

Bacterial growth and motility in sub-micron constrictions

Jaan Männik, Rosalie Driessen, Peter Galajda, Juan E. Keymer, and Cees Dekker¹

Kavli Institute of Nanoscience, Delft University of Technology, Lorentzweg 1, 2628 CJ, Delft, The Netherlands

Communicated by Robert H. Austin, Princeton University, Princeton, NJ, July 10, 2009 (received for review April 18, 2009)

In many naturally occurring habitats, bacteria live in micrometer-size confined spaces. Although bacterial growth and motility in such constrictions is of great interest to fields as varied as soil microbiology, water purification, and biomedical research, quantitative studies of the effects of confinement on bacteria have been limited. Here, we establish how Gram-negative *Escherichia coli* and Gram-positive *Bacillus subtilis* bacteria can grow, move, and penetrate very narrow constrictions with a size comparable to or even smaller than their diameter. We show that peritrichously flagellated *E. coli* and *B. subtilis* are still motile in microfabricated channels where the width of the channel exceeds their diameters only marginally (~30%). For smaller widths, the motility vanishes but bacteria can still pass through these channels by growth and division. We observe *E. coli*, but not *B. subtilis*, to penetrate channels with a width that is smaller than their diameter by a factor of approximately 2. Within these channels, bacteria are considerably squeezed but they still grow and divide. After exiting the channels, *E. coli* bacteria obtain a variety of anomalous cell shapes. Our results reveal that sub-micron size pores and cavities are unexpectedly prolific bacterial habitats where bacteria exhibit morphological adaptations.

biophysics | confinement | microbiology | microfluidics

Bacterial growth and movement in confined spaces is ubiquitous in nature and plays an important role in diverse fields ranging from soil microbiology, water purification, to microbial pathogenesis. The majority of bacteria in soil and bedrock live in pores of size 6 micrometer and smaller (1). These bacteria constitute a large portion of the Earth's biomass (2) and are essential for the functioning of soil. Although distributions of bacteria in soil and Earth's subsurfaces have been studied, it is largely unknown how bacteria grow, move, and penetrate pores of very small size. The latter is also an important question for water treatment and purification. Whereas microbiology textbooks consider output from 0.2- μm pore size filters sterile, it has recently been found that numerous bacteria can pass through these membranes and grow thereafter (3, 4). It is unclear what mechanism bacteria employ to penetrate such membranes. Also, in microbial pathogenesis, bacterial growth and penetration is a problem, for example in dental implants (5), but likely also in soft tissues and bones of a host organism where confined spaces are relevant to bacterial propagation through the extracellular matrix.

Some experimental (6–10) and theoretical (11, 12) studies have discussed the effects of restricting geometry on bacterial motility. It has been established that *Escherichia coli* bacteria can swim in 2.0 μm and wider channels without appreciable slowdown (8) and that bacteria regularly swim in close proximity to surfaces (9), preferring some types of surfaces to others (10). It has been shown that these behaviors can be used to guide bacterial movement in microfluidic structures (10, 13). The effects of confinement on bacterial growth have received very limited attention. Growth of *E. coli* bacteria has been studied by Takeuchi et al. in microfabricated structures (14). In these experiments, confinement affected bacterial growth in the direction of its elongation. The experiments showed that the filamentous bacteria can bend during growth and conform to the shapes of the microfabricated structures. All previous research

on bacterial motility and growth have been carried out in relatively large channels and constrictions where the critical dimension is larger than one micrometer, that is, larger than bacterial diameter. So far, no one has addressed questions such as: How narrow channels can bacteria penetrate using their own motility? How do bacterial movement and growth change in very narrow channels compared with that in unbound medium?

