AMUSE-FIELD. II. NUCLEATION OF EARLY-TYPE GALAXIES IN THE FIELD VERSUS CLUSTER ENVIRONMENT

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Received 2014 February 24; accepted 2014 June 20; published 2014 August 6

ABSTRACT

The optical light profiles of nearby early-type galaxies are known to exhibit a smooth transition from nuclear light deficits to nuclear light excesses with decreasing galaxy mass, with as much as 80% of the galaxies with stellar masses below $10^{10} M_{\odot}$ hosting a massive nuclear star cluster (NSC). At the same time, while all massive galaxies are thought to harbor nuclear supermassive black holes (SMBHs), observational evidence for SMBHs is slim at the low end of the mass function. Here, we explore the environmental dependence of the nucleation fraction by comparing two homogeneous samples of nearby field versus cluster early-type galaxies with uniform Hubble Space Telescope (HST) coverage. Existing Chandra X-ray Telescope data for both samples yield complementary information on low-level accretion onto nuclear SMBHs. Specifically, we report on dual-band (F475W and F850LP) Advanced Camera for Surveys (ACS) imaging data for 28 out of the 103 field early-type galaxies that compose the AMUSE-Field Chandra survey, and compare our results against the companion HST and Chandra surveys for a sample of 100 Virgo Cluster early-types (ACS Virgo Cluster and AMUSE-Virgo surveys, respectively). We model the two-dimensional light profiles of the field targets to identify and characterize NSCs, and find a field nucleation fraction of $26\%_{-11\%}^{+17\%}$ (at the 1σ level), consistent with the measured Virgo nucleation fraction across a comparable mass distribution $(30\%^{+17\%}_{-12\%})$. Coupled with the *Chandra* result that SMBH activity is higher for the field, our findings indicate that, since the last epoch of star formation, the funneling of gas to the nuclear regions has been inhibited more effectively for Virgo galaxies, arguably via ram pressure stripping.

Key words: galaxies: elliptical and lenticular, cD – galaxies: nuclei – galaxies: star clusters: general

Online-only material: color figures

1. INTRODUCTION

The assembly and merging history of supermassive black holes (SMBHs) at the centers of massive galaxies appears to proceed in close connection with-and possibly even regulatethe growth of their host galactic bulges. Perhaps the most well-known incarnation of this is the " $M_{\rm BH}-\sigma$ " relation, or the correlation between the mass $M_{\rm BH}$ of an SMBH and the velocity dispersion σ of the bulge (Ferrarese & Merritt 2000; Gebhardt et al. 2000; Tremaine et al. 2002; Gültekin et al. 2009; McConnell & Ma 2013; see also Woo et al. 2010, 2013 for $M-\sigma$ relation for active galactic nuclei (AGNs)). Tight scaling relations have also been claimed between SMBH mass and bulge mass/luminosity (Marconi & Hunt 2003, Häring & Rix 2004). While the number of reliable dynamical measurements for black hole mass has grown by a factor of about five over the last decade or so, it remains unclear whether these power-law scaling relations break down at the highest and lowest masses (Lauer et al. 2007; Greene et al. 2010; Kormendy & Ho 2013), and whether classical versus pseudo-bulges lead to different scaling relations (see, e.g., Jiang et al. 2011; Kormendy et al. 2011). Related to the above issues, the black hole mass function itself is largely unconstrained at low masses (Greene & Ho 2007; Kelly et al. 2010), and its determination may in turn be biased by the assumption of a single power-law relation with log-normal scatter (Kelly & Merloni 2012).

Based on detailed morphological analysis of a large sample of nearby early-type galaxies spanning over four decades in stellar mass (M_{\star}) , Ferrarese et al. (2006a) proposed that, for galaxies with M_{\star} less than a few times $10^{10} M_{\odot}$, compact stellar nuclei—with half-light radii between 2 and 5 pc and about 20 times brighter than typical globular clusters (Böker et al. 2004)—may take over from SMBHs as the dominant form of mass aggregation in galactic nuclei (a similar result has been reported for a comparably large sample of spiral galaxies by Rossa et al. 2006).

Most relevant to this paper, detailed work on the occurrence rate and properties of these "nuclear star clusters" (NSCs; Böker et al. 2004; Walcher et al. 2005; Carollo et al. 1998; Matthews et al. 1999; Balcells et al. 2003) was carried out within the Advanced Camera for Surveys Virgo Cluster Survey (ACS VCS; Côté et al. 2004), consisting of dual-band Hubble Space Telescope (HST) ACS observations of 100 early-type galaxies in the Virgo Cluster. Later augmented by the Fornax Cluster Survey (FCS; Jordán et al. 2007), the ACS VCS showed that between 66% and 82% of early-type galaxies with absolute B-magnitude $M_{\rm B} < -15$ host NSCs, a much larger % than had been thought based on ground observations (Côté et al. 2006; Turner et al. 2012). Côté et al. (2007) confirmed that NSCs preferentially reside in galaxies with $-19.5 < M_B < -15$ mag, and found that there is a smooth transition from nuclear light deficit to nuclear light excess with decreasing galaxy luminosity. Also using the ACS VCS data, Ferrarese et al. (2006a) found that the masses of NSCs correlate with the virial masses of their host spheroidal galaxies, and that this relation extends from the scaling relation between SMBH masses and the bulge masses of their host galaxies, possibly indicating a common growth mechanism for NSCs and SMBHs, and perhaps a shared formation mechanism. A common scaling relation for NSCs and SMBHs was also found independently by Wehner & Harris (2006). These results would be consistent with a scenario whereby SMBHs are the dominant—perhaps sole—mode of nuclear mass aggregation at the center of bright massive galaxies, becoming progressively less common down the mass function and disappearing entirely at the faint end, to be replaced by NSCs (the existence of a common scaling relation for the SMBHs and the NSCs has been by challenged by Graham 2012 and Leigh et al. 2012).

