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## Summary

This report documents the results of a study conducted to compute the inviscid longitudinal aerodynamic characteristics of a simplified X-33 configuration. This study was conducted in support of the industry led $\mathrm{X}-33$ program. The major components of the $\mathrm{X}-33$ vehicle, namely the body, the canted fin, the vertical fin, and the bodyflap, were simulated in the CFD model. The rear-ward facing surfaces at the base including the aerospike engine surfaces were not simulated. The FELISA software package was used for this study. This software consists of an unstructured surface and volume grid generator and two inviscid flow solvers one for transonic flows and the other for hypersonic flows. The hypersonic flow solver with perfect gas, equilibrium air, and $C F_{4}$ gas options was used in the present study. Computations were made for Mach 4.96, 6.0, and 10.0 with perfect gas air option, and for Mach 10 with equilibrium air option with flow condition of a typical point on the X-33 flight trajectory. Computations were also made with CF4 gas option at Mach 6.0 to simulate the $C F_{4}$ tunnel flow condition. An angle of attack range of 12 to 48 deg. was covered. The CFD results were compared with available wind tunnel data. Comparison was good at low angles of attack; at higher angles of attack (beyond 25 deg.) some differences were found in the pitching moment. These differences progressively increased with increase in angle of attack, and are attributed to the viscous effects. However, the computed results showed the trends exhibited by the wind tunnel data.

## Nomenclature

| $C_{A}$ | $\mathbf{F}_{\mathbf{A}} /\left(q_{\infty} S_{r e f}\right)$, Axial force coefficient |
| :--- | :--- |
| $C_{N}$ | $\mathbf{F}_{\mathbf{N}} /\left(q_{\infty} S_{r e f}\right)$, Normal force coefficient |
| $C_{m}$ | $\mathbf{M}_{\mathbf{y}} /\left(q_{\infty} S_{r e f} l_{r e f}\right)$, Pitching moment coefficient |
| $C_{p}$ | $\left(p-p_{\infty}\right) / q_{\infty}$, Pressure coefficient |
| $\mathbf{F}_{\mathbf{A}}$ | Axial force |
| $\mathbf{F}_{\mathbf{N}}$ | Normal force |
| $l_{r e f}$ | Reference length, $(=758.4$ sq.in. $)$ |
| $\mathbf{M}_{\mathbf{y}}$ | Pitching moment |
| $M_{\infty}$ | Freestream Mach number |
| $p$ | Static pressure |
| $p_{\infty}$ | Freestream static pressure |
| $q_{\infty}$ | Freestream dynamic pressure |
| $S_{r e f}$ | Reference area, $(=231,520.0$ sq.in. $)$ |
| $\mathrm{x}, \mathrm{y}, \mathrm{z}$ | Cartesian co-ordinates of a given point |
| $\alpha$ | Angle of attack, deg. |

## Geometry

The present computational study was done on the Lockheed X-33 F-loft, Rev. F configuration. The primary external components of this vehicle are the body, the canted fin, the vertical fin, the bodyflap, and the aerospike engines. All of these components, except the aerospike engine surfaces, were simulated in the CFD model. In order to preclude separated flow regions, mainly over the rearward facing areas like the base of


Figure 1: The X-33 F-loft Rev. F vehicle.
the vehicle, the flow over the base was not simulated. This was accomplished by extending the surfaces of the canted fin, vertical fin, and the of body downstream of the trailing edge so that they ended on a single surface. These extension surfaces provide a cover for the base. In the CFD computations, the flow was forced to be tangential to these extension surfaces. However, while computing the aerodynamic loads on the vehicle, these surfaces were ignored.

