

Performance of Reinforced Concrete Beams Strengthened in Shear Using L-Shaped CFRP Plates - An Experimental Investigation

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Abstract

This paper presents results of an experimental investigation on reinforced concrete (RC) T-beams retrofitted in shear with prefabricated L-shaped carbon fibre-reinforced polymer (CFRP) plates. Shear-strengthening of RC beams with L-shaped fibre-reinforced polymer (FRP) plates has proved effective. In this method, grooves are made throughout the beam flange to embed fully the vertical leg (perpendicular to the longitudinal axis of the RC beam and in the RC beam web surface) of the L-shaped CFRP plate. However, in some cases, drilling grooves in the concrete flange might not be feasible because of the presence of obstacles such as longitudinal steel in the flange of the RC beams. Therefore, the main objective of this investigation was to evaluate the performance of the RC beams strengthened in shear with externally bonded L-shaped as affected by the embedment length of the L-shaped FRP plates.

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19 In total, six tests were performed on 2500 mm-long T-beams. Three specimens were
20 strengthened in shear using epoxy-bonded L-shaped CFRP plates with different embedment
21 lengths in the RC beam flange. One specimen was shear-strengthened with fully embedded
22 CFRP plates in the concrete beam flange. The second specimen was strengthened with partial
23 embedment of the L-shaped CFRP plate. This specimen is representative of the case where full
24 penetration of the CFRP plate is not feasible because of an obstacle. In this specimen, the
25 embedment length was set to 25 mm to simulate the minimum concrete cover thickness in RC
26 beams. The third specimen was shear-strengthened with L-shaped CFRP plates with no
27 embedment in the concrete beam flange. In addition, the performance of the beams strengthened
28 with L-shaped CFRP plates was compared with that of a similar specimen strengthened with
29 externally bonded (EB) FRP sheets without embedment. Results show that the performance of
30 the specimens strengthened with partially and fully embedded L-shaped CFRP plates in the beam
31 flange was superior to that of the beams strengthened with EB FRP sheets and L-shaped CFRP
32 plates with no embedment.

33

34 **CE Database subject headings:** Concrete beam; Fibre-reinforced polymer; Strengthening;
35 Shear; Epoxy bonding; Debonding; Embedment; L-shaped plates.

36

37 **INTRODUCTION**

38 In the last two decades, the application of fibre-reinforced polymer (FRP) composites has
39 received much attention in the construction engineering industry, particularly for rehabilitation of
40 reinforced concrete (RC) structures. Consequently, many valuable research studies on different
41 aspects of the subject, including shear-strengthening of RC beams with FRP composites, have

42 been conducted (e.g., Uji 1992; Chaallal *et al.* 1998; Khalifa *et al.* 1998; Triantafillou 1998;
43 Czaderski 1998; Chen and Teng 2003; De Lorenzis 2004; and Mofidi and Chaallal 2011a,b).
44 Different techniques such as externally bonded (EB) FRP sheets, near-surface mounted (NSM)
45 FRP rods, and embedded through-section (ETS) FRP rods have been proposed and successfully
46 tested for strengthening of RC beams and girders in shear with FRP composites (e.g., Uji 1992;
47 Chaallal *et al.* 1998; De Lorenzis and Nanni 2001; Monti and Liotta 2006; De Lorenzis 2004;
48 and Mofidi *et al.* 2012a,b).

49 Prefabricated L-shaped FRP plates present a potential alternative to EB FRP sheets, NSM FRP
50 rods, and ETS FRP rods for shear strengthening of reinforced-concrete (RC) beams. Meier
51 (1998) conducted a series of pull-out tests on L-shaped carbon-FRP (CFRP) plates bonded to
52 concrete blocks. In addition, a series of tests on adhesively post-installed embedded (APE) CFRP
53 plates bonded to concrete blocks was also carried out by Meier (1998). Czaderski (1998)
54 investigated the effectiveness of L-shaped CFRP plates in shear-strengthening of RC beams. The
55 test matrix of his investigation included three RC beams with different concrete cross-sectional
56 properties and loading configurations. In 2002, an experimental investigation was conducted at
57 the EMPA laboratories (Eidgenössische Materialprüfungs und Forschungsanstalt) on retrofitting
58 RC beams with L-shaped CFRP plates, which can be described as follows: (i) two shear-
59 strengthened specimens using L-shaped CFRP plates with different internal transverse-steel ratio
60 were tested under static load; (ii) one test was implemented on a cracked RC beam strengthened
61 under load in shear using L-shaped FRP plates; and finally (iii) one strengthened specimen was
62 tested under cyclic loads. The results of this experimental investigation were published in EMPA
63 Report No. 116/7 (2002). Later, Czaderski and Motavalli (2004) focused on the fatigue behavior
64 of RC beams strengthened with L-shaped CFRP plates using the results of the EMPA tests

65 (2002). Chen and Robertson (2004) tested a pre-cracked, pre-stressed concrete T-beam
66 retrofitted in shear using L-shaped CFRP plates. Later, Robertson *et al.* (2007) conducted a
67 cyclic loading test on an AASHTO-type RC beam strengthened with L-shaped CFRP plates.

