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Article

Basic Validation Procedures for Regression Models in QSAR and QSPR Studies: Theory and Application

Rudolf Kiralj and Márcia M. C. Ferreira*

Laboratory for Theoretical and Applied Chemometrics, Institute of Chemistry, State University of Campinas, P.O. Box 6154, 13083-970 Campinas-SP, Brazil

Quatro conjuntos de dados de QSAR e QSPR foram selecionados da literatura e os modelos de regressão foram construídos com 75, 56, 50 e 15 amostras no conjunto de treinamento. Estes modelos foram validados por meio de validação cruzada excluindo uma amostra de cada vez, validação cruzada excluindo *N* amostras de cada vez (LNO), validação externa, randomização do vetor **y** e validação *bootstrap*. Os resultados das validações mostraram que o tamanho do conjunto de treinamento é o fator principal para o bom desempenho de um modelo, uma vez que este piora para os conjuntos de dados pequenos. Modelos oriundos de conjuntos de dados muito pequenos não podem ser testados em toda a sua extensão. Além disto, eles podem falhar e apresentar comportamento atípico em alguns dos testes de validação (como, por exemplo, correlações espúrias, falta de robustez na reamostragem e na validação cruzada), mesmo tendo apresentado um bom desempenho na validação cruzada excluindo uma amostra, no ajuste e até na validação externa. Uma maneira simples de determinar o valor crítico de *N* em LNO foi introduzida, usando o valor limite de 0,1 para oscilações em Q^2 (faixa de variações em único LNO e dois desvios padrões em LNO múltiplo). Foi mostrado que 10 - 25 ciclos de randomização de **y** ou de *bootstrapping* são suficientes para uma validação típica. O uso do método *bootstrap* baseado na análise de agrupamentos por métodos hierárquicos fornece resultados mais confiáveis e razoáveis do que aqueles baseados somente na randomização do conjunto de dados completo. A qualidade de dados em termos de significância estatística das relações descritor - **y** é o segundo fator mais importante para o desempenho do modelo. Uma seleção de variáveis em que as relações insignificantes não foram eliminadas pode conduzir a situações nas quais elas não serão detectadas durante o processo de validação do modelo, especialmente quando o conjunto de dados for grande.

Four quantitative structure-activity relationships (QSAR) and quantitative structure-property relationship (QSPR) data sets were selected from the literature and used to build regression models with 75, 56, 50 and 15 training samples. The models were validated by leave-one-out crossvalidation, leave-*N*-out crossvalidation (LNO), external validation, **y**-randomization and bootstrapping. Validations have shown that the size of the training sets is the crucial factor in determining model performance, which deteriorates as the data set becomes smaller. Models from very small data sets suffer from the impossibility of being thoroughly validated, failure and atypical behavior in certain validations (chance correlation, lack of robustness to resampling and LNO), regardless of their good performance in leave-one-out crossvalidation, fitting and even in external validation. A simple determination of the critical *N* in LNO has been introduced by using the limit of 0.1 for oscillations in Q^2, quantified as the variation range in single LNO and two standard deviations in multiple LNO. It has been demonstrated that it is sufficient to perform 10 - 25 **y**-randomization and bootstrap runs for a typical model validation. The bootstrap schemes based on hierarchical cluster analysis give more reliable and reasonable results than bootstraps relying only on randomization of the complete data set. Data quality in terms of statistical significance of descriptor - **y** relationships is the second important factor for model performance. Variable selection that does not eliminate insignificant descriptor - **y** relationships may lead to situations in which they are not detected during model validation, especially when dealing with large data sets.

Keywords: leave-one-out crossvalidation, leave-*N*-out crossvalidation, **y**-randomization, external validation, bootstrapping

*e-mail: marcia@iqm.unicamp.br

Introduction

Multivariate regression models in chemistry and other sciences quantitatively relate a response (dependent) variable **y** to a block of predictor variables **X**, in the form of a mathematical equation $\mathbf{y} = f(\mathbf{X})$, where the predictors can be determined experimentally or computationally. Among the best known of such quantitative-**X**-**y** relationships (QXYR) are quantitative structure-activity relationships (QSAR)[1-3] and quantitative structure-property relationships (QSPR),[4,5] in which **y** is a biological response (QSAR) or physical or chemical property (QSPR), and any of the predictors, designated as descriptors, may account for a microscopic (*i.e.*, determined by molecular structure) or a macroscopic property. QSAR has become important in medicinal chemistry, pharmacy, toxicology and environmental science because it deals with bioactive substances such as drugs and toxicants. QSPR has become popular in various branches of chemistry (physical, organic, medicinal, analytical etc.) and materials science. There are many other types of QXYR, some of which represent variants of or are closely related to QSAR or QSPR. It is worth mentioning quantitative structure-retention relationship (QSRR),[6] adsorption-distribution-metabolism-excretion-toxicity (ADMET) relationship,[7] quantitative composition-activity relationship (QCAR),[8] linear free energy relationship (LFER),[9] linear solvent energy relationship (LSER)[10] and quantitative structure-correlations in structural science.[11,12] QXYR are also found in cheminformatics,[13] for example, using *z*-scales or scores of amino-acids or nucleotides as molecular descriptors,[14,15] and in bioinformatics where the primary sequence of nucleic acids, peptides and proteins is frequently understood as the molecular structure for generation of independent variables.[16-18] Other QXYR deal with relationships among various molecular features[19] and parameters of intermolecular interactions[20] in computational and quantum chemistry, and correlate various chemical and physical properties of chemicals in chemical technology.[21,22] In this work, all types of QXYR will be termed as QSAR and QSPR rather than molecular chemometrics[23] because **X** can be a block of macroscopic properties which are not calculated from molecular structure.

Continuous progress of science and technology[24] is the generator for a vast diversity of QSAR and QSPR approaches *via* new mathematical theories, computational algorithms and procedures, and advances in computer technology, where chemometrics is the discipline for merging all these elements. Health problems, search for new materials, and environmental and climate changes give rise to new tasks for QSAR and QSPR, as can be noted in the literature. Mathematical methodologies employed in QSAR and QSPR cover a wide range, from traditional regression methods[25-28] such as multiple linear regression (MLR), principal component regression (PCR) and partial least squares (PLS) regression to more diverse approaches of machine learning methods such as neural networks[29,30] and support vector machines.[31] Modern computer programs are capable of generating hundreds and even thousands of descriptors for **X** and, in specific kinds of problems even variables for **y**, in a very easy and fast way. Time for and costs of testing chemicals in bioassays, and several difficulties in physical and chemical experiments are the reasons for more and more variables being computed instead of being measured. Regression models $\mathbf{y} = f(\mathbf{X})$ are obtained from these descriptors with the purpose of comprehensive prediction of values of **y**. Finally, the statistical reliability of the models is numerically and graphically tested[32-34] in various procedures called by the common name of model validation,[35-38] accompanied by other relevant verifications and model interpretation.[3-5,39]

Even though the terms *validation* and *to validate* are frequent in chemometric articles, these words are rarely explained.[40] Among detailed definitions of *validation* in chemometric textbooks, of special interest is that discussed by Smilde *et al.*,[32] who pointed out that *validation* includes theoretical appropriateness, computational correctness, statistical reliability and explanatory validity. According to Brereton,[41] *to validate* is equivalent to "to answer several questions" on a model's performance, and for Massart *et al.*,[42] *to validate* a model means "to verify that the model selected is the correct one", "to check the assumptions" on which the model has to be based, and "to meet defined standards of quality". *Validation* for Snee[43] is a set of "methods to determine the validity of regression models."

The purpose of this work is to present, discuss and give some practical variants of five validation procedures which are still not-so-commonly used[44] in QSAR and QSPR works: leave-one-out crossvalidation, leave-*N*-out crossvalidation, **y**-randomization, bootstrapping (least known among the five) and external validation.[23,38,40,44-46] This statistical validation is the minimum recommended as standard in QSAR and QSPR studies for ensuring reliability, quality and effectiveness of the regression models for practical purposes. Unlike instrumental data generated by a spectrometer, where a huge set of predictors of the same nature (intensities, in general of the same order of magnitude) are highly correlated among themselves and to the dependent variable (analyte concentration) *via* a known physical law (Beer's law), QSAR and QSPR data are more complex and obscure. In QSAR and QSPR studies, the descriptors are of different natures and orders

of magnitude and, therefore careful variable selection and rigorous model validation are crucial.

Five Basic Validation Procedures

The basic statistical parameters, such as root mean square errors (standard deviations), "squared form" correlation coefficients which are regularly used in QSAR and QSPR, and the respective Pearson correlation coefficients that can be also found in several studies, are described in detail in Table 1.

The purpose of validation is to provide a statistically reliable model with selected descriptors as a consequence of the cause-effect and not only of pure numerical relationship obtained by chance. Since statistics can never replace chemistry, non-statistical validations (chemical validations[5]) such as verification of the model in terms of the known mechanism of action or other chemical knowledge, are also necessary. This step becomes crucial for those cases where no mechanism of action is known and also for small and problematic data sets, when some statistical tests are not applicable but the mechanism of action of compounds is well known so that the selected descriptors may be justified *a priori*.

Requirements for the structure of data sets

Statistical validation of the final model should start with all samples in random order and a ready and "clean" data set, *i.e.*, where variable selection has been already performed and outliers removed. Randomness is important since a user-defined samples' order frequently affects the validation, because regularly increasing or decreasing values of variables may be correlated to the position of samples within the set or its blocks (subsets). The structure of such data sets can be characterized by their size, data set split, statistical distribution of all descriptors and the dependent variable, and structural diversity of samples.

From the statistical point of view, small data sets, *i.e.* data sets with a small number of samples, may suffer from various deficiencies like chance correlation, poor regression statistics and inadequacy for carrying out various statistical tests as well as unwanted behavior in performed tests. Any of those may lead to false conclusions in model interpretation and to spurious proposals for the mechanism of action of the studied compounds. Working with small data sets is delicate and even questionable, and it should be avoided whenever possible.

The number of predictor variables (descriptors) also defines the data size. It is generally accepted that there must be at least five samples per descriptor (Topliss ratio) for a simple method as MLR.[38,44] However, PCR and PLS allow using more descriptors, but too many descriptors may cause difficulties in model interpretability. Besides, using several factors (principal components or latent variables) can make model interpretation tedious and lead to a problem similar to that just mentioned about MLR (using too many factors means low compression of original descriptors).

Data set split is another very important item which strongly depends on the size of the whole set and the nature and aim of the study. In an ideal case, the complete data set is split into a training (learning) set used for building the model, and an external validation set (also called test or prediction set) which is employed to test the predictive power of the model. The external validation set should be distinguished from a data set additionally created only to make predictions. This data set, which is sometimes also called prediction set, is blind with respect to eventual absence of dependent variable and has never participated in any modeling step, including variable selection and outlier detection. In cases of small data sets and for special purposes, it is necessary to build first the model with all samples and, *a posteriori*, construct an analogous one based on the split data. In this article, the former and latter models are denominated as the real and auxiliary models, respectively. The aim of the auxiliary model is to carry out validations that are not applicable for the real model (external validation and bootstrapping). Since the auxiliary model has fewer samples than the real, it is expected that its statistics should be improved if the validations were performed on the real model.

It is expected that variables in QSAR and QSPR models follow some defined statistical distribution, most commonly the normal distribution. Moreover, descriptors and the dependent variable should cover sufficiently wide ranges of values, the size of which strongly depends on the nature of the study. From our experience, biological activities expressed as molar concentrations should vary at least two orders of magnitude. Statistical distribution profile of dependent and independent variables can easily be observed in simple histograms which are powerful tools for detection of badly constructed data sets. Examples include histograms with too large gaps, poorly populated or even empty regions, as well as highly populated narrow intervals. Such scenarios are an indication that the studied compounds, in terms of molecular structures, were not sufficiently diverse, *i.e.*, on the one hand, one or more groups of compounds are characterized by small structural differences and on the other hand, there are structurally specific and unique molecules. A special case of such a molecular set is a degenerate (redundant in samples) set,[37] containing several enantiomers, close structural isomers

Table 1. Basic statistical parameters for regression models in QSAR and QSPR

Parameter	Definition[a]
Number of samples (training set or external validation set)	M
Number of factors (LVs or PCs) or original descriptors	k
Root mean square error of crossvalidation (training set)	$\mathrm{RMSECV} = \sqrt{\sum_i \frac{(y_{ei} - y_{vi})^2}{M}}$
Root mean square error of calibration (training set)	$\mathrm{RMSEC} = \sqrt{\sum_i \frac{(y_{ei} - y_{ci})^2}{M - k - 1}}$
Root mean square error of prediction (external validation set)	$\mathrm{RMSEP} = \sqrt{\sum_i \frac{(y_{ei} - y_{pi})^2}{M}}$
Crossvalidated correlation coefficient[b] (training set)	$Q^2 = 1 - \frac{\sum_i (y_{ei} - y_{vi})^2}{\sum_i (y_{ei} - \langle y_e \rangle)^2}$
Correlation coefficient of multiple determination[c] (training set)	$R^2 = 1 - \frac{\sum_i (y_{ei} - y_{ci})^2}{\sum_i (y_{ei} - \langle y_e \rangle)^2}$
Correlation coefficient of multiple determination[c] (external validation set)	$R^2_{\mathrm{ext}} = 1 - \frac{\sum_i (y_{ei} - y_{pi})^2}{\sum_i (y_{ei} - \langle y_e \rangle)^2}$
Correlation coefficient of external validation[d,e] (external validation set)	$Q^2_{\mathrm{ext}} = 1 - \frac{\sum_i (y_{ei} - y_{ci})^2}{\sum_i (y_{ei} - w)^2}$
Pearson correlation coefficient of validation (training set)	$Q = \frac{\sum_i (y_{ei} - \langle y_e \rangle)(y_{vi} - \langle y_v \rangle)}{\sqrt{\sum_i (y_{ei} - \langle y_e \rangle)^2} \sqrt{\sum_i (y_{vi} - \langle y_v \rangle)^2}}$
Pearson correlation coefficient of calibration (training set)	$R = \frac{\sum_i (y_{ei} - \langle y_e \rangle)(y_{ci} - \langle y_c \rangle)}{\sqrt{\sum_i (y_{ei} - \langle y_e \rangle)^2} \sqrt{\sum_i (y_{ci} - \langle y_c \rangle)^2}}$
Pearson correlation coefficient of prediction (external validation set)	$R_{\mathrm{ext}} = \frac{\sum_i (y_{ei} - \langle y_e \rangle)(y_{pi} - \langle y_p \rangle)}{\sqrt{\sum_i (y_{ei} - \langle y_e \rangle)^2} \sqrt{\sum_i (y_{pi} - \langle y_p \rangle)^2}}$

[a]Basic definitions: i - the summation index and also the index of the i-th sample; y_e - experimental values of **y**; y_c - calculated values of **y**, *i.e.*, values from calibration; y_p - predicted values of **y**, *i.e.*, values from the external validation set; y_v - calculated values of **y** from an internal validation (LOO, LNO or **y**-randomization) or bootstrapping; $\langle y_e \rangle$, $\langle y_c \rangle$ and $\langle y_v \rangle$ - average value of y_e, y_c and y_v, respectively.
[b]Also known as (LOO or LNO) crossvalidated correlation coefficient, explained variance in prediction, (LOO or LNO) crossvalidated explained variance, and explained variance by LOO or by LNO. The attributes LOO and LNO are frequently omitted in names for this correlation coefficient.
[c]Also known as coefficient of multiple determination, multiple correlation coefficient and explained variance in fitting.
[d]Also known as external explained variance.
[e]The value $w = \langle y_e \rangle$ is the average for experimental values of **y** calculated for the training set and not for the external validation set.

and very similar molecules. These samples will probably have very similar or equal values of molecular descriptors and of the dependent variable, which can contribute to poor model performance in some validation procedures. This is the reason why degenerate samples should be avoided whenever possible. Furthermore, a data set may contain descriptors that have only a few distinct numerical values (two or three), which is not always a consequence of degenerate samples. These descriptors behave as qualitative variables and should be also avoided, to reduce data degeneracy (variable redundancy). For this purpose, two cases should be distinguished. The first is of so-called

indicator variables,[47,48] which, by their definition, possess only a few distinct values. The very few values of indicator variables should have approximately equal frequency; this way, model validation should always yield reasonable results. The second accounts for other types of descriptors, which, according to their meaning, should contain several distinct numerical values (integers or real numbers), but because of problem definition, computational difficulties, lack of sufficient experimental data, etc., become highly degenerate. When this occurs, one should replace these descriptors by others, or even consider redefining the problem under study.

Leave-one-out crossvalidation

Leave-one-out (LOO) crossvalidation is one of the simplest procedures and a cornerstone for model validation. It consists of excluding each sample once, constructing a new model without this sample (new factors or latent variables are defined), and predicting the value of its dependent variable, y_c. Therefore, for a training set of M samples, LOO is carried out M times for one, two, three, etc. factors in the model, resulting in M predicted values for each number of factors. The residuals, y_c - y_e (differences between experimental and estimated values from the model) are used to calculate the root mean square error of crossvalidation (RMSECV) and the correlation coefficient of leave-one-out crossvalidation (Q^2), as indicated in Table 1.

The prediction statistics of the final model are expressed by the root mean square error of calibration (RMSEC) and the correlation coefficient of multiple determination (R^2), calculated for the training set. Since LOO represents certain perturbations to the model and data size reduction, the corresponding statistics are always characterized by the relations $R^2 > Q^2$ and RMSEC < RMSECV. The minimum acceptable statistics for regression models in QSAR and QSPR include conditions $Q^2 > 0.5$ and $R^2 > 0.6$.[44,49] A large difference between R^2 and Q^2, exceeding 0.2 - 0.3, is a clear indication that the model suffers from overfitting.[38,46]

Leave-N-out crossvalidation

Leave-*N*-out (LNO) crossvalidation,[45,50,51] known also as leave-many-out, is highly recommended to test the robustness of a model. The training set of M samples is divided into consecutive blocks of N samples, where the first N define the first block, the following N samples is the second block, and so on. This way, the number of blocks is the integer of the ratio M/N if M is a multiple of N; otherwise the left out samples usually make the last block. This test is based on the same basic principles as LOO: each block is excluded once, a new model is built without it, and the values of the dependent variable are predicted for the block in question. LNO is performed for N = 2, 3, etc., and the leave-N-out crossvalidated correlation coefficients Q^2_{LNO} are calculated in the same way as for LOO (Table 1). LNO can be performed in two modes: keeping the same number of factors for each value of N (determined by LOO for the real model) or with the optimum number of factors determined by each model.

Contrary to LOO, LNO is sensitive to the order of samples in the data set. For example, leave-two-out crossvalidation for even M means that $M/2$ models are obtained, but this is only a small fraction $(0.5\cdot(M-1)^{-1})$ of all possible combinations of two samples $M!/(M-2)! = M(M-1)$. To avoid any systematic variation of descriptors through a data set or some subset what would affect LNO, the samples should be randomly ordered (in **X** and **y** simultaneously).

It is recommended that N represents a significant fraction of samples (like leave-20 to 30% - out for smaller data sets[40]). It has been shown recently[52] that repeating the LNO test for scrambled data and using average of Q^2_{LNO} with its standard deviation for each N, is statistically more reliable than LNO being performed only once. This multiple LNO test can be also performed in the two modes, with fixed or optimum number of factors. The critical N is the maximum value of N at which Q^2_{LNO} is still stable and high. It is primarily determined by the size of a data set and somewhat less by its quality. For a good model, Q^2_{LNO} should stay close to Q^2 from LOO, with small variations at all values for N up to the critical N. For single LNO, these variations can be quantified in the following way. Variations for single LNO are expressed as the range of Q^2_{LNO} values, which shows how much Q^2_{LNO} oscillates around its average value. By our experience, this range for single LNO should not exceed 0.1. In case of multiple LNO, a more rigorous criterion should be used, where two standard deviations should not be greater than 0.1 for N = 2, 3, etc., including the critical value of N.

***y*-Randomization**

The purpose of the **y**-randomization test[45,46,50,53,54] is to detect and quantify chance correlations between the dependent variable and descriptors. In this context, the term chance correlation means that the real model may contain descriptors which are statistically well correlated to **y** but in reality there is no cause-effect relationship encoded in the respective correlations with **y** because they are not related to the mechanism of action. The **y**-randomization test

consists of several runs for which the original descriptors matrix **X** is kept fixed, and only the vector **y** is randomized (scrambled). The models obtained under such conditions should be of poor quality and without real meaning. One should be aware that the number of factors is kept the same as for the real model, since **y**-randomization is not based on any parameter optimization. The basic LOO statistics of the randomized models (Q^2_{yrand} and R^2_{yrand}) should be poor, otherwise, each resulting model may be based on pure numerical effects.

Two main questions can be raised regarding **y**-randomization: how to analyze the results from each randomization run and how many runs should be carred out? There are various approaches to judge whether the real model is characterized by chance correlation. The simple approach of Eriksson and Wold[53] can be summarized as a set of decision inequalities based on the values of Q^2_{yrand} and R^2_{yrand} and their relationship $R^2_{yrand} > Q^2_{yrand}$:

$Q^2_{yrand} < 0.2$ and $R^2_{yrand} < 0.2 \rightarrow$ no chance correlation;
any Q^2_{yrand} and $0.2 < R^2_{yrand} < 0.3 \rightarrow$ negligible chance correlation;
any Q^2_{yrand} and $0.3 < R^2_{yrand} < 0.4 \rightarrow$ tolerable chance correlation;
any Q^2_{yrand} and $R^2_{yrand} > 0.4 \rightarrow$ recognized chance correlation.

Therefore, the correlation's frequency is counted as the number of randomizations which resulted in models with spurious correlations (falsely good), which is easily visible in a Q^2_{yrand} against R^2_{yrand} plot that also includes Q^2 and R^2 values for the real model.

In another approach,[54] the smallest distance between the real model and all randomized models in units of Q^2 or R^2 is identified. This minimum distance is then expressed relative to the respective standard deviation for the randomization runs. The distinction of the real model from randomized models is judged in terms of an adequate confidence level for the normal distribution. A simple procedure proposed in the present work, is to count randomized models which are statistically not distinguished from the real model (confidence levels are greater than 0.0001).

There is another approach to quantify chance correlation in the literature,[46] based on the absolute value of the Pearson correlation coefficient, *r*, between the original vector **y** and randomized vectors **y**. Two **y** randomization plots r - Q^2_{yrand} and r - R^2_{yrand} are drawn for randomized and real models, and the linear regression lines are obtained:

$$Q^2_{yrand} = a_Q + b_Q r \quad (1)$$
$$R^2_{yrand} = a_R + b_R r \quad (2)$$

The real model is characterized as free of chance correlation when the intercepts are $a_Q < 0.05$ and $a_R < 0.3$. These intercepts are measures for the background chance correlation, *i.e.*, intrinsic chance correlation encoded in **X**, which is visible when statistical effects of randomizing the **y** vector are eliminated, *i.e.*, the correlation between original and randomized **y** vectors is equal to zero ($r = 0$).

The number of randomized models encoding chance correlation depends primarily on two statistical factors. It strongly increases with the decrease of the number of samples in the training set, and is increased moderately for large number of randomization runs.[54] Chemical factors, such as the nature of the samples and their structural similarity, data quality, distribution profile of each variable and variable intercorrelations, modify to a certain extent these statistical dependences. The approach of Wold and Eriksson[53] consists of ten randomization runs for any data set size. This is a sufficiently sensitive test because models based on chance correlation easily fail in one or more (*i.e.*, at least 10%) randomization runs. Several authors propose hundreds or thousands of randomizations independent of the data set size, while others argue that the number of randomizations should depend on the data size. The authors of this work have shown recently[55] that 10 and 1000 randomization runs provide the same qualitative information and, moreover, that the statistics for these two approaches are not clearly distinguished when the linear relationships (**1**) and (**2**) and that one between Q^2_{yrand} and R^2_{yrand} are inspected. Accordingly, it is expected that poor models will show unwanted performance in **y**-randomization, while good models will be free from chance correlation even for a small number of randomizations, as will be shown by the examples in this work.

Bootstrapping

Bootstrapping[56,57] is a kind of validation in which the complete data set is randomly split several times into training and test sets, the respective models are built and their basic LOO statistics (Q^2_{bstr} and R^2_{bstr}) are calculated and compared to that of the real model. Unlike validations (LOO and LNO) where each sample is excluded only once, in bootstraping a sample may be excluded once, or several times, as well as never. Since in each bootstrap run a new model is built, it is expected that the values of Q^2_{bstr} and R^2_{bstr} satisfy the minimum acceptable LOO statistics in all bootstrap runs, and that they oscillate around the real Q^2 and R^2 (the LOO statistics of the real model) within reasonable ranges. The aim of bootstrapping is to perturb the training set, whilst statistics of the test set are not considered.

There are two issues to be considered when performing this validation. One is the procedure for making the bootstrappings *i.e.*, data splits or resamplings, and the other is their number. Different number of splits have been proposed in the literature, ranging from low (ten) to high (hundreds). By its basic conception, bootstrapping does not require that the data split is based on high structural similarity between the training and test sets. The literature proposes random selection of samples for the training set by means of algorithms frequently coupled to various statistical procedures and also a rational split based on data subsets (clusters) in hierarchical cluster analysis (HCA).[25,28] The size of the complete data set is the main factor that influences bootstrap procedures. In general, a small data set is difficult to split and exclusion of significant portion of its samples may seriously harm the model's performance. Exclusion of about 30% of samples from the complete set is a reasonable quantity for smaller sets[40] consisting of a few clusters of samples, some of which are poorly populated. Therefore, purely random procedures that do not take into account the structure and population of the clusters may produce unrealistically good or poor models in particular bootstrap runs. Random sampling within each HCA cluster, or within other types of clusters as, for example, obtained from **y** distribution (low, moderate and highly active compounds), better reflects the chemical structure of the complete data set. In large data sets, highly populated clusters will be always well represented in any random split, making clear why such sets are practically insensitive to exclusion of a significant portion of samples (more than 50%), independent of the type of random split employed.

External validation

Unlike bootstrapping, the external validation test requires only one split of the complete data set into structurally similar training and external validation sets. The purpose of this validation is to test the predictive power of the model. Basic statistical parameters that are used to judge the external validation performance (Table 1) are the root mean square error of prediction (RMSEP), the correlation coefficient of external validation (Q^2_{ext}) and the Pearson correlation coefficient of prediction (R_{ext}). Q^2_{ext} quantifies the validation and is analogous to Q^2 from LOO, with exception of the term w (see Table 1), which is the average value of the dependent variable **y** for the training set and not the external validation set. R_{ext} is a measure of fitting for the external validation set and can be compared to R for the training set.

When performing external validation, two issues have to be dealt with. One is the number of samples in the external validation set and the other is the procedure for selecting them. It is recommended to use 30% of samples for the external validation of smaller data sets[40] and to keep the same percentage of external samples in bootstrapping and external validation.[43] There are various procedures for selecting external samples. All of them have to provide chemical analogy between the training and external samples, structural proximity between the two data sets (similar variable ranges and variable distributions as a consequence of similar molecular diversities), and to provide external predictions as interpolation and not extrapolation. A reasonable approach for splitting the complete data set, which takes all these items into account is to use HCA combined with principal component analysis (PCA)[25,28] scores, **y** distribution (*e.g.*, low, moderate and high biological activity) and other sample classification.

Methods

Data sets

Four data sets of different dimensions were selected from the literature.[5,39,53-55] Basic information about them, including splits adopted and validations performed in this work, are presented in Table 2. The complete data sets are in Supplementary Information (Tables T1-T4). The new splits performed in this work were based on exploratory analysis of autoscaled complete data sets, always using clusters from HCA with complete linkage method,[25] combined with PCA, **y** distribution and some sample classification known *a priori*. The regression models, MLR and PLS, were built using data previously randomized and autoscaled.

