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Additional Information

# An effective iterated greedy algorithm for the mixed no-idle permutation flowshop scheduling problem

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## Abstract

In the no-idle flowshop, machines cannot be idle after finishing one job and before starting the next one. Therefore, start times of jobs must be delayed to guarantee this constraint. In practice machines show this behavior as it might be technically unfeasible or uneconomical to stop a machine in between jobs. This has important ramifications in the modern industry including fiber glass processing, foundries, production of integrated circuits and the steel making industry, among others. However, to assume that all machines in the shop have this no-idle constraint is not realistic. To the best of our knowledge, this is the first paper to study the mixed no-idle extension where only some machines have the no-idle constraint. We present a mixed integer programming model for this new problem and the equations to calculate the makespan. We also propose a set of formulas to accelerate the calculation of insertions that is used both in heuristics as well as in the local search procedures. An effective iterated greedy (IG) algorithm is proposed. We use an NEH-based heuristic to construct a high quality initial solution. A local search using the proposed accelerations is employed to emphasize intensification and exploration in the IG. A new destruction and construction procedure is also shown. To evaluate the proposed algorithm, we present several adaptations of other well-known and recent metaheuristics for the problem and conduct a comprehensive set of

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computational and statistical experiments with a total of 1,750 instances. The results show that the proposed IG algorithm outperforms existing methods in the no-idle and in the mixed no-idle scenarios by a significant margin.

*Keywords:* flowshop, no-idle, heuristics, iterated greedy, local search

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## 1. Introduction

It has been almost 60 years since the seminal work about the two machine flowshop problem with makespan minimization criterion by Johnson (1954). Actually, in the scheduling literature this paper has been regarded as the first in the field (with the possible exception of the paper by Salvesson, 1952). In a flowshop problem we deal with a set  $N$  of  $n$  jobs, modeling client orders of different products to be manufactured, that have to be produced on a set  $M$  of  $m$  machines. The layout of the machines in the production shop is in series, i.e., we have first machine 1, then machine 2 and so on until machine  $m$ . All jobs must visit the machines in the same processing sequence. This sequence can be, without loss of generality,  $\{1, \dots, m\}$ . Therefore, a job is composed of  $m$  tasks or operations. Each task  $j$ ,  $j = \{1, \dots, n\}$  requires a known, deterministic and non-negative amount of time at each machine  $i$ ,  $i = \{1, \dots, m\}$ . This amount is referred to as processing time and denoted by  $p_{ij}$ . The objective is to find a processing sequence of all jobs at each machine so that a given criterion is optimized. There are as many possible sequences of jobs as permutations and this permutation can change from machine to machine which results in a search space of  $(n!)^m$  non-delay schedules for the Flowshop Scheduling Problem (FSP). Given this huge search space, most of the time, the problem is simplified by forbidding job passing, i.e., once a permutation of jobs is obtained for the first machine, it is maintained for all other machines, reducing the search space to  $n!$  solutions. This somewhat simpler problem is referred to as the Permutation Flowshop Scheduling Problem or PFSP. Following the work of Johnson (1954), the most studied optimization criterion is the minimization of the maximal job completion time or makespan ( $C_{\max}$ ) which corresponds to the time at which the last job in the sequence is finished at the last machine in the shop. The PFSP with makespan criterion is denoted as  $F/prmu/C_{\max}$ , following the accepted three field notation of Graham et al. (1979). Reviews about flowshop scheduling with this criterion are given by Framinan et al. (2004), Ruiz and Maroto (2005), Hejazi and Saghafian (2005) and Gupta and Stafford (2006). The literature about flowshop scheduling is huge. Not

32 only does each studied objective span a relatively large sub-field in itself  
33 with hundreds of references, like total tardiness minimization (see Vallada  
34 et al., 2008), flowtime optimization (Pan and Ruiz, 2013) or multiobjective  
35 (Minella et al., 2008), but also problem extensions and variations abound. It  
36 is safe to say that the literature of flowshop scheduling and variants comprises  
37 thousands of papers.

38 One of the seldom studied extensions of the flowshop is the no-idle version.  
39 In the no-idle permutation flowshop (NPFSP), machines are not allowed to  
40 sit idle after they have started processing the first job in the sequence. The  
41 no-idle condition appears in production environments where setup times or  
42 operating costs of machines are so high that shutting down machines after  
43 the initial setup is not cost-effective. Idle times might also not be allowed on  
44 machines due to technological constraints. More specifically, in the no-idle  
45 scenario, a machine must process all jobs in the sequence without interruptions.  
46 Therefore, if needed, the start of some jobs is delayed so as to ensure the no-  
47 idle constraint. Examples of no-idle situations appear in the steppers used in  
48 the production of integrated circuits through photolithography. These fixtures  
49 are so expensive that idling is avoided at all costs. The production of ceramic  
50 frits is an example where idling is technologically impossible due to the usage  
51 of special fusing ovens (called kilns) that burn at extreme temperatures. These  
52 ovens need a continuous thermal mass and therefore, idling is not allowed.  
53 Some other examples are found in fiber glass processing (Kalczyński and  
54 Kamburowski, 2005), and foundries (Saadani et al., 2003) amongst others.  
55 Ruiz et al. (2009) and Goncharov and Sevastyanov (2009) published recent  
56 reviews about the NPFSP or  $F/prmu, no - idle/C_{\max}$ .

57 The current situation is that the no-idle constraint has been so far considered  
58 all or nothing in the flowshop literature, i.e., either we have a regular idle  
59 flowshop where idle times are allowed on all machines or all machines have  
60 the no-idle constraint in the NPFSP. Real life production shops are mixed  
61 and most machines permit idle times whereas some do not accept idle times.  
62 Surprisingly, this realistic mixed no-idle flowshop problem or MNPFSP has not  
63 been studied in the literature before to the best of our knowledge. We denote  
64 this problem by  $F/prmu, mixed no - idle/C_{\max}$ . In the previous examples of  
65 integrated circuits and ceramic frit production, not all machines in the shop  
66 are no-idle. In the case of ceramic frits, only the central fusing kiln has the  
67 no-idle constraint. Other examples arise in the steelmaking industry. When  
68 producing steel, the charges of molten iron enter converter stages to reduce  
69 impurities (carbon, sulfur, silicon) through oxygen burning. These charges

70 undergo several other refining stages where impurities are further reduced,  
71 alloys are added and other operations are carried out. Only after this phase, is  
72 the molten steel is poured into a tundish for casting. The flow of molten steel  
73 goes to the crystallizer where it solidifies into slabs. Technological constraints  
74 force the continuous flow of charges with the same crystallizer and caster.  
75 This is where the no-idle constraint appears. All other stages do not have this  
76 no-idle constraint. There are many other examples in real-life factories. As a  
77 matter of fact, the authors are not aware of any real example in which all the  
78 machines in a flowshop have the no-idle constraint. Therefore, the MNPFSP  
79 is a more realistic problem which has not been studied before and is thus the  
80 motivation for this research. The PFSP is known to be  $\mathcal{NP}$ -Complete in the  
81 strong sense for more than two machines and makespan criterion (Garey et al.,  
82 1976). Similarly, the NPFSP was shown to belong to the same complexity  
83 class for three or more machines by Baptiste and Hguny (1997). As a result  
84 the new MNPFSP studied in this paper is also  $\mathcal{NP}$ -Hard in the strong sense.  
85 The rest of the paper is divided into five more sections. In the next section we  
86 review the literature mainly in the no-idle flowshop. Section 3 introduces the  
87 MNPFSP in more detail. We present a mixed integer programming model,  
88 the formulae to calculate the makespan and a speed-up method for the  
89 efficient calculation of the insertion neighborhood. Section 4 deals with the  
90 proposed Iterated Greedy method. In section 5 we present a comprehensive  
91 computational and statistical campaign to test the proposed methodology.  
92 Finally, section 6 concludes the paper and provides some avenues for further  
93 research.

## 94 2. Literature review

95 As stated, the MNPFSP has not been studied before. As a result, we  
96 focus our summarized review in the no-idle flowshop where all machines have  
97 the no-idle constraint. The NPFSP was first studied by Adiri and Pohoryles  
98 (1982) where polynomial time algorithms were proposed for special cases of  
99 the NPFSP mainly with two machines and total completion time criterion.  
100 Some amendments to this paper were carried out by Čepek et al. (2000). The  
101  $C_{\max}$  objective in the NPFSP was studied for the first time by Vachajitpan  
102 (1982). The author presented mathematical models and branch and bound  
103 methods for small instances. Baptiste and Hguny (1997) also presented a  
104 branch and bound method for the  $m$ -machine NPFSP and makespan criterion  
105 whereas the three machine problem was studied by Narain and Bagga (2003)

106 also with mathematical models and exact approaches. To date, no effective  
107 exact approach has been proposed for the NPFSP and rarely do any published  
108 results solve problems with more than a handful of jobs. As a result of this,  
109 the focus has been on heuristics for the problem. Some of the early heuristic  
110 methods were presented by Woollam (1986) that took some existing heuristics  
111 and recalculated their produced solutions eliminating idle times and doing  
112 some simple adjacent pairwise exchange moves on the results. The adaptation  
113 of the NEH heuristic of Nawaz et al. (1983) produced the best results. Saadani  
114 et al. (2001) presented a method based on heuristics for the traveling salesman  
115 problem denoted as SGM. This research was later published in paper form in  
116 Saadani et al. (2005). The three machine case was studied by Saadani et al.  
117 (2003) to be improved on later by Kamburowski (2004). Heuristics for special  
118 cases with dominating machines are studied by Narain and Bagga (2005a,b).  
119 The general  $m$ -machine NPFSP with makespan criterion has been approached  
120 with successful heuristics by several authors. For example, Kalczynski and  
121 Kamburowski (2005) presented a method based on Johnson's heuristic, de-  
122 noted as KK that was shown to outperform an adaptation of the NEH heuristic  
123 to the no-idle setting and the method of Saadani et al. (2005). A local search  
124 insertion method proposed by Baraz and Mosheiov (2008) is also shown to  
125 outperform that of Saadani et al. (2005) and is denoted by GH\_BM.  
126 Ruiz et al. (2009) presented a comprehensive comparison of heuristic methods,  
127 along with adaptations of the NEH method and the best heuristics proposed  
128 for the PFSP by Rad et al. (2009). The authors also presented an improved  
129 GH\_BM method. All methods were tested with and without the accelerations  
130 of the insertion neighborhood presented by Pan and Wang (2008a,b). The  
131 results of the comprehensive computational and statistical campaign with  
132 a set of 250 instances were clear: the adapted method FRB3 of Rad et al.  
133 (2009) and the improved GH\_BM2 version, both with accelerations produced  
134 the best results.