A sketch of the X-33 model used in the present CFD study is shown in Fig. 1. The axis system used for this study is also shown in the figure. The origin is at the nose of the vehicle with the $z$-axis along the body axis pointing upstream, y-axis perpendicular to the symmetry plane, and the $x$-axis in the symmetry plane perpendicular to the z-axis. The length of the body (from nose to trailing edge of the bodyflap) is approximately 831.1 in . and the tip-to-tip distance of the canted fins is 920.75 in . The canted fins make an angle of 72 deg. to the plane of symmetry. There are two vertical fins separated from each other by 200 in. For the present computations, the control surfaces, namely the rudder and the bodyflaps were in the undeflected position. Since the vehicle has a plane of symmetry, only one half of the vehicle was simulated in the computational model. The reference quantities used for reducing the aerodynamic loads to the non-dimensional form are as follows:

Reference area
Reference length
Pitching moment reference point
$231,520.0$ sq.in.
758.4 in.
(0.0, 0.0, -500.544) in.

| Grid ID | No. of Tets | No. of Points | No. of Triangles | No. of Surface Points |
| :---: | :---: | :---: | :---: | :---: |
| X33A | $7,955,084$ | $1,337,224$ | 242,850 | 121,427 |
| X33C | $6,506,154$ | $1,094,694$ | 203,160 | 101,582 |
| X33D | $7,069,961$ | $1,189,736$ | 220,066 | 110,035 |

Table 1: Properties of grids used in the present computations.

## The Felisa Software

All the computations of the present study were done using the FELISA unstructured grid software. This software package consists of a set of computer codes for the simulation of three-dimensional steady inviscid flows using unstructured tetrahedral grids. Surface triangulation and discretization of the computational domain using tetrahedral elements is done by two separate codes. Two flow solvers are available one applicable for transonic flows, and the other for hypersonic flows with an option for perfect gas air, equilibrium air, or $C F_{4}$ gases. The hypersonic flow solver was used for all the computations in this study. Post-processors like the aerodynamic analysis routine are part of the software package. More information on FELISA may be found in [1]. A description of the hypersonic flow solver may be found in [2].

## Grids Used in the Present Study

Starting with a structured surface grid in the form of a PLOT3D file, and using the software GridTool [3], a set of FELISA data files was generated. This includes the body surface and the computational domain definition file, and a file that specifies the grid spacing. The grid spacings file was modified manually in order to obtain the desired grid spacing near the nose of the vehicle. Using these data files unstructured tetrahedral grids were generated with the FELISA volume grid generator. Three separate unstructured surface and volume grids were generated to suit the freestream conditions. The properties of these grids are shown in Table 1 above. All these grids were generated on an SGI ONYX located in the Aerothermodynamics Branch (AB), NASA Langley.

A minimum grid spacing was 0.4 inch was used near the nose of the body. A plot of a portion of the grid on the symmetry plane near the nose is shown in Fig. 2. The model surface triangulation for grid X33A is shown in Fig. 3.

## Flow Conditions

The freestream conditions and the range of angles of attack covered in the present study are shown in Table 2. All perfect gas air computation (cases 1-12) were done with $\gamma=1.4$. Freestream conditions for the equilibrium air computations (cases 13-15) corresponded to the conditions for a typical point on the X-33 flight trajectory. Some wind tumnel tests had been conducted on an X-33 model in the Langley 31 -inch Mach 10 tunnel and also in the Langley Mach $6 C F_{4}$ tunnel. In order to simulate the $C F_{4}$ tunnel tests, a set of computations was done (cases 18-21) with the $C F_{4}$ gas options and freestream conditions corresponding to the conditions in the $C F_{4}$ tunnel. The freestrean conditions for computations at Mach 9.02 correspond to atmospheric flight at a nominal Mach number of 9 at an altitude of $133,000 \mathrm{ft}$., and the conditions for


Figure 2: A typical triangulation on the symmetry plane near the nose of X-33.