The QSAR data set 1 comprises five molecular descriptors and toxicity, -log[IGC_{50}/(mol L^{-1})], against a ciliate *T. pyriformis* for 153 polar narcotics (phenols). This data set was originally defined by Aptula *et al.*,[58] and it was used for the first time to build a MLR model by Yao *et al.*[59] who also made a modest data split (14% samples out for the external validation). In this work, the real MLR model is based on a rather radical split (51% out) in order to show that even data sets of moderate size can enable good splitting and model performance in all validations.

The data set 2 is from a quantitative genome/structure-activity relationship (QGSAR) study,[39] a hybrid of QSAR and bioinformatics, in which the resistance of 24 strains of the phytopathogenic fungus *P. digitatum* against four demethylation inhibitors was investigated by PLS models. This data set consists of toxicity values -log[EC_{50}/(mol L^{-1})] for 86 samples, described by eight descriptors, from which three are fungal genome descriptors and five are products

Table 2. Data sets used, real and auxiliary regression models built and corresponding validations carried out in this work

Data set[a]	Type[b]	References	Real model[c,d,e]	Auxiliary model[c,d,e]
1: **X**(153×5)	QSAR [MLR]	Ref. 58, 59	75 (tr) + 78 (ev), 51% out: LOO, LNO, YRD, BSR, EXTV	-
2: **X**(86×8)	QGSAR [PLS]	Ref. 39	56 (tr) + 30 (ev), 35% out: LOO, LNO, YRD, BSR, EXTV	-
3: **X**(50×8)	QSPR [PLS]	Ref. 5	50 (tr) + 0: LOO, LNO, YRD	40 (tr) + 10 (ev), 20% out: LOO, BSR, EXTV
4: **X**(15×3)	QSAR [MLR]	Ref. 60	15 (tr) + 0: LOO, LNO, YRD	13 (tr) + 2 (ev), 13% out: LOO, (BSR), (EXTV)

[a]Data sets 1-4 with respective dimensions of the descriptors matrix **X** for the complete data set.
[b]Types of study in which the data sets were originated: quantitative structure-activity relationship (QSAR), quantitative genome/structure-activity relationship (QGSAR) (a combination of QSAR and bioinformatics) and quantitative structure-property relationship (QSPR). Regression models in these studies are multiple linear regression (MLR) and partial least squares regression (PLS).
[c]The real model is the model of main interest in a study, built for practical purposes. The auxiliary model is the model with a smaller number of samples than the real model, used to perform external validation and bootstrapping.
[d]Data split: the number of samples in the training set (tr) + the number of samples in the external validation set (ev), and the percentage (%) of samples excluded from building the model but used for external validation and bootstrapping.
[e]Validations: leave-one-out cross-validation (LOO), leave-*N*-out cross-validation (LNO), **y**-randomization (YRD), bootstrapping (BSR), and external validation (EXTV). Abbreviations in parenthesis (BSR) and (EXTV) mean that due to very a small number of samples, validations were performed in a very limited way.

of some molecular and genome features. The reader may look at the original work[39] for the definition of the matrix **X**. A new data split was applied in this work (35% out), which is more demanding than in the original publication. The purpose of this example is to show that even modest data sets can be successfully validated without using an auxiliary regression model.

The data set 3 is from a QSPR study on the carbonyl oxygen chemical shift (^{18}O) in 50 substituted benzaldehydes,[5] comprising eight molecular descriptors and the shifts δ/ppm. Two literature PLS models, the real and the auxiliary model (20% out), are inspected in more details with respect to the validations carried out, especially bootstrapping.

The smallest data set 4 is from a series of QSAR studies based on MLR models,[60] and it was used to predict mouse cyclooxigenase-2 inhibition by 2-CF_3-4-(4-SO_2Me-phenyl)-5-(X-phenyl)-imidazoles. It consists of three molecular descriptors and the anti-inflammatory activity -log[IC_{50}/molL^{-1}] for 15 compounds. Only a very modest split (13% out) could be applied in this example, to show that very small data sets cannot provide reliable statistics in all the applied validations.

All chemometric analyses were carried out by using the software Pirouette® [61] and MATLAB®.[62]

Validations

Samples in all data sets were randomized prior to any validation. All single and multiple (10 times) leave-*N*-out (LNO) cross-validations were carried out by determining the optimum number of factors for each *N* when using PLS. For each data set, 10 and 25 randomizations were tested, to show the effect of the number of runs on chance correlation statistics. The same data split was used in external validation and bootstrapping, as suggested in the literature,[43] to allow comparison between the respective statistics. At least two different bootstrap split schemes were applied for each data set, where the randomized selection of the training samples was made from the complete set, from subsets (clusters) in HCA, and other types of subsets (PCA clusters, **y** distribution, or some other sample classification). To demonstrate the effect of the number of resamplings on bootstrap statistics, 10 and 25 runs were carried out for each split scheme.

Inspection of data quality versus data set size

Data set size is the primary but not the sole factor that affects model performance. To evaluate how much the data quality, *i.e.*, descriptors and their correlations with **y**, affect the model performance, the following investigations were carried out. First, data sets 1, 2 and 3 were reduced to the size of data set 4 (15 samples) according to the following principles: a) all descriptors possessed at least three distinct values; b) samples were selected throughout the whole range of **y**; c) very influential samples were avoided; and d) one or more samples were selected from each HCA cluster already defined in bootstrapping, proportionally to cluster size. Eventually formed subsets were subject to all validations in the very same way as data set 4. Second, the relationships between descriptors and **y** were inspected for all data sets and subsets in the form of the linear regression

equation $\mathbf{y} = a + b\,\mathbf{x}$, and the following statistical parameters were calculated by using MATLAB® and QuickCalcs[63] software: statistical errors for a (σ_a) and b (σ_b), respective t-test parameters (t_a and t_b), Pearson correlation coefficient between a descriptor and **y** (R), explained fitted variance (R^2), F-ratio (F), and normal confidence levels for parameters t_a, t_b and F. This way, the interplay between data set size and quality could be rationalized and the importance of variable selection discussed.

Results and Discussion

Data set 1: QSAR modeling of phenol toxicity to ciliate T. pyriformis

Yao *et al.*[59] have explored the complete data set of 153 phenol toxicants by building a MLR model (reported: $R = 0.911$ and RMSECV = 0.352; calculated in the present work: $Q^2 = 0.805$, $R^2 = 0.830$, RMSEC = 0.335 and $Q = 0.897$), and also another MLR model with 131 training samples (reported: $R = 0.924$ and RMSEC = 0.309; calculated in this work: $Q^2 = 0.827$, $R^2 = 0.854$, RMSECV = 0.328, $Q = 0.910$, $Q^2_{ext} = 0.702$, $R^2_{ext} = 0.696$, RMSEP = 0.459 and $R_{ext} = 0.835$). This set is larger than those commonly used in QSAR studies and, therefore, various statistical tests could be performed. This was the reason to make a rather radical split into 75 and 78 compounds for the training and external validation sets (51% out), based on HCA analysis (dendrogram not shown). The LOO ($Q^2 = 0.773$, $R^2 = 0.830$, RMSECV = 0.403, RMSEC = 0.363, $Q = 0.880$ and $R = 0.911$) and external validation statistics ($Q^2_{ext} = 0.824$, $R^2_{ext} = 0.824$, RMSEP = 0.313 and $R_{ext} = 0.911$) obtained were satisfactory. To test the self-consistency of the data split, the training and external validation sets were exchanged and a second model with 78 training samples was obtained. Its LOO ($Q^2 = 0.780$, $R^2 = 0.838$, RMSECV = 0.349, RMSEC = 0.313, $Q = 0.884$ and $R = 0.915$) and external statistics ($Q^2_{ext} = 0.817$, $R^2_{ext} = 0.817$, RMSEP = 0.362 and $R_{ext} = 0.908$), were comparable to that of the first model. Results from other validations of the real MLR model are shown in Table 3, Figures 1-3 and Supplementary Information (Tables T5-T9 and Figures F1 and F2).

Among the validations performed for the real model (Table 2), the single LNO statistics shows an extraordinary behavior, with critical $N = 37$ (49% out), because the values of Q^2_{LNO} stay high (Figure 1) and do not oscillate significantly around the average value (Table T5) even at high N. Multiple LNO shows slow but continuous decrease of average Q^2_{LNO} and irregular increase of the respective standard deviations along N, so that up to $N = 17$ (23% out) two standard deviations ($\pm\sigma$) are not greater than 0.1. (Table T5). In other words, the training set with 75 training toxicants is rather stable, robust to exclusion of large blocks (between 17 and 37 inhibitors), and the data split applied is effective.

Three bootstrap schemes for 10 and 25 runs were applied (Tables T6 and T7) to form training sets: by random selection of 75 toxicants from the complete data set, from HCA clusters (10 clusters at the similarity index of 0.60), and from PCA groups (plot not shown). In fact,

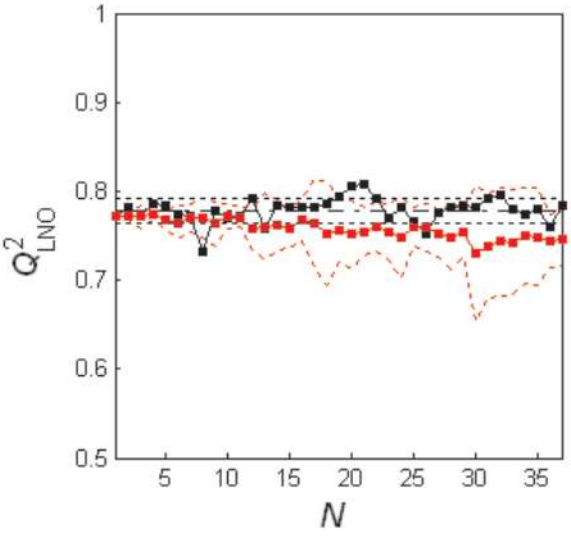

Figure 1. Leave-*N*-out crossvalidation plot for the MLR model on data set 1. Black - single LNO, red - multiple LNO (10 times). Single LNO: average Q^2 - dot-dash line, one standard deviation below and above the average - dotted lines. Multiple LNO: one standard deviation below and above the average - red dotted curved lines.

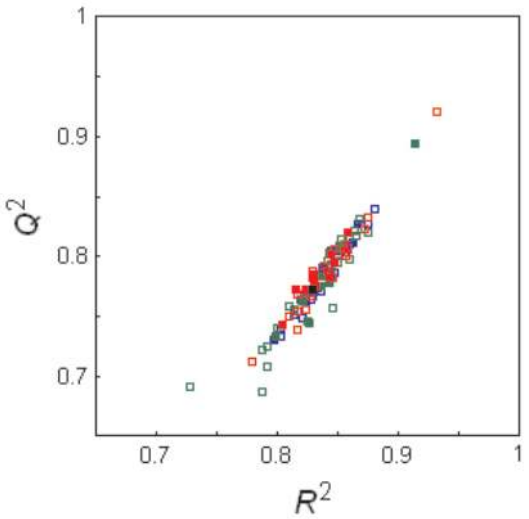

Figure 2. A comparative plot for bootstrapping of the MLR model on data set 1: the real model (black square), models from HCA-based bootstrapping (blue squares: 10 iterations - solid, 25 iterations - open), models from PCA-based bootstrapping (green squares: 10 iterations - solid, 25 iterations - open), and models from simple bootstrapping (red squares: 10 iterations - solid, 25 iterations - open).

three PCA groups were detected in the scores plot, based on three distinct values of descriptor N_{hdon} (see Table T1). Classes of **y** were not applied since no gaps in the statistical distribution of **y** had been noticed. The graphical presentation of the results (Figure 2) shows that the data points are well concentrated along a R^2 - Q^2 diagonal, with negligible dispersion in the region defined by $R^2 < 0.85$ and $Q^2 < 0.80$. The real model (the black point) is placed in the middle of the bootstrap points. Careful comparison of the three bootstrap schemes indicates that HCA-based bootstrapping has certain advantages over the other two schemes. It is less dispersed and more symmetrically distributed around the real model. This would be expected, since each bootstrap training set originating from the HCA contains toxicants that represent well the complete data set in terms of molecular structure and descriptors.

The real MLR model shows excellent performance in **y**-randomization with 10 and 25 runs (Tables T8 and T9). There are no randomized models in the proximity of the real model in the Q^2 - R^2 plot (Figure 3) since they are all concentrated at $Q^2 < 0$ and $R^2 < 0.2$. A significantly larger number of randomization runs should be applied to get some randomized models approaching the real model. This example illustrates how many randomized runs are necessary to detect a model free of chance correlation: the choice of 10 or even 25 runs seems reasonable, which agrees with the method of Eriksson and Wold.[53] When the Q^2 - r and R^2 - r plots are analyzed (Figures F1 and F2), it can be seen that the randomized models are placed around small values of r so that the intercepts of the linear

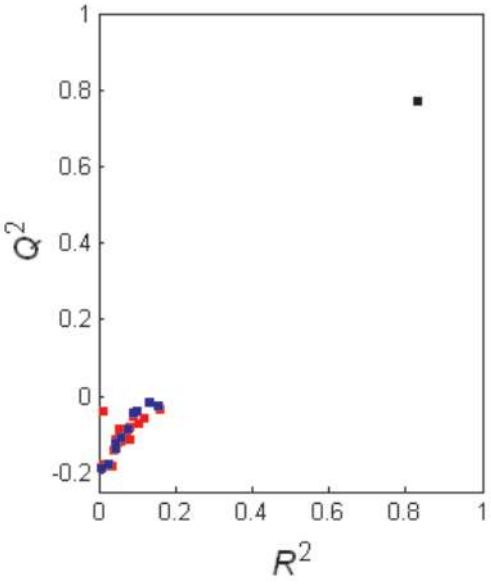

Figure 3. The **y**-randomization plot for the MLR model on data set 1: black ball - the real model, blue balls - 10 randomized models, red balls - 25 randomized models.

Table 3. Comparative statistics of 10 and 25 **y**-randomizations of the MLR model on data set 1

Parameter[a]	10 iterations	25 iterations
Maximum (Q^2_{yrand})	-0.017	-0.017
Maximum (R^2_{yrand})	0.157	0.182
Standard deviation (Q^2_{yrand})	0.062	0.048
Standard deviation (R^2_{yrand})	0.047	0.046
Minimum model-random. Diff. (Q^2_{yrand})[b]	12.67	16.48
Minimum model-random. Diff. (R^2_{yrand})[b]	14.30	14.25
Confidence level for min. diff. (Q^2_{yrand})[c]	<0.0001	<0.0001
Confidence level for min. diff. (R^2_{yrand})[c]	<0.0001	<0.0001
Randomizations %, conf. level > 0.0001 (Q^2_{yrand})[d]	0	0
Randomizations %, conf. level > 0.0001 (R^2_{yrand})[d]	0	0
y-Randomization intercept (r_{yrand} *vs.* Q^2_{yrand})[e]	–0.191	–0.176
y-Randomization intercept (r_{yrand} *vs.* R^2_{yrand})[e]	–0.012	0.003

[a]Statistical parameters are calculated for Q^2 from **y**-randomization (Q^2_{yrand}) and R^2 from **y**-randomization (R^2_{yrand}).
[b]Minimum model-randomizations difference: the difference between the real model (Table 1) and the best **y**-randomization in terms of correlation coefficients Q^2_{yrand} or R^2_{yrand}, expressed in units of the standard deviations of Q^2_{yrand} or R^2_{yrand}, respectively. The best **y**-randomization is defined by the highest Q^2_{rand} or R^2_{rand}.
[c]Confidence level for normal distribution of the minimum difference between the real and randomized models.
[d]Percentage of randomizations characterized by the difference between the real and randomized models (in terms of Q^2_{yrand} or R^2_{yrand}) at confidence levels > 0.0001.
[e]Intercepts obtained from two **y**-randomization plots for each regression model proposed. Q^2_{yrand} or R^2_{yrand} is the vertical axis, whilst the horizontal axis is the absolute value of the correlation coefficient r_{yrand} between the original and randomized vectors **y**. The randomization plots are completed with the data for the real model (r_{yrand} = 1.000, Q^2 or R^2).

regressions (**1**) and (**2**) are very small ($a_Q < -0.15$ and $a_R \leq 0.003$, Table 3).

All the validations for the real MLR model confirm the self-consistency, robustness and good prediction power of the model, its stability to resamplings and the absence of chance correlation. The primary reason for this is the number of compounds. One out of five descriptors (the number of hydrogen bond donors, N_{hdon}, Table T1) shows degeneracy, *i.e.*, it has only three distinct integer values, but it did not affect the model's performance noticeably in this case.

Data set 2: QGSAR modeling of fungal resistance (P. digitatum) to demethylation inhibitors

Kiralj and Ferreira[39] have used five latent variables to model the complete data set of 86 samples using PLS (96.8% variance, Q^2 = 0.851, R^2 = 0.874, RMSECV = 0.286, RMSEC = 0.271, Q = 0.922 and R = 0.935), and also for the data split with 56 training samples when building the auxiliary PLS model (97.1% variance, Q^2 = 0.841, R^2 = 0.881, RMSECV = 0.305, RMSEC = 0.279, Q = 0.917, R = 0.939, Q^2_{ext} = 0.844, R^2_{ext} = 0.843, RMSEP = 0.272 and R_{ext} = 0.935). The split (35% out) was done based on six HCA clusters at a similarity index of 0.65. In this work, the model for 56 training samples was considered as the real model and it was further validated by bootstrapping. Results from validations for data set 2 are shown in Table 4 and in the Supplementary Information (Tables T10-T15 and Figures F3-F7).

The single and multiple LNO statistics (Table 4, Table T10 and Figure F3) show that the critical N is 10 (leave-18%-out) and 17 (leave-30%-out), respectively. The variations of Q^2_{LNO} in single LNO are uniform and less than 0.1, and the same is valid for two standard deviations in multiple LNO. Therefore, the real model is robust to exclusion of blocks in the range of 10 - 17 samples, which is reasonable for a data set of this size.[40]

Four bootstrap schemes were applied (Tables T11 and T12) to randomly select 56 training samples from the following sets: 1) the complete data set; 2) the six HCA clusters; 3) three classes of **y**, based on its statistical distribution (low, moderate and high fungal activity referred to intervals 4.55-5.75, 5.76-6.75, and 6.76-7.70,

Table 4. Important results[a] of single (Q^2_{LNO})[b] and multiple ($<Q^2_{LNO}>$ (σ))[c] leave-N-out crossvalidations for regression models on data sets 2, 3 and 4

	Data set 2		Data set 3		Data set 4	
N	Q^2_{LNO}	$<Q^2_{LNO}>$ (σ)	Q^2_{LNO}	$<Q^2_{LNO}>$ (σ)	Q^2_{LNO}	$<Q^2_{LNO}>$ (σ)
1	0.841	0.841	0.895	0.895	0.798	0.798
2	0.847	0.842(3)	0.894	0.895(2)	0.709	0.801(28)
3	0.839	0.839(6)	0.877	0.896(3)	0.723	0.746(54)
4	0.845	0.839(6)	0.888	0.892(4)	Av: 0.743(48)	
5	0.845	0.842(6)	0.897	0.894(6)		
6	0.850	0.835(8)	0.869	0.890(13)		
7	0.828	0.836(5)	0.898	0.896(4)		
8	0.853	0.839(8)	0.880	0.894(7)		
9	0.834	0.837(11)	0.887	0.894(7)		
10	0.819	0.842(8)	0.897	0.893(9)		
11	Av: 0.840(10)	0.838(13)		0.889(13)		
12		0.831(17)		0.885(14)		
13		0.842(10)		0.888(11)		
14		0.841(13)		0.890(11)		
15		0.842(6)		0.898(7)		
16		0.842(8)		0.896(7)		
17		0.838(9)		0.890(19)		
18				0.886(22)		
19				0.892(13)		

[a]Partial results are shown for values of N at which Q^2 is stable and high.
[b]Results of single LNO: Q^2_{LNO} - Q^2 for a particular N, Av - average of Q^2 with standard deviation in parenthesis (given for the last or last two digits).
[c]Results of multiple LNO: $<Q^2_{LNO}>$ - average of Q^2_{LNO} for ten runs, σ - respective standard deviation (given for the last or last two digits).

respectively); and 4) three MDR (multidrug resistance) classes of fungal strains with respect to pesticides (resistant, moderately resistant and susceptible).[39] The graphical presentation of the bootstrap models when compared to the real model (Figure F4), is very similar to that from data set 1. A new observation can be pointed out here, that the bootstrap models become more scattered as the number of runs increases, which is statistically expected. Resamplings based on HCA and **y** distribution seems to be the most adequate bootstrap schemes, because they are more compact and better distributed around the real model than those for the other two bootstrap schemes.

Results from 10 and 25 **y**-randomization runs (Tables T13 and T14) were analyzed numerically (Table T15) and graphically by means of the Q^2 - R^2 plot (Figure F5), and Q^2 - r and R^2 - r plots (Figures F6 and F7). The results are very similar to those from data set 1, leading to the same conclusion that the explained variance by the real PLS model is not due to chance correlation. In cases like this one, the results from a huge number of randomization runs[18] would concentrate mainly in the region of these 10 or 25 randomizations, confirming the conclusions that the real PLS model is statistically reliable.

Data set 3: QSPR modeling of carbonyl oxygen chemical shift in substituted benzaldehydes

Kiralj and Ferreira[5] have used two latent variables to build the real PLS model for the complete data set of 50 benzaldehydes (92.3% variance, Q^2 = 0.895, R^2 = 0.915, RMSECV = 9.10 ppm, RMSEC = 8.43 ppm, Q = 0.946 and R = 0.957), and also for the data split with 40 training samples to construct an auxiliary PLS model (92.6% variance, Q^2 = 0.842, R^2 = 0.911, RMSECV = 9.59 ppm, RMSEC = 8.83 ppm, Q = 0.942, R = 0.954, Q^2_{ext} = 0.937, R^2_{ext} = 0.936, RMSEP = 6.79 ppm and R_{ext} = 0.970). This split (20% out) was done based on five HCA clusters with a similarity index of 0.70. In this work, these real and auxiliary models were further validated and the validation results were analyzed in detail.

The LNO statistics[5] (Table 4, Table T16 and Figure F8) show that Q^2 stays high and stable up to the value of N = 10 (leave-20%-out) in single LNO and N = 19 (leave-38%-out) in multiple LNO, after which it starts to decrease and oscillate significantly. This is a very satisfactory result for a modest data set of fifty samples.

Three resampling schemes were applied in bootstrap validation (Tables T16 and T17) to exclude 10 from 50 samples randomly from the following sets: 1) the complete data set; 2) the five HCA clusters; and 3) three classes of **y**, based on statistical distribution of **y** (low, moderate and high chemical shifts).[5] Figure 4 shows the Q^2 - R^2 plot taking into account all the resampling schemes for 10 and 25 runs. Unlike the analogues for data sets 1 and 2, a different type of dispersion of the bootstrap models is observed in the plot. In fact, the data points are not well distributed along a diagonal direction but are substantially scattered in the orthogonal direction, along the whole range of values of Q^2 and R^2. The auxiliary model (the green point) is not in the centre of all bootstrap models, whilst the real model (the black point) is out of the main trend due to the different size of the training set. On the other hand, the plot still shows small variations in Q^2 and R^2, and no qualitative changes in this scenario are expected when increasing the number of bootstrap runs. Differences with respect to the analogue plots from data sets 1 and 2 may be a cumulative effect of diverse factors, as for example, smaller training set size, different ranges and statistical distribution profile of **y**, and the nature of **y** (chemical shifts against negative logarithm of molar concentrations). The common point in the three data sets is the performance of HCA-bootstrapping over the other schemes.

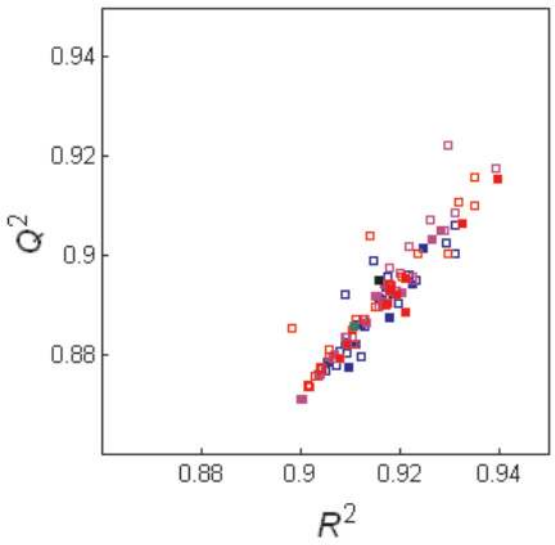

Figure 4. A comparative plot for bootstrapping of the PLS model on data set 3: the real model (black square), the auxiliary model (green square), models from HCA-based bootstrapping (blue squares: 10 iterations - solid, 25 iterations - open), models from bootstrapping based on classes of **y** (pink squares: 10 iterations - solid, 25 iterations - open), and models from simple bootstrapping (red squares: 10 iterations - solid, 25 iterations - open).

Results from 10 and 25 **y**-randomization runs (Tables T18 and T19) were analyzed numerically (Table T20) and graphically (Figures F9 - F11). The Q^2 - R^2 plot (Figure F9) shows no chance correlation. It is likely that the results from a larger number of randomization runs would be concentrated in the region already defined. The Q^2 - r and R^2 - r plots (Figures F10 and F11) also show the absence of chance correlation, which is reconfirmed by numerical approaches in Table T20.

The real model has somewhat weaker statistics than the previous one, but its statistics is still acceptable and in accordance to the data set size and recommendations for the five validation procedures.

Data set 4: QSAR modeling of mouse cyclooxigenase-2 inhibition by imidazoles

Hansch *et al.*[55] have built a MLR model for this small data set containing 15 inhibitors, with acceptable LOO statistics (reported: $Q^2 = 0.798$, $R^2 = 0.886$ and RMSEC = 0.212; calculated in this work: RMSECV = 0.241, $Q = 0.895$ and $R = 0.941$). Besides the real model, an auxiliary model was constructed in this work, by considering inhibitors **4** and **10** (Table T4 in Supporting Information) as external validation samples. This data split, reasonable for such a small data set (13% out), was performed according to the HCA analysis which resulted in one large and one small cluster with 13 and 2 samples, respectively (dendrogram not shown). The two inhibitors selected were from the large cluster. The auxiliary model shows improved LOO statistics with respect to that of the real model ($Q^2 = 0.821$, $R^2 = 0.911$, RMSECV = 0.239, RMSEC = 0.202, $Q = 0.908$ and $R = 0.954$). The external samples **4** and **10** are reasonably well predicted with calculated activities 6.52 and 6.49, respectively, compared to their experimental values 6.72 and 6.19, respectively, which means less than 5% error. The downside of this external validation is that it is not justified to calculate RMSEP, Q^2_{ext} or other statistical parameters for a set of two inhibitors.

Both single and multiple LNO statistics (Table 4, Table T21 and Figure F12) show that the model is stable for $N = 1$ - 3 (leave-20%-out). The values of Q^2_{LNO} in this interval of N oscillate within the limit of 0.1 (see Figure F12). These results indicate that the model is reasonably robust in spite of the data size.

The bootstrap tests for the MLR model were performed by eliminating two inhibitors by random selection from the complete data set and from the large HCA cluster. Other resampling schemes were not applied in this example due to the data size and its **y** distribution. The results obtained (Tables T22 and T23), when compared to that from the auxiliary model of the same data size (Figure 5), show rather unusual behavior. The data points in the R^2 - Q^2 plot are not well distributed along some diagonal direction as in the analyses for data sets 1 and 2, but are rather dispersed in the orthogonal direction, especially at lower values of Q^2 around 0.6. This suggests that Q^2 would easily overcome the limit of 0.65 with increasing the number of resamplings. The auxiliary model (the green point), which should be closer to the bootstrap models than the real model, is placed too high with respect to the centroids of these models. The plot shows an unusual, "asymmetric" aspect unlike the analogue plots for data sets 1 - 3 (Figures 2 - 4), due to the pronounced differences between Q^2 and R^2 (see Tables T22 and T23).

