

An Endogenous Segmentation Mode Choice Model with an Application to Intercity Travel

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Abstract

This paper uses an endogenous segmentation approach to model mode choice. This approach jointly determines the number of market segments in the travel population, assigns individuals probabilistically to each segment, and develops a distinct mode choice model for each segment group. The author proposes a stable and effective hybrid estimation approach for the endogenous segmentation model that combines an Expectation-Maximization (EM) algorithm with standard likelihood maximization routines. If access to general maximum-likelihood software is not available, the multinomial-logit based EM algorithm can be used in isolation. The endogenous segmentation model and other commonly used models in the travel demand field to capture systematic heterogeneity are estimated using a Canadian intercity mode choice dataset. The results show that the endogenous segmentation model fits the data best and provides intuitively more reasonable results compared to the other approaches.

Introduction

The estimation of travel mode choice models is an important component of urban and intercity travel demand analysis and has received substantial attention in the transportation literature (see Ben-Akiva and Lerman, 1985). The most widely used model for urban as well as intercity mode choice is the multinomial logit model (MNL). The MNL model is derived from random utility maximizing behavior at the disaggregate individual level. Therefore, ideally, we should estimate the logit model at the individual level and obtain individual-specific parameters for the intrinsic mode biases and for the mode level-of-service attributes. However, the data used for mode choice estimation is usually cross-sectional; that is, there is only one observation per individual. This precludes estimation of the logit parameters at the individual level and constrains the modeler to pool the data across individuals (even in panel data comprising repeated choices from the same individual, the number of observations per individual is rarely sufficient for consistent and efficient estimation of individual-specific parameters). In such pooled estimations, it is important to accommodate differences in intrinsic mode biases (preference heterogeneity) and differences in responsiveness to level-of-service attributes (response heterogeneity) across individuals. In particular, imposing an assumption of preference and response homogeneity in the population is rather strong and is untenable in most cases (Hensher, 1981). Further, if the assumption of homogeneity is imposed when, in fact, there is heterogeneity, the result is biased and inconsistent parameter and choice probability estimates (see Chamberlain, 1980).

An issue of interest then is: how can preference and response heterogeneity be incorporated into the multinomial logit model when studying mode choice behavior from cross-sectional data?

One approach is to estimate a model with (pure) random coefficients where the logit mode bias and level-of-service parameters are assumed to be randomly distributed in the population. This approach ignores any systematic variations in preferences and response across individuals. As such, it cannot be considered as a substitute for careful identification of systematic variations in the population. The random coefficients cannot even be considered as an alternative approach (*i.e.*, alternative to accommodating systematic effects) to account for heterogeneity in choice models; it can only be considered as a potential “add-on” to a model that has attributed as much heterogeneity to systematic variations as possible (Horowitz, 1991 makes a similar point in the context of the use of multinomial probit models in travel demand

modeling). Typical applications of the random-coefficients specification have used a base systematic model with some allowance for systematic preference heterogeneity (by including individual-related variables directly in the utility function), but with little (or no) allowance for systematic response heterogeneity.¹

It is clear from above that accommodating systematic preference and response heterogeneity in multinomial logit models must be a critical focus in mode choice modeling. Systematic heterogeneity may be accommodated in one of two broad ways: exogenous market segmentation or endogenous market segmentation. We discuss each of these two approaches in the subsequent two paragraphs (as indicated earlier, a random coefficients specification can be super-imposed over the systematic model in each of these approaches; however, in the rest of this paper, we focus only on the systematic specifications).

The exogenous market segmentation approach to capturing systematic heterogeneity assumes the existence of a fixed, finite number of mutually-exclusive market segments (each individual can belong to one and only one segment). The segmentation is based on key socio-demographic variables (sex, income, *etc.*) and possibly trip characteristics (whether an individual travels alone, distance of trip, *etc.*). Within each segment, all individuals are assumed to have *identical* preferences and identical sensitivities to level-of-service variables (*i.e.*, the same utility function).² The total number of segments is a function of the number of segmentation variables and the number of segments defined for each segmentation variable. Ideally, the analyst would consider all socio-demographic and trip-related variables available in the data for segmentation (we will refer to such a segmentation scheme as full-dimensional exogenous market segmentation). However, a practical problem with the full-dimensional exogenous segmentation scheme is that the number of segments grows very fast with the number of segmentation variables, creating both interpretational and estimation problems due to inadequate observations in each segment. To overcome this limitation, researchers have used one of two methods. The

¹ The reader is referred to a report by Electric Power Research Institute, 1977 for an application of the random-coefficients logit (RCL) formulation using cross-sectional data; Gonul and Srinivasan (1993) applied the RCL formulation to estimate brand choice models from panel data. The random-coefficients formulation has also been used in combination with the probit model of choice (Hausman and Wise, 1978; Fischer and Nagin, 1981; Horowitz, 1993).

² To be precise, all individuals in a segment are assumed to have *identical* preference *patterns* and sensitivity to level-of-service *patterns*, not necessarily identical preferences and level-of-service sensitivity. This is because continuous variables such as income and distance can appear in the segment-specific utility functions even if they are used as segmentation variables. For example, within each segment, preference may be a function of income and level-of-service sensitivity may be a function of trip distance.

first method, which we label as the Refined Utility Function Specification method, accommodates preference heterogeneity by introducing key segmentation variables directly into the utility function as alternative-specific variables and recognizes response heterogeneity by interacting the level-of-service variables with the segmentation variables (we will refer to socio-demographic and trip characteristics that are likely to impact mode preferences and level of service sensitivity as segmentation variables). The refined utility function specification method is a restrictive version of the full-dimensional exogenous market segmentation approach where only lower-order interaction effects of the segmentation variables on preference and response are allowed. The second method, which we label the Limited-Dimensional Exogenous Market Segmentation method, overcomes the practical problem of the full-segmentation approach by using only a subset of the demographic and trip variables (typically one or two) for segmentation. The advantage of the two methods just discussed is that they are practical (the parameters can be efficiently estimated with data sizes generally available for mode choice analysis) and are easy to implement (requires only the MNL software). The disadvantage is that their practicality comes at the expense of suppressing potentially higher-order interaction effects of the segmentation variables on preference and response to level-of-service measures. In addition, an intrinsic problem with all exogenous market segmentation methods is that the threshold values of the continuous segmentation variables (for example, income) which define segments have to be established in a rather *ad hoc* fashion.

The endogenous market segmentation approach, on the other hand, attempts to accommodate systematic heterogeneity in a practical manner not by suppressing higher-order interaction effects of segmentation variables (on preference and response to level-of-service measures), but by reducing the dimensionality of the segment-space. Each segment, however, is allowed to be characterized by a large number of segmentation variables. The appropriate number of segments representing the reduced segment-space is determined statistically by successively adding an additional segment till a point is reached where an additional segment does not result in a significant improvement in fit. Individuals are assigned to segments in a probabilistic fashion based on the segmentation variables. The approach jointly determines the number of segments, the assignment of individuals to segments, and segment-specific choice model parameters. Since this approach identifies segments without requiring a multi-way partition of data as in the full-dimensional exogenous market segmentation method, it allows the

use of many segmentation variables in practice and, therefore, facilitates incorporation of the full order of interaction effects of the segmentation variables on preference and level-of-service sensitivity. The method also obviates the need to (arbitrarily) establish the threshold values defining segments for continuous segmentation variables. As we indicate later, the approach also does not exhibit the individual-level independence from irrelevant alternatives (IIA) property of the exogenous segmentation approach. A potential disadvantage is that the model cannot be estimated directly using the MNL software (we overcome this issue in the current paper).

