

Canadian Journal of Civil Engineering

Application of the factor method to the service life prediction of architectural concrete

Canadian Journal of Civil Engineering
cjce-2018-0452.R1
Article
02-Dec-2018
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service life, factor method, architectural concrete
Durability and Climate Change



1	Application of the factor method to the service life prediction of
2	architectural concrete
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4	- Word count: 8992 equivalent words -
5	Abstract:

Architectural concrete surfaces are a durable solution, but their deterioration process is 6 unavoidable, beginning as soon as the element is built. This study establishes a methodology 7 for predicting the service life of architectural concrete surfaces, through the application of the 8 factor method. For this purpose, 239 architectural concrete surfaces in in-service conditions 9 are analysed. Different durability factors are studied, evaluating their impact in the service life 10 of architectural concrete surfaces. Different scenarios are analysed for the quantification of 11 the durability factors. Scenario 4 presents the best results, leading to a higher similarity 12 between the estimated service lives predicted by the factor method and obtained by the 13 graphical method. The application of the factor method, as described in this study, allows 14 predicting the service life of architectural concrete surfaces. An estimated service life ranging 15 between 43 and 48 years was obtained, which agrees with the literature and empirical 16 knowledge. 17

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19 Keywords: service life, factor method, architectural concrete.

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20 **1. Introduction**

21 For decades, concrete has been essentially used as a structural material, protected by different types of coatings. Currently, concrete has been progressively used as a decorative 22 solution, designated architectural concrete. In this study, architectural concrete is defined as 23 24 any concrete surface used as exterior finishing of a building or structure, without any coating other than paint or varnish (Silva et al. 2017). The main difference between architectural 25 concrete and structural concrete lies on the exposed surfaces of architectural concrete, which 26 is more relevant than the strength of the material (Peurifov and Oberlender 2011). These 27 exposed concrete elements can present countless color tones, shapes and types of finishing, 28 resulting in a cladding solution with a remarkable aesthetic quality (Cassar et al. 2003; 29 Freedman 2007). 30

Despite being a durable solution, the degradation process of architectural concrete is 31 32 inevitable, and starts as soon as the element is put into use. Nowadays, various studies have been performed to evaluate the durability and service life of concrete structures (Liang et al. 33 2002; Ahmad 2003; Alghamdi and Ahmad 2014). Nevertheless, as mentioned by Hongke et al. 34 (2016), these studies are limited to the material itself, neglecting the real exposure conditions. In 35 this sense, the research related with the service life of architectural concrete under real exposure 36 conditions is insufficient, since the environmental degradation agents, the age of the element 37 and other durability factors are rarely considered in existing research works. 38

In current practice, under most circumstances, the repair works performed in architectural concrete surfaces are the same regardless of the cause and the extent of the anomaly observed (Farahmandpour et al. 2000). This situation occurs mainly due to the lack of knowledge regarding the impact of different degradation mechanisms in the durability and service life of architectural concrete surfaces. Therefore, the definition of maintenance strategies depends on the knowledge regarding the expected service life of the element, under specific conditions of use, as well as the quantification of the actions required during this period of time (Kessler et al. 2017). This knowledge could lead to more effective measures and different repair techniques according to the different anomalies observed, aiding the optimization of the periodicity of maintenance plans, which is crucial to evaluate the economic and environmental impacts of concrete surfaces through the building's life cycle (Flores-Colen and de Brito 2010).

This study intends to propose a methodology to predict the physical service life of 50 architectural concrete surfaces, through the application of the factor method. The model proposed 51 allows encompassing different durability factors, related with the quality of the materials, design 52 characteristics and environmental exposure conditions, which influence the physical service life of 53 architectural concrete surfaces. The factor method (FM) is established based on the analysis of the 54 55 degradation state of 239 architectural concrete surfaces in in-service conditions. The observed reality is translated by a numerical index and a graphical method (GM), which allow estimating 56 the service life of each architectural concrete surface analysed, according to the anomalies 57 observed, their severity and extent. The results obtained by the FM are compared with those 58 obtained by the GM (which portrays the reality observed in fieldwork), for each case study within 59 the sample analysed. 60

61 2. Background

The service life prediction of buildings components has been gaining importance, for several 62 reasons. The resources available for maintenance and rehabilitation actions are scarce and should 63 be planned in order to maximize the results obtained. To achieve this goal, the decision to 64 intervene should be based on the knowledge of the degradation processes and their interaction 65 with the building materials (Leira et al. 1999). The service life of a building component is 66 intrinsically linked to its sustainability; data regarding the durability of a building component, 67 68 when subjected to specific conditions of use, are essential to compare the durability and, consequently, the economic and environmental impacts, of different solutions over the same 69

70 period of time.

71 According to ISO 15686 (2011), the service life is the period of time, after a building is put to use, during which the building and its elements meet or exceed the minimum performance 72 requirements. The performance requirements are strongly related with users and owners demands 73 and expectations, and the "minimum" acceptable level of performance is usually conditioned by 74 subjective criteria, such as aesthetic reasons, the building's social and economic context, the funds 75 available for maintenance actions, among others. The concept of service life, although always 76 based on the same fundamental assumptions, presents slight differences between authors. Some of 77 them concern, for example, whether or not the buildings should be subjected to periodic 78 79 maintenance actions during this period (Silva et al. 2016).

