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# ANALYSIS OF THE FLUX AND POLARIZATION SPECTRA OF THE TYPE IA SUPERNOVA SN 2001EL: EXPLORING THE GEOMETRY OF THE HIGH-VELOCITY EJECTA

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#### ABSTRACT

SN 2001el is the rst normal Type Ia supernova to show a strong, intrinsic polarization signal. In addition, during the epochs prior to maximum light, the CaIIR triplet absorption is seen distinctly and separately at both normal photospheric velocities and at very high velocities. The high-velocity triplet absorption is highly polarized, with a di erent polarization angle than the rest of the spectrum. The unique observation allow sus to construct a relatively detailed picture of the layered geom etrical structure of the supernova ejecta: in our interpretation, the ejecta layers near the photosphere (v km s 1) obey a near axial symmetry, while a detached, high-velocity structure (v 18;000 km s $^{1}$ ) with high CaII line opacity deviates from the photospheric axisymmetry. By partially obscuring the underlying photosphere, the high-velocity structure causes a more incomplete cancellation of the polarization of the photospheric light, and so gives rise to the polarization peak and rotated polarization angle of the high-velocity IR triplet feature. In an e ort to constrain the ejecta geometry, we develop a technique for calculating 3-D synthetic polarization spectra and use it to generate polarization pro les for several param eterized con gurations. In particular, we exam ine the case where the inner ejecta layers are ellipsoidal and the outer, high-velocity structure is one of four possibilities: a spherical shell, an ellipsoidal shell, a clum ped shell, or a toroid. The synthetic spectra rule out the spherical shell model, disfavor a toroid, and nd a best twith the clumped shell. We show further that dierent geometries can be more clearly discrim inated if observations are obtained from several dierent lines of sight. Thus, assum ing the high velocity structure observed for SN 2001el is a consistent feature of at least a known subset of type Ia supernovae, future observations and analyses such as these m ay allow one to put strong constraints on the ejecta geometry and hence on supernova progenitors and explosion mechanisms.

#### 1. introduction

#### 1.1. Spectropolarim etry of Supernova

The geometrical structure of supernova ejecta, as determined empirically from observations, can give important clues as to the nature of the supernova progenitor system and explosion physics. Spectropolarimetry is a crucial tool in constraining the shape of unresolved supernovae. The scattering atmospheres found in supernovae can linearly polarize light. For an unresolved, spherically symmetric system the dierently aligned polarization vectors around the disk will cancel, resulting in zero net polarization. If the symmetry around the line of sight is broken, however, a net polarization can result due to incomplete cancellation of polarization vectors (Shapiro & Sutherland 1982).

The polarization observations of SN 2001elpresented in W ang et al. (2002) (hereafter Paper I) are the rst observations of a spectroscopically normal Type Ia supernova (SN Ia) which show a signicant intrinsic polarization signal. Most previous observations of SN Ia showed no observable polarization, given the signal-to-noise of the observations (W ang et al. 1996). The only other indication of a clear non-zero polarization in a SN Ia was the subluminous and spectroscopically peculiar SN Ia 1999by, which

showed an intrinsic continuum polarization of about 0.7% (Howell et al. 2001). Chem ical inhom ogeneities were also suggested to explain the rather noisy polarization data of SN 1996x (Wang et al. 1997). In addition, strong intrinsic polarization has been measured in all types of core collapse supernovae (Wang et al. 1996).

A non-zero intrinsic polarization m easurem ent indicates that a supernova is aspherical, but using the spectropolarim etry to constrain the supernova geom etry usually requires theoretical modeling. The detailed theoretical studies so far have been con ned to axisymmetric con gurations. Shapiro & Sutherland (1982) rst estimated the continuum polarization expected from an ellipsoidal, electron scattering supernova atm osphere. Ho ich (1991) used a M onte C arlo code to calculate the continuum polarization from several axisym metric con gurations, including an o -center energy source embedded in a spherical electron scattering envelope. Calculations of synthetic supernova polarization spectra have also been performed, but usually only for the ellipsoidal geometries (see however Chugai (1992)). In the past, such ellipsoidal models have done a fair job in tting gross characteristics of the available spectropolam etric observations, for example those of SNe 1987A (Je rey 1991), 1993J (Ho ich et al. 1996) and

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SN 1999by (Howellet al. 2001).

SN 2001el presents an exciting development in that no axially symmetric geometry is able to account entirely for the spectropolametric observations. In particular, we suggest that the supernova ejecta consists of nearly axially-symmetric inner layers (v . 15;000 km s  $^{\rm 1}$ ), surrounded by a detached, high-velocity structure (v . 20;000 25;000 km s  $^{\rm 1}$ ) with a dierent orientation. The analysis of the system therefore requires that we consider the synthesis of polarization spectra for 3-D con gurations.

In this paper we take an empirical approach, and use a param eterized model to try to extract as much model independent inform ation about the high velocity structure in SN 2001el as the observations will perm it. A unique 3-D reconstruction of the geometry is not possible, as this constitutes a kind of ill-posed inverse problem . However, by restricting our attention to various param eterized system s, we can draw some rather general conclusions about the viability of di erent geom etries. In particular, we exam ine the case where the inner ejecta layers are ellipsoidal and the outer, high-velocity structure is one of four possibilities: a spherical shell, an ellipsoidal shell, a clum ped shell, or a toroid. We develop a technique for calculating 3-D synthetic polarization spectra of the high velocity material. The synthetic spectra rule out the spherical shell model, disfavor a toroid, and nd a best twith the clum ped shell.

Geometrical information extracted empirically from spectropolarim etry must eventually be compared to detailed multi-dim ensional explosion models. As of yet, none of the computed explosion models appear directly applicable to SN 2001el. 3-D de agration models of a SN Ia in the early phases have been computed by K hokhlov (2000) and Reinecke et al. (2002). These models show a quite inhom ogeneous chem ical structure, with large plum es of burned m aterial extending into unburned m aterial. So far the calculations only cover the early stages of the explosion, before free expansion is reached. It is possible that at som e point the de agration transitions into a detonation wave (Khokhlov 1991). The detonation may smooth out the inhom ogeneities in the chem ical composition by burning away the unburnt material between the plumes (Ho ich et al. 2002; Khokhlov 2000). It could also introduce a global asym metry if it occurs at an o -center point (Livne 1999). Other possible sources of asymmetry include rapid rotation of a white dwarf progenitor (M aha y & Hansen 1975), and the binary nature of the progenitor system (Marietta et al. 2000).

#### 12. Supernova SN 2001el

M onard (2001) discovered SN 2001el in the galaxy NGC 1448. The brightness of this nearby supernova (m  $_{\rm B}$  12 at peak) m ade it an ideal candidate for spectropolarin etry. Spectropolam etric observations were taken on Sept 25, Sept 30, 0 ct 9 and N ov 9 of 2001. Details on the observations and the data reduction of the spectra analyzed in this paper can be found in Paper I.

In Figure 1a we show the ux spectrum of SN 2001el for the rst epoch (we have removed the redshift due to the peculiar velocity of the host galaxy). The ux spectrum of SN 2001el resembles the normal SN Ia SN 1994d at about 7 days before maximum light, with the expected

P-Cygni features due to Si II, S II, C a II and Fe II (see e.g. B ranch et al. (1993)). The blueshifts of the m inim a of these features can be used to estimate the photospheric velocities of SN 2001el, which for all features are found to be  $v_{\rm ph}$   $\,$  10;000 km s  $^1$ . The only truly unusual feature of the  $\,$  ux spectrum is a strong absorption near 8000 A, which is discussed in detail below .

We concentrate our analysis on the earliest spectrum (Sept. 25), of SN 2001el. A full description of the ux and polarization spectra at all epochs is given in Paper I.

#### 1.3. High Velocity Material in SNe Ia

The most interesting feature of SN 2001el is the strong absorption feature near 8000 A. The absorption has a \double-dipped" pro le, consisting of two partially blended m in in a separated by about 150 A. It seems to be a pure absorption feature with no obvious emission component to the red. The feature is still strong on Sept 30, but has weakened considerably by 0 ct 9. By the Nov 9 observations, the 8000 A feature has virtually disappeared (see Paper I).

Hatano et al. (1999) identi ed a much weaker 8000 A feature in SN 1994D as a highly blueshifted Ca II IR triplet. The double-dipped pro le now visible in the Sept 25 SN 2001elspectrum supports this conclusion. The redm ost line of the triplet ( 8662) produces the red-side m inim um while the two other triplet lines (8542 & blend to produce the blue-side m in im um. The synthetic spectra to be presented in x4 con m that the IR triplet can reproduce the shape of the double m in im um. Unfortunately, the early spectra do not extend far enough to the blue to observe a corresponding high velocity component to the Ca II H&K lines. We have investigated all other potential lines that m ight have caused the 8000 A feature, but none were able to reproduce the feature without producing another unobserved line signature som ewhere else in the spectrum.

Adopting the IR triplet identication for the 8000 A feature, the implied calcium line of sight velocities span the range 18;000 25;000 km s  $^{1}$  . This should be contrasted with the photospheric velocity of 10,000 km s $^{1}$  as measured from the normal SN Ia features in SN 2001el. We therefore make the distinction between the photospheric material, which gives rise to a seem ingly normal SN Ia spectrum (hereafter, the \photospheric spectrum"), and the high velocity material (HVM), which produces the unusual 8000 A IR triplet feature. In the ux spectrum, there is a clear separation between the photospheric triplet absorption at 8300 A and the HVM feature at 8000 A. In the polarization spectrum, the angle and degree of polarization of the 8000 A feature each dier from the photospheric spectrum. Both of these imply a rather sudden change of the atm ospheric conditions in the HVM.

A high velocity CaII IR triplet feature has been observed in other SN e Ia, albeit rarely and never as strong. The premax spectra of SN 1994D (Patat et al. 1996; Meikle et al. 1996), show a similar, but much weaker absorption. The SiII and Fe II lines of these spectra also suggest som ematerial is moving faster than 25,000 km s  $^1$  (Hatano et al. 1999) The earliest spectrum of SN 1990N at day -14 (Leibundgut et al. 1991) has a deep, rounded 8000 A feature, and the spectrum also showed evidence of high velocity

silicon or carbon (Fisher et al. 1997). The 8000 A feature has also been observed in the maximum light spectrum of SN 2000cx (Liet al. 2001). In this case, however, the line widths are narrower and the two minima are almost completely resolved.

In SN 2001el, the only clear-cut evidence for high velocity material seems to be the 8000 A feature. There is no strong Si II 6150 absorption at v > 20;000, although a weak absorption cannot be ruled out because at this wavelength (5880 A) it would blend completely with the neighboring Si II 5958;5979 feature. There is also no clear indication of high velocity Fe II or S II. The blue edge of the Ca II H & K feature on 0 ct. 9 { the rst available spectrum to go far enough to the blue { is at 27,000 km s  $^{\rm 1}$ . The likelihood of this being HVM is suspect because of the strong possibility of line blending. Since the 8000 A feature is the only unam biguous detection of a high velocity material in SN 2001el, we hereafter refer to it as the HVM feature.

Our analysis will focus almost entirely on the 8000 A HVM feature. In x2 we give an introduction to polarization in supernova atmospheres; x3 describes a parameterized model that allows us to generate synthetic polarization spectra, and in x4 we use the model to explore various geometries for SN 2001el. In x5 we consider the signature of each geometry when viewed from alternative lines of sight. The implication of these constraints on the progenitors and explosion mechanisms of SNe Ia's is discussed brie y in the conclusion.

#### 2. supernova spectropolarimetry

#### 2.1. Polarization Basics

The polarization state of light describes an anisotropy in the time-averaged vibration of the electric eld vector. A beam of radiation where the electric eld vector vibrates in one special collaboration where the electric eld vector vibrates with no preferred direction is unpolarized. Imagine holding a polarization liter in front of a completely linearly polarized light beam of intensity  $I_0$ . The liter only transmits the component of electric eld parallel to the liter axis. Thus as the liter is rotated, the transmitted intensity, which is proportional to the square of the electric eld, varies as  $I() = I_0 \cos^2$ .

