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Baryon Number Creation and Phase Transitions in the Early Universe

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transitions, i.e. changes in gauge symmetries in a cooling Universe. Although the expansion of the Universe can be affected signifor galaxy formation. duction and the generation of the density perturbations required model. Also we briefly discuss problems with monopole pronature of the phase transition, as numerically calculated in a simple ficantly, the final baryon number is surprisingly insensitive to the consider finite temperature effects, namely the existence of phase how the required CP violation can be provided for. Secondly we discuss recent calculations using unified interactions, especially baryon-antibaryon asymmetry in the early Universe. First we Summary. We aim at a consistent scenario for the generation of the

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1. Baryon Number Creation

relevant doson, generally converges, by the symmetry breaking (for a review see Ellis, 1980). Here and in the following we take $\hbar = c = k_R = 1$, but keep $M_{Pl} \equiv G^{-1/2}$ relevant boson, generally denoted by X, received a large mass M_X (p = uud) decay into e^+ spantaneously broken (see Sect. 2) at high energies into the have quarks and leptons in common representations, which may lead to baryon number violating reactions (for example $uu \rightarrow e^+ d$). Grand Unified Theories (GUTs) have a single coupling constant g ($\alpha \equiv g^2/4\pi \sim 1/40$) at high energies ($> M_X \sim 10^{14} - 10^{15}$ GeV) and $=1.22 \ 10^{19}$ μ - uuu) decay into e^+ and $\pi^0=d\overline{d}$, but with a large lifetime τ \sim const $M_X^4/M_p^5 \sim 10^{31\pm2}$ yr (Ellis et al. 1000). Low energy remnants of unified interactions predict proton presently observed weak, electromagnetic and strong interactions. This symmetric (i.e. one simple gauge group G) theory is GeV.

see Weinberg (1972)] compared to the interaction rates. In the charge + parity (CP) can produce a net baryon number density in simplest scenario the final ratio of densities of baryon number over expansion of the Universe [rate $H \equiv \dot{a}/a$, with a(t) the scale factor; provided by the mass of the X bosons ($Ta \neq const$) and the rapid (Weinberg, 1979, and references therein). This last ingredient is conservation and the symmetries of charge (C) conjugation and It is well known that GUTs, which violate baryon number (B) Universe during a period out of thermal equilibrium

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> (Nanopoulos and Weinberg, 1979) entropy is produced by the decay of the lightest superheavy bosons

$$_{B}/s = \frac{45}{4\pi^{4}} \zeta(3) (N_{X}/N) \Delta B,$$
 (1)

in the Weinberg-Salam transition at $T \sim 300$ GeV, but see below). increasing processes at lower temperatures (e.g. some super cooling typical GUTs, where the inequality is required if there are entropy the bosons mass $(T_d < M_X)$ after a period of free $(\Gamma_{decay} < H \text{ for } T$ be generated at temperatures T_d (when $\Gamma_{\text{decay}}(T_d) \sim H(T_d)$) below states of X and all particles (mass $< M_X$), respectively. This n_B will where ΔB is the average net baryon number produced in the decay $> T_d$) expansion giving the required non-thermal distribution $(n_X \sim n_\gamma \sim T^3 \pm n_{\text{therm}} \sim (M_X T)^{3/2} \text{ exp } (-T/M_X))$. The observed $n_B/s \sim 10^{-10} \; (\Omega_{B0}/0.01)$ thus requires $\Delta B \gtrsim 10^{-8}$, since $N_X/N \sim 10^{-2}$ in of an $X - \overline{X}$ pair and N_X and N are the effective number of spin ΔB is determined by the different branching ratios of X and \overline{X}

diagrams (see Appendix A), which come from higher order Feynman

potentials.) vacua exist, analogous θ defines the ground state when topologically distinct Yang-Mills $(\delta\theta_{\rm GUT})$ of the θ parameter of the QCD (SU(3)) vacuum. (This interference graphs and those leading to a finite renormalization connection was noticed (Ellis et al., 1979). The simplest way to have a ΔB of the right magnitude is with two S's of Higgs (Yildiz and Cox, 1979). Recently a direct 1.e. usual Kobayashi-Maskawa matrix (giving CP violation for $n \ge$ (Barr et al. (1979)]. Already Nanopoulos and Weinberg (1979) had sentations) the produced $\Delta B \sim \Gamma_{\rm interference}/\Gamma_{\rm total}$ scalars (these numbers give the dimensionality of the repreobservable at unification energies and essential for ΔB (Ellis et al., matrices (in generation space) f_i and in $\Gamma_{\text{total}} \sim \Gamma_{\text{tree}}$ the trace of $2f_i$'s $=(0, 0, 0, 0, v_0)$ with $v_0 \sim 300$ GeV)), and b) (n-1) parameters only $(n \times n)$. These have a) $(n-1)^2$ parameters to be identified with the scalar fermion-antifermion $f_i \overline{\psi} \phi_i \psi$) of the GUT Lagrangian density within the numerator Im Tr of $4f_i$'s. In the Yukawa terms (i.e. observed the need of different scalars in order to have a net ΔB Γ_{inter} is the imaginary part of the trace of 8 L there are two non-trivial unitary matrices in generation space $\geqq 6$ quark flavours) after breaking with a 5 of Higgs $H\left(\langle H \rangle\right)$ But in the minimal G = SU(5) theory broken by 5 and 45 Higgs to the Bloch functions 1981a) between Yukawa coupling is too small for

observational limits on the electric dipole moment of the neutron d_n , which gets a dominant contribution of the CP violating term with parameter $\theta(1 \text{ GeV}) \gtrsim \delta \theta_{\text{GUT}}$, allow for practically no entropy generation after the n_B generation at unification energies (Ellis Assuming $\theta = 0$ at a high energy, say M_{Planck} ,

zero (Peccei and Quinn, 1977). Another possible alternative (see also the Note) for CP violating decays, namely mixing of X and \overline{X} al., 1981a, b). The reasoning goes as follows: $d_n \gtrsim 4~10^{-16}~\delta\theta_{\rm GUT}~e$ -cm would violate the experimental upper limit (2 $10^{-24}~e$ -cm) if the et al., 1980). (Kolb and Wolfram, 1980b; Nanopoulos and Weinberg, 1979) observed fermions, these bosons all being charged electrically eigenstates, is not allowed for superheavy bosons X coupled to the into X_a and X_b Hamiltonian eigenstates which are not CP anomaly of a global U(1) axial symmetry makes all θ equivalent to Ellis et al. (1981a)]. Note that these arguments do not hold if the smaller they could alleviate the nearly conflicting theoretical ($\delta\theta$ above] were naturally assumed to be O(1). If these are substantially U_{dm} connecting the different contributing Higgses [see point b) $\delta\theta_{\rm GUT}$ and ΔB graphs moduli of typical unitary matrix elements allow for later entropy generation. We remark that in comparing generated $\{n_B/s\}_{GUT}$ had to be significantly larger than 10^{-10} to This needs not hold for a GUT with superheavy fermions (Barbieri < const. $|U_{dm}|^2 n_B/s$) and observational d_n limits [see Eqs. (24) of