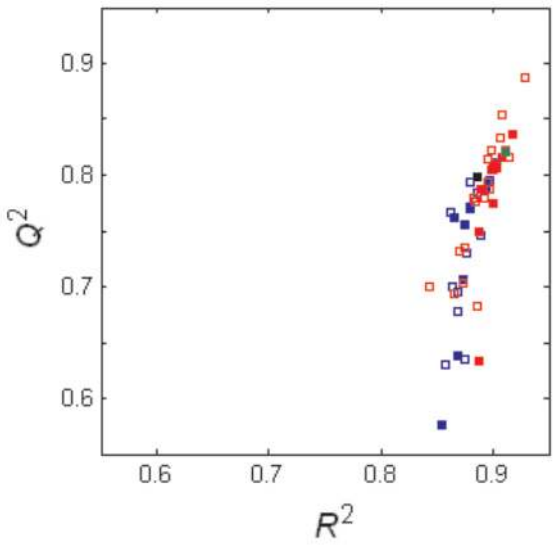

Figure 5. A comparative plot for bootstrapping of the MLR model on data set 4: the real model (black square), the auxiliary model (green square), models from HCA-based bootstrapping (blue squares: 10 iterations - solid, 25 iterations - open), and models from simple bootstrapping (red squares: 10 iterations - solid, 25 iterations - open).

Results from 10 and 25 **y**-randomization runs (Tables T24 and T25), when presented graphically (Figure 6), show a large dispersion of the data points. The points are placed along a R^2 - Q^2 diagonal and also spread around it. Furthermore, it is evident that a slight increase in the number of **y**-randomization runs would result in falsely good models that would be very close to the real model, meaning that this final model is based on chance correlation, and thus, is invalid. Compared to the previous **y**-randomization plots for data sets 1 - 3 (Figures 3, F5 and F9), a systematic increase of the dispersion of the data points can be observed. This trend is followed by the appearance of highly negative values of Q^2 for the randomized models: about –0.2, –0.3, –0.6 and –1.1 for data sets 1, 2, 3, and 4, respectively.

To be more rigorous in this validation, further calculations were carried out, as shown in Table 5 and Figures F13 and F14. The smallest distance between the real model and randomized models is significant in terms of confidence levels of the normal distribution (<0.0001), both in Q^2 and R^2. The situation is even more critical when all distances are expressed in terms of the confidence level, since more than 40% of the randomized models are not statistically distinguished from the real model in Q^2 units, and much less but still noticeable in R^2 units (for more than 10 runs). These tendencies seem to be more

obvious when increasing the number of randomization runs. However, when the linear regression equations (**1**) and (**2**) are obtained, the intercepts do not approach the limits (a_Q < 0.05 and a_R < 0.3) and the validation seems apparently acceptable. It is obvious that this inspection is not sufficient by itself to detect chance correlation in the model and so, one has to investigate the spread of the data points in the region around the intercept in both Q^2 - r and R^2 - r plots. If this spread is pronounced in the way that several data points are situated above the limits for intercepts, then the chance correlation is identified, which is exactly the situation in the present plots (Figures F13 and F14). In fact, the MLR model published by Hansch *et al.*[60] has certainly failed in **y**-randomization, confirming that small data sets seriously tend to incorporate chance correlation. The other possible reason, although of less impact, is data degeneration (redundancy) in columns and rows of the data matrix **X** (see Table T4 in Supporting Information). The cumulative results of **y**-randomization and the other validations show that the real MLR model is not statistically reliable.

Data quality versus data set size: data subset 3

The comparative discussion of models' performance in previous sections was based on data set size. In this section,

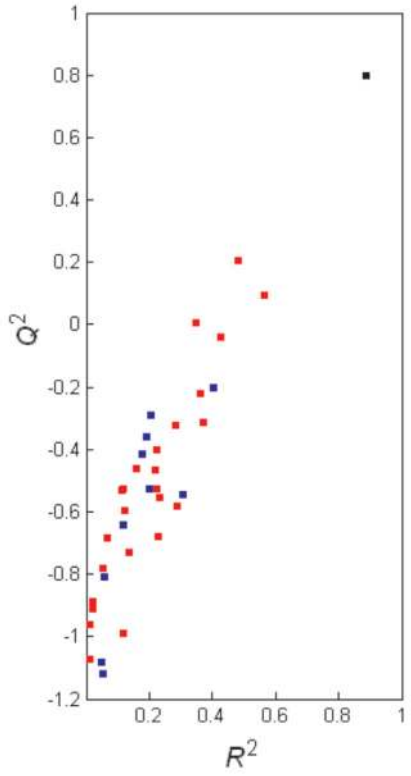

Figure 6. The **y**-randomization plot for the MLR model on data set 4: black ball - the real model, blue balls - 10 randomized models, red balls - 25 randomized models.

Table 5. Comparative statistics of 10 and 25 **y**-randomizations of the MLR model on data set 4

Parameter[a]	10 iterations	25 iterations
Maximum (Q^2_{yrand})	–0.202	0.206
Maximum (R^2_{yrand})	0.404	**0.563**
Standard deviation (Q^2_{yrand})	**0.316**	**0.341**
Standard deviation (R^2_{yrand})	0.115	0.153
Minimum model-random. Diff. (Q^2_{yrand})[b]	3.16	**1.74**
Minimum model-random. Diff. (R^2_{yrand})[b]	4.19	2.10
Confidence level for min. diff. (Q^2_{yrand})[c]	**0.0016**	**0.0819**
Confidence level for min. diff. (R^2_{yrand})[c]	<0.0001	**0.0357**
Randomizations %, conf. level > 0.0001 (Q^2_{yrand})[d]	**40%**	**48%**
Randomizations %, conf. level > 0.0001 (R^2_{yrand})[d]	0	**24%**
y-Randomization intercept (r_{yrand} *vs.* Q^2_{yrand})[e]	–0.989	–0.739
y-Randomization intercept (r_{yrand} *vs.* R^2_{yrand})[e]	–0.011	0.077

[a]Statistical parameters are calculated for Q^2 from **y**-randomization (Q^2_{yrand}) and R^2 from **y**-randomization (R^2_{yrand}). Values typed bold represent obvious critical cases.

[b]Minimum model-randomizations difference: the difference between the real model (Table 1) and the best **y**-randomization in terms of correlation coefficients Q^2_{yrand} or R^2_{yrand}, expressed in units of the standard deviations of Q^2_{yrand} or R^2_{yrand}, respectively. The best **y**-randomization is defined by the highest Q^2_{rand} or R^2_{rand}.

[c]Confidence level for normal distribution of the minimum difference between the real and randomized models.

[d]Percentage of randomizations characterized by the difference between the real and randomized models (in terms of Q^2_{yrand} or R^2_{yrand}) at confidence levels > 0.0001.

[e]Intercepts obtained from two **y**-randomization plots for each regression model real. Q^2_{yrand} or R^2_{yrand} is the vertical axis, whilst the horizontal axis is the absolute value of the correlation coefficient r_{yrand} between the original and randomized vectors **y**. The randomization plots are completed with the data for the real model (r_{yrand} = 1.000, Q^2 or R^2).

the data quality, *i.e.*, relationships between descriptors **X** and the dependent variable **y**, are inspected in two ways. First, data sets 1, 2 and 3 were reduced to small subsets of 15 samples, to inspect how much the data size and its quality affect the performance of the models. Second, to rationalize these results and emphasize the importance of variable selection, correlations between **X** and **y** for all data sets and their subsets were inspected by calculating various statistical parameters.

The largest set, data set 1, was reduced to 15 samples (denominated as subset 1, containing the toxicants **4**, **17**, **20**, **32**, **37**, **51**, **53**, **62**, **70**, **71**, **113**, **133**, **141**, **143** and **149**), but its poor performance in LOO (Q^2 = 0.073) did not justify any further validation. All attempts to reduce data set 2 failed because certain descriptors which were not indicator variables in the original data, became degenerate (*i.e.*, were reduced to two distinct values) due to the loss of information. Among the three data sets tested for size reduction, only data set 3 could be reduced successfully to a subset (denominated as subset 3) and validated in the same way as data set 4. All analyses for this data subset can be found in the Supplementary Information (Tables T26 - T32 and Figures F15 - F19).

The real PLS model for data subset 3 still has acceptable LOO statistics when two latent variables are used (91.8% variance, Q^2 = 0.779, R^2 = 0.897, RMSECV = 13.6 ppm, RMSEC = 10.4 ppm, Q = 0.892 and R = 0.947), which is somewhat inferior to that of the real model for data set 3 (the differences are more obvious in RMSEC and RMSECV than in the correlation coefficients), but is comparable to that of the real model for data set 4. The same number of latent variables is used for the auxiliary model (91.8% variance, Q^2 = 0.738, R^2 = 0.889, RMSECV = 15.0 ppm, RMSEC = 11.1 ppm, Q = 0.874 and R = 0.943), which is obtained when benzaldehydes **7** and **37** are treated as external samples. These samples were selected from an HCA histogram (not shown) and, not surprisingly, the predictions are satisfactory. The experimental chemical shifts are 570.1 and 520.0 ppm for **7** and **37**, respectively, and predicted shifts are 564.3 and 513.9 ppm, respectively, which amounts to less than 7% error. When analyzing the performance of the real model in LNO, bootstrapping and **y**-randomization, it is obvious that the model is much inferior to that from data set 3, due to the difference in the number of samples. However, when compared to that from data set 4, the model for subset 3 is somewhat better in single and multiple LNO (critical N = 4 or leave-27%-out versus N = 3), the same atypical behavior is also observed in the Q^2 - R^2 space for bootstrapping, and the model is also based on chance correlation. The model's failure in most of the numerical and graphical analyses for **y**-randomization is even more obvious than that of the model for data set 4. Even though small data sets allow the construction of models with reasonable LOO, LNO and external validation statistics (as has been shown in this section), this does not imply reasonable performance in bootstrapping and **y**-randomization. Concluding, small data sets of about 15 samples are not suitable for a QSAR or QSPR study.

Effects of sample randomization to leave-N-out crossvalidation and **y***-randomization*

It has been emphasized in this work that sample scrambling is an important step prior to model validation, by which the randomness of a data set is enhanced. The effects of this randomization can be found in the Supplementary Information (Figures F3, F8, F12 and F15, and two special sections containing Tables T33 - T38 and Figures F20 - F26 with discussion), where the results from LNO and **y**-randomization are presented for data sets 1 - 4 and subset 3, using the original descriptor blocks, **X**. The reader should keep in mind that data sets with significant redundancy in samples are not of random character, and consequently, a regression model built on such data will have falsely good performance in validation procedures,[50] even though sample randomization has been performed.

Data quality versus data set size: statistics of **x** *-* **y** *relationships*

There are 90 relationships between descriptors and dependent variables (*i.e.*, **x** - **y** relationships) for all data sets and subsets studied in this article, presented as linear regressions $\mathbf{y} = a + b\mathbf{x}$ and analyzed *via* correlation coefficients, *t*-test and *F*-test parameters (Figures F20 - F25 and Table 33 in Supplementary Information). Careful analysis of these statistics may aid in explaining the behavior of QSAR or QSPR models in all validations performed. First, models built for various subsets of the same data set deteriorate as the number of samples decreases, which is a consequence of the fact that **x** - **y** relationships tend to become less statistically significant when there are fewer samples. Second, some statistical parameters are, although not identical, very highly correlated to each other. This is valid for square of R and R^2; F-value (F) and the square of the t-test parameter for b (t_b); and the confidence levels for t_b (p_b) and F-value (p). Third, minimum values of some parameters are not so problem-dependent but may be well related to the statistical significance of **x** - **y** relationships: $R > 0.3$; $R^2 > 0.1$; $F > 5$; $t_b > 2.5$, and probably $t_a > 2.5$. However, the exact limits for t-test parameters and F-value in a particular study are extracted from statistical tables,

which strongly depend on the number of samples. It is recommended[44,49] to use confidence level 0.05 or 0.01 for *t*-test and *F*-test. In fact, variable selection should provide statistically significant **x** - **y** relationships, so model validation does not have to deal with poor and individual problematic **x** - **y** relationships but with the relationship between the descriptor block **X** as a whole and **y**.

In the light of these facts, it is possible to understand the scatterplots for the data sets studied (Figures F20 - F24 and Table 33). It is rather clear that data set 1 contains only one statistically significant descriptor ($\mathrm{Log}K_{ow}$), whilst another one (N_{hdon}) behaves as a poorly distributed degenerate variable (there are 126, 24 and 3 samples with values N_{hdon} = 1, 2 and 3, respectively). The other three descriptors ($\mathrm{p}K_a$, E_{LUMO} and E_{HOMO}) are characterized by very high dispersion in their scatterplots and, consequently, the **x** - **y** relationships are not statistically significant (see bold descriptors and values in Table T33). In other words, the models built for data set 1 and its subsets are based on at least three statistically not significant **x** - **y** relationships, meaning that the selected variables were not so significant. The large number of samples has simply masked their deficiencies so that they could not be detected by the five validation procedures and, consequently, the model for set 1 showed excellent performance in all tests. However, successful reduction of data set 1 to 15 samples was not possible. Therefore, data set 1 is an example of a large and falsely good set for building QSAR models.

Although **x** - **y** relationships for data set 2, of moderate size, were all statistically significant, it was also not possible to reduce the data from 86 to 15 samples. It probably contains some non-linear relationships, but this is questioned by the following items: a) a few data at high values for certain descriptors are not sufficient to confirm non-linearities; b) how to interpret the non-linearities in terms of fungal genome; and c) how to form subsets since three genome descriptors have only three distinct values.

Another set of moderate size, data set 3, has the most adequate scatterograms, and is based on statistically significant **x** - **y** relationships. When it is reduced to 15 or less samples, only one or two **x** - **y** relationships become partially insignificant in parameters for *a*. Data set 4, besides being small, is characterized by three **x** - **y** relationships from which only one is statistically significant (ClogP), another is insignificant (MgVol) and the third is not sufficiently significant ($B1_{X.2}$). This set is a typical example of a small and falsely good data set, which, in spite of this fact, showed good performance in some validation tests. This is another example indicating the need to couple variable selection based on statistical tests for **x** - **y** relationships and model validation.

A simple way to verify self-consistency of a data is to see if the positive or negative contribution of a descriptor to **y** remains the same during the data split and building regression models. This contribution can be seen from the **x** - **y** relationship, using the signs of correlation coefficient *R* or regression coefficient *b* and the respective regression coefficient from the real model. For self-consistent data, the sign of *R* or *b* for a descriptor should be the same in the complete data set and all of its subsets, and also equal to the corresponding regression coefficient from the real model. In this sense, data set 1 showed being inconsistent both in data split and model building (in 3 out of 5 descriptors), data set 2 only in modeling (due to non-linearities, as seen in 2 out of 8 descriptors), and data sets 3 and 4 and subset 3 were self-consistent in all descriptors (see Table T39). This self-consistency is important from the statistical point of view and also for model interpretation and mechanism of action.

Conclusions

Four QSAR and QSPR data sets from the literature were used to rebuild published or build statistically related regression models. These models were validated by means of leave-one-out crossvalidation, leave-*N*-out crossvalidation, external validation, **y**-randomization and boostrappings. The five validation tests have shown that the size of the data sets, more precisely, of the training sets, is the crucial factor determining model performance. The larger the data set, the better is its validation statistics. Very small data sets suffer from several deficiencies: impossibility of making validations (data split is not possible or is not sufficient), failure and atypical behavior in validations (chance correlation, lack of robustness in resampling and crossvalidations). Obtaining satisfactory statistics in leave-one-out crossvalidation and fitting and even in external validation is not a guarantee for good model performance in other validations procedures. Validation has to be carried out carefully, with detailed graphical and numerical analyses of the results obtained. The critical *N* in LNO at which Q^2 is still stable and high, can be determined by applying the limit of 0.1 for oscillations in Q^2, defined as the variation range in single LNO and two standard deviations in multiple LNO. It has been demonstrated that it is not necessary to perform a large number of **y**-randomization or bootstrap runs to distinguish acceptable from non-acceptable regression models. Comparing various bootstrap schemes, it has been noted for data sets 1 - 3 that resampling based on clusters from hierarchical cluster analysis, and perhaps on some other schemes, gives somewhat more reliable and reasonable results than

that relying only on randomization of the complete data set. Data quality in terms of descriptor - **y** relationships is the second important factor which influences model performance. A reliable model has to be constructed from statistically significant **x** - **y** relationships, emphasizing the important role of variable selection. Statistically insignificant **x** - **y** relationships in large data sets can be masked by data size, resulting in models with excellent performance in all validation procedures, but at the end the QSAR or QSPR models obtained are false.

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Supplementary Information

Data sets used to build regression models, results of validations of the models, graphical and numerical analyses of these results, and additional tests for chance correlation and statistical significance of descriptors used (in total 39 tables, 32 figures, and discussion on randomization effects), are available online at http://jbcs.sbq.org.br.

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Basic Validation Procedures for Regression Models in QSAR and QSPR Studies: Theory and Applications

Rudolf Kiralj, Márcia M. C. Ferreira*

Laboratory of Theoretical and Applied Chemometrics, Institute of Chemistry, State University of Campinas, P.O. Box 6154, 13084-971 Campinas-SP, Brazil

DATA SETS 1-4

Table T1. The QSAR data set 1 for phenols toxicity to ciliate *T. pyriformis*.[a,b,c]

No.	Log*Kow*	p*Ka*	E_{LUMO}/eV	E_{HOMO}/eV	N_{hdon}	–log[IGC_{50}/molL^{-1}]
			Training set			
1	0.16	8.45	0.25	–9.16	3	–1.26
3	3.80	11.39	0.46	–8.76	1	1.30
6	3.58	6.75	–0.56	–9.49	1	2.37
8	2.92	10.63	0.36	–8.84	1	0.28
10	4.37	5.72	–0.66	–9.31	2	1.06
11	3.37	6.35	–0.50	–9.39	1	1.41
13	2.97	10.88	0.42	–8.70	1	0.28
15	0.92	8.96	0.53	–8.65	1	–0.52
17	2.96	7.58	–0.29	–9.31	1	1.13
19	2.47	10.22	0.38	–8.85	1	0.08
20	5.63	12.55	0.50	–8.62	1	1.80
21	2.63	6.78	–0.26	–9.37	1	0.74
25	2.55	10.28	0.36	–9.04	1	0.33
29	2.65	8.54	0.06	–9.07	1	0.39
31	1.60	6.98	–0.43	–9.58	1	0.03
32	1.72	8.73	0.02	–9.28	1	0.19
35	2.86	10.37	0.35	–8.76	1	0.71
38	1.98	9.67	–0.28	–9.33	1	0.55
41	3.58	9.67	–0.51	–9.03	1	1.42
43	0.44	9.92	0.20	–9.24	2	–0.95
44	1.56	9.92	–0.54	–9.42	2	–0.08
45	2.90	10.40	0.41	–8.99	1	0.80
47	2.58	9.88	–0.05	–8.50	1	0.75
48	3.30	11.10	0.42	–8.97	1	1.30
49	3.17	8.63	–0.20	–9.26	1	1.75
50	2.42	10.32	0.43	–8.80	1	0.12
51	3.42	6.20	–0.93	–9.66	1	1.64
56	3.87	6.37	–0.90	–9.72	1	2.34
58	2.47	10.15	0.39	–8.98	1	0.11
60	0.49	9.92	0.22	–8.73	2	-0.16
61	2.72	8.96	–0.26	–9.25	1	1.13
63	2.49	9.10	0.04	–9.30	1	0.87
65	1.80	7.80	–0.44	–9.09	1	0.02
69	1.69	9.94	0.32	–8.36	1	–0.30

*e-mail: marcia@iqm.unicamp.br

Table T1. continuation

No.	Log*Kow*	p*Ka*	E_{LUMO}/eV	E_{HOMO}/eV	N_{hdon}	–log[IGC_{50}/molL^{-1}]
Training set						
71	1.46	9.19	–0.46	–9.40	1	–0.38
77	2.90	8.88	–0.04	–9.34	1	1.12
78	2.90	10.10	0.42	–9.02	1	0.61
79	1.57	9.65	0.36	–8.88	1	–0.33
80	2.40	10.23	0.25	–8.89	1	0.42
84	3.34	10.60	0.24	–8.61	1	1.04
85	3.63	10.00	0.10	–8.99	1	1.17
88	3.63	9.70	0.11	–9.06	1	1.27
89	3.61	8.20	–0.22	–9.23	1	1.28
94	4.41	10.03	0.14	–8.93	1	1.85
95	2.98	9.55	0.13	–9.04	1	0.80
100	1.92	9.89	0.07	–9.09	1	0.02
101	4.22	10.70	0.35	–8.60	1	1.64
102	3.45	9.63	0.30	–8.80	2	1.80
106	1.95	10.05	–0.35	–9.33	1	0.19
107	0.29	9.90	0.17	–9.03	2	–0.70
109	0.28	9.27	0.19	–8.87	2	–0.97
110	1.46	8.05	–0.38	–9.43	1	–0.30
111	0.90	9.52	0.06	–9.30	1	–0.38
112	0.75	4.49	–0.21	–9.48	2	–1.50
114	1.98	8.85	–0.36	–9.41	1	0.05
115	2.90	9.20	0.02	–9.24	1	0.85
118	1.57	10.20	0.31	–8.65	1	–0.14
119	3.20	9.55	–0.10	–8.68	1	1.39
120	3.03	10.30	0.43	–8.91	1	0.64
121	3.43	10.30	0.45	–8.91	1	0.98
125	1.92	6.06	–0.70	–9.33	1	0.62
126	2.17	9.79	–0.64	–9.39	1	0.04
129	2.88	8.68	–0.34	–9.80	1	0.62
130	2.51	8.92	–0.38	–9.50	1	0.57
133	1.28	8.89	–0.49	–9.11	1	–0.14
135	1.99	9.21	–0.48	–9.45	1	–0.05
139	6.20	10.40	0.43	–8.92	1	2.47
141	1.97	10.26	0.40	–8.96	1	–0.30
142	1.97	10.26	0.43	–8.88	1	–0.18
143	0.80	9.44	0.28	–8.98	2	–0.65
144	1.81	8.34	–0.43	–9.50	1	0.42
147	1.28	8.36	–0.19	–9.51	2	–0.24
148	0.88	8.78	–0.46	–9.66	3	0.38
150	2.19	2.98	–0.46	–9.51	2	–0.51
151	1.28	7.40	–0.48	–9.14	1	–0.03
External validation set						
2	2.92	10.48	0.38	–8.81	1	0.36
4	2.84	7.44	–0.25	–9.39	1	1.28
5	2.42	10.50	0.38	–8.93	1	0.12
7	3.58	7.37	–0.51	–9.32	1	2.10
9	3.92	6.80	–0.62	–9.50	1	2.03
12	3.31	7.87	–0.30	–9.33	1	1.40
14	2.96	7.97	–0.19	–9.23	1	1.04
16	1.95	8.58	–0.32	–9.29	1	0.60
18	2.47	10.58	0.44	–8.77	1	0.07
22	2.80	6.75	–0.57	–9.38	1	0.80
23	1.75	7.51	–0.32	–9.46	1	0.47

Table T1. continuation

No.	Log*Kow*	p*Ka*	E_{LUMO}/eV	E_{HOMO}/eV	N_{hdon}	$-\log[IGC_{50}/molL^{-1}]$
External validation set						
24	1.10	9.92	0.39	–8.61	1	–0.60
26	2.85	8.67	0.02	–9.05	1	0.60
27	2.36	9.34	–0.01	–9.24	1	0.33
28	3.10	8.85	0.09	–8.89	1	0.69
30	2.16	8.55	0.07	–9.19	1	0.18
33	1.85	10.11	0.42	–8.73	1	–0.36
34	2.50	10.20	0.40	–8.99	1	0.16
36	2.41	10.23	–0.32	–9.19	1	0.31
37	1.92	9.90	–0.33	–9.32	1	0.08
39	1.32	9.99	0.40	–8.79	1	–0.51
40	3.09	9.55	–0.04	–8.74	1	1.09
42	2.87	10.25	0.41	–8.76	1	0.93
46	3.29	8.18	–0.28	–9.54	1	1.57
52	3.07	6.20	–0.90	–9.58	1	1.55
53	1.60	9.35	0.42	–8.94	1	–0.09
54	5.13	10.32	0.47	–8.93	1	1.64
55	2.64	9.03	–0.05	–9.34	1	1.15
57	2.50	8.85	0.03	–9.22	1	0.76
59	1.60	8.61	–0.50	–9.59	1	–0.06
62	2.50	10.07	0.40	–9.04	1	0.23
64	1.92	9.29	0.03	–9.37	1	0.38
66	0.29	9.67	0.33	–8.68	2	–0.99
67	1.44	9.00	–0.53	–9.43	1	0.09
68	1.56	4.08	–0.57	–9.52	2	–0.81
70	0.44	9.83	0.12	–9.26	2	–1.04
72	3.23	9.63	–0.15	–8.95	1	1.35
73	3.30	10.10	0.43	–9.01	1	0.73
74	5.16	9.92	0.47	–8.85	1	2.10
75	3.30	10.30	0.47	–8.91	1	0.91
76	2.08	7.28	–0.25	–9.03	2	0.97
81	3.52	6.40	–0.52	–9.44	1	1.78
82	2.64	9.34	0.02	–9.20	1	0.68
83	3.16	10.60	0.34	–8.61	1	0.70
86	2.98	9.67	0.12	–9.01	1	0.70
87	3.48	9.65	0.14	–8.99	1	1.20
90	3.51	9.54	0.14	–9.04	1	1.08
91	2.49	9.43	0.10	–9.12	1	0.55
92	1.58	8.11	0.01	–8.98	2	0.13
93	1.60	7.95	–0.40	–9.57	1	0.52
96	2.10	10.50	0.33	–8.61	1	0.01
97	2.50	10.00	0.43	–8.92	1	0.21
98	4.75	10.70	0.35	–8.59	1	2.03
99	1.27	9.85	–0.39	–9.00	1	–0.12
103	1.42	7.96	–0.44	–9.10	1	–0.03
104	0.47	9.92	0.28	–8.78	2	–0.18
105	1.44	7.62	–0.44	–9.49	1	0.27
108	0.33	9.23	–0.25	–9.44	2	–0.78
113	1.56	4.58	–0.49	–9.60	2	–1.02
116	3.07	8.89	–0.49	–9.40	1	1.02
117	0.52	9.92	0.29	–9.06	2	–0.83
122	2.90	10.30	0.44	–8.92	1	0.47
123	3.83	10.30	0.46	–8.90	1	1.23

Table T1. continuation

No.	Log*Kow*	p*Ka*	E_{LUMO}/eV	E_{HOMO}/eV	N_{hdon}	–log[IGC_{50}/molL^{-1}]
External validation set						
124	1.60	9.34	–0.13	–9.29	2	0.34
127	1.31	9.46	0.26	–8.95	2	–0.39
128	3.42	9.49	0.29	–8.93	2	1.31
131	4.30	12.50	0.44	–8.69	1	1.16
132	2.51	9.09	–0.45	–9.44	1	0.48
134	1.53	9.92	0.04	–8.86	1	–0.23
136	1.97	10.10	0.39	–9.02	1	–0.06
137	1.99	9.05	–0.40	–9.54	1	0.08
138	2.49	9.21	–0.31	–9.35	1	0.62
140	1.65	7.91	–0.45	–9.12	1	0.38
145	3.54	9.92	0.43	–8.90	1	1.29
146	1.48	9.99	0.40	–9.11	1	–0.21
149	1.10	9.92	–0.19	–8.99	2	0.25
152	0.85	9.92	–0.36	–9.57	3	0.18
153	0.99	7.62	–0.50	–8.94	1	0.17

[a]This data set was generated by Aptula *et al.*, *Quant. Struct.-Act. Relat.* **2002**, *21*, 12. It was used to build MLR models by Yao *et al.*, *J. Chem. Inf. Comput. Sci.* **2004**, *44*, 1257. [b]Names of samples and variables are from the original publications. [c]The current data split is made in this work.

