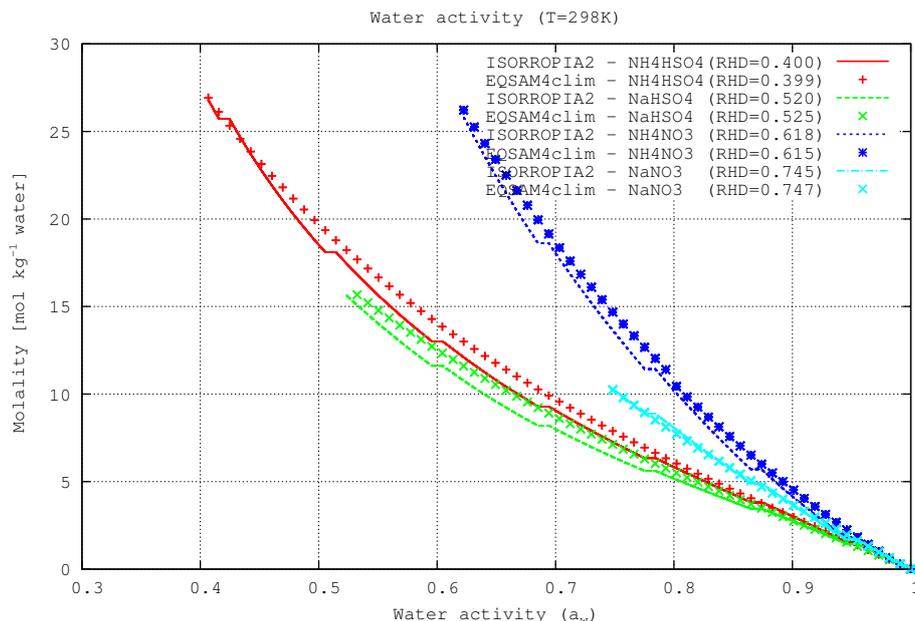


Figure A1. Single solute molality as a function of water activity for several electrolytes: $(\text{NH}_4)\text{HSO}_4$, NaHSO_4 , NH_4NO_3 , NaNO_3 (at $T = 298.15$ K) calculated with EQSAM4clim from Eqs. (A3) and (A6) compared to tabulated molality and RHD measurements of ISORROPIA II used to determine ν_i .

Table A1. List of names and abbreviations.

Abbreviation	Name
AOD	Aerosol Optical Depth
AERONET	AErosol RObotic NETwork (http://aeronet.gsfc.nasa.gov)
CNN	cloud condensation nuclei
CPU	computational performance unit
EQMs	Thermodynamic equilibrium models
E-AIM	(Wexler and Clegg, 2002), http://www.aim.env.uea.ac.uk/aim/aim.php
EQSAM	Equilibrium Simplified Aerosol Model (Metzger et al., 2002b)
EQSAM4clim	Equilibrium Simplified Aerosol Model (Version 4) for Climate Simulations (this work)
EQUISOLV II	Jacobson (1999)
EMAC	Atmospheric Chemistry-climate model ECHAM5/MESy2.50 (Abdelkader et al., 2015)
GMXe	Global Modal-aerosol eXtension (Pringle et al., 2010a, b)
ISORROPIA II	Fountoukis and Nenes (2007)
MODIS	MODerate resolution Imaging Spectroradiometer (http://modis-atmos.gsfc.nasa.gov/)
MISR	Multi-angle Imaging Spectro-Radiometer (http://disc.sci.gsfc.nasa.gov/giovanni)
MINOS	Mediterranean INTensive Oxidant Study (Lelieveld et al., 2002; Salisbury et al., 2003)
NRO	neutralisation reaction order (Sect. 2.3)
M2012	Metzger et al. (2012)
SP2006	Seinfeld and Pandis (2006)

phase (see Sects. 2.6 and 2.7). At solute saturation, the solute mass fraction (Eq. A1) is measured by the widely used mass fraction solubility w_s [–]. Since the saturation molality $\mu_{s,\text{sat}}$ and the mass fraction solubility w_s are related through Eq. (A2), i.e. $\mu_{s,\text{sat}} = \frac{1}{M_s \times [1/w_s - 1]}$, M2012 express the RHD in terms of w_s and a single solute-specific coefficient, ν_i . For a given w_s and RHD data pair, ν_i can be accurately determined if Eq. (A6) is solved with a root-finding method

