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AN EMPIRICAL ANALYSIS OF THE FIXED COEFFICIENT "MANPOWER REQUIREMENTS" MODEL, 1960-1970

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ABSTRACT

The fixed coefficient "manpower requirements" model is one of the most widely used tools in the empirical analysis of labor skills. The model has the advantage of providing information on the effect of changes in the industrial composition of an economy on demand for labor in highly disaggregated occupations at the cost of neglecting factor substitution. This study examines the ability of the fixed coefficient model to explain changes in employment in 3-digit occupations in the United States from 1960 to 1970 and develops an "augmented requirements" model which uses changes in wages as well as fixed coefficient shifts in demand to analyze changes in employment. The paper finds that 1. by themselves, the requirements shifts account for much of the change in employment among detailed occupations in the period studied, though standard errors of estimate are sizeable; 2. even with crude adjustments for factor price effects, demand for detailed skills is far from zero elastic; 3. the fixed coefficient model seems to work not because demand and supply are economically unresponsive but because the variation in the wage structure and corresponding incentive to alter input coefficients is moderate relative to the variation in the shift in demand due to changes in industrial mix.

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One of the most widely used tools in the empirical analysis of labor skills is the fixed coefficient "manpower requirements" model. Variants of the model have been employed by the U.S. Bureau of Labor Statistics to forecast manpower "needs" and provide guidance in vocational decision-making; by the O.E.C.D. in its Mediterranean Regional Project to analyze relations between growth and educational "requirements"; and by numerous developing countries as part of the manpower planning process. Wide usage notwithstanding, the fixed coefficient approach has been severely criticized by many economists. 2 From the perspective of standard factor demand theory, the main flaw of the model is its failure to allow for the adjustment of inputs to changes in factor prices. As a tool of labor market analysis, the approach also suffers from being widely used with extrapolative supply projections to forecast 3 shortages or surpluses in a system that neglects supply as well as demand adjustments. In large measure because of the poor supply projections, requirements/ supply forecasts of market problems have often been seriously in error, projecting "shortages" for example when "surpluses" in fact developed (see Freeman and Breneman).

These difficulties notwithstanding, the fixed coefficient demand model offers the only general analytic tool for studying the effect of changes in the industrial composition of an economy on demand for workers in a large number of disaggregate occupations. The alternative variable coefficient production function methodology cannot handle more than a few different inputs due to the number of elasticity parameters involved.

Like input-output analysis in general, the fixed coefficient manpower model sacrifices potential knowledge about substitution among aggregated inputs for knowledge about disaggregated changes in the industrial mix in the economy. Whether this tradeoff is worthwhile is an empirical issue dependent on the problem under study, the extent of disaggregate shifts in industrial structure, and the extent of factor substitution.

To judge the usefulness of the tool, it is necessary to examine the actual link between fixed coefficient shifts in demand for labor skills and changes in employment at the level of disaggregation on which the analysis focuses.

This paper presents such an investigation using data on 3 digit occupations in the United States from 1960 to 1970. It imbeds the fixedcoefficient manpower approach into a more general demand model, in which the fixed coefficient calculations are interpreted as measures of horizontal shifts in demand whose elasticity is set by standard substitution considerations and in which employment depends on changes in wages as well as shifts in demand. The "augmented" model is estimated and compared to the simple fixed coefficient predictions. There are three basic findings. First, by themselves, the requirements shifts account for much of the change in employment among detailed occupations in the period studied, though standard errors of estimate are sizeable. Second, even crude adjustments for factor price effects show that demand for detailed skills is far from zero elastic. Third, the model seems to work not because demand and supply are economically unresponsive but because the variation in the wage structure and corresponding incentive to alter manpower coefficients is moderate relative to the variation in the shift in demand due to changes in industrial mix.

The paper is divided into five sections. The first sets out the basic methodology of the fixed coefficient approach and develops an augmented requirements model [ARM] which also allows for factor substitution.

The second examines the variation in the changes in employment and income among detailed occupations in the 1960-1970 period and the link between changes in employment predicted by fixed coefficient shifts and actual changes. Section three presents estimates of the reduced form employment and demand equations of the ARM model. Section four seeks to explain the greater variation in changes in employment than in changes in incomes among occupations in terms of the estimated demand relation and the apparently high occupational mobility of the work force. There is a brief conclusion.

I The Model

The principal element in manpower requirements analysis is an interindustry model in which labor skill coefficients—the ratio $\mathbf{a_{ij}}$ of workers in an occupation \mathbf{i} and industry \mathbf{j} [N_{ij}] to total industry employment [N_j]—are assumed to be fixed. The assumption of fixed input ratios means that only a single observation is needed to estimate $\mathbf{a_{ij}}$ (though more observations should improve the estimates), which permits a highly disaggregate analysis of occupational skills across industries that would not be possible if substitution parameters were also estimated. 5

With input ratios within industries fixed, the moving force of the requirements model is the changing industrial composition of employment (or output), which is taken as exogenous to the labor market. Formally, if D₁ is the number of workers "demanded" in occupation i (other factors fixed), the basic coefficient relation is:

(1)
$$D_i = \sum_{j=1}^{n} N_j$$
.

In the year (data set) in which the a_{ij} are calculated, equation (1) is an identity and D_i will equal the actual number employed. The equation becomes a model when a particular a_{ij} matrix is applied to other periods or data sets.

Taking first differences of (1) yields the basic equation relating changes in industry employment to shifts in demand for occupation skills:

(2) $\Delta D_i = \sum_{j} \sum_{i,j} \Delta N_j$ where Δ is the difference operator. Letting L_i = actual employment, the actual change in employment, ΔL_i is, by definition:

(3) $\Delta L_i = \sum_j a_{ij} \Delta N_j + \sum_j \Delta a_{ij} + \sum_j \Delta a_{ij} \Delta N_j = \Delta D_i + \sum_j \Delta a_{ij} + \sum_j \Delta a_{ij} \Delta N_j$ From equation (3) we see that ΔD_i will give a perfect prediction of the change when $\Delta a_{ij} = 0$ or when $\sum_j N_j \Delta a_{ij} + \sum_j \Delta a_{ij} \Delta N_j$ equals zero. That is, when input coefficients are fixed or changes happen to balance out.

Equation (2) can be fruitfully rewritten in percentage change or elasticity form by dividing both sides by D_i (= L_i in the base period):

(4)
$$\dot{D}_{i} = \Delta D_{i}/D_{i} = \sum_{j} a_{ij} N_{j}/D_{i} \frac{\Delta N_{j}}{N_{i}} = \sum_{j} \gamma_{ij} \dot{N}_{j}$$

where $\gamma_{ij} = N_{ij}/D_i = a_{ij}N_j/D_i$ and dots above variables relate to percentage changes. Note that in (4) the parameters which weight changes in employment are not (as before) the proportion of workers in the jth industry employed in the ith occupation (a_{ij}) but the proportion of workers in the ith occupation employed in the jth industry $(a_{ij}, N_j/L_j)$.

