

Astrophysics and cosmology with a deci-hertz gravitational-wave detector: TianGO

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We present the astrophysical science case for a space-based, deci-Hz gravitational-wave (GW) detector. We particularly highlight an ability in inferring a source’s sky location, both when combined with a network of ground-based detectors to form a long triangulation baseline, and by itself for the early warning of merger events. Such an accurate location measurement is the key for using GW signals as standard sirens for constraining the Hubble constant. This kind of detector also opens up the possibility of testing type Ia supernovae progenitor hypotheses by constraining the merger rates of white dwarf binaries with both super- and sub-Chandrasekhar masses separately. We will discuss other scientific outcomes that can be delivered, including the precise determination of black hole spins, the constraint of structure formation in the early Universe, and the search for intermediate-mass black holes.

I. INTRODUCTION

The coming decades will be an exciting time for gravitational-wave (GW) astronomy and astrophysics throughout the frequency band ranging from nano- to kilohertz. In the 10–10,000 Hz band, second generation detectors including Advanced LIGO (aLIGO) [1], Advanced Virgo (aVirgo) [2], and KAGRA [3] are steadily improving towards their designed sensitivities. Meanwhile, various upgrades to current facilities have been proposed, including the incremental A+ upgrade [4] and the Voyager design which reach the limits of the current infrastructures [5]. In long terms, third generation detectors including the Einstein Telescope [6, 7] and Cosmic Explorer [8] are under active research and development. In the millihertz band, LISA is planned to be launched in the 2030s [9]. TianQin is another proposed space-borne mission that is sensitive in the tens to hundreds of millihertz band [10, 11]. At even lower frequencies, pulsar timing arrays are becoming evermore sensitive with more pulsars being added to the network [12, 13]. Nonetheless, gaps still exist between these missions. This especially limits our ability to have a coherent, multi-band coverage of the same source; even a relatively massive $30 M_{\odot}$ - $30 M_{\odot}$ black hole (BH) binary at 0.01 Hz (where LISA is most sensitive) will not enter a ground detector’s sensitive band until 20 years later.

Therefore, we propose a space-based detector, TianGO, which is sensitive in the 0.01–10 Hz band and which fills the gap between LISA and the ground detectors [14]. A possible advanced TianGO (aTianGO) would have 10 times better sensitivity, but is not discussed further here. In this paper we expand on the pioneering work of Ref. [15] and explore the scientific promise of TianGO. Our work also sheds light on other decihertz concepts [16, 17].

Fig. 1 shows the sensitivity of TianGO and other ma-

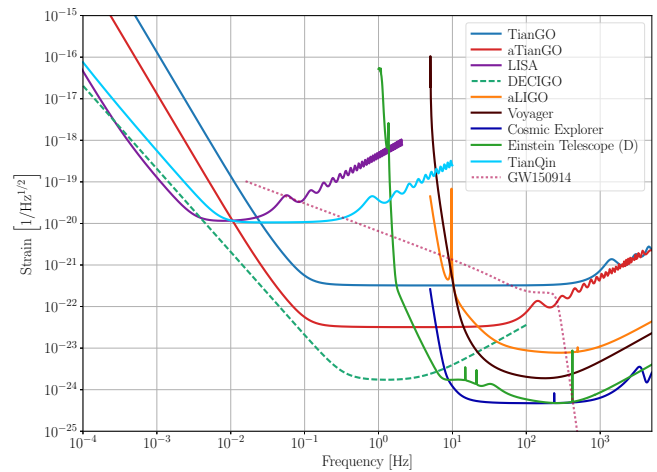


FIG. 1. Sensitivities of future ground and space gravitational wave detectors. The sensitivities are averaged over sky location and polarization. The LISA curve includes two 60° interferometers and the ET curve includes three 60° interferometers. The curve labeled “GW150914” is $2\sqrt{f}h$, where h is the waveform of the first gravitational wave detected [18] starting five years before merger.

for detectors. For the rest of the paper, unless otherwise stated, the ground detectors are assumed to have the Voyager design sensitivity [5] and the ground network consists of the three LIGO detectors at Hanford (H), Livingston (L), and Aundha, India (A); Virgo (V) in Italy; and KAGRA (K) in Japan. The corresponding detection horizons for compact binary sources of different total mass are shown in Fig. 2. For stellar-mass compact objects such as neutron stars (NSs) and BHs, TianGO has a comparable range as the ground detectors. Moreover, even a relatively light NS binary starting at 0.12 Hz, where TianGO is most sensitive, will evolve into the ground detectors’ band and merge within 5 years. This facilitates a multi-band coverage of astrophysical sources.

In particular, by placing TianGO in an orbit from be-

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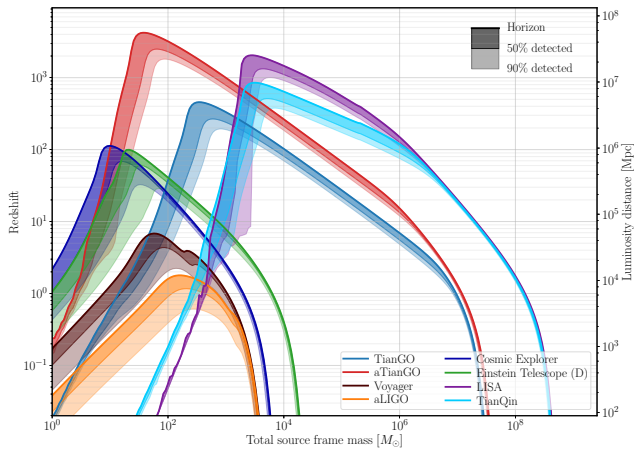


FIG. 2. Horizons for equal mass compact binaries oriented face on for the detectors shown in Fig. 1. The maximum detectable distance, defined as the distance at which a source has an SNR of 8 in a given detector, is computed for 48 source locations uniformly tiling the sky. The horizon is the maximum distance at which the best source is detected, 50% of these sources are detected within the dark shaded band, and 90% of the sources are detected within the light shaded band. If a source stays in a space detector’s sensitivity band for more than 5 years, the 5 year portion of the system’s evolution that gives the best SNR in each detector is used.

tween a 5 and 170 s light travel time from the Earth, the localization of astrophysical sources is significantly improved over that possible with a ground network alone: when combined with the ground network, this extra long baseline allows a combined TianGO-ground network to increase the angular resolution by a factor of 50 over that of the ground alone. This exquisite ability to localize sources enables a combined TianGO-ground network to do precision cosmography. Furthermore, since a binary of two NSs or of a NS and BH will stay in TianGO’s sensitivity band for several years, TianGO will provide an early warning to the ground and electromagnetic telescopes.

Since a source will have many inspiraling cycles while it evolves in TianGO’s band, inspiral parameters, such as effective spin, can be determined with an accuracy greatly exceeding the capabilities of ground detectors. TianGO also opens up the possibility of measuring low-frequency phenomena, like modulations due to the spin precession, which further allows us to construct a 2-dimensional map of the spin distribution of binary BHs.

Meanwhile, there are astrophysical sources that can only be studied by a decihertz detector like TianGO. For example, mass transfer starts at about 30 mHz for a typical white dwarf (WD) binary each with a mass of $0.6 M_{\odot}$. This frequency will be higher for even more massive, super-Chandrasekhar WD binaries. As LISA’s sensitivity starts to degrade above 10 mHz, TianGO will be the most sensitive instrument to study the interactions between double WDs near the end of their binary

evolution, which may eventually lead to type-Ia supernova explosions. Intermediate-mass black holes (IMBHs) are another potential source best studied by a decihertz detector. TianGO is sensitive to the mergers of both a binary of IMBHs and an IMBH with a stellar-mass compact companion. Consequently, TianGO will be the ideal detector to either solidly confirm the existence of IMBHs with a positive detection or strongly disfavor their existence with a null-detection.

The remainder of this paper is organized as follows. We discuss the precision with which binary BHs can be localized with a joint TianGO-ground network and the application to cosmography in Section II. We then examine TianGO’s ability to localize coalescing binary NSs and to serve as an early warning for ground and EM telescopes, the most crucial component for multi-messenger astrophysics, in Section III. This is followed by our study of the progenitor problem of type Ia supernovae in Section IV. We then discuss the detectability of tidal interactions in binary WDs with TianGO in Section V. In Section VI we analyze TianGO’s ability to accurately determine both the effective and the precession spin, and how we may use it to constrain the formation channels of stellar-mass BH binaries as well as the efficiency of angular momentum transfer in the progenitor stars. In Section VII we discuss the possibility of using TianGO to distinguish the cosmological structure formation scenarios and to search for the existence of IMBHs. Lastly, we conclude in Section VIII.

II. GRAVITATIONAL-WAVE COSMOGRAPHY

The Hubble constant H_0 , quantifying the current expansion rate of the universe, is one of the most important cosmological parameters, yet the two traditional methods of measuring it disagree at the 4.4σ level [19]. The first method relies on the physics of the early universe and our understanding of cosmology to fit observations of the CMB to the Λ CDM cosmological model [20]. The second, local measurement, relies on our understanding of astrophysics to calibrate a cosmic distance ladder in order to relate the redshifts of observed sources to their luminosity distances [19]. Gravitational wave astronomy adds a third method of determining H_0 and the prospect of resolving this tension [21–25], a task for which a combined TianGO-ground network is particularly well suited.

To obtain the redshift-distance relationship necessary to determine H_0 , the local measurement first determines the redshift of a galaxy. The luminosity distance cannot be measured directly, however, and relies on the calibration of a cosmic distance ladder to provide “standard candles.” On the other-hand, the luminosity distance is measured directly from a GW observation requiring no calibration and relying only on the assumption that general relativity describes the source. This makes gravitational waves ideal “standard sirens.” If the host galaxy of a gravitational wave source is identified, optical tele-

scopes can measure the redshift.¹ In this way, both the redshift and the distance are measured directly. The BNS GW170817 was the first GW source observed by both gravitational optical telescopes [27]. Since the gravitational wave signal was accompanied by an optical counterpart, the host galaxy was identified and the first direct measurement of H_0 using this method was made [28].

Identifying the host galaxy to make these measurements requires precise sky localization from the GW detector network. This ability is greatly enhanced when TianGO is added to a network of ground detectors. TianGO will either be in a Earth-trailing orbit of up to 20° or an orbit at the L2 Lagrange point [14] thereby adding a baseline of between $1.5 \times 10^6 \text{ km} = 235 R_\oplus$ and $5.2 \times 10^7 \text{ km} = 8.2 \times 10^3 R_\oplus$ to the network, where R_\oplus is the radius of the Earth. Since the same source will be observed by both TianGO and the ground network, the timing accuracy formed by this large baseline significantly improves the sky localization ability over that of the ground alone, as is illustrated in Figs. 3 and 10 and Table I.

The top panel of Fig. 3 shows the angular resolution $\Delta\Omega$ as a function of redshift as determined from the network of ground detectors alone, TianGO alone, and the combined network of the ground and TianGO in a 5° Earth-trailing orbit. The source is a BBH with $\mathcal{M}_c = 25 M_\odot$, $q = 1.05$, and $\iota = 30^\circ$. (The probability of detecting binaries with a given inclination peaks around $\iota = 30^\circ$ [29]. The same figure for $\iota = 0^\circ$ is shown in Fig. 10.) The extra long baseline formed by TianGO and the ground network improves the angular uncertainty by a factor of ~ 50 .

The middle panel of Fig. 3 shows the fractional uncertainty $\Delta D_L/D_L$ in measuring the luminosity distance. Note that the inference accuracy for the ground network is limited by the distance-inclination degeneracy. (This is especially true for face-on sources as can be seen by comparing Figs. 3 and 10.) TianGO breaks this degeneracy due to the time-dependent antenna pattern caused by its tumbling orbit. The combined TianGO-ground uncertainty is thus significantly better than that of the ground alone.