(e.g. bisection). This procedure has been detailed in M2012 and only requires one data pair. To pre-determine ν_i for all salt compounds used in this work, we follow M2012 and use the w_s and RHD measurements at $T_0 = 298$ [K]. The pre-determined ν_i values used are included in Table 1. To solve our mixed solutions framework we assume ν_i constant and independent of the temperature. Therefore, Eq. (A6) is not needed. It could be used during runtime, e.g. within

Table A2. List of greek symbols.

Greek symbol	Name	Unit
ν_i	solute-specific constant (introduced by M2012)	[–]
ν_s	stoichiometric coefficient of solute (\pm ion-pair)	[–]
μ_s	molality of solute	[mol kg ⁻¹ (H ₂ O)]
μ_s^0	reference molality of 1 mole of solute (considering stoichiometry)	[mol kg ⁻¹ (H ₂ O)]
μ_s^{sat}	saturation molality of solute	[mol kg ⁻¹ (H ₂ O)]
ρ_s	density of solute	[kg m ⁻³]
ρ_w	density of water	[kg m ⁻³]
σ_{sol}	surface tension of the solution droplet	[J m ⁻²]
χ_s	solute mass fraction, referring to the solute's dry mass	[–]
χ_s^{sat}	solute mass fraction, referring to the solute's dry mass at saturation	[–]
sat	superscript, indicator for saturation	
(cr)	subscript, phase indicator for anhydrous (solid = crystalline = cr) phase	
(aq)	subscript, phase indicator for aqueous phase	
(g)	subscript, phase indicator for gas phase	

Table A3. List of symbols.

Symbol	Name	Unit
A	A term of Eq. (A4), introduced with Sect. A3	[–]
B	B term of Eq. (A4), introduced with Sect. A3	[–]
a_w	water activity (Raoult-term)	[–]
D_s	dry droplet diameter of the solute	[m]
D_{wet}	wet droplet diameter of the solution	[m]
K_e	surface or Kelvin term of the solution	[–]
m_s	crystalline mass of solute	[kg]
m_w	aqueous mass of water (solvent)	[kg]
M_s	molar mass of solute	[kg mol ⁻¹]
M_w	molar mass of water	[kg mol ⁻¹]
n_s	moles of solute	[mol]
$\sum_i n_i$	summation over all moles of solutes	[mol]
n_w	moles of water	[mol]
GF	Growth Factor	[–]
RH	relative humidity in percent (as used in the text)	[%]
RH	fractional relative humidity (as used in equations)	[–]
RHD	fractional relative humidity of deliquescence	[–]
s	saturation ratio	[–]
S	supersaturation	[–]
S_c	critical supersaturation in percent	[%]
T_{coef}	dimensionless temperature coefficients for the RHD	[–]
T_0	reference temperature in Kelvin	[298.15 K]
T	temperature in Kelvin	[K]
w_s	mass fraction solubility, referring to the solute's dry mass required for saturation	[–]
W_s	mass fraction solubility, referring to the solute's dry mass required for saturation	[%]
tCAT	total cations (for chemical domains; Sect. 2.2)	[mol m ⁻³ (air)]