Table T2. The QGSAR data set 2 for fungal resistance (*P. digitatum* strains) to demethylation inhibitors.[a,b,c]

No.	Toxicant/ Straind	CYP51-g	CYP51-e	PMR1-t	CYP51-e*Npi	PCR*Npi	PMR1-e*Lpi	CYP51-e*Lpi	PCR*Lpi	-log[EC_{50}/ molL^{-1}]
Training set										
1	T/PD5	1	1	100	1	0.25	1	1	0.25	6.636
2	T/DF1	1	1	100	1	0.25	1	1	0.25	6.937
4	T1/LC2	5	100	100	100	0.75	7	100	0.75	5.225
6	T/I1	5	100	100	100	0.75	7	100	0.75	5.093
7	T/DIS03	5	100	1	100	0.75	0	100	0.75	5.895
9	T/DIS96	5	100	1	100	0.75	0	100	0.75	5.858
10	T/PD5	1	1	100	1	0.25	1	1	0.25	6.840
12	T/PD5-7	5	100	100	100	0.75	1	100	0.75	5.335
13	T/PD5-15	5	100	100	100	0.75	1	100	0.75	5.335
15	T/PD5	1	1	100	1	0.25	1	1	0.25	6.948
17	T/DISp21	1	1	1	1	0.25	0	1	0.25	7.694
19	T/LC2	5	100	100	100	0.75	7	100	0.75	5.146
20	T/DIS33	5	100	1	100	0.75	0	100	0.75	6.177
22	T/DIS33-Y8	5	100	100	100	0.75	7	100	0.75	5.179
23	T/DIS33-B0	5	100	10	100	0.75	7	100	0.75	6.007
27	T/DIS33	5	100	1	100	0.75	0	100	0.75	6.283
29	T/PD5	1	1	100	1	0.25	1	1	0.25	6.937
30	T/LC2M	2	50	100	50	0.37	7	50	0.37	5.840
32	T/DIS33	5	100	1	100	0.75	0	100	0.75	6.177
33	T/LC2	5	100	1000	100	0.75	7	100	0.75	5.189
34	T/DISp21	1	1	1	1	0.25	0	1	0.25	7.539
36	T/DIS5-P26	1	1	100	1	0.25	1	1	0.25	6.937
37	F/PD5	1	1	100	3	0.75	2	2	0.50	6.073
39	F/U1	1	1	100	3	0.75	2	2	0.50	6.058
40	F/LC2	5	100	100	300	2.25	14	200	1.50	5.160
42	F/I1	5	100	100	300	2.25	14	200	1.50	4.799
43	F/PD5	1	1	100	3	0.75	2	2	0.50	6.073
45	F/DIS33	5	100	1	300	2.25	0	200	1.50	6.073
46	F/DIS96	5	100	1	300	2.25	0	200	1.50	5.952

Table T2. continuation

No.	Toxicant/ Straind	CYP51-g	CYP51-e	PMR1-t	CYP51-e*Npi	PCR*Npi	PMR1-e*Lpi	CYP51-e*Lpi	PCR*Lpi	-log[EC_{50}/ $molL^{-1}$]
					Training set					
48	F/PD5-21	1	3	100	9	0.75	2	6	0.50	6.122
49	F/PD5-7	5	100	100	300	2.25	2	200	1.50	5.714
51	F/LC2	5	100	100	300	2.25	14	200	1.50	5.241
52	F/PD5	1	1	100	3	0.75	2	2	0.50	6.475
54	F/DISp21	1	1	1	3	0.75	0	2	0.50	6.520
56	F/LC2	5	100	100	300	2.25	14	200	1.50	5.230
57	F/DIS33	5	100	1	300	2.25	0	200	1.50	6.241
59	B/DF1	1	1	100	2	0.50	3	3	0.75	6.081
61	B/LC2	5	100	100	200	1.50	21	300	2.25	5.024
63	B/I1	5	100	100	200	1.50	21	300	2.25	4.546
65	B/DIS33	5	100	1	200	1.50	0	300	2.25	6.298
67	B/LC2	5	100	100	200	1.50	21	300	2.25	5.024
69	B/PD5-21	1	3	100	6	0.50	3	9	0.75	5.984
70	B/PD5-7	5	100	100	200	1.50	3	300	2.25	5.449
72	B/LC2	5	100	100	200	1.50	21	300	2.25	5.113
74	B/DISp12	1	1	1	2	0.50	0	3	0.75	7.324
75	B/DISp21	1	1	1	2	0.50	0	3	0.75	7.324
77	B/LC2	5	100	100	200	1.50	21	300	2.25	5.112
78	B/DIS33	5	100	1	200	1.50	0	300	2.25	6.382
79	P/PD5	1	1	100	3	0.75	3	3	0.75	5.902
80	P/DF1	1	1	100	3	0.75	3	3	0.75	5.664
82	P/PD5	1	1	100	3	0.75	3	3	0.75	6.993
83	P/PD5-21	1	3	100	9	0.75	3	9	0.75	6.023
85	P/PD5-15	5	100	100	300	2.25	3	300	2.25	4.979
87	P/PD5	1	1	100	3	0.75	3	3	0.75	6.993
88	P/DISp12	1	1	1	3	0.75	0	3	0.75	7.023
90	P/ECTp36	1	1	1	3	0.75	0	3	0.75	6.685
					External validation set					
5	T/M1	5	100	100	100	0.75	7	100	0.75	5.432
8	T/DIS33	5	100	1	100	0.75	0	100	0.75	5.971
11	T/PD5-21	1	3	100	3	0.25	1	3	0.25	6.363
14	T/LC2	5	100	100	100	0.75	7	100	0.75	5.141
16	T/DISp12	1	1	1	1	0.25	0	1	0.25	7.694
18	T/ECTp36	1	1	1	1	0.25	0	1	0.25	7.047
21	T/DIS33-Y4	5	100	100	100	0.75	7	100	0.75	5.641
24	T/DIS33-B13	5	100	10	100	0.75	7	100	0.75	6.124
28	T/LC2	5	100	100	100	0.75	7	100	0.75	5.107
31	T/PD5	1	1	100	1	0.25	1	1	0.25	6.937
35	T/DIS5-L22	5	100	100	100	0.75	7	100	0.75	5.202
38	F/DF1	1	1	100	3	0.75	2	2	0.50	6.015
41	F/M1	5	100	100	300	2.25	14	200	1.50	5.093
44	F/DIS07	5	100	1	300	2.25	0	200	1.50	6.002
47	F/PD5	1	1	100	3	0.75	2	2	0.50	6.479
50	F/PD5-15	5	100	100	300	2.25	2	200	1.50	5.542
53	F/DISp12	1	1	1	3	0.75	0	2	0.50	7.219
55	F/ECTp36	1	1	1	3	0.75	0	2	0.50	6.441
58	B/PD5	1	1	100	2	0.50	3	3	0.75	6.186
60	B/U1	1	1	100	2	0.50	3	3	0.75	6.037
62	B/MI	5	100	100	200	1.50	21	300	2.25	5.093
64	B/DIS07	5	100	1	200	1.50	0	300	2.25	6.227
66	B/DIS96	5	100	1	200	1.50	0	300	2.25	6.148
68	B/PD5	1	1	100	2	0.50	3	3	0.75	6.382

Table T2. continuation

No.	Toxicant/ Straind	CYP51-g	CYP51-e	PMR1-t	CYP51-e*Npi	PCR*Npi	PMR1-e*Lpi	CYP51-e*Lpi	PCR*Lpi	-log[EC_{50}/ molL^{-1}]
					External validation set					
71	B/PD5-15	5	100	100	200	1.50	3	300	2.25	5.324
73	B/PD5	1	1	100	2	0.50	3	3	0.75	6.424
76	B/ECTp36	1	1	1	2	0.50	0	3	0.75	6.503
81	P/U1	1	1	100	3	0.75	3	3	0.75	5.595
84	P/PD5-7	5	100	100	300	2.25	3	300	2.25	5.294
89	P/DISp21	1	1	1	3	0.75	0	3	0.75	7.039

[a]This data set was generated and used to build PLS models by Kiralj and Ferreira, *QSAR Comb. Sci.* **2008**, *27*, 289. It was denominated C1 and had six outliers which are already excluded in this table. [b]Names of samples and variables are from the original publication. Abbreviations for toxicants in the sample names: T - triflumizole, F - fenarimol, B - bitertanol and P - pyrifenox. [c]The current data split is from the original publication. [d]A sample is defined as combination toxicant-strain-experiment.

Table T3. The QSPR data set 3 for carbonyl oxygen chemical shift in substituted benzaldehydes.[a,b,c]

No.	E_e/eV	E_{CC}/eV	Δ_{HL}/eV	σ_b/Å	σ_r/Å	D_{CC}/Å	Q_{C2mul}	Q_{Omul}	δ/ppm
1	70.679	122.756	–9.567	0.071	0.003	1.484	–0.201	–0.317	563.2
2	71.061	122.671	–9.284	0.071	0.004	1.483	–0.209	–0.319	561.4
3	72.252	122.749	–9.047	0.071	0.007	1.481	–0.244	–0.322	526.9
4	72.092	122.819	–8.336	0.071	0.008	1.480	–0.240	–0.326	532.8
5	72.150	122.790	–9.012	0.071	0.006	1.481	–0.241	–0.322	545.7
6	65.144	122.617	–9.335	0.072	0.005	1.485	–0.215	–0.313	568.9
7	70.884	122.591	–8.930	0.072	0.003	1.485	–0.204	–0.313	570.1
8	70.633	122.540	–9.315	0.072	0.007	1.486	–0.196	–0.311	570.3
9	70.181	122.431	–9.140	0.072	0.003	1.487	–0.182	–0.305	593.6
10	68.864	122.302	–9.138	0.073	0.004	1.490	–0.143	–0.294	590.1
11	70.690	122.526	–9.298	0.072	0.005	1.486	–0.198	–0.319	575.0
12	74.926	123.365	–8.695	0.067	0.011	1.471	–0.324	–0.360	505.8
13	71.304	122.324	–9.336	0.073	0.006	1.489	–0.217	–0.307	555.0
14	67.203	121.716	–9.367	0.076	0.005	1.499	–0.093	–0.282	576.0
15	69.963	122.470	–9.366	0.072	0.006	1.487	–0.176	–0.309	573.0
16	70.688	122.499	–9.013	0.072	0.003	1.486	–0.198	–0.310	573.0
17	70.367	122.491	–8.962	0.072	0.003	1.486	–0.188	–0.312	569.3
18	69.915	122.457	–9.310	0.072	0.004	1.487	–0.175	–0.309	570.8
19	71.291	122.541	–9.483	0.072	0.003	1.485	–0.216	–0.311	568.4
20	69.495	122.448	–8.905	0.072	0.005	1.486	–0.162	–0.313	555.2
21	71.519	122.396	–9.437	0.073	0.004	1.488	–0.223	–0.303	574.5
22	70.580	122.597	–9.324	0.071	0.007	1.485	–0.195	–0.311	566.0
23	69.529	122.508	–8.894	0.072	0.006	1.486	–0.163	–0.313	562.3
24	74.885	123.200	–8.548	0.068	0.011	1.473	–0.323	–0.353	507.0
25	74.580	123.258	–8.341	0.068	0.011	1.473	–0.314	–0.355	516.2
26	75.864	123.104	–8.915	0.069	0.013	1.476	–0.351	–0.349	522.8
27	73.652	123.179	–8.188	0.068	0.009	1.474	–0.286	–0.355	512.1
28	74.466	123.250	–8.539	0.068	0.011	1.473	–0.310	–0.356	514.7
29	73.572	123.241	–8.215	0.068	0.012	1.473	–0.284	–0.355	511.8
30	74.560	123.263	–8.347	0.068	0.010	1.473	–0.313	–0.355	509.0
31	73.360	123.193	–8.353	0.068	0.011	1.474	–0.279	–0.357	510.0
32	74.192	123.283	–8.292	0.069	0.015	1.473	–0.302	–0.357	513.9
33	74.230	123.166	–8.570	0.069	0.011	1.475	–0.303	–0.351	518.2
34	75.069	123.302	–8.603	0.068	0.011	1.472	–0.327	–0.357	507.0

Table T3. continuation

No.	E_e/eV	E_{CC}/eV	Δ_{HL}/eV	σ_b/Å	σ_t/Å	D_{CC}/Å	Q_{C2mul}	Q_{Omul}	δ/ppm
35	74.719	123.219	–8.217	0.068	0.011	1.474	–0.317	–0.353	515.0
36	74.722	123.230	–8.629	0.068	0.010	1.473	–0.318	–0.354	509.0
37	74.194	123.138	–8.139	0.068	0.010	1.475	–0.303	–0.351	520.0
38	74.517	123.116	–8.155	0.069	0.010	1.475	–0.313	–0.349	512.0
39	75.052	123.188	–8.509	0.068	0.011	1.474	–0.328	–0.351	507.0
40	74.628	123.142	–8.202	0.069	0.012	1.475	–0.315	–0.350	513.0
41	70.289	122.517	–8.677	0.073	0.007	1.485	–0.186	–0.313	550.0
42	70.690	122.507	–9.224	0.072	0.005	1.486	–0.199	–0.315	585.0
43	73.273	122.264	–9.205	0.074	0.005	1.490	–0.275	–0.313	565.0
44	71.796	122.477	–9.004	0.071	0.008	1.486	–0.231	–0.322	545.0
45	70.738	122.356	–8.761	0.074	0.011	1.489	–0.200	–0.307	538.0
46	70.328	122.471	–8.461	0.073	0.008	1.487	–0.188	–0.305	560.0
47	74.358	123.155	–8.050	0.069	0.010	1.475	–0.307	–0.350	518.0
48	74.739	123.148	–8.062	0.069	0.010	1.475	–0.318	–0.348	505.0
49	74.237	123.024	–7.968	0.069	0.010	1.476	–0.304	–0.346	517.0
50	74.405	123.092	–7.888	0.069	0.010	1.476	–0.309	–0.346	513.0

[a]This data set was generated and used to build PLS models by Kiralj and Ferreira, *J. Phys. Chem. A* **2008**, *112*, 6134. [b]Names of samples and variables are from the original publication. [c]The ten samples in the external validation set are **2**, **5**, **7**, **10**, **22**, **26**, **27**, **34**, **41** and **49**. This selection is from the original publication. Table T4. The QSAR data set 4 for mouse cyclooxigenase-2 inhibition by imidazoles.[a,b,c]

Table T4. The QSAR data set 4 for mouse cyclooxigenase-2 inhibition by imidazoles.[a,b,c]

No.	Substituent	ClogP	MgVol/Lmol^{-1}	$B1_{X.2}$/Å	–log[IC_{50}/molL^{-1}]
1	H	3.09	2.37	1.00	6.16
3	3-F	3.24	2.39	1.00	6.62
4	4-F	3.24	2.39	1.00	6.72
5	2-Cl	3.56	2.49	1.80	5.89
6	3-Cl	3.81	2.49	1.00	7.10
8	2-CH_3	3.29	2.51	1.52	5.75
9	3-CH_3	3.59	2.51	1.00	6.22
10	4-CH_3	3.59	2.51	1.00	6.19
11	3-OCH_3	3.10	2.57	1.00	5.62
12	4-OCH_3	3.10	2.57	1.00	5.54
13	3,4-Cl_2	4.40	2.61	1.00	7.40
14	2,4-F_2	3.38	2.40	1.35	6.26
15	3,4-F_2	3.31	2.40	1.00	6.80
16	3-Cl-4-CH_3	4.24	2.63	1.00	6.64
17	2-CH_3-3-F	3.44	2.53	1.52	5.77

[a]This data set was generated and used to build a MLR model by Garg *et al.*, *Chem. Rev.* **2003**, *103*, 703 (Table 17). Two outliers are already excluded. [b]Names of samples and variables are from the original publication. [c]The two samples in the external validation set are **4** and **10**. This selection was made in this work.

ANALYSIS OF DATA SET 1

Table T5. Results for leave-*N*-out for the MLR model on data set 1.

N	Single LNO	Multiple LNO[a]	
	Q^2_{LNO}	$\langle Q^2_{LNO} \rangle$	$\sigma(Q^2_{LNO})$
1	0.7725	0.7725	0
2	0.7815	0.7717	0.0041
3	0.7741	0.7710	0.0123
4	0.7854	0.7732	0.0054
5	0.7841	0.7680	0.0101
6	0.7735	0.7649	0.0184
7	0.7710	0.7694	0.0159
8	0.7321	0.7692	0.0220
9	0.7786	0.7630	0.0255
10	0.7690	0.7721	0.0134
11	0.7718	0.7708	0.0116
12	0.7913	0.7578	0.0233
13	0.7576	0.7593	0.0381
14	0.7840	0.7611	0.0279
15	0.7815	0.7573	0.0217
16	0.7812	0.7676	0.0243
17	0.7818	0.7642	0.0505
18	0.7854	0.7527	0.0577
19	0.7948	0.7566	0.0368
20	0.8057	0.7515	0.0387
21	0.8070	0.7548	0.0262
22	0.7924	0.7599	0.0281
23	0.7699	0.7542	0.0324
24	0.7813	0.7486	0.0459
25	0.7669	0.7594	0.0218
26	0.7523	0.7594	0.0274
27	0.7757	0.7527	0.0268
28	0.7809	0.7486	0.0359
29	0.7837	0.7541	0.0274
30	0.7809	0.7302	0.0750
31	0.7913	0.7386	0.0587
32	0.7963	0.7433	0.0613
33	0.7801	0.7429	0.0589
34	0.7747	0.7503	0.0531
35	0.7791	0.7487	0.0552
36	0.7592	0.7446	0.0295
37	0.7842	0.7469	0.0310
Average	0.7787		
Standard Deviation	0.0140		

[a]Average values of Q^2_{LNO} and respective standard deviations are reported for multiple LNO (ten times reordered data set).

Table T6. Ten bootstrappings with HCA clustering (BH), PCA clustering (BP), and only with random selection (BR) for the MLR model on data set 1.

Bootstrapping	Q^2_{BH}	R^2_{BH}	Q^2_{BP}	R^2_{BP}	Q^2_{BR}	R^2_{BR}
1	0.7642	0.8229	0.8946	0.9141	0.7428	0.8045
2	0.8078	0.8597	0.7753	0.8371	0.7727	0.8163
3	0.7642	0.8200	0.7835	0.8375	0.7817	0.8439
4	0.7960	0.8485	0.7776	0.8442	0.7945	0.8483
5	0.8115	0.8628	0.8095	0.8520	0.7847	0.8315
6	0.8271	0.8675	0.7453	0.8259	0.7747	0.8330
7	0.7905	0.8377	0.7327	0.7994	0.8021	0.8446
8	0.7712	0.8309	0.7631	0.8218	0.7751	0.8307
9	0.7312	0.7981	0.7645	0.8221	0.7727	0.8247
10	0.7884	0.8431	0.8070	0.8523	0.8202	0.8595
Average	0.7852	0.8391	0.7853	0.8406	0.7821	0.8337
Stand. dev.	0.0281	0.0218	0.0453	0.0304	0.0206	0.0162
The model	0.7725	0.8301	0.7725	0.8301	0.7725	0.8301

Table T7. Twenty-five bootstrappings with HCA clustering (BH), PCA clustering (BP), and only with random selection (BR) for the MLR model on data set 1.

Bootstrapping	Q^2_{BH}	R^2_{BH}	Q^2_{BP}	R^2_{BP}	Q^2_{BR}	R^2_{BR}
1	0.7704	0.8253	0.7967	0.8417	0.8031	0.8565
2	0.8108	0.8603	0.7577	0.8466	0.7823	0.8434
3	0.7863	0.8406	0.7584	0.8111	0.7817	0.8295
4	0.7868	0.8482	0.7449	0.8269	0.7842	0.8299
5	0.7703	0.8243	0.7252	0.7924	0.7553	0.8237
6	0.7636	0.8285	0.8197	0.8763	0.7677	0.8178
7	0.7745	0.8342	0.8143	0.8540	0.8000	0.8582
8	0.8052	0.8538	0.7409	0.8009	0.7543	0.8171
9	0.7628	0.8245	0.7223	0.7878	0.7124	0.7801
10	0.7669	0.8303	0.6915	0.7286	0.7390	0.8175
11	0.8067	0.8587	0.8024	0.8501	0.7829	0.8462
12	0.8049	0.8509	0.6866	0.7879	0.7924	0.8401
13	0.7842	0.8447	0.8155	0.8598	0.8109	0.8562
14	0.7490	0.8210	0.8210	0.8640	0.7507	0.8109
15	0.8269	0.8761	0.8054	0.8533	0.7845	0.8439
16	0.8041	0.8457	0.8031	0.8442	0.7676	0.8282
17	0.7512	0.8149	0.8180	0.8661	0.7829	0.8318
18	0.8056	0.8542	0.7945	0.8512	0.8074	0.8585
19	0.7639	0.8226	0.7884	0.8455	0.8323	0.8751
20	0.7334	0.8035	0.7973	0.8602	0.8068	0.8483
21	0.7708	0.8365	0.7076	0.7917	0.8230	0.8726
22	0.8071	0.8515	0.7723	0.8268	0.9205	0.9331
23	0.7920	0.8457	0.7940	0.8448	0.7698	0.8263
24	0.7399	0.8036	0.7563	0.8151	0.7872	0.8426
25	0.8400	0.8808	0.8316	0.8689	0.7877	0.8293
Average	0.7831	0.8392	0.7746	0.8318	0.7875	0.8407
Stand. dev.	0.0271	0.0198	0.0430	0.0348	0.0384	0.0283
The model	0.7725	0.8301	0.7725	0.8301	0.7725	0.8301

Table T8. Ten **y**-randomizations for the MLR model on data set 1.

Randomization	Q^2	R^2
1	–0.0439	0.0912
2	–0.0380	0.1004
3	–0.1212	0.0442
4	–0.1801	0.0255
5	–0.0260	0.1561
6	–0.0847	0.0769
7	–0.1343	0.0458
8	–0.0167	0.1340
9	–0.1084	0.0571
10	–0.1866	0.0087
Maximum	–0.0167	0.1561
Average	–0.0940	0.0740
Standard deviation	0.0623	0.0471
The model	0.7725	0.8301

Table T9. Twenty-five **y**-randomizations for the MLR model on data set 1.

Randomization	Q^2	R^2
1	–0.0545	0.0881
2	–0.1419	0.0415
3	–0.0570	0.1166
4	–0.0697	0.1047
5	–0.0260	0.1561
6	–0.0847	0.0769
7	–0.1343	0.0458
8	–0.0167	0.1340
9	–0.1084	0.0571
11	–0.0326	0.1615
12	–0.0821	0.0825
13	–0.0895	0.0672
14	–0.1808	0.0212
15	–0.1146	0.0823
16	–0.1030	0.0619
17	–0.1217	0.0482
18	–0.1192	0.0584
19	–0.1153	0.0450
20	–0.0876	0.0547
21	–0.1808	0.0330
22	–0.0936	0.0709
23	–0.0998	0.0542
24	–0.1802	0.0111
25	–0.0378	0.0126
Maximum	–0.0167	0.1816
Average	–0.0943	0.0747
Standard deviation	0.0479	0.0455
The model	0.7725	0.8301

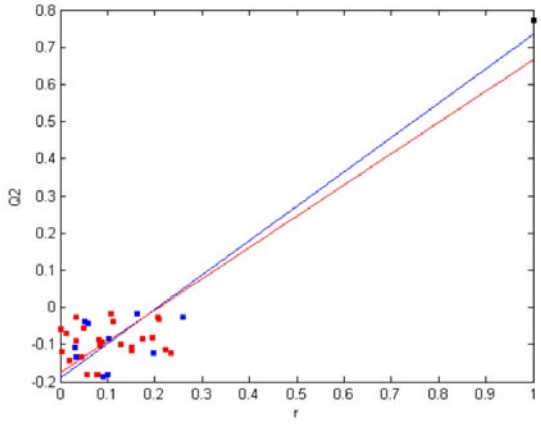

Figure F1. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the MLR model on data set 1: $Q^2 = –0.191 + 0.925\ r$ and $Q^2 = –0.176 + 0.842\ r$, respectively.

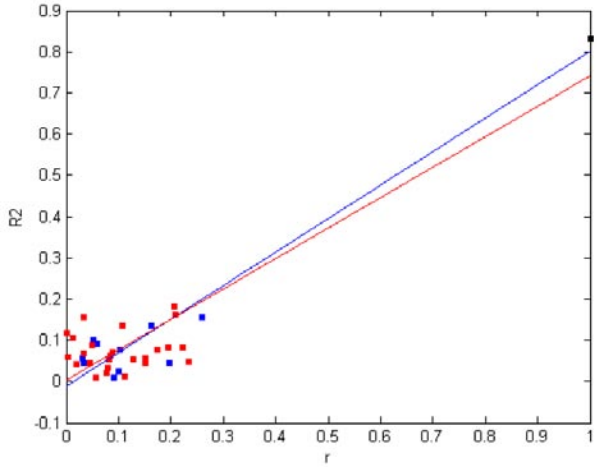

Figure F2. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the MLR model on data set 1: $R^2 = –0.012 + 0.813\ r$ and $R^2 = 0.003 + 0.738\ r$, respectively.

ANALYSIS OF DATA SET 2

Table T10. Results for leave-*N*-out for the PLS model on data set 2.

N	Single LNO	Multiple LNO[a]	
	Q^2_{LNO}	$<Q^2_{LNO}>$	$\sigma(Q^2_{LNO})$
1	0.8409	0.8409	0
2	0.8466	0.8415	0.0031
3	0.8394	0.8387	0.0059
4	0.8449	0.8387	0.0056
5	0.8448	0.8418	0.0059
6	0.8499	0.8346	0.0077
7	0.8277	0.8355	0.0048
8	0.8533	0.8394	0.0084
9	0.8342	0.8369	0.0105
10	0.8193	0.8418	0.0078
11	0.7739	0.8377	0.0128
12	0.8386	0.8313	0.0170
13	0.8493	0.8420	0.0098
14	0.7673	0.8405	0.0133
15	0.8291	0.8424	0.0060
16	0.8322	0.8418	0.0078
17	0.8293	0.8377	0.0085
18	0.7567	0.8125	0.0375
19	0.8316	0.8141	0.0345
20	0.8517	0.8292	0.0149
21	0.8554	0.8216	0.0206
22	0.8567	0.8308	0.0214
23	0.8553	0.8272	0.0192
24	0.8389	0.8210	0.0333
25	0.8481	0.8121	0.0348
26	0.8330	0.8194	0.0395
27	0.7881	0.8245	0.0417
28	0.7602	0.8367	0.0240

[a]Average values of Q^2_{LNO} and respective standard deviations are reported for multiple LNO (ten times reordered data set).

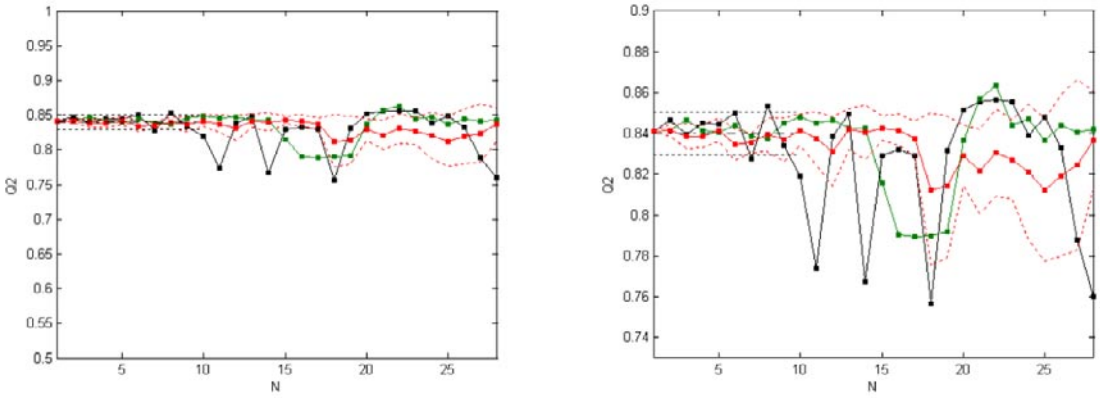

Figure F3. Leave-*N*-out crossvalidation plot for the PLS model on data set 2, showing the general trend (left) and details (right). Black - single LNO, red - multiple LNO (10 times). Single LNO: average Q^2 - dot-dash line, one standard deviation below and above the average - dotted lines. Multiple LNO: one standard deviation below and above the average - red dotted curved lines. Green - single LNO using the original (not randomized) data set.

