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#### Quantum Electronic Structure

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Benchmark calculations of K-edge ionization energies for first-row elements using scalar-relativistic core-valence-separated equation-of-motion coupled-cluster methods

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#### Abstract

Benchmark scalar-relativistic core-valence-separated (CVS) equation-of-motion coupled-cluster ionization potential (EOMIP-CC) calculations of 21 K-edge ionization energies of C, O, N, and F in 14 molecules are reported. The CVS-EOMIP-CC methods are shown to be numerically more stable and more accurate than the parent EOMIP-CC methods, even when the calculations using the latter can be tightly converged. The superior performance of the CVS scheme is attributed to the exclusion of spurious couplings between core-ionized states and valence continuum states. Systematic improvement of computed K-edge ionization energies within the CVS-EOMIP-CC hierarchy, including the CC singles and doubles (CCSD) method, the CC singles, doubles and

triples (CCSDT) method, and the CC singles, doubles, triples, and quadruples (CCS-DTQ) method, is demonstrated, with CCSDTQ yielding essentially quantitative results. Maximum absolute deviations between computed and experimental results amount to 2.54 eV for CCSD/cc-pCVQZ, 0.54 eV for CCSDT/cc-pCVQZ, and 0.23 eV for CCSDT/cc-pCVQZ augmented with quadruples contributions using the cc-pVTZ basis sets. The corresponding standard deviations are 1.91 eV for CCSD/cc-pCVQZ, 0.18 eV for CCSDT/cc-pCVQZ, and 0.10 eV for CCSDT/cc-pCVQZ augmented with quadruples contributions using the cc-pVTZ basis sets. Finally, CVS-EOMIP-CCSDT/ccpCVTZ calculations of core ionization energies in CH<sub>3</sub>CN and CH<sub>3</sub>NC are reported, and experimental re-investigation of carbon 1s ionization energies in CH<sub>3</sub>CN is suggested.

#### Introduction

X-ray spectroscopy is widely used for probing electronic structure and dynamics in molecules, solid state, and biological systems. <sup>1-4</sup> In particular, recent advancements in short-pulse X-ray light sources including synchrotrons, free-electron lasers, and those based on high-harmonic generation  $^{5-11}$  have enabled the study of ultrafast nuclear and electronic dynamics.  $^{12-17}$  Extensive studies of computational techniques aiming at accurate calculations of X-ray photoelectron and absorption spectra are available in the literature. 18,19 The computational techniques can be classified into two broad categories. The ones in the first category perform separate orbital optimizations for core-ionized or excited states. The delta-Hartree-Fock  $(\Delta HF)$  method,  $^{20-23}$  the delta-density-functional-theory  $(\Delta DFT)$  method  $^{23,24}$  as well as its approximate variants,  $^{24-27}$  the delta-restricted-active-space self-consistent-field ( $\Delta RASSCF$ ) method, <sup>21,28–30</sup> the orthogonality-constrained DFT method, <sup>31</sup> the static exchange (STEX) method, <sup>32,33</sup> and the non-orthogonal configuration interaction singles (NOCIS) method <sup>34</sup> fall into this category. These techniques explicitly account for the strong orbital relaxation induced by the creation of core hole(s) and are usually capable of providing good energies

for core-ionized/excited states. Calculations with explicit inclusion of dynamical correlation on top of  $\Delta HF$  have also been reported. 35–38 The techniques in the second category use the ground state of the neutral molecule as the reference state and access core-ionized and excited states via response theory or using a wave operator that accounts for the difference between ground and excited states. The configuration interaction singles (CIS) method, <sup>39-41</sup> CIS with perturbative inclusion of double excitations (CIS(D)), 42 time-dependent DFT linear response (TDDFT-LR) theory, <sup>18,43</sup> the Bethe-Salpeter equation approach, <sup>44</sup> Green's function  $methods, ^{45-48}\ equation-of-motion\ coupled-cluster\ (EOM-CC)\ methods, ^{49,50}/coupled-cluster$ linear response (CC-LR) theory <sup>51,52</sup> and multireference coupled-cluster methods <sup>53–56</sup> belong to this category. We mention that real-time DFT<sup>57-59</sup> and CC methods<sup>60</sup> for calculations of core-ionized/excited states fall into the second category within the present discussion, as the ionization or excitation energies computed with these methods are identical to those obtained using the corresponding linear response theories.

Response theories (and the methods in the second category in general) are flexible tools for calculations of both energies and properties of excited states. However, additional challenges have to be dealt with in calculations of core-ionized or excited states. Since coreionized and excited states are energetically embedded in continuum states, the convergence of excited-state equations has emerged as a major challenge. Several schemes including the complex polarization propagator (CPP) method, <sup>61</sup> the (asymmetric) Lanczos algorithm, <sup>62</sup> the Arnoldi algorithm,  $^{49}$  the energy-specific strategy,  $^{50}$  and the core-valence separation (CVS) scheme <sup>52,63</sup> have been proposed in order to resolve the convergence difficulty. Among these approaches, the CVS scheme originally proposed by Cederbaum et al. 64 appears to be the most promising. The CVS scheme retains only excitations involving at least one core orbitals and thus excludes the problematic pure valence excitations that are (quasi-)degenerate to the core-ionized or excited states of interest. In the literature the CVS scheme has been referred to as "the CVS approximation" to the parent "full" method. However, the "full method" may include spurious couplings between core-ionized or excited states and valence continuum states. One motivation of the present study is to examine the numerical significance of this problem of the "full" method. It has indeed been found and will be reported in Section 3.1 that the CVS scheme is superior to the "full" method and thus is the method of choice for treating core-ionized and excited states.

