

## Anomaly-based Intrusion Detection using Multiclass-SVM with Parameters Optimized by PSO

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### Abstract

Intrusion detection systems (IDS) play an important role in defending network systems from insider misuse as well as external attackers. Compared with misuse-based techniques, anomaly-based intrusion detection techniques perform well in detecting new attacks. Firstly, this paper proposes a feature selection algorithm based on SVM (termed FS-SVM) to reduce the dimensionality of sample data. Moreover, this paper presents an anomaly-based intrusion detection algorithm, i.e., multiclass support vector machine (MSVM) with parameters optimized by particle swarm optimization (PSO) (termed MSVM-PSO), to detect anomalous connections. To verify the effectiveness of these two proposed algorithms (FS-SVM and MSVM-PSO) and the detection precision of MSVM-PSO, this paper conducts experiments on the famous KDD Cup dataset. This paper compares MSVM-PSO with three commonly adopted algorithms, namely, Bayesian, K-Means, and multiclass SVM with parameters optimized grid method (MSVM-grid). The experimental results show that MSVM-PSO outperforms these three algorithms in detection accuracy, FP rate, and FN rate.

**Keywords:** Intrusion detection; Anomaly; Feature selection; Multiclass SVM; Parameter optimization; PSO

### 1. Introduction

Along with the development of IT (information technology), people increasingly rely on computer networks to provide them with news, email and online shopping, etc. To ensure the integrity and availability of network systems, these systems must be defended from insider misuse as well as external attackers, thus promoting the development of intrusion detection systems (IDS).

Intrusion detection techniques can be classified into two categories: *misuse-based* and *anomaly-based* techniques. The misuse-based intrusion detection techniques are based on defining what malicious behaviors (i.e., attacks) are and then monitoring for them. These techniques work well in detecting known attacks but will miss new attacks unless these new attacks are just minor variations on old ones.

In contrast to misuse detection, anomaly detection techniques construct a model to represent normal system usage and then monitor for any behavior that does not fit this model. These techniques work well in detecting new attacks which misuse-based techniques would miss.

Along with the evolution of network attacks, the detection precision of existing anomaly-based techniques (e.g., Bayesian, K-Means) can not meet the requirements of increasingly complex network environment. While support vector machines (SVMs) exhibit many unique advantages in nonlinear and high dimensional classification problems with small-scale sample data. Therefore, this paper proposes SVM-based techniques to solve anomaly intrusion detection.

Firstly, to reduce the dimensionality of sample data, this paper proposes a feature selection algorithm based on SVM (termed FS-SVM). Moreover, this paper presents an anomaly-based intrusion detection algorithm by using multiclass SVM with parameters optimized by particle swarm optimization (PSO) (termed MSVM-PSO). To verify the effectiveness of these two proposed algorithms (FS-SVM and MSVM-PSO) and the detection precision of MSVM-PSO, this paper conducts experiments on KDD Cup datasets, which is a benchmark dataset in the researches on network intrusion detection. Meanwhile, it compares MSVM-PSO with Bayesian 0, [1], K-Means [2] and multiclass SVM with parameters optimized grid method (MSVM-grid). The experimental results show that MSVM-PSO outperforms these three algorithms in detection accuracy, FP rate, and FN rate.

The remainder of this paper is organized as follows. Section 2 introduces related work. Section 3 illustrates the preliminaries of SVM. Section 4 proposes a feature selection algorithm (FS-SVM) based on SVM. Section 5 presents the proposed detection algorithm (MSVM-PSO) in detail. Section 6 conducts experiments and presents analyses. Finally, Section 7 gives conclusions and looks into future work.

## 2. Related Work

This section summarizes research work related to intrusion detection, feature selection, and SVM.

### 2.1. Intrusion Detection

Intrusion detection systems (IDS) protect computer networks from unauthorized users, including perhaps insiders. The intrusion detector (*i.e.*, a classifier) learns to build a predictive model which is capable of distinguishing between *bad* connections (called intrusions or attacks) and *good* normal connections. IDS can be implemented by *misuse-based* or *anomaly-based* intrusion detection techniques.

By using Bayesian networks, Tylman [3] implements a misuse-based intrusion detection system, *Basset* (Bayesian System for Intrusion Detection), which is extended from *Snort*. The ultimate goal of *Basset* is to provide better detection capabilities and less chance of false alarms through evaluating *Snort* alerts by Bayesian networks. However, the inherent limitations of Bayesian networks and misuse-based techniques make *Basset* hard to detect new attacks, *i.e.*, the miss rate is relative high.

Jyothsna *et al.*, [4] survey anomaly-based intrusion detection systems. They elaborate the foundations of commonly adopted anomaly intrusion detection techniques along with their operational architectures. They also classify these techniques based on the type of processing that is related to the behavioral model for the target systems.

Goel *et al.*, [5] propose a novel hybrid intrusion detection model, *i.e.*, parallel misuse and anomaly detection. The former adopts C4.5 based binary decision trees, and the latter adopts CBA (Classification Based Association) based classifier. The model's performance is evaluated on KDD Cup 99 benchmark [6], [7]. However, the parallel nature of the proposed model makes it hard to be deployed upon network systems.

Intrusion detection and corresponding techniques are always continuously concerned issues in literature, regardless that new computing paradigms *e.g.*, cloud computing [8] have emerged. Modi *et al.*, [8] survey different intrusions affecting availability, confidentiality and integrity of Cloud resources and services. They examine Intrusion Detection Systems (IDS) and Intrusion Prevention Systems (IPS) in Cloud, and propose corresponding proposals. Mitchell and Chen [9] survey intrusion detection research for Cyber-Physical Systems (CPSs), *e.g.*, pervasive healthcare systems, smart grids. They classify modern CPS Intrusion Detection System (IDS) techniques based on two design dimensions: detection technique and audit material.

## 2.2. Feature Selection (FS)

The sample data of IDS are usually high-dimensional. For example, the KDD Cup 99 dataset ([7]) contains 41 features. Some features are valueless for anomaly intrusion detection. Feature selection techniques *e.g.*, [10], [11] select an optimal subset of the original features based on some criteria. Existing techniques usually involve exhaustive searching all the possible subsets of the set of original features, thereby usually being time-consuming.