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In this paper I interpret ΔD_i or D_i as measures of horizontal <u>shifts</u> in demand due to changes in the interindustrial mix of employment at fixed wages, <u>not</u> (as is common in the requirements literature) as predicted manpower needs. The changes are part of the more general demand function for occupation i:

(5)
$$\dot{L}_i = \dot{D}_i - \eta_i \dot{W}_i + \mu_i$$

where \dot{L}_{i} = percentage change in demand for labor in occupation i.

 \dot{W}_{i} = percentage change in wages in i

 η_i = elasticity of demand in i

 μ_i = changes in demand not attributable to measured shifts

$$E(\mu_i) = E(\mu_i \dot{W}_i) = E(\mu_i \dot{D}_i) = 0$$
 and $V(\mu_i) = \sigma^2$

In equation (5) other factor prices are assumed constant; in empirical work, the change in wage in occupation i will be compared to the average change for all occupations.

Rewriting the actual change in employment (3) in percentage change form yields a comparable expression for \hat{L}_i in terms of changes in industrial employment and in input coefficients:

(6)
$$\dot{\mathbf{L}}_{\mathbf{i}} = \Sigma \gamma_{\mathbf{i}\mathbf{j}} \dot{\mathbf{N}}_{\mathbf{j}} + \Sigma \gamma_{\mathbf{i}\mathbf{j}} \dot{\mathbf{a}}_{\mathbf{i}\mathbf{j}} + \Sigma \gamma_{\mathbf{i}\mathbf{j}} \dot{\mathbf{a}}_{\mathbf{i}\mathbf{j}} \dot{\mathbf{N}}_{\mathbf{j}}$$

where all summations are taken over j.

If η_{ij} is the elasticity of demand for the ith occupation in industry j, the changes in input coefficients can be written as:

(7)
$$a_{ij} = -\eta_{ij} \dot{w}_{i}$$

where for simplicity other (random) changes in the coefficients are ignored.

Substituting (7) into (6) and noting that $\dot{D}_i = \Sigma \gamma_{i,j} \dot{N}_j$ yields:

(8)
$$\dot{L}_{i} = \dot{D}_{i} - \Sigma \gamma_{ij} \eta_{ij} \dot{w}_{i} - \Sigma \gamma_{ij} \eta_{ij} \dot{w}_{i} \dot{N}_{j}$$

an equation which makes the overall response of demand to changes in wages a weighted average of responses of demand within industries $(\Sigma\gamma_{ij}\eta_{ij}\dot{W}_i)$ and an interaction term $(\Sigma\gamma_{ij}\eta_{ij}\dot{W}_i\dot{N}_j)$.

When the interaction term is sufficiently small to be ignored, 6 equation (8) translates directly into the summary demand equation (5), 7 with

(9)
$$\eta_{i} \simeq \Sigma \gamma_{ii} \eta_{ii}$$

Equation (9) shows that the elasticity of demand for workers in occupation i is a weighted average of the elasticities of demand for the occupation across the j industries.

When the interaction term is large, on the other hand, expression (8) shows that (5) is not an adequate representation of the change in demand, for it ignores the interaction effect. While in general there is no easy way to treat interactions, it can be readily seen that when the η_{ij} are approximately the same $(=\eta_i)$ the right hand side of equation (8) simplifies to:

$$(10) \quad \dot{D}_{i} - \eta_{i} (\Sigma \gamma_{ij}) \dot{W}_{i} - \eta_{i} (\Sigma \gamma_{ij} \dot{N}_{i} \dot{W}_{i}) = \dot{D}_{i} - \eta_{i} \dot{W}_{i} - \eta_{i} \dot{D}_{i} \dot{W}_{i}$$

According to (10) an appropriate specification of demand requires not only shift and wage terms but also their direct multiplicand, which should obtain a coefficient equal to the elasticity of demand. Because of the finite difference form, shifts in demand have small effects on employment when wage changes are large while wage changes have large effects on employment when demand shifts are large.

However one treats the interaction effects, the model of (1)-(10) shows that the assumption that input coefficients respond to changes in wages can yield a relatively simple generalization of the fixed coefficient model, in which changes in wages operate through a single elasticity term.

One additional assumption is needed for the demand model to be empirically tractable. Because the requirements analysis is applied to decadal changes in a large number of occupations, it is not possible to estimate (5) with separate elasticities for each occupation. Instead η_i must be assumed to be the same across occupations, yielding the following demand function to be estimated:

(5')
$$\dot{L}_{i} = \dot{D}_{i} - \eta_{i} \dot{W}_{i} + v_{i}$$

where v_i has a mean 0 and variance σ^2

The augmented requirements model is closed by addition of a supply equation linking changes in the supply of labor to occupations to movements along a supply schedule due to changes in wages and to shifts in the schedule due to other factors (such as changes in the sex distribution of the work force or especially high wages in the base year). Let $\dot{L}_i^s = \ln$ change in number of workers supplied; $\dot{s}_i = \ln$ shift in schedule due to measured factors other than changes in wages 10 ; $\Sigma_i = \text{shifts in supply due to unmeasured}$ factors, with $E(\Sigma_i) = 0$ and $v_i(\Sigma_i) = \sigma_1^2$. Then we can represent changes in the supply of labor by:

(11)
$$\dot{L}_{i}^{s} = \dot{S}_{i} + \phi \dot{W}_{i} + \Sigma_{i}$$

Alternatively, if supply is assumed to decline over time proportionately with the size of the work force due to normal retirement, death, or other mobility patterns, the supply curve can be written as:

(11')
$$\dot{L}_{i} = \dot{S}_{i} + \phi \dot{W}_{i} - \lambda L_{i} (-1) + \Sigma_{i}$$

where λ = rate of attrition of workers. Note that in (11) and in (11'), as in (5'), each occupation is assumed, for reasons of empirical tractability, to have the same elasticity of response.

Employment Determination

The model consisting of demand equation (5') and supply equation (11) yields,

on the assumption of market clearing, a reduced form employment equation linking \dot{L}_i to the shift in demand due to interindustrial mix and to the shift in supply (12) $\dot{L}_i = (\dot{\Phi}\dot{D}_i + \dot{\eta}\dot{S}_i)/(\dot{\Phi} + \dot{\eta}) + (\dot{\Phi}\dot{\mu}_i + \dot{\eta}\dot{\Sigma}_i)/(\dot{\Phi} + \dot{\eta})$

This equation shows that, on average, changes in employment depend on a weighted average of the shift in demand and the shift in supply, with weights reflecting the relative size of the supply and demand parameters. 12 If, for simplicity, we assume no exogenous shifts in supply $(\dot{S}_i = 0)$, the requirements model is seen to provide a perfect prediction of changes in employment under two conditions: when the elasticity of demand is zero $(\eta = 0)$, the usual fixed coefficient postulate; or when the elasticity of supply is infinite $(\Phi = \infty)$, so that wages do not change. More generally, \dot{D} , will give a good fix on \dot{L} , whenever Φ/η is large or, given shifts in supply, when $\Phi D_i/\eta S_i$ is large. The point is that the model does not require zero elastic demand to track changes in demand reasonably well. When supply is highly elastic, so that relative wages do not change greatly; when shifts in supply are dwarfed by shifts in demand; or when the elasticity of supply is large relative to the elasticity of demand, the fixed coefficient model will provide valuable information on changes in employment. The contribution of the model depends, it should be stressed, on the actual magnitude of shifts in demand, changes in wages, and shifts in supply as well as on the elasticities, so that the model may work well in some periods (i.e., when \dot{D}_{i} is large relative to W_i) but not in other periods. Only by an empirical analysis can we judge the usefulness of the model in post-world war II years.