On the other hand, the solution of response equations within the CVS scheme does neglect the contribution from the continuum part of the wave function of core-ionized or excited states. This is a potential source of errors for the computed energies and properties of core-ionized or excited states. Another motivation of this work is to investigate the intrinsic accuracy of this approximation. For this purpose, the hierarchy of CVS-EOMIP-CC methods, <sup>65–69</sup>including the CC singles and doubles (CCSD) method, <sup>66</sup> the CC singles, doubles and triples (CCSDT) method<sup>70,71</sup> as well as CC singles, doubles, triples, and quadruples (CCSDTQ) method, <sup>72</sup> together with correlation-consistent basis sets <sup>73–75</sup> have been used to systematically approach the exact solution for the bound part of the wave function. The benchmark set comprises 21 K-edge ionization energies of C, N, O, F in 14 molecules. Note that relativistic effects essentially contribute a constant shift of K-edge ionization energies in C, N, O, or F. However, relativistic corrections amount to about 0.1 eV for C and around 0.7 eV for F. They are not negligible when high accuracy is desired. <sup>76,77</sup> In the present study we have used spin-free exact-two-component theory in its one-electron variant (SFX2C-1e)<sup>78,79</sup> to treat relativistic effects. Theory and computational details are given in Section 2, while the computational results are presented and discussed in Section 3. The conclusion is given in Section 4.

## 2 Theory and computational details

We first briefly recapitulate the equation-of-motion ionization-potential coupled-cluster (EOMIP-CC) methods <sup>80</sup> used in the present study. Throughout the discussion, we follow the standard convention that  $\{i, j, \dots\}$ ,  $\{a, b, \dots\}$ , and  $\{p, q, \dots\}$  denote occupied, virtual, and arbitrary

orbitals, respectively. The EOMIP-CC wave function  $|\Psi^{\text{EOMIP-CC}}\rangle$  is obtained by applying an "ionization operator"  $\hat{R}$  to the ground state CC wave function  $|\Psi^{\text{CC}}\rangle$ , i.e.,

$$|\Psi^{\text{EOMIP-CC}}\rangle = \hat{R}|\Psi^{\text{CC}}\rangle.$$
 (1)

The wave operator of the ground state CC method takes an exponential parametrization and the CC wave function can be written as  $|\Psi^{\text{CC}}\rangle = e^{\hat{T}}|0\rangle$ , in which  $|0\rangle$  is the reference determinant. The cluster operator  $\hat{T}$  is a weighted combination of excitation operators, e.g., in the CC singles and doubles (CCSD) method  $\hat{T} = \sum_{ia} t_i^a a_a^{\dagger} a_i + \frac{1}{4} \sum_{ijab} t_{ij}^{ab} a_a^{\dagger} a_j^{\dagger} a_i$ . The cluster amplitudes are determined by projected amplitude equations

$$\langle \Phi^{\text{EX}} | \bar{H} | 0 \rangle = 0, \tag{2}$$

in which  $\bar{H}$  denotes the similarity-transformed Hamiltonian,  $\bar{H} = e^{-\hat{T}}\hat{H}e^{\hat{T}}$ , and  $\Phi^{\rm EX}$  represents excited determinants generated by the elementary excitation operators in  $\hat{T}$ , e.g., in CCSD method  $\{|\Phi^{\rm EX}\rangle\} = \{a_a^{\dagger}a_i|0\rangle\} \cup \{a_a^{\dagger}a_i^{\dagger}a_ia_j|0\rangle\}$ . The manifold of elementary ionization operators in  $\hat{R}$  is chosen to be consistent with the excitation manifold in  $\hat{T}$ . In the CCSD method, the ionization operator  $\hat{R}$  is a weighted combination of  $\{a_i\}$  and  $\{a_a^{\dagger}a_ja_i\}$ , i.e.,  $\hat{R} = \sum_i r_i a_i + \frac{1}{2} \sum_{ij,a} r_{ij}^a a_a^{\dagger} a_j a_i$ . The amplitudes  $r_i$  and  $r_{ij}^a$  are determined by configuration-interaction (CI)-like secular equations involving  $\bar{H}$ 

$$\langle \Phi^{\rm IP} | [\bar{H}, \hat{R}] | 0 \rangle = E^{\rm IP} \langle \Phi^{\rm IP} | \hat{R} | 0 \rangle. \tag{3}$$

in which  $|\Phi^{\text{IP}}\rangle$ 's are ionized states generated by the same manifold of elementary ionization operators as in  $\hat{R}$ , e.g.,  $\{|\Phi^{\text{IP, CCSD}}\rangle\} = \{a_i|0\rangle\} \cup \{a_a^{\dagger}a_ja_i|0\rangle\}$ . In the EOMIP-CC calculations, the ground state equations [Eq. (2)] are first solved and then the secular equation [Eq. (3)] is solved for each ionization energy of interest. The present study has employed the series of CCSD, CCSDT, and CCSDTQ methods to systematically approach the full CI limit. The