Here, we establish how *E. coli* and *Bacillus subtilis* bacteria can grow and move in very narrow constrictions with sub- μm width, and we determine the lower limits for the constriction size which these bacteria are able to penetrate. We show that *E. coli* and *B. subtilis* retain their motility in microfabricated channels with a width that exceeds their diameters by only approximately 30%. We also show that bacteria can penetrate even narrower channels. To achieve this, bacteria initiate growth into the channels. In this process, elongation and division pushes bacteria forward until they fill the whole channel. Whereas *B. subtilis* bacteria can grow in such a way in channels as narrow as their diameter, *E. coli* bacteria are even able to penetrate channels with a width that is much smaller than their diameter. Our work demonstrates that growth in channels which are narrower than the bacterial diameter can drastically change the shape of *E. coli* and lead to a morphological phenotype which has not been described previously.

Results

To carry out this study, we design and fabricate microfluidic channels (constrictions) which connect chambers (small bacterial wells) on a silicon chip and image individual GFP-labeled bacteria in these structures using fluorescent time-lapse microscopy. The advantages of using silicon chips for these experiments are the possibility to define sub-micrometer size channels and the capability to carry out long-term measurements with these bacteria. Whereas the bacteria can pass wide channels within seconds, it can take several days before the bacteria are able to cross the narrowest channels. The microfluidic chips that we use make it possible to maintain the necessary conditions for bacterial growth and motility for such periods of time. The schematic of the microfluidic chip used in this experiment is presented in Fig. 1A. The motile bacteria enter the structure of chambers and channels from the left vertical channel. The observations start when the bacteria reach to the left-most chamber of the structure and start to move through the channels toward the chambers on the right end of the arrays. Bacterial movement in channels is partially driven by chemotaxis toward the nutrient source which consists of growth media in the 'feeding channel' on the right end of the arrays. From left to right, the channels are fabricated progressively narrower. This allows monitoring how the population of bacteria is able to negotiate increasingly narrower channels and adapt to life in such a confined environment. On the same silicon chip, a large

Author contributions: J.M., P.G., J.E.K., and C.D. designed research; J.M. performed research; J.M. and R.D. analyzed data; and J.M., P.G., J.E.K., and C.D. wrote the paper.

The authors declare no conflict of interest.

Freely available online through the PNAS open access option.

¹To whom correspondence should be addressed. E-mail: c.dekker@tudelft.nl.

This article contains supporting information online at www.pnas.org/cgi/content/full/0907542106/DCSupplemental.

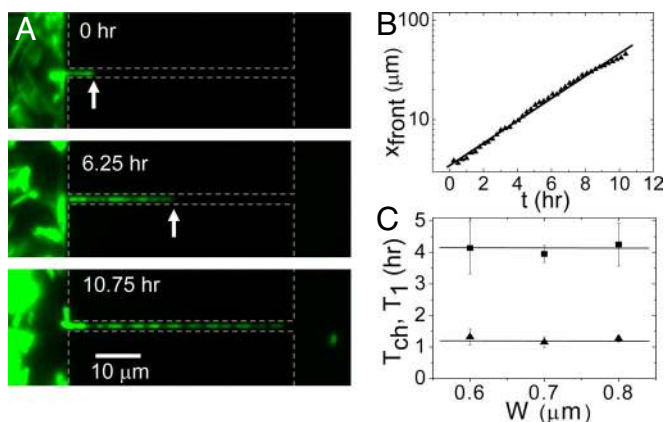


Fig. 3. Bacterial growth through narrow channels. (A) Time-lapse fluorescent images of bacterial growth in a $0.6\text{-}\mu\text{m}$ wide channel. Dashed gray lines show the approximate boundaries of the chambers and channels. The arrows point to the position of the bacterial front. (B) Position of the bacterial front vs. time for the growth process on panel A. The line presents a fit of the function $x_{\text{front}}(t) = L_0 + L_1 2^{t/T_{ch}}$. (C) Doubling time of the chain length T_{ch} (squares) and division time of the first bacterium in the chain T_1 (triangles) vs. channel width. Each T_{ch} and T_1 value in the *Inset* of B represents an average over several populations in channels of the given width on the same chip. Error bars represent standard deviations among different populations.

variation in channel width may seem small, it does represent a significant fraction (25%) of the bacterial diameter. The constancy of the measured doubling times is further verified by plotting the doubling times of the first bacterium at the leading position in the chain (T_1). These doubling times are determined directly from time-lapse movies as time difference between consecutive division events of the bacterium. As shown in the *Inset* of Fig. 3B (triangles), this time is factor of 3.5 shorter and independent of the channel width as well. The average doubling time of the first bacterium ($T_1 = 73 \pm 10$ min) compares well to the division time of bacteria in the chambers (70 ± 26 min) at low cell density.