The bottom panel of Fig. 3 shows the uncertainty in comoving volume localization ΔV_C .² If an optical counterpart is not observed, or does not exist as is likely for most of the sources for which the TianGO-ground network will be sensitive, the GW detector network must localize the host to a single galaxy. To estimate the number of galaxies contained in a comoving volume ΔV_C , the value of $0.01 \text{ galaxies/Mpc}^3$ is assumed. The combined network can localize a source to a single galaxy up to a redshift of $z \sim 0.5$ for the best face-on sources, and to $z \sim 0.35$

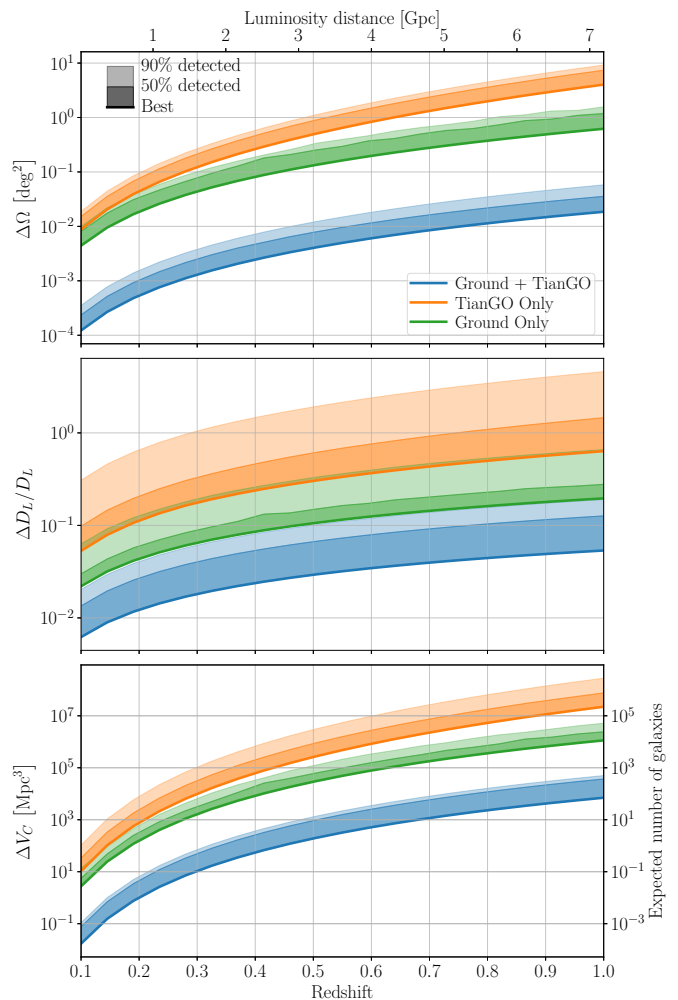


FIG. 3. Sky localization, luminosity distance, and volume localization precision as a function of redshift for a binary black hole system with $\mathcal{M}_c = 25 M_\odot$, $q = 1.05$, and an inclination $\iota = 30^\circ$ and TianGO in a 5° Earth trailing orbit. The density $0.01 \text{ galaxies/Mpc}^3$ is used to convert ΔV_C to expected number of galaxies. Fig. 10 shows the same for face on binaries.

for the median sources at $\iota = 30^\circ$.

Even if the host galaxy cannot be uniquely identified, galaxy catalogs can be used to make a statistical inference about the location of the source [21, 30–32]. This method has been used to reanalyze the measurement from GW170817 to infer H_0 without the unique galaxy determination provided by the observation of the optical counterpart [33] and has been used to improve the original analysis of Ref. [28] with further observations of BBHs without optical counterparts [34]. Future work will quantify the extent to which the TianGO-ground network’s exquisite sky localization can improve the reach of these methods.

¹ The GW standard sirens can also be used to independently calibrate the EM standard candles forming the cosmic distance ladder [26].

² The Planck 2015 cosmology is assumed [20].

TABLE I. Comparison of sky localization for different networks of detectors. The neutron star system is a binary with $\mathcal{M}_c = 1.2 M_\odot$, $q = 1.05$, and $D_L = 50$ Mpc. The black hole system is a binary with $\mathcal{M}_c = 25 M_\odot$, $q = 1.05$, and $D_L = 600$ Mpc. The best and median sources are given in deg^2 . The ground detectors have the Voyager design sensitivity.

Network	Neutron Star		Black Hole	
	Best	Median	Best	Median
HLV	7.9×10^{-3}	4.1×10^{-2}	1.1×10^{-2}	5.4×10^{-2}
HLVKA	2.0×10^{-3}	5.6×10^{-3}	3.1×10^{-3}	8.5×10^{-3}
T	3.5×10^{-5}	5.4×10^{-5}	4.4×10^{-3}	1.1×10^{-2}
HLVKA + L2 T	1.6×10^{-5}	2.9×10^{-5}	5.4×10^{-4}	1.5×10^{-3}
HLVKA + 5° T	5.7×10^{-6}	1.3×10^{-5}	6.6×10^{-5}	1.9×10^{-4}
HLVKA + 20° T	1.3×10^{-6}	3.5×10^{-6}	1.6×10^{-5}	5.2×10^{-5}

III. EARLY WARNING OF BINARY NEUTRON STAR COALESCENCE

The joint detection of a coalescing binary NS in GW [27] and γ -ray [35], and the follow-up observation of the post-merger kilonova in electromagnetic radiations [36] heralds the beginning of an exciting era of multi-messenger astronomy. While the first detection has provided some valuable insights on the nature of short γ -ray bursts and kilonovae, significantly more are expected to come from future multi-messenger observations [37]. The success of such a joint observation relies critically on the GW observatories to release an accurate sky map of the source's location in a timely manner, and TianGO is an ideal instrument to perform the early warning and localization of coalescing NS (or NS-BH) binaries. As a typical NS binary will stay in TianGO's band for a few years before the final merger, the Doppler phase shift and time-dependent antenna patterns due to TianGO's orbital motion enables it to localize the source by itself with high accuracy.

This is illustrated in detail in Fig. 4 and Table I. Fig. 4 shows the *cumulative angular uncertainty* for a typical NS binary with $(M_1, M_2) = (1.4 M_\odot, 1.35 M_\odot)$. More specifically, on the bottom of the frame we show the GW frequency up to which we integrate the data, and on the top of the frame we show the corresponding time to the final merger, given by

$$t_m(f) = 5.4 \left(\frac{\mathcal{M}_c}{1.2 M_\odot} \right)^{-5/3} \left(\frac{f}{1 \text{ Hz}} \right)^{-8/3} \text{ days.} \quad (1)$$

We assume that the source has a face-on orientation, yet we vary its right ascension and declination to cover the entire sky. Two representative distances, $D_L = 50$ Mpc and $D_L = 100$ Mpc, are shown in the plot. With TianGO alone, we can localize the majority of sources to within a few $\times 10^{-3}$ deg^2 approximately 10 days before the final merger. This provides sufficient time for the GW network to process the data and inform the electromag-

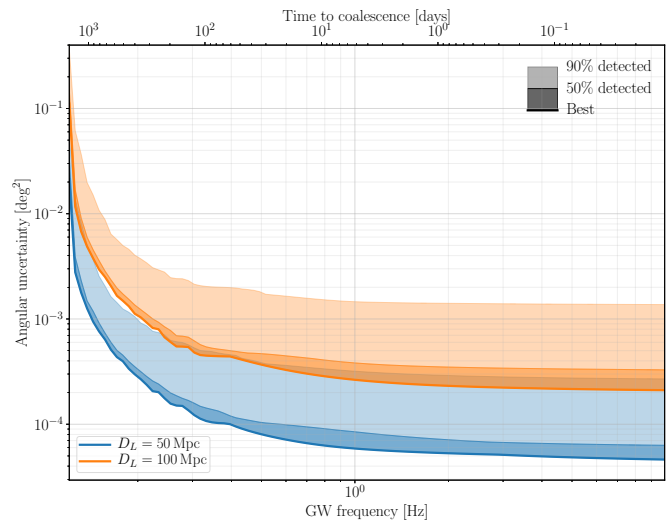


FIG. 4. Angular uncertainty as determined by TianGO alone for a face-on BNS (at 12 source locations uniformly tiling the sky) with $(M_1, M_2) = (1.4 M_\odot, 1.35 M_\odot)$ as a function of GW frequency or, equivalently, time to coalescence.

netic observatories to prepare the telescopes for the final merger.

Furthermore, the localization accuracy for NS binaries obtained by TianGO alone is in fact nearly 100 times better than a network of 5 ground detectors each with Voyager's designed sensitivity (LHVKA; see Table I), and is much smaller than the typical field of view of an optical telescope of $\mathcal{O}(1)$ square-degree.

In addition to post-merger emissions, TianGO also significantly enhances the possibility of capturing the potential precursor emissions during the inspiral phase (see, e.g., Section 2.2 of Ref. [38]). One example is the energy release due to shattering of the NS crust [39], which is suspected to be the source of short- γ -ray burst precursors [40]. The timing when the precursor happens is directly related to the equation of state of materials near the crust-core interface. Additionally, if at least one of the NS is highly magnetized, the orbital motion during the inspiral may also trigger an electron-positron pair fireball that will likely emerge in hard X-ray/gamma ray [41]. In the radio band, the magnetospheric interaction may also extract the orbital energy and give rise to a short burst of coherent radio emission [42]. Such an emission could be a mechanism leading to fast radio bursts [43]. With TianGO's ability to accurately pinpoint a source days prior to the merger, one can unambiguously associate a precursor emission at the right time and location to coalescing binary NSs.

IV. BINARY WHITE DWARVES AS PROGENITORS OF TYPE IA SUPERNOVAE

Type Ia supernovae are one of the most powerful family of standard candles for determining the cosmologi-

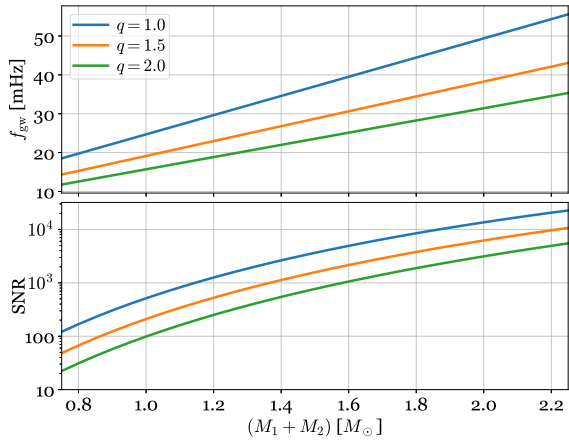


FIG. 5. Upper panel: the GW frequency for WD binaries with different total masses and mass ratios at the onset of Roche-lobe overflow. Bottom panel: angle-averaged SNR seen by TianGO, assuming a source distance of 10 kpc and an observation period of 5 years.

cal distance [44] and they have led to the discovery of the accelerating expansion of the Universe [45]. However, the identity of their progenitors remains an unresolved problem in modern astrophysics despite decades of research. Among all possibilities, the merger of two WDs (also known as the double-degenerate progenitor) is an increasingly favored formation channel, yet it is still unclear if the system’s total mass exceeding the Chandrasekhar limit is a necessary condition for a supernova explosion (for recent reviews, see Refs. [46, 47]). In this section we show how TianGO can help to improve our understanding of the problem.

The key is that TianGO is capable of individually resolve essentially *all* the Galactic WD binaries when they are close to starting or have just started mass transfer. This is illustrated in Figure 5. In the upper panel, we show the GW frequency for WD binaries at the onset of the Roche-lobe overflow. Here we assume a simple mass-radius relation for WDs as

$$R_{\text{wd}}(M_{\text{wd}}) = 10^9 \left(\frac{M_{\text{wd}}}{0.6 M_{\odot}} \right)^{-1/3} \text{ cm}, \quad (2)$$

and we find the orbital separation such that the donor star’s radius is equal to the volume-equivalent radius of its Roche lobe [48]. For such systems, the SNR (averaging over both sky location and source orientation) seen by TianGO over a 5-year observation period is shown in the lower panel. The source distance is fixed at 10 kpc. TianGO thus allows us to construct thorough statistics on the WD population which can further be used to calibrate theoretical population synthesis models (e.g., Refs. [49, 50]). Then, comparing the merger rate of double WDs predicted in the model to the observed type Ia supernovae rate allows a test of the double-degenerate

progenitor hypothesis.