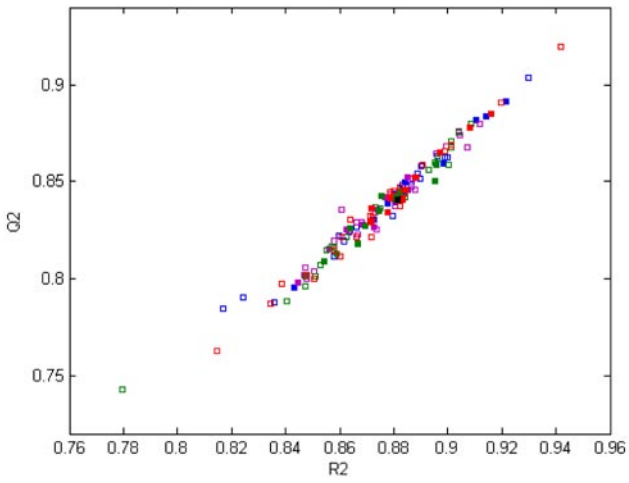

Figure F4. A comparative plot for bootstrappings for the PLS model on data set 2: the real model (black square), models from HCA-based bootstrappings (blue squares: 10 iterations - solid, 25 iterations - open), models from bootstrapping based on classes of Y (pink squares: 10 iterations - solid, 25 iterations - open), models from bootstrapping based MDR resistance classes (green squares: 10 iterations - solid, 25 iterations - open), and models from simple bootstrappings (red squares: 10 iterations - solid, 25 iterations - open).

Table T11. Ten bootstrappings with HCA clustering (BC), with classes of **y** (BY), with MDR resistance classes (BM) and only with random selection (BR) for the PLS model on data set 2.

Bootstrapping	Q^2_{BC}	R^2_{BC}	Q^2_{BY}	R^2_{BY}	Q^2_{BM}	R^2_{BM}	Q^2_{BR}	R^2_{BR}
1	0.8595	0.8983	0.8525	0.8853	0.8587	0.8958	0.8345	0.8778
2	0.8433	0.8820	0.8446	0.8822	0.8505	0.8954	0.8361	0.8716
3	0.8435	0.8810	0.7980	0.8447	0.8425	0.8755	0.8406	0.8833
4	0.8496	0.8841	0.8158	0.8559	0.8257	0.8640	0.8411	0.8787
5	0.8386	0.8777	0.8267	0.8729	0.8131	0.8590	0.8782	0.9083
6	0.8302	0.8729	0.8280	0.8687	0.8349	0.8744	0.8455	0.8848
7	0.8819	0.9104	0.8352	0.8739	0.8088	0.8542	0.8524	0.8878
8	0.8915	0.9215	0.8249	0.8624	0.8271	0.8695	0.8849	0.9159
9	0.8834	0.9140	0.8023	0.8468	0.8180	0.8665	0.8651	0.8971
10	0.7956	0.8434	0.8422	0.8766	0.8453	0.8825	0.8288	0.8717
Average	0.8517	0.8885	0.8270	0.8669	0.8325	0.8737	0.8507	0.8877
Stand. dev.	0.0288	0.0232	0.0178	0.0141	0.0167	0.0141	0.0192	0.0150
The model	0.8409	0.8814	0.8409	0.8814	0.8409	0.8814	0.8409	0.8814

Table T12. Twenty-five bootstrappings with HCA clustering (BC), with classes of **y** (BY), with MDR resistance classes (BM) and only with random selection (BR) for the PLS model on data set 2.

Bootstrapping	Q^2_{BC}	R^2_{BC}	Q^2_{BY}	R^2_{BY}	Q^2_{BM}	R^2_{BM}	Q^2_{BR}	R^2_{BR}
1	0.8630	0.8964	0.8272	0.8696	0.8416	0.8842	0.8118	0.8603
2	0.8623	0.8988	0.8459	0.8878	0.8599	0.8954	0.8654	0.8988
3	0.8119	0.8577	0.8246	0.8641	0.8751	0.9039	0.8018	0.8477
4	0.7878	0.8359	0.8001	0.8476	0.8159	0.8579	0.8445	0.8787
5	0.8222	0.8599	0.8227	0.8669	0.8801	0.9087	0.8322	0.8715
6	0.8484	0.8867	0.8800	0.9120	0.7887	0.8402	0.9198	0.9417
7	0.8484	0.8834	0.8058	0.8473	0.8147	0.8550	0.8210	0.8608
8	0.8195	0.8615	0.8676	0.9073	0.8563	0.8929	0.8909	0.9197
9	0.8539	0.8887	0.8763	0.9039	0.8072	0.8530	0.8213	0.8719
10	0.8467	0.8823	0.8375	0.8807	0.7426	0.7797	0.8003	0.8504
11	0.8241	0.8636	0.8642	0.8959	0.8679	0.9014	0.8689	0.9012
12	0.8450	0.8841	0.8431	0.8787	0.8442	0.8822	0.8454	0.8802
13	0.8320	0.8794	0.8356	0.8606	0.8368	0.8732	0.8376	0.8823
14	0.9035	0.9297	0.8738	0.9043	0.8358	0.8752	0.8585	0.8906
15	0.8455	0.8853	0.8439	0.8841	0.8410	0.8803	0.8315	0.8721
16	0.8440	0.8811	0.8251	0.8735	0.8620	0.8961	0.8438	0.8838
17	0.7844	0.8168	0.8468	0.8867	0.8584	0.9001	0.7630	0.8146
18	0.8416	0.8809	0.8468	0.8867	0.8710	0.9014	0.8214	0.8662
19	0.8517	0.8895	0.8681	0.8996	0.8213	0.8625	0.8146	0.8580
20	0.8624	0.8999	0.8195	0.8579	0.7962	0.8474	0.8300	0.8711
21	0.8578	0.8901	0.8342	0.8733	0.8013	0.8511	0.7871	0.8344
22	0.8395	0.8804	0.8290	0.8681	0.8403	0.8808	0.8520	0.8882
23	0.8262	0.8661	0.8292	0.8663	0.8016	0.8471	0.8302	0.8640
24	0.8458	0.8835	0.8037	0.8507	0.8419	0.8811	0.7972	0.8385
25	0.7902	0.8241	0.8514	0.8868	0.8166	0.8570	0.8470	0.8822
Average	0.8383	0.8762	0.8401	0.8784	0.8327	0.8723	0.8335	0.8732
Stand. dev.	0.0264	0.0244	0.0225	0.0188	0.0323	0.0284	0.0332	0.0268
The model	0.8409	0.8814	0.8409	0.8814	0.8409	0.8814	0.8409	0.8814

Table T13. Ten **y**-randomizations for the PLS model on data set 2.

Randomization	Q^2	R^2
1	0.0304	0.2332
2	–0.2744	0.0257
3	–0.1390	0.1047
4	–0.1468	0.1293
5	–0.2112	0.1165
6	–0.1667	0.1203
7	–0.1892	0.0728
8	–0.3055	0.0920
9	–0.1855	0.0938
10	–0.1616	0.1207
Maximum	0.0304	0.2332
Average	–0.1749	0.1109
Standard deviation	0.0901	0.0526
The model	0.8409	0.8814

Table T14. Twenty-five **y**-randomizations for the PLS model on data set 2.

Randomization	Q^2	R^2
1	–0.1859	0.0827
2	–0.1017	0.1257
3	–0.2452	0.0731
4	–0.1850	0.0602
5	–0.1861	0.1117
6	–0.0807	0.1708
7	–0.0462	0.1939
8	–0.1062	0.1289
9	–0.2632	0.0640
11	–0.0306	0.1461
12	–0.1365	0.1260
13	–0.1653	0.1317
14	–0.2246	0.0880
15	–0.1668	0.0995
16	–0.1735	0.1269
17	–0.1802	0.0521
18	–0.2296	0.0730
19	–0.2282	0.1212
20	–0.1912	0.0807
21	–0.2293	0.0516
22	–0.1348	0.1441
23	–0.2692	0.0333
24	–0.1812	0.1043
25	–0.0817	0.1492
Maximum	–0.0306	0.1939
Average	0.0662	0.0412
Standard deviation	0.0776	0.0508
The model	0.8409	0.8814

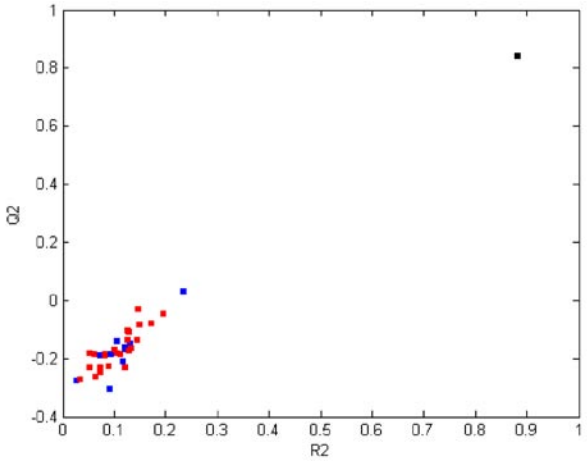

Figure F5. The **y**-randomization plot for the PLS model on data set 2: black square - the real model, blue squares - 10 randomized models, red squares - 25 randomized models.

Table T15. Comparative statistics of 10 and 25 **y**-randomizations for the PLS model on data set 2.

Parameter[a]	10 iterations	25 iterations
Maximum (Q^2_{yrand})	–0.030	–0.031
Maximum (R^2_{yrand})	0.233	0.194
Standard deviation (Q^2_{yrand})	0.090	0.078
Standard deviation (R^2_{yrand})	0.053	0.051
Minimum model-random. diff. (Q^2_{yrand})[b]	9.67	11.23
Minimum model-random. diff. (R^2_{yrand})[b]	12.32	13.53
Confidence level for min. diff. (Q^2_{yrand})[c]	<0.0001	<0.0001
Confidence level for min. diff. (R^2_{yrand})[c]	<0.0001	<0.0001
Randomizations %, conf. level > 0.0001 (Q^2_{yrand})[d]	0	0
Randomizations %, conf. level > 0.0001 (R^2_{yrand})[d]	0	0
y-Randomization intercept (r_{yrand} *vs.* Q^2_{yrand})[e]	–0.219	–0.262
y-Randomization intercept (r_{yrand} *vs.* R^2_{yrand})[e]	0.077	0.035

[a]Statistical parameters are calculated for Q^2 from from **y**-randomization (Q^2_{yrand}) and R^2 from **y**-randomization (R^2_{yrand}). [b]Minimum model-randomizations difference: the difference between the real model (Table 1) and the best **y**-randomization in terms of correlation coefficients Q^2_{yrand} or R^2_{yrand}, expressed in units of the standard deviations of Q^2_{yrand} or R^2_{yrand}, respectively. The best **y**-randomization is defined by the highest Q^2_{rand} or R^2_{rand}. [c]Confidence level for normal distribution of the minimum difference between the real and randomized models. [d]Percentage of randomizations characterized by the difference between the real and randomized models (in terms of Q^2_{yrand} or R^2_{yrand}) at confidence levels > 0.0001. [e]Intercepts obtained from two **y**-randomization plots for each regression model proposed. Q^2_{yrand} or R^2_{yrand} is the vertical axis, whilst the horizontal axis is the absolute value of the correlation coefficient r_{yrand} between the original and randomized vectors **y**. The randomization plots are completed with the data for the real model (r_{yrand} = 1.000, Q^2 or R^2).

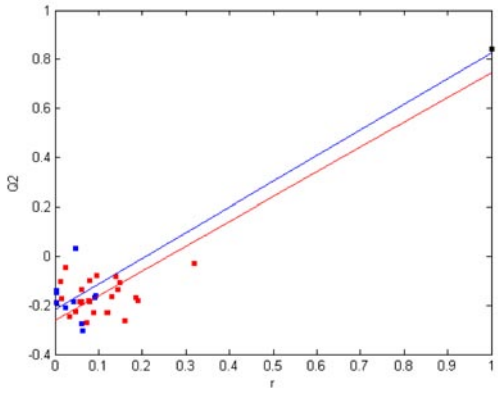

Figure F6. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the PLS model on data set 2: $Q^2 = -0.219 + 1.044\ r$ and $Q^2 = -0.262 + 1.007\ r$, respectively.

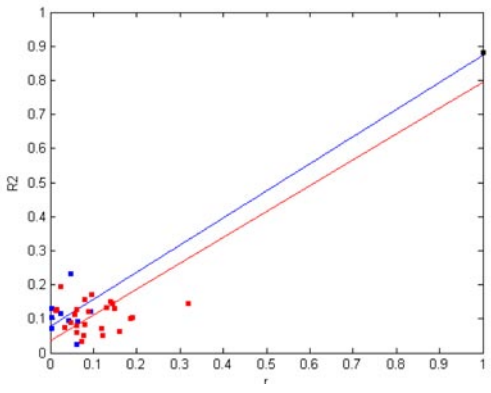

Figure F7. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the PLS model on data set 2: $R^2 = 0.077 + 0.7956\ r$ and $R^2 = 0.035 + 0.759\ r$, respectively.

ANALYSIS OF DATA SET 3

Table T16. Results for leave-*N*-out for the PLS model on data set 3.

N	Single LNO	Multiple LNO[a]	
	Q^2_{LNO}	$\langle Q^2_{LNO} \rangle$	$\sigma(Q^2_{LNO})$
1	0.8951	0.8951	0
2	0.8939	0.8949	0.0015
3	0.8774	0.8960	0.0028
4	0.8875	0.8917	0.0043
5	0.8965	0.8941	0.0058
6	0.8691	0.8896	0.0130
7	0.8982	0.8958	0.0039
8	0.8795	0.8935	0.0072
9	0.8868	0.8935	0.0068
10	0.8968	0.8926	0.0086
11	0.8937	0.8889	0.0127
12	0.8898	0.8849	0.0140
13	0.8926	0.8883	0.0105
14	0.9009	0.8902	0.0114
15	0.8717	0.8976	0.0067
16	0.8559	0.8963	0.0072
17	0.8892	0.8900	0.0187
18	0.8701	0.8863	0.0222
19	0.8915	0.8919	0.0125
20	0.8956	0.8750	0.0255
21	0.9120	0.8816	0.0242
22	0.9108	0.8781	0.0189
23	0.9091	0.8867	0.0110
24	0.9069	0.8854	0.0155
25	0.9066	0.8875	0.0156

[a]Average values of Q^2_{LNO} and respective standard deviations are reported for multiple LNO (ten times reordered data set).

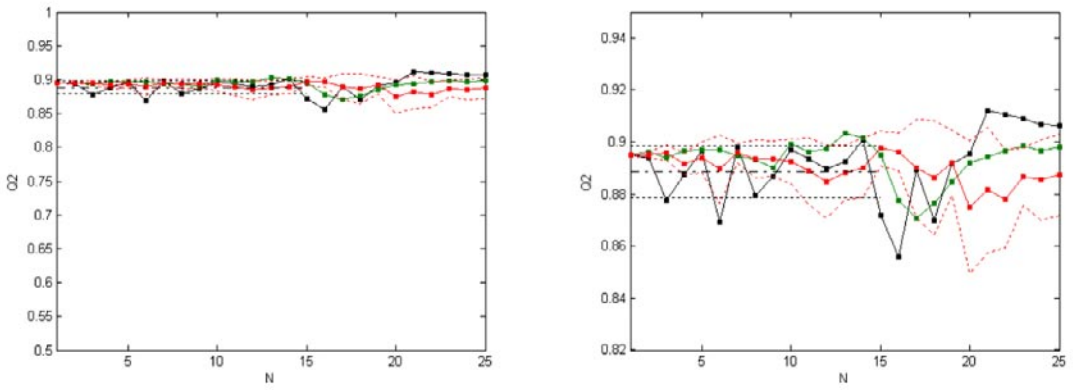

Figure F8. Leave-*N*-out crossvalidation plot for the PLS model on data set 3, showing the general trend (left) and details (right). Black - single LNO, red - multiple LNO (10 times). Single LNO: average Q^2 - dot-dash line, one standard deviation below and above the average - dotted lines. Multiple LNO: one standard deviation below and above the average - red dotted curved lines. Green - single LNO using the original (not randomized) data set.

Table T16. Ten bootstrappings with HCA clustering (BC), with classes of **y** (BY) and only with random selection (BR) for the PLS model on data set 3.

Bootstrapping	Q^2_{BC}	R^2_{BC}	Q^2_{BY}	R^2_{BY}	Q^2_{BR}	R^2_{BR}
1	0.8821	0.9108	0.8864	0.9130	0.8848	0.9102
2	0.8922	0.9185	0.8799	0.9066	0.8952	0.9209
3	0.8874	0.9178	0.8710	0.9003	0.8885	0.9209
4	0.8786	0.9050	0.8933	0.9179	0.9064	0.9324
5	0.8911	0.9161	0.8938	0.9175	0.8903	0.9172
6	0.9015	0.9246	0.8759	0.9038	0.8791	0.9076
7	0.8941	0.9222	0.8917	0.9148	0.9154	0.9394
8	0.8820	0.9086	0.8924	0.9202	0.8820	0.9092
9	0.8773	0.9095	0.9050	0.9281	0.8922	0.9190
10	0.8861	0.9111	0.9031	0.9262	0.8929	0.9176
Average	0.8872	0.9144	0.8892	0.9148	0.8927	0.9194
Standard deviation	0.0076	0.0064	0.0111	0.0092	0.0110	0.0101
The model	0.8951	0.9154	0.8951	0.9154	0.8951	0.9154

Table T17. Twenty-five bootstrappings with HCA clustering (BC), with classes of **y** (BY) and only with random selection (BR) for the PLS model on data set 3.

Bootstrapping	Q^2_{BC}	R^2_{BC}	Q^2_{BY}	R^2_{BY}	Q^2_{BR}	R^2_{BR}
1	0.8861	0.9119	0.9018	0.9215	0.8821	0.9106
2	0.9060	0.9309	0.8791	0.9061	0.9003	0.9233
3	0.8761	0.9034	0.8955	0.9225	0.8957	0.9203
4	0.8806	0.9076	0.8976	0.9178	0.8871	0.9128
5	0.8939	0.9182	0.8948	0.9225	0.8774	0.9039
6	0.8824	0.9092	0.9176	0.9390	0.9107	0.9316
7	0.8776	0.9069	0.8908	0.9163	0.8772	0.9036
8	0.8776	0.9069	0.8857	0.9106	0.8940	0.9182
9	0.8870	0.9124	0.9073	0.9260	0.8809	0.9055
10	0.8804	0.9090	0.8917	0.9151	0.8739	0.9013
11	0.8855	0.9126	0.8927	0.9190	0.9158	0.9347
12	0.8956	0.9172	0.9051	0.9288	0.8899	0.9171
13	0.8959	0.9216	0.8939	0.9172	0.8756	0.9028
14	0.8902	0.9193	0.8941	0.9165	0.8770	0.9042
15	0.8920	0.9086	0.8711	0.8998	0.8933	0.9177
16	0.8935	0.9168	0.8836	0.9091	0.8853	0.8982
17	0.8962	0.9216	0.8963	0.9199	0.8734	0.9013
18	0.8989	0.9146	0.8774	0.9037	0.8941	0.9177
19	0.9024	0.9292	0.9085	0.9308	0.8895	0.9148
20	0.8950	0.9231	0.8835	0.9089	0.8736	0.9017
21	0.8767	0.9048	0.8756	0.9035	0.9003	0.9293
22	0.9004	0.9310	0.8900	0.9165	0.9041	0.9139
23	0.8914	0.9154	0.8834	0.9102	0.9101	0.9347
24	0.8795	0.9119	0.8897	0.9154	0.8797	0.9057
25	0.8870	0.9124	0.9223	0.9294	0.8872	0.9108
Average	0.8891	0.9151	0.8932	0.9170	0.8891	0.9134
Standard deviation	0.0087	0.0078	0.0125	0.0094	0.0125	0.0110
The model	0.8951	0.9154	0.8951	0.9154	0.8951	0.9154

Table T18. Ten **y**-randomizations for the PLS model on data set 3.

Randomization	Q^2	R^2
1	–0.2014	0.0539
2	–0.1909	0.0582
3	–0.0200	0.1402
4	–0.0356	0.1401
5	–0.2101	0.0519
6	–0.1969	0.0178
7	–0.1950	0.0847
8	–0.1780	0.0358
9	–0.1458	0.0715
10	–0.5926	0.0692
Maximum	–0.0200	0.1402
Average	–0.1966	0.0723
Standard deviation	0.1553	0.0403
The model	0.8951	0.9154

Table T19. Twenty-five **y**-randomizations for the PLS model on data set 3.

Randomization	Q^2	R^2
1	–0.0928	0.1172
2	0.0671	0.2237
3	–0.2499	0.0504
4	–0.2531	0.0446
5	–0.1525	0.0732
6	–0.1101	0.0784
7	–0.0417	0.1719
8	–0.1675	0.0851
9	–0.0631	0.1259
11	–0.1041	0.0833
12	–0.1200	0.0750
13	–0.0770	0.1466
14	–0.1658	0.0514
15	–0.0236	0.1409
16	–0.0847	0.2243
17	–0.0874	0.1239
18	–0.2212	0.0261
19	–0.1092	0.0935
20	–0.1526	0.0813
21	–0.0401	0.1307
22	–0.1790	0.0864
23	–0.0561	0.1082
24	–0.1154	0.1088
25	–0.2619	0.0403
Maximum	0.0671	0.2243
Average	–0.1188	0.1037
Standard deviation	0.0776	0.0508
The model	0.8951	0.9154

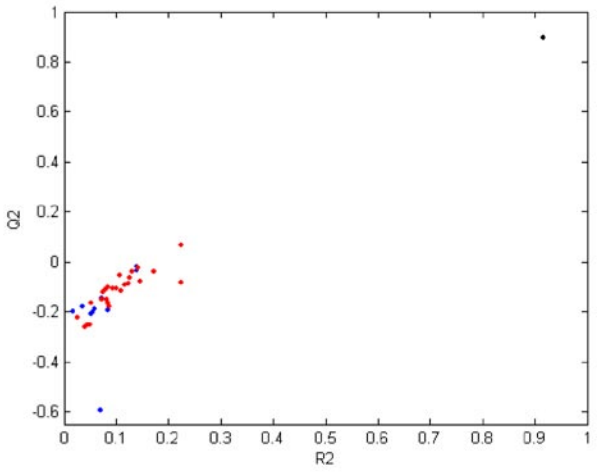

Figure F9. The **y**-randomization plot for the PLS model on data set 3: black ball - the real model, blue balls - 10 randomized models, red balls - 25 randomized models.

Table T20. Comparative statistics of 10 and 25 **y**-randomizations for the PLS model on data set 3.

Parameter[a]	10 iterations	25 iterations
Maximum (Q^2_{yrand})	–0.020	0.067
Maximum (R^2_{yrand})	0.140	0.224
Standard deviation (Q^2_{yrand})	0.155	0.078
Standard deviation (R^2_{yrand})	0.040	0.051
Minimum model-random. diff. (Q^2_{yrand})[b]	11.79	10.67
Minimum model-random. diff. (R^2_{yrand})[b]	19.24	13.60
Confidence level for min. diff. (Q^2_{yrand})[c]	<0.0001	<0.0001
Confidence level for min. diff. (R^2_{yrand})[c]	<0.0001	<0.0001
Randomizations %, conf. level > 0.0001 (Q^2_{yrand})[d]	0	0
Randomizations %, conf. level > 0.0001 (R^2_{yrand})[d]	0	0
y-Randomization intercept (r_{yrand} *vs.* Q^2_{yrand})[e]	–0.304	–0.231
y-Randomization intercept (r_{yrand} *vs.* R^2_{yrand})[e]	–0.004	0.016

[a]Statistical parameters are calculated for Q^2 from from **y**-randomization (Q^2_{yrand}) and R^2 from **y**-randomization (R^2_{yrand}). [b]Minimum model-randomizations difference: the difference between the real model (Table 1) and the best **y**-randomization in terms of correlation coefficients Q^2_{yrand} or R^2_{yrand}, expressed in units of the standard deviations of Q^2_{yrand} or R^2_{yrand}, respectively. The best **y**-randomization is defined by the highest Q^2_{rand} or R^2_{rand}. [c]Confidence level for normal distribution of the minimum difference between the real and randomized models. [d]Percentage of randomizations characterized by the difference between the real and randomized models (in terms of Q^2_{yrand} or R^2_{yrand}) at confidence levels > 0.0001. [e]Intercepts obtained from two **y**-randomization plots for each regression model proposed. Q^2_{yrand} or R^2_{yrand} is the vertical axis, whilst the horizontal axis is the absolute value of the correlation coefficient r_{yrand} between the original and randomized vectors **y**. The randomization plots are completed with the data for the real model (r_{yrand} = 1.000, Q^2 or R^2).

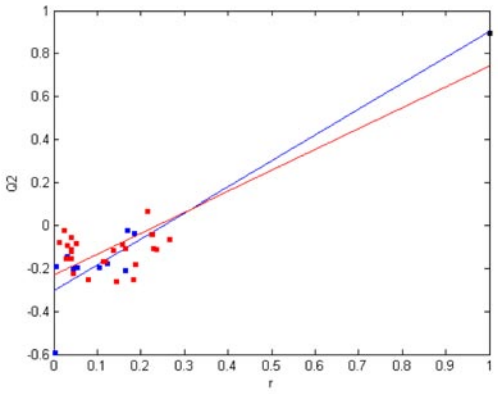

Figure F10. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the PLS model on data set 3: $Q^2 = -0.304 + 1.207\ r$ and $Q^2 = -0.231 + 0.972\ r$, respectively.

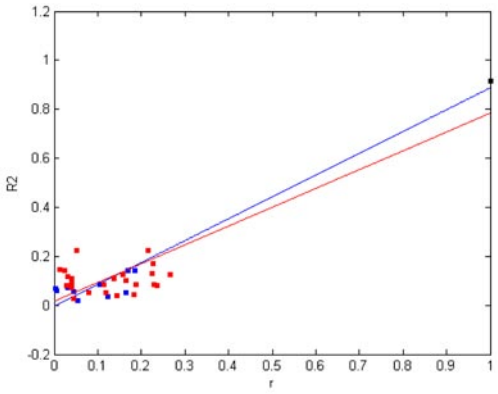

Figure F11. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from y-randomizations of the PLS model on data set 3: $R^2 = -0.004 + 0.891\ r$ and $R^2 = 0.016 + 0.768\ r$, respectively.

ANALYSIS OF DATA SET 4

Table T21. Results for leave-*N*-out for the MLR model on data set 4.

N	Single LNO	Multiple LNO[a]	
	Q^2_{LNO}	$\langle Q^2_{LNO} \rangle$	$\sigma(Q^2_{LNO})$
1	0.7977	0.7977	0
2	0.7093	0.8012	0.0284
3	0.7230	0.7460	0.0536
4	0.6846	0.7778	0.0664
5	0.8494	0.7713	0.0764
6	0.5663	0.6719	0.2721
7	0.7706	0.7178	0.1872

[a]Average values of Q^2_{LNO} and respective standard deviations are reported for multiple LNO (ten times reordered data set).