Currently, there are various methodologies for the service life prediction of buildings and 80 their components. Among these, the factor method stands out, since it is considered a general 81 framework for service life prediction and its application is standardised by ISO 15686 (2011). 82 This method, initially proposed by the Architectural Institute of Japan (AIJ 1993), introduces an 83 easy and expedient way to calculate the estimated service life (ESL) of a component, 84 considering all variables, which are likely to affect its degradation process. This methodology is 85 based on a reference service life (RSL), which is the expected service life for that component, 86 87 under standard conditions of use. The reference service life is subsequently multiplied by a number of factors that affect the durability of the building element under analysis (as shown in 88 Equation (1)), either positively or negatively, depending on whether the elements' 89 characteristics are better or worse than those considered as the reference (ISO 15686: 2011; 90 Straub 2015). 91

$$ESL = RSL \times A \times B \times C \times D \times E \times F \times G$$
(1)

Where *ESL* represents the estimated service life, *RSL* is the reference service life, factor A
is the quality of the construction material, factor B is the design level, factor C is the level of

execution, factor D is related to the characteristics of the external environment, factor Econcerns the characteristics of the indoor environment, factor F depends on the characteristics of use and factor G is the maintenance level.

The factor method has been criticized due to the simplicity with which it models a complex 97 phenomenon. Some of the criticisms refer that this method only provides an empirical estimate 98 of the service life of a given component (Hovde 2002; Marteinsson 2003). The correct 99 application of this method requires that the different durability factors are well known and 100 adequately quantified, to ensure that credible results are obtained (Hovde 2004). In addition, the 101 method has a high sensitivity for small variations of the data, and there is no clear methodology 102 103 for estimating the reference service life. Despite this, the factor method remains the only 104 standardised methodology for predicting the service life of a building component, due to its simplicity and ability to adapt when new techniques or information arise. 105

3. Degradation phenomena of architectural concrete facades

107 The degradation phenomena of architectural concrete surfaces are analysed based on the 108 evaluation of the degradation condition of several case studies in-use conditions, with 109 different ages and characteristics. In this sense, the degradation condition of 239 architectural 110 concrete surfaces is evaluated, during an extensive fieldwork. Each architectural concrete 111 surface is evaluated through a visual inspection, gathering the relevant information to 112 characterise this case study, mapping all the anomalies present in the surface.

The main anomalies that can occur in architectural concrete are (Silva et al. 2017): stains; efflorescence; biological growth; erosion; bug holes; *graffiti*; mapped cracking; oriented cracking; disaggregation; spalling; flatness defects; honeycombing; fastening marks; dribbling; crusts; and formwork incrustation. These anomalies are divided in three main groups (Figure 1): i) aesthetics anomalies; ii) mechanical anomalies; and iii) constructive anomalies.

119 **3.1. Degradation model**

To evaluate the overall degradation condition of the architectural concrete surfaces inspected, a numerical index, called severity of degradation (S_w) , is used. This numerical index, initially proposed by Gaspar and de Brito (2008, 2011), considers the area affected by each anomaly, its degradation level and the relative weight of the anomaly detected - Equation (2).

$$S_w = \frac{\sum (A_n \times k_n \times k)}{A \times \sum (k_{max})}$$
(2)

Where S_w represents the severity of degradation of architectural concrete surfaces, in %, Ais the area of the architectural concrete surface affected by the anomaly n, in m², k is the multiplication factor for the anomaly n, as a function of their degradation level (k_n varies between 0 and 4, as shown in Table 1), $k_{a,n}$ is the weighting coefficient according to the relative weight of the anomaly detected (equal to 1 if no specification is referred, i.e. equal to 1 by default), A is the total surface area, in m² and $\sum(k_{max})$ is the sum of the weighting coefficients, corresponding to the highest possible level of degradation.

The coefficient k allows taking into account the severity of a given anomaly, by defining 132 different degradation levels according to the percentage of area affected by the anomaly, as well 133 as the impact of this anomaly in the overall degradation of the architectural concrete surface. In 134 this study, five degradation levels are established, ranging from A (with no visible degradation) to 135 E (most unfavorable condition). Table 1 shows the different degradation levels for each anomaly 136 137 considered and also the limits that correspond to each level. The anomalies with more serious consequences, for the degradation of architectural concrete surfaces, are only represented at 138 higher levels, e.g. oriented cracking with an opening higher than 3 mm only appears at levels 3 139 and 4, as it is considered quite serious, compromising the integrity and safety of the concrete 140 surface. 141

142 After calculating the value of S_w , for all the case studies inspected in this study, it was

possible to define an average degradation curve, obtained through a third-degree polynomial 143 regression analysis. Figure 2 presents the degradation curve achieved, which graphically 144 represents the evolution of the degradation of architectural concrete surfaces over time. The 145 coefficient of determination - R^2 (R^2 varies between 0 and 1, revealing a regression model 146 with no correlation to the data and a perfect correlation, respectively) - obtained for the 147 polynomial curve, which describes the average curve of degradation, is 0.74. The value 148 obtained reveals a strong correlation between the curve and the sample analyzed, in which 149 74% of the variability of the severity of degradation of concrete surfaces can be explained by 150 their age. 151

In this study, it is conventionally considered that an architectural concrete surface with a value of S_w equal to 20% has reached the end of its physical service life. To illustrate the physical condition associated to the end of physical service life of an architectural concrete surface, Figure 2 presents a case study that has reached the end of its physical service life. Once the service life limit is defined, it is possible to calculate the expected service life value for architectural concrete surfaces. In this study, an average estimated service life of 43 years is obtained, based on the degradation curve.