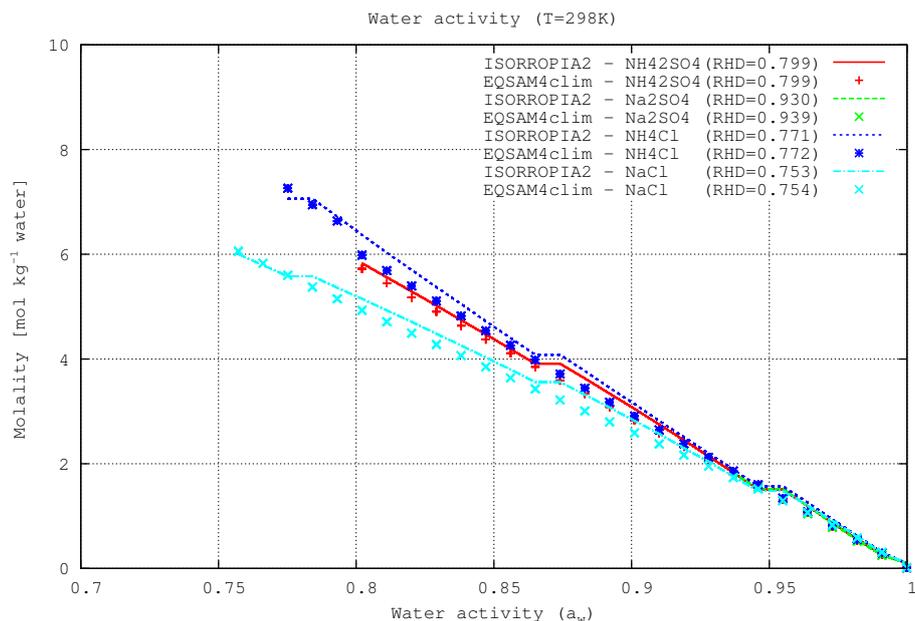


Figure A2. Figure A1 continued for $(\text{NH}_4)_2\text{SO}_4$, Na_2SO_4 , NH_4Cl , NaCl (at $T = 298.15 \text{ K}$).

EQSAM4clim (see Sect. B), to determine v_i for different T . But this is beyond the scope of this work, since the reference models currently available to evaluate our mixed solution parameterisation framework are also based on water activity data at T_0 .

A5 Kelvin term

The parameterisation of solute molality, μ_s (introduced by M2012), depends on the so-called Kelvin term, K_e [–] (Eq. A3), which can be expressed in terms of the growth factor, g_s :

$$K_e = \exp\left(\frac{4 \times M_w \times \sigma_{\text{sol}}}{R \times T \times \rho_w \times D_w}\right) = \exp\left(\frac{4 \times M_w \times \sigma_{\text{sol}}}{R \times T \times \rho_w \times g_s \times D_s}\right) \quad (\text{A7})$$

σ_{sol} [J m^{-2}] denotes the RH-dependent surface tension of the solution droplet. T [K] is the droplet temperature, $R = 8.314409$ [$\text{J mol}^{-1} \text{K}^{-1}$] the ideal gas constant, M_w [kg mol^{-1}] the molar mass and ρ_w [kg m^{-3}] the density of water. D_{wet} and D_s [m] are the ambient and dry droplet diameter, respectively.

A6 Growth factor

Equation (A7) depends on the RH-dependent (mass equivalent) hygroscopic growth factor, g_s [–]. We assume a geometric diameter = mass equivalent diameter of a compact spherical droplet and a constant surface tension of pure water droplets, i.e. $\sigma_{\text{sol}} = 0.0761$ [J m^{-2}]. We further assume that the droplet temperature is in equilibrium with the ambient air,

and we consider the widely used volume additivity. Then, the volume of the solution droplet can be expressed as the sum of volumes of the dry solute and that of the associated pure (aerosol) water contained in the droplet. The ambient diameter, D_{wet} , of the droplet can therefore be expressed in terms of the solute dry diameter, D_s , and g_s :

$$g_s := \frac{D_{\text{wet}}}{D_s} = \left(\frac{V_w + V_s}{V_s}\right)^{1/3} = \left(\frac{V_w}{V_s} + 1\right)^{1/3} = \left(\frac{\rho_s \times m_w}{\rho_w \times m_s} + 1\right)^{1/3} = \left(\frac{\rho_s}{M_s \times \rho_w \times \mu_s} + 1\right)^{1/3}. \quad (\text{A8})$$

$V_w + V_s$ [m^3] is the total volume of the wet droplet with $V_s = m_s/\rho_s = n_s M_s/\rho_s$ and $V_w = m_w/\rho_w = n_w M_w/\rho_w$ [m^3], i.e. the volumes of the initially dry solute and the associated pure water, respectively. m_s and m_w [kg] denote the corresponding solute and water masses, M_s and M_w [kg mol^{-1}] the molar masses, n_s and n_w [mol] the number of moles, and ρ_s and ρ_w [kg m^{-3}] the densities, respectively.