Specifically, for a population of WDs driven by GW radiation only, the number density per orbital separation $n(a)$ should scale with the orbital separation a as

$$n(a) \propto \begin{cases} a^3 & \text{for } \alpha \geq -1, \\ a^{\alpha+4} & \text{for } \alpha < -1, \end{cases} \quad (3)$$

where α is the power-law index of the population’s initial separation distribution. This scaling is valid for binaries with a current separation of $a \ll 0.01$ AU and prior to Roche-lobe overflow. Once we determine the constant of proportionality with TianGO, we can then predict the merger rate as $n(a)da/dt$ [46].

While LISA is expected to detect a similar number of WD binaries as TianGO, there are nonetheless unique advantages of TianGO in constraining the binary WD population. Note that a WD binary in LISA’s more sensitive band of 1-20 mHz will evolve in frequency by so little over a ~ 5 -year observation that it either is unresolvable or can only be used to measure the system’s chirp mass. In the case of the type Ia supernovae progenitor problem, however, it is the system’s total mass and mass ratio that are of interest. TianGO, on the other hand, is more sensitive to systems at higher frequencies ($\gtrsim 20$ mHz) and therefore will see a greater amount of frequency evolution. Moreover, those systems will experience a stronger tidal effect which depends on the masses in a different way than the chirp mass, allowing for a determination of the component masses (see Section V for more details). Consequently, with TianGO we can determine the distributions for double WD systems with different total masses. This is critical for examining the possibility of sub-Chandrasekhar progenitors [51–54].

At the same time, TianGO will also be able to identify the deviation of the power-law distribution for different WD binaries due to the onset of mass transfer. The stability of the mass transfer is a complicated problem that depends on factors like the system’s mass ratio, the nature of the accretion, and the efficiency of tidal coupling [55–59]. TianGO will provide insights on this problem by both locating the cutoffs in the distribution that marks the onset of unstable mass transfer, and measuring directly the waveforms of the surviving systems that may evolve into AM CVn stars [60]. TianGO also has the potential of resolving the current tension between the observed spatial density of AM CVn stars and that predicted by population synthesis models [61].

V. DETECTING WHITE DWARF TIDAL INTERACTIONS

When a WD binary’s orbit decays due to GW radiation, tidal interaction starts to play an increasingly significant role in its evolution. In this section we discuss the prospects of detecting tides in WDs with TianGO.

The tidal response of a fluid can be decomposed into an equilibrium component and a dynamical component.

In the equilibrium tide, the fluid distribution follows the gravitational equipotential instantaneously. In most situations, this already captures the large-scale distortion of the star. The dynamical tide, on the other hand, accounts for the star’s dynamical response to the tidal forcing and represents the excitation of waves. Whereas for NSs in coalescing binaries the equilibrium component dominates the tidal interaction [62–64], for WDs in binaries, it is the dynamical tide that has the most significant effect.

As shown in Refs. [65–69], when a WD binary enters TianGO’s band, the dynamical tide can keep the WD’s spin nearly synchronized with the orbit. Consequently,³

$$\dot{\Omega}_{s,1} \simeq \dot{\Omega}_{s,2} \simeq \dot{\Omega}_{\text{orb}}, \quad (4)$$

where $\Omega_{s,1(2)}$ is the angular spin velocity of mass 1 (2). In terms of energy, we have

$$\frac{\dot{E}_{\text{tide1(2)}}}{\dot{E}_{\text{pp}}} \simeq \frac{3}{2} \frac{I_{1(2)} \Omega_{\text{orb}}^2}{E_{\text{orb}}} \propto f^{4/3}. \quad (5)$$

Here $\dot{E}_{\text{tide1(2)}}$ is the amount of energy transferred per unit time from the orbit to the interior of mass 1(2) and being dissipated there, $I_{1(2)}$ is the moment of inertia of WD 1(2), and \dot{E}_{pp} is the point-particle GW power.

In the top panel of Figure 6, we show the energy dissipation rate via different channels as a function of the system’s GW frequency. Here we focus on a $(M_1, M_2) = (0.72 M_\odot, 0.6 M_\odot)$ WD binary. We compute the radii using Eq. (2) and assume $I_{1(2)} = 0.26 M_{1(2)} R_{1(2)}^2$. When the system enters TianGO’s most sensitive band of $f > 10$ mHz, the dynamical tide accounts for more than 10% of the orbital energy loss. As a comparison, the energy transferred into the equilibrium tide (as computed following Ref. [68]) is only a minor amount.

The tidal interaction accelerates the orbital decay, and thus increases the amount of frequency chirping during a given period, as illustrated in the bottom panel of Fig. 6. In the plot we show, as a function of the system’s initial GW frequency, the increase in frequency over an observation period of 5 years with (the orange trace) and without (the blue trace) the tidal effect. Note that $\dot{E}_{\text{tide1(2)}} \propto I_{1(2)}$. Therefore, measuring the excess frequency shifting will allow us to directly constrain the moment of inertia of WDs.

To quantify the detectability of $I_{1(2)}$, we construct GW waveforms taking into account the tidal interactions (see Appendix B for details) and then use the Fisher matrix to estimate the parameter estimation error. We focus on the same $(M_1, M_2) = (0.72 M_\odot, 0.6 M_\odot)$ WD binary as before and fix its distance to be 10 kpc but randomize

TABLE II. Uncertainties in the sum of WDs’ moment of inertia at different GW frequencies.

f [mHz]	5	10	20	30
$\frac{\Delta(I_1+I_2)}{(I_1+I_2)}$	1.1	3.3×10^{-3}	9.6×10^{-6}	6.7×10^{-7}

its orientation and sky location. The median uncertainty in WD’s moment of inertia over a 5-year observation is summarized in Table II for different initial GW frequencies. Due to the way the moment of inertia enters the waveform, we are most sensitive to the sum $(I_1 + I_2)$ and it can be constrained to a level of better than 1% for sources at a gravitational-wave frequency of $f > 10$ mHz.

With such a high level of statistical accuracy, we can imagine that a precise relation between WD’s mass and moment of inertia can be established after a few detections. Then, we can in turn use this tidal effect to improve the measurability of other parameters. For example, due to a WD binary’s slow orbital motion — $(v_{\text{orb}}/c)^2 < 10^{-4}$ even at the onset of Roche-lobe overflow, where v_{orb} is orbital velocity — it is challenging to measure parameters such as the mass ratio that come from high-order post-Newtonian corrections using the point-particle GW waveform alone. However, it is critical to know not only the chirp mass but also the component masses when tackling problems like identifying progenitors of type Ia supernovae (Section IV). Nonetheless, the tide depends on the masses in a way different from the chirp mass and has a much more prominent effect on the orbital evolution than the post-Newtonian terms. It is thus a promising way to help constrain a WD binary’s component masses.

This is illustrated in Figure 7. Here we compare the parameter estimation uncertainty on the mass ratio for systems with different total masses. We set each system’s GW frequency to be the one right before the Roche-lobe overflow and fix the true mass ratio to be 1.2. When tides are included, we assume a fixed relation between a WD’s moment of inertia and mass as

$$I(M_{\text{wd}}) = 3.1 \times 10^{50} \left(\frac{M_{\text{wd}}}{0.6 M_\odot} \right)^{1/3} \text{ g cm}^2. \quad (6)$$

Compared to the point-particle results (blue traces), the ones including the tidal effect (orange traces) can reduce the statistical error on mass ratio, Δq , by nearly three orders of magnitude over a large portion of parameter space.

VI. CONSTRAINING PROGENITORS OF BLACK HOLE BINARIES BY MEASURING SPINS

The detections by aLIGO and aVirgo have confirmed the existence of stellar-mass BH binaries. A question to ask next is then what is the astrophysical process

³ Here we ignore the rotational modification of the WD structure, as the Coriolis force only mildly modifies the tidal dissipation in subsynchronously rotating WDs [70].

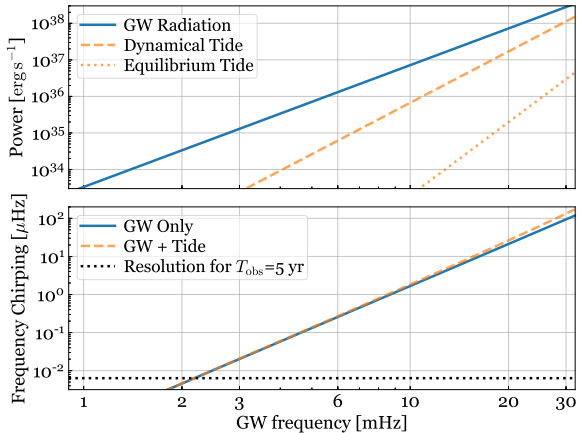


FIG. 6. Upper panel: orbital energy dissipation rate in different channels. Lower panel: the amount of frequency chirping for a $0.72 M_{\odot}$ - $0.6 M_{\odot}$ WD binary.

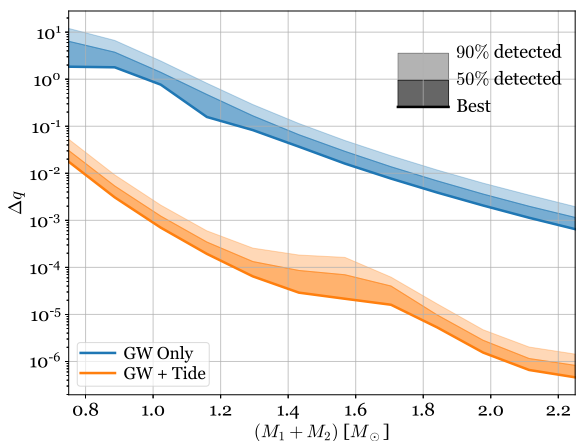


FIG. 7. Uncertainties in inferring the mass ratio, Δq , for WD binaries with different total masses.

that gives birth to these systems. Currently, the two most compelling channels are isolated binary evolution in galactic fields [71, 72] and dynamical formation in dense star clusters [73]. A potentially powerful discriminator of a system’s progenitor is the spin orientation (see, e.g., Refs. [74–77]). Isolated field binaries will preferentially have the spin aligned with the orbital angular momentum, whereas in the case of dynamical formation the orientation is more likely to be isotropic.

While ground detectors are sensitive to the *effective aligned spin parameter* χ_{eff} (the mass-weighted sum of two BHs’ dimensionless spins along the direction of orbital angular momentum [78]), the determination of spin components that lie in the orbital plane, often parameterized as the *effective precession spin parameter* χ_{p} [79],

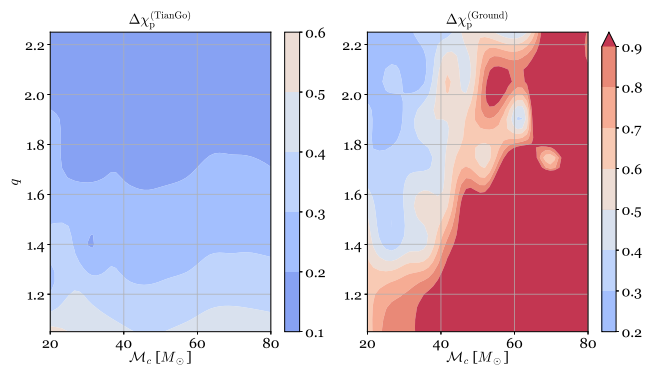


FIG. 8. Uncertainties in the precession spin parameter χ_{p} for TianGO (left) and a network of five Voyager-like detectors (right). We vary the source’s chirp mass and mass ratio, while fixing $(\chi_{\text{eff}}, \chi_{\text{p}}) = (-0.3, 0.6)$. The source is assumed to be at $z = 2$ and sky location is marginalized over.

will be challenging due to the limited sub-10 Hz sensitivities for ground-based detectors [80]. TianGO, on the other hand, is sensitive down to 10 mHz and can thus measure the modulations due to the precession spin χ_{p} with much higher accuracy. TianGO thus allows us to construct a *two-dimensional* spin distribution (in χ_{eff} and χ_{p}) of stellar-mass BH binaries that cannot be constructed with ground detectors alone, and consequently provide valuable insights into the formation history of binaries.