The light measured from astrophysical objects is the superposition of many individual waves of varying polarization. Imagine a light beam consisting of the superposition of two completely linearly polarized beams of intensity  $I_0$ , and  $I_{90}$ , whose electricely vectors are oriented 90 to each other. If the beams add incoherently, the transmitted intensity is the sum of each separate beam intensity:

$$I() = I_0 \cos^2 + I_{00} \cos^2 (+90)$$
$$= I_0 \cos^2 + I_{00} \sin^2$$
(1)

If the beam s are of equal intensity,  $I_0=I_{90}$ , then the transmitted intensity shows no directional dependence upon { i.e. the light is unpolarized. In this sense, we say that the polarization of a light beam is \canceled" by an equal intensity beam of orthogonal { or \opposite" { polarization. If  $I_0 \in I_{90}$  the cancellation is incomplete, and the beam is said to be partially polarized. The degree of polarization P is defined as the maximum percentage change

of the intensity; in this case:

$$P = \frac{(I_0 - I_{90})}{I_0 + I_{90}}$$
 (2)

The polarization position angle (labeled  $\,$  ) is de ned as the angle at which the transmitted intensity is maximum .

It is tempting to think of the polarization as a (two dimensional) vector, since it has both a magnitude and a direction. Actually the polarization is a percent dierence in intensity, and intensity is the square of a vector (the electric eld). The polarization is actually a quasivector, i.e. polarization directions 180 (not 360) apart are considered identical. The additive properties of the polarization thus dier slightly from the vector case, as evidenced by the fact that the polarization is canceled by another equal beam oriented 90 to it, rather than one at 180 as in vector addition.

In this case, a useful convention for describing polarization is through the Stokes Param eters, I;Q and U, which measure the di erence of intensities oriented 90 to each other. A Stokes \Vector" can be de ned and illustrated pictorially as:

$$I = Q = I_0 \quad I_{90} = 1 + $$$

$$I = Q = I_0 \quad I_{90} = 1 \quad $$$

$$U \quad I_{45} \quad I_{45} \quad \& \quad %$$
(3)

where  $I_{90}$ , for instance, designates the intensity measured with the polarizing liter oriented 90 to a specified direction called the polarization reference direction. To determine the superposition of two polarized beams, one simply adds their Stokes vectors. A fourth Stokes parameter V measures the excess of circular polarization in the beam. Non-zero circular polarization has not been measured in supermova, and no circular polarization observations were taken for SN 2001el; therefore we will not discuss Stokes V in this paper. For scattering atmospheres without magnetic elds, the radiative transfer equation for circular polarization separates from the linear polarization equations, allowing us to ignore V in our calculations (C handrasekhar 1960).

We further de ne the fractional polarizations: q=Q=I and u=U=I. The degree of polarization, P, and the position angle can then be written in terms of the Stokes P aram eters:

$$P = \frac{P}{\frac{Q^{2} + U^{2}}{I}} = \frac{P}{q^{2} + u^{2}}$$

$$= \frac{1}{2} \tan^{1} (U = Q) = \frac{1}{2} \tan^{1} (u = q)$$
(4)

A single plot that captures both the change of polarization degree and position angle over a spectrum is the q-u plot of F igure 2. Each point in this gure is a wavelength element of the spectrum, and for each point we can read o P and at that wavelength much as we would read a polar plot. A coording to Equation 4, the degree of polarization P is given by the distance of the point from the origin, while the position angle—is half that of the plot's polar angle. In this sense q and u can be thought of as the two components of a two dimensional polarization quasi-vector.

#### 22. Polarization in Supernova Atmospheres

The major opacities in a supernova atmosphere are due to electron scattering and bound-bound line transitions. The continuum polarization of supernova spectra is attributed to electron scattering. The line opacity can create features (either peaks or troughs) in the polarization spectra.

To understand the polarizing e ect of an electron scattering, note that an electron scatters a fully polarized beam of radiation according to dipole  $\sin^2$  angular distribution, where is the angle measured from the incident polarization direction. Now unpolarized light can be represented by a superposition of two equal intensity, fully-polarized orthogonal beams. Upon electron scattering, the two dierently oriented beams get redistributed according to dierently oriented dipole patterns; thus in certain directions they are no longer equal and do not cancel. The scattered light is therefore polarized with the percent polarization depending upon the scattering angle between incident and scattered rays:

$$P = \frac{1 - \cos^2}{1 + \cos^2} \tag{5}$$

Light scattered at 90 is fully polarized, while that which is forward scattered at 180 remains unpolarized. The direction of the polarization is perpendicular to the scattering plane de ned by the incom ing and outgoing photon directions.

Deep enough within the supernova atmosphere, the light becomes unpolarized for two reasons: (1) Below a certain radius, known as the thermalization depth, the absorptive opacity dominates the scattering opacity and photons are destroyed into the thermal pool. The energy is subsequently re-emitted as blackbody radiation which, being the result of random collision processes, is necessarily unpolarized. (2) Deep within the atmosphere, the radiation eld becomes isotropic. Because the radiation incident on a scatterer is then equal in all directions, the net polarization of scattered light will cancel.

The polarization of the radiation occurs above the inner unpolarized depth, where the election scattering opacity dom inates and the radiation eld becomes anisotropic due to the escape of photons out of the supernova surface. We call this region the electron-scattering zone. The surface above the electron scattering zone at which point photons have a high probability of escaping the atmosphere, is the supernova photosphere. Form ation of the well-know P-C ygni line proles in supernovae is due to line opacity from material primarily above the photosphere. This region is called the line-form ing region.

Figure 3 illustrates how the polarization of speci c intensity beams emergent from an spherical, pure electron scattering photosphere m ight look. The double-arrows indicate the polarization direction of a beam, with the size of the arrow indicating the degree of polarization (not the intensity). Note the following two facts: (1) The polarization is oriented perpendicular to the radial direction. This follows from nature of the anisotropy of the radiation eld. At all points in the atmosphere (except the center) more radiation is traveling in the radial direction than perpendicular to it. Because the polarization from electron scattering is perpendicular to the scattering plane, the dom inant scattering of radially traveling light will produce an excess of polarization perpendicular to the radial

direction. (2) The light from the photosphere  $\lim b$  is more highly polarized than that from the center. This is because the radiation eld at the  $\lim b$  is highly anisotropic { i.e highly peaked in the outward (radial) direction. In addition, photons scattered into the line of sight from the supernova  $\lim b$ , have generally scattered at angles closer to 90.

If the projection of the supernova along the line of sight is circularly symmetric, as in Figure 3a, the polarization of each emergent specic intensity beam will be exactly canceled by an orthogonal beam one quadrant away. The integrated light from the supernova will therefore be unpolarized. A non-zero polarization m easurem ent dem ands som e degree of asphericity; for exam ple in the ellipsoidal photosphere of Figure 3b, vertically polarized light from the long edge of the photosphere dom inates the horizontally polarized light from the short edge. The integrated specic intensity of Figure 3b is then partially polarized with q > 0. Because an axisymmetric system has only one preferred direction, sym metry demands that the polarization angle is aligned either parallel or perpendicular to the axis of sym m etry, thus u = 0 for the geom etry of Figure 3b.

The e ect of line opacity on the polarization spectrum can be complicated. In general, light resonantly scattered in a line can become polarized in much the same way as described above for electrons. However because random-izing collisions tend to destroy the polarization state of an atom during an atom ic transition, the light scattered from lines in supermova atmospheres is often assumed to be completely unpolarized (e.g. Ho ich et al. (1996) { we discuss this assumption in more detail in x3.4). In ellipsoidal models, it has been shown that the elect of depolarizing line opacity is primarily to create a decrease in the level of polarization in the spectrum (Ho ich et al. 1996). Because SN Ia have more lines in the blue, the polarization in such models typically rises from blue to red.

In general, however, the fact that a line is depolarizing does not mean it necessarily produces a decrease in the degree of polarization in the spectrum. The actual e ect will depend sensitively upon the geometry of the line opacity and the electron scattering medium. For example, suppose the electron-scattering regim e is spherical, but in an outer, detached layer there is an asym m etric clum p of line optical depth, as shown in Figure 3c. Because the line obscures light of a particular polarization, the cancellation of the polarization of the photospheric speci c intensity beam s will not be complete. The line thus produces a peak in the polarization spectrum and a corresponding absorption in the ux spectrum. We call this e ect of generating polarization features the partial obscuration line opacity e ect or just partial obscuration. In the case of Figure 3c, the clum p prim arily absorbs diagonally polarized light, so we expect the polarization peak to have a dom inant component in the u-direction.

A non-axially symmetric supernova is shown in Figure 3d. The electron scattering medium is ellipsoidal, so the continuum spectrum will be polarized in the q direction. The clump of line opacity, which breaks the axial symmetry, preferentially obscures diagonally polarized light so the line absorption feature will be polarized primarily in the u direction. As we see in the next section,

this type of two-axis con guration is a relevant one for SN 2001el.

#### 2.3. The Polarization of SN 2001el

#### 231. Polarization of The Photospheric Spectrum

The q-u plot of SN 2001el is shown in Figure 2. In order to interpret the intrinsic supernova polarization, one must rst subtract of the interstellar polarization (ISP), caused by the scattering of the radiation of aspherical dust grain along the way to the observer. The ISP has a very weak wavelength dependence, (Serkowskiet al. 1975) and therefore choosing the magnitude and direction of the ISP is basically equivalent to choosing the zero point of the intrinsic supernova polarization in the q-u plane of Figure 2. The particular choice of ISP can dramatically a ect the theoretical interpretation of the polarization data (see Leonard et al. (2000); Howell et al. (2001)).

The choice of the ISP that leads to the simplest theoretical description is shown as the green square in Figure 2. In this case the photospheric part of the spectrum (open circles), apart from some scatter, draws out a straight line in the q-u plane { i.e. the degree of polarization changes across the photospheric spectrum but the polarization angle remains fairly constant. This would be the case if all of the photospheric material followed the same axial symmetry. The intrinsic polarization spectrum (i.e. percent polarization versus wavelength) of SN 2001el using this choice of ISP is shown in Figure 1b. The degree of polarization rises from blue to red, as expected in ellipsoidal m odels due to the higher line opacity in the blue. The level of continuum polarization in the red is about 0.4%, and the SiII 6150 line represents a depolarization by about the sam e am ount. M odels of ellipsoidal electron scattering atm ospheres indicate that level of polarization m ay roughly correspond to an deviation from spherical symmetry of about 10% (Ho ich 1991).

Although the square in Figure 2 is favored by sim plicity argum ents, it is preferable to make a direct measurement of the ISP, if possible. At late epochs it is believed that the supernova ejecta becomes optically thin to electron scattering. The intrinsic supernova continuum polarization would then be zero, and the observed polarization due only to the ISP. Paper I estimated the ISP in this way, using observations taken on Nov 9. Assuming the intrinsic supernova polarization is zero at this time, the determined ISP (with an estimated error contour) is shown as the green triangle in Figure 2. A lthough the ISP thus determ ined is not grossly inconsistent with the simplest choice, it seems to indicate that the polarization zero point lies o of the main qualine. If this is true, the angle across the photospheric spectrum is no longer constant. The photo spheric m aterial approximates an axial symmetry, but an o -axis, sub-dom inant com ponent (e.g. a photospheric clum p) must exist to account for the o set of the q-u line.

Because the main purpose of this paper is to explore the geometry of the HVM, not the photosphere, we will simplify our discussion by ignoring any of axis photospheric components. We will assume the polarization zero point of the axially-symmetric component is given by the square and that the photosphere can be approximately modeled as an ellipsoid. Although the paricular ISP choice has important implications for the geometry of the photospheric

m aterial, it does not greatly a ectour analysis of the HVM feature

#### 2.3.2. Polarization of The HVM Feature

The HVM ux absorption feature is associated with a polarization peak in the spectrum (Figure 1b). Unlike the ux absorption pro le, the polarization peak does not show a clear double feature. Although the noise of the polarization spectrum makes it dicult to analyze the line pro le, it appears that a peak due to the red triplet line (8662) is absent or suppressed compared to the blue lines (8498 & 8542).