135 As regards metaheuristics, the first papers are by Pan and Wang (2008a,b). In  
136 the first, the authors present a discrete particle swarm optimization method,  
137 referred to as HDPSO. In the second a discrete differential evolution method  
138 is presented (DDE). Both papers are heavily based on insertion local search  
139 and an important result is given: an acceleration of the calculation of the  
140 exploration of this neighborhood. Similar to what Taillard (1990) did, the  
141 authors explain a set of calculations to reduce the complexity of the calcu-  
142 lation of a pass in the insertion neighborhood from  $\mathcal{O}(n^3m)$  to  $\mathcal{O}(n^2m)$  in  
143 the NPFSP. The authors hybridized their methods with the Iterated Greedy

144 algorithm of Ruiz and Stützle (2007) and demonstrated in computational  
145 tests, using the instances of Taillard (1990), a clear superiority over the algo-  
146 rithms presented in Saadani et al. (2005) and in Kalczynski and Kamбуrowski  
147 (2005). However, Ruiz et al. (2009) also tested HDPSO and DDE, along with a  
148 simple adaptation of the IG of Ruiz and Stützle (2007) and showed, in a more  
149 comprehensive benchmark of 250 instances and through detailed statistical  
150 tests, that the simple IG produces better results than the HDPSO and DDE  
151 hybrids.

152 More recently, Deng and Gu (2012) published a hybrid discrete differential  
153 evolution method (HDDE). This method has many similarities to those of  
154 Pan and Wang (2008b) and Ruiz and Stützle (2007). Basically, a different  
155 initialization based on an improvement of the NEH and a modified insertion  
156 local search is used. The 250 instances of Ruiz et al. (2009) are used. According  
157 to their reimplementations, the results show that the new presented HDDE  
158 is better than the IG adaptation of Ruiz et al. (2009) and also the HDPSO  
159 and DDE of Pan and Wang (2008a,b). Also recently, Fatih Tasgetiren et al.  
160 (2013a) have presented a variable iterated greedy and differential evolution  
161 hybrid. The algorithm presented is shown to outperform that of Deng and Gu  
162 (2012). A side paper is that of Fatih Tasgetiren et al. (2013b) where methods  
163 are presented but for the minimization of the total tardiness criterion.

164 As we can see, the mixed no-idle flowshop has not been studied yet, despite  
165 being a more realistic problem. Furthermore, most modern high-performing  
166 methods for the pure no-idle version are based on the accelerated insertion  
167 neighborhood and on variants of the Iterated Greedy of Ruiz and Stützle  
168 (2007). As a matter of fact, IG is being applied to many flowshop variants  
169 like setup times (Ruiz and Stützle, 2008), blocking (Ribas et al., 2011), no-  
170 wait (Pan et al., 2008b), non-permutation (Ying, 2008), tardiness criterion  
171 (Framinan and Leisten, 2008) and multiobjective (Minella et al., 2011) as well  
172 as in many other scheduling problems. Therefore, pursuing the IG avenue for  
173 the research of the new mixed no-idle flowshop, along with the accelerations  
174 of the insertion neighborhood is the most logical step.

### 175 **3. The mixed no-idle permutation flowshop problem**

176 The no-idle flowshop differs from the regular PFSP in that no idle time  
177 exists in between any two consecutive tasks at machines. Extending the  
178 previous notation of the PFSP we denote as  $o_{ij}$  the operation of the task  
179  $i$  of job  $j$ , i.e., the processing of job  $j$  by machine  $i$ . Similarly,  $C_{ij}$  is the

180 completion time of this task  $j$  at machine  $i$ . In general, we have a permutation  
181  $\pi$  of the  $n$  jobs and  $\pi_{(j)}$  denotes the job that occupies the  $j$ -th position in  
182 the permutation. In the regular PFSP the following condition holds for jobs  
183 occupying consecutive positions in the permutation:  $C_{i,\pi_{(j)}} \geq C_{i,\pi_{(j-1)}} + p_{i,\pi_{(j)}}$ .  
184 In the no-idle flowshop, this inequality is transformed into an equality:  $C_{i,\pi_{(j)}} =$   
185  $C_{i,\pi_{(j-1)}} + p_{i,\pi_{(j)}}$ . By joining these two properties we have the mixed no-idle  
186 flowshop or MNPFSFSP. We define the subset of no-idle machines as  $M' \subseteq M$   
187 with  $m'$  no-idle machines. All other machines not in  $M'$  are regular idle  
188 machines. Note that all other common flowshop assumptions apply (Baker,  
189 1974): (1) All jobs are independent and available for processing at time 0.  
190 (2) Machines are continuously available and never break down. (3) Machines  
191 can only process one task at a time. (4) A job can only be processed by one  
192 machine at a time. (5) Tasks are processed without interruptions. (6) Setup  
193 times are either independent from the sequence and included in the processing  
194 times or simply ignored. (7) There is an infinite in-process storage capacity  
195 between machines.  
196 With the previous definitions we propose the following mixed integer linear  
197 programming model.

### 198 3.1. A mixed linear integer program

199 The decision variables are the typical ones in a permutation problem  
200 (Naderi and Ruiz, 2010):

$$\begin{aligned} X_{j,k} &= \begin{cases} 1, & \text{if job } j \text{ occupies position } k \text{ of the sequence} \\ 0, & \text{otherwise} \end{cases} \\ C_{i,k} &= \text{Completion time of job in position } k \text{ on machine } i \\ C_{\max} &= \text{Maximum completion time or makespan} \end{aligned}$$

201 The objective function is the minimization of the makespan, which is  
202 equivalent to the time at which the job occupying the last position of the  
203 permutation finishes at the last machine:

$$\min C_{\max} = C_{m,n}$$

204 Subject to the following constraints:

$$\sum_{k=1}^n X_{j,k} = 1, \quad j = 1, \dots, n \tag{1}$$



$$\sum_{j=1}^n X_{j,k} = 1, \quad k = 1, \dots, n \quad (2)$$

$$C_{1,k} \geq \sum_{j=1}^n X_{j,1} \cdot p_{1,j} \quad k = 1, \dots, n \quad (3)$$

$$C_{i,k} \geq C_{i-1,k} + \sum_{j=1}^n X_{j,k} \cdot p_{i,j} \quad k = 1, \dots, n, i = 2, \dots, m \quad (4)$$

$$\begin{cases} C_{i,k} = C_{i,k-1} + \sum_{j=1}^n X_{j,k} \cdot p_{i,j}, & \text{if } i \in M' \\ C_{i,k} \geq C_{i,k-1} + \sum_{j=1}^n X_{j,k} \cdot p_{i,j}, & \text{otherwise} \end{cases} \quad k = 2, \dots, n, i = 1, \dots, m \quad (5)$$

$$C_{i,k} \geq 0 \quad k = 1, \dots, n, i = 1, \dots, m \quad (6)$$

$$X_{i,k} \in \{0, 1\} \quad k = 1, \dots, n, i = 1, \dots, m \quad (7)$$

205 Constraints (1) and (2) ensure that each job occupies exactly one position  
 206 in the permutation and that each position in the permutation is occupied  
 207 by exactly one job. Constraint set (3) controls the completion time of the  
 208 job placed in the first position of the sequence. Constraints (4) force the  
 209 completion times of tasks on the second and subsequent machines to be larger  
 210 than the completion times of the previous tasks on previous machines plus  
 211 the processing time. The core of the MNPFSP is given in constraint set (5).  
 212 Here we control the completion time of a job at an idle machine so that it is  
 213 exactly equal to its processing time plus the completion time of the job in the  
 214 preceding position in the permutation, i.e., no idle time is allowed. However,  
 215 for regular machines, it suffices to ensure that the completion time of a job is  
 216 just greater to or equal than that of the preceding job plus the processing  
 217 time. Finally, constraints (6) and (7) define the domains and nature of the  
 218 decision variables.

### 219 3.2. Makespan calculation

220 As shown in Ruiz et al. (2009) and in Pan and Wang (2008a,b), calculating  
 221 the makespan for the NPFSP is far from straightforward. Here we extend such  
 222 calculations for the mixed no-idle version. Obviously, being a generalization,  
 223 the proposed formulas reduce to those of the regular flowshop if  $M' = \emptyset$  and

224 to the no-idle flowshop if  $M' = M$ .

225 Let us suppose a permutation  $\pi = \{\pi_1, \pi_2, \dots, \pi_n\}$  where  $\pi_l \in N$  for  $l =$   
 226  $1, \dots, n$  represents the jobs in the permutation. Let  $S_{i,[l]}$  and  $C_{i,[l]}$  denote the  
 227 earliest starting time and completion time of task  $o_{i,[l]}$  or the task at machine  
 228  $i$  of the job occupying position  $l$  of the permutation, respectively. We use the  
 229 simplified notation  $[l]$  to represent the job in position  $l$  of the permutation,  
 230 i.e.,  $\pi_l$  or  $\pi_{(l)}$ .

231 We also denote by  $a_i$  the right shift or delay in the start time of the operation  
 232  $l'$  preceding  $l$  in the permutation, i.e, the delay in  $o_{i,[l']}$  where  $l' = 1, 2, \dots, l-1$   
 233 in order to meet the no-idle constraint. The makespan calculation procedure  
 234 consists of calculating the start and completion times of the job in the first  
 235 position  $\pi_1$ , then  $\pi_2$  and so on until job is tested in position  $n$  or  $\pi_n$ . The  
 236 maximum completion time of the permutation,  $C_{\max}(\pi)$  is obtained with the  
 237 following expressions:

$$\begin{cases} S_{1,[1]} = 0 \\ C_{1,[1]} = S_{1,[1]} + p_{1,[1]} \end{cases} \quad (8)$$

$$\begin{cases} S_{i,[1]} = C_{i-1,[1]} \\ C_{i,[1]} = S_{i,[1]} + p_{i,[1]} \end{cases} \quad i = 2, \dots, m \quad (9)$$

$$\begin{cases} S_{1,[l]} = C_{1,[l-1]} \\ C_{1,[l]} = S_{1,[l]} + p_{1,[l]} \end{cases} \quad l = 2, \dots, n \quad (10)$$

$$\begin{cases} S_{2,[l]} = \max \{C_{2,[l-1]}, C_{1,[l]}\} \\ C_{2,[l]} = S_{2,[l]} + p_{2,[l]} \\ a_2 = \begin{cases} \max \{C_{1,[l]} - C_{2,[l-1]}, 0\} & \text{if machine 2} \in M' \\ 0 & \text{otherwise} \end{cases} \end{cases} \quad l = 2, \dots, n \quad (11)$$

$$\begin{cases} S_{i,[l]} = \max \{C_{i,[l-1]} + a_{i-1}, C_{i-1,[l]}\} \\ C_{i,[l]} = S_{i,[l]} + p_{i,[l]} \\ a_i = a_{i-1} + \begin{cases} \max \{C_{i-1,[l]} - (C_{i,[l-1]} + a_{i-1}), 0\} & i \in M' \\ 0 & \text{otherwise} \end{cases} \end{cases} \quad i = 3, \dots, m, l = 2, \dots, n \quad (12)$$

$$C_{\max}(\pi) = C_{m,[n]} \quad (13)$$

238 From the previous formulas, (8) computes the start and completion time  
 239 for operation  $o_{1,[1]}$  whereas set (9) calculates the same for operations  $o_{i,[1]}$ ,