Lin *et al.*, [12] combine support vector machines (SVM) and simulated annealing (SA) to find the best selected features to elevate the accuracy of anomaly intrusion detection, where SA is adopted to adjust the best values of two parameters in SVM. However, they do not clearly describe how to select the best features. Guyon *et al.*, [13] propose a recursive feature elimination method based on SVM, which removes a feature every time after executing SVM on the remaining set of features. But the number of selected features is a preset value, which relies on human expertise. In section 4, this paper proposes a more effective and reasonable feature selection algorithm based on SVM.

## 2.3. Support Vector Machines (SVMs)

The original SVM algorithm was first invented by Vladimir N. Vapnik. The current standard incarnation (*i.e.*, soft margin SVM, as illustrated in Section 3.2) was proposed by Corinna Cortes and Vapnik in 1993 and published in 1995 ([14]). After twenty years of development, SVMs have been widely and successfully applied in many fields including text categorization, speech recognition, remote sensing image analysis, and time series forecasting ([15]).

In nature, SVM is a kind of supervised learning method. SVM can be applied to classification, regression, and tagging. This paper only concentrates on classification problems. The classical applications of classification include intrusion detection ([5]), violent behavior detection ([16]), fault diagnosis ([17]). This paper introduces SVM-based techniques to anomaly intrusion detection.

## 3. Preliminaries

Notations:

(1) In this paper, an italic letter (maybe with a subscript) (*e.g.*,  $y_i$ ) represents a scalar value.

(2) A bold and italic letter (maybe with a subscript) (*e.g.*,  $\mathbf{x}_i$ ) represents a vector; moreover, all vectors in this paper are column ones. In addition, a bold letter (*e.g.*,  $\mathbf{x}$ ) represents a vector in a Hilbert space.

In addition, a training set contains a number of sample points; each sample point,  $(\mathbf{x}, y)$ , in the training set has a unique sequence number; the input,  $\mathbf{x}$ , in a sample point is usually a vector. While a vector  $\mathbf{x}$  contains several components; each component (scalar) also has a unique sequence number. To avoid confusion, the following agreements are made on these two sequence numbers.

(1) For a sequence containing a list of vectors or scalars, the sequence number of each element in the sequence is represented by a subscript. For example, a training set can be represented by  $T = \{ (\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_N, y_N) \}$ , where  $(\mathbf{x}_i, y_i)$  is a sample point, the input,  $\mathbf{x}_i$ , is a vector, while the output,  $y_i$ , is a scalar. The subscripts in  $\mathbf{x}_i$  and  $y_i$  respectively represent the sequence number of  $\mathbf{x}_i$  and  $y_i$  in the whole sequence. For a component in a vector, its sequence number is also represented by a subscript, *e.g.*,  $\mathbf{x} = (x_1, x_2, \dots, x_n)^T \in R^n$ .

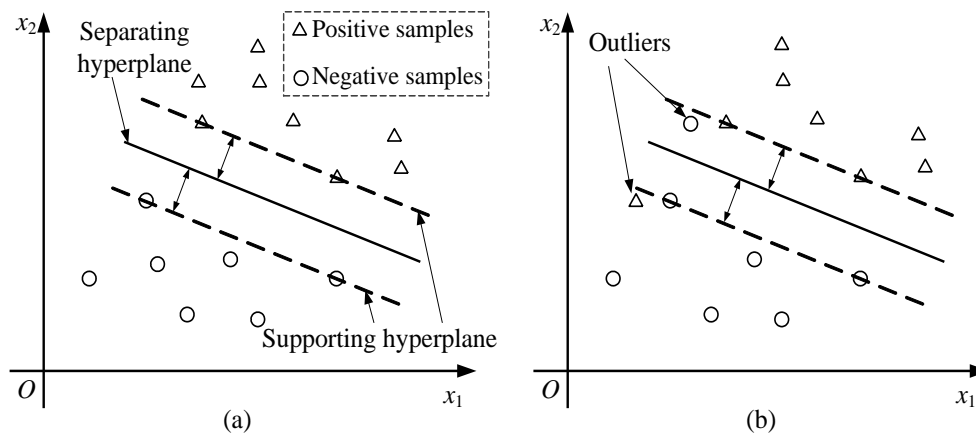
(2) If these two sequence numbers appear at the same time, the first subscript represent the sequence number in the sequence, the second one represents the

sequence number in the vector, *e.g.*, the input of the *i*-th sample point can be completely represented by  $\mathbf{x}_i = (x_{i1}, x_{i2}, \dots, x_{in})^T$ .

In addition, the superscript of a variable in PSO algorithm represents the sequence number of iteration.

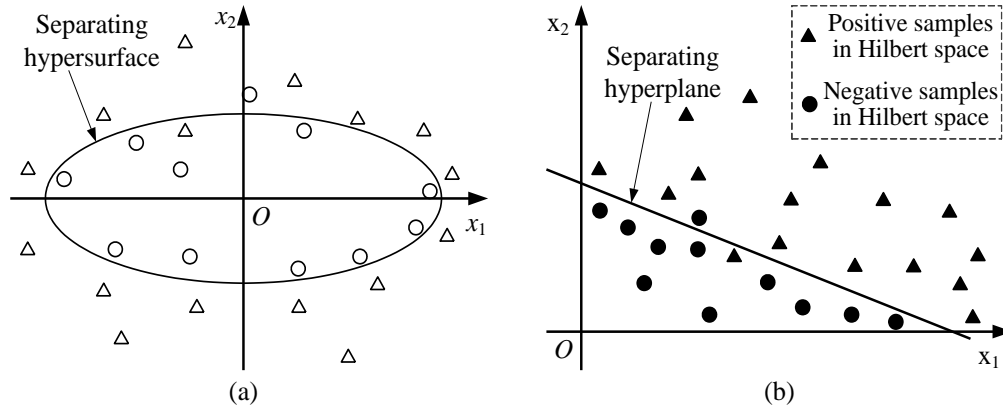
### 3.1. The Basic Idea of SVM

SVM is essentially a binary classification model. SVM is a kind of statistical learning methods, which include three elements, *i.e.*, *model*, *strategy*, and *algorithm*. The basic model of SVM is a linear classifier with maximal margin defined in the feature space. By introducing kernel methods, SVM can also realize nonlinear classification. The learning strategy of SVM is to maximize the margin between two supporting hyperplanes, as shown in Figure 1(a), which can be formed as a convex quadratic programming problem. The learning algorithm of SVM is the one to solve the convex quadratic programming optimization algorithm.



