APPROXIMATING CSISZÁR f–DIVERGENCE BY THE USE OF TAYLOR'S FORMULA WITH INTEGRAL REMAINDER

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Abstract. Some approximations of the Csiszár f − divergence by the use of Taylor's formula and perturbed Taylor's formula and some applications for Kullback-Leibler distance are given.

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Paper MIA-05-42

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