

# BIC-based Speaker Segmentation Using Divide-and-Conquer Strategies with Application to Speaker Diarization

Shih-Sian Cheng, Hsin-Min Wang, *Member, IEEE* and Hsin-Chia Fu, *Member, IEEE*

**Abstract**—In this paper, we propose three divide-and-conquer approaches for BIC-based speaker segmentation. The approaches detect speaker changes by recursively partitioning a large analysis window into two sub-windows and recursively verifying the merging of two adjacent audio segments using  $\Delta BIC$ , a widely-adopted distance measure of two audio segments. We compare our approaches to three popular distance-based approaches, namely, Chen and Gopalakrishnan’s window-growing-based approach, Siegler *et al.*’s fixed-size sliding window approach, and Delacourt and Wellekens’s DISTBIC approach, by performing computational cost analysis and conducting speaker change detection experiments on two broadcast news data sets. The results show that the proposed approaches are more efficient and achieve higher segmentation accuracy than the compared distance-based approaches. In addition, we apply the segmentation approaches discussed in this paper to the speaker diarization task. The experiment results show that a more effective segmentation approach leads to better diarization accuracy.

**Index Terms**—speaker segmentation, speaker change detection, Bayesian Information Criterion, divide-and-conquer, speaker diarization

## I. INTRODUCTION

The goal of speaker (audio) segmentation is to detect speaker (acoustic) change boundaries in an audio stream. In the last decade, researchers in the speech processing community have expended a great deal of effort on this problem because of its application to many speech and audio processing tasks, such as audio classification [1], [2], automatic transcription of audio recordings [3], [4], speaker tracking [5], [6], and speaker diarization [7], [8].

Existing audio segmentation approaches generally fall into two categories, namely, distance-based segmentation [9], [10], [11], [12], [13] and model-decoding-based segmentation [4], [11]. In distance-based segmentation, a distance measure of two audio segments is defined first, and then an acoustic change detection strategy is designed based on the distance

measure. In contrast to model-decoding-based segmentation, which detects acoustic changes in a supervised manner, distance-based segmentation has the advantage that acoustic changes can be detected in an unsupervised manner, i.e., *a priori* knowledge about the content of the input audio stream is unnecessary. In this paper, we focus on distance-based segmentation.

When low-level acoustic features like mel-scale frequency cepstral coefficients (MFCCs) are used in distance-based segmentation, the distance measure is usually derived from a statistical modeling framework. More precisely, it is assumed that the feature vectors in each of the two audio segments arise from some probability distribution (e.g., the multivariate Gaussian distribution); then, the distance between the two segments is represented by the dissimilarity between the two distributions. Several distance measures have been proposed, e.g., the Kullback-Leibler distance (KL or KL2) [10], the Generalized Likelihood Ratio (GLR) [9], [14],  $\Delta BIC$  [11], [15], [16], [13], [17], [18], the Bhattacharyya distance [12], and the XBIC [19]. In addition, some high-level features have been used for audio segmentation; e.g., the spectrum flux and zero-crossing rate (ZCR) [20], [21], and the smoothed zero-crossing rate (SZCR) [22].

Window-growing-based segmentation (WinGrow) [11], [15], [23], [17], fixed-size sliding window segmentation (FixS-lid) [10], [12], [24], [25], [26], and DISTBIC [9] are three popular distance-based segmentation approaches.

- 1) The WinGrow approach was first proposed by Chen and Gopalakrishnan [11]. For the distance measure of two audio segments, they used the Bayesian Information Criterion (BIC) [27], [28] to evaluate the following two hypotheses: 1) the union of the feature vectors of the two segments forms a Gaussian cluster in the feature space, and 2) the feature vectors of each segment form a distinct Gaussian cluster. Then, the difference between the two evaluation scores,  $\Delta BIC$ , is used as the distance measure. In the acoustic change detection procedure, a small analysis window is put at the beginning of the audio stream initially. If no change point is detected in that analysis window, the search range is increased. The decent segmentation accuracy of this approach is widely recognized; however, as the window size grows, it incurs a heavy computational cost due to numerous  $\Delta BIC$  computations, especially when the audio stream contains many long homogenous segments. To reduce the computational cost, Tritschler and Gopinath [29] proposed

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some heuristics that ignore the distance computations at locations where acoustic changes are unlikely to occur. Zhou and Hansen [17] used Hotelling's  $T^2$ -Statistic, which has the advantage of low computational cost, as the distance measure in the WinGrow detection process, and only used  $\Delta BIC$  to verify the acoustic change candidates. In addition, [15] and [13] proposed more efficient implementations for the  $\Delta BIC$  computation that do not affect the segmentation accuracy.