Over the last few years, an increasing number of galaxies hosting both NSCs and SMBHs have been identified (Graham & Spitler 2009; Neumayer & Walcher 2012; Gallo et al. 2010). In particular, Seth et al. (2008a) took a somewhat different approach from previous studies by searching for AGN in 176 galaxies that were previously known to contain NSCs. Based on their analysis, at least 10% of their sample—spanning a wide range in masses and Hubble types—hosts both NSCs and SMBHs, strongly suggesting that galaxies harboring NSCs "have AGN fractions consistent with the population of galaxies as a whole." In order to better understand the connection between these objects, as well as their respective formation mechanisms, it is desirable to undertake systematic studies that characterize both NSCs and SMBH activity over a sample that is unbiased with respect to nuclear properties.

With the goal of delivering the first unbiased census of lowlevel SMBH activity in the local universe, the AMUSE-Virgo (AGN Multi-wavelength Survey of Early-Type Galaxies; Gallo et al. 2008; Gallo et al. 2010; Miller et al. 2012b; Leipski et al. 2012) survey acquired Chandra X-ray Telescope Advanced CCD Imaging Spectrometer (ACIS) observations for all 100 early-type galaxies targeted by the ACS VCS. As the survey was tailored to probe down to Eddington scaled X-ray luminosities as low as $\log(L_X/L_{Edd}) \simeq -9$, it provides a relatively inexpensive (i.e., compared to dynamical studies) way to identify SMBHs in formally "inactive" nearby galactic nuclei. While, in the absence of an NSC, the issue of potential contamination to the nuclear X-ray signal from bright low mass X-ray binaries⁵ (LMXBs) can be addressed quantitatively based on the known shape and normalization of the X-ray luminosity function (XLF) of LMXBs (Gilfanov 2004), the presence of an NSC demands a more conservative treatment (see Gallo et al. 2010 for a detailed discussion). For the VCS sample, the combined Chandra and HST data indicate that between 24% and 34% of the targeted galaxies host a bona fide X-ray active SMBH. The fraction of hybrid nuclei, hosting both an SMBH and an NSC is estimated between 0.3% and 7% for M_{\star} below $10^{11} M_{\odot}$ and to be lower than 32% above it (at the 95% confidence level; Gallo et al. 2010).

Born as an extension of AMUSE-Virgo, the AMUSE-Field Chandra survey (Miller et al. 2012a, 2012b; Plotkin et al. 2014 on ultra-luminous X-ray sources (ULXs); Miller et al. 2014) was designed to deliver the first measurement of low-level SMBH activity in a field environment. AMUSE-Field targeted a volume-limited sample of 103 nearby field early-types spanning over three orders of magnitude in host stellar mass; analogous to the Virgo sample, the field galaxies were selected based solely on optical properties as classified by HyperLeda (Paturel et al. 2003), to create a sample that is unbiased with respect to nuclear properties. For the field sample, $45\% \pm 7\%$ of targets were found to host an X-ray active SMBH (Miller et al. 2012a). However, this measurement relies on the assumption that the fraction of field objects hosting an NSC is the same as that found for the AMUSE-Virgo targets. In order to properly compare the incidence of SMBH activity as well as stellar nucleation as a function of host stellar mass for the field sample as well as for Virgo, we acquired dual-band *HST*/ACS observations for a subsample of the AMUSE-Field galaxies.

Combined, the *Chandra*/ACIS and *HST*/ACS data of the Virgo and field samples provide *uniform* multi-wavelength information on the frequency of SMBHs and NSCs in the local universe, across the mass spectrum and across environment. In this work, we report on the analysis of the ACS observations of the field targets. We model the galaxies' surface brightness profiles to determine what fraction host NSCs, and compare our results to those from the Virgo Cluster. This paper is organized as follows. Section 2 describes our sample, data reduction, and analysis. Section 3 presents our results on the fraction of nucleated (as in hosting an NSC), early-type field galaxies, and our comparison to the fraction found for the Virgo Cluster. Section 4 discusses the implications of these results in the context of NSC formation models.

2. DATA ANALYSIS

The full AMUSE-Field sample is comprised of 103 early-type galaxies. We refer the reader to Section 2 of Miller et al. (2012a) for a detailed description of the selection criteria. Our HST program aimed at acquiring dual-band images for the galaxies with detected nuclear X-ray emission from Chandra (52 out 103 objects). Out of those, 8 already had archival HST data in both the F475W and F850LP filters. The remaining 44 targets were approved for a Snapshot survey in Cycle 19 (PI: Gallo, ID 12951), and 17 of them were eventually observed, with 340.0 s and 340.0+60.0 s exposures for the F475W and F850LP filters, respectively (the completion rate was close to 40%, in line with the average value for HST Snapshot programs). For the purpose of estimating the nucleation fraction-regardless of the nuclear X-ray properties—we included three additional objects from the AMUSE-Field sample with no X-ray detection, but for which ACS data in the same filters was also available in the archive. To summarize, here we report on HST/ACS observations in the F475W and F850LP filters for 28 (17 new, plus 11 archival) out of the 103 AMUSE-Field galaxies; 25 out of those 28 belong to the subsample of 52 galaxies with X-ray detected nuclei.