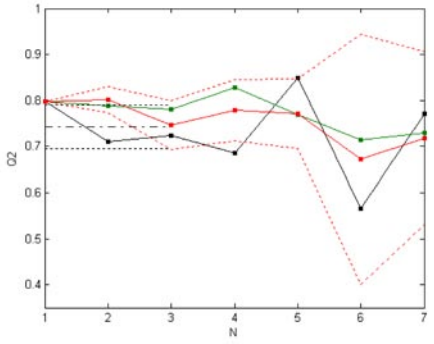

Figure F12. Leave-*N*-out crossvalidation plot for the MLR model on data set 4. Black - single LNO, red - multiple LNO (10 times). Single LNO: average Q^2 - dot-dash line, one standard deviation below and above the average - dotted lines. Multiple LNO: one standard deviation below and above the average - red dotted curved lines. Green - single LNO using the original (not randomized) data set.

Table T22. Ten bootstrappings with HCA clustering (BC) and only with random selection (BR) for the MLR model on data set 4.

Bootstrapping	Q^2_{BC}	R^2_{BC}	Q^2_{BR}	R^2_{BR}
1	0.7868	0.8937	0.8043	0.8979
2	0.7059	0.8739	0.8160	0.9076
3	0.7948	0.8963	0.8209	0.9108
4	0.6379	0.8682	0.8372	0.9171
5	0.7620	0.8647	0.7741	0.9000
6	0.7705	0.8801	0.6337	0.8880
7	0.7705	0.8801	0.7490	0.8872
8	0.5760	0.8551	0.8216	0.9117
9	0.7560	0.8755	0.8100	0.9023
10	0.7620	0.8647	0.7873	0.8888
Average	0.7322	0.8752	0.7865	0.8997
Stand. dev.	0.0716	0.0130	0.0564	0.0112
The model	0.7977	0.8857	0.7977	0.8857

Table T23. Twenty-five bootstrappings with HCA clustering (BC) and only with random selection (BR) for the MLR model on data set 4.

Bootstrapping	Q^2_{BC}	R^2_{BC}	Q^2_{BR}	R^2_{BR}
1	0.7868	0.8937	0.8876	0.9285
2	0.7796	0.8929	0.8543	0.9075
3	0.7298	0.8760	0.7764	0.8839
4	0.7721	0.8796	0.6932	0.8662
5	0.7664	0.8616	0.8042	0.9005
6	0.6773	0.8681	0.7314	0.8708
7	0.7462	0.8886	0.8334	0.9067
8	0.8372	0.9171	0.7796	0.8929
9	0.7620	0.8647	0.7033	0.8731
10	0.8106	0.9031	0.8145	0.8950
11	0.7835	0.8861	0.8065	0.9017
12	0.6306	0.8570	0.6998	0.8431
13	0.7721	0.8796	0.8074	0.9005
14	0.6953	0.8690	0.7939	0.8955
15	0.8160	0.9076	0.7879	0.8972
16	0.6379	0.8682	0.8158	0.9147
17	0.7059	0.8739	0.8100	0.9023
18	0.6993	0.8639	0.6827	0.8859
19	0.7873	0.8907	0.8069	0.9034
20	0.6379	0.8682	0.7879	0.8972
21	0.7705	0.8801	0.7764	0.8839
22	0.7930	0.8798	0.7796	0.8828
23	0.6345	0.8748	0.8224	0.8994
24	0.8074	0.9005	0.7344	0.8748
25	0.7764	0.8839	0.7873	0.8888
Average	0.7446	0.8811	0.7831	0.8919
Stand. dev.	0.0623	0.0153	0.0507	0.0175
The model	0.7977	0.8857	0.7977	0.8857

Table T24. Ten **y**-randomizations for the MLR model on data set 4.

Randomization	Q^2	R^2
1	–1.1201	0.0511
2	–1.0796	0.0494
3	–0.5260	0.1987
4	–0.6397	0.1189
5	–0.2905	0.2057
6	–0.5428	0.3060
7	–0.8073	0.0584
8	–0.3572	0.1894
9	–0.4147	0.1759
10	–0.2020	0.4037
Maximum	–0.2020	0.4037
Average	–0.5980	0.1757
Standard deviation	0.3164	0.1150
The model	0.7977	0.8857

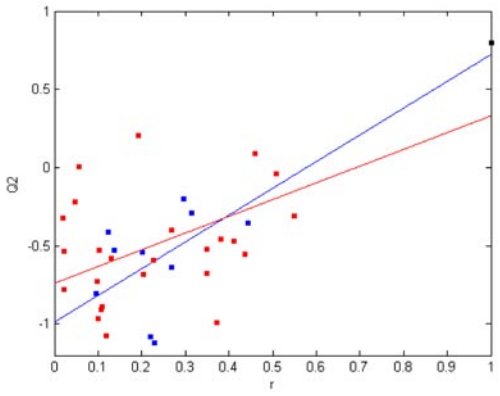

Figure F13. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the MLR model on data set 4: $Q^2 = –0.989 + 1.710\ r$ and $Q^2 = –0.739 + 1.069\ r$, respectively.

Table T25. Twenty-five **y**-randomizations for the MLR model on data set 4.

Randomization	Q^2	R^2
1	–0.6768	0.2281
2	–0.5245	0.2219
3	–0.6821	0.0685
4	–0.9890	0.1179
5	–0.3997	0.2255
6	–0.5940	0.1220
7	–0.5796	0.2874
8	–0.5530	0.2320
9	–0.3110	0.3728
10	–0.9104	0.0214
11	0.0926	0.5633
12	–0.7789	0.0541
13	–0.4595	0.1575
14	–0.2211	0.3617
15	–0.0381	0.4240
16	–0.8862	0.0185
17	–0.9625	0.0099
18	–1.0739	0.0114
19	0.0086	0.3491
20	–0.4680	0.2169
21	–0.5269	0.1176
22	–0.5318	0.1148
23	–0.7300	0.1343
24	0.2062	0.4832
25	–0.3210	0.2831
Maximum	0.2062	0.5633
Average	–0.5164	0.2079
Standard deviation	0.3409	0.1534
The model	0.7977	0.8857

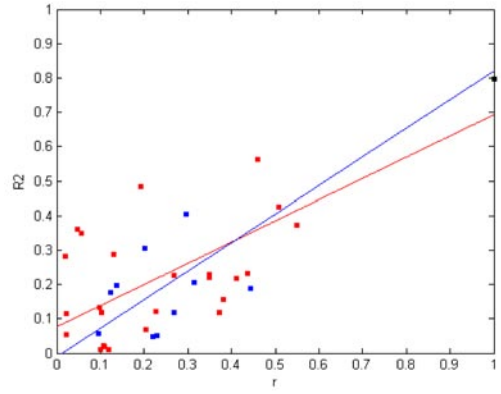

Figure F14. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the MLR model on data set 4: $R^2 = –0.011 + 0.830\ r$ and $R^2 = 0.077 + 0.616\ r$, respectively.

ANALYSIS OF DATA SUBSET 3

Table T26. The QSPR data subset 3 for carbonyl oxygen chemical shift in substituted benzaldehydes.[a,b,c]

No.	E_e/eV	E_{CC}/eV	Δ_{HL}/eV	σ_b/Å	σ_ρ/Å	D_{CC}/Å	Q_{C2mul}	Q_{Omul}	δ_{exp}/ppm
4	72.092	122.819	–8.336	0.071	0.008	1.480	–0.240	–0.326	532.8
6	65.144	122.617	–9.335	0.072	0.005	1.485	–0.215	–0.313	568.9
7	70.884	122.591	–8.930	0.072	0.003	1.485	–0.204	–0.313	570.1
8	70.633	122.540	–9.315	0.072	0.007	1.486	–0.196	–0.311	570.3
9	70.181	122.431	–9.140	0.072	0.003	1.487	–0.182	–0.305	593.6
13	71.304	122.324	–9.336	0.073	0.006	1.489	–0.217	–0.307	555.0
14	67.203	121.716	–9.367	0.076	0.005	1.499	–0.093	–0.282	576.0
19	71.291	122.541	–9.483	0.072	0.003	1.485	–0.216	–0.311	568.4
27	73.652	123.179	–8.188	0.068	0.009	1.474	–0.286	–0.355	512.1
32	74.192	123.283	–8.292	0.069	0.015	1.473	–0.302	–0.357	513.9
33	74.230	123.166	–8.570	0.069	0.011	1.475	–0.303	–0.351	518.2
36	74.722	123.230	–8.629	0.068	0.010	1.473	–0.318	–0.354	509.0
37	74.194	123.138	–8.139	0.068	0.010	1.475	–0.303	–0.351	520.0
46	70.328	122.471	–8.461	0.073	0.008	1.487	–0.188	–0.305	560.0
48	74.739	123.148	–8.062	0.069	0.010	1.475	–0.318	–0.348	505.0

[a]This data subset was generated from data set 3 (Table T3). [b]Names of samples and variables are from the original publication for data set 3. [c]The two samples in the external validation set are **7** and **37**. This selection is based on HCA analysis of this data subset.

Table T27. Results for leave-*N*-out for the PLS model on data subset 3.

N	Single LNO	Multiple LNO[a]	
	Q^2_{LNO}	$\langle Q^2_{LNO} \rangle$	$\sigma(Q^2_{LNO})$
1	0.7785	0.7785	0
2	0.7626	0.7811	0.0164
3	0.7787	0.7752	0.0281
4	0.8366	0.7738	0.0313
5	0.6233	0.7393	0.0672
6	0.6735	0.7593	0.0788
7	0.8214	0.7168	0.1231
Average[b]	0.7891		
Standard deviation[b]	0.0326		

[a]Average values of Q^2_{LNO} and respective standard deviations are reported for multiple LNO (ten times reordered data set). [b]Values calculated from Q^2_{LNO} for N =1, 2, 3, 4.

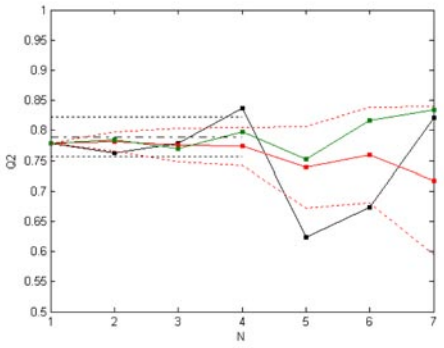

Figure F15. Leave-*N*-out crossvalidation plot for the PLS model on data subset 3. Black - single LNO, red - multiple LNO (10 times). Single LNO: average Q^2 - dot-dash line, one standard deviation below and above the average - dotted lines. Multiple LNO: one standard deviation below and above the average - red dotted curved lines. Green - single LNO using the original (not randomized) data set.

Table T28. Ten bootstrappings with HCA clustering (BC), with classes of Y (BY) and only with random selection (BR) for the PLS model on data subset 3.

Bootstrapping	Q^2_{BC}	R^2_{BC}	Q^2_{BY}	R^2_{BY}	Q^2_{BR}	R^2_{BR}
1	0.7879	0.9134	0.8176	0.8995	0.7479	0.8932
2	0.7773	0.9042	0.8176	0.8995	0.8541	0.9077
3	0.8567	0.9075	0.8495	0.9022	0.7501	0.8942
4	0.8176	0.8995	0.7970	0.9184	0.7556	0.8919
5	0.7505	0.8882	0.7695	0.8970	0.7890	0.9058
6	0.7251	0.8599	0.7186	0.8907	0.7611	0.8958
7	0.7293	0.8623	0.7498	0.8957	0.9065	0.9385
8	0.7959	0.9105	0.7479	0.8932	0.7342	0.8512
9	0.7511	0.9144	0.7627	0.8966	0.7501	0.8594
10	0.7695	0.8970	0.7505	0.8882	0.7405	0.8843
Average	0.7761	0.8957	0.7781	0.8981	0.7789	0.8922
Standard deviation	0.0406	0.0199	0.0407	0.0083	0.0568	0.0245
The model	0.7785	0.8968	0.7785	0.8968	0.7785	0.8968

Table T29. Twenty-five bootstrappings with HCA clustering (BC), with classes of Y (BY) and only with random selection (BR) for the PLS model on data subset 3.

Bootstrapping	Q^2_{BC}	R^2_{BC}	Q^2_{BY}	R^2_{BY}	Q^2_{BR}	R^2_{BR}
1	0.7475	0.8539	0.8063	0.9203	0.7792	0.9016
2	0.7705	0.8958	0.7099	0.8876	0.8567	0.9075
3	0.8176	0.8995	0.7374	0.8918	0.7214	0.8804
4	0.8495	0.9022	0.7302	0.8859	0.7293	0.8623
5	0.8495	0.9022	0.7879	0.9134	0.7444	0.8858
6	0.8567	0.9075	0.7296	0.8876	0.8176	0.8995
7	0.7959	0.9105	0.7348	0.8938	0.7501	0.8942
8	0.7479	0.8932	0.8063	0.9203	0.8541	0.9077
9	0.7479	0.8932	0.8098	0.9201	0.7296	0.8876
10	0.7342	0.8512	0.8063	0.9203	0.7706	0.8979
11	0.7394	0.8532	0.7879	0.9134	0.7382	0.8855
12	0.7505	0.8882	0.7695	0.8970	0.7475	0.8539
13	0.7292	0.8652	0.7879	0.9134	0.7231	0.9038
14	0.7511	0.9144	0.7348	0.8938	0.7501	0.8942
15	0.7342	0.8907	0.8017	0.9232	0.7465	0.8735
16	0.8093	0.8954	0.8567	0.9075	0.7367	0.8556
17	0.7292	0.8652	0.8531	0.9037	0.7183	0.8517
18	0.7498	0.8957	0.8314	0.9280	0.7542	0.8606
19	0.7496	0.8583	0.7970	0.9184	0.7342	0.8512
20	0.8148	0.9242	0.7380	0.8892	0.7628	0.9014
21	0.7501	0.8942	0.7099	0.8876	0.8202	0.9015
22	0.7511	0.9144	0.7879	0.9134	0.7496	0.8854
23	0.7556	0.8919	0.7498	0.8957	0.7475	0.8539
24	0.8531	0.9037	0.8196	0.9199	0.7705	0.8958
25	0.7296	0.8876	0.7348	0.8938	0.8559	0.9086
Average	0.7726	0.8901	0.7767	0.9056	0.7643	0.0201
Standard deviation	0.0437	0.0206	0.0432	0.0140	0.0427	0.0201
The model	0.7785	0.8968	0.7785	0.8968	0.7785	0.8968

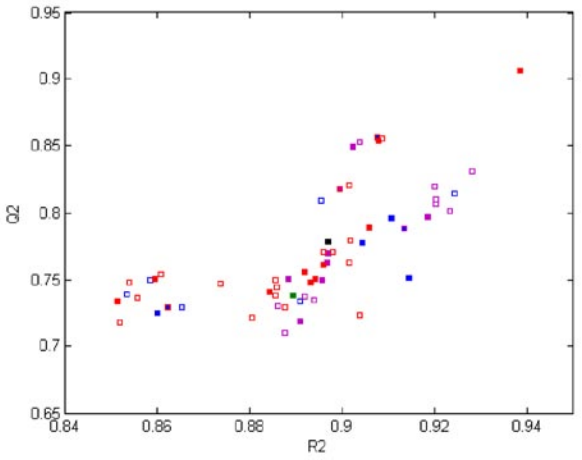

Figure F16. A comparative plot for bootstrappings for the PLS model on data subset 3: the real model (black square) its external validation (green square), models from HCA-based bootstrappings (blue squares: 10 iterations - solid, 25 iterations - open), models from bootstrapping based on classes of Y (pink squares: 10 iterations - solid, 25 iterations - open), , and models from simple bootstrappings (red squares: 10 iterations - solid, 25 iterations - open).

Table T30. Ten **y**-randomizations for the PLS model on data subset 3.

Randomization	Q^2	R^2
1	–1.0528	0.0931
2	–0.4425	0.3529
3	–0.1817	0.6157
4	–0.1583	0.4801
5	–0.1583	0.4801
6	0.0198	0.4445
7	–0.4868	0.4298
8	–0.8862	0.2171
9	–0.5164	0.3825
10	–1.2110	0.1653
Maximum	0.0198	0.6157
Average	–0.5074	0.3661
Standard deviation	0.4175	0.1619
The model	0.7785	0.8968

Table T31. Twenty-five **y**-randomizations for the PLS model on data subset 3.

Randomization	Q^2	R^2
1	–0.4923	0.2017
2	–0.4502	0.2120
3	–0.5006	0.3392
4	–0.6806	0.1838
5	–0.9556	0.2263
6	0.0029	0.4618
7	–0.1742	0.4167
8	0.2178	0.5924
9	–0.6725	0.1585
11	–0.5339	0.2831
12	–1.5136	0.1719
13	–0.4559	0.2486
14	–0.6581	0.3188
15	–1.1838	0.1467
16	–1.2932	0.2028
17	–0.4852	0.4049
18	–1.0034	0.0888
19	–1.2538	0.1834
20	–0.3780	0.3315
21	–0.6874	0.2471
22	–0.5331	0.1824
23	–1.3436	0.1321
24	0.1273	0.4754
25	–0.5868	0.3387
Maximum	0.2178	0.5924
Average	–0.6178	0.2830
Standard deviation	0.4669	0.1334
The model	0.7785	0.8968

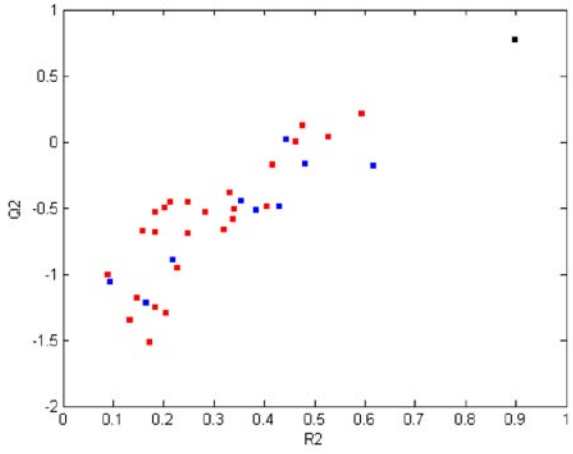

Figure F17. The **y**-randomization plot for the PLS model on data subset 3: black square - the real model, blue squares - 10 randomized models, red squares - 25 randomized models.

Table T32. Comparative statistics of 10 and 25 **y**-randomizations for the PLS model on data subset 3.

Parameter[a]	10 iterations	25 iterations
Maximum (Q^2_{yrand})	0.020	0.218
Maximum (R^2_{yrand})	**0.616**	**0.592**
Standard deviation (Q^2_{yrand})	**0.418**	**0.467**
Standard deviation (R^2_{yrand})	**0.162**	**0.133**
Minimum model-random. diff. (Q^2_{yrand})[b]	**1.82**	**1.20**
Minimum model-random. diff. (R^2_{yrand})[b]	**1.74**	**0.51**
Confidence level for min. diff. (Q^2_{yrand})[c]	**0.069**	**0.230**
Confidence level for min. diff. (R^2_{yrand})[c]	**0.082**	**0.610**
Randomizations %, conf. level > 0.0001 (Q^2_{yrand})[d]	**70%**	**80%**
Randomizations %, conf. level > 0.0001 (R^2_{yrand})[d]	**70%**	**100%**
y-Randomization intercept (r_{yrand} *vs.* Q^2_{yrand})[e]	-0.900	-0.958
y-Randomization intercept (r_{yrand} *vs.* R^2_{yrand})[e]	0.191	0.148

[a]Statistical parameters are calculated for Q^2 from from **y**-randomization (Q^2_{yrand}) and R^2 from **y**-randomization (R^2_{yrand}). Values typed bold represent obvious critical cases. [b]Minimum model-randomizations difference: the difference between the real model (Table 1) and the best **y**-randomization in terms of correlation coefficients Q^2_{yrand} or R^2_{yrand}, expressed in units of the standard deviations of Q^2_{yrand} or R^2_{yrand}, respectively. The best **y**-randomization is defined by the highest Q^2_{rand} or R^2_{rand}. [c]Confidence level for normal distribution of the minimum difference between the real and randomized models. [d]Percentage of randomizations characterized by the difference between the real and randomized models (in terms of Q^2_{yrand} or R^2_{yrand}) at confidence levels > 0.0001. [e]Intercepts obtained from two **y**-randomization plots for each regression model proposed. Q^2_{yrand} or R^2_{yrand} is the vertical axis, whilst the horizontal axis is the absolute value of the correlation coefficient r_{yrand} between the original and randomized vectors **y**. The randomization plots are completed with the data for the real model (r_{yrand} = 1.000, Q^2 or R^2).

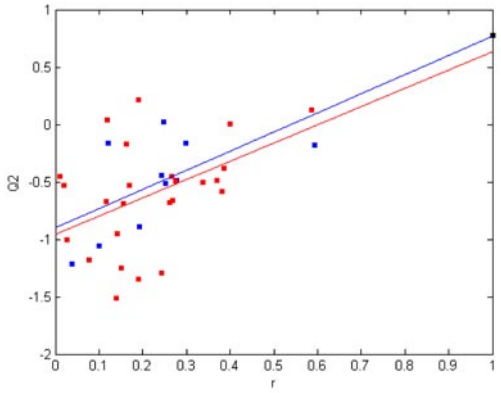

Figure F18. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the PLS model on data subset 3: $Q^2 = -0.900 + 1.667\ r$ and $Q^2 = -0.958 + 1.590\ r$, respectively.

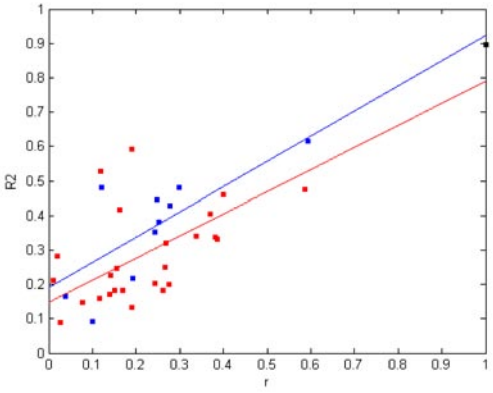

Figure F19. The plot for determining the linear regression equations for 10 (blue) and 25 (red) models from **y**-randomizations of the PLS model on data subset 3: $R^2 = -0.191 + 0.732\ r$ and $R^2 = 0.148 + 0.642\ r$, respectively.

SAMPLES REORDERING EFFECT ON LEAVE-*N*-OUT CROSSVALIDATION

The effect of sample randomization can be noticed when a model is validated by means of two LNO modes: a single LNO using the original (not reordered) data set, and a multiple LNO with the reordered (randomized) data. This is illustrated in the LNO plots for data sets 1 (Figure F20), 2 (Figure F3), 3 (Figure F8) and 4 (Figure F12), and subset 3 (Figure F15). Green curves are from single LNO for original data, compared to red curves for multiple LNO. The green curves do not show randomization effect on LNO for data set 1, probably due to relatively large number of samples and certain statistically insignificant **x** - **y** relationships, and also for subset 3. Data sets 2, 3 and 4, on the contrary, show green curves above the red curves from $N = 1$ to critical N at which Q^2_{LNO} is still stable.

The randomization effect on LNO is more obvious when Pearson correlation coefficients between all variables (descriptors and **y**) and the row index of **X** (*i.e.*, OrdNum, the ordinal number or position of a sample in a data set), are calculated for the original data, randomized data prior to LNO, new randomized data sets for single and multiple LNO (Tables T33 - T37 and Figure F21). This analysis shows significant correlations (absolute values of correlation coefficients over 0.30 are highlighted) between OrdNum and variables in two cases: a) small to moderate original data sets 2, 3, and 4 and subset 3 (15 - 56 samples); and b) small to moderate randomized data sets 3 and 4 and subset 3 (15 - 50 samples). The smaller the data set, the higher is the probability for chance correlation between OrdNum and variables, what results in virtually higher Q^2_{LNO} than in reality. By randomizing the original data, and especially by performing multiple LNO with several runs, one may reduce this chance correlation even for small data sets.

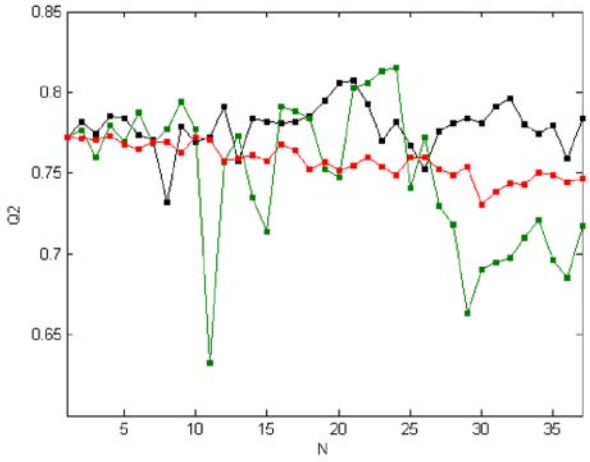

Figure F20. Comparative leave-*N*-out crossvalidation plot for the MLR model on data set 1. Black - single LNO, red - multiple LNO (10 times), and green - single LNO using the original (not randomized) data set.

Table T33. Correlation coefficients between the row index[a] of data set 1 and all variables[b] in single[c] and multiple[d] leave-*N*-out (LNO) crossvalidation runs.

Descriptor	Original	S-LNO	M-LNO-1	M-LNO-2	M-LNO-3	M-LNO-4	M-LNO-5	M-LNO-6	M-LNO-7	M-LNO-8	M-LNO-9	M-LNO-10
LogK_{ow}	–0.2076	0.0832	0.1072	0.0978	0.1571	–0.0886	0.0117	0.0431	0.1765	0.2014	–0.1055	0.1112
pK_a	–0.0761	–0.0937	–0.1219	0.0976	0.1256	–0.0248	0.0111	0.2204	0.1258	0.0695	0.0613	0.0335
E_{LUMO}	–0.1343	–0.0979	–0.1235	0.0970	0.1433	–0.0132	0.1278	0.0768	–0.0115	–0.0930	–0.0901	0.1255
E_{HOMO}	–0.1725	–0.0405	–0.1516	0.0210	0.0925	–0.0614	0.1131	0.1201	–0.0000	–0.0535	–0.0163	0.0931
N_{hdon}	0.0973	0.0680	–0.0453	0.0493	–0.1707	0.2014	0.0360	–0.0960	–0.2787	–0.0747	–0.0827	–0.0493
y	–0.2040	0.0317	0.0988	0.1269	0.1719	–0.1107	0.0226	0.0283	0.2049	0.1877	–0.0885	0.0766
AAR[e]	0.1486	0.0692	0.1080	0.0816	0.1435	0.0833	0.0537	0.0974	0.1329	0.1133	0.0741	0.0815

[a]The row index for **X** or **y** is the OrdNum, the ordinal number or position of a sample in the data set. [b]Molecular and other descriptors and the dependent variable *y*. [c]Single LNO using **X** with originally ordered (Original) and randomly reordered (S-LNO) samples. [d]Ten multiple LNO (M-LNO) run using **X** with randomly re-ordered samples. [e]Average of absolute correlation coefficients.

Table T34. Correlation coefficients[a] between the row index[b] of data set 2 and all variables[c] in single[d] and multiple[e] leave-*N*-out (LNO) crossvalidation runs.