- 2) In FixSlid, a certain distance measure is used to evaluate the dissimilarity between two adjacent windows that slide along the audio stream to produce a distance curve; then, some heuristic thresholds are used to judge whether the locations of peaks are acoustic changes. To detect the change boundary associated with a short homogeneous segment, the size of the analysis window is usually set at a small value (e.g., two seconds). This is a dilemma because a small analysis window does not contain sufficient feature vectors to obtain a reliable distance statistic. For this approach, the KL2, GLR, and  $\Delta BIC$  derived from the uni-Gaussian model are popular distance measures because they have the advantage of low computational cost; however, their effectiveness may be limited due to the limited generalization ability of uni-Gaussian. In [25], the authors proposed a bilateral scoring approach for calculating the distance between two segments based on adapted Gaussian mixture models (GMMs). Because of the good generalization ability of GMMs, this approach has been shown to be more effective than WinGrow and XBIC, which are developed on the basis of the uni-Gaussian model; however, it suffers from a higher computational cost due to the requirement for the adaptation of GMMs and calculation of mixture likelihoods in the distance measure.
- 3) Under the DISTBIC approach, the input audio stream is first segmented by FixSlid; then, the acoustic change candidates are verified sequentially by segment merging using  $\Delta BIC$ . In practical use of this approach, FixSlid is usually applied to over-segment the audio stream to ensure a low miss detection rate at the cost of a high false alarm rate; then, the segment merging process is applied to reduce false alarms while maintaining the low miss detection rate. This approach is highly efficient. Moreover, it has been reported that this approach achieves decent segmentation accuracy [9]. The sequential segment merging process can be replaced by the hierarchical agglomerative clustering (HAC), which has been widely used in many speaker diarization systems [7], [8], [30]. However, it is not as efficient as DISTBIC because of the essential computational cost of HAC.

Although WinGrow is more efficient than the adapted-GMMs approach while maintaining high segmentation accuracy, the computational cost is still quite considerable when applying it to a large-scale task, e.g., the indexing of a database containing thousands of audio recordings. Therefore, more efficient segmentation approaches are desirable. In this paper,

we propose three divide-and-conquer approaches for distance-based speaker segmentation. The first approach (DACDec1) detects speaker changes by recursively partitioning a large analysis window into two sub-windows at the position with the largest positive  $\Delta BIC$  value obtained by Chen's one-change-point detection algorithm [11], rather than by applying a size-growing analysis window. All the divided points are output as change points. The second approach (DACDec2), which is a variant of DACDec1, recursively partitions a large analysis window into two sub-windows at the position with the largest  $\Delta BIC$  value, no matter whether it is larger than zero or not. It then recursively verifies whether the divided points with negative  $\Delta BIC$  values calculated in the division stage are speaker changes based on the new  $\Delta BIC$  measurements of their left and right neighbor segments. The third approach (DACDec3) is a recursive variant of DISTBIC. It recursively partitions an audio stream at the locations of speaker change candidates obtained by FixSlid, and then recursively verifies those candidates based on the  $\Delta BIC$  measurements of their left and right neighbor segments. To compare the performance of WinGrow, FixSlid, DISTBIC, the HAC-based approach and the proposed approaches, we conducted speaker change detection experiments on two broadcast news data sets, namely the MATBN corpus [31] and the broadcast news data in the 2003 NIST rich transcription evaluation data (RT03) [32]. For the efficiency comparison, we analyzed their computational costs and reported their respective run times in the experiments. The experiment results show that DACDec1 and DACDec2's recursive (top-down) multiple-change-point detection strategies are more effective and efficient than WinGrow's bottom-up multiple-change-point detection strategy. The results also show that, by providing a more effective and efficient segment merging process, DACDec3 outperforms DISTBIC and the HAC-based approach. Moreover, it achieves similar segmentation accuracy as WinGrow at a much lower computational cost. We applied the segmentation approaches discussed in this paper to the speaker diarization task, where the segmentation result is input to a HAC speaker clustering module. The experiment results on RT03 show that a more effective segmentation approach leads to better diarization accuracy.