 $=g^2/2M_W^2$. The Yukawa couplings $f\bar{\psi}_1\phi\psi_1$ give after spontaneous symmetry breaking a mass term for lepton l of $fv_0\bar{\psi}_1\psi_1$, hence fthan the gauge coupling g is the following: these terms in $L_{\rm GUT}$ give at lower energies simultaneously with the Weinberg-Salam breakdelayed decay estimates for small enough couplings of the relevant X to the fermions (e. g. $\alpha_{\rm eff} \lesssim 10^{-4}$, $M_X \sim 10^{14}$ GeV). If the lightest X decays with a larger $\alpha_{\rm eff}$ a considerable dilution of the generated (cf. example in Sect. 2) and the small effective Fermi coupling G_F ing to the weak and electromagnetic forces the observed fermion The reason that these Yukawa couplings could very well be smaller baryon number takes place (Kolb and Wolfram, 1980b, Fig. 4). after which a fresh asymmetry is created (Kolb and Wolfram, $(a'b'c' \rightarrow X)$ and X exchanging collisions $(ab \rightarrow cd, B(ab) + B(cd))$, by a complicated interplay of decay $(X \rightarrow abc)$, inverse decay antibaryon asymmetry would be washed out at unification energies scenario. More general calculations have been done, which show Weinberg, 1979) these numerical solutions confirm the simple masses. This breaking (Higgs doublet with $\langle 0|\phi|0\rangle = v_0(^0_1)$, $v_0 \sim 300$ GeV) gives the weak boson W the mass $M_W \sim gv_0 \sim 80$ GeV 1980b, Harvey et al., 1981; Fry et al., 1980). As expected (cf. $\sim m_i v_0^{-1}$ is very small (e.g. Taylor, 1976). Up till now we have considered the simple delayed decay primordial (quantum gravity epoch?) baryon-

2. Phase Transitions

In Sect. 1 all calculations described were done in a flat space zero temperature formalism (as laboratory physics) with as only cosmological effect the use of a statistical ensemble of massive particles driven out of equilibrium by the expansion of the Universe. However an important phenomenon is not taken into account yet: symmetry restoration of spontaneously broken gauge theories at high temperatures $T_c \sim v$. Let us briefly explain the mechanism of spontaneous symmetry breaking (e. g. Taylor, 1976). If the effective potential $V(\phi_{c1})$ of the Higgs scalars ϕ (V is a function of the classical, i.e. not operator valued, fields ϕ_{c1}) has a minimum at $\phi_{c1} = v + 0$, than the vacuum expectation values is nonzero: $\langle 0|\phi|0\rangle = v$. The field theory is most simple with shifted fields $v = \phi - v$, which behave properly, i.e. annihilate the vacuum $\langle 0|v|0\rangle = 0$. The Lagrangian as function of v, which remains renormalizable after the symmetry breaking, shows that the gauge fields corresponding to the broken symmetries [remember the gauge fields are $A_{\mu} = A_{\mu}^a I_{a}$, with I_a the $(n^2 - 1)$ generators of the Lie

group $G(=\mathrm{SU}(n))$ describing the symmetry] have become massive, cf. M_W of Weinberg-Salam. No massless scalars appear, the Goldstone theorem being invalidated by the existence of long-range gauge interactions. Let us give the simplest example possible G=U(1) (e. g. O'Raifeartaigh, 1979): we have a complex scalar field $\phi=\phi_1+i\phi_2$, one gauge field A_μ ($G=e^i\phi$ has one generator) with field strength $F_{\mu\nu}=\partial_\mu A_\nu-\partial_\nu A_\mu$, the gauge covariant derivative $D_\mu\phi=\partial_\mu\phi+igA_\mu\phi$ with coupling constant g and the Lagrange density (from which the equations of motion for A_μ and ϕ follow by functional derivation)

$$L = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{1}{2}|D_{\mu}\phi|^2 - V(\phi), \tag{2a}$$

$$V(\phi) = -\mu |\phi|^2 + \lambda |\phi|^4, \quad \mu, \lambda > 0,$$
 (2b)

which is invariant under the U(1) gauge transformations with *local* parameter A(x) in inifinitesimal form

$$A_{\mu}(x) \rightarrow A_{\mu}(x) + \frac{1}{g} \hat{\sigma}_{\mu} \Lambda(x)$$

 $\phi(x) \rightarrow (1 - iA(x))\phi(x)$

Rewriting L in fields $v = \phi - \overline{\phi}$ around the asymmetric ground state of the potential $|\overline{\phi}|^2 = \mu/2\lambda$ leads to massive gauge fields (the second term of L giving $\frac{1}{2}g^2|\overline{\phi}|^2A_{\mu}^2$) with mass² = $g^2\mu/2\lambda$ and after a gauge rotation we have

$$L = \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} g^2 \frac{\mu}{2\lambda} A_{\mu}^2 + \frac{1}{2} |D_{\mu} \nu_1|^2 + 2\mu \nu_1^2$$

$$-L_{\text{interaction}}(\nu_1, A_{\mu}). \tag{3}$$

Thus after spontaneous symmetry breaking we have a gauge invariant theory with massive vector fields A_{μ} and no massless scalars ν_2 (the Higgs miracle). The precise form of $L_{\text{interaction}}$ in Eq. (3) is crucial to keep gauge invariance, necessary for renormalizability. Note that we do have a massive scalar ν_1 and for realistic G similar ones will turn out to be essential for the baryon number generation in the early Universe.

Presently it is thought that Nature uses the spontaneous breaking of

$$G_{\text{unified}} \xrightarrow{M_U} \text{SU}(3)_{\text{colour}} \times \{\text{SU}(2) \times U(1)\}_{\text{electroweak}}$$

$$M_{WS} \rightarrow SU(3)_{colour} \times U(1)_{electromagnetic}$$

(at low energies the 8 gluons and photon are still massless) at a hierarchy of energies $M_U \sim 10^{15}$ GeV and $M_{WS} \sim 10^2$ GeV (see Ellis, 1980). Finite temperature effects change the potential of Eq. (2b): $V(T, \phi_{c,1}) = -\mu^2 \phi_{c,1}^2 + \lambda \phi_{c,1}^4 + c T^2 \phi_{c,1}^2$, c is a constant (Weinberg, 1974). The non-zero minimum disappears at a critical temperature $T_c = c^{-1/2}\mu$. These symmetry restorations at high temperature resemble phase transitions (for a review see Linde, 1979), but for a small range around T_c the perturbation expansion used, giving the $cT^2\phi_{c,1}^2$ term, breaks down.

The symmetry breaking will lead to a different energy density of the vacuum before and after the transition at $T_c(\Delta\varrho \sim T_c^*)$. The presently observed vanishing of the cosmological constant A and the relation $A_{\rm eff} = 8\pi M_{PlQ_v}^2$ imply $\varrho_v(T=0) \lesssim 10^{-29} {\rm g \ cm^{-3}} \sim (10^{-2} {\rm eV})^4$. Thus the gravitating vacuum energy density is $\varrho_v \sim T_c^4$ and $\varrho_v \sim 0$ 0 before and after the transition, respectively (Kolb and Wolfram, 1980a), which can considerably change the expansion of the Universe (cf. Fig. 1). We will consider the baryon number generation as compared to that of the standard Big Bang model (i.e. $a \sim 1/T \propto t^{1/2}$).