3.2. Extrapolation of the degradation curve for each point of the sample and calculation of the estimated service life for each case

Based on the overall degradation curve, a graphical method can be adopted to determine the estimated service life for all the surfaces under analysis. For this purpose, the ordinates' conversion factor method is used, in which a new curve is drawn (similar to the overall degradation curve), which passes through each of the sample's points, determining the age after which a severity of degradation of 20% is reached.

166 In the ordinates' conversion factor method, a factor k, which corresponds to the ratio 167 between the ordinates of two points A and M, is determined. M is a point on the average degradation curve, which has an age equal to A ($x_A = x_M$). The ordinate of A is the value of its severity of degradation (calculated by Equation (2)) and the ordinate value of M is the value of the degradation curve for that age. The value of k is multiplied by the function f (equation of the average degradation curve), to estimate a function f', as presented in Equation 3, which contains the point A (i.e., the degradation curve that intersects A, thus representing the specific degradation curve of this point) (Magos et al. 2016).

$$f' = k \times f = k \times a \times x^3 + k \times b \times x^2 + k \times c \times x$$
(3)

174 Where *f* represents the function of the average degradation curve, f' is the function of the 175 degradation curve for each point, *k* is the ratio factor between the two curves and *a*, *b* and *c* 176 are the polynomial curve constants of degree 3 that define the function *f*.

177 The application of this graphical method to the sample led to an average estimated service178 life of 48 years for architectural concrete surfaces.

179 4. Identification and weighting of the factors that influence the durability of 180 architectural concrete facades

ISO 15686 (2011) suggests seven durability factors, divided into: material characteristics 181 (A); design conditions (B); execution conditions (C); inner environment characteristics (D); 182 external environmental characteristics (E); use conditions (F) and maintenance level (G). 183 Some of the factors mentioned in ISO 15686 (2011) are not considered in this study, either 184 because it is not possible to obtain reliable information during the fieldwork survey or 185 because they are not relevant for the service life prediction of architectural concrete surfaces 186 (Marques et al., 2018). In this study, the following factors are considered relevant for the 187 explanation of the degradation of architectural concrete: 188

Factor A - regarding the materials characteristics, two durability factors are analysed,
 the first related with the color of the surface (A1) and the second related with the
 surfaces' treatment (A2);

Factor B - for the design characteristics, the type of finishing (B1) is the only factor
 analysed;

Factor C - in this study, this factor is not considered, since the execution conditions 194 are difficult to evaluate only based on visual inspections carried out on surfaces many 195 years after their execution; moreover, the case studies found with serious failures due 196 to execution errors were excluded from this study, because they did not represent the 197 natural degradation evolution of an architectural concrete façade over time, i.e. this 198 study intends to predict the service life of architectural concrete surfaces, modelling 199 the natural degradation process of these elements, in this sense, discrete or 200 unpredictable events can not be modelled mathematically; 201

- Factor *D* this factor is not considered in this study, because the conditions of the interior environment did not influence the degradation process of the outer coatings;
- Factor *E* the characteristics of the external environment strongly influence the degradation process of external architectural concrete surfaces. In this durability factor, five durability factors are considered: surfaces orientation (*E*1); distance from the sea (*E*2); exposure to damp (*E*3); the surface's level of protection (*E*4); and exposure to wind/rain action (*E*5);
- Factor *F* the use conditions factor is difficult to estimate; the only situation resulting
 from incorrect use is *graffiti*. However, actions such as vandalism or accidents cannot
 be modelled since they do not evolve in a predictable way over time. Therefore, this
 factor is not considered;
- Factor *G* regarding the maintenance conditions, only the factor "ease of inspection" is considered.

The quantification of the weighting values of the durability factors considered in this study is done based on two methods (Silva et al. 2016): i) degradation curves, in which an average degradation curves is established for the different characteristics of architectural concrete surfaces,
estimating the average estimated service life for each characteristic; ii) and using the graphical
method, estimating the average estimated service life for the surfaces with the characteristic under
analysis. Moreover, the quantification of the durability factors also considers their physical
meaning.

ISO 15686 (2011) proposes three values for quantifying the durability factors included in 222 the factor method: 1.2 for favorable conditions and characteristics, which positively affect the 223 service life of the element analysed; 1.0 for reference conditions (or when it is not possible to 224 draw clear conclusions regarding the influence of this factor on the service life of the building 225 226 component); and 0.8 for conditions and characteristics that adversely affect the service life of the element analysed. McDuling et al. (2008) suggests a broader approach, proposing the 227 adoption of five possible values for the quantification of the durability factors, according to the 228 exposure conditions: 1.2 (clearly favorable); 1.1 (slightly favorable); 1.0 (slightly aggressive); 229 0.9 (aggressive); 0.8 (very aggressive). These values are thus adopted in a preliminary 230 quantification of the durability factors (in section 5.3 various scenarios are analysed, to fine tune 231 the quantification of the durability factors, to improve the capability of the factor method to 232 233 describe the observed reality).

Table 2 shows the preliminary quantification of the durability factors, considering the estimated service life obtained by the graphical method and the degradation curves. The results achieved through the graphical method are generally very close to those obtained through the degradation curves. These results allow understanding the influence of the different factors analysed on the degradation of architectural concrete surfaces, i.e. it is possible to quantify the effect of each sub factor to increase or decrease the estimated service life of these surfaces, thus allow distinguishing the favorable from the unfavorable situations.