68 Clearly, very few tests have been performed worldwide on RC beams strengthened in shear with
69 L-shaped FRP plates, and the need for more related data has been clearly demonstrated. Of all
70 the tests implemented on retrofitted RC beams with L-shaped plates, few were performed under
71 static load, and none considered partial embedment of RC beams in the flange because of an
72 obstacle that inhibits full penetration. The main objective of this study is twofold: (1) to assess
73 the effectiveness of shear-strengthening using bonded L-shaped CFRP plates with partial and full
74 embedment compared to conventional EB FRP sheets, and (2) to evaluate the effect of
75 embedment length into the flange on the performance of RC beams strengthened in shear with L-
76 shaped laminates.

77 In a companion paper (Mofidi *et al.* 2013), design equations for RC beams strengthened with L-
78 shaped CFRP plates were proposed. These equations were derived considering various observed
79 failure modes, including FRP pull-out, concrete break-out in the flange, FRP plate debonding,
80 and FRP overlap failure at the beam soffit. The proposed design equations showed reasonable
81 correlation with experimental results.

82

83 **EXPERIMENTAL INVESTIGATIONS**

84 The RC beams were tested in three-point load flexure. Overall, the experimental program (Table
85 1) involved six tests performed on half-scale RC T-beams. The control specimen, which was not
86 strengthened with carbon FRP (CFRP), was labelled CON, whereas the specimens retrofitted
87 with L-shaped CFRP plates were labelled LS. The single specimen strengthened with a layer of
88 EB CFRP sheet was labelled EB. In the specimens strengthened with L-shaped CFRP plates, the
89 depth of plate embedment into the RC beam flange was indicated as follows: the beam
90 strengthened with CFRP L-shaped plates with no embedment was labelled NE; the specimen
91 strengthened with CFRP L-shaped plates partially embedded (25 mm) into the RC beam flange
92 was labelled PE; and the beam strengthened with CFRP L-shaped plates fully embedded (102
93 mm) into the beam flange was labelled FE.

94 All the beams tested in this study were labelled S1, except for the S0-CON beam which had no
95 transverse shear reinforcement (hereafter called transverse-steel). Series S1 corresponds to
96 specimens with internal transverse-steel stirrups spaced at $s = d/2$, where $d = 350$ mm and
97 represents the effective depth of the beam cross section (Fig. 1). Thus, for example, specimen
98 S1-LS-PE features the beam with internal steel stirrups spaced at $s = d/2$, which was retrofitted
99 with L-shaped plates embedded one inch into the RC beam flange. The labels used for each
100 beam are provided in Table 1.

101

102 **Specimens**

103 The cross sections of the specimens and their dimensions are presented in Fig. 1. The tested
104 specimens consisted of a T-beam with a web width of 152 mm and a flange depth of 102 mm.
105 The RC beams had an overall length of 2500 mm and a span of 2100 mm. The load was applied

106 at mid-span of the RC beam. The longitudinal-steel reinforcement at the bottom of the RC beam
107 was laid in two layers of four 25M bars (diameter 25.2 mm, area 500 mm²). At the top of the
108 cross section, the longitudinal-steel reinforcement consisted of six 10M bars laid in one layer
109 (diameter 10.3 mm, area 100 mm²). The transverse-steel reinforcement was 8 mm in diameter
110 (area 50 mm²). The spacing between the steel stirrups was 175 mm ($d/2$) for all the specimens
111 with internal transverse steel (Fig. 1). The specimens had chamfered outer corners at the sides of
112 the beam soffit to match the curved corner shape of the CFRP L-shaped plates. The
113 strengthening L-shaped FRP plates were epoxy-bonded mid-way between the steel stirrup
114 locations.

115

116 **Materials**

117 The internal longitudinal and transverse steel had nominal yielding strengths of 540 and 650
118 MPa respectively. A commercially available concrete was delivered to the laboratory by a local
119 supplier. The average concrete strength of 152 mm diameter by 305 mm high concrete cylinders
120 at 28 days was 29.6 MPa, whereas it was 33.7 MPa during the RC beam tests. The scatter
121 between the results of compression tests of the cylinder specimens 28 days after pouring of
122 concrete or on the test day was negligible.