The model formulation in this paper falls under the endogenous segmentation approach to accommodating systematic heterogeneity. We use a multinomial logit formulation for modeling both segment membership as well as mode choice. To the author's knowledge, no previous market segmentation analysis in the travel demand field has adopted this approach. But the approach has been applied earlier in the marketing field. Kamakura and Russell (1989) originally proposed such a method to model brand choice. Their model assumed that the segment membership probabilities were invariant across households (*i.e.*, the only variables in their multinomial logit model for segment membership were segment-specific constants). Such a model is of limited value since the objective of segmentation schemes is to associate heterogeneity with observable individual characteristics. Gupta and Chintagunta (1994) extended the work of Kamakura and Russell by including segmentation variables in the segment membership MNL model (Dayton and Macready, 1988 also propose an endogenous segmentation model in which segment membership is functionally related to individual-related variables; however, the segment membership and choice probabilities do not take a MNL structure).

The model in this paper takes the same form as the model of Gupta and Chintagunta. However, the paper proposes and applies an efficient, stable, hybrid estimation procedure that combines an Expectation-Maximization (EM) formulation (which exploits the special structure of the model) with a traditional quasi-Newton maximization algorithm (both Kamakura and Russell, 1989 and Gupta and Chintagunta, 1994 use a direct maximum likelihood method, which we found to be rather unstable and to require more time than the method proposed here). The EM formulation requires only the standard MNL software and can be used in isolation to estimate the endogenous segmentation model. Hence, it should be of interest to researchers and practitioners who do not have access to, or who are not in a position to invest time and effort in learning to

use, general-purpose maximum likelihood software. The endogenous segmentation model is applied in a travel demand context to study intercity business mode choice behavior in the Toronto-Montreal corridor of Canada and its empirical performance is assessed relative to alternative methods to account for systematic preference and response heterogeneity.

The rest of this paper is structured as follows. The next section presents the structure for the mode choice model with endogenous market segmentation. Section 2 outlines the estimation procedure. Section 3 discusses the empirical results obtained from applying the model to intercity mode choice modeling. Section 4 presents the choice elasticities and examines the policy implications of the results. The final section provides a summary of the research findings.

1. Model Structure

The mode choice model with endogenous segmentation rests on the assumption that there are S relatively homogenous segments in the inter-city travel market (S is to be determined); within each segment, the pattern of intrinsic mode preferences and the sensitivity to level of service measures are identical across individuals. However, there are differences in intrinsic preference patterns and level-of-service sensitivity among the segments. Thus, there is a distinct mode choice model for each segment s ($s = 1, 2, 3, \dots, S$).

We assume a random utility framework as the basis for individuals' choice of mode. We also assume that the random components in the mode utilities have a type I extreme value distribution and are independent and identically distributed. Then, the probability that an individual q chooses mode i from the set C_q of available alternatives, conditional on the individual belonging to segment s , takes the familiar multinomial logit form (McFadden, 1973):

$$P_q(i) | s = \frac{e^{\beta_s' x_{qi}}}{\sum_{j \in C_q} e^{\beta_s' x_{qj}}}, \quad (1)$$

where x_{qi} is a vector comprising level-of-service and alternative-specific variables associated with alternative i and individual q , and β_s is a parameter vector to be estimated.

The probability that individual q belongs to segment s is next written as a function of a vector z_q of socio-demographic and trip-related variables associated with the individual (z_q includes a constant). Using a multinomial logit formulation, this probability can be expressed as:

$$P_{qs} = \frac{e^{\gamma'_s z_q}}{\sum_l e^{\gamma'_l z_q}}. \quad (2)$$

The unconditional (on segment membership) probability of individual q choosing mode i from the set C_q of available alternatives can be written from equations (1) and (2) as:

$$P_q(i) = \sum_{s=1}^S P_{qs} \times [P_q(i) | s]. \quad (3)$$

The assignment of individuals to segments based on socio-demographic and trip characteristics is a critical part of market segmentation, as discussed in section 1. In the current model, this assignment is probabilistic and is based on equation (2) after replacing the γ_s 's with their estimated counterparts. The size of each segment (in terms of share), R_s , may be obtained as:

$$R_s = \frac{\sum_q P_{qs}}{Q} \quad (4)$$

where Q is the total number of individuals in the estimation sample.

The socio-demographic and trip-related attributes that characterize each segment can be inferred from the signs of the coefficients in equation (2). A more intuitive way is to estimate the mean of the attributes in each segment as follows:

$$\bar{z}_s = \frac{\sum_q P_{qs} z_q}{\sum_q P_{qs}}. \quad (5)$$

The model can be used to predict the choice of mode at the individual level, segment level, or the market level. The individual-level choice probabilities can be obtained from equation (3). The segment-level mode choice shares can be obtained as:

$$W_s(i) = \frac{\sum_q P_{qs} \times [P_q(i) | s]}{\sum_q P_{qs}}. \quad (6)$$

Finally, the market-level mode choice shares may be computed as:

$$W(i) = \frac{\sum_s \sum_q P_{qs} \times [P_q(i) | s]}{Q} = \sum_s R_s \times W_s(i). \quad (7)$$

The elasticities of the effect of level-of-service attributes can also be computed at the individual-level, the segment-level, or the market-level. These can be derived in a straightforward fashion from the expressions above and are not presented here due to space considerations. An examination of the individual-level cross-elasticities from the model will show that the endogenous segmentation model is not saddled with the IIA property of the MNL model.

2. Model Estimation

The parameters to be estimated in the mode choice model with endogenous market segmentation are the parameter vectors β_s and γ_s for each s , and the number of segments S . The log likelihood function to be maximized for given S can be written as (we discuss the procedure employed to determine S in section 2.2):

$$L = \sum_{q=1}^Q \log \left\{ \sum_{s=1}^S \left(P_{qs} \times \prod_{i \in C_q} [P_q(i) | s]^{\delta_{qi}} \right) \right\}, \quad (8)$$

Where C_q is the choice set of alternatives for the q th individual and δ_{qi} is defined as follows:

$$\delta_{qi} = \begin{cases} 1 & \text{if the } q\text{th individual chooses alternative } i \\ (q = 1, 2, \dots, Q; i \in C_q) \\ 0 & \text{otherwise,} \end{cases} \quad (9)$$

Equation (8) represents an unconditional likelihood of an observed choice sample and is characteristic of finite probability mixture models. It has been noted earlier (see McLachlan and Basford, 1988 and Redner and Walker, 1984) that maximization of the likelihood function using the usual Newton or quasi-Newton (secant) routines in such mixture models can be computationally unstable (we document our own experience of this unstable behavior in section 3.4). A critical issue in such cases is to start the maximum likelihood iterations with good start parameter estimates. To obtain good start values, we develop a two-stage iterative method which

belongs to the Expectation-Maximization (EM) family of algorithms (Dempster *et al.*, 1977). This family of algorithms has been suggested earlier as a natural candidate for estimation in the general class of finite-mixture models since it is stable and tends to increase the log-likelihood function more than usual quadratic maximization routines in areas of the parameter space distant from the likelihood maximum (Ruud, 1991). The specific EM method is discussed below.

