Anisotropic two-dimensional electron gas at $SrTiO_3$ (110) protected by its native overlayer

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Two dimensional electron gases (2DEGs) at oxide heterostructures are attracting considerable attention, as these might substitute conventional semiconductors for novel electronic devices [1]. Here we present a minimal set-up for such a 2DEG – the $SrTiO_3$ (110)-(4 \times 1) surface, natively terminated with one monolayer of chemically-inert titania. Oxygen vacancies induced by synchrotron radiation migrate underneath this overlayer, this leads to a confining potential and electron doping such that a 2DEG develops. Our angular resolved photoemission spectroscopy (ARPES) and theoretical results show that confinement along (110) is strikingly different from a (001) crystal orientation. In particular the quantized subbands show a surprising "semi-heavy" band, in contrast to the analogue in the bulk, and a high electronic anisotropy. This anisotropy and even the effective mass of the (110) 2DEG is tunable by doping, offering a high flexibility to engineer the properties of this system.

With ongoing miniaturization, conventional Si-based semiconductors are reaching their limits. Current technology is already based on a hybrid between Si and a HfO_2 -based high-k dielectric. Another transition metal oxide, SrTiO₃, has a ten times larger dielectric constant and would allow for even smaller structures. Against this background the 2DEG observed in oxide heterostructures such as LaAlO₃/SrTiO₃ [2] offers a promising alternative, not only for electronics at the nanoscale [3] but also because of the possibility of spin-polarized [4] and superconducting [5, 6] currents. An even simpler set-up is to create a 2DEG directly at $SrTiO_3$. Recently this was achieved by irradiating a (001) surface [7, 8] with synchrotron radiation, albeit the origin of the resulting 2DEG is still under debate [7–9]. This system has two major drawbacks: (i) it is unstable outside an ultra high vacuum (UHV) chamber and (ii) the (001) surface has no unique surface termination, as TiO_2 and SrO terraces may develop, and the surface structure strongly depends on sample treatment and history [10].

Here, we show that a 2DEG can also be induced at $SrTiO_3(110)$, which is stabilized and protected by a reconstructed overlayer. This overlayer automatically

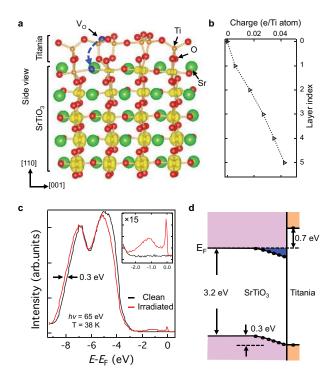


FIG. 1. SrTiO₃(110)-(4 × 1) surface. a Structural model; an oxygen vacancy (V_O) formed at the reconstructed surface spontaneously migrates to the (SrTiO)⁴⁺ plane beneath the top titania layer. The excess electrons from the V_O form a 2DEG confined within a region of about 2 nm thickness. The layer-dependent charge is represented by the yellow lobes and plotted in **b**. **c** Angle-integrated photoemission spectroscopy of the clean surface and after creating V_O's by synchrotron radiation. An in-gap state and a metallic peak near the Fermi level ($E_{\rm F}$) develop, see inset. **d** Schematic band structure at a surface with V_O's; the bands bend downward by 0.3 eV as deduced from the spectra in **c**. The dots denote the surface potential obtained from the shift of Ti 3s states in DFT+U calculations.

forms to compensate the intrinsic polarity of the system. A SrTiO₃ crystal can be viewed as a stack of alternating (SrTiO)⁴⁺ and (O₂)⁴⁻ planes along the [110] orientation, resulting in a dipole moment that diverges with increasing crystal thickness [11]. As is often true for polar surfaces, this is prevented by one of several compensation mechanisms [11]. Specifically, the SrTiO₃(110) surface