As for the color of the surface, the application of the values obtained by the graphical method

reveals that light-colored surfaces present a predicted service life higher than dark surfaces. Darker concrete surfaces tend to show higher degradation levels, since they absorb more solar radiation, than those with lighter shades, and are therefore subjected to greater thermal variations and internal stresses, which contribute to increase cracking and spalling anomalies (Wojciechowski et al. 2014).

For the various factors analysed, the maximum and minimum values of estimated service 247 lives are obtained according to the surfaces' treatment. The maximum value is around 79 248 years for surfaces with paint plus water repellent protection, and the minimum value is 36.5 249 years, for surfaces with varnish. The fact that the extreme values are obtained for this 250 251 characteristic reveals its relevance to the degradation of architectural concrete surfaces. 252 Custódio and Eusébio (2006) refer that external varnished surfaces are extremely susceptible to degradation phenomenon due to the exposure to solar radiation. These surfaces can present 253 an estimated service life between 5 to 10 years (Hopper 2007) and, if not properly maintained, 254 the end of the varnish's service life may adversely affect the natural process of degradation of 255 a concrete surface. Therefore, in this study, surfaces without protection and with varnish are 256 considered the unfavorable situation. On the opposite, surfaces with paint plus water repellent 257 protection present the highest estimated service life, corresponding to the most favorable 258 condition. 259

For the type of finishing, the results obtained by the two methods are consistent. In the sample analysed, textured surfaces present a higher estimated service life than smooth surfaces. This finding is not consensual in the literature. Various authors (PCA 2007; Lahdensivu et al. 2013) refer that textured surfaces are more prone to dirt deposition and biological growth. Köliö et al. (2016) refer that concrete surfaces treated while fresh (e.g. brushed or floated) present a more open porous system, which increases the carbonation rate in dry periods, but also promotes a faster wetting of the surfaces subjected to driving rain. Hurd (1990) refers that smooth concrete surfaces are not easy to obtain, since it is difficult to achieve completely uniform surfaces, without defects due to the casting process and free from bug holes, which leads to the premature appearance of anomalies. The author refers that some designers choose to adopt textured surfaces rather than smooth ones, to avoid these problems. In a preliminary analysis, the type of finishing is considered a neutral factor, but when the durability factors are fine-tuned, it is considered that textured surfaces correspond to the favorable condition, to be coherent with the results observed during the fieldwork survey.

The surfaces' orientation is divided in four categories (Silva et al. 2016; Serralheiro et al. 274 2017): North (N); Northeast, East and Southeast (NE/E/SE); West and Northwest (W/NW); and 275 276 South and Southeast (S/SE). The concrete surfaces analysed are located in Portugal (north 277 hemisphere), and therefore, the discussion of the influence of the surfaces' orientation in their degradation condition is performed accordingly with the region under analysis. In the sample 278 analysed, S/SW oriented surfaces are the less durable, reaching the end of service life sooner. In 279 Portugal, surfaces facing S/SW present longer periods of UV radiation, which promote the 280 occurrence of anomalies due to higher thermal gradients (Serralheiro et al. 2017). W/NW and 281 NE/E/SE correspond to an intermediate situation, without a clear pattern of which orientation is 282 worse. Surfaces facing SE/E/NE also present a higher exposure to the direct incidence of UV 283 284 radiation (Garrido et al. 2012); surfaces facing W/NW are more exposed to the combined effects of wind and rain (Silva et al. 2016). Surfaces facing North present higher estimated 285 service lives; even though these surfaces are more exposed to damp, it seems that the lower 286 287 incidence of solar radiation increases the durability of architectural concrete surfaces. The results obtained seem to indicate that UV radiation is a degradation agent with a significant 288 impact on the surfaces' service life, promoting the occurrence of aesthetics anomalies (e.g. 289 discoloration and darkening) and cracking. 290

291 Concerning distance from the sea, the results obtained through the degradation curves are

coherent, revealing that concrete surfaces in coastal areas (less than 1 km) are the unfavorable condition, reaching the end of service life sooner. The further away from the coastline, the higher the surfaces' estimated service life will be. Concrete surfaces more distant from the coastline are less prone to chemical, physical and mechanical degradation due to the presence of sea salts (e.g. chloride ions), which induce the occurrence of severe anomalies (Islam et al. 2018).

Regarding exposure to damp, Pereira et al. (2018) refer that damp is an aggressive degradation agent and one of the main causes of defects, being responsible for intense changes in the overall appearance of concrete surfaces. The results obtained in both methods are consistent, revealing that surfaces with a high exposure to damp reach the end of service life sooner.

Concerning the surfaces' protection and exposure to wind/rain action, the results obtained 303 by the degradation curves are more reliable. The surfaces' protection considers the 304 surrounding conditions, such as vegetation and adjacent buildings, which increase the 305 surfaces' protection against the environmental agents. As expected, surfaces with unfavorable 306 exposure conditions (without protection and with high exposure to wind-rain action) reach the 307 end of service life sooner, since the incidence of prevailing winds and precipitation lead to 308 309 higher stresses in concrete surfaces, promoting the degradation of these elements (Pakkala et al. 2014, 2016). 310

Regarding the ease of inspection, this factor considers the height of the building, assuming two categories (Silva et al. 2016): surfaces that are easily observed (i.e. yes), for buildings up to three storeys high; and surfaces that are not easily inspected, for buildings with more than three floors. Taller buildings present a lower ESL (according to the degradation curves), since they are more exposed to the degradation agents (e.g. wind and rain), which increase the propensity to present higher degradation levels (Lahdensivu et al. 2013).