Figure 3: Surface triangulation for X33A grid.

| Case No. | Mach No. | Gas Model | Density <br> $\left(\mathrm{Kg} / \mathrm{m}^{3}\right)$ | Temperature <br> $(\mathrm{Kelvin})$ | Velocity <br> $(\mathrm{m} / \mathrm{sec})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1-4$ | 10.0 | Perfect Gas | NA | NA | NA |
| 58 | 6.00 | Perfect Gas | NA | NA | NA |
| $9-12$ | 4.96 | Perfect Gas | NA | NA | NA |
| $13-15$ | 10.0 | Equil. Air | $4.3120 \mathrm{E}-04$ | 259.5 | 3224 |
| 16 | 9.02 | Equil. Air | $3.6867 \mathrm{E}-03$ | 251.9 | 2863 |
| 17 | 12.02 | Equil. Air | $1.0593 \mathrm{E}-03$ | 270.7 | 3958 |
| 1821 | 6.02 | $C F_{4}$ gas | $1.7700 \mathrm{E}-02$ | 170.0 | 850 |

Table 2: Freestream conditions.
computations at Mach 12.02 correspond to atmospheric flight at a nominal Mach number of 12 at an altitude of $163,200 \mathrm{ft}$. These two cases correspond to two critical points in the flight trajectory of the $\mathrm{X}-33$ vehicle.

## Flow Solution

The flow solutions were computed on SGI Origin 2000 class parallel computers having 64 processors sitting on top of 16 G of shared memory. The grids were partitioned so that the problem would run on eight processors. The FELISA hypersonic flow solver with the appropriate gas option was used for these flow computations. Each solution was started with the low-order option, and after a few hundred iterations, the higher-order option was turned on, and the solution was run to convergence. After every 20 iteration, the surface pressures were integrated, and the aerodynamic loads, namely the normal and the axial forces, and the pitching moment acting on the model were computed. The flow solution was assumed converged when these integrated loads reached steady values. Each solution required $32-40$ hours of CPU time. The computed flow solutions were post-processed on the AB ONYX computer to obtain the aerodynamic loads. These loads were non-dimensionalized in the conventional manner, and the aerodynamic coefficients ( $C_{N}$, $C_{A}$, and $C_{m}$ ) were obtained.

It should be recalled at this point that all the present computations are inviscid; hence the boundary layer and skin friction are absent. Absence of the skin friction leads to lower axial forces. Further, since the boundary layer is absent, the effects of boundary layer separation on the aerodynamic coefficients are not simulated. On the X-33, the flow would be fully separated over the base, and possibly over the upper surface of the bodyflap. These surfaces are not simulated in the present CFD model. These factors could introduce inaccuracies in the computed axial and normal forces, and as well as in the pitching moment.

## Results and Discussion

The results of the present study are summarized in Table 3, and also shown graphically in Figures 4, 5, and 6. Tunnel test data in the form of curve fits for $C_{N}, C_{A}$, and $C_{m}$ were available for the cases listed in the
table 4. For the Mach 6 air case, the data at 4 million Reynolds number was chosen for comparison with the computed results.

The computed $C_{N}$ and $C_{m}$ for Mach numbers $4.96,6$, and 10 in perfect gas air are shown plotted Vs. a in Figure 4. Smooth curves have been drawn through the data points. The $C_{N}$ Vs. $\alpha$ curves for the three cases shown in Fig. 4(a) have nearly the same slope. For a given a, the $C_{N}$ values decrease as the Mach number is increased from 4.96 to 10.0 . The pitching moment data for the three Mach numbers is shown in Fig. 4(b). For Mach 4.96 the $C_{m}$ Vs. a has a large negative slope for $\alpha$ up to 35 deg.: beyond this angle of attack the slope becomes less negative. This indicates that the model is stable up to $\alpha=35$ deg., beyond which it becomes less stable. For Mach 10 , the trend is different. The slope of $C_{m}$ Vs. a curve is nearly zero up to $\alpha=25$ deg.; beyond this angle of attack the slope is negative. This indicates that the model is neutrally stable up to $\alpha=25$ deg., beyond this angle of attack the vehicle becomes progressively more stable. The $C_{m}$ Vs. $\alpha$ for Mach 6 lies in between the curves for Mach 4.96 and 10.0.