After bacteria exit from the narrow channels ($W \leq 0.8 \mu\text{m}$) to the chambers, they further proliferate there. These bacteria, which usually can be traced back to a single ancestor in the narrow channel, show a wide variety of shapes and sizes that can differ substantially from the regular rod-shape of *E. coli*. As an example, Fig. 4A shows an image of the chamber, 5 hours after the first bacterium has reached it through a $0.6 \mu\text{m}$ constriction. This image follows the sequence shown in Fig. 3A. Most bacteria in this image show aberrant shapes and cross-sectional sizes that considerably exceed the size of regular *E. coli*. The lateral dimensions of aberrant bacteria (Fig. 4B and C) exceed the diameters of regular *E. coli* (Fig. 4G) by factor of two or more. In some extreme cases, the bacteria are completely round shaped (Fig. 4D), reminiscent to the well-studied L-form morphology (18–20). The aberrant bacteria which we observe frequently show bulges and protuberances on their sidewalls as well as bent cell shapes (Fig. 4E and F). No bacteria with such widths and shape irregularities are observed in chambers which are connected to the inlet through wide channels where motility is possible. Although treatment with cell-wall acting antibiotics has been used in the past to produce the L-form morphology (18, 19), these shapes appear in our experiments where none of such antibiotics were present. The appearance of aberrantly shaped bacteria correlates with the width of the channel: In narrower channels, the ratio of occurrence of aberrant versus regular bacteria increases. Based on these observations, we associate the aberrant phenotype with the passage through narrow channels.

To follow the formation of aberrantly shaped bacteria in real

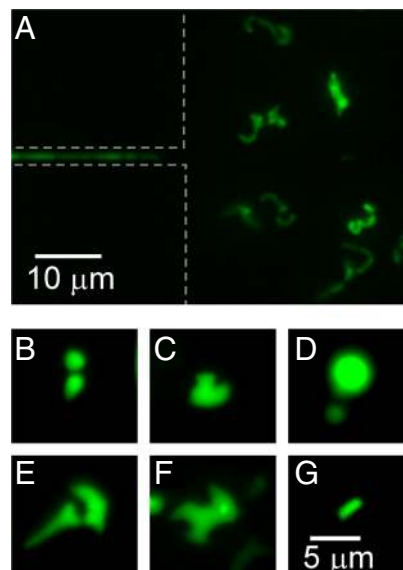


Fig. 4. Aberrant bacteria exit narrow channels. (A) Fluorescence image of $0.6\text{-}\mu\text{m}$ wide channel and a chamber 5 h after the first bacterium appeared in this chamber. Variety of aberrantly shaped bacteria can be seen to populate the chamber. The image is sequence to the series shown in Fig. 3A. (B–F) Different aberrant bacterial shapes at higher magnification. (G) For comparison, fluorescence image of a regularly shaped and sized bacterium which has emerged from the same channel as the bacteria shown in panels E and F. The same scale bar applies for all of the panels from B to G.

time, we fabricate channels with a different geometry (Fig. 5A *Inset* on the right and Fig. S1 and Fig. S2). Whereas previously we discussed bacterial growth in channels which were etched deep and narrow into silicon (vertical channels), the channels which are used here are etched shallow into silicon nitride (horizontal channels) (for details of fabrication see Materials and Methods). In this case, the depth of the trench in silicon nitride determines the effective width of the channel. Such geometry allows a detailed imaging of the bacterial shapes during the growth. Fig. 5A shows an example of the development of bacteria in a $0.3\text{-}\mu\text{m}$ wide horizontal channel. The bacteria are