5. Application of the factor method to the service life prediction of architectural concrete

318 **5.1. Reference service life**

This study addresses the physical service life of architectural concrete surfaces, considering that a surface that reaches a degradation condition corresponding to a severity of degradation of 20% comes to the end of its service life. In this sense, to determine the value of the reference service life, the two previous average values of the estimated service life of architectural concrete surfaces are considered, but two additional methods are also considered (Galbusera et al. 2014; Emídio et al. 2014; Silva et al. 2016).

First, the method of the average exposure conditions for a case is applied. In this method, the reference service life is calculated by estimating the average estimated service life of architectural concretes characterized by standard conditions (i.e. surfaces that feature all the subfactors equal to 1.0). The reference service life (*RSL*) is thus calculated for the case studies closest to the standard conditions. For the sample analyzed, the *RSL* is calculated for surfaces with less than three factors different from 1.0 (since none of the case studies present all the subfactors equal to 1.0). With this method, the reference service life value was 42.1 years.

The second method is that of average exposure conditions, for the entire sample. The following procedure was used: the reference service life was calculated for all surfaces in the sample; then, the relationship between the expected service life through the graphical method and the reference service life is calculated. Subsequently, the *RSL* is given by the average of the values where the *ESL/RSL* ratio's standard deviation is < 3%. Using this method, a *RSL* of 44.8 years is obtained.

338 The reference service life adopted is 43.8 years, corresponding to the average *RSL* 339 obtained using these four methodologies.

340 **5.2.** Calculation formula

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Once the durability factors are identified and the reference service life is determined, it is

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possible to establish the mathematical equation that enables the practical application of thefactor method to the service life prediction of architectural concrete surfaces (Equation (4)).

344
$$ESL = RSL \times A1 \times A2 \times B1 \times E1 \times E2 \times E3 \times E4 \times E5 \times G1$$
(4)

Where *ESL* represents the estimated service life, *RSL* the reference service life (equal to 43.8 years), *A*1 the color of the surface, *A*2 the type of the surface treatment, *B*1 is the type of finishing, *E*1 the surfaces orientation, *E*2 the distance from the sea, *E*3 the exposure to damp, *E*4 the surfaces level of protection, *E*5 the exposure to wind-rain action, and *G*1 the ease of inspection.

349 5.3. Quantification of the factor method's sub-factors

For the quantification of the durability factors, four scenarios are analysed, always considering the physical meaning of the results obtained in the previous sections, which allow evaluating the influence of each factor in the degradation of architectural concrete surfaces. In this sense, the factors with an unfavorable effect in the estimated service life of architectural concrete surfaces always present a k value lower or equal to average and favorable conditions. The following scenarios are thus considered:

Scenario 1 is a neutral scenario, in which a value of 1.00 is assigned to all the durability factors analysed in this study. This scenario allows evaluating the neutral behavior of the proposed model and is only used as comparison with other models.
 The analysis of this scenario intends to evaluate the relevance and usefulness of applying the factor method to the service life prediction of architectural concrete surfaces;

In Scenario 2, the values of each sub factor are assigned according to the ISO
 15686: 2011, i.e. 0.80 for the factors that have an unfavorable effect in the
 estimated service life of architectural concrete surfaces, 1.00 for current situations
 or difficult to access, and 1.20 for the factors considered as favorable;

• Scenario 3 adopts a similar methodology as scenario 2, but in scenario 3, the k

values are 0.90, 1.00 and 1.10. This scenario allows analysing the sensitivity of the
model to small variations in the quantification of the durability factors (Emídio et
al. 2014; Marques et al. 2018);

Finally, scenario 4 corresponds to an optimised scenario, in which the durability
 factors are quantified through an iterative process, intending to obtain the
 combination of *k* values that minimise the deviation between the estimated service
 life obtained by the factor method and the values observed in fieldwork (graphical
 method).

Table 3 shows the quantification of the durability factors according to the different scenarios considered.

377 6. Discussion of the results

The different scenarios are analysed and validated through the comparison between the 378 estimated service life obtained using the factor method (using the different scenarios for the 379 quantification of the durability factors) and the graphical method. The graphical method is 380 based on the reality observed during fieldwork, describing, in a mathematical way, the 381 degradation condition of the surfaces analysed, evaluating the real influence of the different 382 factors to their estimated service life. Therefore, to evaluate the accuracy of the different 383 scenarios proposed, different statistical indicators are used, which consider the ratio between 384 the estimated service life obtained through the factor method (FM) and the estimated service 385 life obtained through the conversion to the average degradation curve (GM), as follows 386 (Emídio et al. 2014; Silva et al. 2016; Marques et al. 2018): 387

The relationship between the average ESL, using the factor method and the graphical method, should not differ from 1 by more than 5% (i.e. the maximum range is [0.95;
1.05]);

391

• The amplitude of the results obtained through the factor method must be lower than

392	the amplitude of the results of	obtained through the	graphical method;
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The results obtained through the factor method must be credible and therefore comply 393 with the limits considered as acceptable for the expected service life of architectural 394 concrete surfaces. In this study, as a minimum value an ESL of 22 years is considered, 395 which corresponds to around half the average expected service of architectural concrete 396 surfaces, according to the sample analysed; moreover, Köliö et al. (2014) refer that the 397 visible damage in concrete facades became visible within 21 and 25 years after 398 construction. For the maximum limit, an estimated service life of 100 years is assumed 399 400 (PCA, 2007);

The cumulative frequency of the ratio between MF/MG, greater than or equal to 0.85, must be greater than 50%;

- The cumulative frequency of the MF/MG ratio, greater than 1.50, should be less than
 10% (i.e. the number of failed estimations should be less than 10%);
- The various iterations should maximise the number of surfaces belonging to the
 interval from 0.85 to 1.15, for the MF/MG ratio.

