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# Age of Information: A New Concept, Metric, and Tool

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# Contents

1	Introduction		
2	The	Introduction of the Concept	5
	2.1	Age of Information	5
	2.2	First Queue-theoretic System Abstractions	10
	2.3	Summary	15
3	The	Early Works	16
	3.1	Sharing the System Among Multiple Traffic Streams	17
	3.2	Basic Scheduling Through Queues	21
	3.3	Peak Age of Information	27
	3.4	Availability of Resources	30
	3.5	Packet Management	40
	3.6	Summary	53
4	Subsequent Works and Extensions		
	4.1	Rate Control Optimization	56
	4.2	Packet Deadlines	61
	4.3	Optimizing Age, Throughput, and Delay	66
	4.4	Summary	68

# Full text available at: http://dx.doi.org/10.1561/1300000060

5	Age	as a Tool	69		
	5.1	Channel State Information	69		
	5.2	Energy Harvesting	72		
	5.3	Scheduling	75		
	5.4	Summary	77		
6	Latest Contributions				
	6.1	Effect of Errors	78		
	6.2	Beyond Single-hop Communication	80		
	6.3	Other Topics	81		
	6.4	Summary	84		
7	Future Directions and Open Questions				
	7.1	Connection with Information Theory	86		
	7.2	Connection with Signal Processing	87		
	7.3	Applications	89		
	7.4	Summary	90		
Acknowledgements					
Re	References				

# Age of Information: A New Concept, Metric, and Tool

Antzela Kosta<sup>1</sup>, Nikolaos Pappas<sup>2</sup> and Vangelis Angelakis<sup>3</sup>

#### ABSTRACT

Age of information (AoI) was introduced in the early 2010s as a notion to characterize the freshness of the knowledge a system has about a process observed remotely. AoI was shown to be a fundamentally novel metric of timeliness, significantly different, to existing ones such as delay and latency. The importance of such a tool is paramount, especially in contexts other than transport of information, since communication takes place also to control, or to compute, or to infer, and not just to reproduce messages of a source. This volume comes to present and discuss the first body of works on AoI and discuss future directions that could yield more challenging and interesting research.

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1

### Introduction

The concept of Age of Information (AoI) was introduced in 2011 in [31] to quantify the freshness of the knowledge we have about the status of a remote system. More specifically, AoI is the time elapsed since the generation of the last successfully received message containing update information about its source system. Utilizing a simple communication system model, in a series of papers ([32], [33], [30], and [58]), the first group of characterizations of the Age of Information metric had appeared by 2012. Since then, AoI has attracted a vivid interest, with over 50 publications, in the last six years <sup>1</sup>.

The attention AoI has been receiving is due to two factors. The first is the sheer novelty brought by AoI in characterizing the freshness of information versus for example that of the metrics of delay or latency. Second, the need and importance of characterizing the freshness of such information is paramount in a wide range of information, communication, and control systems. By now, age has been studied with considerable diversity of systems, being as a concept, a performance metric, and a tool.

 $<sup>^{1}</sup>$ In this volume we take into consideration works that have been published no later than June 2017.

3

The purpose of this volume is to present a critical summary of this first body of works performed on AoI and discuss future research directions. Already at this early point we need to put down our first disclaimer: we have chosen to treat the early works with significantly more detail, going deeper in the derivations and presenting more results and insights from them than we do with more recent works. The reason for this is to achieve a tutorial nature in the volume, which can provide a solid ground of the AoI as a concept. Moreover, the first works, which we chose to present in more detail than the rest, aim to provide fundamentally new knowledge in the premise of maintaining information fresh in a system. This basic goal opens up a wide range of communication contexts that span from estimation and prediction, to applications such as vehicular networks and information caching, to name a few.

With this in mind, we begin this volume presenting the AoI concept as it was originally introduced. For this, we discuss the original models of Kaul, Gruteser and Yates of [33], considering a system where a source is transmitting packets containing status updates to a destination. The analysis presented is based on a simple queueing model. Already in that work the minimization of AoI was shown to be non-trivial for the source sampling methods studied. However, it had already become clear that timely updating a destination about a remote system is neither the same as maximizing the utilization of the communication system, nor of ensuring that generated status updates are received with minimum delay. This is because utilization can be maximized by making the source send updates as fast as possible which would lead to the destination receiving delayed statuses because messages are backlogged in the communication system studied. In this case, delay suffered by the stream of status updates can be reduced by decreasing the rate of updates. Alternatively, decreasing the update rate can also lead to the destination having unnecessarily outdated status information because of lack of updates.

AoI has spawned relevant performance metrics that are more tractable such as the Peak Age of Information or the Cost of Update Delay, opening even more research opportunities. Under the timely update context, the relevant timeliness **performance metrics** should be kept at values

4 Introduction

that ensure high freshness of information. Already the first AoI lower bound had appeared in [33] and we discuss it in Section 2. We then continue the discussion on the early works of AoI as a performance metric in Section 3, where we present the case of AoI for multiple sources, its use in scheduling, and demonstrate packet management techniques that have been employed. Section 4 treats AoI as a metric for rate control, addresses the case of packets with deadlines, and presents an optimal policy for optimizing age, throughput, and delay.

Keeping the AoI metrics low is of high interest when AoI is being treated as a **tool** to facilitate the timely update of information that will eventually improve performance metrics in different contexts. Consider for example remote estimation; if the process under observation consists of highly correlated data, then the frequency of generation and transmission of updates can be significantly reduced without affecting the timeliness of the information at a remote receiver. In Section 5, we discuss three domains in which AoI has been treated as a tool: Channel State Information (CSI) estimation, energy harvesting, and scheduling.

Recent works that have appeared in the time of writing of this volume have been categorized and treated in Section 6. Finally, in Section 7, we provide a brief discussion of indicative future topics on which the AoI can contribute. The topics we cover there are not a complete list, as there is an immense wealth of possible problems associated with the notion of timeliness as captured by age, in the form of either a tool, a performance metric, or even a concept.

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