In Figure 2, the wavelengths corresponding to the HVM feature are shown with closed circles. The HVM polarization angle deviates from the photospheric one, pointing instead mostly in the u-direction. The HVM feature also shows an interesting looping structure { as the wavelength is increased, the polarization moves counterclockwise in the q-u plane. \q-u loops" such as these have been observed before, for example in the H-alpha feature of SN 1987A (Cropper et al. 1988).

The dierent polarization angle of the HVM feature m eans that the geom etry of SN 2001el cannot be completely axially symmetric. The Stokes U parameter changes sign upon re ecting the system about the polarization reference axis (see Equation 3) and therefore must be zero for any system with a re ective symmetry, such as the axially-sym metric system of Figure 3b. The non-zero u-polarization can not solely be a kinematic e ect either, for although the SN ejecta is expanding, the velocity law is supposed to be a spherical, hom ologous one (v / r) which preserves the re ective symmetry. As the supernova expands and evolves the density contours of the system may change as outer layers thin out and revealdi erent parts of the underlying material; however unless the velocity law deviates from homology and shows some preferential direction, the re ective sym metry will always be preserved and we must have u = 0 at all times. In order to get a non-zero u component, we must break the re ective symmetry of the geometry with an o-axis component, such as the clump of Figure 3d.

A natural explanation of the relatively large degree of polarization and change of polarization angle of the HVM feature is partial obscuration of polarized photospheric light, somewhat like Figure 3d. We nd in x4 that this interpretation can also account for the q-u loop. In the next section we describe a technique for calculating partial obscuration that allows us to directly compare synthetic polarization spectra to the data. O therm echanisms could presum ably be invoked to explain the HVM polarization peak, but in this paper we only consider the e ects of partial obscuration.

#### 3. the two-component polarization model

To compute polarization in multi-dimensions most investigators have employed Monte Carlomethods (Code & Whitney 1995; Wood et al. 1996; Ho ich 1991). This approach has the bene ts of generality and ease of coding, but with the drawback of extreme computational expense. A very large number of photons must be followed to escape along each line of sight in order to overcome the random Poisson noise. This noise must be kept much less than

a fraction of a percent in order to confront the small observed polarization levels. It is therefore cum bersome to use M onte C arlo codes in a parameterized way to explore the huge parameter space available with 3-D geometries.

In the case of the HVM , a sim pli cation is possible that allows for a much faster and more insightful computation. A ssum ing that the electron densities in the HVM regime are around  $10^7\,\mathrm{cm}^{-3}$ , the optical depth to electron scattering through the HVM shell is  $_{\mathrm{es}}$  =  $n_{\mathrm{e}}$   $_{\mathrm{t}}R_{\mathrm{sh}}$  =  $10^{-3}$ . Therefore one can ignore electron scattering in the HVM and the radiative transfer problem separates naturally into the two regimes of photosphere and HVM . The photosphere acts as a source of polarized light illuminating a region of basically pure line optical depth in the HVM . A ssuming the lines are depolarizing, the only elect of the HVM is to obscure some of the polarized photospheric light and re-emit some unpolarized light into the observer's line of sight.

Because the model makes a sharp distinction between an inner polarized source (the photosphere) and an outer line-form ing region (the  ${\tt HVM}$  ), we call this approach the two-com ponent model. The model is basically a way to formalize the simple pictures of Figure 3. The two-component model is constructed to apply to the detached layers of the HVM . For line form ing material near the photosphere a sharp separation of the two regimes would be articial since electron scattering is not entirely negligible in the line form ing region. Because the two-component model does not account for the multiple scattering between lines and electrons, photospheric spectra synthesized with it may be incorrect. On the other hand because the model captures som e of the essential features of various geom etries, som e qualitative insight may still be gained with respect to the lines formed near the photosphere. As we are only concemed with the HVM in this paper, this is not relevant for the present work.

#### 3.1. The Sobolev Approximation

The Sobolev approximation is a method for computing line formation in atmospheres with large velocity gradients. Sobolev models (under the assumption of a sharp photosphere plus line forming region) have frequently been used to analyze supernova ux spectra. Typically sphericalsymmetry is assumed (e.g. (Branch et al. 1983; Hatano et al. 1999)) but the method has also been applied in 3D (Thomas et al. 2002). Derivations of the Sobolev method and justication of the approximation in the modeling of supernova atmospheres can be found in (Rybicki & Hummer 1978; Castor 1970; Je ery & Branch 1990); here we only quote the important results.

The geometry used in the models is shown in Figure 4. We use a cylindrical coordinate system, (p; ;z) or alternatively a Cartesian one (x;y;z). In either case the observer line of sight is chosen as the z axis with z decreasing toward the observer (i.e. the observer is at negative in nity). The polarization reference axis is chosen to lie along the = 0 (or y) direction, which is also the photosphere symmetry axis.

For atm ospheres in general expansion, such as supernovae, the wavelength of a propagating photon is constantly redshifting with respect to the local comoving frame of reference. The insight behind the Sobolev ap-

proximation is that the photon will only interact with a line in the small region of the atmosphere where the photon is Doppler-shifted in resonance with the line. The radiative transfer problem then becomes localized to such \resonance regions". Free expansion is established in supernova atmospheres shortly after the explosion; the velocity vector at a point in the atmosphere is in the radial direction and is given by  $v = (r r_0) = t\hat{r}$ , where r is the radius at time t since explosion, and  $r_0$  is the initial radius which is usually small and can be ignored. Consider a beam of radiation em anating from the photosphere and propagating through this atmosphere in the z direction, at an impact parameter p and azim uthalangle. Such a beam was illustrated pictorially as a double-arrow in Figure 3; here we quantify it with a Stokes speci c intensity vector  $I_0$  ( ;p; ). If the wavelength of the beam in the observer fram e is , then the wavelength in the local com oving atm osphere fram e is given by the (non-relativistic) Doppler formula:

$$_{loc} = 1 + \frac{\forall \hat{z}}{c} = 1 + \frac{z}{ct}$$
 (6)

Suppose the only opacity in the atm osphere is due to one line with rest wavelength  $_0$ . A beam of radiation will come into resonance with the line when  $_{\rm loc} = _{0}$ , which by Equation 6 is at a point:

$$z_r = ct(_0 = 1)$$
 (7)

For each wavelength in an observed spectrum there is thus a unique point in the z-direction at which the beam comes in resonance with the line. A coording to the Sobolev approximation, the emergent Stokes special intensity I that reaches the observer at in nity after passing through the line forming region is given by:

I( ;p; )= I $_0$ ( ;p; )e + (1 e)S( ;p; ;z $_r$ ) (8) where is the Sobolev line optical depth at the point (p; ;z $_r$ ) and S is the Stokes source-function of the line at this point. B oth quantities will be explained further in the sections to come. The rst term in Equation 8 represents photospheric light attenuated by the line optical depth; the second term represents light scattered or created to emerge into the line of sight by the line. Equation 8 is identical to the usual, unpolarized expression for the Sobolev approximation (see Rybicki & Hummer (1978)), except now the terms in boldface are all Stokes vectors.

To generate the observed spectrum of an unresolved object, the speci c intensity of Equation 8 m ust be integrated over the projected surface of the atmosphere, i.e. over the plane. A wavelength in the observed spectrum thus gives us information about the line optical depth and source function integrated over a plane at  $z_{\rm r}$ . Such a plane, which is perpendicular to the observer's line of sight, is called a constant-velocity (CV) surface.

In the case of an monotonically expanding atmosphere with more than one line, a beam of radiation will come into resonance with each line one at a time, starting with the bluest line and moving to the red. In this case Equation 8 is readily generalized:

I(;p; ) = I<sub>0</sub>(;p; ) exp 
$$x^{N}$$

$$\downarrow^{i=1}$$
+  $S_{i}(;p;)[1 e^{i}]exp$ 

$$\downarrow^{i=1}$$
(9)

where the indices i and jrun over the lines from red to blue. Before considering the integration of E quation 9 over the CV planes, we discuss in m ore detail the term s  $\rm I_0$ , S, and

#### 32. The Photospheric Intensity

In this section we calculate the intensity and polarization of speci c intensity beam sem ergent from an electron scattering photosphere. We rst consider  $\rm I_0$  (p; ) in the case that photospheric regime is spherical (as in Figure 3a) and later show how to adapt the result to the ellipsoidal case. From the circular symmetry, the intensity and degree of polarization of a speci c intensity beam can only depend upon the impact parameter p and not on . Let  $\rm I_z$  (p) represent the speci c intensity in the 2 direction at p, and  $\rm P_z$  (p) the degree of polarization of this beam . The polarized speci c intensity is  $\rm I_z$  (p)P\_z (p) which will be divided between the Q and U Stokes parameters.

For = 0, the polarization points in the horizontal, or negative Q direction { i.e. Q (p; = 0) =  $I_z$  (p)P $_z$  (p) while U (p; = 0) = 0. The Q and U components at arbitrary are derived by rotating this expression by . The resulting Stokes vector is:

$$I_{0} = \begin{array}{ccc} & & & & & & & \\ & I_{0} & & & & & \\ I_{0} = & Q_{0} & = & P_{z} (p) I_{z} (p) \cos(2) & & \\ & U_{0} & & P_{z} (p) I_{z} (p) \sin(2) & & \end{array}$$
(10)

The fact that the trigonom etric rotation terms depend on 2 rather than rejects the fact that the polarization is actually a quasi-vector (Chandrasekhar 1960).

In the two-component model one must pre-compute the functions  $I_z$  (p) and  $P_z$  (p). Chandrasekhar rst obtained the result for a pure electron scattering, plane-parallel atm osphere (C handrasekhar 1960); in that case  $I_z$  (p) follows closely the linear limb darkening law, while the degree of polarization P, (p) rises from zero in the center to 11:2% at the limb; however, the plane-parallel approximation is not a good one for supernovae, which have extended atm ospheres (i.e. the thickness of the electron scattering zone is a sizable percentage of its radius). In an extended atm osphere the radiation eld tends toward a more anisotropic distribution, peaking in the outward direction. This increased anisotropy of the radiation eld leads to generally higher limb polarizations. Cassinelli & Hummer (1971) solved the polarized radiative transfer Equation for extended, spherical electron scattering spheres with density power laws of index n=2.5 and n=3. They nd the polarization can become higher than 50% at the limb.

We model the photospheric regine as an inner unpolarized boundary surface, surrounded by a pure electron scattering envelope with a power law electron density / r  $^{\rm n}$ . We choose n = 7, a density law motivated by SN Ia explosion models and one that has been often used in direct spectral analysis (Nomoto et al. 1984; Branch et al. 1983). The optical depth (in the radial direction) from the inner boundary surface to in nity is set at  $_{\rm es}$  = 3. The assumption of a pure electron scattering atmosphere should be a good one for the wavelength range we are interested in. The photons that redshift into resonance with the high velocity IR triplet are those with wavelengths from 8000-8500 A, and there are no strong lines or absorptive opacities in this region of the spectrum (see P into & Eastman (2000)). At other wavelengths the presence

of additional opacities in the photospheric regime will decrease the polarization from the pure electron scattering results presented here.

U sing a M onte Carlo code, we computed the functions  $I_z$  (p) and  $P_z$  (p) for the above scenario. Unpolarized photons were emitted isotropically from the inner boundary surface. The polarization of these photons were tracked as they scattered multiple times through the electron scattering zone. Photons that were back-scattered onto the inner boundary surface were assumed to be re-absorbed and were om itted from the calculation. The M onte Carlo code used in this calculation is a new one developed to further study supernova polarization in cases where the twocom ponent model is not applicable. A detailed description of the M onte Carlo code will be presented in a future paper. We note that the output has been checked against the results of Chandrasekhar (1960) and Cassinelli & Hummer (1971), and several other cases including Hillier (1994) and the analytic results of Brown & McLean (1977).