II Changes in the 1960-1970 Decade

This study examines the applicability of the augmented requirements model to changes in employment in 3 digit occupations in the U.S. from 1960 to 1970. The major dependent variable, the change in employment, \hat{L}_i , and the fixed coefficient shift in demand, \hat{D}_i , were calculated from industry by

occupation data provided by the Bureau of Labor Statistics, based on data from the 1960 and 1970 Censuses of Population. ¹³ The 1960 matrix of input coefficients (A_{ij}) was used together with actual 1970 industry employment levels to predict shifts in demand for occupations. These shifts were then compared to actual changes in employment as estimated from the B.L.S. data. With superscripts to reflect the time period, the level of employment in 1960 and 1970 by occupation was obtained from

(13a)
$$L_i^{1960} = (A_{ij})^{1960} N_j^{1960}$$

(13b)
$$L_i^{1970} = (A_{ij})^{1970} N_i^{1970}$$

and the predicted level from

(13c)
$$D_{i}^{1970} = (A_{ij})^{1960} N_{j}^{1970}$$

where L_{i}^{1960} and L_{i}^{1970} are column vectors of employment by occupation; (A_{ij}) is an occupation by industry matrix; N_{j} is a column vector of employment by industry; and D_{i} is a column vector of fixed coefficient "demand" for workers. In the B.L.S. matrix there were 142 industries and 286 occupations. For empirical analysis the number of occupations was reduced to 254, with such groups as unpaid family labor, apprentices, student nurses, some 'not elsewhere classified,' and certain other small categories deleted or amalgamated into others. And certain other small categories deleted or amalgamated into others. Changes in actual employment (L_{i}) were calculated by taking log differences between L_{i}^{1970} and L_{i}^{1960} ; the fixed coefficient shift term was also measured in log form.

The major problem in analyzing the occupational change data is that between 1960 and 1970 the Census altered greatly its occupational definitions, expanding the number of categories from 297 (including diverse not elsewhere classified groups) to 441. To make categories comparable over time, the occupations based on 1970 categories were transformed into occupations based on 1960 definitions using the U.S. Bureau of the Census' Technical Paper 26 1970 Occupation and Industry Classifications in Terms of Their 1960 Occupation and Industry Elements.

Table 1 of that volume provides data on the percent of persons in each 1970 occupation who would have been in the various 1960 groupings. It was deemed more fruitful to collapse occupations based on 1970 definitions into occupations based on 1960 groups than to do the reverse because of the potentially smaller error in aggregating than in decomposing groups and because of the desire to preserve the actual 1960 matrix as the critical component of the analysis. The 1970 industry figures were similarly bridged to 1960 definitions using Table 2 of Technical Paper 26.

The other variables of the model were obtained from published Census data as described in the notes for tables 3 and 4 and were similarly 'bridged' into 1960 categories using the same procedure from Technical Paper 26. Changes in wages were approximated by changes in the average of the median income of male and female workers in an occupation, using the proportion in each occupation by sex to form the average. While it would be more desirable to have changes in mean hourly rates of pay, the published Census data do not permit calculation of that variable for the two periods. Shifts in supply were estimated from changes in the distribution of the total work force by sex and education assuming that workers in a given sex-education class had (with wages fixed) the same propensity to choose a particular occupation in 1970 as in 1960:

(14)
$$\dot{s}_{i} = \Gamma_{ij}\dot{t}_{j}$$

where Γ_{ij} = proportion of workers in occupation in 1960 in the jth sexeducation group

 \dot{E}_{j} = percentage change in persons in the jth sex-education group. The sex-education data were also used to calculate the mean years of schooling of workers in an occupation.

Because of the bridging of the income (and other) Census data needed to obtain comparable 1960-1970 categories, there is a potentially substantial

measurement error for occupations which undergo considerable change. To obtain a 1970 income for a "1960 occupation" which was divided into several groups in 1970, it is necessary to take a weighted average of the incomes in the 1970 occupations, on the assumption that persons who would have been in the 1960 category are paid the average of persons in the 1970 group. When a 1970 occupation contains several 1960 groups, this assumption is liable to be wrong, leading to errors of measurement. As some occupational definitions are essentially the same in both years (accounting, for example) while other undergo sizeable definitional changes (tailors, which in 1970 included what had been previously termed operatives n.e.c. in 5 industries and laundry and dry cleaning operatives) in some calculations the sample is restricted to occupations with relatively small changes in definitions, thereby minimizing measurement problems.

Patterns of Change and Interrelations

The pattern of change in the major variables of concern is examined in table 1, which records the standard deviation of the log changes in employment and in wages among occupations and the standard deviation of the log changes in calculated shifts in demand and supply. Column 1 gives the basic standard deviations while column 2 gives "weighted" standard deviations obtained by weighting the observations by the square root of the number of workers in 1960. The weighted statistics have the advantage of minimizing the impact of the often large log changes in small occupations, where measurement error is likely, and of placing greater importance on the larger and more significant groupings.

What stands out in lines 1 and 2 in the <u>much greater variation in</u> changes in employment than in changes in income. In unweighted form,

Table 1: Standard Deviation in Log Changes in Employment, Income, Shifts in Demand and Supply for 254 3-Digit Occuaptions, 1960-1970

		Standard Unweighted	Deviations Weighted by 1960 Employment		
1.	Employment	.39	.29		
2.	Wages	.13	.12		
3.	Demand Shift	.21	.18		
4	Supply shift	.20	.19		

Source: Lines 1,3 calculated from U.S. B.L.S. Occupation by Industry Master tape as described in text. Line 2 calculated from income data from U.S. Census of Population 1960 Occupational Characteristics, table 1 and U.S. Census of Population 1970, Occupational Characteristics, table 1. Supply shift in line 4 calculated from U.S. Census of Population 1960, Occupational Characteristics, table 9 and U.S. Census of Population 1970 Occupational Characteristics, table 5. Data on 1970 occupations in lines 2 and 4 was bridged from comparability with 1960 occupations, as described in the text, using U.S. Bureau of the Census Technical Paper 26, 1970 Occupation and Industry Classification Systems in terms of their 1960 Occupation and Industry Elements (b.S. C.F.O., July 1972).

σ(L) is three times as large as σ(W). Weighted by the square root of the number of workers in 1960, the standard deviation of log changes in employment falls markedly, indicative of the large variance in employment changes among small occupations, but is still nearly 2 1/2 times the standard deviation in the log changes of wages. Indicative of the greater variation in employment than wages in the underlying data, the unweighted average change in employment in the ten fastest growing occupations from 1960 to 1970 was 1.13 log points compared to an unweighted average change of -.73 points for the ten slowest while the average change in income in the ten occupations with the greatest increases in income was .82 log points compared to an average change of .14 points in the ten occupations with the smallest increases in income.