The remainder of this paper is organized as follows. To help explain our proposed approaches, we review the  $\Delta BIC$  distance measure and the WinGrow approach in Section II. We then present the proposed divide-and-conquer approaches for speaker segmentation in Section III. In Section IV, we analyze the computational costs of the baseline approaches and the proposed approaches. Section V details the experiments on speaker segmentation, Section VI details the application of the segmentation approaches to the speaker diarization task, and Section VII contains some concluding remarks.

## II. WINDOW-GROWING-BASED SEGMENTATION

We review the  $\Delta BIC$  distance measure of two audio segments in Section II-A and window-growing-based segmentation (WinGrow) in Section II-B.

### A. $\Delta BIC$ as the distance measure of two audio segments

1) *Model selection and BIC*: Given a data set  $\mathcal{Z} = \{\mathbf{z}_1, \mathbf{z}_2, \dots, \mathbf{z}_n\} \subset \mathbb{R}^d$  and a set of candidate models  $\mathcal{M} = \{M_1, M_2, \dots, M_k\}$ , the purpose of model selection is to choose the model that best fits the distribution of  $\mathcal{Z}$  from  $\mathcal{M}$ . When using the Bayesian Information Criterion (BIC) for model selection, the BIC value of  $M_i$  for  $\mathcal{Z}$  is

$$BIC(M_i, \mathcal{Z}) = \log p(\mathcal{Z} | \hat{\Theta}_i) - \frac{1}{2} \lambda \#(M_i) \log n, \quad (1)$$

where  $\lambda = 1$ ,  $\hat{\Theta}_i$  is the maximum likelihood estimate of the parameter set of  $M_i$ , and  $\#(M_i)$  is the number of parameters of  $M_i$ . The model with the largest BIC value will be selected.

2)  *$\Delta BIC$  as the distance measure*: Given two audio segments represented by feature vectors,  $\mathcal{X} = \{\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_{n_x}\} \subset \mathbb{R}^d$  and  $\mathcal{Y} = \{\mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_{n_y}\} \subset \mathbb{R}^d$ , we evaluate the following two hypotheses [11]:

$$\begin{aligned} H_0 : \mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_{n_x}, \mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_{n_y} &\sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma}), \\ H_1 : \mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_{n_x} &\sim \mathcal{N}(\boldsymbol{\mu}_{\mathcal{X}}, \boldsymbol{\Sigma}_{\mathcal{X}}); \\ \mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_{n_y} &\sim \mathcal{N}(\boldsymbol{\mu}_{\mathcal{Y}}, \boldsymbol{\Sigma}_{\mathcal{Y}}). \end{aligned} \quad (2)$$

$H_0$  posits that  $\mathcal{X}$  and  $\mathcal{Y}$  are derived from the same multivariate Gaussian, while  $H_1$  posits that they are derived from two distinct multivariate Gaussians.

Let  $\mathcal{Z} = \mathcal{X} \cup \mathcal{Y}$  and  $n = n_x + n_y$ . Then, the  $\Delta BIC$  value can be computed as the difference between the BIC values of  $H_1$  and  $H_0$  as follows:

$$\begin{aligned} \Delta BIC_{\{\mathcal{X}, \mathcal{Y}\}} &= BIC(H_1, \mathcal{Z}) - BIC(H_0, \mathcal{Z}) \\ &= \log p(\mathcal{X} | \hat{\boldsymbol{\mu}}_{\mathcal{X}}, \hat{\boldsymbol{\Sigma}}_{\mathcal{X}}) + \log p(\mathcal{Y} | \hat{\boldsymbol{\mu}}_{\mathcal{Y}}, \hat{\boldsymbol{\Sigma}}_{\mathcal{Y}}) \\ &\quad - \log p(\mathcal{Z} | \hat{\boldsymbol{\mu}}, \hat{\boldsymbol{\Sigma}}) - \frac{1}{2} \lambda (d + \frac{1}{2} d(d+1)) \log n \\ &= \frac{n}{2} \log |\hat{\boldsymbol{\Sigma}}| - \frac{n_x}{2} \log |\hat{\boldsymbol{\Sigma}}_{\mathcal{X}}| - \frac{n_y}{2} \log |\hat{\boldsymbol{\Sigma}}_{\mathcal{Y}}| \\ &\quad - \frac{1}{2} \lambda (d + \frac{1}{2} d(d+1)) \log n, \end{aligned} \quad (3)$$