Computed $C_{N}$ and $C_{m}$ values for Mach 10 perfect gas air and equilibrium air are shown in Fig. 5. Tunnel data for Mach 10 are also plotted in this figure for comparison. Figure 5(a) shows that there is little difference between the computed $C_{N}$ values for perfect gas air and the equilibrium air assumption. It should be recalled here that the freestream conditions for these equilibrium flow computations corresponded to those for a typical point on the X-33 flight trajectory. The total temperature under these conditions is $3040 \dot{\mathrm{~K}}$. At this high temperature there would be considerable changes in the chemical composition and properties of air (see e.g. [4]). These changes do not seem to affect the normal force coefficient. The total temperature for the freestream conditions in the Mach 10 tunnel test section is only 980 K . At this temperature there is very little change in the chemical composition of air; hence these tunnel data should be compared with perfect gas computations.

Figure 5 (b) shows that there are some differences between computed $C_{m}$ values for perfect gas and equilibrium air cases. These differences are due to the differences between the properties of perfect gas air and equilibrium air (at a total temperature of 3040 K ). However, there are significant differences between the computed and the wind tunnel $C_{m}$ data. The differences are, although small at low angles of attack (0.001 up) to $\alpha=30$ deg.), increase as the angle of attack is increased ( 0.004 at $\alpha=48$ deg.). This trend is possibly due to the viscous effects. On the wind tumel model the flow on the upper surface of the canted fin would separate at high angles of attack due to the presence of the trailing edge shock. This would increase the pressures over the aft part of the canted fin, and, due to the large moment arm, result in positive pitching moment.

The computed $C_{N}$ and $C_{m}$ for Mach 6 perfect gas air and $C F_{4}$ gas are shown in Figs. 6(a) and (b) respectively, along with the test data from Langley 20-Inch Mach 6 Air tunnel and Langley Mach $6 C F_{4}$ tumnel. The freestream conditions for the $C F_{4}$ gas computations corresponded to those in the Langley Mach $6 C F_{4}$ tunnel test section with a total temperature of 980 K . Figure $6\left(\right.$ a) shows that the assumption of $C F_{4}$ gas at Mach 6 does not affect the computed normal force. Further, there is good agreement between the computations and the $C F_{4}$ tunnel data. However, there are differences between the computed results and the air tumel data. In the past $C_{N}$ values computed using FELISA had compared well with tunnel data; see for example [5]. The differences noticed in the present case could not be explained.

The computed $C_{m}$ values for perfect gas air and $C F_{4}$ gas cases for Mach 6 are shown in Fig. 6(b). It may be observed that there are differences between the $C_{m}$ values for the two cases. This is primarily due to the fact that air and $C F_{4}$ gas have different thermodynamic properties. For example, the density ratios across a normal shock at Mach 6 in $C F_{4}$ gas is about 10 compared to a value of about 5.3 in air. The pressure distribution over the vehicle for the $C F_{4}$ gas and in perfect gas air would be different. The tunnel test data is also shown in Fig. 6(b). It may be noticed from this figure that the computed $C_{m}$ for $C F_{4}$ gas compares with the tumel data up to about $\alpha=30$ deg. Beyond this angle, the tunnel data exhibits less nose down $C_{m}$