2.1 EM Method for Start Values

Consider the likelihood function in equation (8) and re-write it as:

$$\ln L = \sum_{q=1}^Q \log \left\{ \sum_{s=1}^S P_{qs} L_{qs} \right\} \quad (10)$$

where

$$L_{qs} = \prod_{i \in C_q} [P_q(i) | s]^{\delta_{qi}} .$$

The value L_{qs} is the choice likelihood for individual q conditional on the individual belonging to segment s . Next, note that the expected value of membership in segment s for individual q conditional on socio-demographic/trip characteristics and on the observed mode choice of the individual (*i.e.*, the posterior segment membership probability \tilde{P}_{qs}) can be obtained by revising the expected value of segment membership conditional only on the individual's socio-demographic/trip characteristics (*i.e.*, the prior segment membership probability P_{qs}) in a Bayesian fashion as:

$$\tilde{P}_{qs} = \frac{P_{qs} L_{qs}}{\sum_{s'} P_{qs'} L_{qs'}} . \quad (11)$$

The necessary first-order conditions for maximizing the likelihood function can be written from equation (10) and (11) as:

$$\frac{\partial \mathcal{L}}{\partial \beta_s} = \sum_q \left(\frac{P_{qs}}{\sum_{s'} P_{qs'} L_{qs'}} \right) \cdot \frac{\partial L_{qs}}{\partial \beta_s} = \sum_q \left(\frac{\tilde{P}_{qs}}{L_{qs}} \right) \cdot \frac{\partial L_{qs}}{\partial \beta_s} = \sum_q \tilde{P}_{qs} \cdot \frac{\partial \log L_{qs}}{\partial \beta_s} = 0 \text{ for } s = 1, 2, \dots, S \quad (12)$$

$$\frac{\partial \mathcal{L}}{\partial \gamma_s} = \sum_q \sum_{s'} \left(\frac{L'_{qs}}{\sum_{s'} P'_{qs} L'_{qs}} \right) \cdot \frac{\partial P_{qs'}}{\partial \gamma_s} = \sum_q \sum_{s'} \left(\frac{\tilde{P}'_{qs}}{P'_{qs}} \right) \cdot \frac{\partial P_{qs'}}{\partial \gamma_s} = \sum_q \cdot \frac{\partial \log L_q^*}{\partial \gamma_s} = 0, \quad (13)$$

where

$$L_q^* = \prod_s [P_{qs}]^{\tilde{P}_{qs}} \quad (14)$$

Equation (12) indicates that for given values of \tilde{P}_{qs} , the maximum likelihood estimate of each β_s vector ($s = 1, 2, \dots, S$) is obtained from a standard multinomial logit estimation for choice of mode with the corresponding \tilde{P}_{qs} values as weights (thus, there are S individual multinomial logit estimations). Equation (13) shows that for given values of \tilde{P}_{qs} , the maximum likelihood estimate of the γ_s vector is obtained from a single multinomial logit estimation for choice of segment with the posterior probabilities \tilde{P}_{qs} being used as the “dependent variable” instead of the “missing” segment choice data. A more efficient way to simultaneously obtain the estimates of β_s for each segment and estimates of γ_s (for given values of \tilde{P}_{qs}) is to construct a new log likelihood function as follows:

$$\begin{aligned} \langle^* &= \sum_q \left\{ \sum_s \tilde{P}_{qs} \log L_{qs} + \log L_q^* \right\} \\ &= \sum_q \sum_s \tilde{P}_{qs} \{ \log L_{qs} + \log P_{qs} \}. \end{aligned} \quad (15)$$

Since the log-likelihood function above is a combination of MNL log-likelihood functions, it is globally concave for given \tilde{P}_{qs} values.

Equations (11) and (15) lend themselves gainfully to the application of a EM algorithm. The E-step involves the computation of the *a posteriori* membership probabilities using equation (11) for some given initial guesses for the parameters. In the M-step, equation (15) is maximized with respect to parameters using the *a posteriori* membership probabilities computed in the E-step. Since the function in equation (15) is globally concave for given \tilde{P}_{qs} , a simple Newton-Raphson search will converge quickly. The two steps are then alternated. Dempster *et al.* (1977)

prove (under a very general setting) that, at each iteration, the EM algorithm provides monotone increasing values of the original log-likelihood function in equation (8).

In principle, the EM steps can be iterated until convergence (at convergence, the EM algorithm will return the maximum-likelihood estimates). But, as we show in section 3.4, the rate of convergence of the EM algorithm is slow in the neighborhood of the likelihood maximum (this has also been documented in other applications of the EM algorithm; see Redner and Walker, 1984 and Watson and Engle, 1983). So we stopped the EM algorithm prematurely after a few iterations and used the resulting parameter estimates as the start values for the direct maximization of the log-likelihood in equation (8). However, the reader will note that the EM algorithm proposed here can be used in isolation (without combining with the direct maximum likelihood procedure) to obtain the parameters of the endogenously segmented mode choice model if access to general maximum-likelihood software is not available (the EM method requires only the standard multinomial logit software).

2.2 Determination of Number of Segments

The estimation procedure discussed above is applicable for a given number of segments S . To identify the most appropriate value for S , we estimate the model for increasing values of S ($S = 2, 3, 4, \dots$) until a point is reached where an additional segment does not significantly improve model fit. The evaluation of model fit is based on the Bayesian Information Criterion (BIC):

$$\text{BIC} = -\ell + 0.5 \cdot R \cdot \ln(N). \quad (16)$$

The first term on the right side is the negative of the log-likelihood value at convergence; R is the number of parameters estimated and N is the number of observations (see Allenby, 1990). As the number of segments, S , increases, the BIC value keeps declining till a point is reached where an increase in S results in an increase in the BIC value. Estimation is terminated at this point and the number of segments corresponding to the lowest value of BIC is considered the appropriate number for S .³

³ An alternative procedure to determine the number of segments is to apply the Akaike Information Criterion (AIC) developed by Akaike (1974). This is the procedure adopted by Kamakura and Russell (1989). Gupta and Chintagunta (1994), on the other hand, use the Bayesian Information Criterion (BIC). An advantage of the BIC is that it takes into consideration the sample size used in the analysis. The AIC tends to unduly favor a model with more number of segments for large data samples; the BIC corrects this situation (see Allenby, 1990).

3. An Application to Intercity Mode Choice Modeling

3.1 Background

In this section, we report the empirical results obtained from applying the endogenous segmentation model and other alternative methods of accommodating systematic heterogeneity to an analysis of intercity travel mode choice behavior. The data used in the current empirical analysis was assembled by VIA Rail (the Canadian national rail carrier) in 1989 to develop travel demand models to forecast future intercity travel in the Toronto-Montreal corridor and to estimate shifts in mode split in response to a variety of potential rail service improvements (see KPMG Peat Marwick and Koppelman, 1990 for a detailed description of this data). The data includes socio-demographic and general trip-making characteristics of the traveler, and detailed information on the current trip (purpose, party size, origin and destination cities, etc.). The set of modes available to travelers for their intercity travel was determined based on the geographic location of the trip (the universal choice set included car, air, train and bus). Level of service data were generated for each available mode and each trip based on the origin/destination information of the trip (the assembly of the level-of-service data was done by KPMG Peat Marwick for VIA Rail; for information on detailed procedures to compute level-of-service measures, the reader is referred to KPMG Peat Marwick and Koppelman, 1990).