Descriptor	Original	S-LNO	M-LNO-1	M-LNO-2	M-LNO-3	M-LNO-4	M-LNO-5	M-LNO-6	M-LNO-7	M-LNO-8	M-LNO-9	M-LNO-10
CYP51-g	–0.1755	0.0577	–0.1755	0.1755	0.1325	0.1599	0.0193	–0.1046	–0.0834	–0.0427	–0.0600	0.0711
CYP51-e	–0.1805	0.0696	–0.1642	0.1853	0.1165	0.1617	0.0223	–0.1024	–0.0703	–0.0323	–0.0628	0.0876
PMR1-t	–0.0267	–0.0829	0.1481	0.0639	–0.0831	0.1226	0.2091	0.1425	–0.1371	0.0362	–0.1062	0.0850
CYP51-e*Npi	0.1150	–0.1017	–0.1012	0.1380	0.1302	0.1437	–0.0248	–0.1104	–0.0887	–0.1016	–0.0347	0.0585
PCR*Npi	**0.3409**	–0.1957	–0.0578	0.0885	0.1172	0.0856	0.0026	–0.0663	–0.1499	–0.0892	0.0116	0.0363
PMR1-e*Lpi	0.1778	0.0039	0.0032	0.0689	–0.1401	0.0835	0.1316	0.0817	–0.0244	0.0362	–0.1283	–0.1462
CYP51-e*Lpi	0.2141	–0.0161	–0.1623	0.0593	0.0994	0.0598	0.0476	–0.0799	0.0109	–0.1216	0.0018	–0.0637
PCR*Lpi	**0.4860**	–0.0704	–0.1481	0.0131	0.0415	–0.0117	0.0812	–0.0202	–0.0018	–0.1113	0.0360	–0.1308
y	0.0143	–0.0038	0.0932	–0.2035	0.0764	–0.1299	–0.1297	–0.0601	0.1572	–0.0695	0.1218	–0.0827
AAR[f]	0.1923	0.0669	0.1171	0.1107	0.1041	0.1065	0.0742	0.0853	0.0804	0.0712	0.0626	0.0847

[a]Correlation coefficients with absolute value greater than 0.30 are typed bold and indicate chance correlation. [b]The row index for **X** or **y** is the OrdNum, the ordinal number or position of a sample in the data set. [c]Molecular and other descriptors and the dependent variable *y*. [d]Single LNO using **X** with originally ordered (Original) and randomly reordered (S-LNO) samples. [e]Ten multiple LNO (M-LNO) run using **X** with randomly re-ordered samples. [f]Average of absolute correlation coefficients.

Table T35. Correlation coefficients[a] between the row index[b] of data set 3 and all variables[c] in single[d] and multiple[e] leave-*N*-out (LNO) crossvalidation runs.

Descriptor	Original	S-LNO	M-LNO-1	M-LNO-2	M-LNO-3	M-LNO-4	M-LNO-5	M-LNO-6	M-LNO-7	M-LNO-8	M-LNO-9	M-LNO-10
E_e	**0.5076**	0.0949	0.1407	0.0575	–0.1888	0.0635	0.0045	–0.0507	0.1439	0.1214	0.1908	–0.1330
E_{CC}	**0.3455**	0.0906	0.1727	0.0167	–0.1716	0.0840	0.0846	–0.0124	0.1594	0.0196	0.2338	–0.0371
Δ_{HL}	**0.6466**	–0.0210	**0.3903**	0.0605	–0.1444	–0.0356	0.2341	0.0818	0.0718	0.0414	0.1616	–0.2051
σ_b	**–0.3140**	–0.0831	–0.1223	–0.0013	0.1629	–0.1262	–0.1400	0.0020	–0.1047	–0.0144	–0.2263	–0.0052
σ_r	**0.5748**	0.1643	**0.3680**	0.1362	–0.2463	–0.0196	0.1012	0.0084	0.1725	0.0745	0.1815	–0.2277
D_{CC}	**–0.3603**	–0.0880	–0.1727	–0.0157	0.1691	–0.1063	–0.0894	0.0176	–0.1446	–0.0101	–0.2385	0.0382
Q_{C2mul}	**–0.4845**	–0.1368	–0.1830	–0.0760	0.2348	–0.1148	–0.0253	0.0306	–0.2149	–0.0868	–0.1665	0.1153
Q_{Omul}	**–0.4416**	–0.1062	–0.2009	–0.0430	0.2013	–0.1228	–0.1201	0.0078	–0.1432	–0.0805	–0.2272	0.0694
y	**–0.4989**	–0.0814	–0.2411	–0.0496	0.2182	–0.0617	–0.1332	–0.0034	–0.1767	–0.1379	**–0.3076**	0.1470
AAR[f]	**0.4638**	0.0963	0.2213	0.0507	0.1930	0.0816	0.1036	0.0239	0.1480	0.0652	0.2149	0.1087

[a]Correlation coefficients with absolute value greater than 0.30 are typed bold and indicate chance correlation. [b]The row index for **X** or **y** is the OrdNum, the ordinal number or position of a sample in the data set. [c]Molecular and other descriptors and the dependent variable *y*. [d]Single LNO using **X** with originally ordered (Original) and randomly reordered (S-LNO) samples. [e]Ten multiple LNO (M-LNO) run using **X** with randomly re-ordered samples. [f]Average of absolute correlation coefficients.

Table T36. Correlation coefficients[a] between the row index[b] of data subset 3 and all variables[c] in single[d] and multiple[e] leave-*N*-out (LNO) crossvalidation runs.

Descriptor	Original	S-LNO	M-LNO-1	M-LNO-2	M-LNO-3	M-LNO-4	M-LNO-5	M-LNO-6	M-LNO-7	M-LNO-8	M-LNO-9	M-LNO-10
E_e	**0.6074**	–0.1385	–0.0138	**–0.3049**	**0.3157**	–0.1725	–0.2515	**0.4093**	–0.1385	–0.1385	–0.2413	**0.6744**
E_{CC}	**0.4509**	–0.0597	–0.2841	–0.1276	**0.4816**	0.0622	0.0004	0.2778	–0.0597	–0.0597	**–0.3364**	**0.4872**
Δ_{HL}	**0.5795**	–0.2181	–0.1522	–0.2237	0.1677	–0.0861	–0.1166	**0.4812**	–0.2181	–0.2181	**–0.4683**	**0.4326**
σ_b	**–0.4701**	0.0886	0.2385	0.2657	**–0.5246**	–0.1295	–0.0477	–0.2793	0.0886	0.0886	0.2317	**–0.4565**
σ_r	**0.5803**	0.1950	**–0.4131**	0.0696	**0.3157**	–0.0696	–0.2878	**0.5013**	0.1950	0.1950	**–0.6777**	**0.6267**
D_{CC}	**–0.4584**	0.0673	0.2586	0.1787	**–0.4668**	–0.0778	0.0021	**–0.3028**	0.0673	0.0673	**0.3091**	**–0.5068**
Q_{C2mul}	**–0.5163**	0.0910	0.2006	0.1692	**–0.5001**	–0.0444	0.0560	–0.2107	0.0910	0.0910	0.2682	**–0.6044**
Q_{Omul}	**–0.5114**	0.0611	0.2646	0.1746	**–0.4950**	–0.1096	0.0243	**–0.3742**	0.0611	0.0611	**0.3040**	**–0.5541**
y	**–0.5971**	0.0973	0.2155	0.1517	**–0.4268**	–0.0875	0.1800	**–0.3810**	**0.3282**	**0.5054**	**0.3307**	**–0.6955**
AAR[f]	**0.5302**	0.1130	0.2268	0.1851	**0.4104**	0.0933	0.1074	**0.3575**	0.1386	0.1583	**0.3519**	**0.5598**

[a]Correlation coefficients with absolute value greater than 0.30 are typed bold and indicate chance correlation. [b]The row index for **X** or **y** is the OrdNum, the ordinal number or position of a sample in the data set. [c]Molecular and other descriptors and the dependent variable *y*. [d]Single LNO using **X** with originally ordered (Original) and randomly reordered (S-LNO) samples. [e]Ten multiple LNO (M-LNO) run using **X** with randomly re-ordered samples. [f]Average of absolute correlation coefficients.

Table T37. Correlation coefficients[a] between the row index[b] of data set 4 and all variables[c] in single[d] and multiple[e] leave-*N*-out (LNO) crossvalidation runs.

Descriptor	Original	S-LNO	M-LNO-1	M-LNO-2	M-LNO-3	M-LNO-4	M-LNO-5	M-LNO-6	M-LNO-7	M-LNO-8	M-LNO-9	M-LNO-10
ClogP	**0.3623**	–0.0646	0.1501	–0.2715	**0.3010**	0.1021	–0.0234	0.1319	0.0371	–0.0141	**–0.5656**	0.0694
MgVol	**0.5268**	–0.2474	**–0.5023**	0.0793	**0.4343**	**0.4078**	0.2134	0.0831	–0.1529	0.1416	**–0.3588**	0.2681
$B1_{X.2}$	0.0482	–0.1585	0.0012	–0.1826	**–0.3049**	–0.0042	0.0657	0.0970	0.1525	–0.1741	0.2139	–0.2139
y	–0.0244	0.2429	**0.6429**	–0.2265	0.0638	–0.0759	–0.1541	0.0986	0.1250	–0.0460	**–0.5194**	–0.1308
AAR[f]	0.2404	0.1784	**0.3241**	0.1900	0.2760	0.1475	0.1142	0.1026	0.1169	0.0939	**0.4144**	0.1706

[a]Correlation coefficients with absolute value greater than 0.30 are typed bold and indicate chance correlation. [b]The row index for **X** or **y** is the OrdNum, the ordinal number or position of a sample in the data set. [c]Molecular and other descriptors and the dependent variable *y*. [d]Single LNO using **X** with originally ordered (Original) and randomly reordered (S-LNO) samples. [e]Ten multiple LNO (M-LNO) run using **X** with randomly re-ordered samples. [f]Average of absolute correlation coefficients.

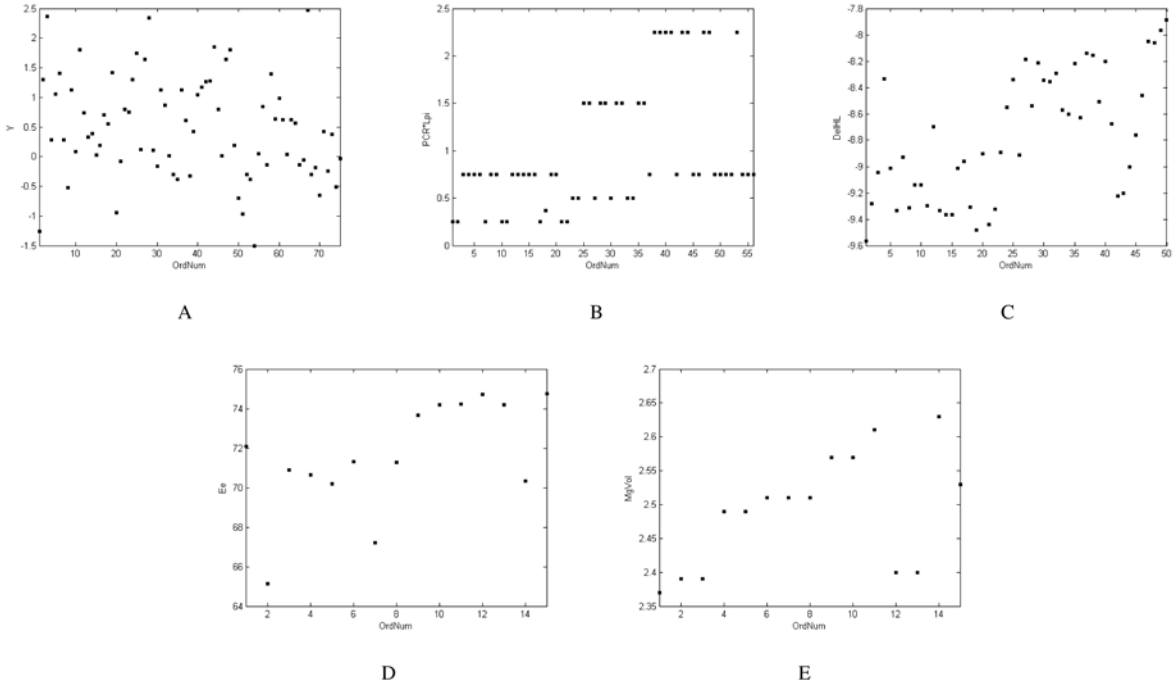

Figure F21. Representative chance correlations between the row index (OrdNum) and variables in the data sets with originally ordered samples: A) data set 1, B) data set 2, C) data set 3, D) data subset 3, and E) data set 4

SAMPLES REORDERING EFFECT ON y-RANDOMIZATION

When the same correlation analysis from LNO is performed for 10 + 25 data sets from **y**-randomization, which were obtained first by reordering (randomizing) the samples in the whole set and *a posteriori* randomizing only **y**, similar conclusions can be drawn (Table T38). Larger data sets 1 and 2 (75 and 50 samples) do not show significant correlation coefficients, data set 3 (50 samples) possesses one critical correlation, whilst data set 4 and subset 3 (15 samples) have ten correlation coefficients above 0.30.

When using the original instead of reordered data for 10 **y**-randomizations, the results show that there is no effect for larger sets 1 (Figure F22) and 2 (Figure F23), but is visible for smaller set 3 (Figure F24), subset 3 (Figure F25) and set 4 (Figure F26). The effect can be noticed as a shift of Q^2 and R^2 towards higher values relative to the normal **y**-randomization procedure.

Table T38. Correlation coefficients between **y** and OrdNum[a] in **y**-randomization.[b*]

	Set 1	Set 2	Set 3	Subset 3	Set 4
Original[c]	–0.2040	0.0143	**–0.4989**	**–0.5971**	–0.0244
Re-ordered[d]	0.0317	–0.0038	–0.0814	0.0973	0.2429
y-R10-1	0.1322	–0.1080	–0.2216	–0.0358	0.2452
y-R10-2	–0.1867	0.0140	–0.1235	0.0261	–0.0655
y-R10-3	0.1668	0.0479	–0.0663	–0.2572	**0.3567**
y-R10-4	0.0899	0.2588	0.0391	–0.0428	–0.1477
y-R10-5	–0.2235	0.2478	0.2140	–0.0098	0.0957
y-R10-6	0.0499	0.1844	–0.2932	**–0.5810**	0.1144
y-R10-7	0.0165	–0.0529	–0.1966	**0.3282**	0.1236
y-R10-8	–0.2058	0.0268	0.2203	**0.5054**	**0.3584**
y-R10-9	0.0441	–0.0935	–0.1300	–0.1778	0.1247
y-R10-10	–0.2310	–0.0352	0.1378	0.1291	–0.1359
y-R25-1	–0.1770	0.0550	0.0998	**–0.4141**	–0.0897
y-R25-2	–0.2189	–0.0423	–0.0054	0.0463	0.1377
y-R25-3	–0.1343	–0.0963	–0.1591	–0.1252	**0.4300**
y-R25-4	0.1972	–0.1300	0.0004	**–0.3551**	0.0362
y-R25-5	0.1405	–0.0487	0.1384	**–0.5050**	**–0.3774**
y-R25-6	–0.1792	0.0220	0.0531	0.0406	**–0.3354**
y-R25-7	–0.0087	–0.0124	–0.1452	**–0.5235**	0.1466
y-R25-8	–0.0691	–0.1661	**0.2999**	–0.1264	–0.0635
y-R25-9	0.0850	0.1182	–0.0999	0.2671	–0.1247
y-R25-10	0.2185	0.1239	–0.2131	0.1948	**0.3627**
y-R25-11	–0.1041	0.0767	0.1457	0.2815	0.1296
y-R25-12	–0.0937	0.1939	0.0193	–0.0004	**–0.3150**
y-R25-13	–0.1239	–0.0477	–0.1114	–0.1422	0.2440
y-R25-14	–0.0398	–0.0852	0.1172	0.2377	**0.5087**
y-R25-15	0.0653	–0.0496	–0.1009	**0.3419**	**–0.3966**
y-R25-16	–0.0387	0.0372	–0.2133	0.1810	–0.0957
y-R25-17	0.0280	–0.1866	–0.2335	0.0156	0.2558
y-R25-18	–0.2136	–0.0252	–0.0933	0.2555	–0.0463
y-R25-19	–0.1357	–0.0046	–0.1250	**–0.6297**	–0.0092
y-R25-20	0.1065	–0.0857	0.0651	**–0.3976**	–0.2409
y-R25-21	–0.0856	–0.0338	–0.0650	0.2878	–0.2365
y-R25-22	–0.0341	–0.0072	0.2350	**0.5616**	–0.2863
y-R25-23	–0.0363	–0.0059	0.2447	0.0034	0.2891
y-R25-24	–0.0628	0.0814	–0.2725	0.1871	**0.3090**
y-R25-25	–0.0180	0.0359	–0.0407	–0.0548	–0.1917
yR-AbsAver[e]	0.1132	0.0812	0.1411	0.2363	0.2122

[a]Pearson correlation coefficients are calculated for all 10 (y-R10) and 25 (y-R25) **y**-randomizations. [b]OrdNum, the ordinal number or position of a sample in the data set, is the row index for **X** or **y** is the OrdNum. [c]Originally ordered samples in a data set. [d]Re-ordered samples in a data set. [e]Average absolute value for all 10 + 25 **y**-randomizations. [*]All correlation coefficients greater than 0.30 are typed bold.

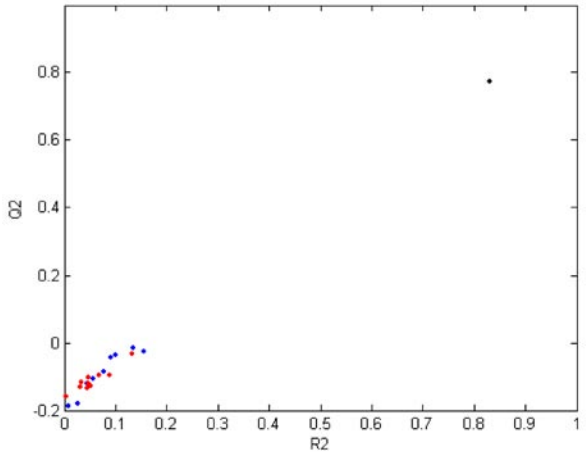

Figure F22. The effect of sample reordering to **y**-randomization plot for the MLR model on data set 1. Black ball - the real model, blue balls - 10 randomized models with re-ordered samples in **X**, and red balls - 10 randomized models with originally ordered samples in **X**. The studied effect cannot be observed.

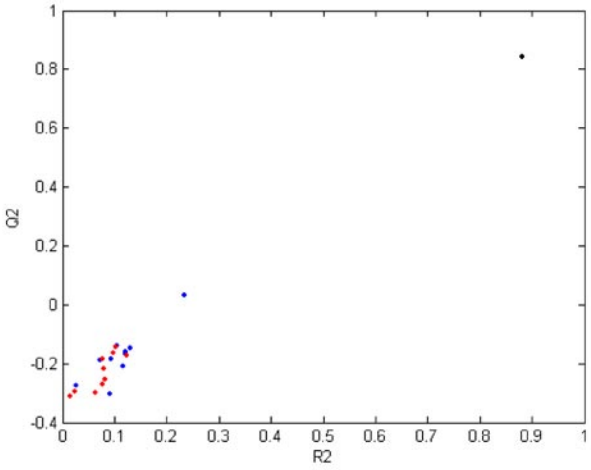

Figure F23. The effect of sample reordering to **y**-randomization plot for the PLS model on data set 2. Black ball - the real model, blue balls - 10 randomized models with re-ordered samples in **X**, and red balls - 10 randomized models with originally ordered samples in **X**. The studied effect cannot be observed.

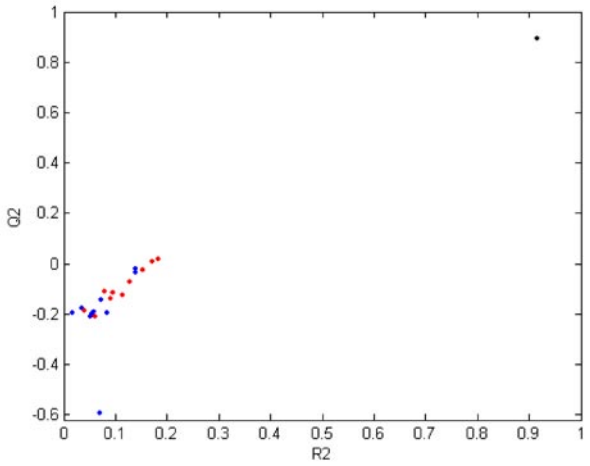

Figure F24. The effect of sample reordering to **y**-randomization plot for the PLS model on data set 3. Black ball - the real model, blue balls - 10 randomized models with re-ordered samples in **X**, and red balls - 10 randomized models with originally ordered samples in **X**. The studied effect can be noticed as the systematic shift of Q^2 and R^2 towards higher values.

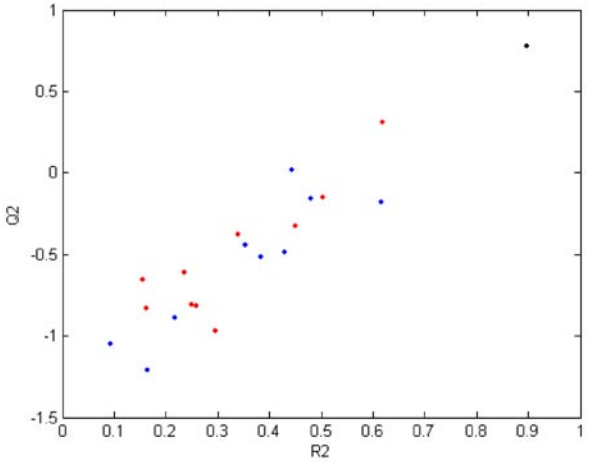

Figure F25. The effect of sample reordering to **y**-randomization plot for the PLS model on data subset 3. Black ball - the real model, blue balls - 10 randomized models with re-ordered samples in **X**, and red balls - 10 randomized models with originally ordered samples in **X**. The studied effect can be noticed as the systematic shift of Q^2 and R^2 towards higher values.

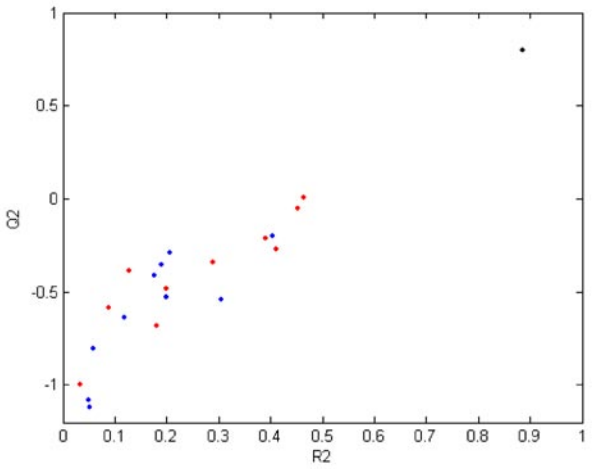

Figure F26. The effect of sample reordering to **y**-randomization plot for the MLR model on data set 4. Black ball - the real model, blue balls - 10 randomized models with re-ordered samples in **X**, and red balls - 10 randomized models with originally ordered samples in **X**. The studied effect can be noticed as the systematic shift of Q^2 and R^2 towards higher values.

ANALYSIS OF x - y RELATIONSHIPS

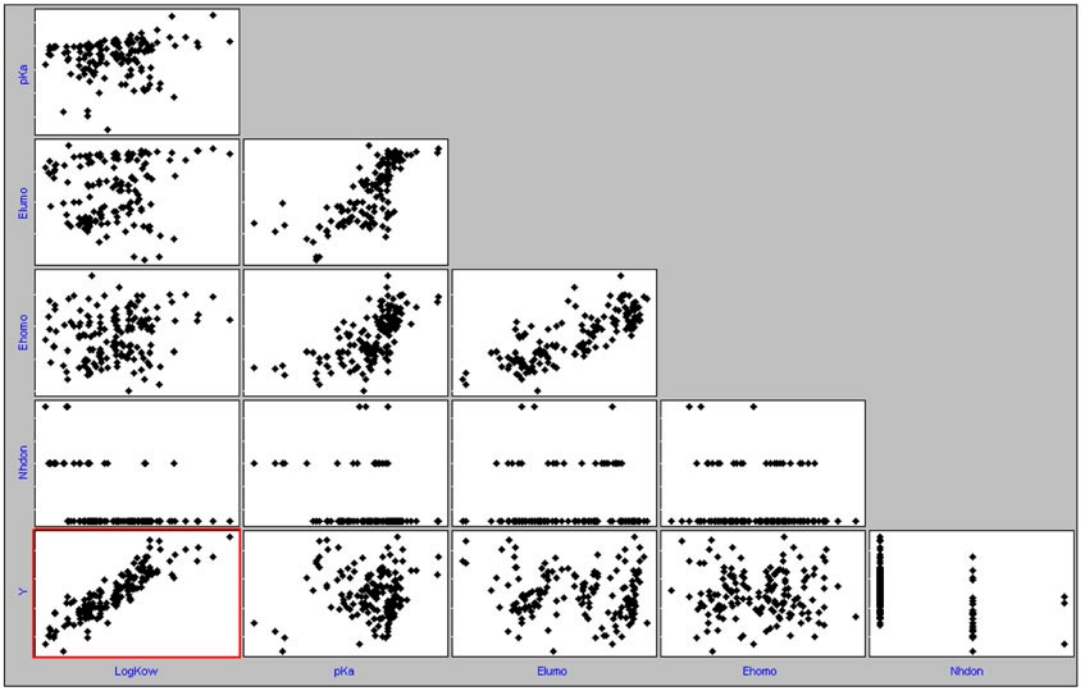

Figure F27. The scatterplots for the complete data set 1 (153 samples). The best **x** - **y** correlation profile is marked in red.

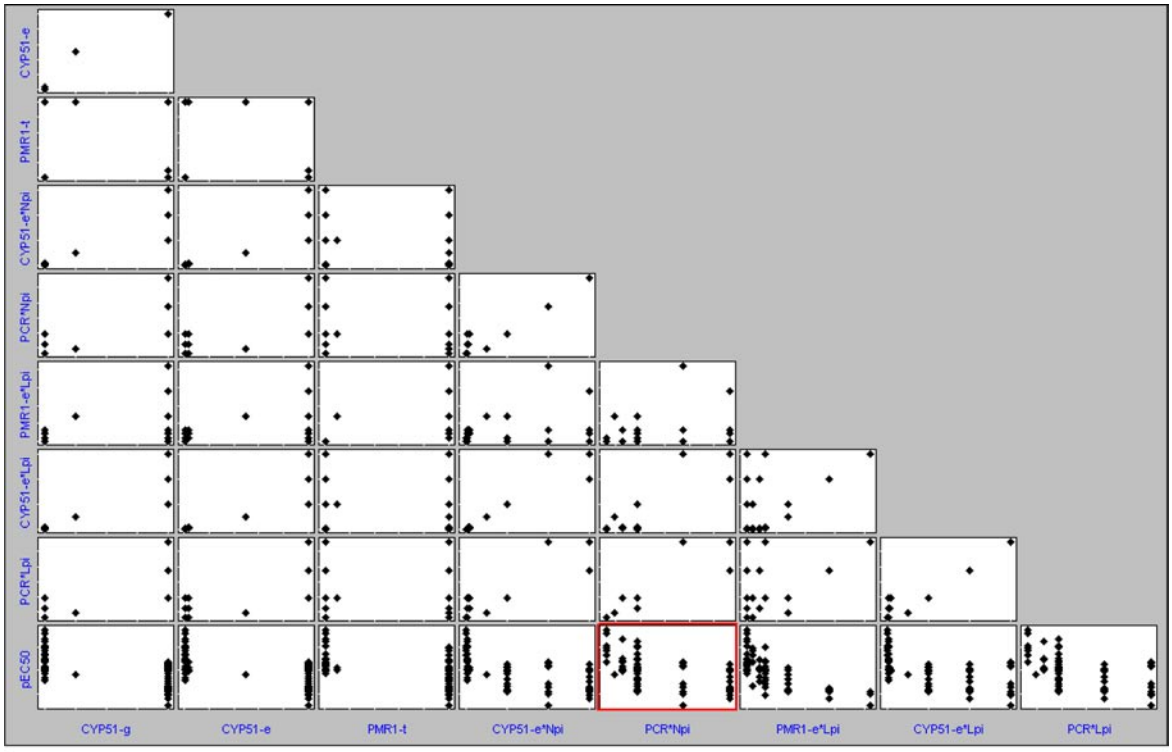

Figure F28. The scatterplots for the complete data set 2 (86 samples). The best **x** - **y** correlation profile is marked in red.