EOMIP-CCSDT method includes triple excitations  $\{a_a^{\dagger}a_b^{\dagger}a_c^{\dagger}a_ka_ja_i\}$  in  $\hat{T}$  and ionizations with two shake-up excitations  $\{a_a^{\dagger}a_b^{\dagger}a_ka_ja_i\}$  in  $\hat{R}$ , while the EOMIP-CCSDTQ method further includes quadruple excitations  $\{a_a^{\dagger}a_b^{\dagger}a_c^{\dagger}a_l^{\dagger}a_la_ka_ja_i\}$  in  $\hat{T}$  and ionizations with three shake-up excitations  $\{a_a^{\dagger}a_b^{\dagger}a_c^{\dagger}a_la_ka_ja_i\}$  in  $\hat{R}$ . As all the molecules studied here are closed-shell systems, the recent implementation of non-orthogonal spin adaptation for CCSDTQ and EOM-CCSDTQ methods  $^{81,82}$  has played an essential role in the present calculations. We mention that all EOMIP-CCSDTQ calculations presented here have been carried out using the EOM-CCSDTQ code for excitation energies (EE) together with the "continuum-orbital trick", i.e., the electron to be ionized is promoted into a "continuum" orbital with zero orbital energy and no coupling with other orbitals in order to obtain the ionized state.  $^{83}$ 

The core-valence separation (CVS) scheme includes in  $\hat{R}$  only elementary ionization operators that contain at least one core orbital. A simple scheme for the implementation of CVS in a standard EOMIP-CC code suggested by Coriani and Koch has been used in the CVS-EOMIP-CCSD and CVS-EOMIP-CCSDT calculations presented here. Namely, all the R amplitudes for pure valence ionizations  $\{r_{i_v}\}, \{r_{i_vj_v}^a\}$  and etc, in which  $\{i_v, j_v, \cdots\}$  represents occupied valence orbitals, are set to zero during the solution of EOMIP-CC secular equations. The CVS-EOMEE-CCSDTQ calculations using continuum-orbital trick presented here have been carried out using an efficient implementation of the CVS scheme, in which only the R amplitudes involving core orbitals are included in the calculation. The details about the efficient implementation of the CVS scheme for the EOM-CCSDT and EOM-CCSDTQ methods go beyond the present context and will be published elsewhere. It should be mentioned that the original proposal of CVS by Cederbaum et al. neglects Hamiltonian integrals that couple valence and core orbitals. This leads to the same scheme for the solution of excited-state secular equation adopted here together with the frozen-core approximation for the ground state calculation.<sup>84</sup> The purpose of the current study is to benchmark the performance of CVS-EOMIP-CC methods for calculations of core ionization energies. In particular, we aim to understand how the results converge with respect to the excitation rank and how the near-CVS-FCI limit compares with experiment. Therefore, we have correlated core electrons in the solution of ground state CC equations for all calculations presented here.

All calculations presented here have been performed using the CFOUR program pack- ${\rm age.}^{66,80-83,85-87} \ {\rm Relativistic \ effects \ have \ been \ included \ using \ spin-free \ exact \ two-component}$ theory in its one-electron variant (SFX2C-1e) $^{78,79}$  with correlation-consistent basis sets $^{73-75}$ recontracted for the SFX2C-1e scheme. The detailed information about the SFX2C-1e recontracted basis sets can be found at www.cfour.de. The experimental equilibrium bond lengths<sup>88</sup> have been used in calculations for diatomic molecules, while the structures optimized at SFX2C-1e-CCSD(T)/cc-pCVQZ level have been used for all polyatomic molecules. The geometrical parameters are documented in the supplementary material. In order to compare the performance of CVS-EOMIP-CCSD and full EOMIP-CCSD, we carried out CVS-EOMIP-CCSD and full EOMIP-CCSD calculations for 1s ionization energies in HF, F<sub>2</sub>, N<sub>2</sub>, CO, and H<sub>2</sub>O using the aug-cc-pCVXZ (X=T, Q, 5) basis sets. To compare the performance of basis sets with and without diffuse functions, CVS-EOMIP-CCSDT calculations have been performed for 1s ionization energies in HF, CO, N<sub>2</sub>, F<sub>2</sub>, and H<sub>2</sub>O using aug-cc-pCVXZ (X=D, T, Q, 5) and cc-pCVXZ (X=D, T, Q, 5) sets. The performance of CCSD and CCSDT methods is studied by performing CVS-EOMIP-CCSD and CCSDT calculations of 1s ionization energies in HF, CO, N<sub>2</sub>, F<sub>2</sub>, and H<sub>2</sub>O using cc-pCVXZ (X=T, Q, 5) sets and in C<sub>2</sub>H<sub>4</sub>, C<sub>2</sub>H<sub>2</sub>, CH<sub>4</sub>, CH<sub>2</sub>O, CO<sub>2</sub>, NNO, NH<sub>3</sub>, HCN and CH<sub>3</sub>OH using cc-pCVTZ and cc-pCVQZ basis sets. Corrections from quadruple excitations have been obtained as the difference between CVS-EOMIP-CCSDTQ and CVS-EOMIP-CCSDT results using the cc-pCVTZ basis sets for HF, F2, N2, CO, H2O and using the cc-pVTZ basis sets for the other polyatomic molecules. We mention that the experimental ionization energies <sup>89</sup> used in the comparison are all taken from experimental studies without vibrational resolution and thus they approximately correspond to vertical ionization energies. Therefore, it is justified to compare the computed vertical ionization energies with these experimental results.

Finally, CVS-EOMIP-CCSD calculations using cc-pCVTZ and cc-pCVQZ basis sets and CVS-EOMIP-CCSDT/cc-pCVTZ calculations have been carried out for the CH<sub>3</sub>CN and CH<sub>3</sub>NC molecules. All EOMIP-CC and CVS-EOMIP-CC calculations have been tightly converged; the convergence threshold for the maximum norm of the elements in the EOMIP energy-weighted residue vector is  $10^{-5}$  a.u., and the variance of ionization energies is below  $10^{-6}$  E<sub>h</sub> upon convergence.