In this paper, we focus on intercity mode choice for paid business travel in the corridor. The study is further confined to a mode choice examination among air, train, and car due to the very few number of individuals choosing the bus mode in the sample and also because of the poor quality of the bus data (see Forinash, 1992). This is not likely to affect the applicability of the mode choice model in any serious way since the bus share for paid business travel in the corridor is less than one percent. The sample used is a choice-based sample and comprises 3593 business travelers. The share of the choice of each mode in the population of travelers was available from supplementary aggregate data. Since the sample is choice-based with known aggregate shares, we employed the Weighted Exogenous Sample Maximum Likelihood (WESML) method proposed by Manski and Lerman (1977) in estimation. The asymptotic covariance matrix of parameters is computed as $H^{-1} \Delta H^{-1}$, where H is the hessian and Δ is the cross-product matrix of the gradients (H and Δ are evaluated at the estimated parameter values). This provides consistent standard errors of the parameters (Borsch-Supan, 1987).

Five variables associated with individual socio-demographics and trip characteristics were available in the data, and all of these were considered for market segmentation. The variables are: income, sex (female or male), travel group size (traveling alone or traveling in a group), day of travel (weekend travel or weekday travel), and (one-way) trip distance. The segmentation variables were introduced as alternative-specific variables in the logit model of equation (3) with the last segment being the base.

The level-of-service variables used to model choice of mode included modal level-of-service measures (frequency of service, total cost, in-vehicle travel time and out-of-vehicle travel time) and a large city indicator which identified whether a trip originated, terminated, or originated and terminated in a large city. This variable may be viewed as a “proxy” level-of-service measure capturing mode characteristics associated with large cities. Table 1 provides descriptive statistics on the modal level-of-service measures in the sample.

3.2 Endogenous Market Segmentation Model Results

We estimated the endogenous segmentation model with $S = 2, 3$, and 4 segments. In all these estimations, travel time was best represented simply by decomposition into in-vehicle and out-of-vehicle travel times. For all S , we found that the use of travel cost was preferred to travel cost deflated by income. The final mode choice model specification for the segmented models included the alternative specific mode-bias constants and the level-of-service variables (we examined if there were differences in preferences based on income and trip distance within each segment by including these variables as alternative specific variables in the mode choice utility, but did not find any statistically significant effects).

We computed the Bayesian Information Criterion (BIC) value as shown in equation (16) for each number of segments. The BIC value decreased as we moved from two to three segments, but increased when we added the fourth segment (the BIC value was 2291 for the two-segment case, 2247.9 for the three-segment case and 2259.8 for the four-segment case). Thus, we selected three segments as the appropriate number of segments.

The estimation results for the three-segment solution are shown in Table 2. The signs of all the level-of-service variables in the segment-specific mode choice models are consistent with *a priori* expectations. However, there are clear differences in intrinsic preferences and sensitivities to level-of-service measures among the segments. Turning to the segmentation

model, the coefficients in this model are, in general, very significant.⁴ A comparison of the coefficients across the segments provides important qualitative information regarding the characteristics of each segment *vis-a-vis* other segments. The constants in the segmentation model contribute to the size of each segment and do not have any substantive interpretation. The segment sizes are computed using equation (4); segment one is largest (48.7% of intercity travelers) and segment two is the smallest (12.2% of intercity travelers).

Table 3 summarizes (qualitatively) the mode choice characteristics and the socio-demographic and trip characteristics of individuals within each segment. Segment two has a high overall preference for train, is highly sensitive to cost, and is low in sensitivity to travel time. This result is reasonable since individuals in segment two earn low incomes, and travel in a group and on weekends; the high intrinsic preference for train in this segment can also be attributed to the intermediate trip distance of travel in the segment. Further, previous studies (for example, KPMG Peat Marwick *et al.*, 1993) have indicated that women prefer common-carrier surface modes more than men do, which is consistent with the result obtained here (segment two has the highest female proportion). The high frequency sensitivity of segment two may be associated with group travel; individuals traveling together may have different schedule conveniences and may therefore place a high premium on frequency of service. Segment three has a high overall preference for air, is not very sensitive to cost, and is highly sensitive to travel time; this is consistent with the high-income of individuals in this segment and the single-individual, weekday, long distance travel characteristics of the segment. The money value of time is very high in this segment. Segment one is the intermediate segment, both in level-of-service sensitivity and socio-demographic/trip characteristics. Individuals in the first segment whose trips do not originate or end in a large city have an intrinsic preference for the car and air modes over the train mode, and for the car mode over the air mode. For individuals whose trips originate or end in a large city, there is a greater intrinsic preference for air over the car mode in this segment.

To characterize each segment more intuitively, we compute the mean values of the segmentation variables within each segment (see equations 5). The results are presented in Table 4 and support our previous observations regarding segment characteristics.

⁴ It is useful to note that had we adopted a full-dimensional exogenous segmentation scheme, there would have been (assuming only two income segments and two trip-distance segments) $2^5 = 32$ market segments with an average of only about 110 observations within each segment.

3.3 Comparison of Endogenous Market Segmentation with Alternative Approaches

In this section, we compare the empirical performance of the endogenous market segmentation approach relative to the two alternative extant methods to accommodating systematic heterogeneity in preference and response across the population (these alternative methods are the refined utility function specification method and the limited-dimensional exogenous market segmentation method).

Table 5 summarizes the results of models obtained using the refined utility function method. We present the overall measures of fit for three different specifications. The first specification includes a) first-order interactions of all the five segmentation variables with mode preferences, b) the large city indicator variable, and c) the four modal level-of-service variables: frequency, cost, and in-vehicle and out-of-vehicle travel times (variants of this specification that incorporate the cost level-of-service as cost/income and the out-of-vehicle time measure as out-of-vehicle over distance, as has been done in some earlier mode choice analyses, were rejected by the specification reported here). All the five segmentation variables had a statistically significant impact on train and air mode preferences (car is the base; the impact of each of these variables was also not the same across the train and air modes). The second specification adds first-order interactions of the five segmentation variables with the level-of-service measures.⁵ This specification, in its full version, effectively adds 28 level-of-service variables to the first specification. However, of these, only six of the interaction terms were significant and these are retained in the preferred version. The third specification, in its full version, adds all (ten) second-order interactions of the five segmentation variables with mode preferences to the full version of the second specification (since there are three modes, this third specification adds 20 additional parameters to the full version of the second specification). In this third specification, only seven of the second-order interactions with preference and seven of the first-order interactions with the level-of-service variables were significant. These are retained in the preferred version. As can be observed from the table, the adjusted likelihood ratio index of the refined utility function specification models are smaller than that of the endogenous segmentation model. The

⁵ For the two continuous variables; income and trip distance; we defined three distinct ranges and allowed the level-of-service sensitivity to be different for the different ranges. The income segments were: less than \$40,000, \$40,000-\$65,000 and greater than \$65,000. The segments for trip-distance were less than 250 miles, 250-500 miles and greater than 500 miles.

endogenous segmentation model rejects the refined utility function models in Table 5 in non-nested adjusted likelihood ratio tests (see Ben-Akiva and Lerman, 1985; page 172 for the structure of the test). Thus, it provides a better fit to the data. We also found that some of the statistically significant coefficients in the refined utility models were non-intuitive. For example, individuals in the lower income bracket were found to be less sensitive to cost and more sensitive to out-of-vehicle time than individuals in the middle and higher income brackets.