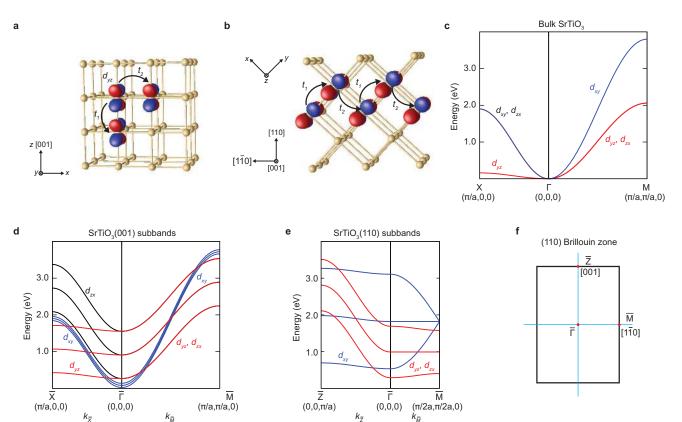


FIG. 2. Effect of Quantum confinement on the electronic structure of (001)- and (110)-oriented SrTiO₃. a-b, Schematics of the Ti lattice in SrTiO₃ oriented along the [001] and [110] direction, respectively. Ti $3d_{yz}$ orbital lobes expand in the y-z plane. Large (t_1) and small (t_2) hopping amplitudes depend on the overlap of the nearest neighbor d-orbitals c, Bulk band structure of SrTiO₃, consisting of a heavy d_{yz} band (red) and light d_{xy}/d_{zx} bands (blue) along k_x , as well as a light d_{xy} band (blue) and semi-light d_{yz}/d_{zx} bands (red) along k_M . d-e, Quantum well states (or subbands) of SrTiO₃ confined along [001] and [110] direction, respectively. The band dispersions of all the quantum well states confined in the (001) direction are the same as in the bulk. Confinement along (110) is different: here the d_{yz}/d_{zx} band becomes "semi-heavy" along the [110] directions and the different (110)-quantum-confined states have a different mass. f, 2D Brillouin zone of the SrTiO₃(110) surface.

spontaneously forms a (4×1) reconstruction upon various different sample treatments, including annealing in a tube furnace with flowing high-purity oxygen [12] and standard UHV preparation procedures [13, 14]. The reconstruction consists of a two-dimensional, tetrahedrallycoordinated titania overlayer (see Fig. 1a), which, with a nominal stoichiometry of $(\text{Ti}_{1.5}\text{O4})^{2-}$, quenches the overall dipole moment [12, 15]. Because the Ti atoms in the tetrahedral titania surface layer of the reconstruction are saturated by strong, directional bonds, the (4×1) surface is chemically quite inert [16].

Exposing the SrTiO₃(110)-(4 × 1) surface to synchrotron radiation creates oxygen vacancies (V_O's) at the surface [16]; they spontaneously migrate beneath the titania overlayer, see Fig. 1a for a sketch and Sec. S4 of the Supplementary Information for details. (This is a major difference to the SrTiO₃(100) surface, where oxygen vacancies remain at the surface; hence in that case the V_O's are not protected by an overlayer and will be filled when oxygen is present at the ambient.) The subsurface V_O's

at SrTiO₃(110) lead to electron-doping, and the photoemission spectrum in Fig. 1c shows the development of a metallic peak at E_F . Simultaneously, the O 2p valence band in Fig. 1c shifts to higher binding energy, indicating a downward band bending of ~ 0.3 eV (relative to E_F) in the vicinity to the surface. This is in agreement with the density functional theory (DFT+U) [17, 18] calculated potential shown as (layer-resolved) dots in 1d. Note that the topmost titania overlayer has a larger bandgap so that it is not only chemically but also electrically inert.

The pronounced surface potential arising from the downward band banding well confines the free charge carriers to a thin layer so that a 2DEG develops beneath the titania overlayer. From our DFT+U calculations we conclude that the charge carriers are localized in the SrTiO₃ layers within about 2 nm thickness (see Fig. 1b and the Supplementary Fig. S7).