Appendix B: EQSAM4clim

We apply our new mixed solution parameterisation framework (Sect. 2) in the Equilibrium Simplified Aerosol Model V4 for climate simulations. Selected results are shown in Sect. 3, which are extended in the Supplement. EQSAM4clim aims at accurate but numerically efficient water uptake calculations that are applicable to high-resolution or long-term modelling at climate timescales, i.e. decades to centuries. In contrast to previous EQSAM versions and

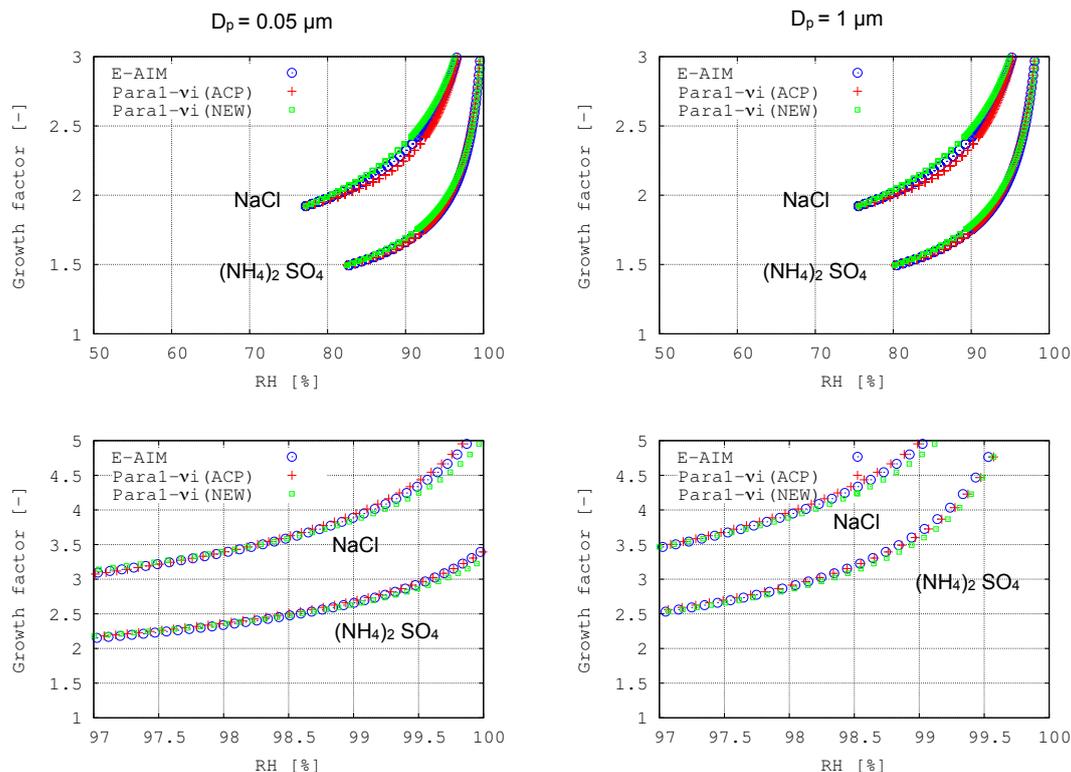


Figure B1. Growth factor of pure $\text{NaCl}_{(\text{cr})}$ and $(\text{NH}_4)_2\text{SO}_{4(\text{cr})}$ particles with a dry diameter $D_s = 0.05 \mu\text{m}$ (UL) and $D_s = 1 \mu\text{m}$ (UR) for $\text{RH} \leq 97 [\%]$. Lower panels show the corresponding values within the subsaturated regime, i.e. $97 \leq \text{RH} \leq 100 [\%]$. The results of the parameterisation used by EQSAM4clim (labelled NEW) are compared to our ACP(M2012) water activity, a_w -parameterisation (labelled ACP, i.e. Para1 of Table 1 in M2012). The comparison includes the results of E-AIM and extends the corresponding figures of M2012.