**Figure 1. Linear Separable SVM and Linear SVM**

SVM consists of three basic models: linear separable SVM, linear SVM, and nonlinear SVM. Figure 1 and Figure 2 illuminate these basic models in a 2-dimensional case. When the training set are linear separable, as shown in Figure 1(a), a linear classifier (*i.e.*, the separating hyperplane, shown in Figure 1(a)) can be learned through maximizing the hard margin. The learned linear classifier is called linear separable SVM, also known as hard margin SVM. When the training set are approximately linear separable, as shown in Figure 1(b), a linear classifier can also be learned through maximizing the soft margin. The learned linear classifier is called linear SVM, also known as soft margin SVM. When the training set are not linear separable, as shown in Figure 2(a), kernel techniques are used to convert the input space  $\mathbf{x} \in R^n$  to a Hilbert space  $\mathbf{x} \in H$ , as shown in Figure 2(b), and then a nonlinear SVM can be learned through maximizing the soft margin.



**Figure 2. Nonlinear SVM**

### 3.2. C-support Vector Classification (C-SVC)

The most fundamental SVM is C-SVC, which is gradually deduced below. Firstly, the related formal definitions are given below.

**Definition 1 (Anomaly-based intrusion detection Problem):** Let  $T$  be a training set,

$$T = \{ (\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_N, y_N) \} \in (\mathbb{R}^n \times \Psi)^N, \quad (1)$$

where  $\mathbf{x}_i = (x_{i1}, x_{i2}, \dots, x_{in})^T \in \mathbb{R}^n$ ,  $N$  is the number of samples.

1) Binary classification: the task is to determine whether a connection (represented by a vector,  $\mathbf{x}$ , consisting of a set of features) is a normal one or an attack, then

$$y_i \in \Psi = \{1, -1\}, i = 1, 2, \dots, N, \quad (2)$$

$y_i$  is the label of  $\mathbf{x}_i$ . When  $y_i = +1$ ,  $\mathbf{x}_i$  is called a positive sample; while when  $y_i = -1$ ,  $\mathbf{x}_i$  is called a negative sample.  $(\mathbf{x}_i, y_i)$  is called a sample point. The goal is to find a real function  $g(\mathbf{x})$  in  $\mathbb{R}^n$ ,

$$y = f(\mathbf{x}) = \text{sgn}(g(\mathbf{x})), \quad (3)$$

where  $\text{sgn}()$  is the sign function and  $f(\mathbf{x})$  derives the value of  $y$  for any  $\mathbf{x}$ .

2) Multiclass (or  $M$ -class) classification: the task is to not only determine a connection is normal or not, but also determine the type of attack for an anomaly connection, then

$$y_i \in \Psi = \{0, 1, \dots, M-1\}, i = 1, 2, \dots, N, \quad (4)$$

$M$  is the number of states including the normal state. The goal is to find a decision function  $f(\mathbf{x})$  in  $\mathbb{R}^n$ ,

$$y = f(\mathbf{x}) : \mathbb{R}^n \rightarrow \Psi, \quad (5)$$

such that the class number  $y$  for any  $\mathbf{x}$  can be predicted by  $y = f(\mathbf{x})$ .

**Definition 2 (Linearly separable problem):** Consider the training set (1)~(2), if there exist  $\mathbf{w} \in \mathbb{R}^n$ ,  $b \in \mathbb{R}$  and a positive number  $\varepsilon$  such that for any subscripts  $i$  with  $y_i = 1$ ,  $(\mathbf{w} \cdot \mathbf{x}_i) + b > \varepsilon$  hold; and for any subscripts  $i$  with  $y_i = -1$ ,  $(\mathbf{w} \cdot \mathbf{x}_i) + b < -\varepsilon$  hold; then the training set and its corresponding classification problem are called linearly separable.

For a linearly separable training set, finding the separating hyperplane through maximizing the hard margin can deduce the following primal optimization algorithm:

$$\min_{\mathbf{w}, b} \frac{1}{2} \|\mathbf{w}\|^2, \quad (6)$$

$$\text{s.t. } y_i((\mathbf{w} \cdot \mathbf{x}_i) + b) \geq 1, \quad i = 1, 2, \dots, N. \quad (7)$$

The intuitive interpretation of maximal margin is to separate the training samples with fully confident degree. Namely, it not only separates the positive sample points and negative ones, but also separates the sample points very close to the separating hyperplane with enough confidence level. Such a separating hyperplane has good classification ability for unknown new samples.

The following dual optimization algorithm can be obtained by applying Lagrange duality:

$$\min_{\alpha} \frac{1}{2} \sum_{i=1}^N \sum_{j=1}^N y_i y_j (\mathbf{x}_i \cdot \mathbf{x}_j) \alpha_i \alpha_j - \sum_{j=1}^N \alpha_j, \quad (8)$$

$$\text{s.t. } \sum_{i=1}^N y_i \alpha_i = 0, \quad (9)$$

$$\alpha_i \geq 0, \quad i = 1, 2, \dots, N. \quad (10)$$

where  $\alpha = (\alpha_1, \alpha_2, \dots, \alpha_N)^T$  is the Lagrange multiplier vector.