We now turn to the unusual properties of the 2DEG at $SrTiO_3(110)-(4 \times 1)$. Experimentally we identify these from ARPES experiments (see Figs. 3 and 4, below) but

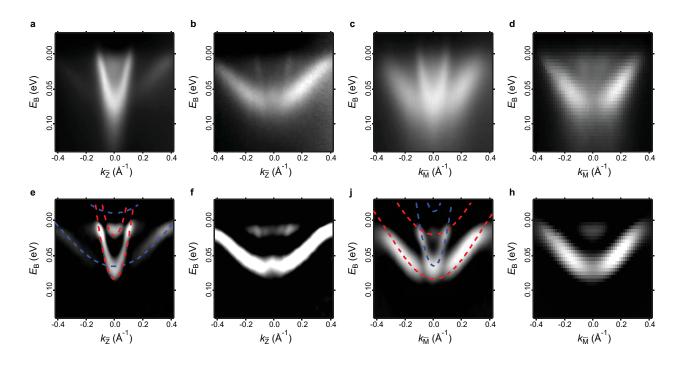


FIG. 3. **ARPES of the electronic structure at SrTiO**₃(110)-(4×1). a-d, Energy-momentum intensity maps ($T_{sample} = 38 \text{ K}$, $h\nu = 65 \text{ eV}$) along the $\overline{\Gamma} \cdot \overline{Z}$ (or [001]) direction and the $\overline{\Gamma} \cdot \overline{M}$ (or [110]) direction, respectively. e-h, Corresponding second derivatives. In each direction, the spectra were measured with linear vertical (a, d) and linear horizontal (b, c) polarized light. Tight-binding fits are overlaid for both directions. The d_{xy} -like bands are drawn in blue and the d_{yz}/d_{zx} -like bands in red. The d_{xy} -derived bands are weakly dispersive and d_{yz}/d_{zx} -derived bands are strongly dispersive along [001]; the d_{yz}/d_{zx} -derived bands become weakly dispersive and d_{xy} -derived band becomes strongly dispersive along [110]. The subbands become more visible in e-h.

for a better understanding we start with a tight binding modeling of this 2DEG; the details of the calculations are presented in the Sec. S8 of the Supplementary Information. In the bulk, $SrTiO_3$ has a gap of 3.2 eV and the three lowest conduction bands are Ti t_{2g} (i.e., d_{xy} , d_{yz} and d_{zx} , see Fig. 2c) orbitals that are degenerate at the Γ point. As the lobes of the d_{yz} orbital point into the y-z plane (see d_{yz} in Fig. 2a), the d_{yz} band has a small hopping amplitude t_2 in the Γ -X direction and is hence weakly dispersive (heavy) along Γ -X. In contrast, d_{xy} and d_{zx} have a larger overlap and hopping amplitude t_1 in this direction, and are thus strongly dispersive (light), as well as degenerate. Along Γ -M, the d_{xy} band is strongly dispersive (light) with hopping amplitude t_1 , while the d_{yz} and d_{zx} bands are "semi-light" with an effective hopping amplitude $(t_1+t_2)/2$, see Fig. 2c.

When the t_{2g} electrons are now confined within a few nm at the SrTiO₃(001) surface, quantum well states (or subbands) are formed. Due to the anisotropy of the t_{2g} orbitals, the level spacing of the quantized subbands strongly depends on the orbital character [7, 19, 20]. Notwithstanding, the [001] confinement does not change the carrier properties, i.e., the band dispersion of the subbands stays the same as in the bulk (see Fig. 2d). In striking contrast, a confinement along the [110] direction modeled with a wedge-shaped potential well (Fig. 1d) strongly changes the properties of the carriers, i.e., their band dispersion. As we show in the Supplementary Sec. S8, the effective hopping amplitude of the d_{xy} orbital along the $\overline{\Gamma}$ - $\overline{\mathrm{M}}$ ([1 $\overline{10}$]) direction becomes $t_1 \cos(\frac{\pi n}{N+1})$, where N is the number of layers and n the quantum number (or subband index). That is, the effective mass of the quantum confined states now depends on the sub-

TABLE I. Comparisons of experimental and theoretical effective masses of 2DEGs. The experimental effective masses are slightly larger than those obtained from tight-binding calculations, indicating a minor mass renormalization due to electronic correlations.