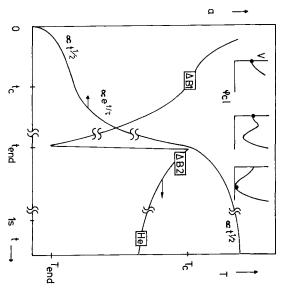


Fig. 1. Sketch of the history of the Universe during a first order phase transition: a is the scalefactor and T the equilibrium temperature (for adiabatic expansion $T \subset a^{-1}$). Included representative forms of the effective potential V, whose minima are possible vacuum state (see text). Twice baryon number (B) nonconserving reactions could have generated a baryon-anti baryon asymmetry, but in the symmetric vacuum state there will be no net B generation during the AB1 period. The observed B should thus be created after the reheating $(T_R \sim T_c)$, which must be smooth in order to preserve a homogeneous Helium synthesis (see text)

When the Universe cools to $T \le T_c$ a phase transition will take place from the symmetric vacuum $\langle \phi \rangle = 0$ (expectation values for a Gibbs ensemble with temperatur T) to the broken state $\langle \phi \rangle = v(T)$. If the transition occurs smoothly at T_c due to the onset of instability of the symmetric state in $V(T_c, \phi_{c1})$, we speak of a second order phase transition $(2PT): v(T) \sim \{1 - T^2/T_c^2\}^{1/2}v(T=0)$. The expansion rate of the Universe $H^2 = (8\pi G/3)$ ($\varrho_v + \pi^2 NT^4/30$) will hardly be changed by the 2PT: the energy density is dominated by the particles $(\varrho \sim NT^4 \gg \varrho_v \sim T_c^4)$. But even in this unspectacular case (2PT) the standard calculations of Sect. 1 (Kolb and Wolfram, 1980b) are not correct for $T > T_c$ [Screening corrections to the cross-sections $(\sigma \sim \alpha^2/T^2)$ instead of $(\tau \sim \alpha^2/M_X^2)$ appear to be quite unimportant for the final n_B , Harvey et al. (1981)]. The same Boltzmann equations can be applied to the cosmological context but with starting conditions of thermal equilibrium at $T = T_c$ instead of at $T = \infty$ (or T_{P_L}).

To illustrate the effects this modification, we consider a simple model (Kolb and Wolfram, 1980b) and solve the differential equations, describing the baryon number changing processes, for a range of initial conditions (details can be found in Appendix A). In Fig. 2 the evolution of the ratio $Y_B = n_B/n_y$ of the net baryon number density to the photon number density is plotted: $Y_B(x; x_0)$ gives Y_B at temperature $T = M_X/X$ under the initial condition of thermal equilibrium at $x_0 = M_X/T_0$. Thus $Y_B(x_0; x_0) \equiv 0$ and $Y_B(\infty; x_0)$ is the final baryon to photon ratio for $T \rightarrow 0$, neglecting a factor O (10^{-1}) from later annihilation heating (e.g. $e^+e^- \rightarrow \gamma$).

Figure 2 shows how the baryon production peaks around x = 1 $(T = M_X)$, followed by substantial damping (quantitative details depend on several parameters, as discussed in Appendix A). Starting at $x_0 \neq 0$ lowers the maximally attainable Y_B , but relaxes to nearly the same final value, due to a balance of production and

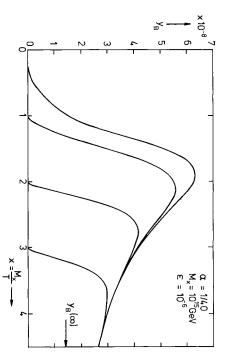


Fig. 2. The generation of the baryon number to photon ratio $Y_B(x;x_0)$, where $x = M_X/T$ and M_X the mass of the *B*-violating boson, is calculated for a simple model, with CP violation parameter ε . Earlier calculations (Kolb and Wolfram, 1980b) use symmetric starting conditions at $x_0 = 0$. Finite temperature effects lead to phase transitions (*PT*), which give the boson a mass M_X only for $T \le T_c \sim M_X/g$. The $Y_B(x;x_0)$ evolution is calculated for realistic starting values after a second order $PT(x_0 \sim g \sim \frac{1}{2})$ or after the smooth reheating ending the period of supercooling of a first order $PT(x_0 \sim 1)$. The final Y_B values are given in Fig. 3

damping at large x. Thus it is clear that the standard calculations, as discussed in Sect. 1, hold true in the case of a 2PT ($x_0 = M_X/T_c \sim g \sim \frac{1}{2}$), to high precision (final deviations $\ll 0.01 \%$ in the model of Fig. 2).

In the case of a first order phase transition (1*PT*) the transition of the symmetric metastable state to the energetically favourable broken state is blocked by a barrier, either (i) from a mass² term in $V: T^2c\phi_{c1}^2$ with c a constant depending on g^2 or λ , or (ii) from temperature independent quantum corrections to the tree potential if $\lambda < g^4$. The Universe cools below T_c with the vacuum remaining in the symmetric state (hence called a false vacuum) and its *constant* energy density $\varrho_v \sim T_c^4$ dominates over that of the particles ($\sim NT^4$, $T \propto 1/a$). This leads to an effective cosmological constant $\Lambda_{\rm eff} = 8\pi G \varrho_v \sim 8\pi T_c^4/M_{P1}^2$ which results in exponential expansion ($a \propto \exp t/\tau$, $t \equiv (8\pi/3)^{-1/2} M_{P1}/T_c^2$) with rapid supercooling ($T \sim a^{-1} \ll T_c$). This is illustrated in Fig. 1.

expands too rapidly, being continuously accelerated (Sato, 1981; Guth and Weinberg, 1981). 2. Nucleation by barrier penetration (a large supercooling results. space volume. Obviously barrier penetration effects are small and a non-perturbative effect, cf. Coleman, 1979) has a constant rate per bubbles cannot catch up with the rest of the quickly fill the below T_c and either the bubble density gets high enough and they of nucleation: 1. Thermal nucleation rates have a maximum (Coleman, 1977; Callan and Coleman, 1977). There are two types which by expansion (velocity $\sim c$) conquer the false vacuum observed broken state by nucleation of bubbles of true vacuum, down to T=0, the Universe can only have reached the presently If the false vacuum remains metastable (confined by a barrier) There are several alternatives to end the period of supercooling Universe (little supercooling) or else these This originally was the motivation for 2. Nucleation by barrier penetration (a Universe which few just