Data was re-reduced using the AstroDrizzle pipeline to improve the point-spread function (PSF) sampling from 0.05 pixel⁻¹ to 0.03 pixel⁻¹ for all objects. Though all objects were originally classified as early-type in HyperLeda, three objects (ESO 540-014, NGC 0855, NGC 3265) revealed irregular or non-early-type morphology in the ACS images, and were thus excluded from further analysis. We refer to the Appendix for descriptions of individual objects. We corrected for extinction within our galaxy using the extinction maps by Schlegel et al. (1998). Additionally, seven objects (NGC 1172, NGC 1370, NGC 3073, NGC 3377, NGC 4036, NGC 4125, and NGC 4278) were identified as suffering from dust contamination through visual inspection. We corrected for dust following the procedure defined in Ferrarese et al. (2006b), which relies on interpolation across dust affected areas. Masses for both galaxies and NSCs were computed using the mass-to-light relations for Sloan g and

⁵ The sample is comprised of early-type galaxies only, ensuring negligible contamination from high mass X-ray binaries.

Galaxy Properties											
Object Name	R.A. (deg)	Decl. (deg)	Distance (Mpc)	Mg (mag)	M_* (M_{\odot})	$(g-z)_{AB}$ (mag)	Nucleated?				
NGC 4125	182.025000	65.174167	23.7	-21.17	11.2	1.37	n				
NGC 3585	168.321250	-26.754722	19.9	-20.94	11.1	1.32	n				
NGC 4036	180.361667	61.895833	24.2	-20.7	11.0	1.41	n				
NGC 4291	185.075833	75.370833	32.2	-20.67	10.9	1.23	n				
NGC 1340	52.082083	-31.068056	20.6	-20.45	10.9	1.32	у				
NGC 4278	185.028333	29.280833	18.5	-20.40	10.8	1.39	n				
NGC 5831	226.029167	1.220000	26.9	-20.25	10.6	1.23	n				
NGC 4697	192.149583	-5.800833	12.2	-20.11	10.6	1.37	n				
NGC 3115	151.308333	-7.718611	9.7	-20.07	10.7	1.47	n				
NGC 5582	215.179583	39.693611	28.2	-20.02	10.6	1.14	n				
NGC 3379	161.956667	12.581667	11.1	-19.83	10.7	1.46	n				
NGC 1439	56.208333	-21.920556	26.4	-19.83	10.6	1.35	n				
NGC 5845	226.503333	1.633889	32.7	-19.82	10.7	1.42	n				
NGC 1426	55.704583	-22.108333	23.3	-19.66	10.6	1.37	у				
NGC 4648	190.435000	74.420833	25.4 ^a	-19.63	10.4	1.27	n				
NGC 3384	162.070417	12.629167	9.2	-19.24	10.4	1.37	у				
NGC 1172	45.400000	-14.836667	22.0	-19.09	10.3	1.30	у				
NGC 3377	161.926250	13.985833	10.2	-18.94	10.3	1.31	n				
UGC 07767	188.885000	73.674722	27.5	-18.57	10.0	1.21	n				
NGC 1331	51.617917	-21.355278	22.9	-18.14	9.8	1.06	у				
NGC 4121	181.985833	65.113889	24.8 ^a	-18.08	9.8	1.11	n				
NGC 2970	145.879583	31.976944	25.9 ^a	-17.86	9.6	0.96	у				
PGC 056821	240.697917	19.787222	27.0 ^a	-17.18	9.5	1.23	n				
NGC 3265	157.778333	28.796667	23.0 ^a								
NGC 3073	150.217083	55.618889	33.4								
NGC 1370	53.810833	-20.373611	13.2 ^a								
NGC 0855	33.514583	27.877222	12.96								
ESO 540-014	10.298750	-21.131667	22.4 ^a								

Table 1 Galaxy Properties

Notes.

R.A. and decl. are taken directly from the HyperLeda database. Distances are calculated from the redshift-independent mod0 distance modulus in HyperLeda.

^a(For objects lacking a mod0 distance modulus, the modz redshift-based distance modulus was used). M_g , M_{\star} , and color are determined as described in Section 2.

z bands⁶ defined in Table 7 of Appendix A of Bell et al. (2003). In calculating masses, magnitude corrections were made for the slight deviations between the *HST* F475W and F850LP and Sloan g and z filters (E. Bell 2013, private communication). Excluding the three aforementioned non-early-type galaxies and two galaxies (NGC 1370 and NGC 3073) for which heavy dust contamination around the nucleus prevented us from doing accurate photometry, our analysis is based on a sample of 23 early-type, field galaxies. Properties of individual galaxies are listed in Table 1.