	$SrTiO_3(001)$		$SrTiO_3(110)$			
	Along $k_{\overline{\mathbf{X}}}$				Along $k_{\overline{M}}$	
Exp. $m^*(m_e)$	$10{\sim}20^{\rm a}$	$0.7^{\rm a}$ $0.5{\sim}0.6^{\rm b}$	9.7	0.67	6.1	0.74
Theor. $m^*(m_e)$					4.7	
Orbital	d_{yz}	d_{xy}/d_{zx}	d_{xy}	d_{yz}/d_{zx}	d_{yz}/d_{zx}	d_{xy}

^a Ref.[7]

^b Ref.[8]

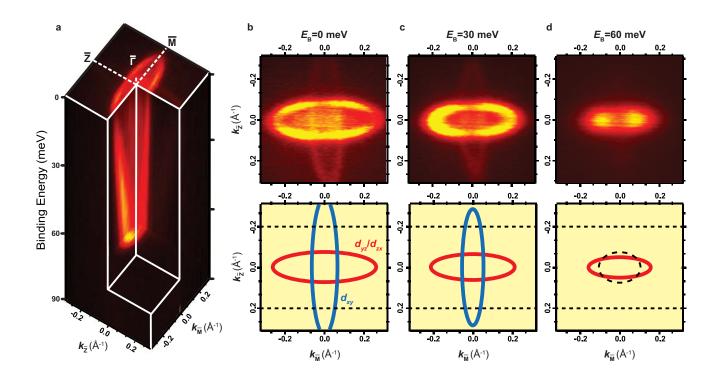


FIG. 4. Overview of the electronic structure. a Full photoemission mapping and b-d Constant energy cuts at different binding energies ($E_B = 0$, 30 and 60 meV) and schematic constant energy surfaces (bottom panels). Data taken with LV light, which emphasizes d_{yz} and d_{zx} orbitals. These appear bright, while d_{xy} -derived states appear faint. In the schematics the reconstructed (4 × 1) Brillouin zone is indicated by dotted lines. Note that the Fermi surface lies in the (1 × 1) Brillouin zone, consistent with the 2DEG being confined at the SrTiO₃ layers beneath the surface reconstruction. At higher binding energy, $E_B = 60$ meV, only the d_{yz}/d_{zx} -derived ellipsoid is occupied. The resulting constant energy surface is strongly anisotropic compared to the bulk projected energy surface (black dashed ellipsoid).

band index n. For particular values of n, such as n = 2 in Fig. 2e, the dispersion becomes flat. This is also the case for the d_{yz}/d_{zx} orbitals where the quantum confinement leads to an effective hopping amplitude $\frac{2t_1t_2}{t_1+t_2}\cos(\frac{\pi n}{N+1})$ along $\overline{\Gamma}$ - \overline{M} . Here, in addition to the quantum number n dependence, the prefactor also changes from its bulk value. As $t_2 \ll t_1$, this prefactor is $\sim 2t_2$ so that the d_{yz}/d_{zx} bands become "semi-heavy", whereas they are "semi-light" (~ $t_1/2$; Fig. 2c) in the bulk. A simple picture for this "semi-heavy" behavior is that the d_{uz}/d_{zx} electrons are quantum confined along [110] and movement along $[1\overline{10}]$ requires a zig-zag path with hopping amplitude alternating between t_2 and t_1 , see Fig. 2b. Hence only one t_2 hopping is required for moving the electrons by two sites, which explains the effective hopping amplitude $2t_2$.

Figure 3 shows angle-resolved photoemission spectroscopy (ARPES) results from the $SrTiO_3(110)-(4 \times 1)$

surface. The measurements were taken along [001] and $[1\overline{10}]$ directions. The intensity of the observed bands strongly depends on the light polarization (linear vertical, LV, and linear horizontal, LH). These dichroic effects are due to selection rules [21], and allow disentangling the symmetry and orbital character of the various bands (see Supplementary Figs. S1-3). This enables us to ascribe the strongly and weakly dispersing bands along the [001] direction to d_{yz}/d_{zx} - and d_{xy} -like orbitals, respectively. Accordingly, the strongly and weakly dispersing bands along $[1\overline{10}]$ direction correspond to d_{xy} - and d_{yz}/d_{zx} -like orbitals.