The differential pattern of change in employment and income constitutes a major empirical relation for the analysis of this study. In the context of supply and demand, there are three possible explanations for the enormous variation in employment among occupations and relatively moderate variation in incomes. First, demand for labor skills could be highly elastic, limiting variation in wages, while the supply of workers shifts greatly over time. This is the high elasticity of substitution interpretation placed by various analysts on cross-country data on relative incomes and employment among skill groups. 15 A second possibility is that shifts in the demand and supply of labor skills are, for unknown reasons, positively correlated, preserving the wage structure while altering the composition of jobs. The third possibility, to be termed the dynamic demand/elastic supply hypothesis, is that the supply of labor is relatively elastic, which limits variation in wages, while the demand for labor is highly variable, producing substantial changes in employment. In this case movements along a demand curve do not contribute greatly to changes in employment not because substitution among labor

skills is limited but because wage variation is moderate due to elastic labor supply schedules.

The standard deviations of the calculated demand and supply shift terms in lines 3 and 4 cast light on potential explanations of changes in employment. They show that changes in the industry mix and in the sex and education mix of the work force produced sizeable and comparable dispersions in the shifts of supply and demand among occupations, which implies a potential role for both forces in the observed differential growth of occupations. More formally, since by reduced form equation (12) \dot{L}_i should be a weighted average of \dot{D}_i and \dot{S}_i , the variances in lines 3 and 4 can also be fruitfully compared to the variance in line 1. If the demand and supply shift terms caught all of the changes in employment, then

$$(15) \ \sigma^{2}(\dot{L}_{i}) = W^{2}\sigma^{2}(\dot{D}) + (1-W)^{2}\sigma^{2}(\dot{S}) + 2W(1-W)R\sigma(\dot{D})\sigma(\dot{S})$$

where W = $\phi/(\phi + \eta)$ < 1 and R is the correlation between \dot{D} and \dot{S} . Given the values of $\sigma(\dot{D})$ and $\sigma(\dot{S})$ in the table and a correlation coefficient of 0.43 between \dot{D} and \dot{S} , the greatest possible variance on the right hand side occurs when W is about one-half. With this value(15) yields a standard deviation of .17, much below the observed value of .29. The implication is that the changes in employment due to unmeasured shifts in supply or demand are also quite important.

Table 2 turns from the pattern of variation in the major variables of concern to the univariate link between the driving force of the augmented requirements model, the fixed coefficient shift in demand, and actual changes in employment in the 254 occupation sample. If \hat{D}_i and \hat{L}_i are closely connected in the simple statistics presented in the table, there is some plausibility to the fixed coefficient approach; if not, we should abandon the exercise at this point. Line 1 records the correlation coefficient between \hat{D}_i and \hat{L}_i while line 2 gives the correlation between the variables, with

the observations by the square root of employment in 1960 in each occupation. The weighted correlation gives greater weight to the larger occupations and less to smaller occupations which, as noted, often evince sizeable log changes in employment. Line 3 records the number of cases in which the predicted change in the share of employment in occupation i has the same sign as the actual change in the share. It is a non-parametric statistic that allows differences in demand or supply elasticities among occupations to create differences in the impact of \dot{D}_{i} on \dot{L}_{i} but which requires that shifts in demand dominate market outcomes in the sense of producing changes in employment in the same direction as the changes in demand.

The statistics show that the fixed coefficient component of the change in demand does a reasonably good job of tracking employment. Despite the large variation in \dot{L}_i due to the changes in small occupations, the correlation coefficient in line 1 is 0.50. With observations weighted by the square root of the number of workers in 1960, the correlation rises to 0.66, so that 44% of the total variation in \dot{L}_i can be attributed to \dot{D}_i . In 70% of the cases the direction of change is correctly predicted, a result that is highly significant by the sign test. 16

II The Augmented Requirements Model

The finding in table 2 of a reasonably close link between the fixed coefficient shift in demand and changes in employment suggests the value of a more detailed investigation of the augmented requirements model. To what extent can the explanation of changes in employment be improved by taking account of supply side developments and movements along demand schedules? In the cross-occupation data treated by the requirements model is there a sizeable or miniscule response of demand to wage changes? What types of supply and demand schedules and

Table 2 Univariate Relations Between Fixed Coefficient Shifts in Demand and Actual Employment Changes, 3 Digit Occupations 1960-1970

- l. Correlation Coefficient (unweighted) .50 L_i and D_i
- 2. Correlation Coefficient (weighted) .66 \dot{L}_{i} and \dot{D}_{i}
- 3. Number of cases in which Δl_1 and Δd_1 have the same sign/total cases

Source: Calculated from 254 occupation sample.

shifts account for the differential variation of changes in employment and in wages by detailed occupation?

As a first step toward answering these questions, the reduced form employment equation (12) was estimated for several samples of 3 digit occupations. The dependent variable in the regressions is the log change of employment in three digit occupations. The independent variables are: the predicted log change from the fixed coefficient model; the predicted shift in supply; and the log of lagged number of workers in occupation. The calculations were done using ordinary least squares and weighted least squares, with weights based on the square root of the number of workers in an occupation in 1960. Because of the potential heteroskedasticity of log changes in employment in small, often ill-defined occupations, ¹⁸ which may be in part due to the fact that the data are based on a 5% sample of the Census rather than a complete count, the weighted regressions are more desirable and will be given greater stress in evaluating results. In no case do results hinge critically on whether the regressions are weighted or not.

The results, summarized in table 3, show that the demand and supply shift terms have a substantive positive effect on employment, with the coeficient on the former always larger than that on the latter, though by an amount that differs depending on the weighting and sample. In line 1, which treats the complete 254 occupations in unweighted regressions, a log change in D changes employment by nearly twice as much as a log change in S. In line 2, where weighted regressions are used, the impact of the demand shift term rises while that of the supply shift term falls, with a resultant differential of nearly 5 to 1. The overall explanatory power of the model is considerably higher and the standard

Table 3: Estimates of the Effect of Demand and Supply Shifts on Changes in Employment, 1960-1970¹

	sample		constant	Regression	Coefficients	s and Standard		Estimate
		regression		Ď	Š	L _i (-1)	R ²	SEE
1.	A	no	.05	.71 (.12)	.44 (.13)	.02	.29	.346
2.	A	yes	.60	.88 (.09)	.14 (.09)	05 (.01)	.49	.208
3.	В	yes	.49	.79 (.10)	.31 (.10)	04 (.01)	.49	.246
4.	С	yes	.51	.79 (.10)	.31 (.10)	04 (.01)	.49	.245

The dependent variable is the log change in employment. Numbers in parentheses are standard errors.

Weighted refers to whether or not the observations were weighted by the square root of the number of workers in 1960.