If most of the sample points are linearly separable except for few outliers, as shown in Figure 1(b), a set of relaxation variable,  $\xi_i \geq 0$ , should be introduced into the constraints (7); meanwhile a penalty item should be introduced into the object function (6). Therefore, finding the separating hyperplane through maximizing the soft margin can deduce the following primal optimization algorithm:

$$\min_{\mathbf{w}, b, \xi} \frac{1}{2} \|\mathbf{w}\|^2 + C \sum_{i=1}^l \xi_i, \quad (11)$$

$$\text{s.t. } y_i((\mathbf{w} \cdot \mathbf{x}_i) + b) \geq 1 - \xi_i, \quad i = 1, 2, \dots, N, \quad (12)$$

$$\xi_i \geq 0, \quad i = 1, 2, \dots, N. \quad (13)$$

where  $C > 0$  is a penalty parameter, and  $\xi = (\xi_1, \xi_2, \dots, \xi_N)^T$ . In the objective function (11), the former item ( $\|\mathbf{w}\|^2$ ) represents the inverse of the margin, the latter item represents a measurement of violation of the constraints,  $y_i((\mathbf{w} \cdot \mathbf{x}_i) + b) \geq 1$ . The parameter  $C$  determines the weighting between the two terms.

Similarly, the following dual optimization algorithm can be obtained by applying Lagrange duality:

$$\min_{\alpha} \frac{1}{2} \sum_{i=1}^N \sum_{j=1}^N y_i y_j (\mathbf{x}_i \cdot \mathbf{x}_j) \alpha_i \alpha_j - \sum_{j=1}^N \alpha_j, \quad (14)$$

$$\text{s.t. } \sum_{i=1}^N y_i \alpha_i = 0, \quad (15)$$

$$0 \leq \alpha_i \leq C, \quad i = 1, 2, \dots, N. \quad (16)$$

When a training set is not linear separable, through finding a proper mapping  $\Phi$  which transforms the input space  $R^n$  to the feature space  $H$ , it is possible to solve a linear classifier in the feature space  $H$  to separate the transformed data set. By introducing a kernel function, it does not need to explicitly define the map  $\Phi$ .

By introducing the map  $\Phi$ , the inner product in (14) should be replaced with  $(\Phi(\mathbf{x}_i) \cdot \Phi(\mathbf{x}_j))$ , while by further introducing the kernel function, the inner product can be expressed as  $K(\mathbf{x}_i, \mathbf{x}_j)$ , which results the following basic SVM algorithm, C-SVC.

**Algorithm 1: C-Support Vector Classification (C-SVC)**

**Input:** the training set  $T = \{ (\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_N, y_N) \}$ , where  $\mathbf{x}_i \in \Xi \subseteq R^n$ ,  $y_i \in \Psi = \{1, -1\}$ ,  $i = 1, 2, \dots, N$ ; choose an appropriate kernel  $K(\mathbf{x}, \mathbf{x}')$ , and a penalty parameter  $C > 0$ .

**Output:** the decision function  $f(\mathbf{x})$ .

(1) Construct and solve the convex quadratic programming problem below:

$$\min_{\alpha} \frac{1}{2} \sum_{i=1}^N \sum_{j=1}^N y_i y_j \alpha_i \alpha_j K(\mathbf{x}_i, \mathbf{x}_j) - \sum_{j=1}^N \alpha_j \tag{17}$$

$$\text{s.t.} \quad \sum_{i=1}^N y_i \alpha_i = 0, \tag{18}$$

$$0 \leq \alpha_i \leq C, i = 1, 2, \dots, N, \tag{19}$$

thus obtaining a solution  $\alpha^* = (\alpha_1^*, \alpha_2^*, \dots, \alpha_N^*)^T$ ;

(2) Compute  $\mathbf{w}^* = \sum_{i=1}^N \alpha_i^* y_i \Phi(\mathbf{x}_i)$ . If only the decision function is needed,  $\mathbf{w}^*$  do not need to be explicitly calculated.

(3) Compute  $b^*$ : Choose a component of  $\alpha^*$ ,  $\alpha_j^* \in (0, C)$ , and compute

$$b^* = y_j - \sum_{i=1}^N y_i \alpha_i^* K(\mathbf{x}_i, \mathbf{x}_j); \tag{20}$$

(4) Construct the decision function:

$$f(\mathbf{x}) = \text{sgn}(g(\mathbf{x})), \tag{21}$$

where

$$g(\mathbf{x}) = \sum_{i=1}^N y_i \alpha_i^* K(\mathbf{x}_i, \mathbf{x}) + b^*. \tag{22}$$

The most commonly adopted kernel function is Gauss kernel function, which is defined by:

$$K(\mathbf{x}, \mathbf{x}') = \exp(-\|\mathbf{x} - \mathbf{x}'\|^2 / \sigma^2), \tag{23}$$

or:

$$K(\mathbf{x}, \mathbf{x}') = \exp(-\lambda \|\mathbf{x} - \mathbf{x}'\|^2). \tag{24}$$

Gauss kernel function maps the original input space to an infinite dimensional one. If  $\sigma$  is set as a much bigger value, the weights of high order features decay very fast. Actually the infinite dimensional space numerically approximates a low-dimensional subspace. On the other hand, if  $\sigma$  is set as a much smaller value, Gauss

kernel can map an arbitrary training set into a linearly separable one. Of course, this is not necessarily good since it may result in serious overfitting. On the whole, Gauss kernel is quite flexible through adjusting the parameter  $\sigma$  (or  $\lambda$ ), which makes it be one of the most widely adopted kernel functions.

#### 4. A Feature Selection Algorithm based on SVM (FS-SVM)

This paper proposes a feature selection algorithm (termed FS-SVM) based on C-SVC, which gradually removes subordinate features from the original feature set. The basic idea of FS-SVM is illustrated as follows.