For the purpose of a meaningful comparison to the Virgo Cluster nucleation fraction, we follow the definition of nucleation given by Côté et al. (2006), whereby a nucleated galaxy is one whose inner light profile lies systematically above that of a Sérsic profile⁷ fit to the galaxy excluding the inner 0'.5. Surface brightness profiles were parameterized with a Sérsic or double-Sérsic profile. We used the IRAF package ELLIPSE to

$$I_{\text{Sérsic}}(R) = I_{\text{e}} \exp\left\{-b_{\text{n}}\left[\left(\frac{R}{R_{\text{e}}}\right)^{1/n} - 1\right]\right\},\tag{1}$$

where R_e is the effective radius which encloses half of the model's light, I_e is the intensity at the effective radius, n is the Sérsic index, and b_n is a constant that is dependent on n.

extract azimuthally averaged surface brightness profiles from both the F475W and F850LP images. Two-dimensional galaxy models were created with GALFIT (Peng et al. 2002) and then projected onto the one-dimensional surface brightness profiles. First, we attempted to fit a Sérsic profile to the overall galaxy, excluding the inner 0".5 (as done in Côté et al. 2006; note that the Field sample was selected to have approximately the same distance as Virgo). When needed, an exponential disk component was added to the model to fit the outer regions of the galaxy (typically beyond 50"; i.e., Dullo & Graham 2013). While GALFIT does not allow the position angle and isophotal ellipticity to radially vary within a component, we did not constrain components to have the same position angle and ellipticity. Example GALFIT models and residuals are shown in Figure 1.

The presence of an NSC is signaled by a light excess with respect to the extrapolation of the best-fit galaxy model within the inner 0".5. When present, such excess was fit with an additional Sérsic component. A good fit was chosen to have residuals between the data and model consistently between -0.2 and +0.2 mag (similar to the residuals for surface brightness profile fits of Côté et al. 2006). Of the 23 objects for which we carried out a surface brightness profile analysis, we find 6 of them to be nucleated based on the definition given by Côté et al. (2006). Table 2 lists half-light radii, masses, and colors of these 6 NSCs.

 $^{^{6}}$ Sloan g and z bands are roughly equivalent to HST F475W and F850LP bands, respectively.

⁷ A Sérsic profile is defined as



Figure 1. *HST*/ACS F850LP images, GALFIT two-dimensional models, and GALFIT residuals for three AMUSE-Field targets. NGC 1331 (left column) was fit with a double-Sérsic profile; NGC 5831 (center column) was fit with a single Sérsic profile; NGC 3379 was fit with a Sérsic profile and an additional outer, low-Sérsic index component. Scaling is the same within each image/model/residual set.

Host Galaxy	$r_{\rm h}$ (pc)	$log(M_{\rm NSC})$ (M_{\odot})	(g-z) (mag)	$M_{\rm NSC}/M_{\rm gal}$	$N(>L_X)$	$1 - P_X$ (%)				
(1)	(2)	(3)	(4)	(5)	(6)	(7)				
NGC 3384	8.0	7.8	1.46	0.003	0.37	30.9				
NGC 1340	131.8	8.9	1.32	0.010	0.10	9.5				
NGC 1426	57.6	8.6	0.81	0.010	0.42	34.3				
NGC 1172	26.1	8.3	1.05	0.010	0.16	14.8				
NGC 2970	11.3	7.5	0.67	0.008	0.01	1.0				
NGC 1331	16.2	7.3	0.69	0.003	0.02	1.9				

 Table 2

 Nuclear Star Cluster Properties

Notes. Column 2: half light radius. Column 3: mass of NSC. Column 4: (g - z) color of NSC. Column 5: fraction of host galaxy stellar mass contained in the NSC. Column 6: for objects with nuclear X-ray detections, number of expected LMXBs with $\log(L_X) > 38.2$ within the *Chandra* PSF. Column 7: for galaxies with nuclear X-ray detections, probability that the *Chandra* PSF is contaminated by an LMXB of $\log(L_X) > 38.2$.



Figure 2. For each AMUSE-Field object with *HST* coverage, we present a one-dimensional light profile, best-fit GALFIT model profile (projected to a one-dimensional surface brightness profile), residuals, and color gradient. The semi-major axis returned by ELLIPSE is plotted on the x axis. The top panel of each plot gives the light profile and the best-fit model profile (a single- or double-Sérsic profile, either with or without an outer disk component). Open circles represent the *z*-band data, and open squares represent the *g*-band data. The best fit to the *z*-band data is given by the solid, red line, while the best fit to the *g*-band data is given by the blue, long dashed line. If multiple components are necessary to fit a light profile, the individual components are shown in short dashed lines. In the middle panel is the residual between the data and best-fit profile (dashed, blue line for *g* band; solid, red line for *z* band). The bottom panel is the (*g* - *z*) color gradient. (A color version of this figure is available in the online journal.)

Figures 2–5 show the one-dimensional surface brightness profiles, along with projected GALFIT models, best-fit residuals, and color gradients for the 23 objects for which we were able to perform reliable photometry.

3. RESULTS

3.1. Nucleation Fraction

Following Côté et al. (2007), we adopt the $\Delta_{0.02}$ parameter to quantify the degree of nucleation in our targets. $\Delta_{0.02}$ is defined as $\log L_g/L_s$, where L_g is the total luminosity of the best-fit galaxy model inside a break radius R_b , and L_s is the luminosity of just the outer Sérsic component in this region. Break radius R_b is equal to $0.02R_e$, which is where deviations from the outer Sérsic profile tend to occur. Negative $\Delta_{0.02}$ values indicate nuclear light deficits; these "cored" galaxies tend to be very luminous ellipticals (Graham & Guzmán 2003). A positive $\Delta_{0.02}$ value indicates a nuclear light excess, i.e., an NSC.