123 The CFRP L-shaped plates used to strengthen the RC beams were unidirectional. The L-shaped
124 plates originally consisted of 500 mm × 200 mm legs. However, the legs of the plates had to be
125 shortened to fit properly into the corresponding configuration of each strengthened specimen,
126 including the embedment lengths. The L-shaped plates were 40 mm wide and 2 mm thick. The
127 modulus of elasticity of the plates was 90 GPa according to the manufacturer's data sheet. The
128 ultimate tensile strength and the ultimate strain of the L-shaped plates were set to 1350 MPa and

129 1.3% respectively. The L-shaped plates were epoxy-bonded to the test zone in a U-shaped
130 envelope around the web, i.e., the short legs of two L-shaped plates at one cross section
131 overlapped onto the soffit of the specimen. The L-shaped CFRP plates were bonded to the beam
132 surface with a two-component adhesive made of a resin and a hardener, both of which are
133 engineered mainly for structural applications and were supplied by the manufacturer. The
134 epoxy's mechanical properties, as specified by the manufacturer, were: 24.8 MPa bond strength,
135 1% elongation at break, and 4.5 GPa tensile modulus of elasticity. The CFRP sheet used for the
136 specimens strengthened with EB FRP sheet was a unidirectional carbon-fibre fabric. It was
137 applied continuously over the test zone in a U-shaped envelope around the web. The continuous
138 composite material was selected because it can provide an appropriate benchmark to evaluate the
139 effectiveness of L-shaped FRP plates in shear-strengthening of RC beams. The mechanical
140 properties of the CFRP sheet according to the manufacturer's datasheet were as follows: 3450
141 MPa tensile strength, 230 GPa tensile E-modulus, 1.5% elongation at break, 1.8 g/cm³ density,
142 and 230 g/m² area weight. The CFRP fabric was bonded to the beam surface with a two-
143 component epoxy paste made of a resin and a hardener. The mechanical properties of the epoxy
144 paste as specified by the manufacturer were as follows: 30 MPa tensile strength, 1.5% elongation
145 at break, and 3.8 GPa flexural modulus of elasticity. Table 2 provides the mechanical and elastic
146 properties of the CFRP plates and sheets as provided by the manufacturers.

147

148 **Test set-up and procedure**

149 As mentioned earlier, the beams were tested in three-point load flexure. The load was applied at
150 a distance $a = 3d$, which corresponds to a slender beam test. A carefully detailed and widely
151 spread measuring plot was chosen for the test series. Using linear variable differential

152 transformers (LVDTs), the vertical displacement was measured under the applied load at the
153 mid-span. Strain gauges were carefully bonded onto the transverse- and longitudinal-steel
154 reinforcements to measure the deformations at different loading phases. The displacement
155 sensors, known as crack gauges, were used to measure the deformations experienced by the
156 CFRP L-shaped plates. These gauges were installed vertically on the strengthening L-shaped
157 plates (Fig. 2). All the tests were conducted under displacement control conditions at 2
158 mm/minute.

159

160 **Strengthening methods**

161 Three of the tested specimens were strengthened with epoxy-bonded L-shaped CFRP plates with
162 different embedment lengths of the CFRP plates in the beam flange. The behaviour of the
163 strengthened RC beams with the L-shaped CFRP plates was compared with that of the specimens
164 strengthened with EB CFRP sheet.

165 To install the L-shaped CFRP plates with no embedment (S1-LS-NE), the following procedure
166 was used: (1) the area of the specimen where the CFRP L-shaped plates were to be bonded was
167 sand-blasted to remove the external cement paste and to round out the beam corners at the beam
168 soffit; (2) the bond area was ground to remove any possible irregularities and to achieve a
169 smooth bond surface; (3) residues were removed by compressed air; and (4) CFRP L-shaped
170 plates were bonded to the bottom and lateral faces of the RC beam using a two-component epoxy
171 resin. Note that two L-shaped plates were used in each section of the RC beam to form a U-
172 shaped jacket. The bottom legs of the L-shaped plates were overlapped onto the soffit face of the
173 T-beam.

174 In specimens S1-LS-PE and S1-LS-FE one leg of each bonded L-shaped CFRP plate was
175 embedded in the RC beams flange to provide a form of end-anchorage to the FRP plates. To
176 install the partially embedded L-shaped plates (S1-LS-PE), the following steps were carried out
177 after the first three steps described above for the specimen strengthened with L-shaped plates
178 with no embedment: (1) 25.4 mm (one-inch)-deep grooves with a cross section of 50.8 mm ×
179 12.7 mm spaced at 175 mm were drilled perpendicular to the bottom of the beam flange at the
180 intersection of the RC beam web and flange (Fig. 3); (2) a thin layer of epoxy paste was applied
181 to the grooves; (3) CFRP L-shaped plates were epoxy-bonded to the web and to the soffit of the
182 RC beam surface. Note that the extended leg of the L-shaped plate was inserted and bonded into
183 the groove.