#### 3 Results and Discussion

#### 3.1 CVS-EOMIP-CC versus full EOMIP-CC

As shown in Table 1 and also in Fig. 1, the 1s ionization energies for HF, F<sub>2</sub>, N<sub>2</sub>, CO, and H<sub>2</sub>O computed at the CVS-EOMIP-CCSD level converge smoothly along aug-cc-pCVXZ (X=T, Q, 5) sets. In contrast, the basis-set convergence of the full EOMIP-CCSD results shows significant oscillations for all cases. This irregular performance of the full EOMIP-CCSD method can be attributed to spurious couplings between the ionized state and highlying pure valence ionized states that are accidentally (quasi-)degenerate. Note that the latter consists of ionization of a valence electron accompanied by an excitation from a valence orbital to a high-lying virtual orbital and should not significantly contribute to core-ionized state. For example, the wave function from the full EOMIP-CCSD/aug-cc-pCVQZ calculation for the fluorine  $1\mathrm{s}^{-1}$  state of  $\mathrm{F}_2$  has a 20% contamination from pure valence ionizations with similar energies. In other words, when basis sets accidentally cover high-lying (continuum) valence ionized states that are (quasi-)degenerate to core-ionized states of interest, unphysical contributions arise and lead to numerical errors in the ionization energies, even if the full EOMIP-CCSD equations are tightly converged. Therefore, the CVS scheme not only expedites the convergence of the EOMIP-CC equations, but also excludes spurious interactions between core-ionized and valence continuum states. Hence, the CVS-EOMIP-CC methods are better than the corresponding full CVS-EOMIP-CC methods for calculations of core-ionized states. Therefore, we have adopted the CVS scheme in all following calculations.

#### 3.2 Effects of diffuse functions on computed ionization energies

Diffuse functions do not contribute much to K-edge ionization energies, as core ionization is a spatially localized process. It is demonstrated in Table 2 that CVS-EOMIP-CCSDT results using aug-cc-pCVXZ (X=D, T, Q, 5) and cc-pCVXZ (X=D, T, Q, 5) sets converge to essentially the same values; the differences between aug-cc-pCV5Z and cc-pCV5Z results are at most 0.03 eV. Interestingly, the cc-pCVXZ results seem to converge more rapidly than the aug-cc-pCVXZ ones. All cc-pCVTZ results are within 0.12 eV in comparison with cc-pCV5Z or aug-cc-pCV5Z results, while the aug-cc-pCVTZ results deviate more substantially from the 5Z results. Double-zeta basis sets (aug-cc-pCVDZ and cc-pCVDZ) do not provide accurate results for K-edge ionization energies and show errors greater than 1 eV for all cases. The use of triple-zeta basis lowers basis-set errors by an order of magnitude. Based on the above observations and analyses of basis-set effects, the cc-pCVXZ (X=T, Q, 5) basis sets have been used in the following studies on the convergence of CVS-EOMIP-CC methods with respect to the excitation rank.

## 3.3 Accuracy of CVS-EOMIP-CCSD and CVS-EOMIP-CCSDT

As shown in Tables 3, 5, and 6, the deviation of CVS-EOMIP-CCSD K-edge ionization energies from experimental values is typically 1-3 eV, while the corresponding deviations for chemical shifts are usually less than 0.5 eV. Here the chemical shifts for the 1s ionization energies of C, N, O, and F are given as the differences with respect to those in CO, N<sub>2</sub>, CO, and HF, respectively. N<sub>2</sub>O appears to be a difficult case, in which the chemical shifts of the terminal nitrogen and the middle nitrogen with respect to N<sub>2</sub> still amount to 0.74 and 0.99 eV, respectively (see Table 6). The relatively slow convergence of the computed ionization energies with respect to the excitation rank within CVS-EOMIP-CC for N<sub>2</sub>O indicates the strong orbital relaxation induced by the creation of the core hole in this molecule. The linear

parametrization of the  $\hat{R}$  operator in EOMCC does not efficiently take orbital rotation into account. Consequently, higher excitations are required when aiming at quantitative results. It can be seen from Tables 3, 5, and 6 that agreement between theory and experiment is much improved when triple excitations are included. Most CVS-EOMIP-CCSDT results are within 0.3 eV in comparison with experimental values. The middle nitrogen in N<sub>2</sub>O remains the most difficult case, with the deviation between CVS-EOMIP-CCSDT and experiment still higher than 0.5 eV.

We mention that, interestingly, the basis-set convergence of the CCSDT results could be quite different from CCSD. For example, the CVS-EOMIP-CCSD/cc-pCVTZ result for F 1s ionization energies in HF is 0.22 eV smaller than the CVS-EOMIP-CCSD/cc-pCV5Z result, while the CVS-EOMIP-CCSDT/cc-pCVTZ value is 0.02 eV higher than the CVS-EOMIP-CCSDT/cc-pCV5Z result. Therefore, additivity schemes that augment lower-level CC results obtained using larger basis sets with corrections from high-level CC calculations using smaller basis sets should be used with care for core ionization energies, especially when aiming at high accuracy. Despite the profound coupling between electron-correlation and basis-set effects, basis-set convergence for core-ionization energies is pretty fast. The cc-pCVTZ basis in general provides accurate treatment of basis-set effects, while CVS-EOMIP-CCSDT/cc-pCVQZ results are within 0.02 eV in comparison with those of CVS-EOMIP-CCSDT/cc-pCV5Z.