The computed functions  $I_z$  (p) and  $P_z$  (p). are shown in Figure 5. Here p is given in units of the photosphere radius, de ned as the radius at which the optical depth to electron scattering equals 1. The intensity and polarization for p < 1 do not dier much from the plane-parallel case, with  $P_z = 13\%$  at p = 1. The photospheric speci c intensity does not, however, term inate sharply at the photospheric radius as is usually assum ed in Sobolev models; rather a signi cant am ount of light is scattered into the line of sight out to p 1:4. Since this limb light is highly polarized (up to 40%) it is important to include it in our calculations. Actually most of the polarized ux com es from an annulus at the edge of the photosphere.  $I_z$  (p) has become negligible out at the HVM distances of 2, which con m s that we can make a clear separation between the photospheric and HVM regimes.

In Figure 5 we also compare the n = 7;  $_{\rm es}$  = 3 results to other models with di ering density laws and optical depths. From the similarity of the n = 7 and n = 5 models in Figure 5a and 5b it is clear that the calculations will not depend sensitively on our choice of power law index. Even if the index were as low as n = 3, (or worse, not even described by a strict power law) the behavior of  $I_z$  (p) and  $P_z$  (p) should still show the same qualitative trends. From Figure 5c and 5d we see the results also do not depend much on  $_{\rm es}$  as long as  $_{\rm es}$  & 3.

The results given so far have not taken into account the asphericity of the photosphere in SN 2001el. One could redo the M onte C arb calculations for various axisym m etric con gurations, but the small degree of polarization in SN 2001el suggests a rather small ( 10%) deviation from spherical sym m etry, so it is not a bad approximation to apply the spherically sym m etric specic intensities to a slightly distorted photosphere. This technique of using spherical results to calculate the polarization from distorted atmospheres has been used, in various manners, by many other authors (Shapiro & Sutherland 1982; M cC all 1984; Je rey 1991; C assinelli & H aisch 1974).

In our models we will only consider the case of an oblate ellipsoidal atmosphere with axis ratio E and viewed edgeon. We do not an ellipsoidal coordinate:

$$= p \frac{1}{x^2 + E^2 y^2}$$
 (11)

Our approximation is that the emergent Stokes inten-

sity from a position ; is given by Equation 10 with  $I_z$  (p = ; = ) and  $P_z$  (p = ; = ). In this case we not an axis ratio of E 0.9 is necessary to produce the 0.4% polarization observed in the red continuum of SN 2001el. This result agrees with previous, 2-D calculations (Je rey 1991; Ho ich 1991).

W hile the above photospheric model provides a simple and rather general description of an axially symmetric photosphere, there is no easy way to assure ourselves that this photospheric model is unique. The actual speci c intensity emergent from an ellipsoidalatmosphere can depend on the depth and shape of the inner boundary surface, as well as the inclination of the system . Moreover, the polarization of the photospheric spectrum of SN 2001el could arise from a dierent kind of asphericity altogether, for instance an o-center N i $^{56}$  source, or a clumpy atmosphere. In the absence of a single preferred photospheric model, we proceed with the above model, but reiterate that it remains just one of many possible scenarios. O ther choices of  $\rm I_z$  (p; ) and  $\rm P_z$  (p; ) must be investigated on a case by case basis.

#### 3.3. The Line Optical Depth

In our synthetic spectra ts, we take the optical depth of the 8542 line, as a free parameter  $_1$ . The optical depths of the other two lines (8662, 8498) are derived from  $_1$ . All three triplet lines come from nearly degenerate lower levels, so in LTE the relative strength of each line depends only upon the weighted oscillator strength gf of the atom ic transition. Even if the level populations deviate from LTE, one expects the deviation to a ect each of the nearly degenerate levels in the same way. The 8542 line has the largest gf value; 8662 is 1.8 times weaker, and 8498 10 times weaker.

#### 3.4. The Line Source Function

The line source function represents light scattered by the line, created from the thermal pool or from NLTE effects. Scattering in a line can polarize light { as in the case of electron scattering, the e ect is due to the anisotropic redistribution of the di erent polarization directions. The angular redistribution depends in general on the angular momentum J of the upper and lower levels of the atom ic transition.

Ham ilton (Ham ilton 1947) has considered the linear polarization from a resonance line, free from collisions. He showed that the angular redistribution function from such a line could be written as the sum of an isotropic and dipole term, the relative contributions depending upon the angular m om entum of the transition levels. The dipole contribution has exactly the same polarizing elect as an electron scattering, while the isotropic contribution is unpolarized. The nalpolarizing e ect is thus generally diluted as com pared to the electron scattering case, and can be described by a polarizabilty factor W 2, which varies from 0 for a depolarizing line to 1 for a line that polarizes like an electron (Sten o 1994). Because the Ham ilton approach provides a simple prescription for estimating the intrinsic polarizing e ects of line scattered light, it has often been used outside its scope to calculate polarized line pro les for nonresonance lines (Je rey 1991).

The Hamilton prescription does not take into account

the e ect of collisions. A firer a photon has excited the atom, the atom is in a polarized state with a speci c m agnetic sublevelM. If the collisional time escale is shorter than the lifetime of the transition, collisions will destroy the polarization state of the atom by redistributing the atom over all the nearly degenerate magnetic sublevels, thereby producing an spherically symmetric conguration. The scattered light will thus be isotropic and unpolarized. This is the assumption made in the models of Howellet al. (2001) (and references therein).

In this paper we use exclusively an isotropic, unpolarized line source function. In addition to the depolarizing e ect of collisions, we suggest two further reasons why the e ect of intrinsic line polarization is likely a small e ect in the case of the HVM feature. (1) If we evaluate the polarizability factor for the lines of the IR triplet we nd that W  $_2$  is almost zero for 8542 (W  $_2$  = 0:02) and exactly zero for 8662. A coording to the Hamilton prescription, only the 8498 line has a moderate polarizing e ect  $(W_2 = 0.32)$ , but this line is by far the weakest of the three. Note however that since the IR triplet lines are not resonance lines, the Hamilton prescription does not strictly apply and complicated NLTE polarizing e ects could be operative (Trujillo Bueno & Manso Sainz 1999). (2) For optically thick lines, photons will multiple scatter within a resonance region before escaping. On average the number of scatters in the resonance region is given by N =  $1=P_{\rm esc}$ where the escape probability  $P_{\rm esc}$  is given by the Sobolev form alism:

$$P_{esc} = \frac{1 - e}{1 - e} \tag{12}$$

This multiple scattering has two depolarizing e ects: (1) the radiation eld in the line tends toward an isotropic distribution (2) the probability of the destruction of a photon into the therm alpool will be increased. For optically thick lines the line-scattered light will then tend to be unpolarized. On the basis of the spectral ts of x4, we will argue that the lines of the IR triplet are saturated ( $_1\ \&\ 5$ ) for the HVM in front of the photosphere and thus largely unpolarized.

For an isotropic, unpolarized source function the Stokes vector is:

$$S = \begin{array}{ccc} S_1 & S_0 &$$

where  $S_0$  is the unpolarized source function. The actual value of  $S_0$  requires a full NLTE computation of the atom ic levels. For our purposes a useful param eterization is:

$$S_0 = (1 {}^{0})J + {}^{0}B (T)$$
 (14)

The rst term represents in pinging light scattered by the line, and so depends upon the mean local radiation eld in the line J; the second term represents light created from the thermal pool and so depends upon the Planck function B and the temperature T. The relative importance of the two factors is governed by  $^{\rm O}$ , the probability a photon is destroyed into the thermal pool on traversing the resonance region of a line. In the Sobolev approximation  $^{\rm O}$  is given by:

$$^{0} = \frac{1}{P_{esc} + (1 - P_{esc})}$$
 (15)

where is the usual static atm osphere destruction probability. In NLTE models of supernova atm ospheres one nds between 0.05 and 0.1 (Nugent 1997). Note as the probability of a photon's escape ( $P_{\rm esc}$ ) decreases, the chances that it gets them alized ( $^0$ ) increases.

For the value of J in the HVM, we use the radiation incident from the photosphere, ignoring multiple scattering of photons between the triplet lines (for a discussion of this approximation, see Thomas et al. (2002)). The photospheric radiation in the HVM is geometrically diluted by a factor of roughly  $r_{\rm ph}^2=4$   $r_{\rm H~V~M}^2$  1=16. Thus for a pure scattering line (  $^0=$  0), the intensity of the line source function is about 16 times weaker than the average photospheric intensity. At the other extreme, for a thermalized line (  $^0=$  1) and an HVM temperature of 5500 K, the line source function is about 4 times weaker than the average photospheric intensity.

Because the line source function light is unpolarized and relatively weak, we not in the end that it has little a ect on the synthetic line pro les. The exact value of is thus not of great in portance. In our models, we use = 0.01.

#### 3.5. The Integrated Spectrum

To obtain the observed Stokes uxes at a certain wavelength one must integrate the speci c intensity over the CV planes of each line. For those CV planes behind the photosphere, we must also account for the attenuation of the line source function light due to scattering o electrons as the beam passes through the photospheric region. If we de ne  $_{\rm es}$  (p; ;z) as the electron scattering optical depth along the z-direction from the point (p; ;z) to the observer, then a fraction (1 e  $^{\rm es}$ ) of photons will be scattered out of the line of sight on their way to the observer. We assume these photons are simply removed from the beam and are not subsequently re-scattered into the line of sight.

For a single line atm osphere, the integrated Stokes uxes at wavelength correspond to material from the CV plane  $z_{\rm r}$  and are given by:

$$F_{I}() = I_{z}(p; )e + \\ (1 e)S_{0}(p; ; z_{r})e \stackrel{es}{=} pdpd \\ Z Z \qquad (16)$$

$$F_{Q}() = P_{z}(p; )I_{z}(p; )cos(2)e pdpd \\ Z Z$$

$$F_{U}() = P_{z}(p; )I_{z}(p; )sin(2)e pdpd$$

The integrals can be easily generalized for the case of multiple lines by applying Equation 9.

G iven our scenario of how the high velocity C aII polarization is formed by partial obscuration, Equations 16 give us some insight into what extent the HVM geometry is constrained by the polarization measurements. For simplicity, consider the formation of a single, unblended line, above a spherical photosphere, and suppose we are trying to reconstruct the distribution of Sobolev line optical depth (p; ;z) over the entire ejecta volume. The Stokes ux at a certain wavelength gives us information about over the corresponding CV plane at  $z_{\rm r}$ . As Equations 16 demonstrate we obviously will not be able to uniquely reconstruct the distribution of over this plane, because all of the information gets integrated over to give the three

quantities we measure:  $F_{\rm I}$  ( );  $F_{\rm Q}$  ( ), and  $F_{\rm U}$  ( ). What we do measure can be thought of as certain \moments" of the distribution over each CV plane.  $F_{\rm I}$  is a type of \zeroth m oment", which depends mostly upon how much material is covering the photosphere, with little dependence on its geometrical distribution. On the other hand the  $F_{\rm Q}$  and  $F_{\rm U}$ , because of the cos2 and  $\sin$ 2 factors, behave somewhat like \rstm oments", and are sensitive to how is distributed over the photosphere. Because the angle factors  $\cos$ 2;  $\sin$ 2 are rather low-frequency, smaller scale structures will be averaged out over the integrals, and the polarization measurements will only constrain the large scale structures in the HVM.

Before proceeding with the spectral synthesis calculations let us sum marize the assum ptions that go into the two-component model. (1) The electron scattering opacity in the HVM is negligible. (2) the photospheric regime is reasonably well described by a pure electron scattering, power law atmosphere, surrounding a nite, unpolarized source at  $_{\rm es}$  3. (3) For small (10 percent) deviations from sphericity in the photosphere, the angular dependence of the polarized radiation eld does not deviate signicantly from the spherical results (4) The line source function light is unpolarized (5) Multiple scattering among the triplet lines and between the HVM and photospheric regime can be ignored.