184 To bond the fully embedded CFRP L-shaped plates (S1-LS-FE) the following steps were used:
185 (1) 102 mm (four-inch)-deep grooves with a cross section of 50.8 mm × 12.7 mm spaced at 175
186 mm were drilled throughout the flange thickness of the RC beam at the flange intersection with
187 the RC beam web; (2) a thin layer of epoxy paste was applied to the grooves; (3) CFRP L-shaped
188 plates were epoxy-bonded to the web and soffit of the RC beam surface. The extended leg of the
189 CFRP L-shaped plate was epoxy-bonded into the groove (Fig 3).

190 Note that for each of the strengthening methods described above, the CFRP L-shaped plates were
191 cut to a length that takes the embedment depth into account.

192 To apply the EB FRP sheet-strengthening method with no anchorage (S1-EB-NA), the following
193 procedures were carried out: (1) the area of the specimen where the continuous CFRP sheet was
194 to be bonded was sand-blasted to remove the exterior cement paste and to round off the beam
195 edges; (2) the bond area was ground to remove possible irregularities and to attain a smooth bond
196 surface; (3) residues were removed by compressed air; and (4) a U-shaped layer of continuous

197 CFRP sheet was glued to the soffit and lateral faces of the RC beam using a two-component
198 epoxy resin.

199

200 **RESULTS AND DISCUSSION**

201 The experimental results obtained for all the specimens are summarized in Table 1. The results
202 are presented in terms of the loads attained at failure; the experimental shear resistance due to
203 concrete, transverse steel, and CFRP; and the shear-capacity gain due to CFRP. Note that the
204 shear contributions of concrete (V_c) and steel (V_s) were calculated based on the results achieved
205 from the control test specimens, i.e., S0-CON and S1-CON. Some of the values provided in
206 Table 1 are calculated based on the following assumptions, which are implicitly stated in the
207 design guidelines: a) the shear resistance due to concrete is the same whether or not the beam is
208 reinforced with transverse steel and whether or not the beam is strengthened with CFRP; and b)
209 the shear resistance due to steel is the same whether or not the beam is strengthened with CFRP.
210 The results reveal that the shear-capacity gain due to CFRP for the specimen strengthened with
211 fully embedded L-shaped plates was 55%, compared to 39%, 36%, and 27% respectively for the
212 corresponding specimens strengthened with partially embedded L-shaped plates, EB sheets, and
213 L-shaped plates with no embedment.

214 These results clearly confirm the effectiveness of all the strengthening methods used in this
215 research study, especially the method of shear-strengthening RC beams with L-shaped CFRP
216 plates with full or partial embedment (specimens S1-LS-FE and S1-LS-PE).

217 Table 1 reveals that the beams strengthened using fully embedded CFRP L-shaped plates (S1-
218 LS-FE) and partially embedded CFRP L-shaped plates (S1-LS-PE) attained the highest shear
219 resistance due to FRP strengthening, compared to the other two strengthened specimens (S1-LS-

220 NE and S1-EB-NA). Specimens S1-LS-FE and S1-LS-PE respectively reached 119.5 kN and
221 84.1 kN shear resistance due to FRP. Specimens S1-LS-NE and S1-EB-NA respectively reached
222 59.2 kN and 77.8 kN shear resistance due to FRP.

223

224 **Failure progression**

225 All the test specimens failed in shear except for the S1-LS-FE specimens. It should be
226 emphasized that for the specimens with transverse steel, shear failure occurred after the
227 transverse steel intersecting with the shear crack had yielded. Failure of each specimen can be
228 described as follows:

229 *S0-CON*: The unstrengthened specimen with no transverse-steel reinforcement failed due to
230 diagonal tension failure in a brittle manner. A diagonal shear crack formed during the loading of
231 beam S0-CON at a load of 78.8 kN. As the load increased, the crack widened and propagated
232 until failure, which occurred at a load of 122.7 kN.

233 *S1-CON*: The control beam with transverse-steel reinforcement spaced at 175 mm ($s=d/2$)
234 developed diagonal shear cracks at a load similar to that at which the shear crack started
235 propagation in S0-CON (78.2 kN). Specimen S1-CON failed due to diagonal tension failure at a
236 load of 432.4 kN, followed by the rupture of the second stirrup located at 263 mm from the
237 support.