Table 4 shows the statistical indicators resulting from the application of each of the 407 scenarios considered. As expected, scenario 1 presents the worst overall results, with the 408 409 higher percentage of failed estimations. For scenario 2, the average of the ratio between the results obtained using the factor method and the graphical method presents a variation higher 410 411 than 5%. In this scenario, the average estimated service life, achieved through the factor 412 method (around 36 years), is quite reduced, in comparison with the average ESL obtained by 413 the graphical method (around 48 years). In scenario 3, the average of the ratio between the FM and the GM is 0.97, fulfilling the defined criteria. This scenario presents an improved 414 415 performance when compared with the previous scenarios analysed. Nevertheless, the results obtained seem to indicate that the values proposed by the ISO 15686: 2011 standard are too 416

broad (have low sensitivity and adaptability) and do not have the capacity of significantlyincreasing the number of cases whose MF/MG ratio is in the range of 0.85 to 1.15.

Scenario 4, as expected, presents the best overall results, since the quantification of the 419 durability factors is based on an iterative process to maximise the similarity between the ESL 420 predicted by the factor method and the ESL observed in reality (GM). This scenario fulfills all 421 the defined acceptance criteria. In this scenario, a MF/MG ratio of 1.02 is obtained and the 422 percentage of case studies whose MF/MG ratio is in the range of 0.85 to 1.15 is also the 423 highest of all scenarios (45.1%), thus revealing that about 45% of the sample has a variation 424 of less than 15% compared to the ideal situation, which would be to obtain a service life 425 426 estimated by the factorial method equal to the service life estimated by the graphical method. 427 Scenario 4 shows a significant improvement (about 11%) in terms of the cumulative frequency of MF/MG results between 0.85 and 1.15, compared to the second-best scenario 428 (scenario 3). 429

The methodology followed in this study has been adopted by the authors to other building 430 components, with good results, namely to renderings (Gaspar and de Brito 2008), ceramic 431 claddings (Galbusera et al. 2014), natural stone claddings (Emídio et al. 2014; Silva et al. 432 2016), paintings (Magos et al. 2016) and ETICS (Marques et al. 2018). Nevertheless, in the 433 434 specific case of architectural concrete surfaces, the factor method led to worse results than when applied to other elements of the buildings' envelope, which reveal that some relevant 435 factors are not included in the proposed model. The technology involved in the execution of 436 architectural concrete surfaces and the formulation of the concrete applied as cladding 437 solution have a significant influence on the durability of the surfaces. Since this study 438 analyses the performance of architectural concrete based only on visual inspections, some 439 aspects related with the design and execution of architectural concrete surfaces (e.g. the 440 concrete formulation and composition, the exposure class, the cover's thickness) cannot be 441

442 considered in the service life prediction model. This limitation can explain the variability of443 the degradation phenomena that is not encompassed in the proposed model.

This study is a first approach for the application of the factor method to the service life 444 prediction of architectural concrete surfaces in Portugal, and future studies are required to 445 improve the proposed model. Nevertheless, the results obtained are in accordance with the 446 reality and the empirical knowledge regarding the durability of architectural concrete 447 surfaces. Figure 3 shows the histogram of the estimated service life predicted by the factor 448 method, adopting the quantification of the durability factors proposed in scenario 4, and the 449 histogram of the service life predicted by the graphical method. The different methodologies 450 451 lead to coherent results ranging between 43 years (for the overall degradation curve, presented 452 in Figure 2) and 48 years (GM). The average estimated service life obtained by the proposed model for architectural concrete surfaces is in accordance to different studies related with the 453 durability and service life of architectural concrete: i) adopting a similar methodology, 454 Serralheiro et al. (2017) obtained an estimated service life of 44 years for architectural concrete 455 surfaces; ii) Pakkala et al. (2014) refer that the expected service life of architectural concrete 456 surfaces should be lower than 50 years, which is the service life conventionally accepted for 457 structural concrete, considering that these surfaces are directly exposed to the degradation 458 459 agents; iii) Takahashi et al. (2008) proposed an estimated service life of 50 years for precast concrete applied as external claddings. 460

461 7. Conclusions

462 Currently, there is a lack of reliable data and methodologies to evaluate the durability and 463 service life of architectural concrete surfaces in in-service conditions. Moreover, the existing 464 studies only address the characteristic of concrete (mechanical properties, composition, 465 among other parameters), neglecting the influence of the real exposure conditions and the 466 environmental degradation agents in the degradation of concrete elements. Moreover, the lack 467 of knowledge regarding the impact of different degradation agents in the service life of 468 architectural concrete surfaces usually leads to the adoption of standardised measures for 469 maintenance and repair of these elements, regardless of the cause, the extent and the severity 470 of the anomaly observed.