| Case No. | Mach No. | $\alpha$, deg. | Gas Model | $C_{N}$ | $C_{A}$ | $C_{m}$ |
| :---: | :---: | :---: | :---: | ---: | ---: | ---: |
| 1 | 10.0 | 24 | P.G. Air | 0.4534 | 0.1033 | 0.0105 |
| 2 | 10.0 | 36 | P.G. Air | 0.8922 | 0.1014 | 0.0037 |
| 3 | 10.0 | 48 | P.G. Air | 1.3245 | 0.0919 | -0.0033 |
| 4 | 10.0 | 12 | P.G. Air | 0.1232 | 0.1048 | 0.0111 |
| 5 | 6.00 | 24 | P.G. Air | 0.4898 | 0.1030 | 0.0089 |
| 6 | 6.00 | 36 | P.G. Air | 0.9252 | 0.0998 | 0.0032 |
| 7 | 6.00 | 48 | P.G. Air | 1.3401 | 0.0909 | -0.0002 |
| 8 | 6.00 | 12 | P.G. Air | 0.1434 | 0.1065 | 0.0118 |
| 9 | 4.96 | 24 | P.G. Air | 0.5146 | 0.1025 | 0.0082 |
| 10 | 4.96 | 36 | P.G.Air | 0.9481 | 0.0979 | 0.0030 |
| 11 | 4.96 | 48 | P.G. Air | 1.3555 | 0.0881 | 0.0012 |
| 12 | 4.96 | 12 | P.G. Air | 0.1579 | 0.1071 | 0.0123 |
| 13 | 10.0 | 36 | Equil. Air | 0.8853 | 0.1079 | 0.0048 |
| 14 | 10.0 | 48 | Equil. Air | 1.3286 | 0.1040 | -0.0041 |
| 15 | 10.0 | 24 | Equil. Air | 0.4484 | 0.1070 | 0.0113 |
| 16 | 9.02 | 20 | Equil. Air | 0.3279 | 0.1062 | 0.0116 |
| 17 | 12.02 | 35 | Equil. Air | 0.8318 | 0.1092 | 0.0060 |
| 18 | 6.02 | 12 | $C F_{4}$ Gas | 0.1458 | 0.1090 | 0.0118 |
| 19 | 6.02 | 24 | $C F_{4}$ Gas | 0.4763 | 0.1065 | 0.0116 |
| 20 | 6.02 | 36 | $C F_{4}$ Gas | 0.9044 | 0.1057 | 0.0059 |
| 21 | 6.02 | 48 | $C F_{4}$ Gas | 1.3526 | 0.0991 | -0.0039 |

Table 3: Summary of computed aerodynamic coefficients for X-33.

| Tunnel | Mach No. | Reynolds No. | $\alpha$ Range | Mount |
| :---: | :---: | :---: | :---: | :---: |
| Langley 20-Inch Mach 6 Air | 6.0 | $0.5 \mathrm{E}+06$ | -4 to 48 deg. | Sting |
| Langley 20-Inch Mach 6 Air | 6.0 | $2.0 \mathrm{E}+06$ | -4 to 48 deg. | Sting |
| Langley 20-Inch Mach 6 Air | 6.0 | $4.0 \mathrm{E}+06$ | -4 to 48 deg. | Sting |
| Langley $C F_{4}$ | 6.0 | $.0 .4 \mathrm{E}+06$ | -4 to 48 deg. | Sting |
| Langley 31-Inch Air | 10.0 | $2.0 \mathrm{E}+06$ | 5 to 50 deg. | Blade |

Table 4: Available wind tunnel data for $\mathrm{X}-33$.


Figure 4: Computed $C_{N}$ and $C_{m}$ for X-33 in perfect gas air at Mach 4.96, 6.0, and 10.0.


Figure 5: Comparison of computed and wind tunnel data for $\mathrm{X}-33$ in perfect gas air and equilibrium air at Mach 10.0.

| $\alpha$ <br> (deg.) | Body |  |  | Canted Fin |  |  | Bodyflap |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $C_{N}$ | $C_{A}$ | $C_{m}$ | $C_{N}$ | $C_{A}$ | $C_{m}$ | $C_{N}$ | $C_{A}$ | $C_{m}$ |
| 12 | 0.1221 | 0.0834 | 0.0137 | 0.1221 | 0.0834 | 0.0137 | 0.1221 | 0.0834 | 0.0137 |
| 24 | 0.3748 | 0.0931 | 0.0325 | 0.3748 | 0.0931 | 0.0325 | 0.3748 | 0.0931 | 0.0325 |
| 36 | 0.7182 | 0.1023 | 0.0518 | 0.7182 | 0.1023 | 0.0518 | 0.1067 | -0.0025 | -0.0242 |
| 48 | 1.0691 | 0.1050 | 0.0678 | 1.0691 | 0.1050 | 0.0678 | 0.1619 | -0.0147 | -0.0380 |