In Figure 8, we show the sky-location-averaged uncertainty in χ_{p} for sources located at a redshift of $z = 2$ ($D_L \simeq 16$ Gpc). To capture the precession effect, we use the IMRPhenomPv2 waveform model [78] and assume all sources to have a moderate spin rate of $(\chi_{\text{eff}}, \chi_{\text{p}}) = (-0.3, 0.6)$.⁴ We have chosen this set of values for illustration purposes, yet the conclusion we draw is generic. The source-frame chirp mass \mathcal{M}_c and mass ratio q are allowed to vary. As shown in the figure, for TianGO (left panel), χ_{p} is measurable ($\Delta\chi_{\text{p}} < |\chi_{\text{p}}|$) in almost the entire parameter space as long as the mass ratio is slightly greater than 1. As a comparison, a network of ground detectors consisting of HLVKA (right panel), can only detect χ_{p} over a small portion of the parameter space ($\mathcal{M}_c < 40 M_{\odot}$ and $q > 1.4$). This demonstrates TianGO’s unparalleled ability to determine χ_{p} .

One caveat though is that the above analysis assumes binary BHs have a broad range of spin with $0.1 \lesssim a/M < 1$ as in the case of X-ray binaries [81]. However, the

⁴ Specifically, here we set the components of the spins as $\chi_{1z} = \chi_{2z} = \chi_{\text{eff}}$, $\chi_{1x} = \chi_{2x} = \chi_{\text{p}}$, and $\chi_{1y} = \chi_{2y} = 0$. The (non-unique) way of choosing the components does not significantly affect the final results, as these components only enter the inspiral part of the waveform via the combination $(\chi_{\text{eff}}, \chi_{\text{p}})$ in the IMRPhenomPv2 waveform. The initial frequency we choose to set the spin components is fixed at 0.01 Hz, consequently fixing the orbital and spin precession phases.

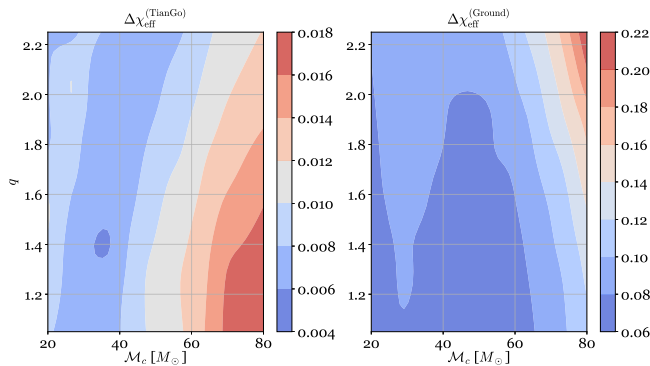


FIG. 9. Similar to Figure 8 but showing the uncertainties in χ_{eff} , for binaries with $(\chi_{\text{eff}}, \chi_{\text{p}}) = (0.05, 0)$. Note that the color scales are different in the two panels.

BBHs detected by aLIGO and aVirgo during the first and second observing runs [82] suggest that most BHs may have only low spins of $a/M < 0.1^5$ [84], which may be the consequence of an efficient angular momentum transfer in the progenitor stars [85]. In this case, a moderate χ_{p} would be an indication of the merger event involving a second-generation BH [86].

As for the majority of the slowly spinning BHs, TianGO can still deliver valuable information ground detectors cannot access. This is illustrated in Figure 9 where we present the uncertainty in χ_{eff} . This time we assume the system to only have a slow spin rate of $(\chi_{\text{eff}}, \chi_{\text{p}}) = (0.05, 0)$ while the other parameters are the same as in Figure 8. The Voyager network cannot constrain χ_{eff} for systems spinning at such a slow rate. TianGO, on the other hand, can still achieve an accuracy of $\Delta\chi_{\text{eff}}/\chi_{\text{eff}} \lesssim 0.3$ over most of the parameter space. This opens up the possibility of discriminating different angular momentum transfer models that all predict the majority of BHs having a spin in the range of $a/M \sim 0.01 - 0.1$ [85, 87–90].

VII. COSMOLOGICAL STRUCTURE FORMATION AND INTERMEDIATE-MASS BLACK HOLES

Massive BHs reside in the center of most local galaxies. Despite the fact that the mass of the central BH is only $\sim 0.1\%$ of the total mass of the host galaxy, surprisingly clear correlations between the massive BH’s mass and the properties of the host galaxy have been observed (e.g., Ref. [91]). This thus suggests a co-evolution of the massive BH and its host galaxy [92], which is further sensitive to the seed from which the massive BHs

grow (see Ref. [93] for a review). Broadly speaking, a massive BH may grow from either a “heavy seed” with mass $\sim 10^4 - 10^6 M_{\odot}$ at a relatively late cosmic time of $z \sim 5 - 10$, or from a “light seed” with mass $\simeq 100 - 600 M_{\odot}$ at an earlier time of $z \simeq 20$. Those “light seeds” may be generated from the collapse of Pop III stars [94] and they may merge with each other in the early Universe [95].

The characteristic frequency of such a merger is given by the system’s quasi-normal mode frequency. For a Schwarzschild BH, the fundamental, axially symmetric, quadrupolar mode oscillates at a frequency of [96],

$$f_{\text{QNM}}^{(\text{det})} \simeq 1.21 \left(\frac{10}{1+z} \right) \left(\frac{10^3 M_{\odot}}{M_1 + M_2} \right) \text{ Hz}. \quad (7)$$

We have used the superscript “(det)” to represent quantities measured in the detector-frame. While it is a frequency too low for ground detectors and too high for LISA, it falls right into TianGO’s most sensitive band. Indeed, as shown in Figure 2, TianGO is especially sensitive to systems with masses in the range of $100 - 1000 M_{\odot}$ and can detect them up to a redshift of $z \sim 100$. Consequently, if massive BHs grow from light seeds, TianGO will be able to map out the entire growth history throughout the Universe. On the other hand, a null detection of such mergers by TianGO can then rule out the “light seed” scenario. It will also constrain our models of Pop III stars that will be otherwise challenging to detect even with the *James Webb Space Telescope* [97]. In either case, TianGO will provide indispensable insights in our understanding of cosmological structure formation (see also Refs. [98–100] for relevant discussions for LISA and the third-generation ground GW observatories).

Meanwhile, those seed BHs that failed to grow into massive and supermassive BHs may be left to become IMBHs in the local Universe [101, 102]. While a few IMBH candidates have been reported (see, e.g., [103–105]), a solid confirmation is still lacking from electromagnetic observation. This makes the potential GW detection of an IMBH particularly exciting. In addition to the merger of two IMBHs (similar to the mergers of light BH seeds discussed above), another potential GW source involving an IMBH is the intermediate-mass-ratio inspirals (IMRIs): a stellar mass object (BH, NS, or WD) merges with an IMBH. IMRIs may be found in the dense cores of globular clusters [106, 107].

TianGO will detect a typical IMRI source with $(M_1, M_2) = (1000 M_{\odot}, 10 M_{\odot})$ at $z = 1$ with an SNR of 10 after averaging over both orientation and sky location. If the event rate for such a merger is about 1 per Gpc³ per year as argued in Ref. [15], we would be able to detect nearly 1000 IMRI mergers over a 5-year observation of TianGO. The numerous detections would thus allow us to both place constraints on the dynamics in globular clusters and perform potential tests of general relativity in a way similar to those using the extreme-mass-ratio inspirals [108].

⁵ Ref. [83] reported a highly spinning BBH, yet this event has lower detection significance compared to the others. If the event is indeed astrophysical, it might hint at a chemically homogeneous formation [72].

VIII. CONCLUSION AND DISCUSSIONS

We have examined the potential scientific outcomes that can be delivered by the TianGO mission. We showed that TianGO can significantly enhance the sky localization and distance estimation accuracy of binary BHs when combined with a network of ground detectors. This has the potential to resolve the tension between the local and cosmological measurements of the Hubble constant. It can also localize a coalescing NS binary with unparalleled accuracy weeks before the final merger, consequently facilitating multi-messenger astronomy. Identifying the progenitors of type Ia supernovae is another critical science case that is addressed by TianGO. Meanwhile, it also helps constrain the formation history of today's massive BHs and the search for IMBHs.

In addition to the science case made in the main text, there are many other topics TianGO may enable. For example, TianGO may detect a population of exoplanets orbiting WD binaries [109, 110]. It may also enable a direct detection of the GW memory effect [111, 112] or test the angular distribution of the memory background [113]. If TianGO does detect IMBHs, we may further use them to search for or rule out the existence of ultra-light bosons via superradiance [114, 115]. We plan to carry out more in depth studies of TianGO's scientific capabilities in the future.

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Appendix A: Parameter Estimation with a Combined Network of Space and Ground Detectors

The calculations done in this paper use the well-known Fisher matrix formalism [116–118] which we briefly summarize here. We then explain the methods used to simultaneously analyze combined network of both space and ground gravitational wave detectors.

Suppose the frequency domain signal measured in the detector a is

$$s_a(f) = h_a(f, \theta) + n_a(f) \quad (\text{A1})$$

where $h_a(f, \theta)$ is the gravitational wave waveform and n_a is stationary Gaussian noise with single-sided power spectral density $S_a(f)$. The waveform depends on a set

of parameters θ that are to be inferred from the measurement of s_a . For large signal to noise ratios, the differences $\Delta\theta_i$ between the measured and true parameters, as measured by detector a , are normally distributed

$$p(\Delta\theta) \propto e^{-\Gamma_{ij}^a \Delta\theta_i \Delta\theta_j / 2} \quad (\text{A2})$$

where

$$\Gamma_{ij}^a = \left(\frac{\partial h}{\partial \theta_i} \middle| \frac{\partial h}{\partial \theta_j} \right)_a \quad (\text{A3})$$

is the Fisher information matrix and

$$(g|h)_a = 4 \operatorname{Re} \int_0^\infty \frac{g^*(f)h(f)}{S_a(f)} df \quad (\text{A4})$$

is the noise weighted inner product for detector a .

The covariance for estimating the parameters θ with a network of detectors is the inverse of the network Fisher matrix obtained by summing the individual Fisher matrices

$$\begin{aligned} \Gamma_{ij} &= \sum_a \Gamma_{ij}^a \\ \Sigma_{ij} &= \langle \Delta\theta_i \Delta\theta_j \rangle = (\Gamma^{-1})_{ij}. \end{aligned} \quad (\text{A5})$$

The angular uncertainty in determining a source's sky location is

$$\Delta\Omega = 2\pi |\cos \delta| \sqrt{\Sigma_{\alpha\alpha} \Sigma_{\delta\delta} - (\Sigma_{\alpha\delta})^2}, \quad (\text{A6})$$

where α is the right ascension and δ is the declination.

To simultaneously describe the signal measured in both the ground and space detectors, especially since TianGO's sensitivity band extends well into that of the ground detectors (see Fig. 1), one needs a waveform that captures both the high frequency merger-ringdown as well as the low frequency time-dependence associated with Doppler shifts and time-dependent antenna patterns. To do so, we modify the approach of Ref. [119] to include phenomenological waveforms which include the merger and ringdown.