#### 4. the geometry of the high velocity material

The speed of the two-component model allows us to explore many dierent con gurations for the HVM. We report on four possibilities here, each of which may approximate a structure that is the result of some particular physicalmechanism: (1) A spherically symmetric shell (2) An ellipsoidal shell with an axis of symmetry rotated from the photosphere axis of symmetry. (3) A clumped spherical shell (4) A toroidal structure with a symmetry axis rotated with respect to the photospheric axis. The geometry used in the models is shown in Figure 4.

The photosphere is modeled as discussed in x32, as an oblate ellipsoid with axis ratio E = 0:91, viewed edgeon. It is not the purpose of this paper to explore the detailed geometry of the photosphere, therefore the ellipsoidal model was chosen as the simplest possibility that captures the essential features of the axisymmetric photosphere. The photosphere symmetry axis is the y-axis, which is also the polarization reference direction. The photospheric intensity is assumed to follow a blackbody distribution with a temperature  $T_{bb}=9000~{\rm K}$  chosen to the slope of the red continuum. We do not attach any physical signicance to the value of  $T_{bb}$ , but consider it only a convenient tiparameter.

The param eterization of the various HVM geom etries is kept simple and general. The HVM is chosen axially symmetric, with the orientation of the HVM axis dened by the two angles and . The velocities  $\gamma$  and  $\gamma$  denote the inner and outer radial boundaries of the HVM, while is the opening angle (see Figure 4). The reference optical depth 1 of the 8542 line is assumed constant throughout the dened structure boundaries. Although this is an idealization of the real HVM, it allows us to isolate the dening geometrical features of each structure individually. Table 1 summarizes the tted parameters of each

HVM geometry considered in the sections to follow. Before considering the speci c models, we rst discuss the general constraints that must be met by any HVM model.

#### 4.1. General Constraints

Figure 6 is a diagram of the form ation of the CaII IR triplet feature in SN 2001el. The HVM has for illustration been shown as a spherical shell. The atm osphere can be divided into three regions, the high-velocity material in each region having a di erent a ect on the spectrum . (1) The absorption region: Material in the tube directly in front of the photosphere absorbs photospheric light and em its line source function light into the line of sight. Since the line source function intensity is usually weaker than the photospheric intensity, this e ect produces an absorption feature in the spectrum . (2) The em ission region: material in the outer lobes does not obscure the photosphere but only adds line source function light; this produces an em ission feature to the red of the absorption. (2) The occluded region: Material in the tube behind the photosphere is occluded by the photosphere and is not visible.

Because in our models it is the partial obscuration of polarized photospheric light that gives rise to the HVM polarization feature, all of our geom etrical inform ation on the HVM will be about the distribution of CaII in the absorption region. Whether there is any HVM CaII in the emission region, and if so, what its geometry may be, will be very dicult to say. In addition we will have absolutely no information about the material in the occluded region. In the spherical HVM shell of Figure 6, about 5% of the material is in the absorption region, 5% is in the occluded region, and 90% is in the emission region. Thus we only probe a small portion of the potential HVM. We now consider the general constraints of these regions in more detail.

#### 4.1.1. Constraints on the Absorption Region Material

We can list 4 general constraints on the HVM absorption region material that are directly deducible from the Sept. 25 spectra:

- (1) The width of the HVM ux absorption feature constrains  $_1$  to be non-zero only over the line-of-sight velocity range 18;000  $_2$ 5;000 km s  $_1$   $_1$  is thus conned to a relatively thin region that is signicantly detached from the photosphere. The edges of the ux feature are sharp, suggesting that the boundaries of the HVM are well-dened.
- (2) At them inimum of the HVM absorption the ux has decreased by 43% from the continuum level. For geometries where the HVM covers the entire photosphere, the optical depth in plied is  $$3.0\,\mathrm{n}$  the other hand, some geom etries may have higher optical depths and smaller covering factors, the minimal covering factor being  $f_\mathrm{min}=43\%$  for when the lines are completely opaque. Note that in this context the term \covering factor" denotes the percent of the photospheric area obscured by the slice of HVM on a plane perpendicular to the line of sight, corresponding to the resonance surface of a certain wavelength. Since this diers from the traditional usage of the term, we hereafter call this the z-plane covering factor.

We can use the double-dipped ux pro le to constrain the z-plane covering factor of the HVM. Because the 8542 blue triplet line is intrinsically stronger than the 8662 red triplet line (with a gf value 1.8 times larger), the blue minima of the IR triplet feature will be about twice as deep the red one unless both lines are saturated. Because the minima in the HVM feature are of about equal depth, we conclude that the two lines are indeed saturated (i.e.  $_{\rm l}$  & 5) and the z-plane covering factor is in fact the minimal one,  $f_{\rm min}=43\%$ .

- (3) The shape of the ux pro lem ay also constrain the value  $_1$ . Note that two minima in the ux pro le have roughly equal widths. On the other hand if all three triplet lines are saturated the blue minima will tend to be wider than the red, due to the blending of the 8498 with the 8542 line. This suggests that the 8498 line is weak while the other two lines are strong, a situation that occurs when  $_1$  5.
- (4) Finally, the HVM polarization feature points primarily in the u-direction. This means the distribution of the HVM is weighted along the 45 line to the photosphere symmetry axis.

#### 4.12. Constraints on the Emission Region Material

The material in the emission region may be observable as a ux emission feature to the red of the HVM absorption. If, for example, the HVM was a spherical shell, this emission feature would extend from about z = to z = 20;000, or over 1000 A. The emission from a shell is then very broad, but because the line source function is much less than the photospheric intensity, the feature is typically weak and dicult to detect in the spectrum. A serious problem, evident from Figure 6, is that the HVM em ission feature overlaps with the photospheric triplet absorption and emission, making it dicult to separate the two contributions. Only for the HVM material with z & 15;000 (i.e. > 8700 A) is the HVM emission feature not blended with the photospheric. Unfortunately the available spectra of SN 2001eldo not extend that far to the red.

The em ission region material also a ects the polarization level by diluting the photospheric light with unpolarized line source function light, thus creating a depolarization feature in the spectrum. O fcourse this depolarization feature gives no additional clue as to the orientation of the em ission region material, as the unpolarized line light carries no directional information. The polarization spectrum of SN 2001el does have a signicant depolarization to the red of the HVM peak, but since the overlapping photospheric triplet feature may also depolarize at these wavelengths, it is again not easy to use this to directly constrain the HVM em ission region material. In our models, we do not attempt to the region redward of 8200 A, where the HVM feature is blended with the photospheric feature.

We not that the red em ission/depolarization feature is not a very sensitive diagnostic of em ission region material. The elect on the spectrum is shown in Figure 7 for a spherical shell with various values of the destruction probability. For a pure scattering line ( = 0) the em ission is hardly visible. For the thermalized line ( = 1) and a temperature T = 5500K, the em ission would be substantial but dicult to separate from the photospheric component. A value = 1 is also unlikely for supernova atmospheres; NLTE models and 0:05.

The best way to constrain the amount of emission region material is by line of sight variations (see x5). Them aterial in the emission region from one line of sight, becomes material in the absorption region from another. With a larger sample of supernovae one may be able to piece together a picture of the entire volume of high velocity ejecta.

#### 42. Spherical Shell

The rst HVM geometry we consider is a spherically symmetric shell. We take the boundaries of the spherical shell to be  $v_1=20$ ; 200 km s  $^1$  and  $v_2=25$ ; 300 km s  $^1$  in order to reproduce the line width. Because the shell curves around, these dimensions actually give an extension in the z-direction of 18;000 25;000 km s  $^1$ , consistent with constraint (1) of x4.1.1. The z-plane covering factor is found to be 1, and the optical depth necessary to the line depth  $_1=0$ :77.

The triplet lines are not saturated in the spherical shell, so the model does not satisfy constraint (2) of x4.1.1 and willnot well reproduce the ux prole. In Figure 8 we compare the synthetic spectra to the observed data. While the overall tof the ux feature is decent, the redside minimum is not well reproduced. We will not better to the double-dipped prole using non-spherical geometries with smaller z-plane covering factors and saturated lines. Thus the ux spectrum alone suggests a deviation from spherical symmetry, although the evidence is rather subtle.

The e ect of the spherical shell on the polarization is demonstrated by the slice plots of Figure 9. At the blue end of the absorption feature (slice a), the line obscures the weakly polarized, central light, allowing highly polarized, edge light to reach the observer. This creates a peak in the polarization spectrum. Further to the red of the feature (slice b), the line obscures the edge light and thus depolarizes the spectrum. Even further to the red (slice c), the line no longer obscures the photosphere, but the emission region materialem its unpolarized line source function light into the line of sight, and a small level of depolarization continues. This polarization feature resembles an inverted P-Cygnipro le, as discussed by Je rey (1989).

In Figure 8b we see that the spherical shell naturally reproduces the correct shape and size of the HVM polarization peak. The fact that the synthetic polarization feature has only a single peak is the result of a line blending e ect: the red-side depolarization of the 8542 feature suppresses the peak due to the 8662 line. Note that while the observed depolarization minimum near 8400 A is not well t, this is not necessarily a weakness of the model. As discussed in x412 the feature at these wavelengths is produced mostly by the calcium near the photosphere, which has not been included in the model. In any case, the spherical shell, which follows the axial symmetry of the photosphere, does not change the polarization position angle as is observed (Figure 8c). This rules it out as a potential model for the HVM.

#### 4.3. Rotated Ellipsoidal Shell

The good to the polarization level in Figure 8 suggests that a shell-like structure may be a viable candidate for the HVM, as long as the shell is somehow distorted from perfect spherical symmetry to account for the rotation of the HVM polarization angle. The simplest scenario is one

where the HVM layers of the ejecta are ellipsoidal with the same oblateness as the photospheric layers, but with a rotated axis of symmetry. Exactly how such a relative rotation of the outer layers could arise from an SN Ia explosion is not obvious. One might envision that the rapid rotation of a white dwarf progenitor coupled with a deagration to detonation transition at an orangement. (Livne 1999) could produce something like this geometry.

The e ect of the rotated ellipsoidal shell on the polarization spectrum is demonstrated in the slice plots of Figure 10. The slices closely resemble those of the spherical shell (Figure 9) except that now the cross-sections of the HVM are ellipses. The shape and size of the ux and polarization features are thus very similar to the spherical case. For = 0 (HVM and photosphere axis aligned) the system is axially symmetric and the HVM polarization feature points in the q-direction. As is increased, the ellipses begin to absorb diagonally polarized light and the HVM polarization feature rotates into the u-direction.

The synthetic spectra for = 25;  $_1 = 0.77$  are shown in Figure 11. The ellipsoidal shell, like the spherical one, fails to meet constraint (2) and does not reproduce the double-dipped ux pro le. This problem cannot be xed by changing the ellipticity of the shell. On the other hand, the ellipsoidal shell is able to the polarization peak and the change of polarization angle.

Even more interestingly, the ellipsoidal shell produces a q-u loop sim ilar to that observed in the data. In our models, we not that a q-u loop is a common signature of partial obscuration in two-axis systems. The absorption of the photospheric light typically produces a peak in both the q and u polarization. The partial obscuration e ect on the q and u polarizations is distinct, so that in general these features do not peak at the same wavelength, but rather are out of phase. When plotted in the q-u plane, this phase o set makes a loop.

#### 4.4. Clum ped Shell

We parameterize a clumped shell as the section of the spherical shell lying within a cone of an opening angle (a \bowl" shaped structure, see Figure 4). A single clump like this could perhaps arise if the calcium in the HVM was produced by nuclear burning that occurred along a preferential axis. The clumped shell could also represent one piece of a shell broken into numerous clumps by an instability, a possibility discussed in more detail at the end of this section.

In deciding on the appropriate values for the clump param eters, we are guided by the constraints listed in x4.1.1. The opening angle is constrained to \$25, so as to achieve the m inimalz-plane covering factor (constraint 2). The orientation of the clump axis is chosen so that the clump lies in between the observer and the photosphere, obscuring the photosphere's diagonal (constraint 4).