238 *S1-LS-NE*: Beam S1-LS-NE had the same transverse-steel reinforcement as the control specimen
239 S1-CON, but was strengthened with epoxy-bonded CFRP L-shaped plates without any
240 embedment of the L-shaped plates in the RC beam flange. The ultimate load attained was 550.7
241 kN, that is, 27% greater than the ultimate capacity of S1-CON. Specimen S1-LS-NE failed due

242 to debonding of the FRP plates followed by diagonal tension failure of the beam (Fig. 4). Note
243 that the longitudinal-steel reinforcement yielded before the ultimate shear failure.

244 *S1-LS-PE*: The ultimate load was attained at 600.5 kN, that is, 39% greater than the ultimate
245 capacity of the S1-CON control beam and 9% greater than the ultimate capacity of S1-LS-NE.
246 Specimen S1-LS-PE failed due to break-out of the FRP plate from the concrete flange around the
247 embedded L-shaped FRP plate, which was followed by debonding of the FRP plate from the RC
248 beam web (Fig. 5). Similarly to specimen S1-LS-NE, the longitudinal-steel reinforcement
249 yielded before the ultimate shear failure.

250 *S1-LS-FE*: The ultimate load attained was 671.4 kN, which was 55% greater than the shear
251 capacity of control beam S1-CON and 22% greater than the ultimate shear capacity of S1-LS-
252 NE. No sign of CFRP plate debonding was observed. Failure occurred by yielding of
253 longitudinal steel followed by flexural compression failure (Fig. 6).

254 *S1-EB-NA*: Beam S1-EB-NA had similar transverse-steel reinforcement to the control specimen
255 S1-CON, but was strengthened with epoxy-bonded CFRP sheet with no anchorage. The ultimate
256 load attained 587.9 kN, that is, 36% greater than the ultimate capacity of S1-CON and 7%
257 greater than the ultimate capacity of S1-LS-NE. Specimen S1-EB-NA failed due to debonding of
258 the CFRP sheet followed by diagonal tension failure (Fig. 7). The longitudinal-steel
259 reinforcement yielded before the ultimate shear failure.

260

261 **Deflection response**

262 Figure 8 presents load versus maximum deflection curves at the mid-span for beams
263 strengthened with FRP L-shaped plates and sheets and for the control beams. The maximum load
264 at failure and the maximum deflection attained at the loading point for each specimen are

265 provided in Table 1. Specimen S1-LS-FE exhibited a higher deflection at the loading point than
266 the other strengthened and unstrengthened specimens. Moreover, specimen S1-LS-FE achieved a
267 higher maximum load at failure than the rest of the specimens (Table 1). Specimen S1-LS-FE
268 was the only one that reached its flexural capacity limit (Fig. 8). Therefore, the failure of
269 specimen S1-LS-FE was more ductile compared to other strengthened and unstrengthened
270 specimens. Note that specimens S1-LS-NE, S1-LS-PE, and S1-EB-NA also failed in a ductile
271 manner. The longitudinal steel in specimens S1-LS-NE, S1-LS-PE, and S1-EB-NA yielded
272 before the ultimate shear failure. Nevertheless, specimen S1-LS-FE reached the maximum
273 displacement ductility factor (μ) among all the strengthened beams. The maximum displacement
274 ductility factor of S1-LS-FE was 5.64, whereas μ was 1.70, 2.69, and 2.37 for S1-LS-NE, S1-LS-
275 PE, and S1-EB-NA respectively. The deflection ductility is defined here as the ratio of the
276 maximum attained deflection to the displacement corresponding to yielding. It can be seen that
277 the deflection behavior of the beams strengthened with fully embedded and partially embedded
278 L-shaped CFRP plates is more ductile than that of the other effective shear-strengthened
279 specimens (Table 1). For example, the deflection under point load of beam S1-LS-FE at
280 maximum load was 2.17 times that of beam S1-LS-NE at maximum load (42.9 mm at load 671.4
281 kN versus 19.8 mm at 550.7 kN) and 2.01 times that of beam S1-EB-NA at maximum load (42.9
282 mm at load 671.4 kN versus 21.3 mm at 587.9 kN), whereas the S1-CON beam failed at a
283 maximum load of 432.4 kN with a maximum deflection at the mid-span of 11.9 mm.