 $\Delta_{0.02}$ is plotted against absolute *B*-band magnitude (from Miller et al. 2012a) in Figure 6 for 22 of the 23 objects in our analysis; we exclude NGC 4697 from this calculation because its nuclear disk precluded us from calculating an accurate $\Delta_{0.02}$ value. For objects with nuclear light deficits, we calculate L_g based on the flux inside R_b , as measured by ELLIPSE, as opposed to the best-fit model, and use the outer Sérsic component to calculate L_s . The Spearman rank for this



Figure 3. Light profiles for AMUSE-Field objects with *HST* coverage. See Figure 2 for description. (A color version of this figure is available in the online journal.)

relation, calculated using the $\Delta_{0.02}$ values measured from the *g* band data, is 0.36 with a *p*-value of 0.11, indicating a positive correlation between magnitude and $\Delta_{0.02}$ at the 89% confidence level. Unlike Côté et al. (2007), who find a consistent trend from nuclear light deficit to excess with a clearly defined transition region between $-20 < M_{\rm B} < -19.5$ mag, we do not observe such a sharp transition region for our sample. We check that the same qualitative results hold if the analysis is performed in the *z* band.

Next, we compare our results for early-type field galaxies to those for the 100 early-type galaxies that compose the ACS VCS (Côté et al. 2004), in order to test whether the nucleation fraction has an environmental dependence. In order to properly account for the different mass distributions across the two samples, we use the procedure outlined in Section 2.2 of Miller et al. (2012b) to match the mass distributions, thus controlling for stellar mass (the mass distribution of the field sample is biased toward high stellar masses, since observations targeted objects with X-ray detections). In brief, we represent the field and Virgo M_{\star} distributions as a sum of Gaussian functions, then use a weighting function (equivalent to the ratio of the field to Virgo Gaussian representations) to draw subsamples from the Virgo sample that have the same mass distribution as the field sample. Figure 7 shows the two M_{\star} distributions and their Gaussian representations, along with the weighting function that is used to draw subsamples from the Virgo Cluster sample. We draw 500 such subsamples of 23 Virgo galaxies each, and find that they contain, on average, 7.16 nucleated objects, corresponding to $30\%^{+17\%}_{-12\%}$ of galaxies (error given at 1σ confidence level; Gehrels 1986). For the field, we found 6 out of 23 objects to be nucleated, corresponding to $26\%^{+11\%}_{-18\%}$ (errors given at the 1σ confidence level). Poisson statistics shows that for an expected value of 6 nucleated galaxies, there is a 15% chance of finding eight or more nucleated objects in a sample of 23. This argues for



Figure 4. Light profiles for AMUSE-Field objects with *HST* coverage. See Figure 2 for description. (A color version of this figure is available in the online journal.)

no statistically significant difference in the nucleation fractions of the field and Virgo samples.

It is important to note that our fitting procedure differs from that of the ACS VCS; GALFIT performs two-dimensional modeling, while the ACS VCS fits directly to the one-dimensional surface brightness profile. Additionally, the ACS VCS only fitted either a Sérsic or core-Sérsic profile to the galaxy surface brightness profile, while we sometimes include an extra component to the outer regions of the galaxy. In order to explore whether this difference in method would result in differing classifications, and if so, whether it would affect the soundness of our nucleation fraction comparison, we tested our fitting procedure on eight ACS VCS objects. For seven out of eight objects, the classifications were consistent between methods. One object, VCC 2095, which was classified by the ACS VCS as nucleated, was found not to be nucleated based on our GALFIT modeling. However, we also failed to identify an NSC when fitting to the one-dimensional surface brightness profile, as done in Côté et al. (2006). We believe this particular discrepancy to be due to the ACS VCS supplementing the light profile fitting-based classifications with by-eye classifications. To summarize, while there may be slight inconsistencies between classification methods, we expect the effect on the nucleation fraction to be small compared to the 1σ error bars, and not to affect the final conclusion that the nucleation fraction is consistent across environment.

3.2. Nucleation and X-Ray Emission

As discussed in Section 1, the X-ray luminosity threshold of the *Chandra* AMUSE surveys demands a careful assessment of the possible contamination of the nuclear X-ray signal from bright LMXBs, as opposed to low-luminosity SMBHs. While Miller et al. (2012a) *assumed* that the same level of nucleation (and thus contamination) measured in Virgo applied to the



Figure 5. Light profiles for AMUSE-Field objects with *HST* coverage. See Figure 2 for description. (A color version of this figure is available in the online journal.)

field galaxies, the ACS observations presented here enable us to verify this assumption by directly measuring the nucleation fraction. While, in the absence of an NSC, the XLF—and thus expected number—of LMXBs within the *Chandra* PSF simply scales within the enclosed stellar mass (Gallo et al. 2008, 2010 and references therein), the presence of an NSC likely implies an enhanced LMXB contribution to the nuclear X-ray signal, as discussed below. In order to quantify this effect, following Gallo et al. (2010) we adopt the functional shape of the XLF for LMXBs in globular clusters as estimated by Sivakoff et al. (2007).⁸ We expect this to be a conservative estimate of the probability of contamination for NSCs, as illustrated by the following discussion.