We first use `lalinference` [120, 121] to generate a phenomenological frequency domain waveform

$$u_{\text{ph}}(f) = A_{\text{ph}}(f) e^{i\Psi_{\text{ph}}(f)} \quad (\text{A7})$$

defined by the chirp mass \mathcal{M}_c , mass ratio q , luminosity distance D_L , and, where appropriate, the effective spin χ_{eff} and spin precession χ_p . Except for in Section VI where the `IMRPhenomPv2` waveform [78] is used, the `IMRPhenomD` waveform [122] is used throughout the paper. The source location is described by the right ascension α and declination δ , and the orientation is described by the azimuthal and polar angles, ϕ_L and θ_L , of the source's angular momentum $\hat{\mathbf{L}}$. These remaining four extrinsic parameters as well as the coalescence time t_c and phase ϕ_c are then added by hand as appropriate for the ground and space detectors. The coalescence time

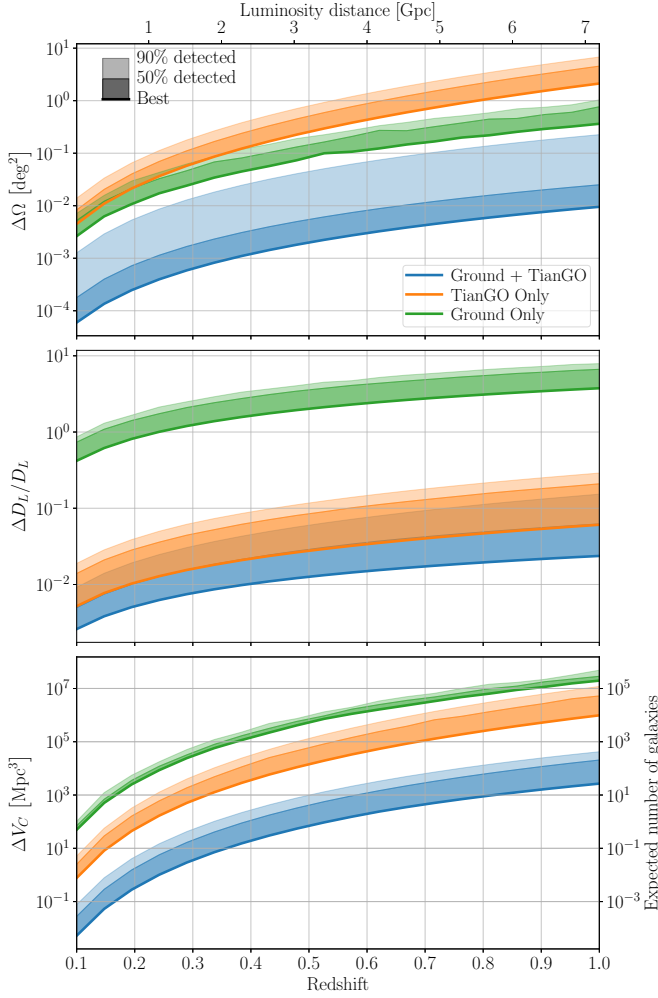


FIG. 10. The same as Fig. 3 except for face on binaries.

is defined as the time the wave arrives at the solar system barycenter.

For the ground detectors, the + and × polarizations are first computed from u_{ph}

$$h_+(f) = A_{\text{ph}}(f) e^{i\Psi_{\text{ph}}(f)} \left(\frac{1 + \cos^2 \iota}{2} \right) \quad (\text{A8a})$$

$$h_\times(f) = A_{\text{ph}}(f) e^{i[\Psi_{\text{ph}}(f) + \pi/2]} \cos \iota, \quad (\text{A8b})$$

where ι is the source inclination. The signal observed in the ground detector a is obtained by projecting h_+ and h_\times onto the usual + and × antenna patterns for that detector, $F_+^a(\alpha, \delta, \psi)$ and $F_\times^a(\alpha, \delta, \psi)$, where ψ is the polarization phase.⁶ See, for example, Appendix B of Ref. [123].

⁶ The conversion from ϕ_L and θ_L to ψ and ι is

$$\begin{aligned} \cos \iota &= \cos \theta_L \sin \delta + \sin \theta_L \cos \delta \cos(\phi_L - \alpha) \\ \tan \psi &= \frac{\cos \theta_L + \cos \iota \sin \delta}{\cos \delta \sin \theta_L \sin(\phi_L - \alpha)}. \end{aligned}$$

Finally, since the coalescence time is defined at the solar system barycenter, the phase is shifted by the light travel time $\tau_a(\alpha, \delta) = -\mathbf{d}_a \cdot \hat{\mathbf{n}}(\alpha, \delta)/c$ from the solar system barycenter to the detector where $\hat{\mathbf{n}}(\alpha, \delta)$ is the unit vector pointing from the barycenter to the source, and \mathbf{d}_a is the vector from the barycenter to the detector. The waveform observed in detector a is then

$$h_a(f) = e^{i[2\pi f(t_c + \tau_a) - \phi_c]} [F_+^a h_+(f) + F_\times^a h_\times(f)]. \quad (\text{A9})$$

For TianGO, the time dependence of the antenna pattern and Doppler phase shift caused by the detector's orbit need to be included. The strategy employed by Ref. [119], which we follow, is to solve for the time dependence in the time domain and then, using a post-Newtonian expansion, find time as a function of frequency. This leads to the amplitude of the waveform being modulated by

$$\Lambda(f) = \sqrt{[1 + (\hat{\mathbf{L}} \cdot \hat{\mathbf{n}})^2] F_+^2(f) + 4(\hat{\mathbf{L}} \cdot \hat{\mathbf{n}})^2 F_\times^2(f)} \quad (\text{A10})$$

and gaining an extra phase

$$\tan \phi_p(f) = \frac{2(\hat{\mathbf{L}} \cdot \hat{\mathbf{n}}) F_\times(f)}{[1 + (\hat{\mathbf{L}} \cdot \hat{\mathbf{n}})^2] F_+(f)}. \quad (\text{A11})$$

Finally, as with the ground detectors, the phase associated with the propagation time from the solar system barycenter to TianGO must be included. Since sources can stay in TianGO's band for a significant portion of an orbit, this correction is the frequency dependent Doppler phase

$$\phi_D(f) = \frac{2\pi f}{c} R \cos \delta \cos[\phi_T(f) - \alpha], \quad (\text{A12})$$

where $\phi_T(f)$ is the azimuthal angle of TianGO in its orbit around the sun and $R = 1 \text{ AU}$ is the radius of the orbit. As discussed in Ref. [119], higher order corrections to Eq. (A12) are of order $|\phi_D|(v/c) \lesssim 0.3 (f/1 \text{ Hz})$, where $v = 2\pi R/T$ is the velocity of TianGO in its orbit and $T = 1 \text{ yr}$. While this is not of concern for LISA, TianGO's sensitivity band extends past 10 Hz where this correction becomes $\mathcal{O}(1)$. Future work can address the effects of this correction if necessary.

Putting it all together, the waveform observed by TianGO is

$$h_T(f) = \Lambda(f) A_{\text{ph}}(f) e^{i[\Psi_{\text{ph}}(f) - \phi_D(f) - \phi_p(f) - \phi_c]}. \quad (\text{A13})$$

See Appendix A1 below for explicit expressions for $F_+(f)$, $F_\times(f)$, and $\phi_T(f)$.

Fisher matrices are known to give unreliable results when waveforms that terminate abruptly in a detector's sensitivity band are used—as is often done when using inspiral only waveforms that terminate at the innermost stable circular orbit [124]. Our analysis is not susceptible to such effects since we use a hybrid waveform that includes the merger and ringdown and which does not abruptly terminate.

1. Explicit expressions for time-dependent waveforms

We collect here the important expressions from Ref. [119] necessary to complete TianGO's waveform Eq. (A13). The post-Newtonian expansion of Ref. [119] is done in the parameter

$$x = \left(\frac{G}{c^3} \pi M_\odot \right)^{2/3} \frac{\mathcal{M}_c}{\mu} \left[\left(\frac{\mathcal{M}_c}{M_\odot} \right) \left(\frac{f}{1 \text{ Hz}} \right) \right]^{2/3} \quad (\text{A14})$$

where $\mu = \mathcal{M}_c [q/(1+q)]^{2/5}$ is the reduced mass. The time as a function of frequency is

$$t(f) \equiv t_f = t_c - t_x \left[1 + \frac{4}{3} \left(\frac{743}{336} + \frac{11}{4} \frac{\mu}{M} \right) x - \frac{32\pi}{5} x^{3/2} \right], \quad (\text{A15a})$$

where

$$t_x = 5c^{5/3} \left(8\pi \frac{f}{1 \text{ Hz}} \right)^{-8/3} \left(\frac{GM_\odot}{c^2} \right)^{-5/3} \left(\frac{\mathcal{M}_c}{M_\odot} \right)^{-5/3}, \quad (\text{A15b})$$

and M is the total mass. The azimuthal angle of TianGO in its orbit around the sun is $\phi_T(f) = 2\pi t_f/T$ where $T = 1 \text{ yr}$.

If $\phi = \alpha$, $\theta = \pi/2 - \delta$, and ψ are the sky locations of a source and its polarization in the ecliptic frame, let $\tilde{\phi}$, $\tilde{\theta}$ and $\tilde{\psi}$ be those in the frame of the detector. Similarly, ϕ_L and θ_L are the azimuthal and polar angles of the source angular momentum $\hat{\mathbf{L}}$ in the detector frame. If $\hat{\mathbf{z}}$ is the unit vector along the z direction, the polar angle of the source in the detector frame is

$$\cos \tilde{\theta}(t_f) = \hat{\mathbf{z}} \cdot \hat{\mathbf{n}} = \frac{1}{2} \cos \theta - \frac{\sqrt{3}}{2} \sin \theta \cos(\phi_T(f) - \phi), \quad (\text{A16})$$

the azimuthal angle of the source in the detector frame is

$$\tilde{\phi}(t_f) = \phi_T(f) + \arctan \left[\frac{\sqrt{3} \cos \theta + \sin \theta \cos(\phi_T(t) - \phi)}{2 \sin \theta \sin(\phi_T(f) - \phi)} \right], \quad (\text{A17})$$

and the polarization phase of the source in the detector frame is

$$\tan \tilde{\psi}(t_f) = \frac{\hat{\mathbf{L}} \cdot \hat{\mathbf{z}} - (\hat{\mathbf{L}} \cdot \hat{\mathbf{n}})(\hat{\mathbf{z}} \cdot \hat{\mathbf{n}})}{\hat{\mathbf{n}} \cdot (\hat{\mathbf{L}} \times \hat{\mathbf{z}})} \quad (\text{A18})$$

where

$$\hat{\mathbf{L}} \cdot \hat{\mathbf{z}} = \frac{1}{2} \cos \theta_L - \frac{\sqrt{3}}{2} \sin \theta_L \cos(\bar{\phi}(t_f) - \phi_L) \quad (\text{A19})$$

$$\hat{\mathbf{L}} \cdot \hat{\mathbf{n}} = \cos \theta_L \cos \theta + \sin \theta_L \sin \theta \cos(\phi_L - \phi), \quad (\text{A20})$$

and

$$\begin{aligned} \hat{\mathbf{n}} \cdot (\hat{\mathbf{L}} \times \hat{\mathbf{z}}) &= \frac{1}{2} \sin \theta_L \sin \theta \sin(\phi_L - \phi) \\ &\quad - \frac{\sqrt{3}}{2} \cos \phi_T(f) \cos \theta_L \sin \theta \sin \phi \\ &\quad + \frac{\sqrt{3}}{2} \cos \phi_T(f) \cos \theta \sin \theta_L \sin \phi_L \\ &\quad - \frac{\sqrt{3}}{2} \sin \phi_T(f) \cos \theta \sin \theta_L \sin \phi_L \\ &\quad + \frac{\sqrt{3}}{2} \sin \phi_T(f) \cos \theta_L \sin \theta \sin \phi. \end{aligned} \quad (\text{A21})$$

Eqs. (A16) to (A18) are functions of frequency through Eq. (A15).

The time-dependent antenna patterns as a function of frequency are given by plugging the detector frame angles Eqs. (A16) to (A18) into the standard antenna patterns

$$F_+(f) = \left(\frac{1 + \cos^2 \tilde{\theta}}{2} \right) \cos 2\tilde{\phi} \cos 2\tilde{\psi} - \cos \tilde{\theta} \sin 2\tilde{\phi} \sin 2\tilde{\psi} \quad (\text{A22a})$$

$$F_\times(f) = \left(\frac{1 + \cos^2 \tilde{\theta}}{2} \right) \cos 2\tilde{\phi} \sin 2\tilde{\psi} + \cos \tilde{\theta} \sin 2\tilde{\phi} \cos 2\tilde{\psi}. \quad (\text{A22b})$$

Appendix B: GW waveforms including tides in WDs

In this section we derive the phase $\Psi(f)$ of the frequency-domain waveform $h(f) \propto \exp[i\Psi(f)]$ including the effect of tidal interaction in WD binaries. As shown in Ref. [117], $\Psi(f)$ is related to the time-domain phase $\phi(t)$ as

$$\Psi(f) = 2\pi f t(f) - \phi[t(f)] - \pi/4, \quad (\text{B1})$$

we thus want to find how $t(f)$ and $\phi[t(f)]$ are modified by the tide.