Through trial and error, a reasonable to the data was found for = 24;  $_1 = 5$ ; = 83.5; = 4.2 The synthetic spectra are shown in Figure 12. Because the lines are now saturated, the clump is able to reproduce the two equal minima of the ux absorption. The clumped shell also reproduces the important features of the polarization spectrum { i.e. the level of polarization, the polarization angle, and the q-u loop. On the other hand, the red edges

of the synthetic ux and polarization spectra do not quite match the observed. In the polarization spectrum, the peak due to the 8662 feature is not suppressed by blending as it was in the shell models. This suggests that our param eterized clump geometry may be too simple and a more realistic model may involve a complicated superposition of clumps and shell.

In the geometry described above, the clump axis was chosen almost, but not quite, perpendicular to the photosphere axis ( = 83.5). One might wonder if the two axes could possibly be orthogonal ( = 90). Such a scenario is permissible if the clump axis remains at an angle = 4.2 to the line of sight and the whole system is rotated to be observed at an inclination i = 90 83.5 = 6.5. One might imagine this geometry as a blob of material that was ejected in the equatorial direction of the ellipsoidal photosphere.

Although our clum ped shellm odel consists of only a single clum p, it is possible that m any m ore clum ps exist in the em ission region of the shell as the extra clum pswould leave no obvious signature on the spectra (see x4.1.2). Clum piness in a shell could be caused by various hydrodynam ical instabilities. The expected scale of such clumpiness is unknown { it could perhaps take the form of a single large clump or it could be in the form of numerous smaller clumps. As we noted in reference to Equation 16 (see x3.5), the polarization feature due to partial obscuration is not sensitive to small scale structure, giving rather the integrated \m om ents" of the optical depth distribution. Thus we will not be able to empirically constrain the small scale structure of the clum piness. We can say two things though: (1) W hatever the size of the clumps, their angular distribution must be weighted along the clump axis de ned above. If the clum pswere instead small structures distributed uniform ly over the shell, when integrated up they would average out to the uniform spherical shell analyzed in the previous section, which did not show a rotation of the polarization angle. (2) This weighted angular distribution of the clum ps cannot vary in the radial direction. If it did, the polarization angle of the HVM feature { which is set by however the random ly placed clum ps happen to be distributed over the photosphere { would vary random ly across the HVM feature rather than forming a q-u loop oriented in the u-direction. Both of these suggest that the scale of the clum piness is not much smaller than the single clump used in the model.

#### 4.5. Toroid

A toroid would be an especially interesting structure to nd in the ejecta of a SN Ia, as it m ight give a hint as to the binary nature of the progenitor system. In the currently preferred progenitor scenarios (see Branch et al. (1995)), SN e Ia are the result of a white dwarf accreting m aterial either from the Roche-lobe over ow of a companion star or the coalescence with another C-O white dwarf. The orientation of the accretion disk axis naturally suggests an independent orientation of the outer ejecta layers, and this could provide a natural explanation why the HVM of SN 2001el deviates from the photospheric axis of symmetry.

W hether an accretion disk could maintains a toroidal structure after the supernova explosion can only be addressed by multi-dim ensional explosion modeling. Here we can calculate what e ect such a structure would have on the ux and polarization spectrum, and whether it could possibly account for the HVM feature in SN 2001el. We parameterize the toroid as the ring of a spherical shell lying within opening angle (see Figure 4).

We rst consider a system where the toroid is observed edge-on. We set  $\,=\,30$ , giving the m in in al z-plane covering factor, and  $_1=\,5$ . We orient the torus axis at  $\,=\,45\,$  to preferentially absorb the diagonal light. The results are shown in Figure 13. The ux feature is a good m atch to the double-dipped pro le, but the polarization peak at 5% is much too large. The reason is clear from the slice plot in Figure 14 { the edge-on toroid, which occludes opposite sides of the photosphere, is very elective at blocking light of a particular polarization.

A good t to the polarization feature can still be sought by changing the inclination of the toroid. As the inclination is increased, the toroid rotates of the photodisk and both the fux and polarization feature decrease. The boundaries of the toroid and the opening angle must then be readjusted to properly to the fux feature. In the present model a perfect to cannot be found for any inclination. For all cases where the feature is well to the polarization feature is too strong. A compromise to is shown in Figure 15. Here  $v_1 = 20;500$ ,  $v_2 = 24;750 = 45$ ,  $v_3 = 43$ , and  $v_4 = 35$ . The feature is too weak, and the polarization too strong.

#### 5. the high velocity material from other lines of sight

P revious discussions have pointed out that several different geom etrical con gurations are capable of providing reasonable ts to both the ux and polarization HVM features. The degeneracy problem is two-fold: (1) Dierent distributions of absorbing material in front of the photosphere can lead to similar polarization features (see the discussion in x3.5) (2) There is no strong diagnostic of the amount and distribution of material in the emission region (x4.1.2). In this section we consider how the degeneracy problem can be overcome by observing the HVM from multiple lines of sight.

One diculty in exploring line of sight variations is that the num ber of possible con gurations in a two-axis system is enorm ous. Even holding the boundaries of the HVM xed, we still have as free parameters the angle between the photosphere and HVM symmetry axis and two angles specifying the line of sight. There is no easy way to catalog all the possibilities. Therefore to keep the discussion simple and general, in the following calculations we choose the underlying photosphere to be spherical. The HVM axis can then be aligned in the z-y plane (i.e. = 0), leaving as the only free parameter the inclination. The polarization is then in the q direction. Note that in light of Equation 3, a positive q-polarization indicates the net ux is vertically polarized, while a negative q-polarization indicates it is horizontally polarized.

The ellipsoidal shell of x43 shows only subtle variations with inclination (Figure 16). A ux absorption is visible from all lines of sight, with the absorption pro le barely changing with inclination. The only e ect on the pro le is a small shift of the minimum to the red as the short

(ie slow) end of the shell moves into the line of sight. For = 0 (shell viewed edge-on) the polarization is a maximum at 0.8%; this level is comparable to the HVM feature of SN 2001el. As is increased, the polarization feature decreases monotonically. For = 90 (shell viewed pole on) circular symmetry is recovered and the polarization is zero.

The clumped shell of x4.4, on the other hand, shows strong variations with inclination (Figure 17). The ux absorption is deepest for = 90, when the clump is viewed top on, directly in between the photosphere and observer. At this inclination, the system is circularly symm etric and the polarization cancels (the perfect cancellation is of course the unnatural result of our simple \bow |like" clum p param eterization; a m ore irregularly shaped clump would show a small polarization feature). As decreased, the clum p m oves to the edge of the photodisk, where it covers lower intensity, more highly-polarized light. As a result, the ux absorption gets weaker while the polarization feature becom es stronger. A strict inverse relationship holds for the inclinations 90 70 and provides an important signature for the single clump model. For inclinations smaller than 60 the polarization begins to decrease, but still remains much stronger than the ux feature. An especially striking signature occurs for the line of sight = 40. Here the ux feature is barely visible while the polarization feature is strong ( 1%). The observation of this type of feature would clearly rule out an ellipsoidal shell and favor a single clump HVM geometry.

The variety of possible ux pro les from the clumped shell model correspond nicely to the variety of proles that have already been observed in some other supernova. As the inclination is decreased from 90, the clump extends further in the z-direction { the two lines therefore become broader and the two minimamore blended. When the clump is viewed directly on ( = 90), the two minim a are largely resolved, which is not unlike the feature in SN 2001cx (Lietal. 2001). At slightly smaller inclinations 80) we found the best ts to the partially blended ( m in im a of SN 2001el. For = 40 the feature is weaker and the two minima are almost completely blended, resembling the rounded feature of SN 1990N (Leibundgut et al. 1991). For = 20, the feature is very weak and about the depth that it was observed in SN 1994D (Meikle et al. 1996; Patat et al. 1996). Thus the clum ped shell may be a singlem odel capable of reproducing the full range of available observations on the HVM ux feature. More observations are necessary, however, to determ ine if the variety of ux pro les is indeed a line of sight e ect or rather represents individual di erences in the high velocity ejecta.

The most obvious signature of the toroidal geometry (Figure 18) is the high levels of polarization ( 5%) when viewed near edge-on ( = 0). An edge-on toroid occludes vertically polarized light from the edges of the photosphere, giving a polarization feature with q < 0. As the toroid is inclined, the structure rotates of the photodisk and both the fux absorption and polarization peak weaken (in contrast to the clumped shell model). At inclinations greater than 20, the toroid begins to occlude the horizontally polarized light from the bottom of the photosphere ( q then fips sign and becomes positive.

#### 6. summary and conclusions

High quality spectropolam etric observations of supernova may allow us to extract detailed information on the geom etrical structure of the ejecta. Interpreting the polarization observations through modeling is a dicult endeavor, however, largely because of the the enormous number of congurations available in arbitrary 3-D geometries. The huge parameter space and multiple lines of sight make a direct comparison of data and rst principle calculations dicult, not to mention computationally expensive. A parameterized approach is therefore useful in understanding the general polarization signatures arising from dierent geometrical structures. We have taken this approach here and calculated the polarization features expected from several geometries potentially relevant to SN 2001el.

The models computed in this paper highlight the wide range of spectropolam etric features possible when aspherical geometries are considered. Depolarizing line opacity in the supernova atmosphere does not in general produce simple depolarization features in the polarization spectrum. A symmetrically distributed line opacity offen creates a polarization peak by partially obscuring the underlying photosphere. In systems where the line opacity follows a dierent axis of symmetry from the electron scattering medium, the resulting polarization feature generally creates a loop in the q-u plane. The two-component model described in this paper provides a convenient approach for quickly calculating and gaining intuition into the types polarization features arising from partial obscuration.

For the case of the high velocity material in type Ia supernova, partial obscuration will be a dominant e ect on the line features, resulting in large polarization peaks ( 1%) for practically any geometry considered. We have therefore explored to what extent partial obscuration alone can explain the CaII IR triplet polarization peak in SN 2001el. Our picture of the SN 2001elejecta consists of nearly axially sym m etric photospheric m aterial surrounded by a detached, asymmetric structure at high velocity. We have investigated four possible geometries for the HVM: (1) A detached spherical shell is ruled out because it cannot account for the change of polarization angle over the HVM feature. The spherical shell also does not t the shape of double-dipped ux absorption pro le. (2) An ellipsoidal shell, with axis of symmetry rotated from the photosphere symmetry axis, can account for all the general features of the HVM polarization spectrum { the level of polarization, the polarization angle, and the q-u loop. However the ellipsoidal shell, like the spherical one, does not well the shape of the ux absorption prole. (3) A clumped shell, which could represent a single clum p or a piece of a clum py shell, can account for all the general features of the ux and polarization spectra. (4) A toroid, in the present model, produces a polarization

D i erent HVM geom etries can be clearly discrim inated by observing them from varying lines of sight. Depending upon the HVM geom etry, a ux absorption similar to that of SN 2001elwill be observed in SN Ia with dierent frequency. For a shell-like model, the ux signature will be observed from all lines of sight, while for the toroid and clump, only a fraction of the lines of sight produce the signature absorption. Under the assumption that the HVM

feature that is larger than observed.

has a similar structure in all (or at least a known subset) of SN Ia's, it may be possible to constrain the geometry with a statistical sample of early ux spectra. Because the different models leave even more dramatic signatures on the polarization spectra, only a few well-observed supernovalike SN 2001el are needed to discriminate the various scenarios (see x5).

We have not attempted in this paper to constrain the detailed geometry of the photospheric material. Because this material demonstrates a near axial symmetry, we have adopted the simple and general model of an edge-on oblate ellipsoid with a power law electron density prole. The actual photospheric geometry is likely more complicated, and may deviate from a strict axial symmetry. Given a more complicated photospheric structure, one could use the technique described here to calculate the HVM partial obscuration eect. Detailed monte-carlo studies on the structure of the photospheric material are under way; because the overall asymmetry of the photospheric material is rather small, however, our main conclusions about the HVM likely hold even when a more complicated photospheric geometry is used.

Although more observations are necessary to pin down the exact geometry of the HVM, one can begin to speculate as to its origin. Two questions in particular must be addressed: Why is the HVM feature geometrically detached from the photospheric material? And: Why does the HVM deviate from the dominant axis of symmetry of the photospheric material?