## 3.4 Quadruples corrections

For all diatomic molecules in the benchmark set as well as for  $H_2O$ , effects of quadruple excitations have been studied at the CVS-EOMIP-CCSDTQ/cc-pCVTZ level and are summarized in Table 3. The absolute values for the quadruples corrections to K-edge ionization energies in these small molecules range from 0.08 to 0.23 eV, about an order of magnitude smaller than the corresponding triples corrections. As it is a reasonable assumption that corrections from even higher excitations are smaller, the CVS-EOMIP-CCSDTQ results for

K-edge ionization energies are expected to be very close to the corresponding FCI results.

As CVS-EOMIP-CCSDTQ/cc-pCVTZ is still too expensive for other polyatomic molecules in the benchmark set, we have investigated the dependence of quadruples corrections to corecorrelating functions in the basis sets. In Table 4 we summarize the computed quadruples corrections using the cc-pCVTZ and cc-pVTZ basis sets as well as a combination of ccpCVTZ and cc-pVTZ, in which cc-pCVTZ is used for the targeted atom and cc-pVTZ is used for all other atoms. The core-correlating functions on other atomic centers seem to have negligible contributions, as the cc-pCVTZ/cc-pVTZ results are essentially indistinguishable from cc-pCVTZ results. The cc-pVTZ results for absolute core-ionization energies are 0.2-0.5 eV lower than the cc-pCVTZ ones, while cc-pVTZ calculations seem to provide reasonably good estimates for quadruples corrections. We have obtained quadruples corrections for all other polyatomic molecules except CH<sub>3</sub>OH using the cc-pVTZ basis and the results are presented in Table 5. Computational results with inclusion of quadruples corrections show a standard deviation of 0.10 eV from experiment and can be regarded as essentially quantitative. For the middle nitrogen in N<sub>2</sub>O, the quadruples correction amounts to -0.31 eV, and the inclusion reduces the deviation with respect to experiment from 0.54 eV to 0.23 eV. The excellent agreement between CVS-EOMIP-CC results with inclusion of quadruple excitations and experimental values indicates that in calculations of core-ionization energies the approximation of neglecting the continuum part of the wave function in the CVS scheme is numerically insignificant.

## 3.5 Carbon 1s ionization energies in $\mathrm{CH_3CN}$ and $\mathrm{CH_3NC}$

CVS-EOMIP-CCSD/cc-pCVTZ, CVS-EOMIP-CCSD/cc-pCVQZ, and CVS-EOMIP-CCSDT/cc-pCVTZ calculations have been carried out for CH<sub>3</sub>CN and CH<sub>3</sub>NC and compared with two different sets of experimental results available in the literature. <sup>90,91</sup> As shown in Table 7, comparison between CVS-EOMIP-CCSD/cc-pCVTZ and CVS-EOMIP-CCSD/cc-pCVQZ confirms that basis-set effects beyond cc-pCVTZ play a minor role. On the other hand,

triples corrections are significant. Although the absolute magnitude for the triples correction to the relative shift between the two carbons in CH<sub>3</sub>CN is only 0.17 eV, the inclusion of triples corrections reverses the ordering of carbon 1s ionization energies for the methyl carbon and the cyano carbon. The computational results (292.90 eV for cyano carbon and 292.81 eV for methyl carbon with a relative shift of 0.09 eV) differ significantly from the more recent experimental results (292.45 eV for cyano carbon and 292.98 eV for methyl carbon with a relative shift of -0.53 eV). Since the triples correction to this relative shift is only 0.17 eV, we do not expect the corresponding quadruples correction to be close to the difference of -0.62 eV between the computational and experimental results. Interestingly, the computational results qualitatively agree with an earlier experiment with a lower resolution (293.2 for cyano carbon and 293.1 for methyl carbon with a relative shift of 0.1 eV). It is also observed that, for CH<sub>3</sub>NC, our CVS-EOMIP-CCSDT/cc-pCVTZ results agree very well with the more recent experimental study, and differ considerably from the earlier ones. We would suggest an experimental re-investigation of CH<sub>3</sub>CN to settle these issues.

## 4 Conclusion

The present manuscript reports benchmark calculations for K-edge ionization energies in C, N, O, F using core-valence-separated (CVS) equation-of-motion ionization-potential coupled-cluster (EOMIP-CC) methods. It is shown that the CVS scheme excludes spurious couplings between core-ionized states and valence continuum states and thus the CVS-EOMIP-CC methods turn out to be better than the parent EOMIP-CC methods in terms of numerical accuracy. Convergence of computed K-edge ionization energies within the hierarchy of CVS-EOMIP-CC methods has been carefully studied. Essentially quantitative agreement between computed and experimental results is obtained when quadruples contributions are included. We mention that the magnitude of the remaining errors of CCSDTQ for the electronic contributions to K-edge ionization energies are comparable with or even smaller than that of

vibrational corrections. Therefore, computational studies with vibrational corrections taken into account and the comparison of the corresponding results with vibrationally resolved experimental results would be of great interest for future studies. Finally, computational results for carbon 1s ionization energies in  $\mathrm{CH_3CN}$  and  $\mathrm{CH_3NC}$  suggest an experimental re-investigation of these molecules.

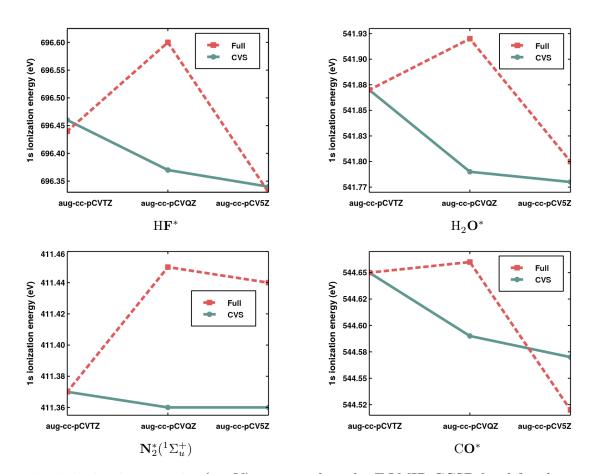


Figure 1: 1s ionization energies (in eV) computed at the EOMIP-CCSD level for the atoms in bold letter marked with an asterisk. "CVS" denotes the use of the core-valence separation scheme. "Full" stands for the solution of EOMIP-CCSD equations in the full singles and doubles space.