When a training set is classified by applying C-SVC, the obtained normal vector of the separating hyperplane is given by:

$$\mathbf{w}^* = (w_1, w_1, \dots, w_n)^T, \quad (25)$$

If a component  $w_j = 0$ , then the decision function

$$f(\mathbf{x}) = \text{sgn}\left[\left(\sum_{i=1}^N w_i x_i\right) + b^*\right]. \quad (26)$$

does not contain the  $j$ -th feature and this feature can be removed. Generally, a component of  $\mathbf{w}^*$  with a much smaller absolute value can also be removed. In order to remove features more efficiently, FS-SVM applies C-SVC and finds the normal vector  $\mathbf{w}^*$  several times. Each time, it only removes a feature that corresponds to the component with the smallest absolute value of  $\mathbf{w}^*$ . This process continues until the classification accuracy is less than a predefined threshold. The selected features are used in the training and the test periods of the designed intrusion detection algorithm. The proposed algorithm is listed as follows.

##### Algorithm 2: Feature selection based on SVM (FS-SVM)

**Input:** the training set  $T = \{(\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_N, y_N)\} \in (R^n \times \Psi)^N$ , where  $\mathbf{x}_i = (x_{i1}, x_{i2}, \dots, x_{in})^T \in R^n$ ,  $y_i \in \Psi = \{1, -1\}$ ,  $i = 1, 2, \dots, N$ ,  $n$  is the number of original features,  $N$  is the number of samples; the threshold of classification accuracy,  $h$ .

**Output:** the selected feature set,  $\{x_1, x_2, \dots, x_d\}$ , where  $d$  is the number of selected features.

- (1) set  $k = 0$ , and construct the training set  $T_0 = T$ ;
- (2) Apply C-SVC on the training set  $T_k$ , compute the normal vector  $\mathbf{w}^*$  of the separating hyperplane, and compute the corresponding classification accuracy,  $R_{acc}$ .
- (3) if  $R_{acc} < h$ , the algorithm ends,  $T_k$  is the selected feature set, moreover,  $d = n - k$ ; otherwise, remove the feature in  $T_k$  which has the smallest absolute value of the components of  $\mathbf{w}^*$ , and obtain  $T_{k+1}$ , set  $k = k + 1$ , and go to step 2.

#### 5. An Anomaly-Based Intrusion Detection Algorithm based on Multiclass SVM with Parameters Optimized by PSO

This section presents an anomaly-based intrusion detection algorithm based on one-versus-the-rest multiclass SVM with parameters optimized by PSO.

##### 5.1. A multi-Class Classification Algorithm based on SVM

SVM is powerful for binary classification. Several methods have been proposed to extend SVM for multiclass classification. Two commonly adopted methods are one-versus-one (*i.e.*, pairwise) classification and one-versus-the-rest classification. The former needs to solve  $M(M-1)/2$  decision functions for  $M$ -class classification. Therefore, this paper adopts the latter method.



For an  $M$ -class classification problem with training set (1), (4), the one-versus-the-rest method constructs  $M$  binary classification problems. The  $j$ -th one separates the  $j$ -th class from the rest, yielding the decision function  $f^j(\mathbf{x}) = \text{sgn}(g^j(\mathbf{x}))$ ,  $j = 0, \dots, M-1$ . The next step is doing multiclass classification according to  $g^0(\mathbf{x}), \dots, g^{M-1}(\mathbf{x})$ , which classify the input  $\mathbf{x}$  to class  $J$ , where  $J$  is the superscript of the largest among  $g^0(\mathbf{x}), \dots, g^{M-1}(\mathbf{x})$ . The specific process is listed as follows ([15]).

**Algorithm 3: One-versus-the-rest multiclass SVM**

**Input:** the training set  $T = \{ (\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_N, y_N) \} \in (\mathbb{R}^n \times \Psi)^N$ , where  $\mathbf{x}_i = (x_{i1}, x_{i2}, \dots, x_{in})^T \in \mathbb{R}^n$ ,  $y_i \in \Psi = \{ 0, 1, \dots, M-1 \}$ ,  $i = 1, 2, \dots, N$ .

**Output:** a decision function,  $f(\mathbf{x})$ , to determine the class of an input  $\mathbf{x}$ .

(1) For  $j = 0, \dots, M-1$ , construct the training set of the  $j$ -th binary problem with the training set

$$T^j = \{ (\mathbf{x}_1, y_1^j), (\mathbf{x}_2, y_2^j), \dots, (\mathbf{x}_N, y_N^j) \}, \tag{27}$$

where

$$y_i^j = \begin{cases} 1, & \text{if } y_i = j; \\ 0, & \text{otherwise.} \end{cases} \tag{28}$$

Find the corresponding decision function by applying C-SVC.

$$f^j(\mathbf{x}) = \text{sgn}(g^j(\mathbf{x})). \tag{29}$$

(2) Construct the decision function

$$f(\mathbf{x}) = \arg \max_{j=0,1,\dots,M-1} g^j(\mathbf{x}). \tag{30}$$

where  $\arg \max_{j=0,1,\dots,M-1} g^j(\mathbf{x})$  means the superscript of the largest among  $g^0(\mathbf{x}), \dots, g^{M-1}(\mathbf{x})$ .

**5.2. Parameter Optimization by PSO**

There are two important parameters in Algorithm 1, 2, and 3, *i.e.*,  $C$  and  $\lambda$ . This paper adopts particle swarm optimization (PSO) algorithm to seek the optimal values of these two parameters. PSO is originally attributed to Kennedy and Eberhart ([18]). A latest overview on PSO ([19]) can be found in the initial issue of *Swarm Intelligence*.

PSO is an evolutionary algorithm. Assume a swarm consists of  $n$  particles. For the  $i$ -th particle, the position vector is represented by  $\mathbf{X}_i = (x_{i1}, x_{i2}, \dots, x_{iD})$ , and the velocity vector is represented by  $\mathbf{V}_i = (v_{i1}, v_{i2}, \dots, v_{iD})$ ,  $i = 1, 2, \dots, n$ . Each particle denotes a possible solution to a problem in a  $D$ -dimensional space. During each iteration, each particle is accelerated approaching the particle's previous best position and the global best position.  $\mathbf{P}_i = (p_{i1}, p_{i2}, \dots, p_{iD})$  and  $\mathbf{P}_g = (p_{g1}, p_{g2}, \dots, p_{gD})$  respectively represent the best previously visited position of the  $i$ -th particle and that of the swarm. The new velocity is used to calculate the next position of the  $i$ -th particle. This iteration process will end when a maximum number of iterations finish or a minimum error is achieved. The velocity and position of the  $i$ -th particle can be updated by [20]:

$$v_{id}^{l+1} = w \times v_{id}^l + c_1 \times rd_1^l \times (p_{id}^l - x_{id}^l) + c_2 \times rd_2^l \times (p_{gd}^l - x_{id}^l), \tag{31}$$

$$x_{id}^{l+1} = v_{id}^{l+1} + x_{id}^l. \quad (32)$$

where  $i = 1, 2, \dots, n$ ,  $d = 1, 2, \dots, D$ .