For the time as a function of frequency, we have

$$\begin{aligned} t(f) &= \int \frac{df}{\dot{f}} = \int \frac{df}{\dot{f}_{\text{pp}} + \dot{f}_{\text{tide}}}, \\ &\simeq \int \frac{df}{\dot{f}_{\text{pp}}} \left(1 - \frac{\dot{E}_{\text{tide}}}{\dot{E}_{\text{pp}}} \right), \\ &= t_{\text{pp}}(f) - \int \frac{1}{\dot{f}_{\text{pp}}} \frac{\dot{E}_{\text{tide}}}{\dot{E}_{\text{pp}}} df. \end{aligned} \quad (\text{B2})$$

In the above derivation we have decomposed the total frequency evolution rate \dot{f} as the sum of a point-particle ("pp") part \dot{f}_{pp} driven by the GW radiation and a tidal contribution \dot{f}_{tide} . We have also treated the tidal effect as a small perturbation and have assumed that the orbit remains quasi-circular, which allows us to relate the tidally induced GW frequency shift to the excess energy dissipation as $\dot{f}_{\text{tide}}/\dot{f}_{\text{pp}} \simeq \dot{E}_{\text{tide}}/\dot{E}_{\text{pp}}$. Here $\dot{E}_{\text{tide}} = \dot{E}_{\text{tide1}} + \dot{E}_{\text{tide2}}$ [cf. eq. (5)].

Similarly, the time-domain phase can be written as

$$\begin{aligned}\phi[t(f)] &= 2\pi \int \frac{f}{\dot{f}} df \\ &\simeq 2\pi \int \frac{f}{\dot{f}_{\text{pp}}} df - 2\pi \int \frac{f}{\dot{f}_{\text{pp}}} \frac{\dot{E}_{\text{tide}}}{\dot{E}_{\text{pp}}} df \\ &= \phi_{\text{pp}}[t(f)] - 2\pi \int \frac{f}{\dot{f}_{\text{pp}}} \frac{\dot{E}_{\text{tide}}}{\dot{E}_{\text{pp}}} df.\end{aligned}\quad (\text{B3})$$

Thus the frequency-domain phase can now be written

as

$$\Psi(f) = \Psi_{\text{pp}}(f) - 2\pi \left(f \int \frac{1}{\dot{f}_{\text{pp}}} \frac{\dot{E}_{\text{tide}}}{\dot{E}_{\text{pp}}} df - \int \frac{f}{\dot{f}_{\text{pp}}} \frac{\dot{E}_{\text{tide}}}{\dot{E}_{\text{pp}}} df \right).\quad (\text{B4})$$

The lower and upper limits of the integrals are f_0 and f , respectively, where f_0 is the initial frequency of the signal. Therefore we always align the tidal waveform to the point-particle one at the beginning of the signal.

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- [1] LIGO Scientific Collaboration, Advanced LIGO, *Classical and Quantum Gravity* **32**, 074001 (2015), [arXiv:1411.4547 \[gr-qc\]](#).
- [2] F. Acernese, M. Agathos, K. Agatsuma, D. Aisa, N. Allemandou, A. Allocca, J. Amarni, P. Astone, and et al., Advanced Virgo: a second-generation interferometric gravitational wave detector, *Classical and Quantum Gravity* **32**, 024001 (2015), [arXiv:1408.3978 \[gr-qc\]](#).
- [3] T. Akutsu, M. Ando, K. Arai, Y. Arai, S. Araki, A. Araya, N. Aritomi, H. Asada, and et al., KAGRA: 2.5 Generation Interferometric Gravitational Wave Detector, arXiv e-prints , [arXiv:1811.08079 \(2018\)](#), [arXiv:1811.08079 \[gr-qc\]](#).
- [4] The LIGO Scientific collaboration, Gravitational wave astronomy with LIGO and similar detectors in the next decade, arXiv e-prints , [arXiv:1904.03187 \(2019\)](#), [arXiv:1904.03187 \[gr-qc\]](#).
- [5] R. X. Adhikari, N. Smith, A. Brooks, L. Barsotti, B. Shapiro, B. Lantz, D. McClelland, E. K. Gustafson, D. V. Martynov, V. Mitrofanov, D. Coyne, K. Arai, C. Torrie, and C. Wipf, *LIGO Voyager Upgrade: Design Concept*, Tech. Rep. LIGO-T1400226 (2018).
- [6] S. Hild, S. Chelkowski, A. Freise, J. Franc, N. Morgado, R. Flaminio, and R. DeSalvo, A xylophone configuration for a third-generation gravitational wave detector, *Classical and Quantum Gravity* **27**, 015003 (2010), [arXiv:0906.2655 \[gr-qc\]](#).
- [7] B. Sathyaprakash, M. Abernathy, F. Acernese, P. Ajith, B. Allen, P. Amaro-Seoane, N. Andersson, S. Aoudia, K. Arun, P. Astone, and et al., Scientific objectives of Einstein Telescope, *Classical and Quantum Gravity* **29**, 124013 (2012), [arXiv:1206.0331 \[gr-qc\]](#).
- [8] B. P. Abbott, R. Abbott, T. D. Abbott, M. R. Abernathy, K. Ackley, C. Adams, P. Addesso, R. X. Adhikari, V. B. Adya, C. Affeldt, and et al., Exploring the sensitivity of next generation gravitational wave detectors, *Classical and Quantum Gravity* **34**, 044001 (2017), [arXiv:1607.08697 \[astro-ph.IM\]](#).
- [9] P. Amaro-Seoane, H. Audley, S. Babak, J. Baker, E. Barausse, P. Bender, E. Berti, P. Binetruy, and et al., Laser Interferometer Space Antenna, arXiv e-prints , [arXiv:1702.00786 \(2017\)](#), [arXiv:1702.00786 \[astro-ph.IM\]](#).
- [10] J. Luo, L.-S. Chen, H.-Z. Duan, Y.-G. Gong, S. Hu, J. Ji, Q. Liu, J. Mei, and et al., TianQin: a space-borne gravitational wave detector, *Classical and Quantum Gravity* **33**, 035010 (2016), [arXiv:1512.02076 \[astro-ph.IM\]](#).
- [11] H.-T. Wang, Z. Jiang, A. Sesana, E. Barausse, S.-J. Huang, Y.-F. Wang, W.-F. Feng, Y. Wang, and et al., Science with TianQin: Preliminary Results on Massive Black Hole Binaries, arXiv e-prints , [arXiv:1902.04423 \(2019\)](#), [arXiv:1902.04423 \[astro-ph.HE\]](#).
- [12] J. P. W. Verbiest, L. Lentati, G. Hobbs, R. van Haasteren, P. B. Demorest, G. H. Janssen, J.-B. Wang, G. Desvignes, and et al., The International Pulsar Timing Array: First data release, *MNRAS* **458**, 1267 (2016), [arXiv:1602.03640 \[astro-ph.IM\]](#).
- [13] NANOGrav Collaboration, The NANOGrav 11 Year Data Set: Pulsar-timing Constraints on the Stochastic Gravitational-wave Background, *ApJ* **859**, 47 (2018), [arXiv:1801.02617 \[astro-ph.HE\]](#).
- [14] K. A. Kuns, R. X. Adhikari, Y. Chen, H. Yu, and G. Lovelace, A quantum-enhanced space interferometer for cosmography, In preparation (2019).
- [15] I. Mandel, A. Sesana, and A. Vecchio, The astrophysical science case for a decihertz gravitational-wave detector, *Classical and Quantum Gravity* **35**, 054004 (2018), [arXiv:1710.11187 \[astro-ph.HE\]](#).
- [16] S. Sato, S. Kawamura, M. Ando, T. Nakamura, K. Tsubono, A. Araya, I. Funaki, K. Ioka, and et al., The status of DECIGO, in *Journal of Physics Conference Series*, Vol. 840 (2017) p. 012010.
- [17] G. M. Harry, P. Fritschel, D. A. Shaddock, W. Folkner, and E. S. Phinney, Laser interferometry for the Big Bang Observer, *Classical and Quantum Gravity* **23**, 4887 (2006).
- [18] LIGO Scientific Collaboration and Virgo Collaboration (LIGO Scientific Collaboration and Virgo Collaboration), Observation of gravitational waves from a binary black hole merger, *Phys. Rev. Lett.* **116**, 061102 (2016).
- [19] A. G. Riess, S. Casertano, W. Yuan, L. M. Macri, and D. Scolnic, Large magellanic cloud cepheid standards provide a 1% foundation for the determination of the hubble constant and stronger evidence for physics beyond $\{\text{up}\Lambda\}$ CDM, *The Astrophysical Journal* **876**, 85 (2019).
- [20] Planck Collaboration, P. A. R. Ade, N. Aghanim, M. Arnaud, M. Ashdown, J. Aumont, C. Baccalupi, A. J. Banday, R. B. Barreiro, J. G. Bartlett, and et al., Planck 2015 results. XIII. Cosmological parameters, *A&A* **594**, A13 (2016), [arXiv:1502.01589](#).
- [21] Schutz Bernard F., Determining the Hubble constant from gravitational wave observations, *Nature* **323**, 310