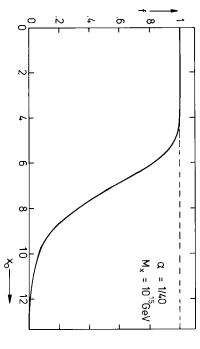


Fig. 3. Final baryon-number to photon ratio $Y_B(\infty, x_0)$ for realistic starting conditions $(x_0 \sim 1)$ as compared to $x_0 = 0$: $f \equiv Y_B(\infty, x_0)/Y_B(\infty, 0)$. In this case $Y_B(\infty, 0) = 1.43 \ 10^{-8}$

considering 1 PTs, where the stretched horizons $(d_{\rm H}=a(t))$

 $dt'/a(t') \sim \tau e^{t/t}$) may reduce the monopole density, one per $d_{\rm H}(t_{\rm end})^3$ Sect. 1 (see below). could jeopardize the standard baryon number creation results of the reheating is instantaneous and that $\sim T_c$ will be attained; this travel time of one light-second; see Fig. 1) and 2. It is not clear that energy in the bubble walls before He production, which is to give in the presently observable Universe (Zel'dovich et al., 1974). If the cosmic background radiation excludes the presence of bubble walls hibits a complete vaccum conversion. But the isotropy of the ongoing exponential expansion in the false vacuum region transition false→true has taken place approaches unity, the Guth, 1981): although at every fixed point the probability that a Universe can have made the transition to the true vacuum (cf. the tunneling nucleation rate is small, leading to a cooling to typically (Einhorn et al., 1980; Guth and Tye, 1980; see below). If $T \ll T_c$, it is not clear how at a certain temperature the whole PT ends with huge bubbles, of galaxy size, say, filling the everywhere, two further problems arise: 1. Thermalisation of the seems impossible (bubble sizes>available pro-

Another way to end the period of supercooling (evading the above problems) is that the false vacuum becomes unstable at $T_1 < T_c$. This may happen if the barrier vanishes [in the U(1) Higgs model if $3g^4/16\pi^2 < \lambda < g^4$ (Linde, 1979); in G = SU(5) region d of Guth and Weinberg (1981)]. At $\sim T_1$ the whole of the Universe still in the symmetric state will shift to the broken one, with a diverging nucleation rate when the confining barrier vanishes. The latent heat $(\varrho_v(>T_1)-\varrho_v(<T_1)\sim T_c^4)$ relaxed in the many small bubbles from the last "flash" of nucleation probably will be thermalised, quickly reheating the Universe to just below T_c .

Which scenario the Universe follows (2 PT; 1 PT thermal or tunneling nucleation, or T_1 shift) depends on the yet unknown coupling constants in the GUT Lagrangian. Daniel and Vayonakis (1981) find for SU(5) a weak 1 PT typically. If the Higgs potential has scalars with bare masses vanishing ($V_{\rm tree} = \lambda \phi_{\rm cl}^4/4$!), quantum corrections from the gauge bosons still may give symmetry breaking, for U(1): one loop $V^{(1)} = (3g^4/64\pi^2)\phi_{\rm cl}^4$ (In $(\phi_{\rm cl}^2/\langle\phi\rangle^2)$ –1/2) and $\lambda = (33/8\pi^2)g^4$ (Coleman and Weinberg, 1973). There are two strong arguments to expect radiatively broken SU(5): 1. this might explain the hierarchy problems $M_{WS} \ll M_U \ll M_{P1}$, and 2. this SU(5) GUT with massless scalars and 3 generations of $(\bar{5}+10)$ fermions (as observed) might be the remnant of the N=8 extended

supergravity theory (references in Hut and Klinkhamer, 1981). The phase transition for the radiatively broken SU(5) GUT is strongly 1 PT, and supercooling goes to \sim 1 GeV when the nucleation rate equals the expansion rate (Billoire and Tamvakis, 1981; Daniel, 1981). Recently it was realised that non-perturbative effects may reduce the period of supercooling, destabilising the vacuum perhaps at T=0 (106 GeV) (Tamvakis and Vayonakis, 1981).

Let us mention another possible origin for a general shift of the vacuum (Hut and Klinkhamer, 1981). Until now local fields on a flat background were used, but global space-time effects probably are important at low enough temperatures and might induce a shift to the broken state at $T_1 \sim T_c^2/T_{Pl} \sim 10^{11}$ GeV [for radiatively broken SU(5)]. Basically thermal radiation at this temperature will have wavelengths of the order of the event horizon $D_H \sim T_{Pl}/T_c^2$, thus invalidating the usual flat space-time description of the barrier that should stabilize the symmetric state.

Now we consider the baryon number generation after the reheating in a strong 1 PT. We assume that the supercooling ends at T_1 by destabilisation of the false vacuum. For definiteness we will consider the radiatively broken SU(5) theory. Unfortunately nothing is known about the thermalisation involving bubble-bubble and bubble-particle interactions. We estimate the typical bubble size, nucleated when the barrier became vanishingly small, to be of order $v^{-1} \sim T_c^{-1}$ and we assume the thermalisation to take place in the same time scale. In the cosmological context this means instantaneous ($\ll H^{-1}(T_c) \sim N^{-1/2}T_{p1}T_c^{-2}$) and smooth [\ll effective horizon after $T_R \sim H_{\rm standard}(T_R)$] reheating.

strongly diminished than in the standard scenario. Both gauge generation, i.e. deviation from thermal equilibrium when the Universe cools below the boson mass (cf. Kolb and Wolfram, the Higgs bosons have a mass (defined by $\delta^2 V/\delta\phi_a\delta\phi_b$) of order $m_{\rm H}$ symmetric state, in which the gauge bosons are still massless and first occasion, however, baryon number violating reactions are important (Fig. 1). At the more by an extra factor $\sim (T_1/T_c)^3$. heat released at the transition reduces this primordial n_B/s even $\{-\alpha_{\text{GUT}}^2 N^{-1/2} T_{PI}/T_I\}$ [cf. Kolb and Wolfram, 1980b, Eq. (4.2)] Thus for $T_1 \lesssim 10^{-2} T_c$ the damping is huge ($\lesssim 10^{-40}$). The latent boson X (inverse) decays and X exchanging 2-2 reactions will now be in equilibrium (rates $\Gamma > H$) for 10^{16} GeV $\gtrsim T \ge T_1$, for example baryon number from the quantum gravity epoch will be even more $(\Gamma/H)_{2-2} \sim \alpha_{\text{GUT}}^2(T_{Pl}/T)$ (cf. Ellis et al., 1980b). Hence any primor-Another important modification is that any truly primordial 1980b), is thus missing since $m_X = 0$, cf. Toussaint et al. (1979) $\sim gT$ (Linde, 1979). The crucial ingredient of baryon number The Universe passes twice through temperature regimes where baryon asymmetry deviation from thermal equilibrium the Universe cools below ıs damped ф 2 factor Ħ the

With no surviving baryon number it is all the more important to have sufficient reheating after the period of supercooling. Comparing the number of degrees of freedom (Einhorn and Sato, 1980) before the transition at $T_1(N_1)$ and after reheating to $T_R(N_R)$ we find

$$T_{\rm R} = T_{\rm c} \big\{ 30/(N_{\rm R} \pi^2) + (N_1/N_{\rm R}) \ (T_1/T_{\rm c})^4 \big\}^{1/4} \sim 0.4 \ T_{\rm c}$$

for $\{\mathrm{SU}(3) \times \mathrm{SU}(2) \times U(1)\}_R$, 6 quark flavours and one 5 of SU(5) Higgs giving one Weinberg-Salam doublet, $N_R = 106.75$. Note that if the SU(5) theory is a remnant of SU(8)/E(7) superunification the many superheavies ($\sim M_{Pl}$) will not count in estimating T_R , because of densities $\propto \exp(-M/T_1)$ from the period of equilibrium unified interactions as discussed above.