Table 1: 1s ionization energies (in eV) computed at the EOMIP-CCSD level for the atoms in bold letter marked with an asterisk. "CVS" denotes the use of the core-valence separation scheme, while "full" stands for the solution of EOMIP-CCSD equations in the full singles and doubles space.

		aug-cc-pCVTZ	aug-cc-pCVQZ	aug-cc-pCV5Z
$\mathrm{H}\mathbf{F}^*$	full	696.44	696.60	696.33
	CVS	696.46	696.37	696.34
$\mathbf{F}_2^*(^1\Sigma_g^+)$	full	699.20	699.59	699.07
	CVS	699.23	699.14	699.12
$\mathbf{F}_2^*(^1\Sigma_u^+)$	full	699.19	699.03	699.06
	CVS	699.22	699.13	699.11
$\mathbf{N}_2^*(^1\Sigma_g^+)$	full	411.47	411.51	411.48
	CVS	411.47	411.46	411.46
$\mathbf{N}_2^*(^1\Sigma_u^+)$	full	411.37	411.45	411.44
	CVS	411.37	411.36	411.36
$\mathbf{C}^*$ O	full	297.73	297.73	297.74
	CVS	297.72	297.71	297.72
C <b>O</b> *	full	544.65	544.66	544.52
	CVS	544.65	544.59	544.57
$\mathrm{H}_2\mathbf{O}^*$	full	541.87	541.92	541.80
	CVS	541.87	541.79	541.78

Table 2: 1s ionization energies (in eV) computed at the CVS-EOMIP-CCSDT level for the atoms in bold letter marked with an asterisk. "CXZ" and "ACXZ" (X=D, T, Q, 5) represent cc-pCVXZ and aug-cc-pCVXZ sets, respectively. The SFX2C-1e scheme has been used to treat scalar-relativistic effects.

Molecule	ACDZ	ACTZ	ACQZ	AC5Z	CDZ	CTZ	CQZ	C5Z
$\mathrm{H}\mathbf{F}^*$	696.66	694.45	694.28	694.23	695.98	694.22	694.19	694.20
$\mathbf{C}^*\mathrm{O}$	297.85	296.53	296.46	296.45	297.83	296.47	296.44	296.45
$\mathrm{C}\mathbf{O}^*$	544.50	542.64	542.50	542.46	544.29	542.57	542.48	542.46
$\mathbf{N}_2^*(^1\Sigma_g^+)$	411.89	410.20	410.11	410.09	411.69	410.11	410.08	410.07
$\mathbf{N}_2^*(^1\Sigma_u^+)$	411.80	410.11	410.03	410.01	411.60	410.03	409.99	409.99
$\mathbf{F}_2^*(^1\Sigma_g^+)$	699.10	696.90	696.74	696.70	698.59	696.73	696.67	696.67
$\mathbf{F}_2^*(^1\Sigma_u^+)$	699.09	696.89	696.73	696.69	698.58	696.72	696.66	696.66
$\mathrm{H}_2\mathbf{O}^*$	541.90	540.00	539.85	539.81	541.36	539.79	539.76	539.78

Table 3: 1s ionization energies (in eV) for the atoms in bold letter marked with an asterisk. "CXZ" (X=T, Q, 5) denotes cc-pCVXZ sets. The deviations from experimental values are enclosed in parentheses. The core-valence separation scheme has been used. Scalar-relativistic effects have been taken into account using the SFX2C-1e scheme.

Molecule	EOMIP-CCSD			EON	MIP-CC	SDT	EOMIP-CCSDTQ	4 . 4 . 1a	Exp. 89
Wiolectile	CTZ	CQZ	C5Z	$\overline{\text{CTZ}}$	CQZ	C5Z	CTZ	total	Exp.
$\mathrm{H}\mathbf{F}^*$	696.09	696.23	696.31	694.22	694.19	694.20	694.45	694.44	694.23
	(1.86)	(2.00)	(2.08)	(-0.01)	(-0.04)	(-0.03)	(0.22)	(0.21)	
$\mathbf{C}^*O$	297.64	297.69	297.71	296.47	296.44	296.45	296.30	296.27	296.21
	(1.43)	(1.48)	(1.50)	(0.26)	(0.23)	(0.24)	(0.09)	(0.06)	
$CO^*$	544.57	544.56	544.57	542.57	542.48	542.46	542.68	542.57	542.55
	(2.02)	(2.01)	(2.02)	(0.02)	(-0.07)	(-0.09)	(0.13)	(0.02)	
$\mathbf{N}_2^*(^1\Sigma_g^+)$	411.35	411.41	411.43	410.11	410.08	410.07	410.03	409.99	409.98
	(1.37)	(1.43)	(1.45)	(0.13)	(0.10)	(0.09)	(0.05)	(0.01)	
$\mathbf{N}_2^*(^1\Sigma_u^+)$	411.25	411.31	411.33	410.03	409.99	409.99	409.95	409.91	409.98
	(1.27)	(1.33)	(1.35)	(0.05)	(0.01)	(0.01)	(-0.03)	(-0.07)	
$\mathbf{F}_2^*(^1\Sigma_g^+)$	699.01	699.06	699.09	696.73	696.67	696.67	696.82	696.75	696.69
	(2.32)	(2.37)	(2.40)	(0.04)	(-0.02)	(-0.02)	(0.13)	(0.06)	
$\mathbf{F}_2^*(^1\Sigma_u^+)$	699.00	699.05	699.08	696.72	696.66	696.66	696.81	696.75	696.69
	(2.31)	(2.36)	(2.39)	(0.03)	(-0.03)	(-0.03)	(0.12)	(0.06)	
$\mathrm{H}_2\mathbf{O}^*$	541.53	541.65	541.74	539.79	539.76	539.78	539.99	539.98	539.90
	(1.63)	(1.75)	(1.84)	(-0.11)	(-0.14)	(-0.11)	(0.09)	(0.08)	