240  $i = 2, \dots, m$ . Set (10) computes the start and completion times for operations  
 241  $o_{1,[l]}$ ,  $l = 2, \dots, n$ . In set (11) we calculate the start times for operations  
 242  $o_{2,[l]}$  and  $a_2 = \max\{C_{1,[l]} - C_{2,[l-1]}, 0\}$  is the right shift or delay in the start  
 243 time of operation  $o_{2,[l]}$ ,  $l' = 1, \dots, l - 1$  to ensure that there is no idle time  
 244 between the operations on machine 2 if it is a no-idle machine. On the  
 245 contrary,  $a_2 = 0$  if machine 2 is a regular idle machine. In set (12) a similar  
 246 calculation is carried out for operations  $o_{i,[l]}$ ,  $i = 3, \dots, m, l = 2, \dots, n$ . Note  
 247 that  $\max\{C_{i-1,[l]} - (C_{i,[l-1]} + a_{i-1}), 0\}$  is the right shift or delay generated  
 248 by machine  $i$  (if it is a no-idle machine) and  $a_{i-1}$  is the right shift or delay  
 249 generated by all upstream no-idle machines. Therefore,  $a_i$  is the total delay.  
 250 Finally, equation (13) gives us the makespan value of permutation  $\pi$ .  
 251 Let us consider an example with four jobs and five machines, i.e.,  $N =$   
 252  $\{1, 2, 3, 4\}$  and  $M = \{1, 2, 3, 4, 5\}$ . Machines two and four are idle machines,  
 253 i.e.,  $M' = \{2, 4\}$ . The processing times of the four jobs in the five machines  
 254 are the following:

$$[p_{ij}]_{5 \times 4} = \begin{bmatrix} 3 & 6 & 6 & 5 \\ 4 & 5 & 6 & 5 \\ 4 & 5 & 4 & 6 \\ 3 & 4 & 5 & 4 \\ 5 & 5 & 4 & 5 \end{bmatrix}$$

255 Let us suppose that we have a FIFO schedule, i.e.,  $\pi = \{1, 2, 3, 4\}$ . Using  
 256 the previous formulas (8) and (9) we calculate the start and completion  
 257 times for all operations of job  $\pi_1 = \{1\}$  as follows:  $S_{1,[1]} = 0$ ,  $C_{1,[1]} = 3$ ,  
 258  $S_{2,[1]} = 3$ ,  $C_{2,[1]} = 7$ ,  $S_{3,[1]} = 7$ ,  $C_{3,[1]} = 11$ ,  $S_{4,[1]} = 11$ ,  $C_{4,[1]} = 14$ ,  $S_{5,[1]} = 14$ ,  
 259  $C_{5,[1]} = 19$ . The next job in the sequence is  $\pi_2 = \{2\}$  and the calculations  
 260 of the start and completion times, using expressions (10), (11) and (12) are  
 261 the following:  $S_{1,[2]} = 3$ ,  $C_{1,[2]} = 9$ ,  $S_{2,[2]} = \max\{C_{1,[2]}, C_{2,[1]}\} = 9$ ,  $C_{2,[2]} =$   
 262  $14$ ,  $a_2 = \max\{C_{1,[2]} - C_{2,[1]}, 0\} = 2$ ,  $S_{3,[2]} = \max\{C_{3,[1]} + a_2, C_{2,[2]}\} = 14$ ,  
 263  $C_{3,[2]} = 19$ ,  $a_3 = a_2 = 2$ ,  $S_{4,[2]} = \max\{C_{4,[1]} + a_3, C_{3,[2]}\} = 19$ ,  $C_{4,[2]} = 23$ ,  
 264  $a_4 = a_3 + \max\{C_{3,[2]} - (C_{4,[1]} - a_3), 0\} = 5$ ,  $S_{5,[2]} = \max\{C_{5,[1]} + a_4, C_{4,[2]}\} = 24$ ,  
 265  $C_{5,[2]} = 29$ . We can see these calculations in Figure 1.

266 Similarly, the start and completion times for jobs  $\pi_3 = \{3\}$  and  $\pi_4 = \{4\}$   
 267 are summarized as follows:  $S_{1,[3]} = 9$ ,  $C_{1,[3]} = 15$ ,  $S_{2,[3]} = 15$ ,  $C_{2,[3]} = 21$ ,  
 268  $a_2 = 1$ ,  $S_{3,[3]} = 21$ ,  $C_{3,[3]} = 25$ ,  $a_3 = a_2 = 1$ ,  $S_{4,[3]} = 25$ ,  $C_{4,[3]} = 30$ ,  $a_4 = 2$ ,  
 269  $S_{5,[3]} = 31$ ,  $C_{5,[3]} = 35$ .  $S_{1,[4]} = 15$ ,  $C_{1,[4]} = 20$ ,  $S_{2,[4]} = 21$ ,  $C_{2,[4]} = 25$ ,  $a_2 = 0$ ,  
 270  $S_{3,[4]} = 26$ ,  $C_{3,[4]} = 32$ ,  $a_3 = 0$ ,  $S_{4,[4]} = 32$ ,  $C_{4,[4]} = 36$ ,  $a_4 = 2$ ,  $S_{5,[4]} = 37$ ,

271  $C_{5,[4]} = 42$ . Finally, the makespan for the permutation  $\pi = \{1, 2, 3, 4\}$  is  
 272  $C_{\max}(\pi) = C_{5,[4]} = 42$ .

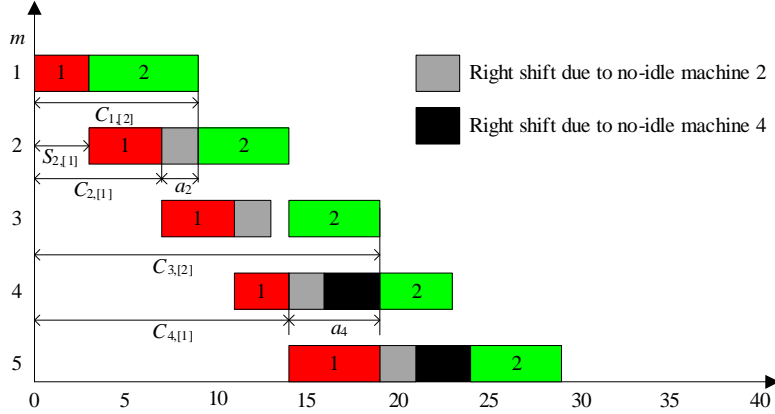


Figure 1: Makespan calculation for the first two jobs in the example.

### 273 3.3. A speed-up method for the insertion neighborhood

274 The insertion neighborhood is, by far, the most widely used neighborhood  
 275 in the flowshop scheduling literature. Inspired by the early work of Nawaz et al.  
 276 (1983), many authors have used this neighborhood with very good results. The  
 277 papers of Osman and Potts (1989), Taillard (1990) or Nowicki and Smutnicki  
 278 (1996) are some examples. Some of the state-of-the-art methods for the PFSP  
 279 and variants employ this neighborhood (Vallada et al., 2008; Pan and Ruiz,  
 280 2013; Ruiz et al., 2009; Pan and Wang, 2008a,b; Ruiz and Stützle, 2007; Deng  
 281 and Gu, 2012; Ruiz and Stützle, 2008; Ribas et al., 2011; Pan et al., 2008b;  
 282 Minella et al., 2011 and many others).

283 The insertion neighborhood of a given permutation  $\pi$  of  $n$  jobs is the result  
 284 of the consideration of all pairs of positions  $j, k \in \{1, \dots, n\}$  of  $\pi$ ,  $j \neq k$   
 285 where the job in position  $j$  is removed from  $\pi$  and inserted in position  $k$ . The  
 286 resulting sequence after such a movement is

$$\pi' = \{\pi(1), \dots, \pi(j-1), \pi(j+1), \dots, \pi(k), \pi(j), \pi(k+1), \dots, \pi(n)\}$$

287 if  $j < k$ , or

$$\pi' = \{\pi(1), \dots, \pi(k-1), \pi(j), \pi(k), \dots, \pi(j-1), \pi(j+1), \dots, \pi(n)\}$$

288 if  $j > k$ . The set of insertion moves  $I$  is defined as

$$I = \{(j, k) : j \neq k, 1 \leq j, k \leq n \wedge j \neq k - 1, 1 \leq j \leq n, 2 \leq k \leq n\}$$

289 and the insertion neighborhood of  $\pi$  is defined as  $V(I, \pi) = \{\pi_v : v \in I\}$ . The  
 290 cardinality of the insertion neighborhood is  $(n - 1)^2$ .

291 Since calculating the makespan for PFSP problems usually involves  $\mathcal{O}(nm)$   
 292 operations, the complexity of examining the insertion neighborhood (a single  
 293 pass) is  $\mathcal{O}(n^3m)$ . This can be computationally costly for moderate to large  
 294 values of  $n$ . However, Taillard (1990) proposed the famous so called “acceler-  
 295 ations” to reduce the complexity of the insertion neighborhood to  $\mathcal{O}(n^2m)$ .  
 296 As a matter of fact, the accelerations were proposed for the NEH heuristic  
 297 and as explained in Rad et al. (2009), the largest instances of Taillard (1993)  
 298 with 500 jobs and 20 machines ( $500 \times 20$ ) require up to 30 seconds of CPU  
 299 time without accelerations and as little as 77 milliseconds with accelerations  
 300 on a Pentium IV computer running at 3.2 GHz. As we can see, the impact of  
 301 the accelerations is huge, as the accelerated NEH requires almost 400 times  
 302 less CPU time. From the results of Taillard (1990), accelerations for the  
 303 calculation of the insertion neighborhood with makespan criterion have been  
 304 profusely proposed for many flowshop variants. As commented, the closest  
 305 references are the accelerations proposed by Pan and Wang (2008a,b) for the  
 306 NPFSP.

307 Given the calculation of the makespan in the mixed no-idle PFSP with  $\mathcal{O}(nm)$   
 308 steps of section 3.2, we now propose accelerations for the insertion neighbor-  
 309 hood so as to reduce its complexity to  $\mathcal{O}(n^2m)$ .