 $^{^{3}}$ The samples are defined as follows:

A = 254 occupations, complete sample

B = 231 occupations, all not elsewhere classified (nec) occupation deleted

C = 215 occupations, all occupations with "bad bridge" and all nec's deleted

error of estimate for the equation considerably lower in the weighted than in the unweighted regressions, presumably because the former attach less importance to the random variation in the log changes of employment in occupations with relatively few workers. Lines 3 and 4 report the results of experiments with smaller more narrowly defined groupings. Line 3 omits all 'not elsewhere classified' occupations. This raises the coefficient on \hat{s}_i and lowers that on \hat{D}_i but still leaves a sizeable differential sizeable differential impact of 2 1/2 to 1. Line 4 deletes additional occupations for which the bridging of 1970 categories into 1960 categories seemed worst, with roughly comparable results. In these cases, moreover, the differences between weighted and unweighted (not reported in the table) regressions were much smaller, supporting the interpretation of the marked differential in the complete sample as being largely due to changes in ill-defined or badly measured groups.

According to equation (12) the coefficients on D to S reflect the elasticities of demand and supply. If the shift variables are reasonably good measures of horizontal changes, their regression coefficients will sum to unity and the ratio of the D to S coefficients reflect the elasticity of supply relative to demand. The sum is close to unity in lines 2-4 but exceeds it somewhat in the unweighted regression of line 1. The ratio of coefficients is always above one, by amounts ranging from 1.7 to 6.3, which implies that supply is more elastic than demand. Taking the restricted sample results as providing the "best" estimates of the key parameters, supply is estimated to be 2.5 times as elastic as demand.

Shares of Employment

Because requirements forecasts often focus on the <u>share</u> of workers in various occupations, it is of some value to examine the relation between changes in the share of employment in occupations predicted by the fixed coefficient model and actual changes in the share of employment in occupations.

There are two basic ways to analyze changes in shares. First, information theoretic concepts, which treat predicted or actual proportions, can be used to calculate the "nits" of information given by the demand shift model. In terms of information theory (see Theil for a detailed discussion) the inaccuracy of the fixed coefficient predictions can be measured by

(16)
$$I_1 = \sum_{i=1}^{n} \log(\ell_i/d_i)$$

where ℓ_i = share of workers in occupation i in 1970

 d_i = share of workers in occupation i in 1970 predicted by the requirements model. (D, divided by total employment in 1970).

This measure reflects the inaccuracy of the predictions in terms of the deviation of the true (posterior) proportion (ℓ_1) from the predicted (rior) proportion (d_i). When all predicted proportions are exactly correct ($d_i = \ell_i$), no new information is conveyed by actual developments and $I_1 = 0$. When predicted proportions are not correct ($d_i \neq \ell_i$ for some i), I_1 takes on a negative value, indicating that the predicted proportions do not explain fully actual proportions. In the data set under study, $I_1 = -.00010$, which means that there is only a relatively small average error in using d_i to predict ℓ_i .

A stronger test of the information content of the requirements shift is to compare the inaccuracy of predictions based on the d_i with the inaccuracy of an alternative predictor. A reasonable alternative is the 1960 share of workers in an occupation (ℓ_i (-1)) which is the appropriate share under the "null hypothesis" that proportions do not change. In this case we obtain:

(17)
$$I_2 = \sum_{i=1}^{n} \log[\ell_i(-1)/d_i] = I_1 - \sum_{i=1}^{n} \log[\ell_i/\ell_i(-1)]$$

which will be negative when the d_i are closer to the actual ℓ_i than are the ℓ_i (-1) and positive when the d_i are further from ℓ_i than are the ℓ_i (-1).

In the 254 occupation sample I_2 takes on the value of -.0007. The

negative value shows that d_i does a much better job in predicting ℓ_i than does the lagged share: the average error with the d_i prediction is .00017 points (= -.00010 - .00007) lower than the error that would result from the prediction of no change.

A second way to analyze the link between predicted and actual changes in shares is to perform a regression analysis similar to that in table 2, with figures written as changes in shares rather than as log changes. Let $\Delta \ell_i = \ell_i - \ell_i$ (-1), the change in the share of employment in occupation i from 1960 to 1970; $\Delta d_i = d_i - \ell_i$ (-1), the predicted change in the share of employment in occupation i from the requirements model; ℓ_i (-1) = the share of employment in occupation i in 1960. Regression of $\Delta \ell_i$ on Δd_i and ℓ_i (-1) for the entire 254 occupation sample yielded the following equation:

(18)
$$\Delta l_i = .035 + .85 \Delta d_i - .09 l_i$$
 () $R^2 = .610$ (.009) (.06) (.01) SEE = .134

This equation shows that Δd_i does an extremely good job of explaining Δl_i , both in terms of the R^2 and the standard error, which is only a bit more than one-tenth of a percentage point. Addition of the predicted change in the share of workers supplying services to occupation i based on equation (14) gave an insignificant negative coefficient to the change in supply variable, indicating that with the change in share functional form demand effects are the driving force of employment changes.

The Demand Equation

Direct estimates of the augmented requirements equation are given in table 4 using both unweighted and weighted regressions. Lines 1-3 record ordinary least squares estimates of the effect of shifts in demand and of changes in wages on employment in the entire sample and in the restricted sample which excludes all not elsewhere classified groups.

Lines 3-6 gives instrumental variable estimates, in part to correct for simultaneity in the determination of changes in incomes and in part for likely measurement in the wage change variable. The OLS calculations provide a base for evaluating the IV results and may, because Census income figures relate to the previous year, be sufficiently free of simultaneous bias to provide a useful estimate of the elasticity of demand itself. The instruments (in addition to those in the equation) are listed in the table notes. Both the OLS and IV regressions accord a significant and sizeable negative coefficient to the change in income, which supports the basic notion that the fixed coefficient analysis can be improved upon by taking account of movements along the demand curve. In the OLS calculations, the elasticity estimates range from -.42 (line 2. full sample, weighted) to -.61 (line 3, restricted sample, weighted) The demand shift term obtains a coefficient close to unity in lines 1 and 2, suggesting that it does reflect horizontal shifts, but a smaller coefficient in line 3. In the IV calculations, the unweighted regressions in line 4 essentially replicate the OLS results in line 1. The weighted regressions in lines 4 and 5, however, differ noticeably from the comparable OLS regressions: the coefficient on W rises, as expected, while that on D declines. The estimated elasticity of demand goes from - .42 to -.81 in the full sample and from -.61 to -.91 in the restricted sample. The drop in the coefficient on D is anomalous for it means that D is negatively rather than positively correlated with W in the instrumental equation, a result which might be attributed to the greater impact of measurement errors than of simultaneous errors in the data and/or to the possible positive correlation between unmeasured shifts in supply and the measured shift in demand. 19 Even with this problem, however, the results show that the augmented demand model offers a better representation of demand than the standard fixed coefficient model.

Coefficients and Standard Errors

.29

.45

.49

.225

.215

.245

Table 4 Estimates of the Augmented Requirements Demand Equation
3 Digit Occupations, 1960-1970¹

 R^2 sample² estimating SEE weighted constant technique regression -.57 .29 .337 .93 .30 1 0LS no (.16)(.10).91 -.42 .46 .214 .18 2 OLS yes (.08)(.13).242 .83 -.61 .50 .35 3 C OLS yes (.09)(.14)

.29

.25

.52

no

yes

yes

.93

(.10)

.88

(.10)

.72

(.11)

-.57

(.45)

-.55

(.25)

-.91

(.23)

5

6

C

Source: Change in employment; shift in supply/shift in demand, change in incomes see table 1; mean years of education, calculated from U.S. Census of Population 1960 Occupational Characteristics, table 9; percent female, calculated from U.S. Census of Population 1960, Occupational Characteristics, table 2; income of education groups in 1960 from U.S. Census of Population 1960 Educational Attainment, tables 6, 7; income of education group in 1970 from U.S. Census of Population 1970, Educational Attainment, tables 7, 8.