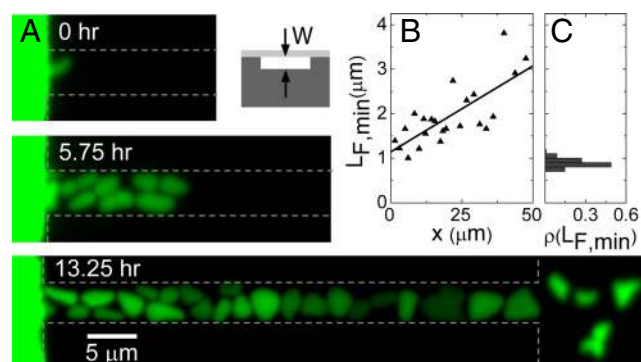


Fig. 5. Morphogenesis of *E. coli* in shallow horizontal channels. (A) Time-lapse fluorescence images of bacteria in channel of $0.3 \mu\text{m}$ width (and other dimensions 5 and $50 \mu\text{m}$). Dashed lines show approximate boundaries of chambers and channels. *Inset*: schematic side-view cross-section of such channel. Darker gray corresponds to silicon and lighter gray to PDMS. (B) Minimum Feret's diameter vs. bacterial position in the channel (right vertical axes). The position is measured from the channel entrance. The data points correspond to the bacteria on the *Bottom* image of panel A. (C) For comparison, distribution of minimum Feret's diameters in batch culture. Batch culture has grown to optical density $\text{OD}_{600} = 2.3$. The vertical axes of this plot is the same as in B.

pressed into the channel by the neighboring bacteria in a densely packed chamber (Fig. S3). Upon entering the channel, the bacteria are strongly squeezed by the channel walls and they flatten. Despite the significant flattening, these bacteria are still able to grow and divide (Movie S3 and Movie S4). During growth in the channel, the bacteria widen further, becoming almost round shaped near the exit from the 50- μm long channel. The broadening of bacteria is quantitatively analyzed in Fig. 5B where the minimum Feret's diameter $L_{F,min}$ is plotted as a function of the bacterial position from the channel entrance. Here, $L_{F,min}$ is defined as the minimum distance between parallel tangents at opposing borders of the bacterium. The borders of the object are defined by zero crossings of the second derivative in the direction of intensity gradient. For comparison, Fig. 5C shows the distribution of $L_{F,min}$ in batch cultures. Note that $L_{F,min}$ overestimates the actual diameter of the rod-shaped bacterium by $\approx 17\%$. Fig. 5B shows that bacteria considerably widen as they move within the channel. At the exit of the 50- μm long channel they have become wider by about factor of 3 than their width at the entrance. The stress imposed by the channel walls thus not only deforms the bacteria, but also promotes bacterial growth in the sideways direction. Further changes in bacterial shape occur when bacteria exit the channels. Here, bacteria contract and frequently obtain rugged shapes with bulges and protuberances as described above (Movie S5).

Essentially all of the aberrant bacteria that exit narrow channels ($W < 0.8 \mu\text{m}$) are nonmotile. Most of these bacteria are able to grow and divide. Exceptions are the round-shaped bacteria which we do not observe to divide. After 1–2 days, a population with regular shape and size recovers from the aberrantly shaped bacteria that seeded the chamber in the beginning (Fig. S4 and Movie S5). These bacteria have also restored their motility. Interestingly, on the chip, where several chambers and narrow channels are connected in row, repeated transitions from aberrant to regular cells thus take place multiple times as the bacterial population advances from one chamber to the next.