The strongly (weakly) dispersing $d_{yz}/d_{zx}(d_{xy})$ -like band along [001] has a bandwidth of ~72 meV (~62 meV) and a Fermi momentum of 0.11 Å⁻¹ (0.40 Å⁻¹). A fit to a parabolic dispersion yields an effective mass $m^* = 0.67m_e$ (9.7 m_e), with m_e the free electron mass. These [001] effective masses are consistent with those from a 2DEG on the vacuum-fractured SrTiO₃(001) surface [7, 8] and the tight binding description, see Table I. Around the Γ point the orbital degeneracy is lifted by a splitting of ~10 meV between the d_{yz}/d_{zx} - and d_{xy} -like bands.

From our tight-binding calculations we expect a quite different behavior along the $[1\overline{10}]$ direction. The $d_{yz}/d_{zx}(d_{xy})$ -derived ARPES bands have bandwidths of ~ 72 meV (62 meV), Fermi momenta of 0.34 Å⁻¹ (0.10 Å⁻¹), and effective masses of 6.1 (0.74), see Fig. 3c,d. The former corresponds to a "semi-heavy" band distinct from its "semi-light" behavior in the bulk. In particular, the "semi-heavy" carriers predicted by the tight-binding calculations agree well with the experimental ones, see Table I for a summary of the effective masses.

Figure 3 e-h show the second derivatives of the ARPES data along with the corresponding tight-binding subbands dispersion (Figs. 3 e,j). In addition to the bands discussed above, shallower bands becomes more visible. These are attributed to d_{yz}/d_{zx} -like subbands, indicating that quantum well states of a 2DEG are formed at SrTiO₃(110). The 2D character of the observed bands is further confirmed by the fact that the bands have no dispersion along the [110] direction (surface normal) in photon energy dependent measurements (see Supplementary Fig. S4). From the tight-binding calculations we found both d_{yz}/d_{zx} - and d_{xy} -like carriers to be confined within ≈ 2 nm, in excellent agreement with the DFT+U prediction (see Supplementary Fig. S7 and S10).

Figure 4 shows full photoemission mapping and constant energy cuts obtained with LV light polarization and detection along the [110] direction. The resulting Fermi surface consists of two perpendicular ellipsoids and a small ellipsoid centered at the Γ point. The bright (faint) ellipsoid is derived from $d_{yz}/d_{zx}(d_{xy})$ -like band and has semi-axes of ~0.11 Å⁻¹(0.4 Å⁻¹) and 0.34 Å⁻¹(0.10 Å⁻¹) along [001] and [110], respectively. From the area (A_F) enclosed by each Fermi surface, the corresponding 2D carrier density is $n_{2D} = A_F/2\pi^2$. Taking into account the three bands that cross E_F , we find 0.39 electrons per 1 × 1 unit cell of SrTiO₃(110) (or about 1.8×10^{14} cm⁻²), a value even larger than the sheet carrier density measured at the bare SrTiO₃(100) surface [7, 8].

The Fermi surface measurements further support the conclusion that the 2DEG is not residing at, but underneath the reconstructed surface layer, as in the former case we would expect a gap opening related to the "4×" periodicity along the [001] direction. Indeed, the Fermi surface lies in the (1×1) but not in the reconstructed (4×1) Brillouin zone (which is indicated by the dashed lines in Figs. 4 b-d).