 $^{^{}m l}$ The dependent variable is the log change in employment. Numbers in parentheses are standard errors.

Samples, see table 3, footnote 3.

³The instruments were: the shift in supply (\hat{s}_i) , mean years of education in occupation in 1960, percent female, income in 1960, changes in the income of workers with the same education and sex profile as those in the occupation. To obtain this figure for 1960 and 1970 I calculated $\sum_i W_i$ where Y_i = proportion of workers in occupation i in a specified education and sex group in 1960 and W_i = income of persons in that education and sex group in 1970 and then took log changes between the values for 1970 and 1960.

Further Analysis

The analysis of interactions in equation (10) of section I raised the possibility that the effects of D and W on employment would be interrelated. To test for the possibility of such an interaction, I added the multiplicand of D and W to the demand equations of table 4. When the elasticities of demand for an occupation are the same among industries, DW is the appropriate interaction term and will obtain a negative coefficient equal in magnitude to the product of the coefficient on D and the coefficient on W. In all of the regressions, DW entered with the expected negative sign, obtaining an especially significant effect in the OLS weighted regressions in the complete sample:

(19)
$$\dot{L} = .13 - .37\dot{w} + 1.38D - .85\dot{D}\dot{w}$$
 $R^2 = .462$ (.13) (.28) (.49) SEE = .213

where numbers in parentheses are standard errors. The negative interaction shows that, as expected, changes in wages have a greater effect on employment when demand is shifting upward. Moreover, the coefficient on DW is only moderately different from the product of those on W and D. This is consistent with the finite expansion term in equation (10), given similar within-industry elasticities of demand for occupations. As the interactions could be due to other factors which might lead to interactive functional forms, no strong conclusions should be drawn from the results, especially in light of the measurement error problems. What (19) does suggest is the value of more detailed analysis of interaction effects in analysis of decadal changes, due to the finite change formulae.

IV The Differential Variation of Employment and Wage Changes

The final issue to consider is the potential causes of the strikingly greater variation of changes in employment than of changes in incomes presented

in table 1. On the basis of the estimates of the augmented requirements model, which of the three hypotheses outlined earlier—shifts in supply along a stable highly elastic demand curve; correlated shifts in supply and demand; or shifts in demand along an elastic supply shedule (the dynamic demand/elastic supply hypothesis)—appear best able to account for the observed pattern?

While not definitive, the estimated equations tend to favor the dynamic demand/elastic supply hypothesis and to rule out an explanation based on shifts in supply along a highly elastic demand curve. First, as noted, the reduced form calculations in table 3 yielded coefficients on the demand shift variable considerably larger than the coefficients on the supply shift variables. According to equation (12) this implies that the supply of labor to occupations is more elastic than is the demand for labor. Second, the demand elasticities in table 4, though non-negligible, are much below the magnitudes needed to sustain the argument that demand for detailed skills is highly elastic.

Another way to judge the hypotheses is to use the estimated coefficients on D and S and the variation of the variables in the data to calculate standardized Beta weights for D and S. These weights measure the effect of a standard deviation change in D and S on a standard deviation change in employment.

If demand shifts are the predominant force altering employment among occupations, the Beta weight for D should exceed that for S. Using the regression coefficients of table 3 to obtain estimated coefficients and the relevant standard deviations in D and in S in the samples yields the following Beta weights: for line 1 of table 4, 1.32 for D versus ,86 for S; for line 2 of table 3, 1.42 for D versus .21 for S; for lines 3 and 4, .82 for D versus .48 for S. Thus, in each case, the Beta weights for the demand shift factor exceed the Beta weights for the supply shift factor, implying that demand factors dominate the observed patterns of change. This does not mean, however, that supply

shifts were unimportant nor that correlated shifts in demand and supply may not have contributed to the observed pattern. In all of the calculations the Beta weight on S was non-negligible. The shift terms in the two schedules were correlated at .43. Because the supply shift term treats the educational upgrading of the work force and increased labor participation of women as exogenous, however, it probably overstates the "true" exogenous shifts in supply and probably overstates the correlation between supply and demand shifts in the period. To some extent at least, the upgrading of the education of the work force and increased participation of women are likely to represent endogenous behavior. These considerations strengthen the case for the dynamic demand/elastic supply interpretation.

The plausibility of the dynamic demand/elastic supply hypothesis can be probed further by examining one particular component of supply, the occupational mobility of the work force, on which the Bureau of Labor Statistics has recently provided considerable information. Mobility of of workers from one occupation to another is, according to the Bureau of Labor Statistics' study, a major element in changes in employment by occupation: from 1965 to 1970 the B.L.S. estimates that nearly one-third of workers reporting in the 1970 Census of Population transferred from one three-digit occupation to another while less than one-half remained in the same occupation. 21 If this substantial volume of occupational movement is related to economic incentives, an important component of the dynamic demand/elastic hypothesis will be established. If the movement is unrelated to economic incentives, it will be difficult to maintain the hypothesis that the large change in employment relative to the change in incomes is, at least in part, the resultant of shifts in demand along reasonably elastic supply curves.

To test the responsiveness of occupational mobility to market conditions,

I "bridged" the B.L.S. estimates of the percentage of workers in each three digit

occupation transferring to a different occupation (SWITCH) or remaining in the same occupation (STAY) from 1965 to 1970 to be comparable to the 1960 occupational categories used in this study. two variables were then regressed on two indicators of economic incentives, the level of incomes in the occupation in 1960 and the change in income from 1960 to 1970; on the percentage of the occupation in 1960 who were women, on the hypothesis that women are less likely to be occupationally mobile than men; and on the percentage of workers aged 30 or below in 1960 and the percentage aged 45 or over in 1960, on the hypothesis that young workers are likely to be highly mobile across occupations and older workers likely to be less mobile. Persons aged 30 or below would be less than 35 years of age in 1965 while those 45 or over would be 50 years or older in 1965. Two functional forms were used in the analysis: a log-log equation in which the log of the relevant percentage was the dependent variable; and a logit regression in which the log odds ratio of the variable was dependent. In the former case, the coefficients on the log of income or on changes in log income represent the supply elasticities with respect to the given occupation's income versus income of all other occupations. the latter, the coefficients represent the logistic curve parameters of the effect of the variables. The coefficients must be multiplied by 1-P, where P is the mean proportion who switched or stayed, to obtain elasticities at the mean. Formally, the log odds equation is

(20)
$$\log P/1-P = \sum_{i} x_{i}$$

where P = percentage in the category

 β_i = coefficient of effect in logit form

 $X_{i} = explanatory variable$

and

(21)
$$dP/dX_i = P(1-P)\beta_i$$

Table 5: Estimates of the Effect of Income on Occupational Mobility Patterns $1965-1970^{1}$

line	dependent variable ²	constant	ů _i	W ₁ (60)	% under 30	% over 45	% female	R ²	SEE
1	log(SWITCH)	5.27	74 (.18)	25 (.05)	1.50 (.21)	.02 (.14)	40 (.06)	.52	.236
2	logit(SWITCH)	1.68	-1.01 (.23)	33 (.07)	2.00 (.27)	.01 (.18)	54 (.08)	.55	. 297
3	log(STAY)	1.47	.46 (.09)	.30 (.03)	72 (.10)	05 (.06)	.05 (.03)	.69	.127
4	logit(STAY)	-5.08	.88 (.18)	.63 (.05)	-1.34 (.21)	11 (.12)	.06 (.07)	.68	.263

Source: Occupational Mobility data from D. Sommers and A. Eck, "Occupational Mobility in the American Labor Force," Monthly Labor Review Jan. 1977, table 5. Age distributions from U.S. Bureau of the Census, Occupational Characteristics 1960, table 4, calculated by taking the ratio of male and female workers in the given age group to all male and female workers in the occupation. Other data as described in tables 3 and 4.