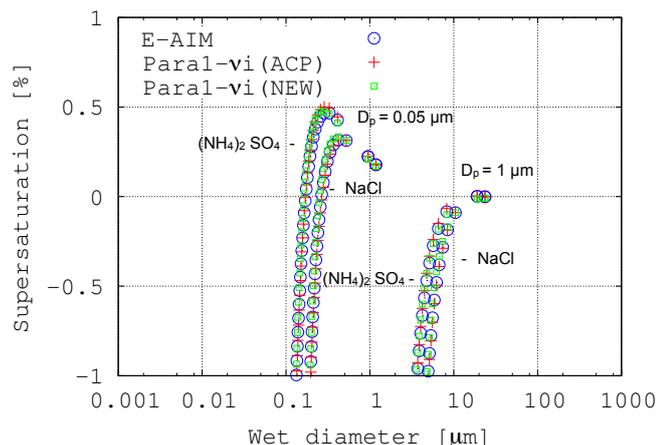


Figure B2. Wet particle diameter, D_{wet} , as a function of supersaturation for pure NaCl and $(\text{NH}_4)_2\text{SO}_4$ aerosols with different dry diameters, i.e. $D_s = 0.05$ and $D_s = 1 \mu\text{m}$ as shown in Fig. 5 of M2012. S is defined as $S = (s - 1) \times 100 [\%]$; s is the saturation = fractional RH.

all other thermodynamic gas–liquid–solid aerosol partitioning models, EQSAM4clim considers a consistent, simplified mixed solution parameterisation, which can be solved ana-

lytically. Our key equation of solute molality, μ_s , (Eq. A3), and the entire mixed solution phase partitioning (Sect. 2) can be solved analytically, even with a pen and pocket calculator as demonstrated in the Supplement (Sect. 1). EQSAM4clim (as all other EQSAM versions) builds on the fact that for atmospheric applications, μ_s can be expressed as a function of relative humidity (RH); Sect. A2. This was first demonstrated by Metzger et al. (2002a) (based on Metzger et al., 1999; Metzger 2000, PhD Thesis, University of Utrecht, the Netherlands; <http://adsabs.harvard.edu/abs/2000PhDT....328M>; provided by the SAO/NASA Astrophysics Data System).

To solve our mixed solution framework, we express g_s in terms of μ_s to reduce the number of unknowns to one, i.e. v_i ; assuming the aerosol dry size D_s , temperature (T) and relative humidity (RH) are prescribed (e.g. given during runtime as model input). Since $g_s [-]$ is defined as the ratio of wet to dry droplet diameter, it can be expressed in terms of the solute molality (by using either Eq. A2 or Eq. A3). Due to its implicit character in μ_s , solving Eq. (A3) requires iterations. One can apply an efficient root finding algorithm, which converges quickly. Treating K_e and the B term as perturbation, it is possible to truncate after the fourth iteration. Higher accuracy will not improve the results much further.

For EQSAM4clim, we solve Eq. (A3) for a given aerosol composition, with T , RH and D_s as the unknown variables that are given at model input for each model grid box and time step. Note that we use the K_e term for Eq. (A3), so that EQSAM4clim compares to Para1 of M2012 (see their Table 1).

We solve μ_s for all compounds listed in Table 1 for a given RH from a two-step approach:

- Step one: $K_e = 1$, and $B = 0$ to obtain the initial μ_s from Eq. (A3).
- Step two, repeated three times: μ_s from previous iteration is used to calculate K_e from Eq. (A7), χ_s from Eq. (A1), B from Eq. (A4). Then a new μ_s is obtained from Eq. (A3).