Comparison of the Channel Widths to the Bacterial Diameters. Next we make a detailed comparison of the diameter of our *E. coli* strain to the width of the channels that these bacteria penetrate by either motility or growth. We measure the diameter distributions of bacteria in batch cultures using fluorescence images. These measurements are summarized in Fig. 6A. As Fig. 4A shows, the diameters of *E. coli* in stationary-phase cultures (black, $\bar{D} = 0.76 \pm 0.05 \mu\text{m}$) are $\approx 18\%$ smaller than in mid-log phase (blue, $\bar{D} = 0.91 \pm 0.05 \mu\text{m}$), in agreement with previous observations (21–23). Because the bacterial density in the chambers is comparable with the density of stationary culture, we consider the average diameter $\bar{D} = 0.76 \mu\text{m}$ to be a good estimate for the typical bacterial diameter in our experiments. The ratio of the channel width to the bacterial diameter, W/\bar{D} , is a relevant parameter for the hydrodynamics of bacterial swimming as well as for comparisons to measurements performed with other organisms. We find the channel width that is characteristic to the transition between motility and no motility to be $W = 0.95 \pm 0.05 \mu\text{m}$ (Fig. 2C), which results in $W/\bar{D} = 1.25 \pm 0.07$. However, it is likely that the bacteria that are observed moving in channels where $W/\bar{D} \approx 1.25$, are those whose diameters are smaller than the mean diameter of the population \bar{D} . The smallest bacterial diameter that we measure in a population is 12% lower than the mean diameter. If we assume that the bacteria with this smallest diameter are responsible for the observed motility then $W/D_{smallest} = 1.4$. We thus conclude that flagellar motility is still possible in channels that are only 25–40% wider than the cell diameter.

The narrowest vertical channel which we observe *E. coli* to penetrate by growth and division is 0.4- μm wide. Fig. 5 shows

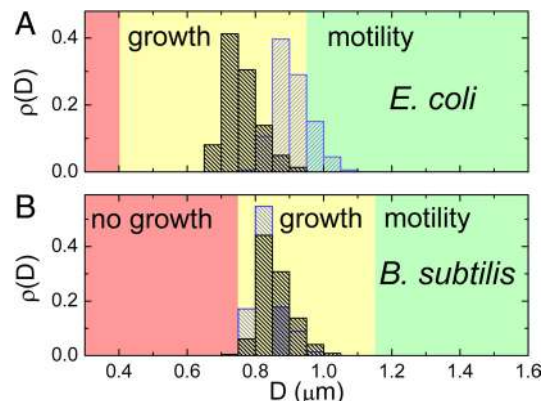


Fig. 6. Comparison of channel widths to bacterial diameters. (A) Distribution of bacterial diameters in log ($\text{OD}_{600} = 0.6$, blue) and in stationary phase ($\text{OD}_{600} = 2.3$, black) for *E. coli* as determined from fluorescence intensity profiles of individual bacteria from batch cultures. Details of the size determination are given in S1 Text. The average diameters are $\bar{D} = 0.91 \pm 0.05 \mu\text{m}$ in log and $\bar{D} = 0.76 \pm 0.05 \mu\text{m}$ in stationary phase. The range of channel widths where bacteria are motile or grow are indicated by the green or yellow colored background, respectively. The range of channel widths where no penetration is observed is shown in red. (B) The same for *B. subtilis* strain for the log ($\text{OD}_{600} = 0.4$, blue) and for stationary phase distributions ($\text{OD}_{600} = 2.0$, black) where the average diameters are $\bar{D} = 0.84 \pm 0.04 \mu\text{m}$ and $\bar{D} = 0.86 \pm 0.04 \mu\text{m}$, respectively.