310 It is well known that flowshop problems have a reversibility property (Ribas  
 311 et al., 2010, among others). Under this property, the makespan of a per-  
 312 mutation  $\pi$  can be calculated traversing the permutation from the first to  
 313 the last job or in reverse order, i.e., from the last job in the sequence to  
 314 the first. Therefore, we can divide permutation  $\pi$  into two partial sequences,  
 315  $\pi^1 = \{\pi_{(1)}, \pi_{(2)}, \dots, \pi_{(k)}\}$  and  $\pi^2 = \{\pi_{(k+1)}, \pi_{(k+2)}, \dots, \pi_{(n)}\}$ . The forward cal-  
 316 culation pass involves  $\pi^1$  and the backward pass  $\pi^2$ . We denote by  $S'_{i,[l]}(C'_{i,[l]})$   
 317 the starting (completion) time of operation  $o_{i,[l]}$ ,  $l = k + 1, k + 2, \dots, n$  in  
 318 the reverse sequence. With this, the makespan  $C_{\max}(\pi)$  can be calculated as  
 319 follows:

$$L_1 = C_{1,[k]} + C'_{1,[k+1]} \tag{14}$$

$$\begin{cases} L_2 = C_{2,[k]} + C'_{2,[k+1]} \\ L = \max\{L_1, L_2\} \\ a_2 = \begin{cases} \max\{L - L_2, 0\} & \text{if machine 2} \in M' \\ 0 & \text{otherwise} \end{cases} \end{cases} \tag{15}$$

$$\begin{cases} L_i = C_{i,[k]} + a_{i-1} + C'_{i,[k+1]} \\ L = \max\{L, L_i\} \\ a_i = a_{i-1} + \begin{cases} \max\{L - L_i, 0\} & \text{if machine } i \in M' \\ 0 & \text{otherwise} \end{cases} \end{cases} \quad i = 3, \dots, m \quad (16)$$

$$C_{\max}(\pi) = L \quad (17)$$

320 Let us apply the acceleration formulas to the previous example with  
 321  $\pi^1 = \{1, 2\}$  and  $\pi^2 = \{3, 4\}$ . After calculating job 1, we calculate job 2 with  
 322 the forward pass and job 3 with the reverse (also after having calculated job  
 323 4):  $C_{1,[2]} = 9$ ,  $C_{2,[2]} = 14$ ,  $C_{3,[2]} = 19$ ,  $C_{4,[2]} = 23$ ,  $C_{5,[2]} = 29$  and  $C'_{1,[3]} = 32$ ,  
 324  $C'_{2,[3]} = 26$ ,  $C'_{3,[3]} = 19$ ,  $C'_{4,[3]} = 14$ ,  $C'_{5,[3]} = 9$ . Then the makespan is as follows:

$$L_1 = C_{1,[2]} + C'_{1,[3]} = 41;$$

$$L_2 = C_{2,[2]} + C'_{2,[3]} = 40, L = \max\{L_1, L_2\} = 41, a_2 = \max\{L - L_2, 0\} = 1;$$

$$L_3 = C_{3,[2]} + a_2 + C'_{3,[3]} = 39, L = \max\{L, L_3\} = 41, a_3 = a_2 = 1;$$

$$L_4 = C_{4,[2]} + a_3 + C'_{4,[3]} = 38, L = \max\{L, L_4\} = 41, a_4 = a_3 + \max\{L - L_4\} = 4;$$

$$L_5 = C_{5,[2]} + a_4 + C'_{5,[3]} = 42, L = \max\{L, L_5\} = 42, a_5 = a_4 = 4;$$

$$C_{\max}(\pi) = L = 42.$$

325 A graphical depiction of the process is given in Figure 2.

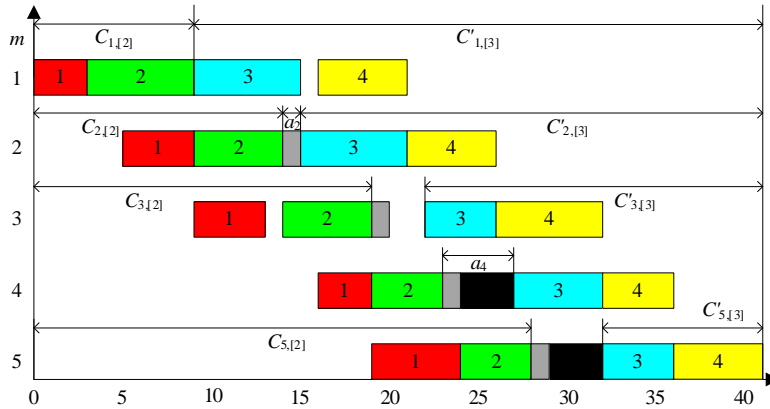


Figure 2: Calculations of sequences  $\pi^1 = \{1, 2\}$  and  $\pi^2 = \{3, 4\}$  for the example.

326 The speed-up method then consists of evaluating all permutations gener-

327 ated by the insertion of a single job in all possible positions of a sequence.  
 328 Let  $\pi = \{\pi_{(1)}, \pi_{(2)}, \dots, \pi_{(n-1)}\}$  be a partial sequence of  $n - 1$  jobs. We want  
 329 to insert job  $j_k$  into all possible  $n$  positions of  $\pi$ , generating  $n$  complete  
 330 permutations. Using the formulas of Section 3.2 this would require  $\mathcal{O}(n^2m)$   
 331 steps for one job or  $\mathcal{O}(n^3m)$  for all jobs. With the previous formulas and the  
 332 following procedure, this complexity is reduced to  $\mathcal{O}(nm)$  for a single job:

333 **Step 1.** Compute  $S_{i,[l]}$  and  $C_{i,[l]}$  for  $i = 1, 2, \dots, m$  and  $l = 1, 2, \dots, n - 1$   
 334 with the forward pass and  $S'_{i,[l]}$  and  $C'_{i,[l]}$  for  $i = m, m - 1, \dots, 1$  and  
 335  $l = n - 1, n, \dots, 1$  with the backward pass.

336 **Step 2** For  $l = 1, \dots, n$  do the following steps:

337 **Step 2.1** Insert job  $j_k$  into the  $l^{\text{th}}$  position of the partial sequence  $\pi$  and  
 338 generate a full permutation  $\omega = \{\pi_{(1)}, \pi_{(2)}, \dots, \pi_{(l-1)}, j_k, \pi_{(l)}, \dots, \pi_{(n-1)}\}$ .

339 **Step 2.2** Divide  $\omega$  into two partial sequences:  $\omega^1 = \{\pi_{(1)}, \pi_{(2)}, \dots, \pi_{(l-1)}, j_k\}$   
 340 and  $\omega^2 = \{\pi_{(l)}, \pi_{(l+1)}, \dots, \pi_{(n-1)}\}$ . Note that  $\omega^1 = \emptyset$  if  $l = 1$  and  $\omega^2 = \emptyset$  if  
 341  $l = n$ .

342 **Step 2.3** Calculate the starting and completion time for the last job  $j_k$  of  $\omega^1$   
 343 after obtaining  $S_{i,[l-1]}$  and  $C_{i,[l-1]}$  in Step 1 with formulas (8) to (13).

344 **Step 2.4** Calculate the makespan of  $\omega$  using equations (14) to (17).

345

346 Step 1 has a computational complexity of  $\mathcal{O}(nm)$ . Step 2 contains a loop  
 347 of  $n$  steps where each step has a complexity of  $\mathcal{O}(m)$ . Therefore, Step 2 has a  
 348  $\mathcal{O}(nm)$  complexity as a whole. This means that testing a job in all possible  
 349  $n$  positions of a sequence has a computational complexity of  $\mathcal{O}(nm)$ . Since  
 350 there are  $n$  jobs to test, the full examination of the insertion neighborhood  
 351 needs  $\mathcal{O}(n^2m)$  steps.

## 352 4. Iterated Greedy approach

353 The first application of the Iterated Greedy for flowshop problems was  
 354 given by Ruiz and Stützle (2007) and as commented in Section 2, IG methods  
 355 have been applied to all sorts of scheduling problems since then. The main  
 356 feature of the IG is its simplicity which is contrary to sophisticated algorithms  
 357 that embed problem specific knowledge and that usually have many control  
 358 parameters. In contrast, IG has very few parameters. Despite its simplicity,  
 359 IG has shown state-of-the-art results under different flowshop variants and  
 360 objectives.

361 An IG algorithm consists basically of a few steps. First, a starting solution is  
 362 built, usually by means of a high performing constructive heuristic. Then the

363 main loop is run until a termination criterion is reached. Inside this loop, two  
364 operators are iteratively applied. The first operator is a random destruction,  
365 where some elements of the solution are removed. The second operator is a  
366 greedy reconstruction method which reinserts the removed elements in order to  
367 form a new complete solution. The reconstruction also uses a high performing  
368 heuristic. After a new complete solution is obtained, an acceptance criterion  
369 is applied in order to decide if the new solution substitutes the incumbent.  
370 Optionally, a local search procedure can be applied, typically after the initial  
371 solution construction and before the acceptance criterion at each pass of the  
372 main loop. All these steps are explained in the following sections.

#### 373 *4.1. Initialization*

374 By far, the NEH algorithm of Nawaz et al. (1983) is the heuristic of choice  
375 for the initialization of metaheuristics in the flowshop literature. The NEH is  
376 a greedy constructive heuristic. Jobs are initially sorted according to total  
377 processing times and then the two possible permutations containing the first  
378 two sorted jobs are calculated. The best among the two is kept for the third  
379 step. In the third step, the third sorted job is inserted in the first, second  
380 and third possible positions of the partial sequence. The job is finally placed  
381 in the position resulting in the best makespan value. The process continues  
382 with the fourth job and completes when all jobs have been inserted. Most  
383 state-of-the-art methods for the PFSP and many variants employ the NEH.  
384 Ruiz and Maroto (2005) demonstrated the NEH to be the best heuristic,  
385 better even than more modern heuristics. Some authors, like Dong et al.  
386 (2008) or Kalczynski and Kamburowski (2007) have shown some methods that  
387 improve on the NEH performance. However, the outperformance is relatively  
388 small as these methods focus on the ties that occur in the insertion steps  
389 of the NEH. Clearly better heuristics are presented in Rad et al. (2009)  
390 where the authors proposed five methods, referred to as FRB1-FRB5 and  
391 demonstrated a significant advantage over the NEH. This outperformance  
392 comes at an additional computational cost as the methods are based on  
393 reinsertions of already inserted jobs. The authors also demonstrated that  
394 initializing competitive metaheuristics with some of their proposed methods  
395 instead of with the NEH produced better end results. Following these results,  
396 we also employ an improved heuristic instead of NEH. More precisely, we  
397 present an improvement of the FRB4<sub>k</sub> method of Rad et al. (2009). FRB4<sub>k</sub>  
398 produces good results while at the same time the additional CPU time needed  
399 is small. The idea behind the FRB4<sub>k</sub> is simple: after a job has been inserted in