- (1986).
- [22] D. E. Holz and S. A. Hughes, Using gravitational-wave standard sirens, *The Astrophysical Journal* **629**, 15 (2005).
- [23] C. Cutler and D. E. Holz, Ultrahigh precision cosmology from gravitational waves, *Phys. Rev. D* **80**, 104009 (2009).
- [24] K. Kyutoku and N. Seto, Gravitational-wave cosmography with lisa and the hubble tension, *Phys. Rev. D* **95**, 083525 (2017).
- [25] B. S. Sathyaprakash, B. F. Schutz, and C. V. D. Broeck, Cosmography with the einstein telescope, *Classical and Quantum Gravity* **27**, 215006 (2010).
- [26] A. Gupta, D. Fox, B. S. Sathyaprakash, and B. F. Schutz, Calibrating the cosmic distance ladder using gravitational-wave observations, arXiv e-prints, arXiv:1907.09897 (2019), arXiv:1907.09897 [astro-ph.CO].
- [27] LIGO Scientific Collaboration and Virgo Collaboration, GW170817: Observation of Gravitational Waves from a Binary Neutron Star Inspiral, *Phys. Rev. Lett.* **119**, 161101 (2017), arXiv:1710.05832 [gr-qc].
- [28] B. P. Abbott, R. Abbott, T. D. Abbott, F. Acernese, K. Ackley, C. Adams, T. Adams, P. Addesso, and et al., A gravitational-wave standard siren measurement of the Hubble constant, *Nature* **551**, 85 (2017), arXiv:1710.05835 [astro-ph.CO].
- [29] B. F. Schutz, Networks of gravitational wave detectors and three figures of merit, *Classical and Quantum Gravity* **28**, 125023 (2011).
- [30] W. Del Pozzo, Inference of cosmological parameters from gravitational waves: Applications to second generation interferometers, *Phys. Rev. D* **86**, 043011 (2012).
- [31] C. L. MacLeod and C. J. Hogan, Precision of hubble constant derived using black hole binary absolute distances and statistical redshift information, *Phys. Rev. D* **77**, 043512 (2008).
- [32] R. Nair, S. Bose, and T. D. Saini, Measuring the hubble constant: Gravitational wave observations meet galaxy clustering, *Phys. Rev. D* **98**, 023502 (2018).
- [33] M. Fishbach, R. Gray, I. M. Hernandez, H. Qi, A. Sur, F. Acernese, L. Aiello, A. Allocca, and et al., A standard siren measurement of the hubble constant from GW170817 without the electromagnetic counterpart, *The Astrophysical Journal* **871**, L13 (2019).
- [34] B. P. Abbott, R. Abbott, T. D. Abbott, S. Abraham, F. Acernese, K. Ackley, C. Adams, R. X. Adhikari, V. B. Adya, C. Affeldt, and et al., A gravitational-wave measurement of the Hubble constant following the second observing run of Advanced LIGO and Virgo, In preparation (2019).
- [35] A. Goldstein, P. Veres, E. Burns, M. S. Briggs, R. Hamburg, D. Kocevski, C. A. Wilson-Hodge, R. D. Preece, and et al., An Ordinary Short Gamma-Ray Burst with Extraordinary Implications: Fermi-GBM Detection of GRB 170817A, *ApJ* **848**, L14 (2017), arXiv:1710.05446 [astro-ph.HE].
- [36] B. P. Abbott, R. Abbott, T. D. Abbott, F. Acernese, K. Ackley, C. Adams, T. Adams, P. Addesso, R. X. Adhikari, V. B. Adya, and et al., Multi-messenger Observations of a Binary Neutron Star Merger, *Astrophys. J. Lett.* **848**, L12 (2017), arXiv:1710.05833 [astro-ph.HE].
- [37] E. Burns, A. Tohuavohu, J. Buckley, T. D. Canton, B. Cenko, J. Conklin, F. D'ammann o, D. Eichler, C. Fryer, A. van der Horst, M. Kamionkowski, M. Kasliwal, R. Margutti, B. Metzger, K. Murase, S. Nissanke, D. Radice, J. Tomsick, C. Wilson-Hodge, and B. Zhang, A Summary of Multimessenger Science with Neutron Star Mergers, *BAAS* **51**, 38 (2019), arXiv:1903.03582 [astro-ph.HE].
- [38] R. Fernández and B. D. Metzger, Electromagnetic Signatures of Neutron Star Mergers in the Advanced LIGO Era, *Annual Review of Nuclear and Particle Science* **66**, 23 (2016), arXiv:1512.05435 [astro-ph.HE].
- [39] D. Tsang, J. S. Read, T. Hinderer, A. L. Piro, and R. Bondarescu, Resonant Shattering of Neutron Star Crusts, *Phys. Rev. Lett.* **108**, 011102 (2012), arXiv:1110.0467 [astro-ph.HE].
- [40] E. Troja, S. Rosswog, and N. Gehrels, Precursors of Short Gamma-ray Bursts, *ApJ* **723**, 1711 (2010), arXiv:1009.1385 [astro-ph.HE].
- [41] B. D. Metzger and C. Zivancev, Pair fireball precursors of neutron star mergers, *MNRAS* **461**, 4435 (2016), arXiv:1605.01060 [astro-ph.HE].
- [42] B. M. S. Hansen and M. Lyutikov, Radio and X-ray signatures of merging neutron stars, *MNRAS* **322**, 695 (2001), arXiv:astro-ph/0003218 [astro-ph].
- [43] D. Thornton, B. Stappers, M. Bailes, B. Barsdell, S. Bates, N. D. R. Bhat, M. Burgay, S. Burke-Spolaor, D. J. Champion, P. Coster, N. D'Amico, A. Jameson, S. Johnston, M. Keith, M. Kramer, L. Levin, S. Milia, C. Ng, A. Possenti, and W. van Straten, A Population of Fast Radio Bursts at Cosmological Distances, *Science* **341**, 53 (2013), arXiv:1307.1628 [astro-ph.HE].
- [44] D. A. Howell, Type Ia supernovae as stellar endpoints and cosmological tools, *Nature Communications* **2**, 350 (2011), arXiv:1011.0441 [astro-ph.CO].
- [45] A. G. Riess, A. V. Filippenko, P. Challis, A. Clocchiatti, A. Diercks, P. M. Garnavich, R. L. Gilliland, C. J. Hogan, S. Jha, R. P. Kirshner, and et al., Observational Evidence from Supernovae for an Accelerating Universe and a Cosmological Constant, *AJ* **116**, 1009 (1998), arXiv:astro-ph/9805201 [astro-ph].
- [46] D. Maoz and F. Mannucci, Type-Ia Supernova Rates and the Progenitor Problem: A Review, *PASA* **29**, 447 (2012), arXiv:1111.4492 [astro-ph.CO].
- [47] D. Maoz, F. Mannucci, and G. Nelemans, Observational Clues to the Progenitors of Type Ia Supernovae, *ARA&A* **52**, 107 (2014), arXiv:1312.0628 [astro-ph.CO].
- [48] P. P. Eggleton, Approximations to the radii of Roche lobes, *ApJ* **268**, 368 (1983).
- [49] J. R. Hurley, C. A. Tout, and O. R. Pols, Evolution of binary stars and the effect of tides on binary populations, *MNRAS* **329**, 897 (2002), astro-ph/0201220.
- [50] S. Toonen, G. Nelemans, and S. Portegies Zwart, Supernova Type Ia progenitors from merging double white dwarfs. Using a new population synthesis model, *A&A* **546**, A70 (2012), arXiv:1208.6446 [astro-ph.HE].
- [51] S. A. Sim, F. K. Röpk, W. Hillebrandt, M. Kromer, R. Pakmor, M. Fink, A. J. Ruiter, and I. R. Seitenzahl, Detonations in Sub-Chandrasekhar-mass C+O White Dwarfs, *ApJ* **714**, L52 (2010), arXiv:1003.2917 [astro-ph.HE].
- [52] M. H. van Kerkwijk, P. Chang, and S. Justham, Sub-Chandrasekhar White Dwarf Mergers as the Progenitors of Type Ia Supernovae, *ApJ* **722**, L157 (2010), arXiv:1006.4391 [astro-ph.SR].
- [53] S. E. Woosley and D. Kasen, Sub-Chandrasekhar

- Mass Models for Supernovae, *ApJ* **734**, 38 (2011), [arXiv:1010.5292 \[astro-ph.HE\]](#).
- [54] A. Polin, P. Nugent, and D. Kasen, Observational Predictions for Sub-Chandrasekhar Mass Explosions: Further Evidence for Multiple Progenitor Systems for Type Ia Supernovae, *ApJ* **873**, 84 (2019), [arXiv:1811.07127 \[astro-ph.HE\]](#).
- [55] T. R. Marsh, G. Nelemans, and D. Steeghs, Mass transfer between double white dwarfs, *MNRAS* **350**, 113 (2004), [astro-ph/0312577](#).
- [56] V. Gokhale, X. M. Peng, and J. Frank, Evolution of Close White Dwarf Binaries, *ApJ* **655**, 1010 (2007), [astro-ph/0610919](#).
- [57] M. Dan, S. Rosswog, J. Guillochon, and E. Ramirez-Ruiz, Prelude to A Double Degenerate Merger: The Onset of Mass Transfer and Its Impact on Gravitational Waves and Surface Detonations, *ApJ* **737**, 89 (2011), [arXiv:1101.5132 \[astro-ph.HE\]](#).
- [58] K. Kremer, J. Sepinsky, and V. Kalogera, Long-term Evolution of Double White Dwarf Binaries Accreting through Direct Impact, *ApJ* **806**, 76 (2015), [arXiv:1502.06147 \[astro-ph.SR\]](#).
- [59] K. Kremer, K. Breivik, S. L. Larson, and V. Kalogera, Accreting Double White Dwarf Binaries: Implications for LISA, *ApJ* **846**, 95 (2017), [arXiv:1707.01104 \[astro-ph.HE\]](#).
- [60] G. Nelemans, AM CVn stars, in *The Astrophysics of Cataclysmic Variables and Related Objects*, Astronomical Society of the Pacific Conference Series, Vol. 330, edited by J. M. Hameury and J. P. Lasota (2005) p. 27, [arXiv:astro-ph/0409676 \[astro-ph\]](#).
- [61] G. H. A. Roelofs, G. Nelemans, and P. J. Groot, The population of AM CVn stars from the Sloan Digital Sky Survey, *MNRAS* **382**, 685 (2007), [arXiv:0709.2951](#).
- [62] É. É. Flanagan and T. Hinderer, Constraining neutron-star tidal Love numbers with gravitational-wave detectors, *Phys. Rev. D* **77**, 021502 (2008), [arXiv:0709.1915 \[astro-ph\]](#).
- [63] T. Hinderer, B. D. Lackey, R. N. Lang, and J. S. Read, Tidal deformability of neutron stars with realistic equations of state and their gravitational wave signatures in binary inspiral, *Phys. Rev. D* **81**, 123016 (2010), [arXiv:0911.3535 \[astro-ph.HE\]](#).
- [64] B. P. Abbott, R. Abbott, T. D. Abbott, F. Acernese, K. Ackley, C. Adams, T. Adams, P. Addesso, R. X. Adhikari, V. B. Adya, and et al., GW170817: Measurements of Neutron Star Radii and Equation of State, *Phys. Rev. Lett.* **121**, 161101 (2018), [arXiv:1805.11581 \[gr-qc\]](#).
- [65] A. L. Piro, Tidal Interactions in Merging White Dwarf Binaries, *ApJ* **740**, L53 (2011), [arXiv:1108.3110 \[astro-ph.SR\]](#).
- [66] J. Fuller and D. Lai, Dynamical tides in compact white dwarf binaries: tidal synchronization and dissipation, *MNRAS* **421**, 426 (2012), [arXiv:1108.4910 \[astro-ph.SR\]](#).
- [67] J. Fuller and D. Lai, Tidal Novae in Compact Binary White Dwarfs, *ApJ* **756**, L17 (2012), [arXiv:1206.0470 \[astro-ph.SR\]](#).
- [68] J. Burkart, E. Quataert, P. Arras, and N. N. Weinberg, Tidal resonance locks in inspiraling white dwarf binaries, *MNRAS* **433**, 332 (2013), [arXiv:1211.1393 \[astro-ph.SR\]](#).
- [69] A. L. Piro, Inferring the Presence of Tides in Detached White Dwarf Binaries, arXiv e-prints, [arXiv:1908.04896 \(2019\)](#), [arXiv:1908.04896 \[astro-ph.SR\]](#).
- [70] J. Fuller and D. Lai, Dynamical tides in compact white dwarf binaries: influence of rotation, *MNRAS* **444**, 3488 (2014), [arXiv:1406.2717 \[astro-ph.SR\]](#).
- [71] K. Belczynski, D. E. Holz, T. Bulik, and R. O’Shaughnessy, The first gravitational-wave source from the isolated evolution of two stars in the 40-100 solar mass range, *Nature* **534**, 512 (2016), [arXiv:1602.04531 \[astro-ph.HE\]](#).
- [72] I. Mandel and S. E. de Mink, Merging binary black holes formed through chemically homogeneous evolution in short-period stellar binaries, *MNRAS* **458**, 2634 (2016), [arXiv:1601.00007 \[astro-ph.HE\]](#).
- [73] C. L. Rodriguez, M. Morscher, B. Pattabiraman, S. Chatterjee, C.-J. Haster, and F. A. Rasio, Binary Black Hole Mergers from Globular Clusters: Implications for Advanced LIGO, *Phys. Rev. Lett.* **115**, 051101 (2015), [arXiv:1505.00792 \[astro-ph.HE\]](#).
- [74] C. L. Rodriguez, M. Zevin, C. Pankow, V. Kalogera, and F. A. Rasio, Illuminating Black Hole Binary Formation Channels with Spins in Advanced LIGO, *ApJ* **832**, L2 (2016), [arXiv:1609.05916 \[astro-ph.HE\]](#).
- [75] W. M. Farr, S. Stevenson, M. C. Miller, I. Mandel, B. Farr, and A. Vecchio, Distinguishing spin-aligned and isotropic black hole populations with gravitational waves, *Nature* **548**, 426 (2017), [arXiv:1706.01385 \[astro-ph.HE\]](#).
- [76] S. Stevenson, C. P. L. Berry, and I. Mandel, Hierarchical analysis of gravitational-wave measurements of binary black hole spin-orbit misalignments, *MNRAS* **471**, 2801 (2017), [arXiv:1703.06873 \[astro-ph.HE\]](#).
- [77] B. Farr, D. E. Holz, and W. M. Farr, Using Spin to Understand the Formation of LIGO and Virgo’s Black Holes, *ApJ* **854**, L9 (2018), [arXiv:1709.07896 \[astro-ph.HE\]](#).
- [78] M. Hannam, P. Schmidt, A. Bohé, L. Haegel, S. Husa, F. Ohme, G. Pratten, and M. Pürrer, Simple Model of Complete Precessing Black-Hole-Binary Gravitational Waveforms, *Phys. Rev. Lett.* **113**, 151101 (2014), [arXiv:1308.3271 \[gr-qc\]](#).
- [79] P. Schmidt, F. Ohme, and M. Hannam, Towards models of gravitational waveforms from generic binaries: II. Modelling precession effects with a single effective precession parameter, *Phys. Rev. D* **91**, 024043 (2015), [arXiv:1408.1810 \[gr-qc\]](#).
- [80] H. Yu, D. Martynov, S. Vitale, M. Evans, D. Shoemaker, B. Barr, G. Hammond, S. Hild, J. Hough, S. Huttner, S. Rowan, B. Sorazu, L. Carbone, A. Freise, C. Mow-Lowry, K. L. Dooley, P. Fulda, H. Grote, and D. Sigg, Prospects for Detecting Gravitational Waves at 5 Hz with Ground-Based Detectors, *Phys. Rev. Lett.* **120**, 141102 (2018), [arXiv:1712.05417 \[astro-ph.IM\]](#).
- [81] M. C. Miller and J. M. Miller, The masses and spins of neutron stars and stellar-mass black holes, *Phys. Rep.* **548**, 1 (2015), [arXiv:1408.4145 \[astro-ph.HE\]](#).
- [82] The LIGO Scientific Collaboration, the Virgo Collaboration, B. P. Abbott, R. Abbott, T. D. Abbott, S. Abraham, F. Acernese, K. Ackley, C. Adams, R. X. Adhikari, and et al., GWTC-1: A Gravitational-Wave Transient Catalog of Compact Binary Mergers Observed by LIGO and Virgo during the First and Second Observing Runs, arXiv e-prints, [arXiv:1811.12907 \(2018\)](#),