that *E. coli* can penetrate horizontal channels of 0.3- μm width and we have observed *E. coli* to enter and grow in even narrower horizontal channels. In these channels, however, we expect that bacteria are able to deform to some extent the ceiling of the channel which is made of elastic PDMS. Because of such a deformation, the actual width of the channel may exceed its defined value of 0.3 μm once the bacteria enter it. Even for an observation period of 1 week, we have not observed bacteria to enter and grow in 0.3- μm wide vertical channels, which are much less deformable because of their rigid silicon walls. The limiting width of the channel is independent on nutrient conditions in which we carried out the experiments. In separate experiments we varied the nutrient concentration by allowing or stopping flow of growth medium in the “feeding channel” (see Fig. 1A and B), and we obtained the same results. Based on these observations, we consider 0.4 μm the limit to the channel width which *E. coli* can penetrate by growth and division. If we use the average diameter $\bar{D} = 0.76 \mu\text{m}$, we obtain a ratio $W/\bar{D} \approx 0.5$. Thus, *E. coli* can penetrate constrictions with a size twice narrower than their typical sizes in stationary-phase batch cultures.

We also investigate growth and motility of *B. subtilis* in the same on-chip setting as for *E. coli*. The diameters of the *B. subtilis* strain used in this study (24) ($\bar{D} = 0.86 \pm 0.04 \mu\text{m}$, see Fig. 4B) are comparable to those of *E. coli*. Unlike *E. coli*, the diameter of *B. subtilis* is essentially constant during the various growth phases, indicating that *B. subtilis* exhibits less morphological plasticity than *E. coli*. Swimming of *B. subtilis* is similar to the swimming of *E. coli* in wider constrictions. The transition from swimming motility to no motility takes place at $W = 1.15 \pm 0.05 \mu\text{m}$, yielding a ratio $W/\bar{D} = 1.3 \pm 0.06$ and $W/D_{smallest} = 1.5$ (the diameter of the narrowest bacterium was 13% smaller than the mean), comparable to the values found for *E. coli*. In the range of channel widths from 1.05 to 0.75 μm , *B. subtilis* is able to penetrate the channels through growth, similar to what was observed for *E. coli* (Fig. S5 and Movie S6). However, we do not see *B. subtilis* growing through channels narrower than 0.75 μm even after a week-long observation. This yields a lower limit for growth of $W/\bar{D} = 0.9$. The ratio for the smallest measured

defined by using e-beam lithography. Two types of channels with different geometry were fabricated. Following their geometry they were referred to as vertical or horizontal channels. The vertical channels were etched deep (5–7 μm) and narrow (from 2 to 0.3 μm) whereas horizontal channels were etched shallow (300 nm and less) but extended more in lateral direction (from 1 to 10 μm). To create vertical channels a cryo-etch process with SF_6 and O_2 gases at -120°C was used to etch silicon. For horizontal channels a standard reactive ion etching process with CHF_3 and Ar gases was used to etch silicon nitride layer which was deposited on the top of the silicon wafer. In the chip with horizontal channels, the chambers and connecting flow channels were created using additional cryo-etching step which allowed making these structures deeper (1.7–1.8 μm). The channels and chambers were closed using PDMS (polydimethylsiloxane) covered glass coverslips of 150- μm thickness. The approximately 30- μm thick PDMS layer was treated with oxygen plasma just before bonding the glass slide to the silicon chip. Access holes to the microfluidic channels were created by a KOH wet etch through the silicon chip beforehand. The widths of the vertical channels were determined by cutting channels across and imaging the cross-sections of channels in a SEM. The widths of horizontal channels were determined by Tencor Alpha Step 500 profilometer.

Bacterial Strains. *E. coli* used in the experiments were RP437 strain which was transformed with two different plasmids. The original was a high copy number plasmid expressing ampicillin resistance and GFP (35). The second plasmid used in these bacteria was derived from the original plasmid in our laboratory. In this plasmid, ampicillin-resistance gene was excised and a kanamycin resis-

tance gene inserted into this location. The *B. subtilis* strain used in this study carries GFP fused to the *abrB* promoter (*PabrB-gfp*) stably integrated in the chromosome along with chloramphenicol resistance (24). All bacteria were grown in standard Luria-Bertani media (1% wt peptone from casein, 0.5% wt yeast extract, and 1% wt NaCl) complemented with respective antibiotics for each strain of bacteria (100 $\mu\text{g}/\text{mL}$ ampicillin, 50 $\mu\text{g}/\text{mL}$ kanamycin, and 5 $\mu\text{g}/\text{mL}$ chloramphenicol). The measurements with bacteria were done at $25\text{--}26^\circ\text{C}$.