Now we will discuss the baryon asymmetry generated for $T \leq T_R$. First we assume that the thermalisation process for the small (T_c^{-1}) bubbles produces no asymmetry itself. Again, earlier

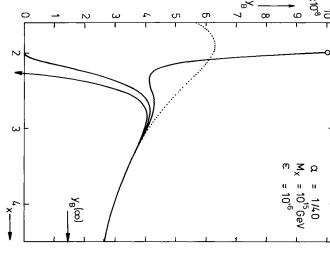


Fig. 4. The generation of the final baryon-antibaryon asymmetry for a first order phase transition, if the thermalisation of the small bubbles of true vacuum at the end of the supercooling epoch itself gives a net baryon number $Y_B^{\text{bubbles}}(x_0=2)=\pm 10^{-7}$. For comparison the curves for $Y_B(x_0=0)=0$ (dotted) and $Y_B(x_0=2)=0$ (Fig. 2) are given

contribution will be larger because 1. the CP violating diagrams are of lower order than for the gauge boson X, and 2. dilution of the GeV) and the light Higgs bosons (for radiatively broken GUTs: considered here was taken to be a gauge boson $(M_X \sim gT_C \sim 10^{15})$ we conclude that details of this mode as long as smooth reheating takes place to $T_R \gtrsim \frac{1}{3} M_X$, for this mode as long as smooth reheating takes place to $T_R \gtrsim \frac{1}{3} M_X$, units of $Y_B(\infty; 0)$. Nearly the same baryon number is produced in baryon number density from the delayed Higgs decay will be less delayed decay at temperatures lower than $T_R \sim 0.4 T_c$. which holds true for all realistic unification models. we conclude that details of the initial conditions are unimportant the range $x_0 = 0 \sim 5$, followed by a sharp drop around $x_0 = 7$. Thus after the supercooling, with starting values $x_0 \sim M_X/0.4 T_c \sim 1$. In discussion of 2 PT's, and use Fig. 2 in case of smooth reheating model of Kolb and Wolfram (1980b), we can extend the previous initial conditions in solving the same rate equations. For the simple calculations have to be modified only by taking more realistic $Y_B(\infty; x_0)$ on the reheating temperature $T_R = M_X/x_0$ is plotted in $<\alpha$; see Sect. 1). 3 the dependence of the finally generated baryonnumber $\alpha^{1/2}M_X$) will give the major contribution to $Y_B(\infty)$ from This Higgs But the

Finally the assumption of baryon number conserving thermalisation processes after the reheating can be dropped: in Fig. 4 it is shown that a sizeable asymmetry $Y_B(x_0; x_0) = \pm 10^{-7}$ will be damped out for moderate x_0 -values (in Fig. 4 we chose $x_0 = 2$).

3. Discussion

We have presented a consistent scenario of baryon number generation in the early Universe, taking into account the effects of

are presented in the Appendix A. But the major contribution to the accelerated expansion. change the behaviour of the Universe, leading to a period of since the final result depends mainly on processes operative at second order phase transition the final n_B/s turns out to be the same Higgs bosons, which have larger CP violating amplitudes final n_B/s will come from the simple delayed decay of the lighter temperature calculations! For a simple model, quantitative details roughly the same baryon number density as in the standard zero $T \lesssim M_X$. A strongly first order phase transition will drastically timates and numerical calculations are invalid at $T > T_c$. After a phase transitions of gauge symmetries. Previous analytical es- $\sim \alpha^{-1} \varepsilon^{\text{Gauge}}$) and less dilution. by thermalization, But even in this case, the gauge bosons will produce after reheating

To complete our discussion of the realistic baryon number creation we discuss two further problems: 1. The generation of density inhomogeneities leading to the formation of the present structure, e.g. galaxies. In Appendix 2 we argue against an origin for the required inhomogeneities from 1 PTs only; most plausibly the origin lies in the quantum gravity epoch. 2. Directly related to phase transitions and vacuum structure is the problem of monopole creation in the early Universe.

These monopoles are classical finite energy solutions of the Yang-Mills equations of motion with boundary solutions of $\phi(\theta, \varphi, r = \infty)$ that minimize $V(\phi)$ with a non-trivial mapping of S_2 (i.e. the sphere at infinity) on the remaining symmetry G/H, if H is the little group of the V minima (for a review see Actor, 1979). For the 't Hooft-Polyakov monopole [G = SU(2), H = U(1)] which gives

the monopole-like long distance force,
$$V(\phi) = -\frac{1}{2}m^2\phi^2 + \frac{\lambda}{4}\phi^4$$
 for

self-dual, obviously have $E(n) = nE(1) = n(4\pi/g^2)gD$ [note that for m^2 , $\lambda \neq 0$ 't Hooft found the same E(1) up to a constant $1 \leq C(\lambda/g^2)$ even sufficient yet (see below). annihilation calculated by Preskill (1979) is correct, although not charged monopoles remains (cf. interactions; hopefully the attraction between two most general multi-monopole solutions this seems to imply no proved (Jaffe and Taubes, 1980). The axial $n \ge 2$ solutions, being monopole solutions of arbitrary charge and separations has been and Rossi, 1980). Even more generally the existence of multi equal to 2 (Ward, 1981) and generally $n \ge 1$ (Prasad, 1981; Prasad mapping $S_2 \rightarrow G/H$, which is linked to the magnetic charge g_m solutions with topological charge n (i.e. the homotopy class of the roads to quantization see Jackiw, 1977). These are axisymmetric fixed) in 4-dimensional Minkowski space have been found (for of the classical SU(2) theory with Higgs triplet $(\lambda, m \to 0, m^2/\lambda = D^2)$ nopole, i.e. static, localized, non-singular, finite energy, solutions with the group space vector n_a fixed at $r \to \infty$. Recently multimoand group indices) is not continuously deformable to $\phi_a = n_a m \lambda^{-1/2}$ $+(\cos t/gr) \exp(-2^{1/2}mr)$ $\sim \tilde{r}_a m \lambda^{-1/2}$ (note the mixing of space triplet ϕ_a , a=1,2,3] the asymptotic value at $r\to\infty$ $\phi_a=\tilde{r}_a\{m\lambda^{-1/2}\}$ ≤ 1.787]. If this (for *n* equal, centered charges) also holds for the Manton, 1977), so that differently

calculation of the eventual monopole creation at a phase transition $G \rightarrow G' \times U(1)$, with G and G' simple groups, has not been done yet. all trivial and that a correct gauge invariant (cf. Jackiw, 1980) enormous mass density, invalidating the standard result ⁴He If after the phase transition the distribution of ϕ directions in group space is "random" one expects typically p monopoles per volume l^3 , where $p \sim 0.1$ a combinatorial factor and l the ϕ direction Because $M_{\rm mon} \sim \alpha$ correlation \sim 25%. Before proceeding we remark that the "if" above is not at length, $^{-1}M_X$ and $t(T_c)$ is very small, this leads to an which will be *l*≤2 ct from causality

If we stick to the naive "if" the trick of a 1 PT is to have a larger l at symmetry breaking than in the standard model (Einhorn et al., 1980; Guth and Tye, 1980). There are two possible estimates of the l_{1PT} : a) l_{1PT} as the stretched up particle horizon from the period of supercooling $(T_c - T_{\rm end})$, and b) first as the field correlation length $\xi \sim (2|g)|T^2 - T_{\rm end}^2|^{-1/2}$, but then with limited growth $d\xi/dt \le 1 + \xi'/a \sim 1 + \xi/\tau$ (Einhorn and Sato, 1981). In Sect. 2 we discussed the two alternatives for the transition.