400 position  $p$  of the sequence in a given step of the NEH,  $k$  jobs around position  
401  $p$  are reinserted in all positions looking for a better fit. The higher the  $k$ , the  
402 more jobs are reinserted and therefore the better results but also at a cost of  
403 more CPU time as the computational complexity is  $\mathcal{O}(kn^2m)$ . Our proposed  
404 improvement over the FRB4 $_k$  is based on the recent work of Pan and Wang  
405 (2012). In this paper, it was observed that the initial LPT ordering of the NEH  
406 is being broken during the insertions. The authors proposed a modification  
407 in which a partial LPT sequence of jobs is kept and the NEH process starts  
408 after a number of jobs  $\lambda$  have been assigned in the initial sequence. The side  
409 benefit of this modification is that less steps are needed in the main loop and  
410 the FRB4 $_k$  gains speed. Furthermore, to speed up the process, we fix  $k$  at the  
411 lowest possible value of one. A pseudo-algorithm for this improved method,  
412 referred to as FRB4 $_1^*$ , is given in Figure 3.

```

procedure FRB4 $_1^*(\lambda)$ 
  Calculate  $P_j = \sum_{i=1}^m p_{ij}, \forall j \in N$     % (LPT order)
  Sort jobs according to decreasing order of  $P_j$  obtaining  $\beta = \{\beta_{(1)}, \dots, \beta_{(n)}\}$ 
   $\pi := \{\beta_{(1)}, \beta_{(2)}, \dots, \beta_{(\lambda-1)}\}$     % Initial partial LPT sequence
  for  $l := \lambda$  to  $n$  do
    Take job  $\beta_{(l)}$  and test it in all positions of  $\pi$ 
    Insert job  $\beta_{(l)}$  in position  $p$  of  $\pi$  resulting in the best  $C_{\max}$ 
    for  $m := \max(1, p - 1)$  to  $\min(l, p + 1)$  do
      Extract job  $\pi_{(m)}$  from position  $m$  of  $\pi$  and test it in all positions of  $\pi$ 
      Insert job  $\pi_{(m)}$  at the position resulting in the best  $C_{\max}$ 
    endfor
  endfor
end

```

Figure 3: Improved constructive heuristic FRB4 $_1^*$ .

413 Note that the initial solution obtained after applying the FRB4 $_1^*$  method  
414 is further improved with the local search algorithm detailed in Section 4.2.  
415 The proposed FRB4 $_1^*$  method has a working parameter  $\lambda$  indicating when the  
416 NEH insertions start. This parameter will be calibrated in Section 4.4.

#### 417 4.2. Local search

418 Similar to the NEH, which is an insertion constructive heuristic, most  
419 competitive local search methods for the PFSP and variants are based on the  
420 insertion neighborhood. Good results with the insertion neighborhood are  
421 obtained in many papers, most notably Ruiz and Stützle (2007), Framinan

422 and Leisten (2008) and Vallada and Ruiz (2009), to cite just a few. In the  
 423 insertion neighborhood, a job is extracted from its position and inserted in  
 424 all other  $n - 1$  possible positions of the sequence (excluding the original one).  
 425 If a better  $C_{\max}$  value is found in a different position, the job is relocated  
 426 and the process is repeated for another job. The process terminates when  
 427 all jobs have been placed in all possible positions without improvements.  
 428 Note that the accelerations given in Section 3.3 fit perfectly into this scheme,  
 429 allowing us to reap the speed benefits. This local search was used for the IG  
 430 by Ruiz and Stützle (2007), Ruiz and Stützle (2008) and Vallada and Ruiz  
 431 (2009) for problems other than the no-idle flowshop and by Ruiz et al. (2009)  
 432 for the no-idle version. In this local search, jobs to be inserted are selected  
 433 randomly, without repetition, until local optimality is reached. However, quite  
 434 recently, Pan et al. (2008a) and Pan and Ruiz (2012) have used a similar but  
 435 better performing version, referred to as referenced local search (RLS). In this  
 436 version, jobs are not extracted randomly but in the order given by a referenced  
 437 permutation. Recently, Deng and Gu (2012) also applied RLS to the no-idle  
 438 flowshop. Let  $\pi^{\text{ref}} = \{\pi_{(1)}^{\text{ref}}, \pi_{(2)}^{\text{ref}}, \dots, \pi_{(n)}^{\text{ref}}\}$  be the referenced sequence, which, in  
 439 this paper, is the best found solution so far. The RLS is detailed in Figure 4.  
 440 Both the regular local search of Ruiz and Stützle (2007) and the presented  
 441 RLS will be tested in the proposed IG.

```

procedure RLS( $\pi, \pi^{\text{ref}}$ )
   $i := 1$ ;  $counter := 0$ 
  repeat
    Locate and extract job  $\pi_{(i)}^{\text{ref}}$  from  $\pi$ 
    Take job  $\pi_{(i)}^{\text{ref}}$  and test it in all positions of  $\pi$ 
     $\pi^* :=$  Insert job  $\pi_{(i)}^{\text{ref}}$  at the position resulting in the best  $C_{\max}$ 
    if  $C_{\max}(\pi^*) < C_{\max}(\pi)$  then
       $\pi := \pi^*$ ;  $counter := 1$ 
    elseif
       $counter := counter + 1$ 
    endif
     $i := \text{mod}(i + 1, n)$ 
  until  $counter = n$ 
  return  $\pi$ 
end
  
```

Figure 4: Referenced Local Search (RLS) in the insertion neighborhood.

442 *4.3. Destruction, reconstruction and acceptance criterion*

443 In the destruction phase of the Iterated Greedy, and according to Ruiz and  
444 Stützle (2007),  $d$  jobs are randomly extracted from the incumbent permuta-  
445 tion  $\pi$  and inserted into a list of removed jobs  $\pi_R$ . Then, in the reconstruction  
446 phase, all jobs in  $\pi_R$  are reinserted, one by one, back into  $\pi$  using the NEH  
447 insertion procedure. This is referred to as the  $DC$  operator (Destruction-  
448 reConstruction). We propose a minor but, as we will see, important mod-  
449 ification as regards the final performance of the proposed method. After  
450 reinserting one job, the jobs occupying the previous and posterior positions  
451 are also reinserted in all positions of  $\pi$ . This is, in essence, the application of  
452 the  $FRB4_1^*$  ideas presented previously. This improved  $DC$  operator is referred  
453 to as  $\epsilon DC$ . The local search operator is applied after the solution has been  
454 fully reconstructed.

455 Note that the choice of  $d$  in the destruction procedure is key. A small  $d$  value  
456 will result in difficulties for IG in escaping strong local optima whereas a  
457 large  $d$  value is no different from a randomized NEH procedure. Similar to  
458 what Ruiz and Stützle (2007) did, we will calibrate the  $d$  value using strong  
459 statistical techniques.

460 At each iteration, after the destruction, reconstruction and local search steps  
461 we have a new solution. It has to be decided if this solution replaces the current  
462 incumbent one. We adopt the same acceptance criterion as Ruiz and Stützle  
463 (2007) and Ruiz and Stützle (2008) which in turn is based on the constant  
464 temperature Simulated Annealing-like criterion of Osman and Potts (1989).

465 Basically, a constant temperature is calculated as  $Temp = T \cdot \frac{\sum_{i=1}^m \sum_{j=1}^n p_{ij}}{n \cdot m \cdot 10}$ ,  
466 where  $T$  is another value to calibrate. Ruiz and Stützle (2007) demonstrated  
467 this value to be very robust and basically any other value except 0 is accept-  
468 able. The final proposed IG method, including some alternative operators, is  
469 given in Figure 5.

470 *4.4. Calibration of the  $FRB4_1^*$  heuristic and proposed IG*

471 In this section we calibrate the  $\lambda$  parameter of the  $FRB4_1^*$  heuristic and  
472 also test the two local search schemes, construction and reconstruction opera-  
473 tors of the IG method, along with the temperature  $T$  and number of jobs to  
474 destruct in the destruction phase ( $d$ ). In order to calibrate these methods we  
475 need some test instances.

476 In this paper we propose a comprehensive benchmark. Since there is no  
477 known benchmark for the MNPFSPP, we base our instances on those for

```

procedure IG( $d, T$ )
 $\pi := \text{FRB4}_1^*$ 
 $\pi := \text{LS}(\pi)$  or  $\text{RLS}(\pi)$     % Choice of local search
 $\pi_b := \pi$ 
while (termination criterion not satisfied) do
   $\pi' := \pi$ 
  for  $i := 1$  to  $d$  do    % Destruction phase
     $\pi' :=$  remove one job at random from  $\pi'$  and insert it in  $\pi'_R$ 
  endfor
  for  $i := 1$  to  $d$  do    % Reconstruction phase
     $\pi' :=$  Insert job  $\pi'_{R(i)}$  in position  $p$  resulting in the best  $C_{\max}$ 
    % Improved eDC operator
     $\pi' :=$  Reinsert jobs  $\pi'_{(p\pm 1)}$  in positions resulting in the best  $C_{\max}$ 
  endfor
   $\pi'' := \text{LS}(\pi')$  or  $\text{RLS}(\pi')$     % Choice of local search
  if  $C_{\max}(\pi'') < C_{\max}(\pi)$  then    % Acceptance Criterion
     $\pi := \pi''$ 
    if  $C_{\max}(\pi) < C_{\max}(\pi_b)$  then    % New best solution
       $\pi_b := \pi$ 
    endif
  elseif  $(\text{random} \leq e^{-(C_{\max}(\pi'') - C_{\max}(\pi)) / \text{Temp}})$  then
     $\pi := \pi''$ 
  endif
endwhile
end

```

Figure 5: Proposed Iterated Greedy (IG) method.