Fluorescence Microscopy. An Olympus IX81 inverted fluorescence microscope with a $100\times$ NA 1.3 oil immersion and a $60\times$ dry objective was used for imaging the bacteria. Fluorescence from GFP was excited by 100 W Hg lamp through a 0.25 or 0.5 neutral density filter and Chroma EN GFP filtercube. Hamamatsu 3CCD color camera was used for imaging at maximum frame rate of 10 Hz. A Mad City Labs MicroStage 20E stage was used for automated positioning over multiple locations on the chip. For image analysis, MatLab Image Analysis Toolbox and DipImage Toolbox were used. A detailed description of the measurements of the bacterial diameters using fluorescent images can be found from *SI Text* and [Fig. S6–S10](#).

ACKNOWLEDGMENTS. We thank S. Donkers, S. Hage, and M. Zuiddam for technical assistance; J.-W. Veening for the *B. subtilis* strain; and B. Rieger, K.C. Huang, and C. Woldringh for valuable discussions. This work has been supported in part by research grants from Stichting voor Fundamenteel Onderzoek der Materie (FOM), de Nederlandse Organisatie voor Wetenschappelijk Onderzoek (NWO), and Nanoned. J.E.K. acknowledges support from Delft University of Technology Start-up Fund.

- Ranjard L, Richaume AS (2001) Quantitative and qualitative microscale distribution of bacteria in soil. *Res Microbiol* 152:707–716.
- Whitman WB, Coleman DC, Wiebe WJ (1998) Prokaryotes: The unseen majority. *Proc Natl Acad Sci USA* 95:6578–6583.
- Hahn MW (2004) Broad diversity of viable bacteria in 'sterile' (0.2 μm) filtered water. *Res Microbiol* 155:688–691.
- Wang Y, Hammes F, Boon N, Egli T (2007) Quantification of the filterability of freshwater bacteria through 0.45, 0.22, and 0.1 μm pore size filters and shape-dependent enrichment of filterable bacterial communities. *Environ Sci Technol* 41:7080–7086.
- do Nascimento C, et al. (2008) Bacterial leakage along the implant-abutment interface of premachined or cast components. *Int J Oral Maxillofac Surg* 37:177–180.
- Frymier PD, Ford RM (1997) Analysis of bacterial swimming speed approaching a solid-liquid interface. *AIChE J* 43:1341–1347.
- Frymier PD, Ford RM, Berg HC, Cummings PT (1995) 3-Dimensional tracking of motile bacteria near a solid planar surface. *Proc Natl Acad Sci USA* 92:6195–6199.
- Biondi SA, Quinn JA, Goldfine H (1998) Random motility of swimming bacteria in restricted geometries. *AIChE J* 44:1923–1929.
- Vigeant MAS, Ford RM, Wagner M, Tamm LK (2002) Reversible and irreversible adhesion of motile *Escherichia coli* cells analyzed by total internal reflection aqueous fluorescence microscopy. *Appl Environ Microbiol* 68:2794–2801.
- DiLuzio WR, et al. (2005) *Escherichia coli* swim on the right-hand side. *Nature* 435:1271–1274.
- Ramia M, Tullock DL, Phanthien N (1993) The role of hydrodynamic interaction in the locomotion of microorganisms. *Biophys J* 65:755–778.
- Lauga E, DiLuzio WR, Whitesides GM, Stone HA (2006) Swimming in circles: Motion of bacteria near solid boundaries. *Biophys J* 90:400–412.
- Galajda P, Keymer J, Chaikin P, Austin R (2007) A wall of funnels concentrates swimming bacteria. *J Bacteriol* 189:8704–8707.