Table 5: Computed aerodynamic data for body, canted fin, and bodyflap, Mach 10, perfect gas air.

| $\alpha$ <br> deg. $)$ | Body |  |  | Canted Fin |  |  | Bodyflap |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $C_{N}$ | $C_{A}$ | $C_{m}$ | $C_{N}$ | $C_{A}$ | $C_{m}$ | $C_{N}$ | $C_{A}$ | $C_{m}$ |
| 24 | 0.3715 | 0.0965 | 0.0329 | 0.0427 | 0.0094 | -0.0095 | 0.0342 | 0.0010 | -0.0122 |
| 36 | 0.7098 | 0.1085 | 0.0535 | 0.1058 | -0.0018 | -0.0240 | 0.0695 | 0.0012 | -0.0247 |
| 48 | 1.0608 | 0.1170 | 0.0706 | 0.1655 | -0.0138 | -0.0386 | 0.1021 | 0.0008 | -0.0361 |

Table 6: Computed aerodynamic data for body, canted fin, and bodyflap, Mach 10. equilibrium air

For the perfect gas air case, the comparison is not as good. The difference increases progressively with increase in $\alpha$ for zero at $\alpha=12$ deg. to 0.006 at $\alpha=48$ deg.

In the Mach 6 and Mach 10 cases, the tumnel $C_{m}$, values are invariably higher than the computed values at angles of attack 30 deg. and beyond. As noted earlier, this is possibly due to the effects of flow separation on the canted fin. The present computations are inviscid, as such there is no flow separation any surface, including the canted fins.

The contributions to $C_{N}$ and $C_{m}$ due to the body, canted fin, bodyflap, and the vertical fin were computed separately for all the cases. In all the cases the contributions from the vertical fin to $C_{N}$ and $C_{m}$ were found to be negligible. The contribution from the body, canted fin, and the bodyflap for Mach 10 perfect gas and Mach 10 equilibrium air cases are listed in Tables 5 and 6, and are also shown plotted in Figures 7 and 8. It may be noticed from these figures that body contributes the most to both normal force and pitching moment. The contributions of the canted fin and the bodyflap are of comparable magnitude.

Similarly, the results for Mach 6 perfect gas air and Mach $6 C F_{4}$ gas cases are listed in Tables 7 and 8, and are also shown plotted in Figure 9 and 10.

## Conclusion

Inviscid longitudinal aerodynamic characteristics of the Lockheed X-33 f-loft, Rev. F velicle were computed for Mach 4.96, 6.0, and 10.0 over an angle of attack range of $4-48$ deg. using the FELISA unstructured grid software package. The bodyflap and the rudder were in undeflected position. The canted fin, the vertical fin and the body surfaces were extended downstream in the computational model in order to preclude regions of separated flows. Computations were made for Mach 10 with the perfect gas air and equilibrium air


Figure 6: Comparison of computed $C_{N}$ and $C_{m}$ for X-33 in perfect gas air and $C F_{4}$ gas at Mach 6


Figure 7: Computed $C_{N}$ and $C_{m}$ due to the body, canted fin, and bodyflap, and the complete vehicle for $\mathrm{M}=10$, perfect gas air.


Figure 8: Computed $C_{N}$ and $C_{m}$ due to the body, canted fin, and bodyflap, and the complete vehicle for $\mathrm{M}=10$, equilibrium air.


Figure 9: Computed $C_{N}$ and $C_{m}$ due to the body, canted fin, and bodyflap, and the complete vehicle for $\mathrm{M}=6$, perfect gas air.