<sup>&</sup>lt;sup>a</sup> CCSDT/cc-pCV5Z results augmented with quadruples corrections obtained using the cc-pCVTZ basis.

Table 4: 1s ionization energies (in eV) for the atoms in bold letter marked with an asterisk computed using CVS-EOMIP-CC methods.

Molecules	Method	cc-pCVTZ	$cc\text{-}pCVTZ/cc\text{-}pVTZ^a$	cc-pVTZ
$\mathbf{C}^*$ O	CCSDT	296.47	296.47	295.97
	CCSDTQ	296.30	296.29	295.81
	$\Delta_{ m Q}$	-0.17	-0.17	-0.16
$\mathrm{C}\mathbf{O}^*$	CCSDT	542.57	542.57	542.21
	CCSDTQ	542.68	542.68	542.34
	$\Delta_{ m Q}$	0.11	0.11	0.13
$\mathbf{N}_2^*(\Sigma_g^+)$	CCSDT	410.11	410.11	409.68
	CCSDTQ	410.03	410.03	409.62
	$\Delta_{ m Q}$	-0.08	-0.08	-0.07
$\mathbf{N}_2^*(\Sigma_u^+)$	CCSDT	410.03	410.03	409.60
	CCSDTQ	409.95	409.95	409.53
	$\Delta_{ m Q}$	-0.08	-0.08	-0.06
$\mathbf{F}_2^*(\Sigma_g^+)$	CCSDT	696.73	696.73	696.45
	CCSDTQ	696.82	696.82	696.57
	$\Delta_{ m Q}$	0.09	0.09	0.13
$\mathbf{F}_2^*(\Sigma_u^+)$	CCSDT	696.72	696.72	696.44
	CCSDTQ	696.81	696.81	696.56
	$\Delta_{ m Q}$	0.09	0.09	0.13
$\mathrm{H}\mathbf{F}^*$	CCSDT	694.22	694.22	693.93
	CCSDTQ	694.45	694.45	694.19
	$\Delta_{ m Q}$	0.23	0.23	0.26

<sup>&</sup>lt;sup>a</sup> cc-pCVTZ basis for the targeted atom and cc-pVTZ basis for the other atoms.

Table 5: Computed 1s ionization energies (in eV) for the atoms in bold letter marked with an asterisk. CXZ (X=T,Q) denote cc-pCVXZ basis sets. The core-valence separation scheme has been used, and relativistic effects have been treated using the SFX2C-1e scheme. "MAE" represents the mean absolute deviation with respect to experimental values.

	EOMIP-CCSD		EOMIP-	EOMIP-CCSDT		D h	D 89	Λ (Th T )
	CTZ	CQZ	$\overline{\text{CTZ}}$	CQZ	$\Delta_{ m Q}^{ m a}$	Best theory <sup>b</sup>	Exp. °°	$\Delta(\text{Theory-Exp})$
$\mathbf{C}_2^* \mathbf{H}_4(A_g)$	292.32	292.32	290.89	290.81	0.00	290.81	290.82	-0.01
$\mathbf{C}_2^* \mathbf{H}_4(B_{2u})$	292.26	292.27	290.85	290.76	0.00	290.77	290.82	-0.05
$\mathbf{C}_2^*\mathbf{H}_2(^1\Sigma_g^+)$	292.72	292.73	291.45	291.36	-0.06	291.31	291.14	0.17
$\mathbf{C}_2^*\mathbf{H}_2(^1\Sigma_u^+)$	292.62	292.63	291.36	291.28	-0.05	291.22	291.14	0.08
$\mathbf{C}^*\mathrm{H}_4$	292.07	292.04	290.86	290.75	0.05	290.80	290.91	-0.11
$\mathrm{CH}_2\mathbf{O}^*$	541.68	541.70	539.44	539.36	0.12	539.48	539.48	0.00
$\mathbf{C}^*\mathrm{H}_2\mathrm{O}$	295.94	295.99	294.62	294.58	-0.12	294.46	294.47	-0.01
$\mathrm{C}\mathbf{O}_2^*$	543.70	543.73	541.40	541.35	-0.01	541.34	541.28	0.06
$\mathbf{C}^*\mathrm{O}_2$	299.52	299.59	298.03	298.02	-0.26	297.76	297.69	0.07
$NNO^*$	543.92	543.96	541.63	541.57	-0.02	541.55	541.42	0.13
$NN^*O$	414.90	414.96	413.15	413.13	-0.31	412.82	412.59	0.23
$\mathbf{N}^* \mathrm{NO}$	410.76	410.83	408.92	408.90	-0.11	408.79	408.71	0.08
$\mathbf{N}^*\mathrm{H}_3$	407.04	407.13	405.55	405.51	0.14	405.65	405.56	0.09
$\mathrm{HC}\mathbf{N}^*$	408.45	408.47	406.88	406.81	0.01	406.82	406.78	0.04
$HC^*N$	294.66	294.68	293.59	293.53	-0.12	293.41	293.40	0.01
$\mathrm{CH_3}\mathbf{O}^*\mathrm{H}$	541.05	541.11	539.00	538.95	-	-	539.11	-0.16
$\mathbf{C}^*\mathrm{H}_3\mathrm{OH}$	293.76	293.79	292.47	292.41	-	-	292.43	-0.02
MAE	1.74	1.78	0.16	0.15	-	0.08	-	-

<sup>&</sup>lt;sup>a</sup> Quadruples corrections obtained using the cc-pVTZ basis.