Therefore, this study intends to propose the application of the factor method for the service life prediction of architectural concrete surfaces, thus allowing encompassing different durability factors that influence the service life of architectural concrete surfaces. In this study, 239 architectural concrete surfaces are analysed *in situ*.

This study proposes a mathematical equation for the practical application of the factor 475 method to the service life prediction of architectural concrete surfaces. In order to apply the 476 477 proposed equation, practitioners should use the durability factors quantified by scenario 4, which shows the best overall results, i.e. this scenario allows maximising the similarity 478 between the ESL predicted by the factor method and the ESL observed in reality. The results 479 obtained show that the values predicted, by the model, are in accordance with reality and the 480 empirical knowledge regarding the durability of architectural concrete surfaces. However, the 481 application of the factor method to the service life prediction of architectural concrete, and the 482 mathematical equation proposed, as well as the quantification of the durability factors as 483 484 suggested in this study, should not be taken as an absolute truth, but rather as the best approach to the sample analysed. In this sense, the equation and the quantification of the 485 durability factors proposed in this study can be used, as proposed, in similar contexts (with 486 487 similar exposure to environmental conditions). Moreover, the proposed method can be applied in other geographical contexts (mainly in Europe and other developed countries in the 488 North hemisphere), with some adaptations (e.g. considering the effects of freeze/thaw cycles). 489 The proposed model can be easily adapted, by tailoring the durability factors, adjusting the 490 mathematical formulation to the specific reality and context of the architectural concrete 491

analysed.

The factor method is an adequate and easily applicable tool for the service life prediction of architectural concrete surfaces, which can aid the establishment of maintenance and repair requirements, according to the potential degradation mechanisms and the correspondent estimated service life.

This study is a first approach for the application of a standardised service life prediction method to architectural concrete surfaces, providing some guidance, which can be used in future research. In future studies, this method can be applied to a new universe of cases, since the larger the sample analysed, the greater the reliability and applicability of the factor method.

Despite the various limitations, that this method presents, in an overall analysis, its application is expeditious and highly operational, especially when considering the complexity and the numerous factors that influence the evolution of the degradation of an external cladding. Due to these advantages, the factor method is the basis of international standards, as a general framework for estimating the service life of buildings and their elements.

507 Acknowledgements

The authors gratefully acknowledge the support of the CERIS-ICIST Research Institute, IST, University of Lisbon and the FCT (Foundation for Science and Technology) through project PTDC/ECM-COM/5772/2014.

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- 614 Figure 1. Anomalies in architectural concrete: a) biological growth (aesthetics); b) mapped cracking
- 615 (mechanical); and c) honeycombing (constructive)
- Figure 2. Degradation curve obtained for the 239 architectural concrete surfaces analyzed, and an illustrative
- 617 case study that has reached the end of its physical service life
- 618 Figure 3. Histograms of the ESL obtained by factor and graphical methods

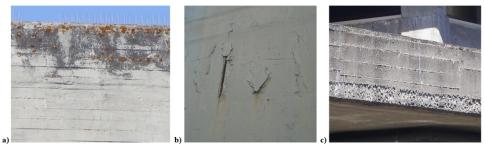
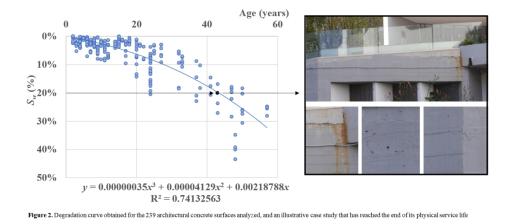


Figure 1. Anomalies in architectural concrete: a) biological growth (aesthetics); b) cracking and disaggregation/spalling (mechanical); and c) honeycombing (constructive)

138x46mm (300 x 300 DPI)



149x63mm (300 x 300 DPI)

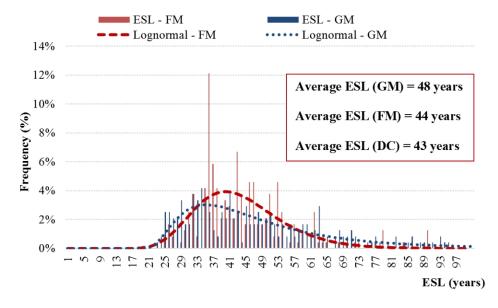


Figure 3. Histograms of the ESL obtained by factor and graphical methods

100x64mm (300 x 300 DPI)

Table 1. Degradation levels for the different anomalies observed in architectural concrete surfaces (data

Anomalies	Anomalias description	1.		Degradation level				
group	Anomalies description	k _{a,n}	Level A	Level B	Level C	Level D	Level E	
	Dirt stains	0.15						
	Moisture stains	0.15		<15%	15% to 40%	> 40%		
Aasthatia	Corrosion stains	0.50						
Aesthetic anomalies	Wear/erosion	2.00					-	
anomanes	Bug holes	0.10		< 100/	10% to 30%	> 30%		
	Biological growth	0.60		< 10%	10% 10 30%	> 30%		
	Efflorescence	0.20	-					
	Disageragetion/spalling	5.00/	No visible		< 10%	10% to 30%	> 30%	
	Disaggregation/spalling	4.00		-	< 1070	107010 3070	> 30%	
Mechanical	Oriented cracking (≤ 0.5 mm)	1.00	degradation		< 5%	-	-	
anomalies	Oriented cracking	1.00	degradation			\geq 5%		
anomanes	(> 0.5 mm and < 3 mm)				-	≥ 370	-	
	Oriented cracking (\geq 3 mm)	1.00			-	< 5%	\geq 5%	
	Mapped cracking	0.15			-	< 50%	$\geq 50\%$	
	Flatness defects	0.10		< 20%	20% to 50%	> 50%		
C	Dribbling	0.10	-	< 10%	$\geq 10\%$	-		
Constructive anomalies	Fastening marks	0.10			$\leq 5\%$	> 5%	-	
anomanes	Honeycombing	0.30		-	< 10%	> 1.09/		
	Formwork incrustation	0.10			× 10%	$\geq 10\%$		