Table 6 presents model results for one-way segmentations and for all possible combinations of two-way variable segmentations in the spirit of the limited-dimensional exogenous market segmentation method. The specification adopted within each segment is based on the first specification of the refined utility function specification in Table 5.

The one-way segmentation results show that, on the basis of the adjusted likelihood ratio index $\bar{\rho}^2$, distance is the most important segmentation variable (all segmentations reject the unsegmented model in nested likelihood ratio tests at the 0.05 significance level or better). We also find that all the exogenously segmented models have a $\bar{\rho}^2$ which is significantly less than that of the endogenous segmentation model based on a non-nested test. Since these results may be deceiving (the analyst can specify improved exogenous segmentation models by constraining coefficients across segments), we computed the $\bar{\rho}^2$ for the one-way segmented models under the most favorable (albeit unrealistic) scenario where the likelihood value corresponds to the exogenously segmented model, but the number of parameters is assumed to be equal to that of the unsegmented model. The resulting $\bar{\rho}_{fav}^2$ values are shown in the Table and indicate that, even in this most favorable scenario, the $\bar{\rho}^2$ for the one-way segmentation models are significantly smaller than that of the endogenous segmentation model.

The results of the two-way exogenous segmentation models reject the corresponding one-way segmentation models in nested likelihood ratio tests. This suggests that there is benefit to increasing the order of interaction effects of the segmentation variables on preference and response. But, even for these two-way segmentations, the $\bar{\rho}^2$ values are significantly smaller than that of the endogenous segmentation model. As in the case of the one-way segmentation model, we computed a “favorable” $\bar{\rho}^2$ value for the two-way models, this time assuming that the number of parameters in the two-way segmentation models is the same as in the endogenous segmentation model (*i.e.*, 36 parameters). These values are presented in the final column and

indicate that, even under this favorable scenario, the only model that is close to the endogenous segmentation model is the one that segments by income and trip distance. However, a non-nested test convincingly rejects even this best “favorable-scenario”-specification relative to the endogenous segmentation model. In addition, as in the refined utility specifications, we obtained non-intuitive results in the income-distance two-way segmentation model; the parameter on cost was positive in all the segments (and in two segments, significantly so) except in the high income-high trip distance segment. Further, in all but two segments, the parameter on in-vehicle time was statistically insignificant (in part, this is a consequence of imprecision in coefficient estimates due to the small number of observations in the segments).

In summary, the empirical results indicate clearly that the endogenous segmentation model provides a better fit to the data and offers more intuitively appealing results compared to other extant approaches to incorporating systematic heterogeneity. This can be attributed to the inclusion of the full order of interaction effects of the segmentation variables on preference and level-of-service sensitivity.

3.4 Assessment of the Performance of the Hybrid EM-DFP Algorithm

The EM algorithm produces iteration sequences with good global convergence characteristics (*i.e.*, the EM iteration sequence converges to a local maximizer of the likelihood function) in mixture models, even when the starting values are distant from the maximizing values (the theory and proofs of this result, and a review of an exhaustive body of empirical evidence to support this result, can be found in Redner and Walker, 1984). On the other hand, the complex nature of the dependence of the log-likelihood function on the mixture-model parameters can produce Newton and quasi-Newton iteration sequences that get stalled at some point and never make further progress toward convergence, especially when the starting parameter values are distant from the maximizing values (this is because the Newton and quasi-Newton iterative schemes rely on approximations that are valid only in the neighborhood of the maximizing parameter values; see Redner and Walker, 1984 and Cramer, 1986, page 72).

Our own empirical experience during the maximization of the likelihood function of the endogenous segmentation model reinforces the theoretical analysis and empirical evidence discussed earlier. A natural starting point for the iterations in the endogenous segmentation model is to use the unsegmented mode choice model parameters for the mode choice model in

each segment and set all segment membership model parameters to zero.⁶ We considered three algorithms for estimation: the EM method, the DFP (Davidson, Fletcher, Powell) algorithm (which is a widely used and effective quasi-Newton algorithm, see Greene, 1990; page 370), and a hybrid EM-DFP algorithm that starts the iteration with the EM algorithm but switches to the DFP algorithm later.

In terms of stability, we found that the EM algorithm outperformed the DFP algorithm. In particular, the EM algorithm was predictable; it produced very similar and monotonically-increasing (in the likelihood function) iteration sequences in repeated trials. The DFP algorithm, on the other hand, was quite unpredictable in its iteration sequence in repeated trials. Some iteration sequences appeared to proceed well, while others wandered aimlessly without any improvement to the log-likelihood function and without ever converging. The cause of such behavior appeared to be due to the line search; the DFP algorithm had some difficulty in early iterations in finding an appropriate step length and, therefore, entered a random direction-search mode. The random search sometimes resulted in a subsequent stable iteration sequence and sometimes did not proceed anywhere. We never obtained a convergent iteration sequence with the DFP algorithm for the endogenous segmentation model with four segments. We obtained a convergent sequence in three out of five trials for the two-segment solution and in two of five trials for the three-segment solution.⁷ We did not encounter any stability problems in the hybrid EM-DFP method since the DFP iterations were started with parameter values close to their maximizing values.

We now compare the computational speeds of the EM algorithm, the DFP algorithm, and the hybrid EM-DFP algorithm. We focus on the three-segment solution. For the DFP algorithm, we present the results for the fastest successful run. All estimations were done using the GAUSS matrix programming language on a 486-DX2, 66 MHz. computer. The gradient of the log-likelihood function was coded for the DFP algorithm and the gradient and hessian were coded

⁶ In practice, at least one mode choice parameter should be shifted slightly (up or down) in one of the segments to start the iterations; otherwise, there is no incentive for the segment membership parameters to be updated and “convergence” will be achieved immediately.

⁷ Both Kamakura and Russell (1988) and Gupta and Chintagunta (1994) do not cite any problems in their estimations. It is not clear whether they did not encounter any problems or whether they just did not report them. It should also be emphasized that while the study here and many earlier empirical studies with mixture models have documented difficulties with the usual maximization algorithms, this need not be an universal finding in all data contexts. Theoretical and empirical examination of the relationship between data contexts and algorithm performance would be a useful direction for future research.

for the MNL estimation in the EM algorithm. The results are shown in Figure 1. Each point represents an iteration of the indicated algorithm. The vertical axis represents the log-likelihood function divided by the number of observations in the sample.

The EM algorithm has a stable *S*-shaped pattern. It takes a few small steps at the beginning before taking large steps toward increasing the log-likelihood function (this is in contrast to some earlier applications of the algorithm where the algorithm makes the largest leap in the first iteration and the rate of the leap decreases monotonically thereafter; see Ruud, 1991 and Watson and Engle, 1984). The secondary MNL iterations in each main EM iteration ranged from two to three with the largest EM iteration leaps being associated with three MNL iterations. As documented in other applications of the EM algorithm (see Watson and Engle, 1984 and Redner and Walker, 1984), most of the change in the log-likelihood function is realized in the first few iterations and the algorithm is very slow in convergence rate near the likelihood maximum.

Each iteration of the DFP algorithm, in general, is less time-consuming than the EM iteration; however, because of entering into a random direction-search mode, some early iterations take a substantial amount of time. The iteration sequence for the DFP is not smooth; there are sequences with little improvement in the log-likelihood function. But the algorithm converges much more rapidly near the likelihood maximum relative to the EM method.