Pooley et al. (2003) finds that the number of LMXBs in a dense stellar environments scales as the stellar encounter rate, Γ , to the 0.74 power; in turn, $\Gamma \propto (\rho_0^2 r_c^3 / v_0)$, where ρ_0 is the central density, r_c is the system core radius, and v_0 is the central velocity dispersion. While the NSCs have higher central densities compared to globulars (NSCs are about an order of magnitude more massive than the typical Milky Way globular cluster (Walcher et al. 2005), the smaller core radii and the observed higher velocity dispersions for the NSCs suggest that globular clusters would have higher encounter rates, and thus a larger number of LMXBs (see Walcher et al. 2005 for velocity dispersions of Milky Way globular cluster; see Capuzzo-Dolcetta & Miocchi 2008 for a comparison between the NSC and globular cluster profiles).

Table 2 lists probabilities of contamination for objects that contain NSCs and have nuclear X-ray detections. For reference,

⁸ Number of LMXBs ($L_X > 3.2 \times 10^{38} \text{ erg s}^{-1}$) $\propto 10^{0.90(g-z)} r_{h,cor}^{-2.22} M^{1.24}$, where $r_{h,cor}$ is the half-light radius in parsecs, and M is the stellar mass in units of $10^6 M_{\odot}$.



Figure 6. $\Delta_{0.02} = \log(L_g/L_s)$ (as measured using *g*-band data) vs. absolute *B*-band magnitude. Positive values of $\Delta_{0.02}$ indicate there is a nuclear light excess, while negative values indicate a nuclear light deficit. Dashed vertical lines bound the transition region from light deficit to excess identified by Côté et al. (2007).

(A color version of this figure is available in the online journal.)

we point out that NGC 3384, which has the highest expected number of LMXBs of all the hybrid nuclei, is known to host an SMBH based on dynamical evidence (Gebhardt et al. 2003). The listed probabilities have been incorporated in an accompanying paper (B. P. Miller et al., submitted) where the Virgo and field samples combined are used to provide the first measurement of the SMBH occupation fraction in the local universe.

4. DISCUSSION AND CONCLUSIONS

Detailed morphological analysis of a sample of 100 earlytype galaxies in the Virgo Cluster has shown evidence that the majority of galaxies with stellar mass below $10^{10} M_{\odot}$ host NSCs (e.g., Ferrarese et al. 2006a). In this paper, we explored the possibility of an environmental dependence of the nucleation fraction using dual-band (F475W and F850LP) *HST*/ACS images of a sample of 28 field early-type galaxies out of the 103 galaxies that compose the AMUSE-Field X-ray survey (Miller et al. 2012a). After controlling for different stellar mass distributions, we found there to be no statistically significant difference between the nucleation fraction for field $(26\%^{+17\%}_{-11\%})$ and Virgo $(30\%^{+17\%}_{-12\%})$ early-type galaxies (from the ACS VCS survey). Here, we discuss our results in the context of NSC formation theories, and compare the measured nucleation fractions with the active fractions as estimated from X-ray diagnostics.

The mechanism behind the mass assembly and evolution of NSCs is still uncertain, but two prevalent formation theories have emerged. The *dissipationless* model suggests that NSCs form from the infall of globular clusters through dynamical friction (Tremaine et al. 1975), while the *dissipative* model posits that NSCs form by gas accumulating at the center of a galaxy (via mergers, i.e., Mihos & Hernquist 1994, or transport of gas in a disk; i.e., Milosavljević 2004) and forming stars in situ. Additionally, both processes may contribute to nucleus formation, and evidence for recurring episodes of star formation and/or distinct kinematics (Rossa et al. 2006; Seth et al. 2008b; Paudel et al. 2011; Seth et al. 2010)—particularly in late-type



Figure 7. Histograms of stellar mass distributions for the ACS VCS sample and Field sample with *HST* coverage. We represent these histograms as the sum of Gaussians. Also shown is the weighting function (arbitrary normalization) used to draw mass distribution matched subsamples from the Virgo Cluster; the weighting function is equivalent to the ratio of the Field to Virgo Gaussian representations.

(A color version of this figure is available in the online journal.)

galaxies—implies that even if globular cluster infall forms the bulk of the mass in the NSC, some gas needs to accrete to the center and form stars at later times.

Simulations show that in-falling globular clusters can form NSCs with global properties that generally match those of observed NSCs, and can reproduce scaling relations observed between NSCs and their host galaxies (Capuzzo-Dolcetta & Miocchi 2008; Antonini et al. 2012; Antonini 2013; Agarwal & Milosavljević 2011; Gnedin et al. 2013). This formation scenario is consistent with the observed radial distribution of the number of globular clusters near galaxy centers being flatter than that of the spheroidal stellar component with the same age and metallicity (Capuzzo-Dolcetta & Mastrobuono-Battisti 2009), indicative of inner depletion of globular clusters via dynamical processes. There is also evidence, particularly in latetype galaxies, for more recent gas accretion, from observations of multiple stellar populations (e.g., Walcher et al. 2006; Rossa et al. 2006) and kinematic features that cannot be reproduced solely by globular cluster infall (Hartmann et al. 2011). Overall, while globular cluster infall is able to reproduce the bulk properties of NSCs (masses and radii), subsequent injection of gas seems to be necessary to explain the full spectrum of observed properties.