- Takeuchi S, DiLuzio WR, Weibel DB, Whitesides GM (2005) Controlling the shape of filamentous cells of *Escherichia coli*. *Nano Lett* 5:1819–1823.
- Berg HC (2000) Motile behavior of bacteria. *Phys Today* 53:24–29.
- Alon U, et al. (1998) Response regulator output in bacterial chemotaxis. *EMBO J* 17:4238–4248.
- Amsler CD, Cho MS, Matsumura P (1993) Multiple factors underlying the maximum motility of *Escherichia coli* as cultures enter postexponential growth. *J Bacteriol* 175:6238–6244.
- Kleineberger E (1935) The natural occurrence of pleuropneumonia-like organisms in apparent symbiosis with *Streptobacillus moniliformis* and other bacteria. *J Pathol Bacteriol* 40:93.
- Joseleu-Petit D, Liebart JC, Ayala JA, D'Ari R (2007) Unstable *Escherichia coli* L forms revisited: Growth requires peptidoglycan synthesis. *J Bacteriol* 189:6512–6520.
- Leaver M, Dominguez-Cuevas P, Coxhead JM, Daniel RA, Errington J (2009) Life without a wall or division machine in *Bacillus subtilis*. *Nature* 457:849–854.
- Koch AL (2001) in *Bacterial Growth and Form* (Kluwer, Dordrecht).
- Bronk BV, Vandemerwe WP, Stanley M (1992) In vivo measure of average bacterial-cell size from a polarized-light scattering function. *Cytometry* 13:155–162.
- Woldringh CL, Grover NB, Rosenberger RF, Zaritsky A (1980) Dimensional rearrangement of rod-shaped bacteria following nutritional shift-up. 2. Experiments with *Escherichia coli* B-R. *J Theor Biol* 86:441–454.
- Veening JW, Kuipers OP, Brul S, Hellingwerf KJ, Kort R (2006) Effects of phosphorelay perturbations on architecture, sporulation, and spore resistance in biofilms of *Bacillus subtilis*. *J Bacteriol* 188:3099–3109.
- Turner L, Ryu WS, Berg HC (2000) Real-time imaging of fluorescent flagellar filaments. *J Bacteriol* 182:2793–2801.
- Yao X, et al. (2002) Atomic force microscopy and theoretical considerations of surface properties and turgor pressures of bacteria. *Colloid Surf B-Biointerfaces* 23:213–230.
- Chattopadhyay S, Moldovan R, Yeung C, Wu XL (2006) Swimming efficiency of bacterium *Escherichia coli*. *Proc Natl Acad Sci USA* 103:13712–13717.
- Keymer JE, Galajda P, Muldoon C, Park S, Austin RH (2006) Bacterial metapopulations in nanofabricated landscapes. *Proc Natl Acad Sci USA* 103:17290–17295.
- Matias VRF, Beveridge TJ (2005) Cryo-electron microscopy reveals native polymeric cell wall structure in *Bacillus subtilis* 168 and the existence of a periplasmic space. *Mol Microbiol* 56:240–251.
- Yao X, Jericho M, Pink D, Beveridge T (1999) Thickness and elasticity of Gram-negative *Murein sacculi* measured by atomic force microscopy. *J Bacteriol* 181:6865–6875.
- Arnoldi M, et al. (2000) Bacterial turgor pressure can be measured by atomic force microscopy. *Phys Rev E* 62:1034–1044.
- Koch AL (1983) The surface stress theory of microbial morphogenesis. *Adv Microb Physiol* 24:301–366.
- Boulbitch A, Quinn B, Pink D (2000) Elasticity of the rod-shaped Gram-negative eubacteria. *Phys Rev Lett* 85:5246–5249.
- Huang KC, Mukhopadhyay R, Wen B, Gitai Z, Wingreen NS (2008) Cell shape and cell-wall organization in Gram-negative bacteria. *Proc Natl Acad Sci USA* 105:19282–19287.
- Cormack BP, Valdivia RH, Falkow S (1996) FACS-optimized mutants of the green fluorescent protein (GFP). *Gene* 173:33–38.