sourced from Serralheiro et al., 2017)

Table 2. Service life predicted by the graphical method and by the degradation curves for the durability

factors under analysis

Surface	s' characteristics		Graphical method	Degradation curves	<i>k</i> initial value
Color (41)	Dark	<i>k</i> 1	42.6	46.0	0.95
Color (A1)	Light	k2	50.2	42.6	1.00
	Without protection	<i>k</i> 1	47.3	43.9	0.80
	Paint	k2	48.9	39.0	1.10
Surfaces'	Water repellent	k3	49.2	39.3	1.00
treatment (A2)	Paint + water repellent	<i>k</i> 4	67.5	79.1	1.20
	Varnish	k5	36.5	42.7	0.80
Type of finish	Flat	<i>k</i> 1	46.7	41.7	1.00
(B1)	Textured	k2	53.1	45.3	1.00
	North	<i>k</i> 1	50.7	42.3	1.00
Orientation $(E1)$	W/NW	k2	47.7	46.8	0.90
Orientation (E1)	SE/E/NE	<i>k</i> 3	48.3	40.0	1.00
	S/SW	<i>k</i> 4	47.3	40.7	0.80
	< 1 km	<i>k</i> 1	47.3	35.5	0.90
Distance from the sea (E2)	Between 1 km and 5 km	k2	52.0	44.5	1.00
	> 5 km	<i>k</i> 3	46.0	48.5	1.10
Exposure to	Low	<i>k</i> 1	51.5	45.9	1.10
damp (E3)	High	k2	45.0	39.9	1.00
Surfaces'	With protection	<i>k</i> 1	47.3	45.3	1.00
protection (E4)	Without protection	k2	49.8	37.5	0.90
Wind/rain	Low	<i>k</i> 1	45.3	45.6	1.00
exposure (E5)	High	k2	49.9	42.0	0.95
Ease of	Yes	<i>k</i> 1	47.3	45.3	1.20
inspection (G1)	No	k2	49.8	37.5	1.00

Con	ditioning factors	Scenario 2 Scenario 3 Scenario 4			
Color	Dark	<i>k</i> 1	0.80	0.90	0.900
	Light	k2	1.00	1.00	1.200
Surface Without protection		<i>k</i> 1	0.80	0.90	0.800
treatment	Paint	k2	1.00	1.00	1.100
	Water repellent	<i>k</i> 3	1.00	1.00	1.025
	Paint + water repellent	<i>k</i> 4	1.20	1.10	1.200
	Varnish	<i>k</i> 5	0.80	0.90	0.900
Type of finish	Flat	<i>k</i> 1	1.00	1.00	0.800
	Textured	k2	1.20	1.10	1.200
Orientation	North	<i>k</i> 1	1.20	1.00	1.100
	W/NW	k2	1.00	1.00	1.000
	SE/E/NE	<i>k</i> 3	1.00	1.00	1.000
	S/SW	<i>k</i> 4	0.80	0.90	0.850
Distance from	< 1 km	<i>k</i> 1	0.80	0.90	0.800
the sea	Between 1 km and 5	k2	1.00		
	km			1.00	0.950
	> 5 km	<i>k</i> 3	1.20	1.10	1.000
Exposure to	Low	<i>k</i> 1	1.20	1.10	1.000
damp	High	k2	1.00	0.90	0.875
Surface	With protection	<i>k</i> 1	1.00	1.00	1.050
protection	Without protection	k2	0.80	0.90	1.000
Wind/rain	Low	<i>k</i> 1	1.00	1.00	1.250
exposure	High	k2	0.80	0.90	1.000
Ease of	Yes	<i>k</i> 1	1.00	1.10	1.050
inspection	No	k2	0.80	1.00	1.000

Table 3	Factors	for	each	of the	scenarios	considered
Table 5.	Factors	101	each	or the	scenarios	considered



Sce	narios	1	2	3	4
FM/GM av	1.04	0.85	0.97	1.02	
Standar	d deviation	0.37	0.37	0.35	0.37
	Factor method (years)	0.0	58.31	37.63	65.60
Amplitude of results	Graphical method (years)	85.29	85.29	85.29	85.29
Extremes values	Maximum = 100 years	43.42	72.67	63.49	89.89
obtained in the factor method	Minimum = 22 years	43.42	14.35	25.87	24.29
FM/GM ≥	64.85%	47.28%	61.51%	70.71%	
FM/GM ≥	12.97%	5.86%	6.69%	8.79%	
$0.85 \leq FN$	I/GM ≤ 1.15	28.45%	31.96%	34.31%	45.19%

Table 4.	Statistical	indicators	of the	scenarios	considered