284

285 **Strain in transverse steel**

286 Curves representing applied load versus strain in the transverse-steel reinforcement are presented
287 in Fig. 9. It is clear that the transverse-steel reinforcement contributed very little to the load-

288 carrying capacity in the early stages of loading. The transverse steel started to contribute to shear
289 resistance only after shear diagonal cracks formed in the concrete. The transverse-steel
290 contribution was initiated at applied loads of between 50 and 100 kN for all the test specimens.
291 The transverse-steel strain continued to increase sharply as the applied load increased until either
292 the transverse steel yielded at $3250 \mu\text{strains}$ or ultimate failure of the specimen occurred. Figure
293 9 shows that the transverse steel crossing the shear crack lines yielded in all the specimens tested
294 in this study.

295 Given the applied load, the strain in the transverse steel was relatively less in specimens S1-LS-
296 PE, S1-LS-FE, and S1-EB-NA than in specimens S1-CON and S1-LS-NE (Fig. 9). This could be
297 due to the effectiveness of FRP in specimens S1-LS-PE, S1-LS-FE, and S1-EB-NA compared to
298 specimens S1-CON and S1-LS-NE (Table 1). Figure 9 reveals that for the specimens with
299 greater shear-capacity gain due to CFRP, the transverse steel experienced less strain during the
300 tests. Therefore, it can be concluded that the CFRP strengthening method effectively eased the
301 strains in the transverse steel. Hence, the transverse steel yielded at a greater applied load in
302 specimens that were effectively strengthened with FRP compared to the corresponding
303 specimens with no FRP strengthening or with less effective FRP strengthening methods. The
304 reported transverse-steel strain is the measured strain in the steel stirrup that reached the
305 maximum strain during loading.

306

307 **Strain in FRP**

308 In this part of the study, the CFRP strain readings for all the strengthened specimens were
309 analyzed. Figure 10 shows the load versus FRP strain curves for the beams strengthened with L-
310 shaped FRP plates and EB U-jacket sheets. The curves show that for the strengthened specimens

311 (except for S1-LS-PE and S1-LS-FE), the CFRP did not contribute to load-carrying capacity in
312 the initial stage of loading until the applied load reached between 180 and 200 kN. In specimens
313 S1-LS-PE and S1-LS-FE, the FRP started to contribute to shear resistance at a loading of 50 kN.
314 This could be due to the embedment of the L-shaped FRP plates into the concrete flange, which
315 might have rendered the L-shaped CFRP plates effective at an earlier stage of loading than in
316 specimens S1-LS-NE and S1-EB-NA.

317 In all specimens, after the CFRP started to contribute to shear resistance, the CFRP strain
318 continued to increase sharply under increasing load. The increase in the FRP strain continued to
319 a certain limit that differed from one specimen to another, depending on the strengthening
320 method, before the strain started to increase drastically. The maximum strain recorded
321 corresponding to the mentioned limit reached 4262 $\mu\epsilon$, 2085 $\mu\epsilon$, 3061 $\mu\epsilon$, and 1080 $\mu\epsilon$ for
322 specimens S1-LS-NE, S1-LS-PE, S1-LS-FE, and S1-EB-NA respectively. Ultimately, the CFRP
323 strain rate started to increase drastically as the load increased further. This could be due to
324 yielding of transverse steel, which further engaged the CFRP to contribute more to the shear
325 resistance of the RC beams. The rapid increase in CFRP strain continued until ultimate failure
326 took place.

327 Figure 10 shows that the FRP strain in specimens strengthened with partially and fully embedded
328 L-shaped CFRP plates was distributed more effectively than in specimens strengthened with L-
329 shaped FRP and EB sheets with no anchorage. Unlike specimens S1-LS-NE and S1-EB-NA,
330 specimens S1-LS-PE and S1-LS-FE had the following positive features: (i) the FRP contributed
331 to the shear resistance in the early stages of loading (it was effective at service loads); (ii) the
332 FRP strain increased almost linearly with applied load; (iii) no drastic decrease in FRP strain was
333 observed at ultimate failure, or in other words, FRP debonding was avoided. Note that the

334 reported strain values were not necessarily the absolute maximum values experienced by the
335 CFRP, but the maximum measured values. The two values could be different if the strain gauges
336 did not intercept the main cracks.

337

338 **Strain in longitudinal-steel reinforcement**

339 Figure 11 presents the variation with applied load of the strains in the longitudinal-steel
340 reinforcement. These curves show that most of the curves for load versus strain in longitudinal
341 steel coincide (except for specimen S1-EB-NA). The flexural stiffness of specimen S1-EB-NA,
342 which was strengthened with continuous CFRP sheets, was slightly greater than that of both the
343 control beam and the beams strengthened with CFRP L-shaped plates (Fig. 11). The greater
344 flexural stiffness in specimen S1-EB-NA could be due to the effect of CFRP sheet continuity.
345 The uniaxial CFRP sheet used in this study could also carry some load in the direction
346 perpendicular to its fibre orientation because the sheet has a tensile modulus of 5876 MPa and a
347 tensile strength of 27 MPa in the minor direction (90°).