The detachment of the HVM indicates that the atmospheric conditions change rather suddenly at high velocity. Three possible changes (or a combination thereof) could result in an HVM feature (see Hatano et al. (1999)): (1) A spike in the overall density in the HVM: In the SN Ia deagration modelW 7, the material at high velocity consists of unburnt carbon and oxygen with a solar abundance of calcium. The densities of these layers during the epoch in question are too low to produce an optically thick Ca II IR triplet. NLTE models (Nugent et al. 2002) show that { all other things being equal { a density increase at high

velocity of more than an order of magnitude is necessary to produce an HVM feature. (2) A spike in the calcium abundance: For the W 7 densities, the calcium abundance must be increased by  $10^3$  from solar in order to produce an HVM feature (Nugent et al. 2002). This could, for example, be the result of blob of ejecta material that had undergone explosive oxygen burning, which increases the calcium abundance by 104 (K hokhlov et al. 1993) (3) A sudden change in the ionization/excitation of the calcium: The optical depth of the IR triplet is a decreasing function oftem perature (due to the increased ionization of Ca II to C a III). Thus it is possible that a tem perature decrease in the outer ejecta layers could make the IR triplet optically thick at high velocity. However it seems unlikely in this case that this optical depth spike would have sharp geom etrical boundaries that persisted over several epochs of observations, as found for SN 2001el.

The distinct orientation of the HVM as compared to the photospheric material could be (1) the result of random processes in the explosion physics/hydrodynam ics such as Raleigh-Taylor instabilities producing large scale clumpiness or (2) an indication of a preferred direction in the progenitor system. For example, the photospheric dominant axis could represent the rotation direction of the white dwarfwhile the HVM axis could represent the orientation of an accretion disk. Further explosion and hydrodynamical modeling is necessary to assess the plausibility of various scenarios.

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 $\label{eq:table 1} \mbox{Table 1}$  Fitted parameters for HVM models

N am e	v <sub>1</sub> a	v <sub>2</sub> ª	E b	1 °	d	е	е	t– gure
spherical shell	20,200	25 <b>,</b> 300	1.0	0.83	_	_	_	8
ellipsoidal shell	21 <b>,</b> 200	24,800	0.91	1.20	_	25	90	11
clum ped shell	20,600	24,300	1.0	5.0	23	83 <b>:</b> 5	4:2	12
edge-on toroid	20,900	24 <b>,</b> 500	1.0	5.0	30	45	90	13
inclined toroid	20 <b>,</b> 500	24 <b>,</b> 700	1.0	5.0	35	45	43	15

 $<sup>^{\</sup>text{a}}\text{v}_{\text{1}}\text{,}\text{v}_{\text{2}}\text{:}$  inner/outer radial or sem i+m a jor boundary in km  $\text{ s}^{\text{ 1}}$ 

<sup>&</sup>lt;sup>b</sup>E: Axis ratio

 $<sup>^{\</sup>mathrm{c}}$   $_{1}$ : optical depth of reference line ( 8542)

d: opening angle (see Figure 4)

 $<sup>^{\</sup>rm e}$  ; :angles de ning orientation of HVM  $\,$  sym m etry axis (see Figure 4)

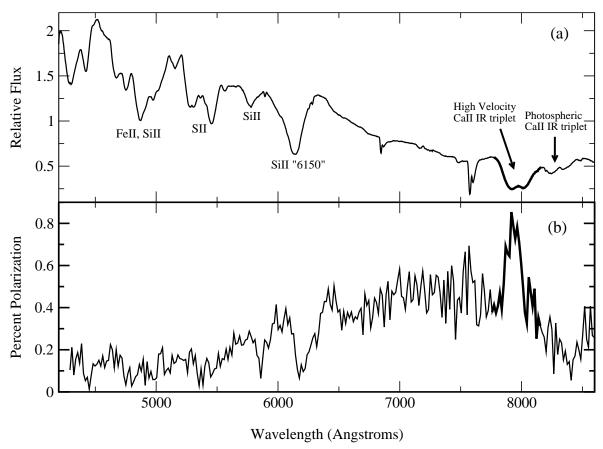


Fig. 1.| Flux and polarization spectrum of SN 2001elon Sept 25. The HVM feature is shown in bold lines. The polarization spectrum has been ISP subtracted using the ISP shown as the square in Figure 2.

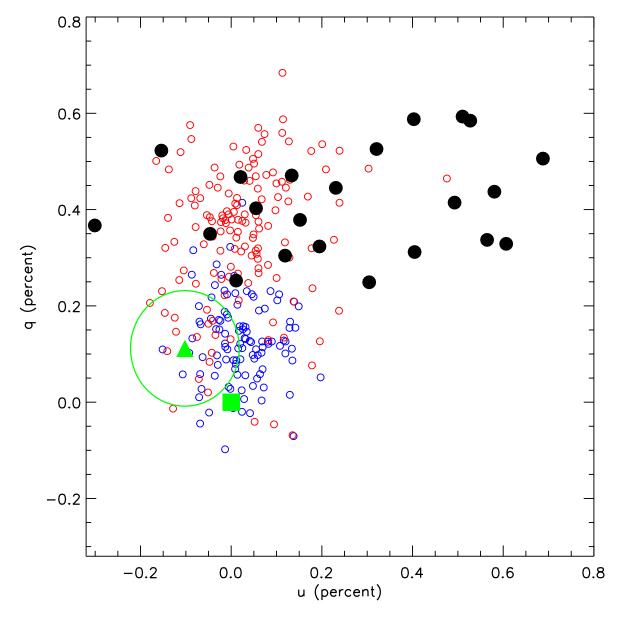


Fig. 2. | q-u plot of SN 2001el on Sept 25. Each point in the gure represents a wavelength element of the polarization spectrum. Large lled circles are points from the HVM feature (7800-8100 A). Small open circles are points from photospheric spectrum, where the blue open circles come from the wavelength range (4000-6000 A) and the red ones from (6000-8500 A). The green square at the origin represents the choice of the ISP leading to the sim plest theoretical interpretation, and the one used in the paper. The green triangle is the ISP determined using later time observations and assuming the intrinsic supermova polarization is zero at this time. The green circle is the rough estimated error on the ISP determined in this way.

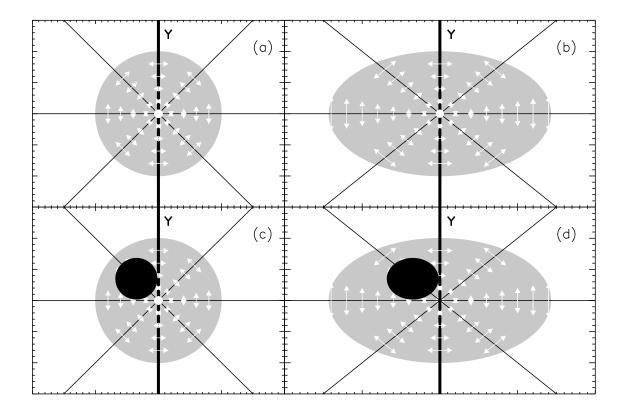


Fig. 3.| The polarization from supernova atmospheres. Each double arrow in the gure represent a Stokes specic intensity beam emerging from the photosphere in the observers line of sight. Larger arrows indicate a higher degree of polarization, not a higher intensity. The Y-axis is the polarization reference direction. (a) A spherical photosphere; the polarization of each beam is exactly canceled by another one quadrant away so the net polarization is zero. (b) An ellipsoidal photosphere; vertically polarized light from the long edge exceeds the horizontally polarized light from the short edge so q > 0. (c) A spherical photosphere with a clump of line optical depth; the continuum polarization cancels but the obscuration of diagonally polarized light by the line leads to a polarization peak feature with u > 0 (d) An ellipsoidal photosphere with a clump of line optical depth; the continuum is polarized in the q direction and the line in the u direction.

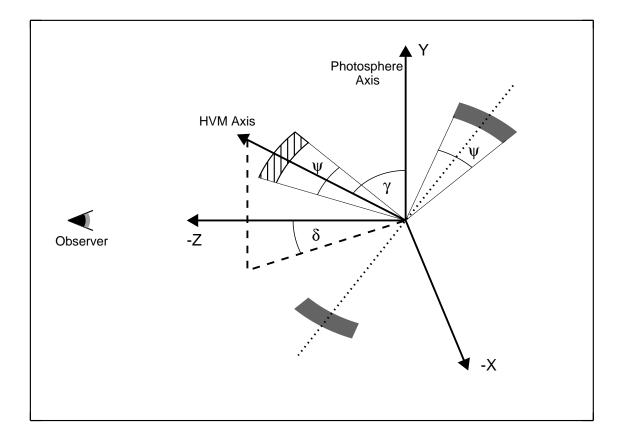


Fig. 4. Geometry used in the models. The line of sight is in the negative z-direction. The y-axis is both the polarization reference direction and the photosphere symmetry axis. The angles and denote the orientation of the HVM symmetry axis, where is the angle between the y-axis and the HVM axis, and is the angle between the line of sight and the projection of the HVM axis onto the z-x plane. denotes the opening angle of the clump (hashed arc) and the toroid (solid arc). The two structures are generated by spinning the arcs about the HVM axis.

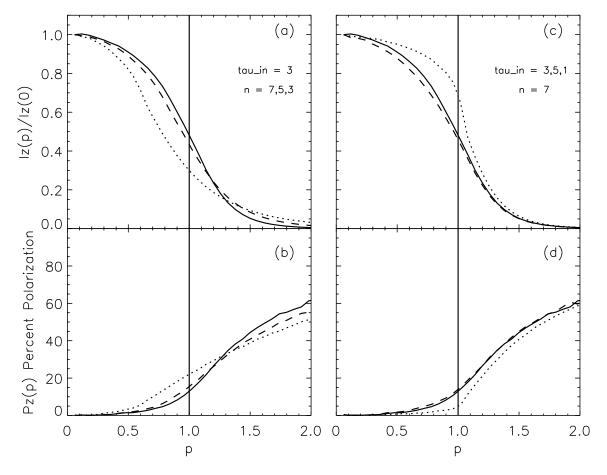


Fig. 5.| The intensity and polarization of speci c intensity beam s em erging from the spherical electron scattering photosphere described in section x3.2. The impact parameter p is given in units of the photospheric radius, de ned as continuum optical depth of one. The solid lines are the values used in the paper and the others lines show comparisons with slightly dierent models. (a,b) show the dependence on the power law index n assum ing  $_{ez} = 3$ ; solid line:  $_{ez} = 7$ , dashed line:  $_{ez} = 5$ , dotted line:  $_{ez} = 1$ .

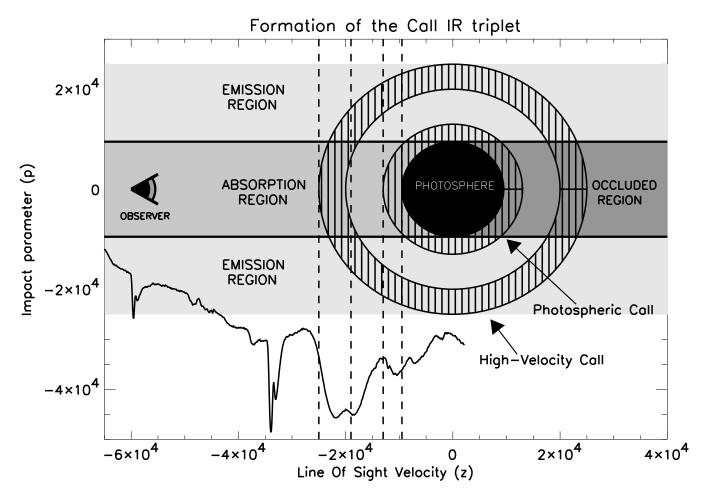


Fig. 6.| Schematic diagram of line formation of the CaII IR triplet feature in SN 2001el. The HVM has for illustration been shown with a spherical shell conguration. The line prole below is the actual ux spectrum of the HVM feature on Sept 25. The vertical lines represent a few of the CV planes of the 8542 line. Each CV plane corresponds to unique wavelength in the spectrum, given in the gure by the wavelength at which they intersect the line prole.