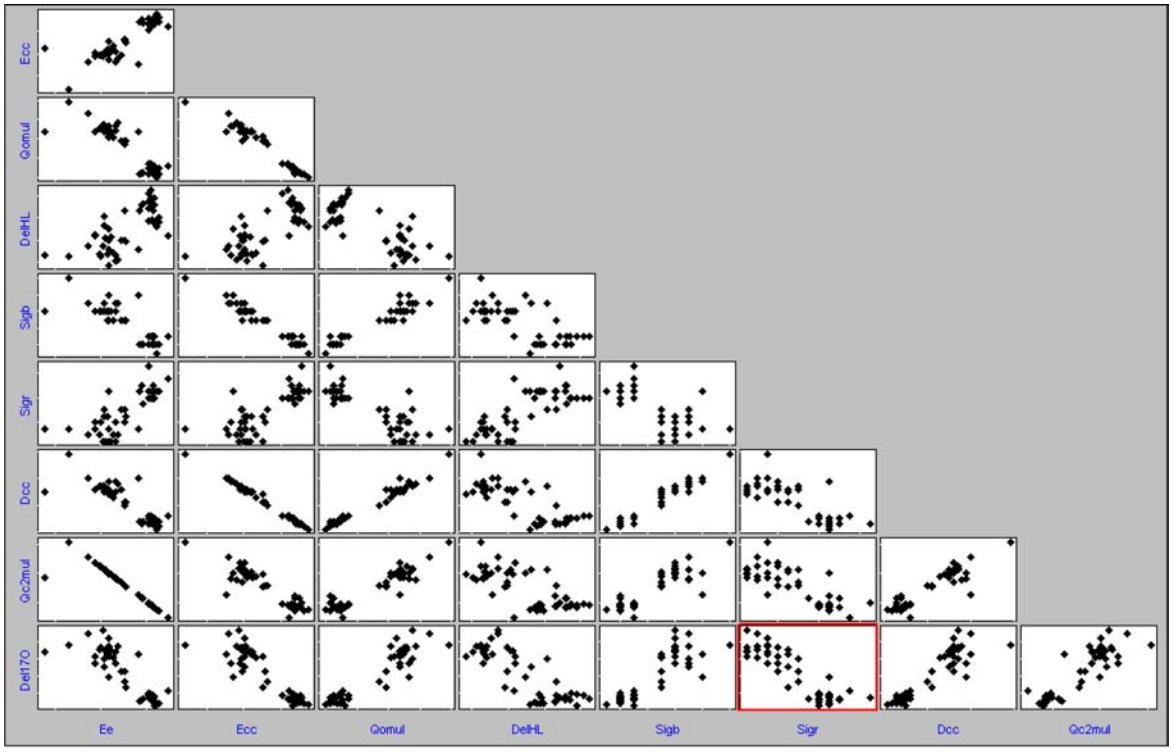

Figure F29. The scatterplots for the complete data set 3 (50 samples). The best **x** - **y** correlation profile is marked in red.

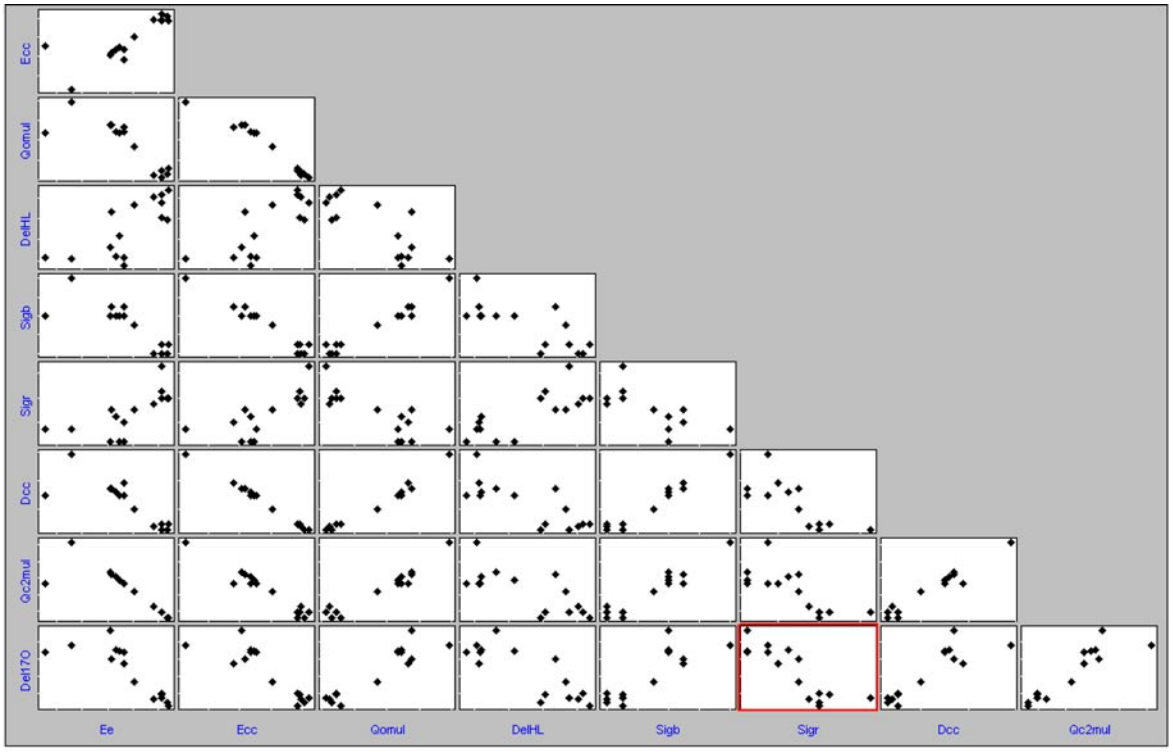

Figure F30. The scatterplots for the complete data subset 3 (15 samples). The best **x** - **y** correlation profile is marked in red.

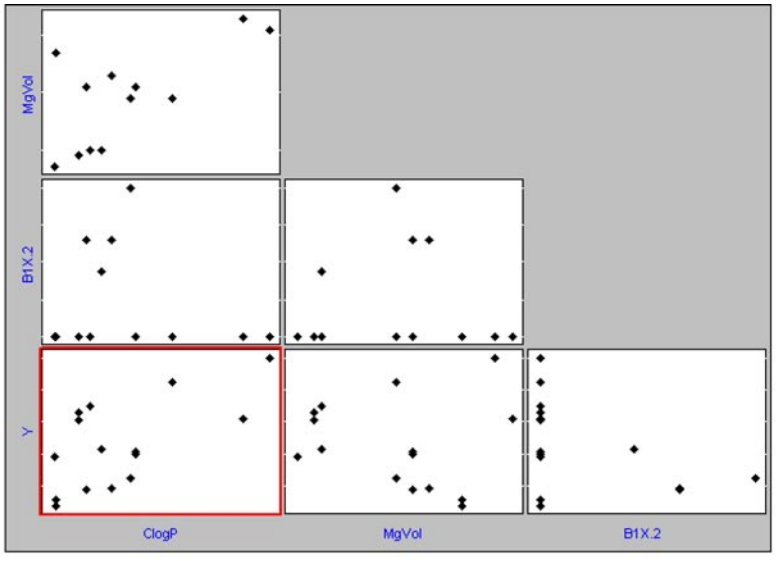

Figure F31. The scatterplots for the complete data set 4 (15 samples). The best **x** - **y** correlation profile is marked in red.

Table T39. Statistics for univariate descriptor - dependent variable (**x** - **y**) relationships in all the data sets and subsets studied.

Data set	Subset	n[a]	Descriptor[b]	R[c]	a (σ_a)[d]	b (σ_b)[d]	$t_{a,n-1}$ (p_a)[e]	$t_{b,n-1}$ (p_b)[e]	R^2[f]	$F_{1,n-2}$ (p)[g]
1	Complete set	153	LogK_{ow} [+]	0.881	–1.02(7)	0.63(3)	–14.0 (<0.0001)	22.8 (<0.0001)	0.776	522.0 (<0.0001)
			pK_a [+]	**0.025**	**0.4(4)**	**0.01(4)**	**0.9 (0.36)**	**0.3 (0.76)**	**0.0006**	**0.1 (0.76)**
			E_{LUMO} [–]	**–0.100**	**0.49(6)**	**–0.2(2)**	7.6 (<0.0001)	**1.2 (0.22)**	**0.010**	**1.5 (0.22)**
			E_{HOMO} [+]	**–0.006**	**0.4(20)**	**–0.02(22)**	**0.2 (0.86)**	**0.07 (0.94)**	**0.00003**	**0.005 (0.94)**
			N_{hdon} [+]	–0.410	1.4(2)	–0.7(1)	8.1 (<0.0001)	5.5 (<0.0001)	0.168	30.5 (<0.0001)
	Training set	75	LogK_{ow} [+]	0.890	–1.1(1)	0.64(4)	10.3 (<0.0001)	16.6 (<0.0001)	0.792	277.0 (<0.0001)
			pK_a [+]	**0.082**	**0.1(6)**	**0.04(6)**	**0.2 (0.86)**	**0.7 (0.48)**	**0.007**	**0.5 (0.48)**
			E_{LUMO} [–]	**–0.106**	**0.5(1)**	**–0.2(3)**	4.9 (<0.0001)	**0.9 (0.36)**	**0.011**	**0.8 (0.36)**
			E_{HOMO} [+]	**0.021**	**1.0(29)**	**0.3(3)**	**0.4 (0.73)**	**0.2 (0.86)**	**0.0004**	**0.03 (0.86)**
			N_{hdon} [+]	–0.408	1.3(2)	–0.7(2)	5.8 (<0.0001)	3.9 (0.0002)	0.170	14.9 (0.0002)
	External validation set	78	LogK_{ow} [+]	0.871	–0.97(10)	0.62(4)	9.3 (<0.0001)	15.5 (<0.0001)	0.759	238.8 (<0.0001)
			pK_a [+]	**–0.047**	**0.7(6)**	**–0.03(6)**	**1.3 (0.21)**	**0.4 (0.68)**	**0.002**	**0.2 (0.68)**
			E_{LUMO} [–]	**–0.093**	0.49(9)	**–0.2(2)**	5.8 (<0.0001)	**0.8 (0.42)**	**0.009**	**0.7 (0.42)**
			E_{HOMO} [+]	**–0.039**	**–0.4(28)**	**–0.1(3)**	**0.2 (0.87)**	**0.3 (0.74)**	**0.002**	**0.1 (0.74)**
			N_{hdon} [+]	–0.408	1.3(2)	–0.7(2)	5.8 (<0.0001)	3.9 (0.0002)	0.166	15.2 (0.0002)
2	Complete set	86	CYP51-g [–]	–0.722	6.9(1)	–0.27(3)	66.4 (<0.0001)	9.6 (<0.0001)	0.522	91.6 (<0.0001)
			CYP51-e [–]	–0.726	6.61(8)	–0.011(1)	80.7 (<0.0001)	9.7 (<0.0001)	0.528	93.8 (<0.0001)
			PMR1-t [–]	–0.502	6.6(1)	–0.008(2)	53.8 (<0.0001)	5.3 (<0.0001)	0.252	28.3 (<0.0001)
			CYP51-e*Npi [+]	–0.624	6.45(8)	–0.004(1)	76.0 (<0.0001)	7.3 (<0.0001)	0.389	53.5 (<0.0001)
			PCR*Npi [–]	–0.556	6.7(1)	–0.6(1)	54.2 (<0.0001)	6.1 (<0.0001)	0.309	37.5 (<0.0001)
			PMR1-e*Lpi [–]	–0.678	6.39(7)	–0.09(1)	87.3 (<0.0001)	8.4 (<0.0001)	0.459	71.3 (<0.0001)
			CYP51-e*Lpi [+]	–0.634	6.45(8)	–0.004(1)	76.9 (<0.0001)	7.5 (<0.0001)	0.402	56.4 (<0.0001)
			PCR*Lpi [–]	–0.564	6.7(1)	–0.6(1)	55.2 (<0.0001)	6.3 (<0.0001)	0.318	39.1 (<0.0001)
	Training set	56	CYP51-g [–]	–0.721	6.9(1)	–0.27(4)	50.7 (<0.0001)	7.6 (<0.0001)	0.519	58.3 (<0.0001)
			CYP51-e [–]	–0.726	6.6(1)	–0.011(2)	61.6 (<0.0001)	7.8 (<0.0001)	0.528	60.3 (<0.0001)
			PMR1-t [–]	–0.461	6.5(2)	–0.008(2)	39.6 (<0.0001)	3.8 (0.0003)	0.213	14.6 (<0.0001)
			CYP51-e*Npi [+]	–0.631	6.5(1)	–0.004(1)	58.7 (<0.0001)	6.0 (<0.0001)	0.398	35.7 (<0.0001)
			PCR*Npi [–]	–0.568	6.7(2)	–0.7(1)	42.4 (<0.0001)	5.1 (<0.0001)	0.322	25.7 (<0.0001)
			PMR1-e*Lpi [–]	–0.690	6.40(9)	–0.08(1)	68.9 (<0.0001)	7.0 (<0.0001)	0.476	49.0 (<0.0001)
			CYP51-e*Lpi [+]	–0.661	6.5(1)	–0.005(1)	60.9 (<0.0001)	6.5 (<0.0001)	0.437	42.0 (<0.0001)
			PCR*Lpi [–]	–0.590	6.7(2)	–0.7(1)	43.9 (<0.0001)	5.4 (<0.0001)	0.348	28.8 (<0.0001)
	External validation set	30	CYP51-g	–0.729	6.8(2)	–0.25(4)	42.4 (<0.0001)	5.6 (<0.0001)	0.531	31.7 (<0.0001)
			CYP51-e	–0.729	6.6(1)	–0.010(2)	51.6 (<0.0001)	5.6 (<0.0001)	0.531	31.7 (<0.0001)
			PMR1-t	–0.587	6.6(2)	–0.009(2)	37.3 (<0.0001)	3.8 (0.0006)	0.344	14.7 (0.0007)
			CYP51-e*Npi	–0.609	6.4(1)	–0.004(1)	47.3 (<0.0001)	4.1 (0.0003)	0.371	16.5 (0.0004)
			PCR*Npi	–0.529	6.6(2)	–0.6(2)	32.9 (<0.0001)	3.3 (0.003)	0.280	10.9 (0.003)
			PMR1-e*Lpi	–0.656	6.4(1)	–0.10(2)	51.8 (<0.0001)	4.6 (<0.0001)	0.430	21.1 (<0.0001)
			CYP51-e*Lpi	–0.579	6.4(1)	–0.004(1)	46.1 (<0.0001)	3.8 (0.0008)	0.336	14.1 (0.0008)
			CYP51-g	–0.510	6.6(2)	–0.5(2)	32.7 (<0.0001)	3.1 (0.004)	0.260	9.8 (0.004)
3	Complete set	50	E_e [–]	–0.856	1289(65)	–10.4(9)	19.8 (<0.0001)	11.5 (<0.0001)	0.733	131.7 (<0.0001)
			E_{CC} [–]	–0.892	8592(589)	–66(5)	14.6 (<0.0001)	13.7 (<0.0001)	0.796	187.0 (<0.0001)
			Δ_{HL} [–]	–0.827	111(42)	–49(5)	2.6 (0.01)	10.2 (<0.0001)	0.683	103.6 (<0.0001)
			σ_b [+]	0.862	–2650(69)	11437(971)	3.9 (0.0003)	11.8 (<0.0001)	0.743	138.7 (<0.0001)
			σ_r [–]	–0.891	602(5)	–7799(575)	123.9 (<0.0001)	13.6 (<0.0001)	0.793	183.9 (<0.0001)
			D_{CC} [+]	0.907	–5131(380)	3830(257)	13.5 (<0.0001)	14.9 (<0.0001)	0.823	222.4 (<0.0001)
			Q_{C2mul} [+]	0.892	641(8)	402(29)	85.0 (<0.0001)	13.6 (<0.0001)	0.795	185.9 (<0.0001)
			Q_{Omul} [+]	0.928	938(23)	1205(70)	40.8 (<0.0001)	17.3 (<0.0001)	0.862	298.8 (<0.0001)
	Training set	40	E_e [–]	–0.851	1250(71)	–10(1)	17.7 (<0.0001)	10.0 (<0.0001)	0.725	100.0 (<0.0001)
			E_{CC} [–]	–0.874	8295(700)	–63(6)	11.9 (<0.0001)	11.1 (<0.0001)	0.764	122.8 (<0.0001)
			Δ_{HL} [–]	–0.849	132(42)	–47(5)	3.2 (0.003)	9.9 (<0.0001)	0.721	98.1 (<0.0001)
			σ_b [+]	0.846	–236(80)	11020(1127)	3.0 (0.09)	9.8 (<0.0001)	0.716	95.7 (<0.0001)

Table T39. continuation

Data set	Subset	n[a]	Descriptor[b]	R[c]	a (σ_a)[d]	b (σ_b)[d]	$t_{a,n-1}$ (p_a)[e]	$t_{b,n-1}$ (p_b)[e]	R^2[f]	$F_{1,n-2}$ (p)[g]
3	Training set	40	σ_r [–]	–0.891	601(5)	–7674(635)	115.9 (<0.0001)	12.1 (<0.0001)	0.794	146.1 (<0.0001)
			D_{CC} [+]	0.894	–4954(448)	3710(302)	11.1 (<0.0001)	12.3 (<0.0001)	0.799	150.7 (<0.0001)
			Q_{C2mul} [+]	0.892	638(8)	392(32)	79.1 (<0.0001)	12.1 (<0.0001)	0.795	147.3 (<0.0001)
			Q_{Omul} [+]	0.915	921(30)	1152(82)	34.1 (<0.0001)	14.0 (<0.0001)	0.838	196.5 (<0.0001)
	External validation set	10	E_e	–0.901	1548(172)	–14(2)	9.0 (<0.0001)	5.9 (0.0002)	0.812	34.7 (0.0004)
			E_{CC}	–0.945	9715(1129)	–75(9)	8.6 (<0.0001)	8.1 (<0.0001)	0.892	66.1 (<0.0001)
			Δ_{HL}	–0.779	**11(149)**	–60(17)	**0.1 (0.95)**	3.5 (0.007)	0.607	12.4 (0.008)
			σ_b	0.905	–367(150)	12904(2146)	2.4 (0.04)	6.0 (0.0002)	0.819	36.2 (0.0003)
			σ_r	–0.889	610(15)	–8437(1537)	41.7 (<0.0001)	5.5 (0.0004)	0.790	30.1 (0.0006)
			D_{CC}	0.946	–5817(773)	4295(522)	7.5 (<0.0001)	8.2 (<0.0001)	0.895	67.6 (<0.0001)
			Q_{C2mul}	0.901	661(22)	464(79)	30.0 (<0.0001)	5.9 (0.0002)	0.812	34.6 (0.0004)
			Q_{Omul}	0.978	1021(37)	1444(109)	27.8 (<0.0001)	13.3 (<0.0001)	0.957	176.0 (<0.0001)
4	Complete set	15	ClogP [+]	0.632	3(1)	0.9(3)	3.0 (0.009)	2.9 (0.011)	0.400	8.7 (0.01)
			MgVol [–]	**–0.107**	**8(5)**	**–0.7(18)**	**1.8 (0.10)**	**0.4 (0.70)**	**0.012**	**0.2 (0.70)**
			B1$_{X,2}$ [–]	–0.451	7.4(6)	**–0.9(5)**	12.1 (<0.0001)	**1.8 (0.09)**	0.203	**3.3 (0.09)**
	Training set	13	ClogP [+]	0.698	3(1)	1.0(3)	2.7 (0.02)	3.2 (0.007)	0.487	10.4 (0.008)
			MgVol [–]	–0.041	7(5)	–0.3(21)	1.4 (0.20)	0.1 (0.89)	0.002	0.02 (0.89)
			B1$_{X,2}$ [–]	–0.449	7.4(7)	**–0.9(6)**	10.9 (<0.0001)	**1.7 (0.12)**	0.201	**2.8 (0.12)**
Sub-1	Complete set	15	LogK_{ow} [+]	0.861	–1.0(3)	0.6(1)	3.6 (0.003)	6.1 (<0.0001)	0.741	37.1 (<0.0001)
			pK_a [+]	**0.115**	**–0.04(130)**	**0.06(14)**	**0.03 (0.97)**	**0.4 (0.68)**	**0.013**	**0.2 (0.68)**
			E_{LUMO} [–]	**–0.174**	**0.4(3)**	**–0.4(6)**	**1.7 (0.1)**	**0.6 (0.53)**	**0.030**	**0.4 (0.53)**
			E_{HOMO} [–]	**0.017**	**0.9(69)**	**0.05(75)**	**0.13 (0.90)**	**0.06 (0.95)**	**0.0003**	**0.004 (0.95)**
			N_{hdon} [–]	–0.416	1.4(6)	**–0.7(4)**	2.3 (0.04)	**1.6 (0.12)**	0.173	**2.7 (0.12)**
Sub-3	Complete set	15	E_e [–]	–0.816	1166(122)	-9(2)	9.5 (<0.0001)	5.1 (0.0002)	0.666	25.9 (0.0002)
			E_{CC} [–]	–0.859	7650(1176)	–58(10)	6.5 (<0.0001)	6.0 (<0.0001)	0.737	36.5 (<0.0001)
			Δ_{HL} [–]	–0.827	**128(79)**	–48(9)	**1.6 (0.13)**	5.3 (0.0001)	0.683	28.0 (0.0001)
			σ_b [+]	0.846	**–219(134)**	10771(1884)	**1.6 (0.12)**	5.7 (<0.0001)	0.716	32.7 (<0.0001)
			σ_r [–]	–0.855	601(10)	–7417(1248)	58.5 (<0.0001)	5.9 (<0.0001)	0.731	35.3 (<0.0001)
			D_{CC} [+]	0.872	–4532(791)	3426(534)	5.7 (<0.0001)	6.4 (<0.0001)	0.760	41.2 (<0.0001)
			Q_{C2mul} [+]	0.894	643(14)	412(57)	45.6 (<0.0001)	7.2 (<0.0001)	0.800	51.9 (<0.0001)
			Q_{Omul} [+]	0.920	913(43)	1129(133)	21.0 (<0.0001)	8.5 (<0.0001)	0.847	72.1 (<0.0001)
	Training set	13	E_e [–]	–0.814	1151(131)	–9(2)	8.8 (<0.0001)	4.6 (0.0006)	0.662	21.5 (0.0007)
			E_{CC} [–]	–0.857	7499(1264)	–57(10)	5.9 (<0.0001)	5.5 (0.0001)	0.734	30.3 (0.0002)
			Δ_{HL} [–]	–0.826	**123(87)**	–47(10)	**1.4 (0.18)**	4.9 (0.0004)	0.682	23.6 (0.0005)
			σ_b [+]	0.841	**–229(150)**	10891(2111)	**1.5 (0.15)**	5.2 (0.0002)	0.708	26.6 (0.0003)
			σ_r [–]	–0.844	603(12)	–7592(1452)	49.7 (<0.0001)	5.2 (0.0002)	0.713	27.3 (0.0003)
			D_{CC} [+]	0.868	–4432(858)	3358(579)	5.1 (0.0002)	5.8 (<0.0001)	0.754	33.6 (0.0001)
			Q_{C2mul} [+]	0.889	641(16)	408(63)	41.2 (<0.0001)	6.4 (<0.0001)	0.789	41.2 (<0.0001)
			Q_{Omul} [+]	0.918	910(48)	1124(147)	19.1 (<0.0001)	7.7 (<0.0001)	0.843	58.9 (<0.0001)

[a]Number of samples in a given data set or its subset.

[b]Statistically not significant relationships are typed bold. Molecular descriptors which are characterized by most or all of such relationships are also typed bold. This means that the data set containing such descriptors is not statistically justified. Signs "+" and "–" in square brackets for a particular descriptor denote its positive or negative regression coefficient in the regression model.

[c]Pearson correlation coefficient between a descriptor and the dependent variable **y**.

[d]Regression coefficients a and b from a linear regression equation for **y** and descriptor **x**: $\mathbf{y} = a + b\,\mathbf{x}$. Statistical errors on the coefficients a and b are σ_a and σ_b, respectively. The values of the coefficients are rounded to significant figures and the respective errors are given in brackets.

[e]Student t-test parameters for the regression coefficients a and b are $t_{a,n-1} = a/\sigma_a$ and $t_{b,n-1} = b/\sigma_b$, respectively. The parameters are for n number of samples, *i.e.*, n-1 degrees of freedom. Corresponding probabilities p_a and p_b, *i.e.*, probabilities that the regression coefficients are not statistically significant (statistically not different from zero), are given in brackets, rounded to one or two significant figures.

[f]Explained fitted variance, defined in Table 1 as the coefficient of multiple determination. In the special case of linear regression, it may be considered as the coefficient of (univariate) determination.

[g]F-value from F-test and the corresponding probability in brackets, *i.e.*, the probability that the obtained linear regression equation is not statistically significant (obtained by chance). F-values are given for one variable and n-2 degrees of freedom. F-value is rounded to one digit and its probability is given for one or two significant figures.

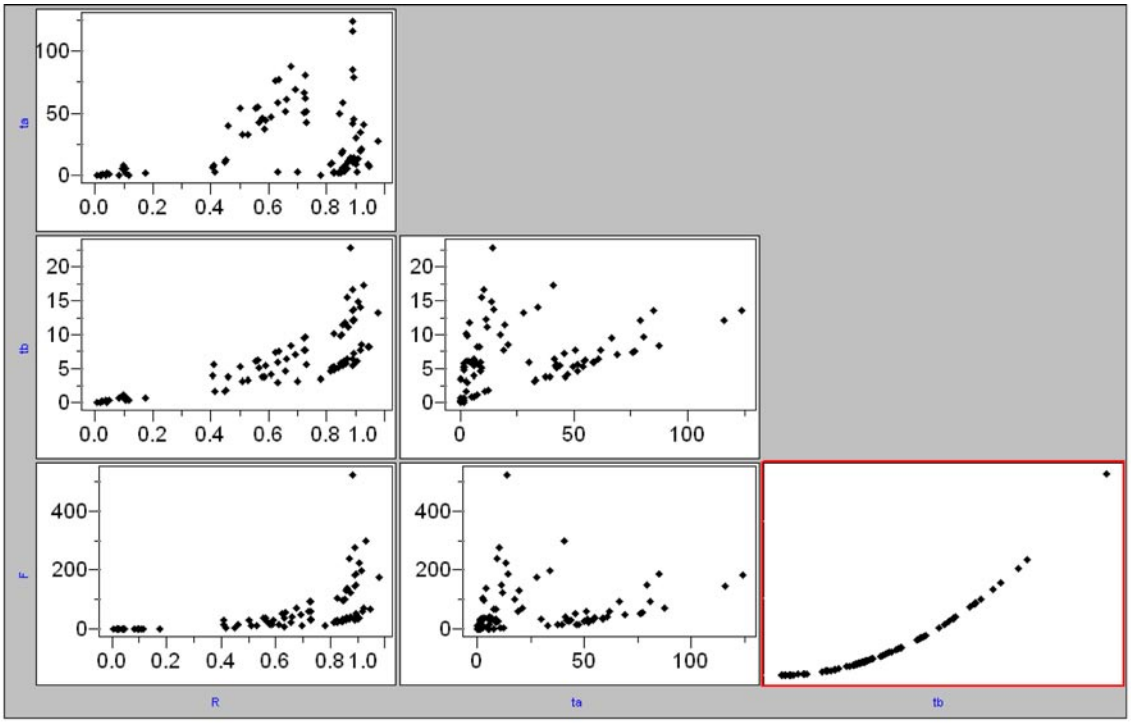

Figure F32. The scatterplots illustrating some of the relationships between statistical parameters from Table T33. The analytical relationship F - t_b is marked in red.