478 the no-idle PFSP of Ruiz et al. (2009). The basic benchmark contains 250  
479 instances. All combinations of the following  $n$  and  $m$  values are used:  $n =$   
480  $\{50, 100, 150, 200, 250, 300, 350, 400, 450, 500\}$  and  $m = \{10, 20, 30, 40, 50\}$ . For  
481 each one of the  $10 \times 5 = 50$  combinations, five replicates are obtained which  
482 results in 250 instances. Furthermore, in order to test different mixed no-idle  
483 scenarios, we generate seven different groups as follows: Group 1: The first  
484 50% of the machines have the no-idle constraint. The remaining 50% are  
485 regular idle machines. Group 2: The second 50% of the machines have the  
486 no-idle constraint. Group 3: The machines alternate, in order, between regular  
487 and no-idle constraints. Group 4: A random 25% of the machines are no-idle.  
488 Group 5: 50% random no-idle machines. Group 6: 75% random no-idle ma-  
489 chines. Group 7: This group contains the 250 original no-idle instances of  
490 Ruiz et al. (2009), i.e., in this group all machines have the no-idle constraint.  
491 Since there are 250 instances in each group, the grand total of instances in  
492 the benchmark is 1,750. The processing times for all instances are generated

493 following a uniform distribution in the range  $U[1, 99]$  as it is common in the  
494 scheduling literature. Note that this is a comprehensive benchmark that will  
495 allow us to use detailed results in the computational comparison.  
496 Calibrating algorithms with the same instances that will later be used for  
497 computational results and comparisons constitutes poor practice. If an algo-  
498 rithm is calibrated on the same instances that will be later tested we risk  
499 having biased or over fitted results. In order to remedy this problem we also  
500 generate a calibration benchmark of 100 random instances. To generate each  
501 instance, a random  $n$ ,  $m$  and group are selected and the instance is generated.  
502 All instances, both the test and the calibration benchmarks are available for  
503 download at <http://soa.iti.es>.

504

505 A first quick experiment was carried out to calibrate the  $\lambda$  parameter of  
506 the FRB4<sub>1</sub><sup>\*</sup>. We use the 100 calibration instances and test  $\lambda$  from 0 to 100%.  
507 This percentage relates to the number of jobs  $n$  so a  $\lambda = 50\%$  means that 50%  
508 of the initial sequence is maintained as LPT before starting the NEH insertion  
509 procedure. We use a step equal to 5% which means that we test 21 different  
510 values for  $\lambda$ . We solve the 100 calibration instances with these 21 versions  
511 of the FRB4<sub>1</sub><sup>\*</sup>. The response variable to measure is the Relative Percentage  
512 Deviation from the best known solution denoted as  $RPD = \frac{Some_{sol} - Best_{sol}}{Best_{sol}} \cdot 100$ .  
513  $Some_{sol}$  is the solution obtained by one of the versions on a given instance  
514 and  $Best_{sol}$  is the lowest makespan known for that instance. All best known  
515 solutions for the test instances are also available at <http://soa.iti.es>.  
516 All tests are carried out in a cluster with 30 blades, each one containing two  
517 Intel XEON E5420 processors with a core clock of 2.5 GHz. and 4 cores each  
518 (8 in total per blade) and 16 GBytes of RAM memory (480 GBytes in total).  
519 To analyze the results we carry out a full factorial design of experiments with  
520 one factor ( $\lambda$ ) at 21 levels on 100 instances which gives 2,100 treatments.  
521 The results of the experiment are analyzed by means of the Analysis of  
522 Variance (ANOVA) technique. ANOVA is a parametric statistical technique  
523 and three main hypotheses must be met. In order of importance these are  
524 the independence of the residuals, homoscedasticity of the different levels  
525 and variants of the factors studied (homogeneity of variance) and normality  
526 of the residuals. No significant deviations were found in the fulfillment of the  
527 hypotheses. The detailed results of this short initial experiment are omitted  
528 due to space constraints but suffice to say that the statistically best result is  
529 obtained when  $\lambda = 50\%n$ .

530

531 A much larger Design of Experiments (see Montgomery (2012), among  
 532 many others) is carried out to calibrate the proposed IG. We test the following  
 533 factors: 1) type of destruction-reconstruction operator, tested at two variants:  
 534 regular *DC* and improved *eDC*. 2) type of local search, tested at two variants:  
 535 regular *LS* and referenced local search *RLS*. 3) Destruction size  $d$  tested at  
 536 six levels: 8-13. 4)  $T$  tested at five levels: 0.4-0.8. Apart from these controlled  
 537 factors, each IG configuration is run five different times on each instance  
 538 (we call this the replicate witness factor which should not be statistically  
 539 significant). Note that the IG needs a termination criterion, which we set at a  
 540 given elapsed CPU time equal to  $t = 5nm$  milliseconds. Setting the CPU time  
 541 depending on the instance size (number of jobs  $n$  and number of machines  $m$ )  
 542 is good practice in order to better observe the effect of the factors. With a  
 543 fixed CPU time, smaller instances end up with large CPU times and become  
 544 “easy” whereas large instances might not have enough CPU time and might be  
 545 wrongly portrayed as “hard”. To sum up, we have a multi-factor full factorial  
 546 experimental design with  $100 \cdot 5 \cdot 2 \cdot 2 \cdot 6 \cdot 5 = 60,000$  treatments. With  
 547 such a large and powerful experiment, we will be able to fully calibrate the  
 548 proposed IG with a high degree of accuracy. The same computer is used for  
 549 the experiments and the *RPD* response variable is analyzed in a multi-factor  
 550 ANOVA. We do not show here the ANOVA table with interactions of second  
 551 order due to space limitations. Instead, we reproduce the means plots with  
 552 confidence intervals of the most important and statistically significant factors.  
 553 The most significant factors are the type of local search and  $d$ , followed by the  
 554 type of destruction-reconstruction factors. The means plots of these factors,  
 555 together with 95% Tukey’s Honest Significant Difference (HSD) confidence  
 556 intervals are given in Figure 6. Recall that overlapping confidence intervals  
 557 means that the observed difference in the response variable (*RPD*) of the two  
 558 overlapped means is statistically insignificant.

559 As can be seen, the improved *eDC* destruction-reconstruction operator is  
 560 statistically better than the Ruiz and Stützle (2007) regular operator. The  
 561 same can be said about the referenced local search *RLS*. While in Figure 6  
 562 it might seem that the differences are small, combined, the usage of *eDC* in  
 563 conjunction with *RLS* results in significant improvements over the regular  
 564 *LS* and *DC* operators. As regards  $d$ , the differences are small for central  
 565 values and we settle for  $d = 10$ . Finally, the factor  $T$  is not statistically  
 566 significant, which coincides with the results of Ruiz and Stützle (2007). We  
 567 select the central value of  $T = 0.6$ . Detailed ANOVA tables and all results of  
 568 the experiments are available upon request from the authors.

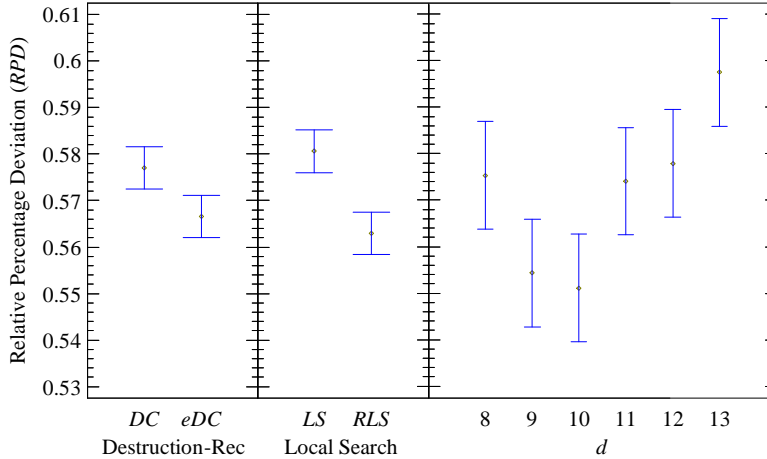


Figure 6: Means plot for the type of destruction-reconstruction operator, type of local search and  $d$  factors for the IG ANOVA calibration experiment. All means have Tukey’s Honest Significant Difference (HSD) 95% confidence intervals.

## 569 5. Computational comparisons and statistical analysis

570 After calibrating the proposed IG method we compare it with the state-of-  
571 the-art algorithms from the literature. Since there are no MNPFSP methods  
572 proposed so far, we take the best competing algorithms from the no-idle PFSP  
573 literature. We will use the 1,750 test instances detailed in Section 4.4 for  
574 the computational comparisons. Note that the 7th group in those instances  
575 are no-idle problems so the proposed IG will be tested against existing  
576 methods on no-idle instances as well. The following methods have been fully  
577 reimplemented: 1) The hybrid Genetic Algorithm of Ruiz et al. (2006) (hGA).  
578 2) The hybrid discrete PSO of Pan and Wang (2008a) (hDPSO). 3) The hybrid  
579 discrete differential evolution algorithm of Pan and Wang (2008b) (hDDE<sub>P</sub>).  
580 4,5) The IG method of Ruiz et al. (2009) tested with  $d = 4$  and  $d = 8$  (IG<sub>R<sub>4</sub></sub>  
581 and IG<sub>R<sub>8</sub></sub>, respectively). 6) The hybrid discrete differential evolution algorithm  
582 of Deng and Gu (2012) (hDDE<sub>D</sub>). 7) The recent variable IG hybridized with  
583 differential evolution of Fatih Tasgetiren et al. (2013a) (IG<sub>T</sub>) and finally the  
584 eighth method is the IG algorithm proposed in this paper (IG). Note that all  
585 methods have been reimplemented and use the proposed accelerations of the  
586 insertion neighborhood. Makespan calculation functions are also shared. All  
587 methods have been coded in Visual C++ 6.0 and have been run on the same  
588 computers. Therefore, the results are fully and completely comparable.  
589 All algorithms have a natural stopping criterion which we set at a predefined

590 elapsed CPU time following the expression  $t = n \times (m/2) \times \rho$  milliseconds  
591 where  $\rho$  has been tested at values 10, 20, 30, 60, 90. Our objective is to analyze  
592 the performance of all the methods from short to very long CPU times. Note  
593 that for  $\rho = 90$  the largest instances of 500 jobs and 50 machines are run for  
594 almost 19 minutes. Given the 8 algorithms tested, 1,750 instances, 5 different  
595 stopping times and 5 replicates we have a total of  $1,750 \times 5 \times 5 \times 8 = 350,000$   
596 results. This is an extremely rich dataset which will allow us to draw strong  
597 conclusions. Note that the total CPU time needed for all experiments was  
598 1.92 years (the real time was much shorter as all tests were divided among  
599 the 30 blade clusters). The average relative percentage deviation, grouped  
600 only by instance group (250 instances  $\times$  5 replicates  $\times$  5 different stopping  
601 times = 6,250 values averaged at each cell) are given in Table 1.