Figure 10: Computed $C_{N}$ and $C_{n}$ due to the body, canted fin, and bodyflap, and the complete vehicle for $\mathrm{M}=6, C F_{4}$ gas.

| $\alpha$ <br> $($ deg. $)$ | $C_{N}$ |  |  | $C_{A}$ | $C_{m}$ | $C_{N}$ | $C_{A}$ | $C_{m}$ | $C_{N}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $C_{A}$ | $C_{m}$ |  |  |  |  |  |  |  |
| 12 | 0.1439 | 0.0848 | 0.0140 | -0.0115 | 0.0202 | 0.0017 | 0.0113 | 0.0008 | -0.0041 |
| 24 | 0.4018 | 0.0940 | 0.0336 | 0.0510 | 0.0078 | -0.0116 | 0.0366 | 0.0010 | -0.0130 |
| 36 | 0.7405 | 0.1029 | 0.0539 | 0.1159 | -0.0042 | -0.0264 | 0.0682 | 0.0011 | -0.0242 |
| 48 | 1.0791 | 0.1065 | 0.0720 | 0.1670 | -0.0162 | -0.0391 | 0.0936 | 0.0001 | -0.0330 |

Table 7: Computed aerodynamic data for body, canted fin, and bodyflap, Mach 6, perfect gas air.

| $\alpha$ <br> (deg.) | Body |  |  | Canted Fin |  |  | Bodyflap |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $C_{N}$ | $C_{A}$ | $C_{m}$ | $C_{N}$ | $C_{A}$ | $C_{m}$ | $C_{N}$ | $C_{A}$ | $C_{m}$ |
| 12 | 0.1456 | 0.0873 | 0.0143 | -0.0105 | 0.0202 | 0.0013 | 0.0110 | 0.0008 | -0.0039 |
| 24 | 0.3977 | 0.0960 | 0.0339 | 0.0441 | 0.0093 | -0.0100 | 0.0341 | 0.0010 | -0.0122 |
| 36 | 0.7280 | 0.1058 | 0.0550 | 0.1062 | -0.0015 | -0.0242 | 0.0697 | 0.0013 | -0.0247 |
| 48 | 1.0796 | 0.1118 | 0.0720 | 0.1695 | -0.0138 | -0.0393 | 0.1028 | 0.0008 | -0.0309 |

Table 8: Computed aerodynamic data for body, canted fin, and bodyflap, Mach 6. CF 4 gas.
assumptions, and for Mach 6 with the perfect gas air and $C F_{4}$ gas assumptions. For the Mach 10 case, the computed $C_{N}$ values compared well with the tumel data. However, for the Mach 6 case, there were some differences. In the past $C_{N}$ values computed using FELISA had compared well with tumel data. See for example [5]. The differences noticed in the present case could not be explained.

The general trend of the $C_{m} V \mathrm{~V} . a$ curves noticed in the tunnel data are present the computed results. The computed pitching moment values for Mach 6 and 10 compared well with the tunnel data at low angles of attack. At higher angles of attack the tumel data show gradual pitch-up compared to the computed results at both the Mach numbers. This is likely to be the result of flow separation on the upper surface of the canted fin. Flow separation occurs because of the the boundary layer interaction with the trailing edge shock. The present computations are inviscid; hence there is no flow separation. However, the trends of the tumnel data are predicted by the computations.

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## References

[1] Peiro, J., Peraire, J., and Morgan, K., "FELISA System Reference Manual and User's Guide," Technical Report, University College, Swansea, Wales, 1993. NASA CP 3291, May 1995.
[2] Bibb, K.L., Peraire, J., and Riley, C.J.: "Hypersonic Flow Computation on Unstructured Meshes," AIAA Paper 97-0625, January 1997.
[3] Samereh, J., "GridTool: A Surface Modeling and Grid Generation Tool," NASA CP 3291, May 1995.
[4] Prabhu, R.K. and Erickson, W.F.: "A Rapid Method for the Computation of Equilibrium Chemical Composition of Air to 15000 K ," NASA TP 2792, March 1988.
[5] Prabhu, R.K.: "Computational Study of a McDonnell Douglas Single-Stage-to-Orbit Vehicle Concept for Aerodynamic analysis," NASA CR 201606, September 1996.
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