Numbers in parentheses are standard errors of estimate. The variables are defined as: SWITCH = % who transferred from the occupation, 1965-1970; STAY = % who remain in the occupation, 1965-1970; \dot{W}_1 = log change in income, 1960-1970; \dot{W}_1 (60) = log of income in 1960; % under 30 = % 30 years old or younger in 1960; % over 45 = % 45 years old or older in 1960; % female = % female in 1960.

logit = log odds ratio of the variable.

The analysis treats both the percentage switching and the percentage staying in occupations because the two variables are <u>not</u> complements. They differ by the percentage of workers who left the labor force or died. Because the B.L.S. reported no figures in cases where the standard error on the proportion exceeded 10 percent, moreover, the two variables are available for different numbers of occupations. In the samples under study there were 184 occupations with data for STAY and 158 occupations with data for SWITCH.

The regression results are summarized in table 5. What stands out in the table is the substantial and significant effect of the income variables on occupational mobility, with changes in income and levels of income reducing the proportion of workers who transfer out of occupations and increasing the proportion of workers who remain in the same occupation over time. In line 1 the percentage of switchers has an elasticity with respect to changes in incomes of 0.7 and an elasticity with respect to the level of income of .3. The logit regressions in line 2 yield different coefficients but imply similar elasticities (-1.01 and -0.33) at the mean value of SWITCH (.24). In lines 3 and 4 the proportion who remain in an occupation has a somewhat smaller but still marked elasticity, again of comparable magnitude at the mean percentage (.55) in the two forms. In all the calculations, the higher the percentage of females, the less likely is occupational mobility, while the higher the percentage of workers less than 30, the greater is mobility.

Since responsiveness to market conditions is likely to be greater among new entrants (who have not yet invested heavily in occupations) the estimates in the table provide lower bounds on the extent of flexibility of the work force. While more detailed analysis of occupational mobility patterns, which takes into account incomes in fields to which persons move as well as incomes in their 1965 occupations, is surely needed, the overall impression is that occupational mobility patterns are sufficiently sizeable and responsive to be consistent with the dynamic demand/elastic

supply hypothesis.

IV Conclusion

This study has examined the applicability of the fixed coefficient manpower requirements model to changes in employment in detailed occupations in the U.S. from 1960 to 1970 and explored the possibility of improving the model by taking account of factor substitution at an aggregate occupational level. The principal findings can be summarized briefly:

- 1) The fixed coefficient manpower requirements model can be treated as a model of <u>shifts</u> in demand for labor in the context of a more general augmented requirements demand model, in which movements along demand schedules due to changes in incomes as well as shifts in demand are treated as determinants of changes in employment.
- 2) By itself the fixed coefficient shift term provides a good fix on changes in employment, accounting for about 60% of changes in the share of the work force in occupations and 44% of changes in the log of employment, weighted by the size of occupations.
- 3) Allowing for movements along the demand curves induced by income variation tends to improve the analysis noticeably. Direct estimates of the elasticity of demand for occupational skills clearly rejects the hypothesis of fixed or economically unresponsive manpower coefficients. Estimated (average) elasticities of demand with respect to incomes are on the order of -.4 to -.9. In addition, there is indication of interactions between change in income and shifts in demand, which result from the finite change formulae.
- 4) The variation in changes in employment among occupations exceeds the variation in changes in incomes. There are three possible explanations of this phenomenon: movements of highly variable supply schedules along elastic demand curves; correlated shifts in supply and demand; or movements

of a highly variable demand schedule along elastic supply schedules, which we have termed the dynamic demand/elastic supply hypothesis. The evidence suggests that the dynamic demand/elastic supply hypothesis explains at least part of the observed difference in variation. Shifts in demand for detailed occupational skills appear to have contributed more to changes in employment than shifts in supply. The demand for labor in three digit occupations appears to have a moderate elasticity. High significant occupational mobility seems to make the supply of labor relatively elastic to three digit occupations.

5) Since even the best fitting equations leave considerable standard errors of estimate, the fixed coefficient model must be used cautiously in projections and policy analysis.

Because of the great difficulties with changing Census definitions, some of these results may be altered given better data. The findings are, however, generally similar to those obtained in a comparable analysis of the 1950-1960 period, when occupational definitions did not undergo great change, and given the usual effect of measurement errors are, if anything, likely to be strengthened by better data sets. Overall, the evidence supports the use of the fixed coefficient model in demand analysis but indicates that the model can be improved by taking account of factor substitution, even in a highly aggregate manner. Further work to bridge the traditional dichotomy between the fixed coefficient and factor methodologies should improve our understanding of and ability to forecast changes in the distribution of workers around detailed occupations.

Footnotes

- Employment Patterns for 1960 and 1975 (Bulletin 1599). O.E.C.D.

 Mediterranean Regional Project Country Reports, Greece, Turkey, Italy.

 For a detailed discussion of the O.E.C.D. model see J. Tinbergen and

 H. Bos, Econometric Models of Education, Some Applications (Paris:

 O.E.C.D., 1965). U.S. National Science Foundation, Long Range Demand for Scientific and Technical Personnel.
- R. Freeman and D. Breneman, <u>Forecasting the Ph.D. Labor Market</u> (National Board of Graduate Education, Technical Report No. 2, April 1974).
 M. Blaug, "An Economic Interpretation of the Private Demand for Education," Economica, May 1966.
- 3 In this paper I use words of projection and forecast interchangeably.
- In a general production function, which permits different elasticities of substitution among different labor inputs, the number of Allen elasticities is $(\frac{i}{2})$ where i = number of inputs. The technology is such that with available data points, it is virtually impossible to estimate factor demand relations for more than 5 inputs (10 elasticities).
- Since one form of economy wide substitution is to shift employment among sectors with different skill mixes, the methodology does not, in fact, necessarily involve more rigidity than standard demand models which focus on factor prices. A very detailed fixed coefficient model in which industry scale depended on wages through the effect of wages on cost and cost on price could predict greater changes in employment than would occur via factor substitution, industry mix fixed. However, existing models do not take industry scale as dependent on wages.