where  $\hat{\boldsymbol{\mu}}$ ,  $\hat{\boldsymbol{\mu}}_{\mathcal{X}}$ , and  $\hat{\boldsymbol{\mu}}_{\mathcal{Y}}$  are, respectively, the sample mean vectors of  $\mathcal{Z}$ ,  $\mathcal{X}$ , and  $\mathcal{Y}$ ;  $\hat{\boldsymbol{\Sigma}}$ ,  $\hat{\boldsymbol{\Sigma}}_{\mathcal{X}}$ , and  $\hat{\boldsymbol{\Sigma}}_{\mathcal{Y}}$  are, respectively, the sample covariance matrices of  $\mathcal{Z}$ ,  $\mathcal{X}$ , and  $\mathcal{Y}$ ; and  $d$  is the dimension of the feature vector [13]. The larger the value of  $\Delta BIC$ , the less similar the two segments will be; thus, the larger the distance between the two segments will be. When  $\lambda = 0$ , the  $\Delta BIC$  distance between two segments is equivalent to the GLR distance [11], [33].

### B. Window-growing-based segmentation

1) *One-change-point detection*: Let the feature vectors of the input audio stream be  $\mathcal{Z} = \{\mathbf{z}_1, \mathbf{z}_2, \dots, \mathbf{z}_n\}$ . In Chen and Gopalakrishnan's one-change-point detection algorithm [11] (denoted as OCD-Chen in this paper), it is assumed that there is at most one change point in  $\mathcal{Z}$ . Then, the  $\Delta BIC_{\{\mathcal{X}_i, \mathcal{Y}_i\}}(i)$  value for  $i_{min} < i \leq n - i_{min}$  is computed as

$$\begin{aligned} \Delta BIC_{\{\mathcal{X}_i, \mathcal{Y}_i\}}(i) &= \frac{n}{2} \log |\hat{\boldsymbol{\Sigma}}| - \frac{i}{2} \log |\hat{\boldsymbol{\Sigma}}_{\mathcal{X}_i}| - \frac{n-i}{2} \log |\hat{\boldsymbol{\Sigma}}_{\mathcal{Y}_i}| \\ &\quad - \frac{1}{2} \lambda (d + \frac{1}{2} d(d+1)) \log n, \end{aligned} \quad (4)$$

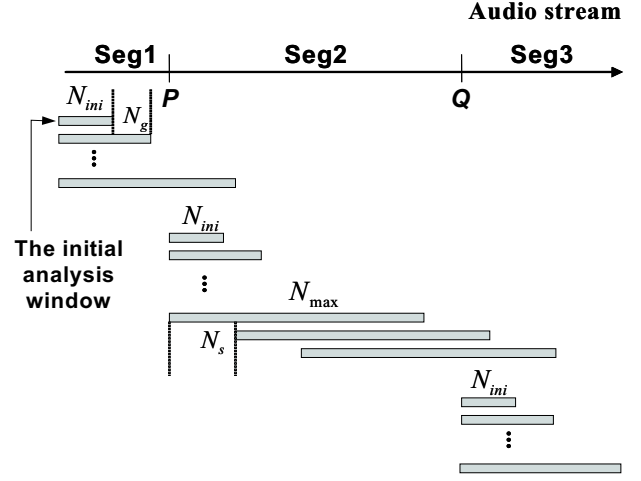


Fig. 1. Diagram of the multiple-change-point detection in window-growing-based segmentation (WinGrow). The audio stream contains three segments, namely Seg1, Seg2, and Seg3;  $P$  and  $Q$  denote the change points.

where  $\hat{\boldsymbol{\Sigma}}$ ,  $\hat{\boldsymbol{\Sigma}}_{\mathcal{X}_i}$ , and  $\hat{\boldsymbol{\Sigma}}_{\mathcal{Y}_i}$  are, respectively, the sample covariance matrices of  $\mathcal{Z}$ ,  $\mathcal{X}_i = \{\mathbf{z}_1, \mathbf{z}_2, \dots, \mathbf{z}_i\}$ , and  $\mathcal{Y}_i = \{\mathbf{z}_{i+1}, \mathbf{z}_{i+2}, \dots, \mathbf{z}_n\}$ . If  $\max_{i_{min} < i \leq n - i_{min}} \Delta BIC_{\{\mathcal{X}_i, \mathcal{Y}_i\}}(i) > 0$ , the time index corresponding to the maximum value is output as the change point; otherwise, there is no change point in  $\mathcal{Z}$ . It is not necessary to compute the  $\Delta BIC$  value for time indices within the ranges 1 to  $i_{min}$  and  $n - i_{min} + 1$  to  $n$  because in these cases the number of samples in  $\mathcal{X}_i$  or  $\mathcal{Y}_i$  is insufficient to give a reliable estimate of the parameters. Empirically, it is appropriate to set  $i_{min}$  at a value within the range 30 to 50 for practical applications. According to the BIC theory, the penalty factor  $\lambda$  in Eq. (4) is 1; however, in practical segmentation tasks, it is usually adjusted to allow a tradeoff between error types.