Notations:

- (1) the superscript  $l$  denotes the  $l$ -th iteration;
- (2)  $w$  is the nonnegative inertial weight coefficient, which affect the overall optimization ability;
- (3)  $c_1$  and  $c_2$  are learning factors;
- (4)  $rd_1^l$  and  $rd_2^l$  are positive random number ranging from 0 to 1 under normal distribution;
- (5)  $x_{id}^l$  is the  $d$ -th component in the  $D$ -dimensional position vector of the  $i$ -th particle, which represents the current value of SVM parameters,  $C$  and  $\lambda$ ;
- (6)  $v_{id} \in [v_{min}, v_{max}]$  denotes the  $d$ -th component in the  $D$ -dimensional velocity vector of the  $i$ -th particle, which determines the update direction and distance of the next generation of  $C$  and  $\lambda$ .

This paper adopts linear decreasing inertia weight ([20]). It is computed by:

$$w(l) = w_{start} - l \times \frac{w_{start} - w_{end}}{T_{max}}. \quad (33)$$

where  $l$  is the current iteration number,  $T_{max}$  is the maximum number of iteration,  $w_{start}$  and  $w_{end}$  are the maximum and the minimum values of  $w$ .

A constriction factor  $\Xi$  is adopted to the velocity evolution equation (31) to improve the convergence speed of PSO [20]:

$$v_{id}^{l+1} = \Xi \{w \times v_{id}^l + c_1 \times rd_1^l \times (p_{id}^l - x_{id}^l) + c_2 \times rd_2^l \times (p_{gd}^l - x_{id}^l)\}, \quad (34)$$

## 6. Experiments and Analyses

This section conducts experiments on KDD Cup dataset and presents analyses.

### 6.1. Dataset Description

KDD Cup dataset ([7]) includes a wide variety of intrusions simulated in a military network environment. The dataset contains a training dataset and a test dataset. The former includes 7 weeks of network traffic, and 4,898,431 connection records totally. The latter includes 2 weeks of network traffic, and 2,984,154 connection records totally. Each connection is labeled as either normal, or as an attack, with exactly one specific attack type.

KDD Cup dataset contains the following four main categories of attacks:

- (1) Denial-Of-Service (DOS): *e.g.*, syn flood.
- (2) Surveillance or probe (Probe): surveillance and other probing, *e.g.*, port scanning.
- (3) User to Root (U2R): unauthorized access to local superuser (root) privileges, *e.g.*, various “buffer overflow” attacks.
- (4) Remote to Local (R2L): unauthorized access from a remote machine, *e.g.*, guessing password.

Since the training dataset and the test dataset contain too much samples, usually a subset of 10% dataset are adopted. The 10% training dataset contains 494,021 connection records, while the 10% test dataset contains 311,029 connection records. The number and percentage of each attack category contained in these two 10% datasets are shown in Table 1.

**Table 1. Attack Categories in the 10% KDD Cup Dataset**

| Attack category | 10% Training Data |            | 10% Test Data |            |
|-----------------|-------------------|------------|---------------|------------|
|                 | # of samples      | Percentage | # of samples  | Percentage |
| Normal (0)      | 97278             | 19.69%     | 60593         | 19.48%     |
| Probe (1)       | 4116              | 0.83%      | 4166          | 1.34%      |
| DOS (2)         | 391458            | 79.24%     | 229853        | 73.90%     |
| U2R (3)         | 52                | 0.01%      | 228           | 0.07%      |
| R2L (4)         | 1126              | 0.23%      | 16189         | 5.20%      |
| Total           | 494021            |            | 311029        |            |

More importantly, the test dataset is not from the same probability distribution as the training dataset ([7]), and it includes specific attack types not in the training dataset, which is helpful to verify the effectiveness of the designed IDS. Table 2 lists the number of samples of each kind of attack in these two 10% datasets. Totally, there are 23 kinds of attacks in the 10% training dataset, while there are 38 kinds of attacks in the 10% test dataset (both including the normal connection). In the 10% testing dataset, there are 19.48% normal, 74.50% old attack, and 6.02% new attack connections which have not been shown in training set ([5]).