348 Overall, the longitudinal-steel reinforcement reached yielding between applied loads of 471 to
349 516 kN in all the strengthened specimens. However, the ultimate failure of specimens S1-LS-PE,
350 S1-LS-NE, and S1-EB-NA occurred due to diagonal tension failure of the concrete cross section.

351

352 **Efficiency of L-shaped CFRP plates versus CFRP sheets**

353 Table 1 shows that the specimen strengthened with fully embedded CFRP L-shaped plate
354 experienced significant increase in shear capacity with respect to the control beams and other
355 strengthened specimens. Specimen S1-LS-FE failed at a loading of 671.4 kN in flexural
356 compression failure mode, whereas specimens S1-LS-PE, S1-LS-NE, and S1-EB-NA failed in

357 shear at loadings of 600.5 kN, 550.7 kN, and 587.9 kN respectively. The shear contribution of
358 FRP for specimens S1-LS-FE, S1-LS-PE, S1-LS-NE, and S1-EB-NA was 119.5 kN, 84.1 kN,
359 59.2 kN, and 77.8 kN respectively. However, it is important to quantify the efficiency of the FRP
360 shear-strengthening methods in terms of the shear contribution of FRP versus the amount of FRP
361 used.

362 To define the efficiency of CFRP for each of the strengthening methods used in this study, the
363 amount of FRP per unit length was calculated. The cross-sectional area of CFRP bonded to both
364 sides of the web per metre of shear span used in all specimens strengthened with L-shaped CFRP
365 plates (with or without embedment of the plate) was 914 mm²/m. For the specimens strengthened
366 with EB FRP sheets, the cross-sectional area of CFRP per metre of shear span was 254 mm²/m.
367 The ultimate tensile capacity per unit length of the retrofitted specimens with L-shaped CFRP
368 plates (with or without plate embedment) was 1234 kN/m. For the specimens strengthened with
369 EB FRP sheets, the ultimate tensile capacity per unit length was 882 kN/m.

370 The efficiency of CFRP (ψ_f) is a tool that enables researchers to quantify rationally and hence to
371 compare the effectiveness of various strengthening methods involving application of FRP
372 material. The efficiency of a FRP strengthening method (ψ_f) for an RC beam is defined as the
373 shear contribution of FRP, V_f , divided by the ultimate tensile capacity per unit length of the FRP
374 used in the strengthened beam. Table 3 shows the efficiency of each of the FRP strengthening
375 methods used in this study. It can be seen that the beam strengthened with fully embedded CFRP
376 L-shaped plates reaches the highest FRP efficiency among all the strengthened beams in this
377 study. Note that in this comparison, the dry fibre material characteristics of the CFRP sheet are
378 based on manufacturers' data sheets.

379

380 CONCLUSIONS

381 Prefabricated L-shaped CFRP plates can enhance significantly the shear capacity of RC beams.

382 In this study, the average increase in shear capacity reached 40% for the beam retrofitted with

383 epoxy-bonded L-shaped CFRP plates. Within the experimental scope of this research study, the

384 following conclusions can be drawn:

385 • The effective application of partially embedded L-shaped CFRP plates to shear-
386 strengthening of RC beams was verified based on experimental investigations.

387 • Among the tested specimens, partial embedment of L-shaped CFRP plates was the most
388 effective alternative to full embedment of L-shaped CFRP plates when full embedment of
389 L-shaped plates is not feasible.

390 • Specimens strengthened with partially and fully embedded L-shaped FRP plates (S1-LS-
391 PE and S1-LS-FE) reached the highest gain in shear resistance due to FRP strengthening
392 and outperformed the other strengthened specimens with no embedment or anchorage
393 (S1-LS-NE and S1-LS-NA).

394 • In specimen S1-LS-FE, shear failure was prevented by effective embedment of the plate
395 in the concrete beam flange. Specimen S1-LS-FE failed in a ductile manner in flexure
396 with a maximum displacement ductility factor of 5.64.

397 • Unlike specimens S1-LS-NE and S1-EB-NA, specimens S1-LS-PE and S1-LS-FE had
398 the following positive features: (i) the FRP contributed to shear resistance at early stages
399 of loading (it was effective at service loads); (ii) the strain in the FRP increased almost
400 linearly with applied load; and (iii) no drastic decrease in FRP strain was observed at
401 ultimate failure, or in other words, FRP debonding was avoided.

402

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455 carbon fibre sheets. *Trans. Jpn. Concr. Institute* 14, 253–266.