1. Ending by the filling with bubbles if the barrier between false and true vacuum remains. For all bubbles nucleated at T_c (each with independent mean ϕ directions) one might use estimate a) and then $T_{\rm end} < 10^{12}$ GeV and of course a lower $T_{\rm end}$ if there are also smaller bubbles, but anyway estimate b) requires $T_{\rm end} < 10^8$ GeV.

2. If the barrier disappears at T_1 we cannot use a), because there will be a very great number of small bubbles, but again b) requires $T_{\rm end} < 10^8$ GeV. Of course the numberical values (Einhorn and Sato, 1981) of these limits are quite uncertain.

Thus the apparent monopole problem might be alleviated by a strongly first order phase transition ending with smooth reheating, which also guarantees the successes of the Friedmann model of the Universe: baryon number creation and Helium-synthesis.

Note

vations (Steigman, 1976) suggests a clean shaven Universe : $n_B/s \sim +10^{-10}$ everywhere. 5's of Higgs. It is clear that we disfavour Senjanovic and Stecker's (1980) suggestion and, of course, Occam's razor on the obserauthors invoke a period of exponential expansion to stretch the very small domains, each with $n_B/s \sim \pm 10^{-10}$ where the sign of the Gaillard, 1979) and 2. the calculated proton lifetime and SU(2) larger Higgs sector needed 1. $\delta heta_{
m weak}$ perhaps is too large (Ellis and be very smooth. Two further arguments might be that with the perturbative effects. As discussed in the Sect. 2 the reheating has to (Billoire and Tamvakis, 1981), or even less low because of nonpotential (bare mass zero) the cooling goes only (!) to $O(1~{
m GeV})$ Higgs masses are needed whereas for a Coleman-Weinberg required supercooling to T = O(100 eV) very small renormalised (1981)] and assuming supercooling to occur, we note that for the would contain domain walls, Zel'dovich et al. (1974) and Vilenkin values of some Higgses for all energies [otherwise our Universe Apart from the unnaturalness of requiring non-zero expectation breaking is correlated, to at least galaxy cluster sizes (Sato, 1981b) (Senjanovic and Stecker, 1980). To counter the standard objections symmetry breaking, has been evoked to get an overall B=0Soft CP breaking, i.e. complex phases arising in spontaneous -U(1) mixing angle sin θ_W go down and up, respectively, for more Ellis et al., 1980b) of annihilation and separation these

Appendix A: A Model for Baryon Number Creation

All calculations, illustrating baryon number generation after phase transitions, are done for the simple model introduced by Kolb and Wolfram (1980b). First we will summarize the model and the reaction rate equations. After that we will discuss the modifications if we take phase transitions into account.

The model consists of two types of particles: nearly massless particles b and \overline{b} carrying baryon numbers $B=\frac{1}{2}$ and $B=-\frac{1}{2}$ respectively, and massive bosons X and \overline{X} mediating baryon-number violating reactions. The decay amplitudes M of these

massive bosons are parametrized as

$$|M(X \to bb)|^2 = (1+\eta)^{\frac{1}{2}} |M_0|^2,$$

$$|M(X \to b\bar{b})|^2 = (1-\eta)^{\frac{1}{2}} |M_0|^2,$$

$$|M(\bar{X} \to b\bar{b})|^2 = (1+\bar{\eta})^{\frac{1}{2}} |M_0|^2,$$

$$|M(\bar{X} \to b\bar{b})|^2 = (1-\bar{\eta})^{\frac{1}{2}} |M_0|^2,$$
(A1)

with $|M_0|^2$ of the order of a small coupling constant α . Because of unitarity and CPT invariance only two free parameters η , $\bar{\eta}$ are left, where $\eta - \bar{\eta} = O(\alpha)$ measures the amount of CP breaking. Thus a state initially containing an equal number of X and $\bar{X}(n_X^0 = n_X^0)$ will decay, in the absence of back reactions, to a system with a net baryon number $n_B = (\eta - \bar{\eta}) \frac{1}{2} (n_X^0 + n_X^0)$. For simplicity all particles are given only one spin degree of freedom, and obey Maxwell-Boltzmann distributions. Because in the expanding Universe all densities drop quickly, a convenient type of variable is

$$I_A = n_A/n$$

the relative number density of particle $A(=b,\bar{b},X$ or $\bar{X})$ with respect to photons. Finally an "effective Planck mass" M_P is defined as

$$M_P = (\pi/8)^{1/2} G^{-1/2} N^{-1/2} \simeq 7.5 (N)^{-1/2} 10^{18} \text{ GeV},$$

where G is the gravitational constant and N is the number of massless particle species (which is temperature dependent).

The reaction-rate equations gouverning the time evolution of n_b , $n_{\bar{b}}$, $n_{\bar{X}}$, $n_{\bar{X}}$ can be simplified by the choice of a dimensionless "time" parameter $x = M_X/T$, for which

$$\frac{dY_A}{dx} = \frac{x}{M_X x_P} \frac{dY_A}{dt},$$

where $x_P = M_X/M_P$ is a constant. Assuming the b, \bar{b} to undergo many baryon-number conserving reactions $(\gamma b \to \gamma b)$ with the other particles in the Universe, b and \bar{b} must have exactly opposite chemical potentials, leaving only one degree of freedom for

$$Y_B = Y_b - Y_{\bar{b}}$$

since
$$Y_b + Y_{\bar{b}} = 2$$
. Defining

$$Y_{\pm} = \frac{1}{2} (Y_X \pm Y_{\bar{X}})$$

the rate equations read [Kolb and Wolfram, 1980b, Eq. (3.1.2)]:

$$\frac{dY_{+}}{dx} = -A(x) \left[(Y_{+} - Y_{+}^{eq}) + \left(\frac{\eta - \bar{\eta}}{2} \right) Y_{B} Y_{+}^{eq} \right]
\frac{dY_{-}}{dx} = -A(x) \left[Y_{-} - \left(\frac{\eta + \bar{\eta}}{2} \right) Y_{B} Y_{+}^{eq} \right]
\frac{dY_{B}}{dx} = A(x) \left[\left\{ (\eta - \bar{\eta}) (Y_{+} - Y_{+}^{eq}) + (\eta + \bar{\eta}) Y_{-} \right\}
-2 Y_{B} \left\{ Y_{+}^{eq} + \frac{n_{\gamma}}{\langle \Gamma_{x} \rangle} \langle v \left\{ \sigma'(bb \rightarrow b\bar{b}) + \sigma'(b\bar{b} \rightarrow b\bar{b}) \right\} \right\} \right].$$
(A2)