Instance group	hDDE <sub>D</sub>	hDDE <sub>P</sub>	hDPSO	hGA	IG	IG <sub>R<sub>4</sub></sub>	IG <sub>R<sub>8</sub></sub>	IG <sub>T</sub>
1	0.42	0.41	0.42	0.65	<b>0.33</b>	0.61	0.42	0.95
2	0.42	0.41	0.44	0.66	<b>0.35</b>	0.63	0.42	0.96
3	0.42	0.42	0.43	0.66	<b>0.31</b>	0.65	0.43	0.95
4	0.47	0.45	0.47	0.74	<b>0.37</b>	0.64	0.46	1.14
5	0.44	0.42	0.45	0.68	<b>0.31</b>	0.66	0.44	0.98
6	0.42	0.40	0.41	0.62	<b>0.26</b>	0.62	0.40	0.81
7	0.39	0.37	0.40	0.56	<b>0.23</b>	0.61	0.37	0.71
<b>Average</b>	0.42	0.41	0.43	0.65	<b>0.31</b>	0.63	0.42	0.93

Table 1: Average Relative Percentage Deviation for all the 8 tested algorithms and the 1,750 test instances. Results grouped by type of instance.

602 As can be seen, the proposed IG produces the best results in all instance  
603 groups. While for groups 1-6 this is somewhat expected, as these are the  
604 mixed no-idle groups and the other methods were not designed for this setting,  
605 the differences are also large for group 7, which is the full no-idle case. For  
606 group 7, the Average *RPD* of the proposed IG is 0.23 whereas the second best  
607 method is hDDE<sub>P</sub> (tied with IG<sub>R<sub>8</sub></sub>), which have an Average *RPD* of 0.37%.  
608 This means that the IG produces solutions that are, on average, almost 61%  
609 better for the no-idle flowshop. Clearly, IG presents itself as the new state-  
610 of-the-art for the no-idle flowshop problem. On average, the best algorithm  
611 is the IG with an overall *RPD* for the 1,750 instances of 0.31%. The second  
612 best overall method is hDDE<sub>P</sub> with an Average *RPD* of 0.41%, again, with  
613 a large outperformance of more than 33%. It is also of interest to examine



614 the results of Table 1 but broken down according to the allowed CPU time  $\rho$ .  
 615 This is given in Table 2.

$\rho$	hDDE <sub>D</sub>	hDDE <sub>P</sub>	hDPSO	hGA	IG	IG <sub>R<sub>4</sub></sub>	IG <sub>R<sub>8</sub></sub>	IG <sub>T</sub>
10	0.47	0.49	0.49	0.72	<b>0.36</b>	0.73	0.48	1.06
20	0.44	0.44	0.45	0.67	<b>0.32</b>	0.67	0.44	1.01
30	0.42	0.41	0.43	0.64	<b>0.31</b>	0.63	0.42	0.97
60	0.40	0.37	0.40	0.62	<b>0.28</b>	0.58	0.39	0.85
90	0.39	0.35	0.39	0.61	<b>0.27</b>	0.55	0.37	0.76
<b>Average</b>	0.42	0.41	0.43	0.65	<b>0.31</b>	0.63	0.42	0.93

Table 2: Average Relative Percentage Deviation for all the 8 tested algorithms and the 1,750 test instances. Results grouped by allowed CPU time  $\rho$ .

616 Once again, the superiority of the proposed IG method is clear. While we  
 617 were expecting that for larger values of  $\rho$  the differences between methods  
 618 would diminish, we have found this not to be the case. The IG method has a  
 619 lead of more than 30% in Average *RPD* regardless of  $\rho$  value.

620 While the differences between IG and competing methods depicted in Tables 1  
 621 and 2 are quite large, it is still mandatory to run some statistical tests on  
 622 the results in order to ascertain if the observed differences in the Average  
 623 *RPD* values are indeed statistically significant. We have conducted a multi-  
 624 factor ANOVA where  $n$ ,  $m$ , instance group,  $\rho$ , replica (witness factor) and  
 625 algorithm are all controlled factors. Single factor effects as well as two way  
 626 interactions are studied. As expected with such a large dataset, most factors  
 627 are statistically significant (after all, with an infinite sample size, all differences  
 628 in the means, even if they tend to zero, are statistically significant). We are  
 629 most interested in the interaction between the algorithm and  $\rho$ , shown in  
 630 Figure 7.

631 As can be seen, there are four groups of algorithms with no statistically  
 632 significant differences in the Average *RPD* within each group. The first group  
 633 is composed of algorithm IG<sub>T</sub>, which, despite being a very recent proposal for  
 634 the no-idle flowshop, it no better than the rest. However, and as we can see,  
 635 it is the algorithm that benefits most from the added CPU time. The second  
 636 group is made up of hGA and IG<sub>R<sub>4</sub></sub>. These results are expected since, and  
 637 according to the results of Ruiz and Stützle (2007), the basic IG performs  
 638 very similar to that of the GA of Ruiz et al. (2006). A tight third group is  
 639 formed by IG<sub>R<sub>8</sub></sub>, hDDE<sub>D</sub>, hDDE<sub>P</sub> and hDPSO. With the exception of IG<sub>R<sub>8</sub></sub>,  
 640 which was not tested with  $d = 8$  by the original authors (Ruiz et al., 2009),

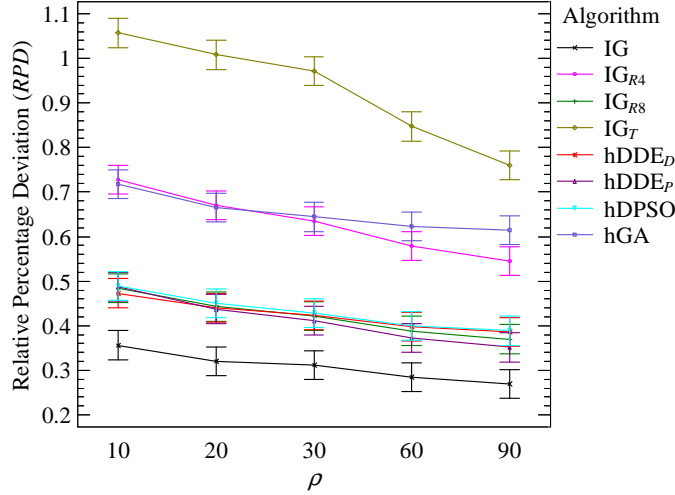


Figure 7: Means plot for the interaction between the algorithm and elapsed CPU time stopping criterion ( $\rho$ ). All means have Tukey's Honest Significant Difference (HSD) 95% confidence intervals.

641 the other three algorithms are very similar and therefore it is expected that  
 642 their performance is comparable with one another. The last group is formed  
 643 of the proposed method IG. We can see that for all CPU times (values of  $\rho$ )  
 644 its Tukey's Honest Significant Difference (HSD) 95% confidence intervals do  
 645 not overlap with the intervals of any of the other methods. This means that  
 646 for all tested values of  $\rho$ , the proposed IG is statistically better than all other  
 647 methods and by a significant margin. A full table with the breakdown of  $n$   
 648 and  $m$ , as well as all results, best detailed solutions, excel files and statistical  
 649 tests are available upon request from the authors.

## 650 6. Conclusions and future research

651 This paper proposes for the first time a generalization of both the regular  
 652 permutation flowshop and no-idle permutation flowshop scheduling problem  
 653 resulting from the consideration of both regular as well as no-idle machines  
 654 in the shop. The result is referred to as the mixed no-idle problem or MNPFSP.  
 655 It has many practical applications in the ceramic tile industry, the production  
 656 of ceramic frits, the steelmaking industry and the manufacturing of integrated  
 657 circuits among many others.

658 We have reviewed the existing literature and have proved the novelty of  
 659 the MNPFSP setting, for which we have presented a mixed linear integer

660 programming model. We have shown how to calculate the makespan value and  
661 have demonstrated that it is far from trivial. The insertion neighborhood is  
662 frequently employed by heuristics and metaheuristics in the flowshop literature  
663 and we have also presented in this paper a method for calculating all insertions  
664 of a job in a sequence in  $\mathcal{O}(nm)$  steps, reducing the computational complexity  
665 and allowing for fast methods. We have presented an improved Iterated  
666 Greedy (IG) method that builds on the successful algorithms of Ruiz and  
667 Stützle (2007). We have extended the method with a more comprehensive  
668 initialization, an improved destruction-reconstruction operator and referenced  
669 local search. After careful calibration, we have tested our proposed IG against  
670 7 other state-of-the-art methods mainly proposed for the no-idle flowshop. In  
671 a comprehensive benchmark of 1,750 instances and after an accumulated CPU  
672 time of almost two years we have demonstrated that the proposed IG is not  
673 only statistically better than all other methods in the mixed no-idle settings  
674 but also in the full no-idle environment and by a wide and significant margin.  
675 The outcome of the experimentation is also interesting since the proposed  
676 IG is much simpler than the competing hybrid discrete differential evolution  
677 and hybrid discrete particle swarm optimization methods. Our experiments  
678 include 350,000 different results which, along with the powerful statistical  
679 analyses allow us to conclude that the proposed IG is the new state-of-the-art  
680 both for the no-idle flowshop as well as for the new mixed no-idle flowshop.  
681 Future research will include the consideration of other optimization objectives  
682 and sequence dependent setup times, possibly for the regular idling machines  
683 as these configurations are common within industry. Hybrid no-idle or hybrid  
684 mixed no-idle flowshops pose another interesting avenue for future research.

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695 **References**

- 696 Adiri, I. and Pohoryles, D. (1982). Flowshop no-idle or no-wait scheduling to  
697 minimize the sum of completion times. *Naval Research Logistics*, 29(3):495–  
698 504.
- 699 Baker, K. R. (1974). *Introduction to Sequencing and Scheduling*. John Wiley &  
700 Sons, New York.
- 701 Baptiste, P. and Hguny, L. K. (1997). A branch and bound algorithm for the  
702  $F/no - idle/C_{max}$ . In *Proceedings of the International Conference on Indus-*  
703 *trial Engineering and Production Management, IEPM'97*, volume 1, pages  
704 429–438, Lyon, France.
- 705 Baraz, D. and Mosheiov, G. (2008). A note on a greedy heuristic for flow-  
706 shop makespan minimization with no machine idle-time. *European Journal of*  
707 *Operational Research*, 184(2):810–813.
- 708 Deng, G. and Gu, X. (2012). A hybrid discrete differential evolution algorithm for  
709 the no-idle permutation flow shop scheduling problem with makespan criterion.  
710 *Computers & Operations Research*, 39(9):2152–2160.
- 711 Dong, X., Huang, H., and Chen, P. (2008). An improved NEH-based heuristic  
712 for the permutation flowshop problem. *Computers & Operations Research*,  
713 35(12):3962–3968.
- 714 Fatih Tasgetiren, M., Pan, Q.-K., Suganthan, P. N., and Buyukdagli, O. (2013a).  
715 A variable iterated greedy algorithm with differential evolution for the no-idle  
716 permutation flowshop scheduling problem. *Computers & Operations Research*,  
717 40(7):1729–1743.
- 718 Fatih Tasgetiren, M., Pan, Q.-K., Suganthan, P. N., and Oner, A. (2013b). A  
719 discrete artificial bee colony algorithm for the no-idle permutation flowshop  
720 scheduling problem with the total tardiness criterion. *Applied Mathematical*  
721 *Modelling*, 37(10-11):6758–6779.
- 722 Framinan, J. M., Gupta, J. N. D., and Leisten, R. (2004). A review and clas-  
723 sification of heuristics for permutation flow-shop scheduling with makespan  
724 objective. *Journal of the Operational Research Society*, 55(1):1243–1255.
- 725 Framinan, J. M. and Leisten, R. (2008). Total tardiness minimization in per-  
726 mutation flow shops: a simple approach based on a variable greedy algorithm.  
727 *International Journal of Production Research*, 46(22):6479–6498.
- 728 Garey, M. R., Johnson, D. S., and Sethi, R. (1976). The complexity of flowshop  
729 and jobshop scheduling. *Mathematics of Operations Research*, 1(2):117–129.
- 730 Goncharov, Y. and Sevastyanov, S. (2009). The flow shop problem with no-idle  
731 constraints: A review and approximation. *European Journal of Operational*  
732 *Research*, 196(2):450–456.
- 733 Graham, R. L., Lawler, E. L., Lenstra, J. K., and Rinnooy Kan, A. H. G. (1979).  
734 Optimization and approximation in deterministic sequencing and scheduling:  
735 A survey. *Annals of Discrete Mathematics*, 5:287–326.
- 736 Gupta, J. N. D. and Stafford, Jr, E. F. (2006). Flowshop scheduling research  
737 after five decades. *European Journal of Operational Research*, 169(3):699–711.
- 738 Hejazi, S. R. and Saghafian, S. (2005). Flowshop-scheduling problems with