 6 A small interaction effect is likely given actual changes in the data. With changes in wages of say 20% (relative to the average change) and changes in input coefficients of, say, a similar magnitude, the interaction term would be just .04. The actual standard deviations in \dot{N}_{i} and $\dot{\dot{W}}_{i}$ shown in table 1 suggest that unless η_{ij} is very large, or N_{ij} and $\dot{\dot{W}}_{i}$ are extraordinarily correlated, interactions should have only a modest effect on results.

⁷Essentially the interaction term is being equated with the residual in equation (5).

 8 Note, however, that η_{i} is on average a "reduced form" elasticity rather than the more fundamental elasticity of demand for the occupation with an industry.

⁹An alternative way of going from equation (5) to equation (5') is to assume that the elasticity of demand for occupations varies randomly around a mean in the context of a random coefficients model. In this case let $\eta_i = \eta + \varepsilon_i$ where ε_i has mean 0, variance σ^2 and where $E(\mathring{W}_i = \varepsilon_i) = E(\varepsilon_i\mathring{D}_i) = 0$. The resultant equation to be estimated becomes

$$\dot{L}_{i} = \dot{D}_{i} - \eta \dot{W}_{i} + \dot{U}_{i} + \Sigma_{i} \dot{W}_{i}$$

Least squares provides a consistent estimate of η since $E(\Sigma_1 W_1) = 0$ but will not be efficient. No effort was made in this paper to use generalized least squares to obtain more efficient estimates.

10 For some purposes it may be fruitful to decembese shifts in the schedule into three components: shifts due to the normal inflow of workers into the occupation; shifts due to special inflows resulting from changes in the demographic mix of the work force; shifts due to abnormally high wages or rates of return to investing in the field.

- This equation is essentially a stock adjustment equation in which $\dot{S}_i + \dot{\phi}\dot{W}_i$ represents new "investment" and $-\lambda L_i(-1)$ is the depreciation of the stock. The stock of labor reaches an equilibrium, with fixed wages, when $\dot{S}_i = \lambda L_i(-1)$, where \dot{S}_i is viewed as the normal inflow of workers into the occupation.
- ¹²The solution to the model with supply equation (11') is similar. It includes the lagged number of workers in addition to \dot{D}_i and \dot{S}_i .
- The Bureau of Labor Statistics modified the Census data in several ways.

 First they dropped "allocated" and "not specified" groups, distributing those workers proportionately by industry or occupation. Second, they adjusted the Census data for seasonality (due to the fact that the Census is conducted in the spring), by altering totals to be on a comparable basis to the Employment and Earnings annual averages. Third, certain cells were adjusted so that row and column sums added up.
- The following categories (with 1960 Census occupation codes in parentheses) were deleted from all computations as not representing the type of occupations of concern to a requirements forecast: all apprentices (601-621); unpaid family farm workers (903); bootblacks (820); newsboys (390); and student nurses (151). In addition, two not elsewhere classified (n.e.c.) categories were deleted, entertainers n.e.c. (101); and professional, technical n.e.c. (195) as being clear outliers due to bridging problems.

The following categories were grouped: registered nurses (150) and practical nurses (842); farm managers (222) and farm owners and tenants (200); religious workers (170) and clergymen (23); stenographers (345) and secretaries (342) as representing similar functional categories, differentiation among whom is not possible in the fixed coefficient model. Telegraph operators (351), which were included in the B.C.S. tape but for whom no figures are published in the Census, were grouped with messenger and office boys (324)

The high elasticity interpretation has been offered by S. Bowles,

Planning Educational Systems for Economic Growth (Cambridge, Mass, 1969)

and supported by G. Psacharopoulos and K. Hinchliffe "Further Evidence on the Elasticity of Substitution Among Different Types of Educated Labor" Journal of Political Economy 80 (July/Aug. 1972); pp. 786-92 and C. R. S. Doughtery, "Estimates of Labor Aggregation Functions" JPE 80 (Nov./Dec. 1972): 1101-19.

More recent work, however, tends to find elasticities that reject this hypothesis and explanation. See J. Tinbergen "Substitution of Graduate By Other Laborers" Kyklos 27 (1974) 1-18 and P. R. Layard and P. Fallon, "Capital-Skill Complementarity, Income Distribution, and Output Accounting" JPE (Vol. 83, No. 2, April 1975) pp. 279-302.

- With these parameter values, the right hand side is roughly $\left[W^2 + (1-w)^2 \right] \left(.2 \right)^2 + 2 \left(W \right) \left(1-W \right) \left(.5 \right) \left(.2 \right)^2.$ When W = 1/2, this becomes $1/2 \left(.04 \right) + 1.4 \left(.04 \right) = .03$ whose square root is .17.
- With this number of observations the sign test that over half of the cases have been correctly specified can be approximated by the statistic $Z = (X 1/2 \text{ N}) (1/2\sqrt{N})$, where Z is N(0, 1.2 \sqrt{N}) and N = number of observations; X = number of correct cases. The fixed coefficient predictions yield a Z of 6.27, significant at all standard levels. See S. Siegal, Nonparametric Statistics for the Behavioral Sciences (McGraw-Hill, 1956) pp. 68-78.
- ¹⁸Formally, the assumption which justifies the weighted regression is that the residual in the equation has mean 0 but variance $\sigma_{\bf i}^2 = \sigma^2/L_{\bf i}(-1)$ where $L_{\bf i}(-1)$ is employment in the base year. With this variance, the appropriate weighted least squares model calls for weighting all observations by $\sqrt{L_{\bf i}}$. An alternative

possible model is to let $\sigma_1^2 = \sigma_1^2 + \sigma_2^2/L_i(-1)$ which makes the variance depend on one component common to all occupations (σ_1^2) and one that depends on the size of the occupation $[\sigma_2^2/L_i(-1)]$. A model of this type is intermediate between the unweighted and weighted regressions in the text.

- 19 If supply shifts are imperfectly measured and correlated with demand shifts, the coefficient on D in the instrument equation would be negative. Since the supply shift term assumes that this increased educational attainment of workers and greater share of female workers is exogenous, there is good reason to believe that it is prone to measurement error. Problems with the supply shift term may also cause the instrumental variable estimate of the elasticity of demand to be biased downward.
- Specifically, when \hat{b} is the regression coefficient of y on x, then the Beta weight is $\hat{b}(\sigma_y/\sigma_x)$ where σ_y and σ_x are the standard deviations of the dependent and independent variables, respectively.
- D. Summers and A. Eck, "Occupational Mobility in the American Labor Force,"

 Monthly Labor Review, Jan. 1977, pp. 3-26.
- Attempts to estimate a supply equation based on the changes in employment figures used in the demand equations of this study yielded weak or perverse results on changes in incomes, presumably due to identification problems and the mixture of age, education, and sex groups with very different elasticities of response. This suggests the need to decompose carefully the various components of supply: the supply of new entrants; the occupational mobility of existing workers; and to distinguish between various demographic groups of workers and, where possible, various occupations. as well-
- 23 R. Freeman, "Manpower Requirements and Substitution Analysis of Labor Skills: A Synthesis," in Reserch in Labor Economics (ed. R. Ehrenberg, Johnson Publishers, 1977).

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