Here A(x) determines the overall reaction rate and is given by

$$A(x) = \frac{x}{x_P} \frac{\langle \Gamma_X \rangle}{M_X}.$$

The relative number density of X, \overline{X} in thermal equilibrium is given by

$$Y_{+}^{eq}(x) = \frac{1}{2}x^2K_2(x)$$

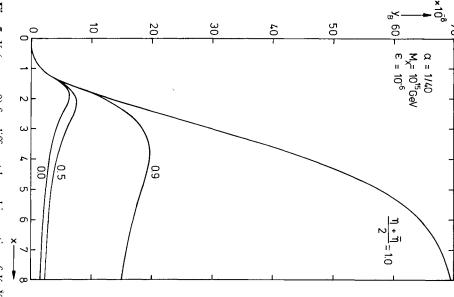


Fig. 5. $Y_B(x; x_0 = 0)$ for different branching ratios of X, X decays (see Appendix A). For $(\eta + \bar{\eta})/2 = 1$ there is a nearly total suppression of the B damping processes

where $K_2(x)$ is the modified Bessel function (using the notation of Gradshteyn and Ryzhik, 1965).

Finally

$$\langle \Gamma_X \rangle = \frac{K_1(x)}{K_2(x)} \Gamma_X = \frac{1}{4} \frac{K_1(x)}{K_2(x)} M_X \alpha$$

and in the low-energy approximation for the cross sections $\sigma'(bb\!\to\!b\bar{b})$ and $\sigma'(b\bar{b}\!\to\!b\bar{b})$

$$\langle v\sigma'\rangle \sim \frac{18\pi\alpha^2 T^2}{M_X^4},$$

$$\frac{n_{\gamma}}{\langle \Gamma_{X} \rangle} \langle v \sigma' \rangle = \frac{72\alpha}{\pi} \cdot \frac{1}{x^{5}} \cdot \frac{K_{2}(x)}{K_{1}(x)}.$$

For a discussion of the approximations made to derive Eqs. (A2),

combination $\varepsilon = \eta - \bar{\eta}$, measuring the amount of CP violation, we use $\varepsilon = 10^{-6}$. These four values, which are reasonable for GUTs as initial conditions and numerical values of the parameters α , η , $\tilde{\eta}$, discussed in Sect. 1, are the same as used by Kolb and Wolfram $M_X = 10^{15}$ GeV, and N = 100, leading to $x_P = 0.00131$. For the see Kolb and Wolfram (1980b).
In order to integrate the three coupled rate Eqs. (A2), we need In all calculations presented in Figs. 2–5 we use $\alpha = 1/40$,

> calculations are insensitive to the value of $\eta + \bar{\eta}$. As can be seen from the X, \bar{X} decay amplitudes (A1), $\eta \sim \bar{\eta} \sim 1$ would imply a strong preference for the decay modes $X \to bb$ and $\bar{X} \to b\bar{b}$, and therefore decays and inverse decays of X, \bar{X} would be inefficient in relaxing for $x \to \infty$ to $Y_B \to 7.04 \ 10^{-7}$.) effective and much more baryon number will be produced. (For $\eta + \bar{\eta} = 2$ the maximum Y_B is reached at x = 12 as $Y_B = 7.05 \cdot 10^{-7}$, the decay channels of X, \overline{X} nearly blocked, damping becomes less insensitive to the precise value. Only just below $\eta + \bar{\eta} = 2$ are half moderate values of $\eta + \bar{\eta}$ between 0 and 1, say, the calculations are very early times: $Y_+ = 1$ and $Y_- = Y_B = 0$ at $x_0 = 0$. As expected, for effect very clearly. Initial conditions used thermal equilibrium at number density to increase monotonically with the absolute value $\eta - \bar{\eta} = \varepsilon = 10^{-6}$, $\eta \sim \bar{\eta}$ and we expect the finally produced baryon would imply a maximal damping of any net baryon number. Since the damping of a net baryon number. On the other hand, $\eta \sim \bar{\eta} \sim 0$ (1980b). However we disagree with their statement that the $|\eta + \bar{\eta}|$. In Fig. 5 are plotted a few sample calculations, showing this

consideration Fig. 5 shows how a sizeable mixing between X, \bar{X} own antiparticle \bar{X} , which implies $Y_{-}=0$. Indeed the second rate Eq. (A2) guarantees $Y_{-}(x)=0$ if $Y_{-}(x_{0})=0$, for $\eta+\bar{\eta}=0$. We are decay channels produces comparable results. and cannot be its own antiparticle, but in the simple model under left with only two equations for Y_+ and Y_B . Of course in realistic well as for $X \to b\bar{b}$ and $\bar{X} \to b\bar{b}$. Therefore X can be taken to be its GUTs X has an electric charge (Nanopoulos and Weinberg, 1979) = 0. This implies equal decay amplitudes for $X \rightarrow bb$ and $\overline{X} \rightarrow bb$, as In all other calculations, except those of Fig. 5, we used $\eta + \bar{\eta}$

X-paricles, Y_+ – generation is proportional to the deviation from equilibrium of the From the last Eq. (A2) it can be seen that baryon number Y_{+}^{eq} . Choosing this as a new variable

$$Y_{{\scriptscriptstyle A}} = Y_+ - Y_+^{eq}$$

we have, with $\eta + \bar{\eta} = 0$, the following two rate equations:

$$\frac{dY_A}{dx} = \frac{1}{2}x^2 K_1(x)
-\frac{\alpha}{4x_P} \left\{ x \frac{K_1(x)}{K_2(x)} Y_A(x) + \frac{1}{4} \varepsilon x^3 K_1(x) Y_B(x) \right\}
\frac{dY_B}{dx} = \frac{\alpha}{4x_P} \left\{ \varepsilon x \frac{K_1(x)}{K_2(x)} Y_A(x) - x^3 K_1(x) Y_B(x)
-\frac{288\alpha}{\pi} x^{-4} Y_B(x) \right\}.$$
(A)

destroys the deviation from equilibrium of the Xs, and is therefore proportional to α/x_p or $\alpha G^{-1/2}$ (G is the gravitational constant): the as a function of temperature only $(T = M_X/x)$. The second term Y_A is nearly completely Y_B -independent, and $Y_A(x; x_0)$ is fixed by specifying the initial condition $Y_A(x_0; x_0)$ independent of Y_B . magnitude of the deviation is governed by a competition between the production of Y_A , independent of already existing Y_A and Y_B . our calculations ($\varepsilon = 10^{-6}$; $Y_B \lesssim \varepsilon$). Therefore the rate equation for typically ten orders of magnitude smaller than the second one in particle reaction rates and Universe expansion. The third term is In the first equation it is clear how the first RHS terms determines

damping of Y_B , by means of all baryon number changing processes, independent of ε , which already indicates that $Y_{B\max} \le \varepsilon$. The first of these two terms describes inverse decays of X, violation parameter ε. the same reaction vs. expansion factor α/x_P , but also the small CP The rate equation for Y_B shows a production term $\propto Y_A$, with The next two terms $\propto Y_B$ determine the