- 739 makespan criterion: A review. *International Journal of Production Research*,  
740 43(14):2895–2929.
- 741 Johnson, S. M. (1954). Optimal two- and three-stage production schedules with  
742 setup times included. *Naval Research Logistics Quarterly*, 1(1):61–68.
- 743 Kalczynski, P. and Kamburowski, J. (2007). On the neh heuristic for minimizing  
744 the makespan in permutation flow shops. *OMEGA, the International Journal  
745 of Management Science*, 35(1):53–60.
- 746 Kalczynski, P. J. and Kamburowski, J. (2005). A heuristic for minimizing the  
747 makespan in no-idle permutation flow shops. *Computers & Industrial Engi-  
748 neering*, 49(1):146–154.
- 749 Kamburowski, J. (2004). More on three-machine no-idle flow shops. *Computers  
750 & Industrial Engineering*, 46(3):461–466.
- 751 Minella, G., Ruiz, R., and Ciavotta, M. (2008). A review and evaluation of  
752 multi-objective algorithms for the flowshop scheduling problem. *INFORMS  
753 Journal on Computing*, 20(3):451–471.
- 754 Minella, G., Ruiz, R., and Ciavotta, M. (2011). Restarted iterated pareto greedy  
755 algorithm for multi-objective flowshop scheduling problems. *Computers &  
756 Operations Research*, 38(11):1521–1533.
- 757 Montgomery, D. C. (2012). *Design and Analysis of Experiments*. Wiley, eight  
758 edition.
- 759 Naderi, B. and Ruiz, R. (2010). The distributed permutation flowshop scheduling  
760 problem. *Computers & Operations Research*, 37(4):754–768.
- 761 Narain, L. and Bagga, P. C. (2003). Minimizing total elapsed time subject to  
762 zero total idle time of machines in  $n \times 3$  flowshop problem. *Indian Journal of  
763 Pure & Applied Mathematics*, 34(2):219–228.
- 764 Narain, L. and Bagga, P. C. (2005a). Flowshop/no-idle scheduling to minimise  
765 the mean flowtime. *Anziam Journal*, 47:265–275.
- 766 Narain, L. and Bagga, P. C. (2005b). Flowshop/no-idle scheduling to minimize  
767 total elapsed time. *Journal of Global Optimization*, 33(3):349–367.
- 768 Nawaz, M., Ensore, Jr, E. E., and Ham, I. (1983). A Heuristic Algorithm  
769 for the  $m$ -Machine,  $n$ -Job Flow-shop Sequencing Problem. *OMEGA, The  
770 International Journal of Management Science*, 11(1):91–95.
- 771 Nowicki, E. and Smutnicki, C. (1996). A fast tabu search algorithm for the  
772 permutation flow-shop problem. *European Journal of Operational Research*,  
773 91(1):160–175.
- 774 Osman, I. and Potts, C. (1989). Simulated annealing for permutation flow-  
775 shop scheduling. *OMEGA, The International Journal of Management Science*,  
776 17(6):551–557.
- 777 Pan, Q.-K., Fatih Tasgetiren, M., and Liang, Y.-C. (2008a). A discrete differ-  
778 ential evolution algorithm for the permutation flowshop scheduling problem.  
779 *Computers & Industrial Engineering*, 55(4):795–816.
- 780 Pan, Q.-K. and Ruiz, R. (2012). An estimation of distribution algorithm for lot-  
781 streaming flow shop problems with setup times. *OMEGA, the International  
782 Journal of Management Science*, 40(2):166–180.
- 783 Pan, Q.-K. and Ruiz, R. (2013). A comprehensive review and evaluation of per-

- 784 mutation flowshop heuristics to minimize flowtime. *Computers & Operations*  
785 *Research*, 40(1):117–128.
- 786 Pan, Q.-K. and Wang, L. (2008a). No-idle permutation flow shop scheduling  
787 based on a hybrid discrete particle swarm optimization algorithm. *International*  
788 *Journal of Advanced Manufacturing Technology*, 39(7-8):796–807.
- 789 Pan, Q.-K. and Wang, L. (2008b). A novel differential evolution algorithm  
790 for no-idle permutation flow-shop scheduling problems. *European Journal of*  
791 *Industrial Engineering*, 2(3):279–297.
- 792 Pan, Q.-K. and Wang, L. (2012). Effective heuristics for the blocking flowshop  
793 scheduling problem with makespan minimization. *OMEGA, the International*  
794 *Journal of Management Science*, 40(2):218–229.
- 795 Pan, Q.-K., Wang, L., and Zhao, B. H. (2008b). An improved iterated greedy  
796 algorithm for the no-wait flow shop scheduling problem with makespan cri-  
797 terion. *International Journal of Advanced Manufacturing Technology*, 38(7-  
798 8):778–786.
- 799 Rad, S. F., Ruiz, R., and Boroojerdian, N. (2009). New high performing heuris-  
800 tics for minimizing makespan in permutation flowshops. *OMEGA, the Inter-*  
801 *national Journal of Management Science*, 37(2):331–345.
- 802 Ribas, I., Companys, R., and Tort-Martorell, X. (2010). Comparing three-step  
803 heuristics for the permutation flow shop problem. *Computers & Operations*  
804 *Research*, 37(12):2062–2070.
- 805 Ribas, I., Companys, R., and Tort-Martorell, X. (2011). An iterated greedy  
806 algorithm for the flowshop scheduling problem with blocking. *OMEGA, The*  
807 *International Journal of Management Science*, 39(3):293–301.
- 808 Ruiz, R. and Maroto, C. (2005). A comprehensive review and evaluation of  
809 permutation flowshop heuristics. *European Journal of Operational Research*,  
810 165(2):479–494.
- 811 Ruiz, R., Maroto, C., and Alcaraz, J. (2006). Two new robust genetic algorithms  
812 for the flowshop scheduling problem. *OMEGA, the International Journal of*  
813 *Management Science*, 34:461–476.
- 814 Ruiz, R. and Stützle, T. (2007). A simple and effective iterated greedy algo-  
815 rithm for the permutation flowshop scheduling problem. *European Journal of*  
816 *Operational Research*, 177(3):2033–2049.
- 817 Ruiz, R. and Stützle, T. (2008). An iterated greedy heuristic for the sequence de-  
818 pendent setup times flowshop problem with makespan and weighted tardiness  
819 objectives. *European Journal of Operational Research*, 187(3):1143–1159.
- 820 Ruiz, R., Vallada, E., and Fernández-Martínez, C. (2009). Scheduling in flow-  
821 shops with no-idle machines. In Chakraborty, U., editor, *Computational In-*  
822 *telligence in Flow Shop and Job Shop Scheduling*, chapter 2, pages 21–51.  
823 Springer, New York.
- 824 Saadani, N. E. H., Guinet, A., and Moalla, M. (2001). A travelling salesman  
825 approach to solve the  $F/no - idle/C_{max}$  problem. In *Proceedings of the Inter-*  
826 *national Conference on Industrial Engineering and Production Management,*  
827 *IEPM'01*, volume 2, pages 880–888, Quebec, Canada.
- 828 Saadani, N. E. H., Guinet, A., and Moalla, M. (2003). Three stage no-idle

- 829 flow-shops. *Computers & Industrial Engineering*, 44(3):425–434.
- 830 Saadani, N. E. H., Guinet, A., and Moalla, M. (2005). A travelling salesman  
831 approach to solve the  $F/no - idle/C_{max}$  problem. *European Journal of Oper-*  
832 *ational Research*, 161(1):11–20.
- 833 Salveson, M. E. (1952). On a quantitative method in production planning and  
834 scheduling. *Econometrica*, 20(4):554–590.
- 835 Taillard, E. (1990). Some efficient heuristic methods for the flow shop sequencing  
836 problem. *European Journal of Operational Research*, 47(1):67–74.
- 837 Taillard, E. (1993). Benchmarks for basic scheduling problems. *European Journal*  
838 *of Operational Research*, 64(2):278–285.
- 839 Vachajitpan, P. (1982). Job sequencing with continuous machine operation.  
840 *Computers & Industrial Engineering*, 6(3):255–259.
- 841 Vallada, E. and Ruiz, R. (2009). Cooperative metaheuristics for the permuta-  
842 tion flowshop scheduling problem. *European Journal of Operational Research*,  
843 193(2):365–376.
- 844 Vallada, E., Ruiz, R., and Minella, G. (2008). Minimising total tardiness in  
845 the  $m$ -machine flowshop problem: A review and evaluation of heuristics and  
846 metaheuristics. *Computers & Operations Research*, 35(4):1350–1373.
- 847 Čepek, O., Okada, M., and Vlach, M. (2000). Note: On the two-machine no-idle  
848 flowshop problem. *Naval Research Logistics*, 47(4):353–358.
- 849 Woollam, C. R. (1986). Flowshop with no idle machine time allowed. *Computers*  
850 *& Industrial Engineering*, 10(1):69–76.
- 851 Ying, K. C. (2008). Solving non-permutation flowshop scheduling problems  
852 by an effective iterated greedy heuristic. *International Journal of Advanced*  
853 *Manufacturing Technology*, 38(3-4):348–354.