**Table 2. The Number of Samples of each Kind of Attack in Two 10% Datasets**

| Attack category | 10% Training Data |               | 10% Test Data |              | continue    |               |               |              |         |
|-----------------|-------------------|---------------|---------------|--------------|-------------|---------------|---------------|--------------|---------|
|                 | Attacks (23)      | # of samples  | Attacks (38)  | # of samples |             |               |               |              |         |
| Normal (0)      | normal            | 97278         | normal        | 60593        | DOS (2)     | perl          | 3             | perl         | 2       |
|                 | Probe (1)         | ip sweep      | 1247          | ip sweep     |             | 306           | rootkit       | 10           | rootkit |
| nmap            |                   | 231           | nmap          | 84           |             | loadmodule    | 9             | loadmodule   | 2       |
| portsweep       |                   | 1040          | portsweep     | 354          |             | buf_overflow  | 30            | buf_overflow | 22      |
| satan           |                   | 1589          | satan         | 1633         |             |               |               | htptunnel    | 158     |
| DOS (2)         |                   |               | saint         | 736          |             |               |               | ps           | 16      |
|                 |                   |               | mscan         | 1053         |             |               |               | sqlattack    | 2       |
|                 | back              | 2203          | back          | 1098         |             |               |               | xterm        | 13      |
|                 | land              | 21            | land          | 9            |             | ftp-write     | 8             | ftp-write    | 3       |
|                 | neptune           | 107201        | neptune       | 58001        |             | guess-passwd  | 53            | guess-passwd | 4367    |
| R2L (4)         | pod               | 264           | pod           | 87           | multihop    | 7             | multihop      | 18           |         |
|                 | smurf             | 280790        | smurf         | 164091       | phf         | 4             | phf           | 2            |         |
|                 | teardrop          | 979           | teardrop      | 12           | imap        | 12            | imap          | 1            |         |
|                 |                   |               | apache2       | 794          | spy         | 2             | spy           |              |         |
|                 |                   |               | mailbomb      | 5000         | warezclient | 1020          | warezclient   |              |         |
|                 |                   |               | udpstorm      | 2            | warezmaster | 20            | warezmaster   | 1602         |         |
|                 |                   |               | processtable  | 759          |             |               | named         | 17           |         |
|                 |                   |               |               |              |             |               | xsnoop        | 4            |         |
|                 |                   |               |               |              |             | xlock         | 9             |              |         |
|                 |                   |               |               |              |             | sendmail      | 17            |              |         |
|                 |                   |               |               |              |             | worm          | 2             |              |         |
|                 |                   |               |               |              |             | snmpgetattack | 7741          |              |         |
|                 |                   |               |               |              |             | snmpguess     | 2406          |              |         |
| <b>Total</b>    |                   | <b>494021</b> |               |              |             |               | <b>311029</b> |              |         |

Both the training dataset and the test dataset are in ASCII format, and adopt the same record format. Each line represents a connection record, which contains 41 features ([7]), excluding the label of attack category.

## 6.2. The Selected Features

Although the KDD Cup dataset contains 41 features, most of them are valueless for anomaly intrusion detection. Therefore, the proposed FS-SVM algorithm (the threshold  $h$  is set as 97.5%) is first applied on the training dataset to select the best features. After applying FS-SVM, 18 features are selected, which are listed in Table 3, where the first column represents the original sequence number of each selected feature. Therefore, the sample data reduction achieved by FS-SVM is over 57.14% ( $=24/42$ ), where the denominator is the number of features including the label.

For fair comparison, all these four algorithms adopt the selected features.

**Table 3. The Selected Features of KDD Cup Dataset**

| Number | Name                        | Description   | Data type  |
|--------|-----------------------------|---|------------|
| 2      | protocol_type               | type of the protocol, e.g. tcp, udp, etc.   | symbolic   |
| 3      | service                     | network service on the destination, e.g., http, telnet, etc.                                | symbolic   |
| 4      | flag                        | normal or error status of the connection  | symbolic   |
| 5      | src_bytes                   | number of data bytes from source to destination   | continuous |
| 6      | dst_bytes                   | number of data bytes from destination to source   | continuous |
| 11     | num_failed_logins           | number of failed login attempts   | continuous |
| 16     | num_root                    | number of "root" accesses   | continuous |
| 23     | count                       | number of connections to the same host as the current connection in the past two seconds    | continuous |
| 24     | srv_count                   | number of connections to the same service as the current connection in the past two seconds | continuous |
| 27     | error_rate                  | % of connections that have "REJ" errors   | continuous |
| 29     | same_srv_rate               | % of connections to the same service  | continuous |
| 30     | diff_srv_rate               | % of connections to different services  | continuous |
| 33     | dst_host_srv_count          | Count of connections having the same destination host and using the same service            | continuous |
| 34     | dst_host_same_srv_rate      | % of connections having the same destination host and using the same service                | continuous |
| 35     | dst_host_diff_srv_rate      | % of different services on the current host   | continuous |
| 36     | dst_host_same_src_port_rate | % of connections to the current host having the same src port                               | continuous |
| 37     | dst_host_srv_diff_host_rate | % of connections to the same service coming from different hosts                            | continuous |
| 39     | dst_host_srv_serror_rate    | % of connections to the current host and specified service that have an S0 error            | continuous |

## 6.3. Experimental Results and Analyses

Compared with the actual state of connections, the detection results can be classified into four categories:

- (1) False positive ( $F_P$ ): a normal connection is falsely detected as an attack.
- (2) False negative ( $F_N$ ): an attack is falsely detected as a normal connection.
- (3) True positive ( $T_P$ ): an attack is correctly detected as an attack.
- (4) True negative ( $T_N$ ): a normal connection is correctly detected as a normal connection.

Three performance measures are introduced in this paper to evaluate the performance of the designed intrusion detection system:

- (1) *Detection accuracy* is the proportion of correctly detected attacks and normal connections to the total number of connections. It is computed by:

$$Accuracy = \frac{T_P + T_N}{T_P + T_N + F_P + F_N}. \quad (35)$$

- (2) *FP rate* is the probability of identifying a normal connection as an attack. It is computed by:

$$FP\ rate = \frac{F_P}{F_P + T_N} \tag{36}$$

(3) *FN rate* is the probability of identifying an attack as a normal connection. It is computed by:

$$FN\ rate = \frac{F_N}{F_N + T_P} \tag{37}$$

A well-designed intrusion detection system should ensure as high detection accuracy as possible, meanwhile as low FP rate and FN rate as possible.

This paper implements FS-SVM and MSVM-PSO in Matlab with LIBSVM ([21]). The parameter *C* and of  $\lambda$  SVM varies from 0.01 to 50,000.

This paper also compares MSVM-PSO with three commonly adopted models, *i.e.*, Bayesian, K-Means and MSVM-grid.