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464 Table 1 – Experimental results.

Specimen	Load at rupture	Total shear resistance	Resistance due to concrete	Resistance due to steel	Resistance due to CFRP	Gain due to CFRP	Deflection at load point	Failure mode
	kN	kN	kN	kN	kN	%	mm	
S0-CON	162.4	81.2	81.2	0.0	0.0	0	2.6	Shear
S1-CON	432.4	216.2	81.2	135.0	0.0	0	11.9	Shear
S1-LS-NE	550.7	275.4	81.2	135.0	59.2	27	19.8	Shear
S1-LS-PE	600.5	300.3	81.2	135.0	84.1	39	19.2	Shear
S1-LS-FE	671.4	335.7	81.2	135.0	119.5	55	42.9	Flexure
S1-EB-NA	587.9	294.0	81.2	135.0	77.8	36	21.3	Shear

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467 Table 2 – Mechanical properties of CFRP L-shaped plate and CFRP sheets used.

Property	L-shaped CFRP plate	Dry fibre sheet	Wet layup FRP sheet
Modulus of elasticity, GPa	90	230	65
Ultimate elongation, %	1.30	1.50	1.33
Ultimate stress, MPa	1350	3450	894

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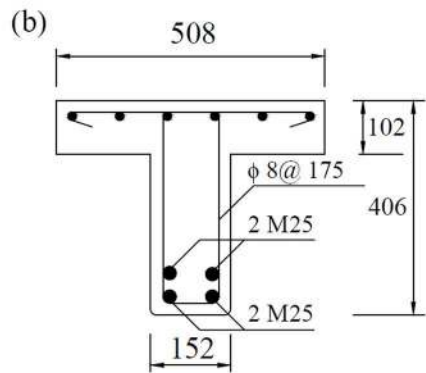
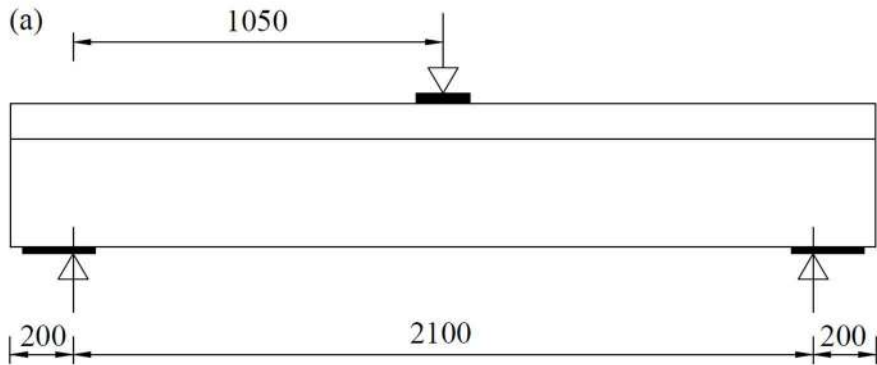
470 Table 3 – Efficiency of FRP using different strengthening methods.

Specimen	Area of CFRP	Ultimate tensile capacity per unit length	V_f	ψ_f Efficiency of FRP
	mm ² /m	kN/m	kN	%
S1-LS-NE	914	1234	59.2	4.8
S1-LS-PE	914	1234	84.1	6.8
S1-LS-FE	914	1234	119.5	9.7
S1-EB-NA	256	882	77.8	8.8

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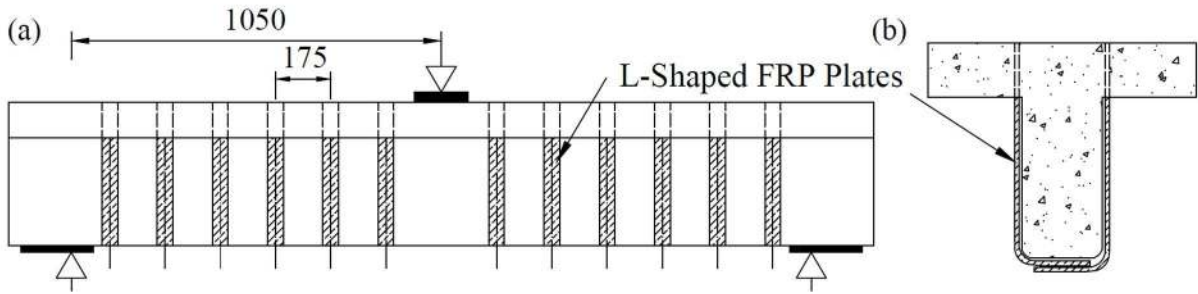


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ST-1







LS-4L

LS-4R