- arXiv:1811.12907 [astro-ph.HE].
- [83] B. Zackay, T. Venumadhav, L. Dai, J. Roulet, and M. Zaldarriaga, Highly spinning and aligned binary black hole merger in the Advanced LIGO first observing run, *Phys. Rev. D* **100**, 023007 (2019), arXiv:1902.10331 [astro-ph.HE].
- [84] The LIGO Scientific Collaboration, the Virgo Collaboration, B. P. Abbott, R. Abbott, T. D. Abbott, S. Abraham, F. Acernese, K. Ackley, C. Adams, R. X. Adhikari, and et al., Binary Black Hole Population Properties Inferred from the First and Second Observing Runs of Advanced LIGO and Advanced Virgo, arXiv e-prints , arXiv:1811.12940 (2018), arXiv:1811.12940 [astro-ph.HE].
- [85] J. Fuller and L. Ma, Most Black Holes are Born Very Slowly Rotating, arXiv e-prints , arXiv:1907.03714 (2019), arXiv:1907.03714 [astro-ph.SR].
- [86] C. L. Rodriguez, P. Amaro-Seoane, S. Chatterjee, K. Kremer, F. A. Rasio, J. Samsing, C. S. Ye, and M. Zevin, Post-Newtonian dynamics in dense star clusters: Formation, masses, and merger rates of highly-eccentric black hole binaries, *Phys. Rev. D* **98**, 123005 (2018), arXiv:1811.04926 [astro-ph.HE].
- [87] H. C. Spruit, Dynamo action by differential rotation in a stably stratified stellar interior, *A&A* **381**, 923 (2002), arXiv:astro-ph/0108207 [astro-ph].
- [88] A. Heger, S. E. Woosley, and H. C. Spruit, Presupernova Evolution of Differentially Rotating Massive Stars Including Magnetic Fields, *ApJ* **626**, 350 (2005), arXiv:astro-ph/0409422 [astro-ph].
- [89] Y. Qin, T. Fragos, G. Meynet, J. Andrews, M. Sørensen, and H. F. Song, The spin of the second-born black hole in coalescing binary black holes, *A&A* **616**, A28 (2018), arXiv:1802.05738 [astro-ph.SR].
- [90] J. Fuller, A. L. Piro, and A. S. Jermyn, Slowing the spins of stellar cores, *MNRAS* **485**, 3661 (2019), arXiv:1902.08227 [astro-ph.SR].
- [91] A. Beifiori, S. Courteau, E. M. Corsini, and Y. Zhu, On the correlations between galaxy properties and supermassive black hole mass, *MNRAS* **419**, 2497 (2012), arXiv:1109.6265 [astro-ph.CO].
- [92] J. Kormendy and L. C. Ho, Coevolution (Or Not) of Supermassive Black Holes and Host Galaxies, *ARA&A* **51**, 511 (2013), arXiv:1304.7762.
- [93] M. Volonteri, Formation of supermassive black holes, *A&A Rev.* **18**, 279 (2010), arXiv:1003.4404 [astro-ph.CO].
- [94] P. Madau and M. J. Rees, Massive Black Holes as Population III Remnants, *ApJ* **551**, L27 (2001), arXiv:astro-ph/0101223 [astro-ph].
- [95] M. Volonteri, P. Madau, and F. Haardt, The Formation of Galaxy Stellar Cores by the Hierarchical Merging of Supermassive Black Holes, *ApJ* **593**, 661 (2003), arXiv:astro-ph/0304389 [astro-ph].
- [96] K. D. Kokkotas and B. G. Schmidt, Quasi-Normal Modes of Stars and Black Holes, *Living Reviews in Relativity* **2**, 2 (1999), arXiv:gr-qc/9909058 [gr-qc].
- [97] C.-E. Rydberg, E. Zackrisson, P. Lundqvist, and P. Scott, Detection of isolated Population III stars with the James Webb Space Telescope, *MNRAS* **429**, 3658 (2013), arXiv:1206.0007 [astro-ph.CO].
- [98] S. A. Hughes, Untangling the merger history of massive black holes with LISA, *MNRAS* **331**, 805 (2002), arXiv:astro-ph/0108483 [astro-ph].
- [99] A. Sesana, M. Volonteri, and F. Haardt, The imprint of massive black hole formation models on the LISA data stream, *MNRAS* **377**, 1711 (2007), arXiv:astro-ph/0701556 [astro-ph].
- [100] A. Sesana, J. Gair, I. Mandel, and A. Vecchio, Observing Gravitational Waves from the First Generation of Black Holes, *ApJ* **698**, L129 (2009), arXiv:0903.4177 [astro-ph.CO].
- [101] F. Koliopanos, Intermediate Mass Black Holes: A Review, in *Proceedings of the XII Multifrequency Behaviour of High Energy Cosmic Sources Workshop. 12-17 June* (2017) p. 51, arXiv:1801.01095 [astro-ph.GA].
- [102] M. Mezcua, Observational evidence for intermediate-mass black holes, *International Journal of Modern Physics D* **26**, 1730021 (2017), arXiv:1705.09667 [astro-ph.GA].
- [103] A. V. Filippenko and L. C. Ho, A Low-Mass Central Black Hole in the Bulgeless Seyfert 1 Galaxy NGC 4395, *ApJ* **588**, L13 (2003), arXiv:astro-ph/0303429 [astro-ph].
- [104] S. A. Farrell, N. A. Webb, D. Barret, O. Godet, and J. M. Rodrigues, An intermediate-mass black hole of over 500 solar masses in the galaxy ESO243-49, *Nature* **460**, 73 (2009), arXiv:1001.0567 [astro-ph.HE].
- [105] B. Kızıltan, H. Baumgardt, and A. Loeb, An intermediate-mass black hole in the centre of the globular cluster 47 Tucanae, *Nature* **542**, 203 (2017), arXiv:1702.02149 [astro-ph.GA].
- [106] C.-J. Haster, Z. Wang, C. P. L. Berry, S. Stevenson, J. Veitch, and I. Mandel, Inference on gravitational waves from coalescences of stellar-mass compact objects and intermediate-mass black holes, *MNRAS* **457**, 4499 (2016), arXiv:1511.01431 [astro-ph.HE].
- [107] C.-J. Haster, F. Antonini, V. Kalogera, and I. Mandel, N-Body Dynamics of Intermediate Mass-ratio Inspirals in Star Clusters, *ApJ* **832**, 192 (2016), arXiv:1606.07097 [astro-ph.HE].
- [108] S. A. Hughes, (Sort of) Testing relativity with extreme mass ratio inspirals, in *Laser Interferometer Space Antenna: 6th International LISA Symposium*, American Institute of Physics Conference Series, Vol. 873, edited by S. M. Merkowitz and J. C. Livas (2006) pp. 233–240, gr-qc/0608140.
- [109] N. Seto, Detecting Planets around Compact Binaries with Gravitational Wave Detectors in Space, *ApJ* **677**, L55 (2008), arXiv:0802.3411 [astro-ph].
- [110] N. Tamanini and C. Danielski, The gravitational-wave detection of exoplanets orbiting white dwarf binaries using LISA, *Nature Astronomy* , 381 (2019).
- [111] D. Christodoulou, Nonlinear nature of gravitation and gravitational-wave experiments, *Phys. Rev. Lett.* **67**, 1486 (1991).
- [112] M. Favata, Nonlinear Gravitational-Wave Memory from Binary Black Hole Mergers, *Astrophys. J. Lett.* **696**, L159 (2009), arXiv:0902.3660 [astro-ph.SR].
- [113] H. Yang and D. Martynov, Testing Gravitational Memory Generation with Compact Binary Mergers, *Phys. Rev. Lett.* **121**, 071102 (2018), arXiv:1803.02429 [gr-qc].
- [114] W. E. East and F. Pretorius, Superradiant instability and backreaction of massive vector fields around Kerr black holes, *Phys. Rev. Lett.* **119**, 041101 (2017).
- [115] R. Brito, S. Ghosh, E. Barausse, E. Berti, V. Cardoso, I. Dvorkin, A. Klein, and P. Pani, Gravitational wave

- searches for ultralight bosons with LIGO and LISA, *Phys. Rev. D* **96**, 064050 (2017), arXiv:1706.06311 [gr-qc].
- [116] L. S. Finn, Detection, measurement, and gravitational radiation, *Phys. Rev. D* **46**, 5236 (1992).
- [117] C. Cutler and E. E. Flanagan, Gravitational waves from merging compact binaries: How accurately can one extract the binary's parameters from the inspiral waveform?, *Phys. Rev. D* **49**, 2658 (1994).
- [118] M. Vallisneri, Use and abuse of the Fisher information matrix in the assessment of gravitational-wave parameter-estimation prospects, *Phys. Rev. D* **77**, 042001 (2008).
- [119] C. Cutler, Angular resolution of the LISA gravitational wave detector, *Phys. Rev. D* **57**, 7089 (1998).
- [120] J. Veitch, V. Raymond, B. Farr, W. Farr, P. Graff, S. Vitale, B. Aylott, K. Blackburn, N. Christensen, M. Coughlin, W. Del Pozzo, F. Feroz, J. Gair, C.-J. Haster, V. Kalogera, T. Littenberg, I. Mandel, R. O'Shaughnessy, M. Pitkin, C. Rodriguez, C. Röver, T. Sidery, R. Smith, M. Van Der Sluys, A. Vecchio, W. Vousden, and L. Wade, Parameter estimation for compact binaries with ground-based gravitational-wave observations using the lalinference software library, *Phys. Rev. D* **91**, 042003 (2015).
- [121] LIGO Scientific Collaboration, *LIGO Algorithm Library - LALSuite*, free software (GPL) (2018).
- [122] S. Khan, S. Husa, M. Hannam, F. Ohme, M. Pürrer, X. J. Forteza, and A. Bohé, Frequency-domain gravitational waves from nonprecessing black-hole binaries. ii. a phenomenological model for the advanced detector era, *Phys. Rev. D* **93**, 044007 (2016).
- [123] W. G. Anderson, P. R. Brady, J. D. E. Creighton, and E. E. Flanagan, Excess power statistic for detection of burst sources of gravitational radiation, *Phys. Rev. D* **63**, 042003 (2001).
- [124] I. Mandel, C. P. L. Berry, F. Ohme, S. Fairhurst, and W. M. Farr, Parameter estimation on compact binary coalescences with abruptly terminating gravitational waveforms, *Classical and Quantum Gravity* **31**, 155005 (2014).