In the hybrid EM-DFP algorithm, we used a criterion of less than 0.01 difference in successive values of the average log-likelihood function of equation (15) to switch from the EM algorithm to the DFP algorithm (this criterion was applied only after a minimum of five EM iterations). The results clearly show the effectiveness of the hybrid algorithm which combines the large and stable steps of the EM algorithm at the beginning of the maximization with the stable and relatively rapid convergence of the DFP algorithm near the likelihood maximum.

4. Choice Elasticities and Policy Implications

The results in Table 7 present the choice elasticities and the mode shares obtained from the endogenous segmentation model at the segment-level and the market level. We present the

relevant elasticities for changes in rail level of service characteristics only.⁸ The entries in the segment-level columns represent the contribution of the corresponding segment to the overall percentage change in market share of the modes due to a one percent increase in the train level-of-service variables. We present these values rather than the actual segment-level elasticities since the current entries provide a better basis to examine the differential effects (across segments) of policy actions to improve rail level-of-service (the segment-level elasticities provide information only on within-segment shifts; they are not useful for cross-segment comparisons since they do not account for the different segment sizes and because they are a function of segment-level mode choice probabilities).

The choice elasticities in the table reflect our earlier qualitative discussion of the level-of-service sensitivity differences among the segments. It is also useful to note that the market share sensitivity of car and air are about the same due to an increase in rail frequency or rail cost for segments two and three, but the sensitivity of the car mode is greater than air for segment one.

The mode choice shares in individual segments in the segmented model show that the car share is highest for segment one, the rail share is highest for segment two, and the air share is highest for segment three. The market share predictions from the segmented model are not exactly equal to the actual market shares (as represented by the weighted estimation sample) if we consider all significant digits; they are however the same as the actual market shares up to two decimal places in this empirical analysis (if we use the *a posteriori* segment membership probabilities instead of the *a priori* segment membership probabilities in computing the mode shares, then it is relatively straightforward to show using equation (12) that the market share predictions from the segmented model will equal the actual market shares represented by the weighted estimation sample).

The choice elasticities of the segmented model provide valuable insights for the targeting of informational campaigns regarding rail service improvements and for positioning of rail improvements in the travel market. In particular, the results indicate that it is most efficient to target individuals who have low-income earnings, who are female, and who travel in a group (segment two) for informational campaigns on rail frequency improvements or rail cost decreases. Rail frequency improvements and rail cost reductions are best positioned in the

⁸ Since the objective of the original study for which the data were collected was to examine the effect of alternative improvements in rail level of service characteristics, we focus on the elasticity matrix corresponding to changes in rail level of service here.

medium-distance intercity travel corridors and in the weekend business travel market. The above strategies lead to the maximum increase in rail share in response to frequency improvements and cost reductions, but the increase in rail share is due to almost equal percentage decreases in car and air shares. If the primary objective is to decrease auto-congestion on highways, while at the same time ensuring a reasonable increase in rail share, then it may be more appropriate to target the male traveling population with medium incomes, and to position frequency improvements and cost reductions in the short-distance travel corridors and in the weekday travel market (segment one). Informational campaigns regarding rail travel time improvements are best directed toward the high-income travelers; such improvements are best positioned in the long-distance travel corridors and in the weekday travel market.

5. Summary and Conclusions

In this paper, we propose the use of an endogenous market segmentation model in a travel demand context. In this model, membership in a segment is probabilistic and is a function of the socio-demographic and trip characteristics of each individual. The formulation enables the use of a number of segmentation variables without requiring the multi-way partition of data and obviates the need to establish *ad hoc* threshold values of continuous segmentation variables. An examination of the individual-level cross-elasticities indicates that the endogenous segmentation model does not have the IIA property of the standard multinomial logit formulation. We have also developed a stable, efficient estimation procedure for estimating the segmentation model. This procedure involves the use of an EM algorithm to obtain starting values for the subsequent direct maximization of the likelihood function of the segmentation model. While we have developed the hybrid EM-DFP technique in the context of a multinomial logit formulation for mode choice, the same technique can be used for more complex mode choice formulations such as the nested logit or multinomial probit. A particularly valuable contribution of our estimation approach is that the EM algorithm (which requires only the standard multinomial logit software for estimation) can be used in isolation to obtain the parameters of the segmentation model and their asymptotic standard errors if access to general maximum-likelihood software is not available (this approach will, however, be quite time-consuming due to the slow nature of convergence of the EM algorithm in the vicinity of the likelihood maximum).

We applied the endogenous segmentation model to the estimation of inter-city travel mode choice in the Toronto-Montreal corridor. Using the Bayesian Information Criterion, we found that the preferred specification used a three-segment solution. The probability of belonging to any segment was a function of income, sex, travel group size, day of travel, and trip distance. In a comparative empirical assessment of the endogenous segmentation model with other commonly used methods to account for systematic heterogeneity, we found the endogenous segmentation model to be the most appropriate based on fit to the data and reasonability of the results. Our assessment of the performance of the hybrid EM-DFP algorithm *vis-a-vis* the DFP method also clearly indicated the superiority of the former over the latter.

The results of the preferred three-segment solution of the endogenous segmentation model showed that the intrinsic preferences for modes and level-of-service sensitivity were quite different among the three segment groups. These differences, in combination with the socio-demographic and trip-related characteristics of individuals in each segment, provide important information for effective targeting and strategic positioning of rail service improvements. More generally, the endogenous segmentation model represents a valuable methodology for evaluating the effects of intercity traffic congestion-alleviation strategies in urban and intercity travel contexts.