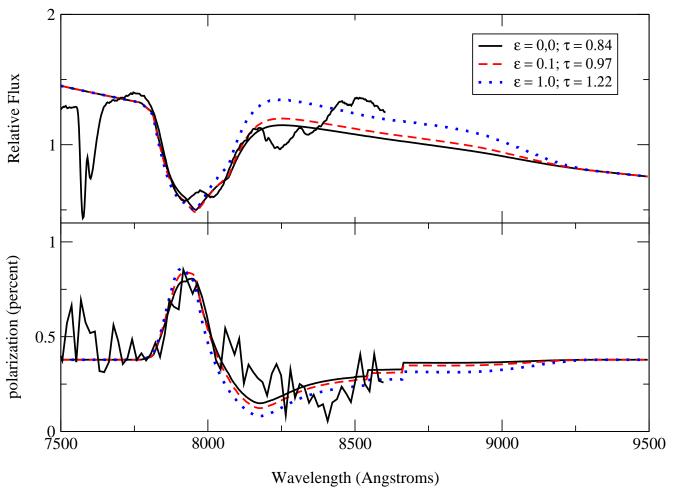


Fig. 7.| The e ect of em ission region m aterial from a spherical shell at a tem perature  $T=5500\,\mathrm{K}$ . Note that as the line source function is increased, the line optical depth must also be increased in order to reproduce the observed line depth. A pure scattering line ( = 0; solid line) does not produce a visible em ission feature. A therm alized line ( = 1; dotted line) produces an em ission, but because this will be blended with the photospheric triplet absorption and em ission, it may still be discult to detect.

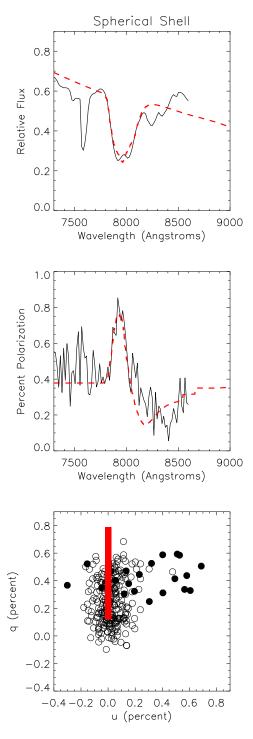


Fig. 8.| Synthetic spectra to the observed HVM feature using the spherical shell model of x42. In the top two plots, the solid black line is the observed data, and the dashed red line the t. In the bottom q-u plot, the black circles are the data and the red squares the t. The open circles indicate wavelengths corresponding to the photospheric spectrum and the solid circles the HVM feature.

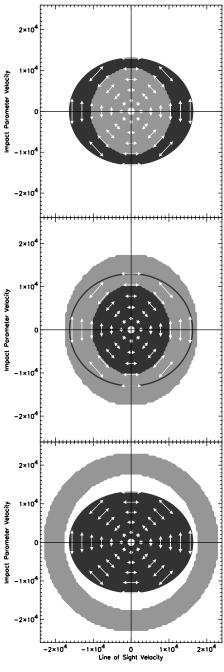


Fig. 9.| Three slices through the spherical shell HVM, which demonstrate how a detached spherical shelle ects the polarization at three dierent wavelengths. Each slice in red is the HVM cross-section on a plane perpendicular to the z (line of sight) axis, corresponding to an CV surface for the 8542 line at a particular wavelength. top:  $v_z=22;500 \text{ km s}^1!=7900 \text{ A}$ ; the line obscures the low ly polarized central light, leading to a polarization peak m iddle:  $v_z=15;500 \text{ km s}^1!=8100 \text{ A}$ ; the line obscures the highly polarized edge light, leading to a depolarization of the spectrum bottom:  $v_z=5000 \text{ km s}^1!=8400 \text{ A}$ ; the line obscures the highly polarized edge light, leading em its some unpolarized line source function light, thus depolarizing the spectrum. Note: the photospheric axis-ratio has been exaggerated (E = 0.8 rather than E = 0.91) to clarify the asymm etry.

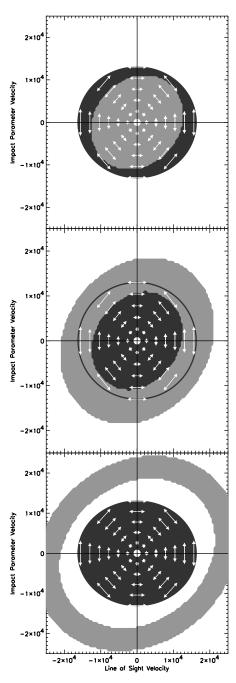


Fig. 10.] Three slices through the rotated ellipsoidal HVM . Panels are the same as in Figure 9. Because the rotated ellipsoidal shell preferentially obscures diagonal light, it will produce a polarization feature with a non-zero u component. The axis ratio of both the photosphere and HVM shell are exaggerated (E = 0.8 rather than 0.91) in order to clarify the asymmetries.

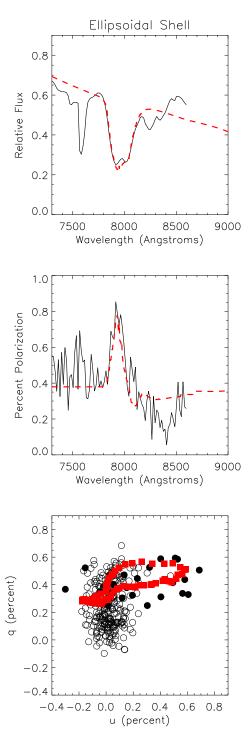


Fig. 11.| Synthetic spectrum ts for the ellipsoidal shell geometry of x4.3. The panels are the same as in gure 8. The ts to the ux and polarization spectra are similar to the spherical shell, but now the HVM feature is polarized primarily in the u-direction. The synthetic feature draws a loop in the q-u plane, which is similar to that in the observed data.

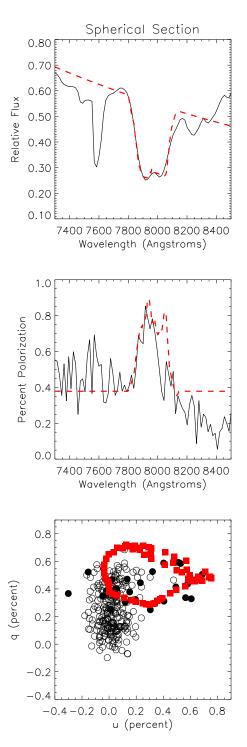


Fig. 12.| Synthetic spectra ts to the HVM feature using the clum ped shell geom etry described in x4.4. Panels are the same as in gure 8

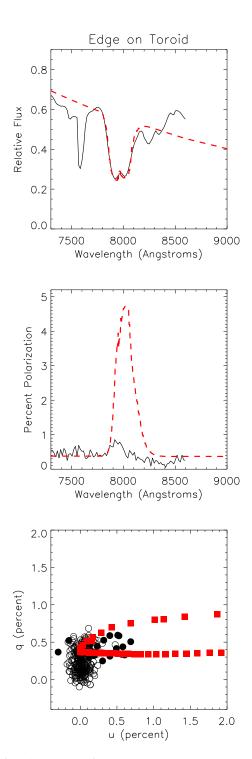


Fig. 13. Synthetic spectra to to the HVM feature using the edge-on toroid section geometry described in x4.5. Panels are the same as in gure 8. The polarization feature is much to strong.

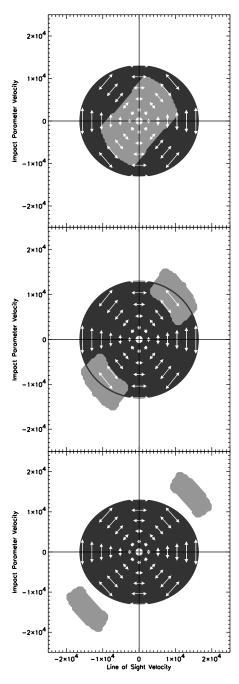


Fig. 14.] Three slices through the edge-on toroid HVM .P anels are the same as in Figure 9. Because the toroid is very elective in blocking light of a particular polarization, it will lead to large polarization peaks.

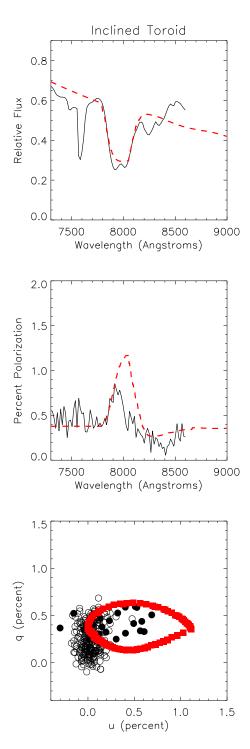


Fig. 15.| Synthetic spectra ts to the HVM feature using the inclined toroid geom etry described in x4.5. Panels are the same as in gure 8. The polarization feature is still too strong, while the ux absorption is too weak.

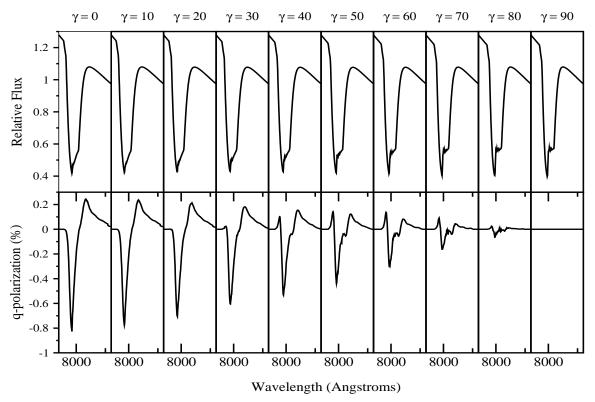


Fig. 16.| Pro le from the ellipsoidal shell model along lines of sight with various inclinations. Positive (negative) q-polarization indicates vertically (horizontally) polarized light. An absorption feature is visible from all lines of sight.

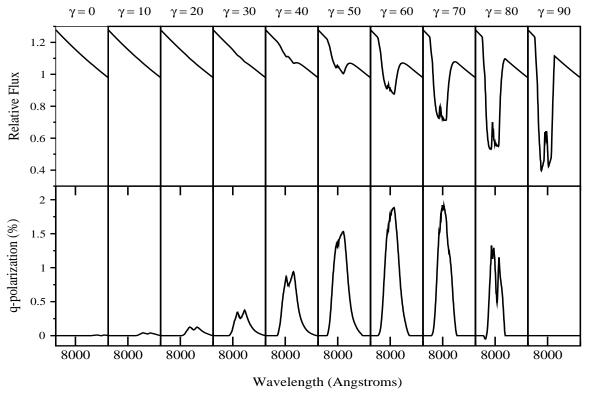


Fig. 17.| Pro le from the clum ped shell model from various lines of sight. As the section moves to the edge of the disk, it blocks lower intensity, highly polarized edge light. The ux feature thus gets weaker while the polarization gets stronger. Note for = 40 the ux absorption is hardly visible while the polarization feature is strong.

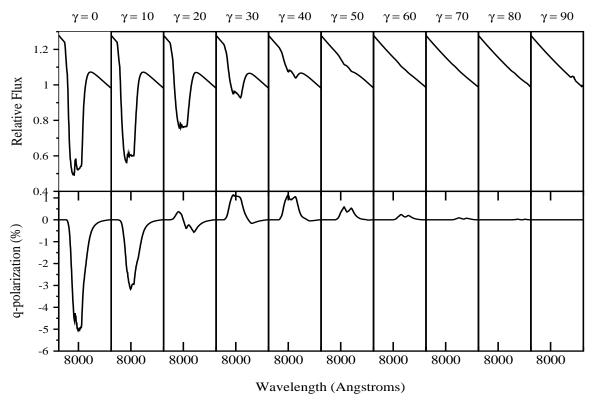


Fig. 18.| Pro les from the toroid model from various lines of sight