Further information on the nature of nucleation comes from comparing different environments. For example, Turner et al. (2012) explored the nucleation fraction and NSC properties between the Virgo and Fornax early-type cluster members (through the ACS VCS and ACS FCS), and found them to be consistent with each other. They suggest that this agreement in nucleation fraction between the two different cluster environments-with Fornax being substantially smaller, colder and denser than its Northern counterpart-indicates that factors related to largescale environmental properties do not have large effects on the formation of NSCs in early-type galaxies. Although our sample size is smaller than those of both the VCS and FCS, our results confirm and strengthen this hypothesis, as we find no statistically significant difference in the nucleation fraction between the field and the clusters' samples. In addition, earlytype galaxies in both cluster environments as well as the field



Figure 9. Simple model for the evolution of the (g - z) color of a single stellar population with stellar mass $M_{\star} = 10^7 M_{\odot}$. Plotted for comparison are the median colors of the Virgo and Field NSCs in galaxies with $\log(M_{\star}/M_{\odot}) > 10.0$.

(A color version of this figure is available in the online journal.)

demonstrate a trend in which their nuclei move from having nuclear light deficits to nuclear light excesses as galaxy luminosity decreases.

In Figure 8, we explore whether environmental differences are reflected in the colors of field and Virgo NSCs. As discussed by Turner et al. (2012), there is a tendency for Virgo NSCs (displayed as red filled circles) to become redder with increasing host galaxy mass/luminosity (see the caption of Figure 8 for a quantitative analysis). According to single stellar population models (Kotulla et al. 2009), the extremely red colors of the more massive Virgo NSCs (with (g - z) as high as 1.7) can only be achieved in less than a Hubble time for super-solar metallicities (see Figure 9). Thus, Turner et al. (2012) interpret these results as being suggestive of two main channels of growth for NSCs, with low mass nuclei being primarily assembled via globular cluster infall, and higher mass nuclei growing further through subsequent accretion, mergers, and/or tidal torques involving metal-enriched gas. Our sample size is too small to ascertain whether field NSCs (displayed as blue triangles in Figure 8) show the same reddening with host stellar mass. If the higher mass Virgo nuclei do redden as a result of growth through the aforementioned mechanisms, we might expect that NSCs in the field (where events like mergers and tidal torques are less common) show a more constant (g - z) color as a function of stellar mass.

At the same time, highly sub-Eddington SMBH activity, as indicated by X-ray observations, changes with environment. The higher incidence of nuclear X-ray activity in the field sample $(50\% \pm 7\% \text{ versus } 32\% \pm 6\%)$, and the tendency of field galaxies toward marginally higher X-ray luminosity (by $0.38 \pm 0.14 \text{ dex})$ for a given host stellar mass, has been interpreted by Miller et al. (2012b) as due to the field galaxies, and their nuclear SMBHs, having access to greater cold gas reservoirs than the cluster galaxies, possibly as a result of enhanced ram pressure in a cluster environment.

Combined, the X-ray and optical diagnostics point toward the following scenario. In the field NSCs, small amounts of gas, possibly from residual star formation, has the potential to keep feeding a nuclear SMBH well after the major NSC mass assembly has occurred. In contrast, gas is more likely to be depleted from cluster members due to ram pressure stripping. It is important to note that the colors of the reddest Virgo NSCs still imply a stellar population that is older than ~ 1 Gyr (Figure 9). This is comparable to the crossing time for a massive galaxy cluster, making it likely that gas could have been stripped between the last episode of star formation and the present day, decreasing the amount of gas available to funnel to the nucleus.

Complementary questions about the interplay between SMBHs, NSCs and globular clusters can potentially be addressed by exploring their relative spatial distribution within clusters. E.g., Peng et al. (2008) presents evidence for an environmental dependence of the specific frequency⁹ of globular clusters. They find that Virgo dwarf galaxies with high specific frequencies tend to reside within 1 Mpc of M87, implying that globular cluster formation may be biased toward denser environments. Although Binggeli et al. (1987) found that nucleated galaxies in Virgo are more centrally concentrated than non-nucleated galaxies, Côté et al. (2006) did not replicate this trend, and attribute this finding to the surface brightness limit of Binggeli et al. (1987). However, Côté et al. (2006) used only galaxies with $B_{\rm T} \ge 13.7$ to test this result, corresponding to 40 nucleated galaxies and just four non-nucleated galaxies. Whether nucleated galaxies are more centrally concentrated than non-nucleated galaxies, whether this aligns with the concentration of galaxies with higher frequencies of globular clusters, and whether these correlate at all with nuclear SMBH accretion, warrants further investigation.

V.F.B. is supported by the National Science Foundation Graduate Research Fellowship Program grant DGE 1256260. This work was supported in part by the National Science Foundation under grant No. NSF PHY11-25915 and by NASA through grant HST-GO-12591 from the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS 5-26555. J.H.W. acknowledges support by the National Research Foundation of Korea (NRF) grant funded by the Korea government (MEST; No. 2012-006087). V.F.B. thanks Oleg Gnedin for useful suggestions.

APPENDIX

ADDITIONAL INFORMATION ON INDIVIDUAL OBJECTS

ESO 540-014

This object was misclassified as an early-type galaxy based on observations from the ground. Our observations reveal clumps of star formation and an irregular morphology with no clear nucleus. This object may be considered a dE/dIrr object, as defined in Ferrarese et al. (2006b). This object was excluded from analysis.