References

- G. Allenby, "Hypothesis Testing with Scanner Data: The Advantage of Bayesian Methods", *Journal of Marketing Research* 27, 379-389 (1990).
- M. Ben-Akiva and S.R. Lerman, *Discrete Choice Analysis: Theory and Application to Travel Demand*, The MIT Press, Cambridge, 1985.
- A. Börsch-Supan, *Econometric Analysis of Discrete Choice*, Lecture Notes in Economics and Mathematical Systems, Springer-Verlag, Berlin, Germany, page 34, 1987.
- G. Chamberlain, "Analysis of Covariance with Qualitative Data", *Review of Economic Studies* 47, 225-238 (1980).
- J.S. Cramer, *Econometric Applications of Maximum Likelihood Methods*, Cambridge University Press, Cambridge, London, 1986.
- M.C. Dayton and G.B. Macready, "Concomitant-Variable Latent Class Models", *Journal of the American Statistical Society* 83, 173-179 (1988).
- A.P. Dempster, N.M. Laird and D.B. Rubin, "Maximum Likelihood from Incomplete Data via the EM Algorithm", *Journal of the Royal Statistical Society B* 39, 1-38 (1977).
- Electric Power Research Institute, "Methodology for Predicting the Demand for New Electricity-Using Goods", EA-593, Project 488-1, Final Report, 1977.
- G.W. Fischer and D. Nagin, "Random Versus Fixed Coefficient Quantal Choice Models", in Manski, C.F. and D. McFadden (eds.) *Structural Analysis of Discrete Data with Econometric Applications*, MIT Press, Cambridge, Massachusetts, 273-304, 1981.
- C.V. Forinash, "A Comparison of Model Structures for Intercity Travel Mode Choice", unpublished Master's Thesis, Department of Civil Engineering, Northwestern University, Evanston, Illinois, 1992.
- F. Gonül and K. Srinivasan, "Modeling Multiple Sources of Heterogeneity in Multinomial Logit Models: Methodological and Managerial Issues", *Marketing Science* 12, 213-229 (1993).
- W.H. Greene, *Econometric Analysis*, Macmillan Publishing Company, New York, 1990.
- S. Gupta and P.K. Chintagunta, "On Using Demographic Variables to Determine Segment Membership in Logit Mixture Models", *Journal of Marketing Research* 31, 128-136 (1994).
- J.A. Hausman and D. Wise, "A Conditional Probit Model for Qualitative Choice: Discrete Decisions Recognizing Interdependence and Heterogenous Preferences", *Econometrica*, 46, 403-426 (1978).
- D.A. Hensher, "Two Contentions Related to Conceptual Context in Behavioral Travel Modeling", in *New Horizons in Travel Behavior Research*, editors: P.R. Stopher, A.H. Meyburg, and W. Brög, Lexington Books, Lexington, Massachusetts, 509-514, 1981.
- J.L. Horowitz, "Reconsidering the Multinomial Probit Model", *Transportation Research* 25B, 433-438 (1991).
- J.L. Horowitz, "Semiparametric Estimation of a Work-Trip Mode Choice Model", *Journal of Econometrics* 58, 49-70 (1993).
- W.A. Kamakura and G.J. Russell, "A Probabilistic Choice Model for Market Segmentation and Elasticity Structure", *Journal of Marketing Research* 26, 379-390 (1989).
- KPMG Peat Marwick and F.S. Koppelman, *Proposal for Analysis of the Market Demand for High Speed Rail in the Quebec/Ontario Corridor*, submitted to Ontario/Quebec Rapid Train Task Force, 1990.

- KPMG Peat Marwick in association with ICF Kaiser Engineers, Inc., Midwest System Sciences, Resource Systems Group, Comsis Corporation and Transportation Consulting Group, "Florida High Speed and Intercity Rail Market and Ridership Study: Final Report", submitted to Florida Department of Transportation, 1993.
- C. Manski and S. Lerman, "The Estimation of Choice Probabilities from Choice-Based Samples", *Econometrica* 45, 1977-1988 (1977).
- D. McFadden, "Conditional Logit Analysis of Qualitative Choice Behavior" in Zarembka, P. (ed.) *Frontiers in Econometrics*, Academic press, New York, 1973.
- G.J. McLachlan and K.E. Basford, *Mixture Models: Inference and Applications to Clustering*, Marcel Dekker, Inc., New York, 1988.
- R.A. Redner and H.F. Walker. "Mixture densities, Maximum Likelihood, and the EM Algorithm", *SIAM Review* 2, 195-239 (1984).
- P.A. Ruud, Extensions of Estimation Methods Using the EM Algorithm, *Journal of Econometrics* 49, 305-341 (1991).
- M.W. Watson and R.F. Engle, "Alternative Algorithms for the Estimation of Dynamic Factor, MIMIC and Varying Coefficient Regression Models", *Journal of Econometrics* 23, 385_400 (1983).

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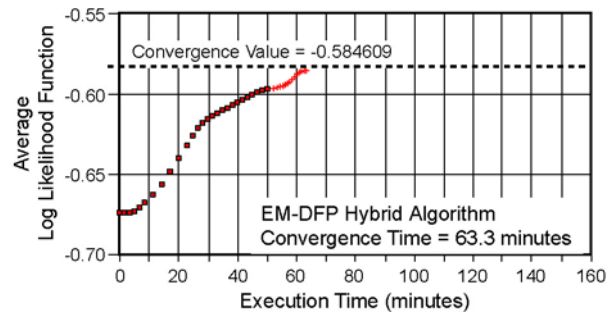
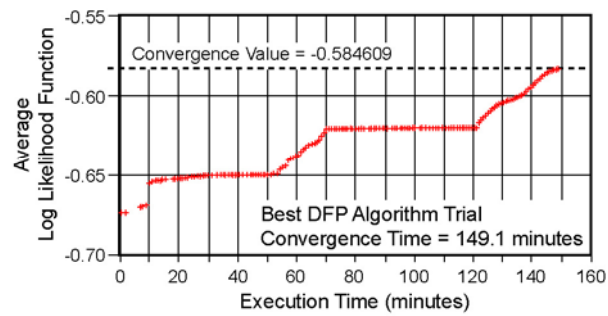
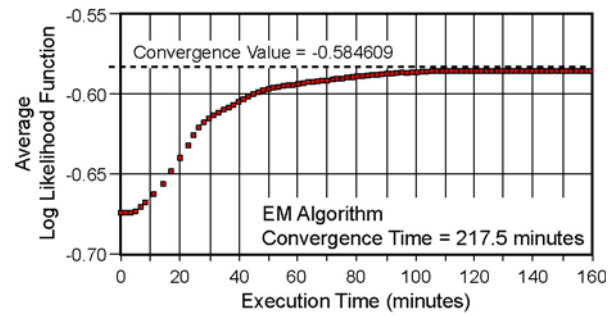


Figure 1. Performance of alternative algorithms for the three-segment solution

Table 1. Mean and (Standard Deviation) of Modal Level-of-Service Variables

Mode	Frequency (departures/day)	Total cost (in Canadian \$)	In-vehicle time (in mins.)	Out-of-vehicle time (in mins.)
Train	4.21 (2.3)	58.58 (17.7)	244.50 (115.0)	86.32 (22.0)
Air	25.24 (14.0)	157.33 (21.7)	57.72 (19.2)	106.74 (24.9)
Car	not applicable	70.56 (32.7)	249.60 (107.5)	0.00 (0.0)

Note: All measures are one-way values. Air and train frequency refer to total departures by all carriers.

Table 2. Intercity Mode Choice Analysis: Parameter Estimates for Three-Segment Solution

Model	Variable	Segment 1		Segment 2		Segment 3	
		Parameter	t-statistic	Parameter	t-statistic	Parameter	t-statistic
Segment-Specific Mode Choice Model	Mode Constants						
	Train	-3.0617	-2.54	4.7763	2.12	1.1737	0.60
	Air	-1.0516	-1.82	-1.3691	-1.01	4.3404	3.36
	Large City Indicator						
	Train	1.9273	2.20	0.2146	0.32	-0.0840	-0.12
	Air	2.2240	3.46	-1.3691	-1.01	2.6892	2.37
	Frequency of Service (deps./day)	0.1615	6.38	0.5784	3.49	0.1790	3.92
	Travel Cost (Canadian \$)	-0.0591	-4.53	-0.1728	-3.27	-0.0166	-0.54
	Travel Time (minutes)						
In-Vehicle	-0.0254	-3.25	-0.0030	-1.20	-0.0657	-5.21	
Out-of-Vehicle	-0.0436	-2.91	-0.0239	-1.84	-0.1627	-5.01	
Segmentation Model	Constant	4.4227	7.62	1.5366	2.56	Base Segment	
	Income	-0.0293	-5.73	-0.0447	-8.60		
	Female Sex	-0.7614	-3.46	0.9703	4.05		
	Traveling Alone	-0.1657	-1.70	-0.7226	-4.07		
	Weekend Travel	0.2423	0.65	1.5326	4.71		
	Trip Distance	-0.0047	-5.91	-0.0030	-3.79		
Segment Size		0.4866		0.1220		0.3914	

Note: The log-likelihood value at zero is -3947.3; the log-likelihood value for the unsegmented model with only alternative specific constants is -3648.2. The log-likelihood value at convergence for the three segment solution is -2100.5.