Taking the 10% training dataset, the classifiers are respectively trained by MSVM-PSO, MSVM-grid, Bayesian, and K-Means. Then taking the 10% test dataset, the trained classifiers are adopted to classify each connection into five categories. Figure 3 illustrates the resulting confusion matrices of these four algorithms.

| Actual     | Predict    |           |         |         |         |
|------------|------------|-----------|---------|---------|---------|
|            | Normal (0) | Probe (1) | DOS (2) | U2R (3) | R2L (4) |
| Normal (0) | 59368      | 257       | 919     | 0       | 49      |
| Probe (1)  | 453        | 3536      | 152     | 0       | 25      |
| DOS (2)    | 5147       | 23        | 224674  | 0       | 9       |
| U2R (3)    | 5          | 0         | 12      | 201     | 10      |
| R2L (4)    | 519        | 11        | 147     | 0       | 15512   |

(a) MSVM-PSO

| Actual     | Predict    |           |         |         |         |
|------------|------------|-----------|---------|---------|---------|
|            | Normal (0) | Probe (1) | DOS (2) | U2R (3) | R2L (4) |
| Normal (0) | 58945      | 623       | 784     | 0       | 241     |
| Probe (1)  | 1019       | 2415      | 329     | 0       | 403     |
| DOS (2)    | 6009       | 123       | 223695  | 1       | 25      |
| U2R (3)    | 0          | 0         | 23      | 194     | 11      |
| R2L (4)    | 1611       | 9         | 419     | 5       | 14145   |

(b) MSVM-grid

| Actual     | Predict    |           |         |         |         |
|------------|------------|-----------|---------|---------|---------|
|            | Normal (0) | Probe (1) | DOS (2) | U2R (3) | R2L (4) |
| Normal (0) | 58711      | 651       | 1092    | 0       | 139     |
| Probe (1)  | 973        | 2619      | 313     | 0       | 261     |
| DOS (2)    | 5901       | 45        | 223904  | 3       | 0       |
| U2R (3)    | 30         | 0         | 16      | 177     | 5       |
| R2L (4)    | 1538       | 11        | 317     | 2       | 14321   |

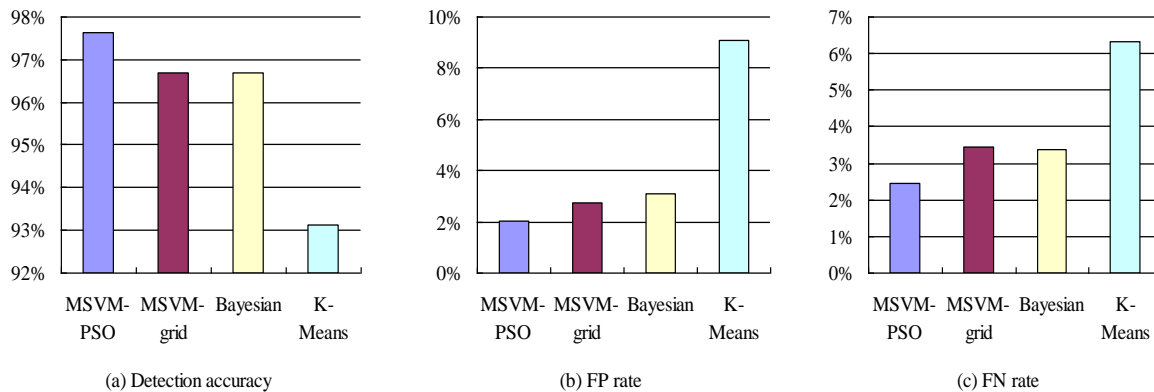
(c) Bayesian

| Actual     | Predict    |           |         |         |         |
|------------|------------|-----------|---------|---------|---------|
|            | Normal (0) | Probe (1) | DOS (2) | U2R (3) | R2L (4) |
| Normal (0) | 55084      | 1530      | 2737    | 0       | 1242    |
| Probe (1)  | 906        | 2666      | 347     | 0       | 247     |
| DOS (2)    | 11041      | 765       | 218047  | 0       | 0       |
| U2R (3)    | 0          | 0         | 19      | 203     | 6       |
| R2L (4)    | 3902       | 518       | 541     | 0       | 11228   |

(d) K-Means

**Figure 3. The Confusion Matrices of MSVM-PSO, MSVM-grid, Bayesian, and K-Means**

According the confusion matrices, the above three performance measures of these four algorithms are calculated and plotted in Figure 4.



**Figure 4. The Performance Measures of MSVM-PSO, MSVM-grid, Bayesian, and K-Means**

From Figure 3 and Figure 4, it can be concluded that the performance of Bayesian obviously outperforms that of K-Means; the performance of MSVM-grid is close to that of Bayesian; while the performance of MSVM-PSO outperforms that of all other three algorithms. The underlying reasons are summarized as follows.

(1) K-Means is a clustering-based and unsupervised method, while the other three methods are supervised. The supervised methods take full advantage of the label information of KDD Cup dataset. Therefore, they obviously outperform K-Means.

(2) SVM-based techniques are powerful for nonlinear and high dimensional classification problems. Even though MSVM-grid adopts the most simple and primitive parameter optimization method (*i.e.*, grid), its performance is very close to that of Bayesian. Equipped with a more effective parameter optimization method (*i.e.*, PSO), the performance of MSVM-PSO is obviously enhanced. The detection accuracy of MSVM-PSO is 97.64%; while the FP rate and the FN rate are 2.02% and 2.45% respectively.

## 7. Conclusion and Future Work

This paper proposes SVM-based techniques to implement anomaly intrusion detection. A SVM-based feature selection algorithm (FS-SVM) is proposed to reduce the dimensionality of sample data. A multiclass SVM algorithm with parameters optimized by PSO (MSVM-PSO) is presented to learn a classifier to detect multiclass attacks. The experimental results verify the effectiveness and performance of the proposed techniques. The future work of this paper will extend the proposed techniques to new computing environments (*e.g.*, Cloud) to detect anomalous physical or virtual nodes. Extensive experiments will be conducted to testify the performance of the SVM-based techniques.

## Acknowledgments

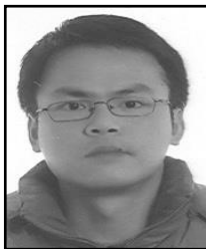
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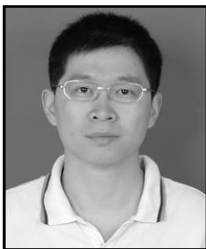


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