for $x \gg 1$). The last term is the Fermi approximation for $2 \rightarrow 2$ scattering processes $(bb \rightarrow b\overline{b}$, etc.), which is the dominating, but still rather unimportant, term for $x \gtrsim 20$. For high energies this treatment of the $2\rightarrow 2$ processes would be unnecessary in this Therefore we just replaced x^{-4} by 1 for x < 1, since a detailed the previous term (see Kolb and Wolfram, 1980b, Sect. 2.3.2). by the exchange of on-shell intermediate X's is already included in term is unimportant, since the large contribution to $2\rightarrow 2$ scattering $X(bb \rightarrow X, \text{ etc.})$, and drops off quickly for high $x(K_1(x) \propto x^{-1/2}e^{-x}$

effects of an initial baryon number density, as a possible result of the thermalisation after a 1 PT: we choose at the starting value $x_0 = 2$, $Y_A(2) = 0$, and $Y_B(2) = \pm 10^{-7}$. From Fig. 4 it is clear that a direct effect of the steep increase of Y_A , starting from $Y_A = 0$ at $x_0 = 2$, and reaching its maximum value around x = 2.4. Starting from thermal equilibrium, $Y_A(x_0) = Y_B(x_0) = 0$, Fig. 2 shows $Y_B(x; x_0)$ for the values $x_0 = 0, 1, 2, 3$. Figure 3 shows how starting from thermal equilibrium $(Y_B(2)=0)$. Note how the Y_B curve starting at $Y_B=+10^{-7}$ drops to a minimum. The short rise is already at x = 3 the two curves nearly coincide with a third one, number creation, we solved Eq. (A3) for various initial conditions $Y_B(\infty;x_0)$ drops quickly for $x_0 \ge 7$. Finally we investigate the To investigate the effects of phase transitions on baryon

Appendix B: Galaxy Formation

their selfgravity, give the observed structure: galaxies to (super) clusters ($\sim 10^{12}-10^{16}\,M_{\odot}$; cf. Peebles, 1980). This optimism was based on the fact that 1 PT have two valuable ingredients:

1. During the period of supercooling (from t_c to t_{end}) the Several authors (e.g. Guth and Tye, 1980) have suggested that strong first order phase transitions (1 PT) might generate the required small density perturbations that later, after growth by

exponential expansion of the Universe $(a \sim a(t_c) \exp((t-t_c)/\tau))$

greatly enlarges the particle horizon
$$d_H^{1PT} = a(t_{end}) \int_{t_c}^{t_c} dt'/a(t')$$

 $\sim \tau \exp{(t_{\rm end} - t_c)/\tau}$ so that after the instantaneous reheating to T_c at $t_{\rm end}$ the stretched up horizon $d_h^{\rm 1PT}$ can be much larger (roughly by standard problem of the generation of perturbations on a galaxy a factor $T_c/T_{\rm end}$) than in the standard scenario $d_h^{\rm stand}=2\,t_c$, where $\tau\sim T_{Pl}T_c^{-2}$ and $t_c\sim N^{-1/2}\,T_{Pl}T_c^{-2}$. This might (partially) resolve the scale for which $\lambda \gg$ the causally connected region d_h^{stand}

all the released latent energy of the false vacuum is put in the differences [note that for bubbles nucleated by barrier penetration acceleration of the bubble walls; Coleman (1977)]. Nucleation of true vacuum might very well lead to density

Our pessimism is based on the following points:

- production which requires a sufficient thermalisation (causal process) of the bubble wall inhomogeneities. How does this arise naturally, i.e. what determines the precise parameters in the naturally, i.e. what determines the precise parameters in the Lagrangian, which give the required $T_{\rm end}/T_c$ and the nucleation nucleated before the transition $(T \gg T_{end})$. But on the other hand >(a(t)/a(1 s)) 1 s if we want to preserve the homogeneous He the corresponding strong (?) inhomogeneities cannot be on scales a) To profit from the stretching some bubbles must have been
- precise nature of the inhomogeneities formed after thermalisation? Which kind of density enhancements arise from an effective pressure of moving walls? Also gravitational collapse must be interactions? How does thermalisation take place? What is the b) What is the form of the wall-particle and the wall-wall

evaporated by now. avoided, or at least for masses $> 10^{15}$ g, which cannot have

distance between these cavities by L, the smeared out density contrast in a volume L^3 is $\overline{\delta\varrho/\varrho} \sim (\lambda_{\text{bubble}}/L)^3$. On larger scales, optimal case: $(\delta\varrho/\varrho)_{\rm tend} \sim 1$ on a size $\lambda_{\rm bubble} \sim \{a(t_{\rm end})/a(1~{\rm s})\}\,1$ s or $\sim 1~M_{\odot}$ of baryons.—Thermalisation of the false vacuum will true vacuum, which remain nearly empty. Denoting the mean produce a homogeneous energy density outside the rare bubbles of containing N cavities, we have c) Pending the problems mentioned above, let us consider the

$$\overline{\delta\varrho/\varrho} \sim \left(\frac{\lambda_{\text{bubble}}}{L}\right)^3 N^{-1/2}. \tag{B1}$$

 δ_{hor} (galaxy) *could* be made. from the few thermal bubbles giving a $\delta \propto N^{-1/2}$ spectrum. There bubbles; nearly the whole Universe smoothly shifting to the real vacuum at T_1 ($\lesssim 10^8$ GeV?); the cavities remaining after the shift easily be provided by a small thermal nucleation rate at $\sim T_c$ (Guth and Weinberg, 1981). The scenario would be: very few thermal to grow as $\delta \equiv \delta \varrho / \varrho \propto t$, so that to arrive at the required δ_{hor} (galaxy) buted at random (excluded, of course, the interior regions of existing bubbles). We then expect the large scale inhomogeneities fluctuations are made by reshuffling particles, i.e. with energy-momentum conservation (Zel'dovich, 1965), we have here a really statistical exponent -1/2, since the nucleation centers are distrimight thus be a positive ring, because a priori large enough Contrary to the usual exponent -7/6, which arises if density $\sim 10^{-3}$ the bubble density must be very low at $t_{\rm end}$; which can

turbations will be of the adiabatic type. If isothermal perturbations holes) is of the Zel'dovich type; $(\delta\varrho/\varrho)_{horizon} = constant \leqslant 1$. The corresponding small constant metric perturbations (cf. Peebles, scale shear at $T \sim M_X$ (Bond et al., 1981), but the (quantum) epoch of baryon number generation the resulting density perlike to mention an argument in favour of a quantum gravity origin survives phase transition complications. In conclusion we would the required density perturbations for galaxy formation. We are strongly first order phase transitions do not provide naturally gravitational origin of this shear again is an open question are demanded by observations these could be generated from large 1980) are suggestive of a (quantum) gravitational origin. After the turbations on any scale (pro Friedmann, contra primordial black continuous density spectrum which avoids large metric of the density perturbations (cf. Klinkhamer, 1981). The only already happy that the homogeneous AB and 4He production We conclude that, pending new information on GUTs

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