Our results explain the dopant-dependent anisotropy at the (110)-oriented LaAlO₃/SrTiO₃ interface that was observed recently [22]. Although both d_{xy} and d_{yz}/d_{zx} derived Fermi surfaces are strongly anisotropic, the difference along the [001] and [110] directions themselves is not very pronounced at higher carrier density, when both ellipsoids are occupied (see Fig. 4). However, at a higher binding energy of $E_B = 60$ meV, only the d_{yz}/d_{zx} -derived ellipsoids appears, with a corresponding carrier density of $\sim 1.7 \times 10^{13}$ cm⁻². Remarkably, this is the same carrier density where a pronounced anisotropic conductivity was observed in transport measurements [22]. At this doping level, the big difference between the "semi-heavy" and light carriers comes to bear. In the bulk, however, the anisotropy is not so pronounced (see dashed ellipsoid in Fig. 4d).

In conclusion, we have demonstrated that an anisotropic 2DEG with tunable properties can be created on $SrTiO_3(110)$. The chemically inert and electrically insulating titania overlayer is native to this system, as it forms spontaneously to lift the intrinsic polarity of this system. It provides for a robust 2DEG that is less vulnerable against atmospheric contaminations than a 2DEG at the bare surface, and less dependent on the chemical complexity inherent to interfacial 2DEGs. The (110) 2DEG turns out to be strikingly different from the (001) 2DEG, which has been the subject of previous ARPES studies. The band dispersion is not only distinct from the one of the bulk, it even depends on the quantum number for the (110) confinement. Hence one can engineer a completely flat band along $[1\overline{10}]$, which is promising for (flat band) ferromagnetism [23], thermoelectricity and, possibly, superconductivity [24]. Tuning the carrier density should provide for facile control of flat band physics as well as of the anisotopic features of the (110) 2DEG. This is possible by the amount of oxygen vacancies, applying an electric field [25], and the deposition of metal adatoms on the titania overlayer [26]. Our work hence paves the way for novel electronics at oxide surfaces.

METHODS

Experiments. The Nb-doped (0.5 wt%) SrTiO₃(110) surface was prepared by cycles of Ar^+ sputtering (1 keV, 5 μ A, 10 minutes) followed by annealing in 3 \times 10⁻⁶ mbar oxygen at 900 °C for 1h. The samples were heated by electron beam and the temperature was monitored with an infrared pyrometer. The surface reconstruction was checked by low energy electron diffraction (LEED) and tuned by depositing Sr metals on the surface at RT followed by annealing until a sharp (4×1) LEED patter was observed [14]. The ARPES measurements were performed at the ARPES 1² beamline at BESSY II, Germany. All ARPES spectra were recorded using photons with energy of 50-70 eV, linearly polarized along the horizontal/vertical direction. A Scienta R8000 analyzer with vertical detection slit geometry was used, with the energy and angular resolution of $\sim 10 \text{ meV}$ and 0.3° , respectively. Sample temperature was at ~ 38 K.

Theory. DFT calculations with the inclusion of an effective on-site Coulomb repulsion $U_{eff} = 4.5$ eV for the Ti *d* states were carried out with the Vienna ab initio simulation package (VASP) [17, 18], within the pro-

jector augmented-wave method and the Perdew-Burke-Ernzerhof functional [27]. The computational cell was modeled with a symmetric slab consisting of 45 atomic layers separated by a 12 Å thick vacuum region. One oxygen vacancy was created on both sides of the symmetrical slab (see Supplement). The kinetic energy cutoff for the plane-wave expansion was set to 600 eV. We adopted a (4×1) two-dimensional unit cell, and a (2×3×1) Monkhorst-Pack k-point mesh. During the structural optimization, atoms in the central nine layers were kept fixed to the corresponding bulk positions, whereas the other atoms were allowed to relax until the forces on each atom were less than 0.02 eV/Å.

The hopping parameters for the tight binding calculations have been obtained both by (i) fitting the nearest neighbor hopping parameters to the DFT bandwidth of bulk SrTiO₃ yielding $t_1 = -0.455$ ev and $t_2 = -0.04$ eV, and (ii) more thoroughly though a Wannier function projection [28, 29] of a Wien2K [30] DFT calculation, using the generalized gradient approximation [27] and $10 \times 10 \times 10$ k-point grid. For the furthergoing tight binding calculations, up to next nearest neighbor hopping has been taken into account, see Sec. S8 and S9 of Supplementary Information for details.

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