Figures A1 and A2 show μ_s obtained from Eq. (A3) (applied within EQSAM4clim) as a function of bulk water activity, i.e. $K_e = 1$ and $a_w = \text{RH}$, for major electrolytes (at $T = 298.15 \text{ K}$). All single solute molalities compare well with the tabulated solute molality data (Sect. A1) used in ISORROPIA II (and other EQMs) for the entire a_w -range: from the water activity at saturation, i.e. RHD, up to $a_w = 1$ (pure water). Furthermore, the results of M2012 can be reproduced with Eq. (A3) using the modified B -term, Eq. (A4) with $A = 1$. Figure B1 compares the GF obtained with Eq. (A8) (marked as NEW) for pure $\text{NaCl}_{(\text{cr})}$ and $(\text{NH}_4)_2\text{SO}_{4(\text{cr})}$ particles with a dry diameter $D_s = 0.05 \text{ } [\mu\text{m}]$ and $D_s = 1 \text{ } [\mu\text{m}]$ against those of M2012 (marked as ACP(M2012) = Para1) and E-AIM for the subsaturated RH regime with $\text{RH} \leq 97 \text{ } [\%]$ (upper panels), and the subsequent regime, i.e. $97 \leq \text{RH} \leq 100 \text{ } [\%]$ (lower panels). Figure B2 compares the corresponding wet particle diameter, D_{wet} , as a function of supersaturation (all at $T = 298.15 \text{ K}$); see description of Figs. 3, 4 and 5 of M2012.

Besides significant computational speed-up, another advantage is that our framework minimises the number of thermodynamic data that are typically required, while it enables greater flexibility with respect to the extension to other compounds, not considered in this evaluation. EQSAM4clim (v09) is limited to the same salt compounds as ISORROPIA II, so that the single solute parameter ν_i , which is required to solve the single solute molality, μ_s (Eq. A3), can be determined from a single reference data pair (Sect. A4). In addition, most computations are comprehensive and complex. In contrast, the numerical algorithm of EQSAM4clim is simple and easier to verify, since it does not involve any numerical solution or iteration to solve the gas–liquid–solid partitioning for the reasons summarised in Sect. 2.7.

EQSAM4clim has the advantage of being a short Fortran 90 (f90) code with approximately 850 lines, including comments (or 8 pages); see Fig. S1 in the Supplement for a sample. Figure S2.1 in the Supplement shows the flow chart of processes and operations; the computational algorithm is summarised in the Supplement (Sect. S2). For compari-

son, the gas–aerosol partitioning routine ISORROPIA II, also used in EMAC counts roughly 36 300 lines (or approx. 360 pages). For comparison, this is about one-third of the source code of the EMAC climate model core (ECHAM5.3.02), which has about 120 000 lines of f90 code (both including comments). Last but not least, due to its analytical structure the additional computational costs of EQSAM4clim are negligible for our climate applications, which will be detailed and presented separately.

Appendix C: Evaluation metrics

- RMSE – root mean square error between the model (m) and the observations (o):

$$\text{RMSE} = \sqrt{\frac{1}{N} \sum (X_m - X_o)^2} \quad (\text{C1})$$

- σ – standard deviation of the model (σ_m) and the observed (σ_o) value:

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (X_i - \bar{X})^2}, \text{ where } \bar{X} = \frac{1}{N} \sum_{i=1}^N X_i \quad (\text{C2})$$

- R – correlation coefficient between the model (m) and the observations (o):

$$R = \frac{\sum_{i=1}^N (X_i^m - \bar{X}^m)(X_i^o - \bar{X}^o)}{\sqrt{\sum_{i=1}^N (X_i^m - \bar{X}^m)^2 \sum_{i=1}^N (X_i^o - \bar{X}^o)^2}} \quad (\text{C3})$$

- MBE – mean bias error between the model (m) and the observations (o):

$$\text{MBE} = \frac{1}{N} \sum (X_m - X_o) \quad (\text{C4})$$

- r – geometric mean of the model (r_m) and the observations (r_o):

$$r = \sqrt[n]{\prod_{i=1}^N X} \quad (\text{C5})$$

- GFE – growth factorial error:

$$\text{GFE} = \frac{1}{N} \sum \frac{|(X_m - X_o)|}{X_m + X_o} \quad (\text{C6})$$

- SS1 – skill score between the model (_m) and the observations (_o):

$$\text{SS1} = \frac{4(1 + R)}{(\sigma_f + 1/\sigma_f)^2(1 + R_0)},$$

where $\sigma_f = \frac{\sigma_o}{\sigma_m}$ $R_0 = 0.0$ (C7)

PF2 is fraction of the number of points within a factor of 2 of the observations, PF10 is fraction of the number of points within a factor of 10 of the observations, and NPoints is the number of points used.

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