NGC 0855

This object is highly irregular, with many clumps of star formation extending in a bar across the galaxy. There is also a great deal of dust contamination. This object may be considered a dE/dIrr object, as defined in Ferrarese et al. (2006b). This object was excluded from analysis.

⁹ Defined as the number of globular clusters normalized to a galaxy luminosity of $M_V = -15$ (Harris & van den Bergh 1981).



Figure 8. (g - z) color of NSC vs. host galaxy absolute *B*-band magnitude. Red circles correspond to Virgo Cluster galaxies; blue diamonds to Field galaxies. Shown are the results of a linear regression analysis to test the presence of a relation of the form $(g - z) - 1.2 = a + b(M_b)$. A statistically significant correlation is found for the Virgo NSCs (with best-fit slope $\beta = -0.15 \pm 0.03$, at 1σ), while no significant correlation is found for the field. (A color version of this figure is available in the online journal.)

NGC 1172

NGC 1172 is elliptical, with dust lanes stretching across the galaxy and diffuse dust throughout. NGC 1172 is nucleated and is well fit by a double Sérsic profile with the addition of low ($n \sim 0.5$) Sérsic index component to fit the outer regions.

NGC 1331

NGC 1331 is an elliptical galaxy with an NSC. This object's light profile is well fit by a double-Sérsic profile. The nucleus is slightly bluer than the outer regions of the galaxy. In fitting with GALFIT, the Sérsic index of the nucleus had to be held fixed.

NGC 1340

NGC 1340 is nucleated and is well fit by a double Sérsic profile.

NGC 1370

NGC 1370 has an extremely dusty torus. Dust dominates a significant portion of the galaxy in g band, and is visible around the nucleus in z band. This object was excluded from analysis.

NGC 1426

NGC 1426 is nucleated and is best fit by a double-Sérsic profile.

NGC 1439

NGC 1439 has a dusty disk around its nucleus extending about 0'.5. The majority of the galaxy is well fit by a single Sérsic profile, but an extra component is necessary to fit the region past 20''.

NGC 2970

NGC 2970 has a faint spiral structure, perhaps from a merger. It is the bluest object in our sample with a (g - z) color of 0.8. NGC 2970 has an NSC and is well fit by a double-Sérsic profile.

NGC 3073

NGC 3073 suffers from dust contamination throughout the galaxy. It is particularly problematic in g band, but the dust is also visible in z band. This object was excluded from analysis.

NGC 3115

NGC 3115 is a highly edge-on S0 galaxy. The light profile was fit by a Sérsic profile plus an exponential disk.

NGC 3265

NGC 3265 appears to have very diffuse spiral arms and is highly contaminated by dust. This object was excluded from analysis.

NGC 3585

NGC 3585 appears to have a disk. The light profile was fit by a Sérsic profile plus an outer exponential disk component.

NGC 3377

NGC 3377 has an extremely depleted core, which is also very blue. Excluding the central region, we can fit the light profile of this galaxy with a Sérsic profile plus an outer disk component. NGC 3377 has a dust lane as well as diffuse dust contamination in the g band. There is a steep color gradient from the nucleus to the outer regions of the galaxy, with the g - z color getting redder with increasing radius.

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NGC 3379

NGC 3379 had a chip gap across the nucleus, but we were able to correct for it. There appears to be a disk in the central 2" but the chip gap covers part of it. This galaxy is well fit by a Sérsic profile plus an outer disk-like component.

NGC 3384

NGC 3384 required a multiple component fit for the outer galaxy, and was found to have an NSC. This galaxy has been referenced in the literature as having both an NSC and SMBH (Graham & Spitler 2009).

NGC 4036

NGC 4036 suffers from significant dust contamination, including some contamination surrounding the nucleus. The light profile was fit by a Sérsic component plus an outer exponential disk component.

NGC 4121

NGC 4121 is well fit by a Sérsic component for most of the galaxy plus an outer exponential disk component.

NGC 4125

NGC 4125 suffers from diffuse dust contamination across most of the galaxy and across the nucleus. The light profile is well fit by a single Sérsic component.

NGC 4278

NGC 4278 is well fit by a single Sérsic component.

NGC 4291

NGC 4291 has a depleted core, but the outer regions of the galaxy are well fit by a single Sérsic profile.

NGC 4648

The light profile of NGC 4648 is well fit by a Sérsic component for most of the galaxy plus an outer exponential disk component.

NGC 4697

NGC 4697 has a disk in the center which complicates light profile fitting. The disk extends from 0.4 to 4.0, corresponding to a dip in the light profile visible in this region. While NGC 4697's light profile can be fit with a double Sérsic profile, we are not convinced it is truly nucleated as opposed to appearing to have a central light excess with respect to the nuclear disk.

NGC 5582

The light profile of NGC 5582 is well fit by a single Sérsic profile.

NGC 5831

The light profile of NGC 5831 is well fit by a single Sérsic profile.

NGC 5845

NGC 5845 has a dusty disk in the center. Its light profile is well fit by a single Sérsic profile.

PGC 056821

The light profile of PGC 056821 is well fit by a single Sérsic profile. The images of PGC 056821 taken in the F850LP filter suffer from streaks of scattered light from a nearby star. Some of these streaks cut across the galaxy. These were corrected for by masking them, creating a model using the IRAF ELLIPSE and BMODEL tasks, and filling in those regions with the model.

UGC 07767

The light profile of UGC 07767 is well fit by a Sérsic component plus an outer exponential disk component.

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