 $<sup>^{\</sup>rm b}$  CCSDT/cc-pCVQZ results augmented with quadruples corrections obtained using the cc-pVTZ basis.

Table 6: Chemical shifts (in eV) of C and O 1s ionization energies (IEs) relative to CO, N 1s IEs relative to  $N_2$ , and F 1s IEs relative to HF. The cc-pCVQZ basis has been used in all CVS-EOMIP-CCSD and CCSDT calculations, while all quadruples corrections have been obtained using the cc-pVTZ basis. The deviations between computation and experiment are given in parenthesis.

	Experiment	CCSD	CCSDT	CCSDTQ
$\mathbf{C}^*$ O	296.21	297.69	296.44	296.28
$\mathbf{C}^*\mathrm{H}_4$	-5.30	-5.64(-0.34)	-5.69(-0.39)	-5.48(-0.18)
$\mathbf{C}_2^* \mathbf{H}_2$	-5.07	-5.01(0.06)	$-5.12(-0.05)^{a}$	-5.01(0.06) a
$\mathbf{C}_2^* \mathbf{H}_4$	-5.39	-5.39(0.00)	$-5.65(-0.26)^{a}$	-5.49(-0.10) <sup>a</sup>
$\mathbf{C}^*\mathbf{H}_2\mathbf{O}$	-1.74	-1.70(0.04)	-1.86(-0.12)	-1.82(-0.08)
$\mathbf{C}^*\mathrm{O}_2$	1.48	1.90(0.42)	1.58(0.10)	1.48(0.00)
$HC^*N$	-2.81	-3.00(-0.19)	-2.91(-0.10)	-2.87(-0.06)
$\mathbf{C}^*\mathrm{H}_3\mathrm{OH}$	-3.78	-3.90(-0.12)	-4.03(-0.25)	-
$\mathbf{N}_2^*$	409.98	411.36 <sup>a</sup>	410.03 <sup>a</sup>	409.97 <sup>a</sup>
N*NO	-1.27	-0.53(0.74)	-1.13(0.14)	-1.17(0.10)
$NN^*O$	2.61	3.60(0.99)	3.10(0.49)	2.85(0.24)
$\mathbf{N}^* \mathbf{H}_3$	-4.42	-4.23(0.19)	-4.52(-0.10)	-4.32(0.10)
$HCN^*$	-3.20	-2.88(0.32)	-3.22(-0.02)	-3.15(0.05)
C <b>O</b> *	542.55	544.56	542.48	542.61
$\mathrm{H}_2\mathbf{O}^*$	-2.65	-2.91(-0.26)	-2.71(-0.06)	-2.63(0.02)
$\mathrm{CH}_2\mathbf{O}^*$	-3.07	-2.86( 0.21)	-3.12(-0.05)	-3.13(-0.06)
$\mathrm{C}\mathbf{O}_2^*$	-1.27	-0.83( 0.44)	-1.13( 0.14)	-1.27(0.00)
$N_2\mathbf{O}^*$	-1.13	-0.60( 0.53)	-0.90( 0.23)	-1.06(0.07)
$\mathrm{CH}_3\mathbf{O}^*\mathrm{H}$	-3.44	-3.45(-0.01)	-3.53(-0.09)	-
$\mathrm{H}\mathbf{F}^*$	694.23	696.23	694.19	694.45
$\mathbf{F}_2^*$	2.46	2.82(0.36) <sup>a</sup>	$2.47(0.01)^{a}$	2.34(-0.12) <sup>a</sup>

<sup>&</sup>lt;sup>a</sup> An average of gerade and ungerade states.

Table 7: 1s ionization energies (in eV) for the atoms in bold letter marked with an asterisk.

	D 91	D 00	CVS-EOM	IIP-CCSD	CVS-EOMIP-CCSDT
	Exp. 91	Exp. 90	cc-pCVTZ	cc-pCVQZ	cc-pCVTZ
$\mathrm{CH_3}\mathbf{C}^*\mathrm{N}$	292.45	293.2	294.06	294.09	292.90
$\mathbf{C}^*\mathrm{H}_3\mathrm{CN}$	292.98	293.1	294.13	294.13	292.81
$\mathrm{CH_{3}C}\mathbf{N}^{*}$	405.64	405.9	407.52	407.54	405.71
$\overline{\mathrm{CH_3N}\mathbf{C}^*}$	292.37	293.8	294.07	294.12	292.35
$\mathbf{C}^*\mathbf{H}_3\mathbf{NC}$	293.35	293.1	294.78	294.78	293.41
$\mathrm{CH_3}\mathbf{N}^*\mathrm{C}$	406.67	407.1	408.38	408.40	407.02

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## Supporting Information Available

The geometrical parameters for the molecules used in the present study have been compiled and given in the supplementary material. This material is available free of charge via the Internet at http://pubs.acs.org/.

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## **Graphical TOC Entry**