Table 3 Qualitative Characterization of Mode Choice Preferences and Socio-Demographic/Trip Attributes of Segments

Preferences/Attributes	Characteristic	Segment 1	Segment 2	Segment 3
Mode Choice Preferences	Intrinsic Preference for	Car; if trip originates or ends in large city, air is preferred	Train	Air
	Sensitivity to Frequency	Low	High	Low
	Sensitivity to Cost	Medium	High	Low
	Sensitivity to IVTT	Medium (Money Value = \$26/hour)	Low (Money Value = \$1.05/hour)	High (Money Value = \$237/hour)
	Sensitivity to OVTT	Medium (Money Value = \$44/hour)	Low (Money Value = \$8.30/hour)	High (Money Value = \$588/hour)
Socio-Demographic and Trip Attributes	Income	About average market income	Lower than average market income	Higher than average market income
	Sex	High proportion of males	High proportion of females	Same proportion as overall market
	Travel Group Size	Same proportion as overall market	High proportion of individuals traveling in a group	High proportion of individuals traveling alone
	Day of Travel	High proportion of weekday travelers	High proportion of weekend travelers	High proportion of weekday travelers
	Trip Distance	Short	Medium	Long

Note: MV stands for “money value of time”

Table 4. Mean Values of Demographic and Trip Variables in Each Segment

Variable	Segment 1	Segment 2	Segment 3	Overall Market
Income (x 10 ³ Can\$)	52.16	44.09	60.28	54.36
Female	0.13	0.48	0.20	0.20
Traveling Alone	0.69	0.57	0.77	0.70
Weekend Travel	0.20	0.62	0.19	0.25
Trip Distance (km)	311.80	373.37	444.76	371.35

Table 5. Empirical Comparison of the Endogenous Segmentation Model with Refined Utility Function Specification Models

Statistic	First-order preference interactions	First-order preference and first-order response interactions		Second-order preference and first-order response interactions	
		Full version	Preferred version	Full version	Preferred version
Number of parameters	18	46	24	66	32
Log-likelihood at convergence	-2299.38	-2199.07	-2211.48	-2154.09	-2174.71
Adjusted likelihood ratio index, $\bar{\rho}^{2\ 1}$	0.4129	0.4312	0.4337	0.4376	0.4409
Result of non-nested likelihood ratio index test with endogenous segmentation model	Reject very strongly the hypotheses that any (and each) of the above models is as good as the endogenous segmentation model.				

Note: The likelihood value at convergence for the endogenous segmentation model is -2100.5 and the adjusted likelihood ratio index for this model is 0.4587 (number of parameters in the model is 36).

¹The adjusted likelihood ratio index is computed as $\bar{\rho}^2 = 1 - [(\hat{\beta}) - k] / \langle (0)$, where $\langle (\hat{\beta})$, $\langle (0)$, and k are the log-likelihood function value at convergence, the log-likelihood value at zero, and the number of model parameters, respectively.

Table 6. Empirical Comparison of the Endogenous Segmentation Model with Limited-Dimensional Exogenous Segmentation Models

Segmentation variable	Number of Segms.	Number of parms.	LL at converg.	$\bar{\rho}^2$ ¹	$\bar{\rho}_{fav}^2$ ²	Two-way segmentation with...	Number of Segms.	Number of parms.	LL at converg.	$\bar{\rho}^2$	$\bar{\rho}_{fav}^2$ ³
Income ⁴	3	52	-2242.9	0.4186	0.4272	Sex	6	92	-2214.8	0.4156	0.4298
						Group size	6	92	-2208.9	0.4186	0.4313
						Day of travel	6	92	-2216.6	0.4151	0.4293
						Trip distance	9	156	-2108.1	0.4264	0.4568
Sex	2	32	-2287.4	0.4124	0.4160	Group size	4	64	-2262.0	0.4107	0.4178
						Day of travel	4	64	-2260.1	0.4112	0.4183
						Trip distance	6	96	-2179.7	0.4235	0.4387
Group size	2	32	-2278.5	0.4147	0.4182	Day of travel	4	64	-2250.9	0.4135	0.4206
						Trip distance	6	96	-2163.2	0.4277	0.4429
Day of travel	2	32	-2279.3	0.4145	0.4180	Trip distance	6	96	-2172.3	0.4253	0.4406
Trip distance	3	54	-2212.4	0.4258	0.4350	-	-	-	-	-	-

Note: The adjusted likelihood ratio index for the endogenous segmentation model is 0.4587 and the number of parameters in this model is 36.

¹ The adjusted likelihood ratio index is computed as $\bar{\rho}^2 = 1 - [(\hat{\beta}) - k] / \langle (0)$, where $\langle (\hat{\beta})$, $\langle (0)$, and k are the log-likelihood function value at convergence, the log-likelihood value at zero, and the number of model parameters, respectively.

² The “favorable” adjusted likelihood ratio index for the one-way segmentations is computed by using the log-likelihood value at convergence for the segmented models, but by assuming the number of parameters to be equal to that in the unsegmented model.

³ The “favorable” adjusted likelihood ratio index for two-way segmentations is computed by using the log-likelihood at convergence from the segmented models, but assuming the number of parameters to be the same as that in the endogenous segmentation model.

⁴ There was no variation in income in the highest income segment and hence income is not introduced as an alternative specific variable in the high-income segment.

Table 7. Choice Elasticities (in Response to Change in Rail Service) and Mode Choice Shares from the Endogenous Segmentation Mode

Rail Level of Service Attribute	Segment 1			Segment 2			Segment 3			Market ¹		
	Rail	Air	Car	Rail	Air	Car	Rail	Air	Car	Rail	Air	Car
Frequency	0.15	-0.01	-0.04	0.20	-0.03	-0.04	0.06	-0.01	-0.01	0.41	-0.05	-0.10
Cost	-0.57	0.06	0.14	-0.77	0.14	0.15	-0.14	0.03	0.03	-1.48	0.22	0.31
IVTT ²	-0.32	0.01	0.09	-0.03	0.00	0.00	-0.51	0.07	0.12	-0.86	0.09	0.21
OVTT ³	-0.35	0.03	0.09	-0.18	0.03	0.04	-0.67	0.08	0.16	-1.20	0.14	0.29
Mode Choice Shares ⁴	0.07	0.20	0.73	0.80	0.07	0.13	0.06	0.76	0.18	0.15	0.40	0.44

¹ The overall market elasticity is the sum of the “elasticity” entries in the individual segments. The “elasticity” entries at the segment level represent the contribution of the corresponding segment to the overall percentage change in market share due to a 1 % increase in rail level-of-service attribute. The actual increase (decrease) in rail share at the market level is equal to the decrease (increase) in the air and car shares at the market level. These conditions do not hold exactly in the table due to rounding of the elasticity entries.

² IVTT represents In-Vehicle Travel Time.

³ OVTT represents Out-of-Vehicle Travel Time.

⁴ The overall market share of each mode in the joint segmentation/mode choice model is equal to the weighted average of the corresponding segment-level mode shares, where the weights are the segment sizes.