2) *Multiple-change-point detection*: OCD-Chen outputs at most one change point, even though there are multiple change points in the analysis window. To detect multiple change points in an audio stream, as shown in Fig. 1, OCD-Chen can be applied sequentially to a sliding, size-growing analysis window whose initial size is  $N_{ini}$  samples. The window repeatedly grows by  $N_g$  samples until a change point is detected or its size exceeds a pre-defined upper bound  $N_{max}$ . Here, the upper bound ensures the search efficiency [15], [13]. If a change point is detected during the window growing step, the detection process restarts at that change point with an analysis window of  $N_{ini}$  samples. When the size of the window grows to  $N_{max}$ , it is repeatedly shifted by  $N_s$  samples until a change point is detected or the analysis window reaches the end of the audio stream. In this way, the change points in the audio stream can be detected sequentially.

### III. DIVIDE-AND-CONQUER-BASED SEGMENTATION

In this section, we present three implementations of the divide-and-conquer paradigm for detecting multiple change points in an analysis window. Note that the proposed approaches are based on the same assumption as that of WinGrow, i.e., the feature vectors of audio segments from

**Algorithm 1**  $CP \leftarrow \text{DACDec1}(W)$ 


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**Require:**  $W$ : the analysis window  
**Ensure:**  $CP$ : the set of change points detected in  $W$

Begin

- 1) detect whether there is a change point in  $W$  by OCD-Chen;
- 2) //Check termination  
 if (there is no change point in  $W$  or the size of  $W$  is smaller than  $N_{min}$ )  
 $CP \leftarrow \phi$ ; //empty set  
 goto End; //return
- 3) //Divide  
 let  $\hat{t}$  be the change point detected in 1);  
 divide  $W$  into two sub-windows,  $W_1$  and  $W_2$ , at  $\hat{t}$ ;
- 4) //Solve sub-instances  
 $CP_{W_1} \leftarrow \text{DACDec1}(W_1)$ ;  $CP_{W_2} \leftarrow \text{DACDec1}(W_2)$ ;
- 5) //Combine  
 $CP \leftarrow \hat{t} \cup CP_{W_1} \cup CP_{W_2}$ ;

End

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different speakers are derived from different Gaussian distributions.

### A. The DACDec1 approach

We use the example in Fig. 2 to explain the concept of divide-and-conquer-based segmentation. It is assumed that the audio stream in Fig. 2 (a) consists of three homogeneous segments derived from different speakers. Initially, OCD-Chen is applied in an analysis window that covers the entire audio stream. After the change point  $C_2$  has been detected with the  $\Delta BIC$  curve in Fig. 2 (b), the audio stream is divided into two analysis windows. Then, OCD-Chen is recursively applied in these two windows to search for the remaining change points so that  $C_1$  can be detected. This approach, called DACDec1, allows us to detect the change points by a divide-and-conquer (DAC) strategy. As described in Algorithm 1, DACDec1 terminates (returns) if no change point is detected by OCD-Chen in the analysis window or the size of the analysis window is smaller than a pre-defined value, denoted as  $N_{min}$  samples. In the *Divide* stage, the analysis window is partitioned into two sub-windows at the change point detected by OCD-Chen. Then, the sub-windows are input to DACDec1 in the *Solve sub-instances* stage. Finally, the *Combine* stage outputs all the change points detected in step 1) and step 4) (i.e., the *Solve sub-instances* stage).

1) *Discussion:* In general, when the data samples are derived from more than one Gaussian distribution, two Gaussians (the  $H_1$  hypothesis) fit the distribution of the data better than one Gaussian (the  $H_0$  hypothesis) if the samples belonging to the same Gaussian are used together to estimate the parameters. For example, Fig. 3 schematically illustrates a case where the three audio segments are derived from three different speakers and their feature vectors distribute as three Gaussian clusters. This case explains why the  $\Delta BIC$  values at  $C_1$  and  $C_2$  in Fig. 2 (b) are positive. From the above perspective, if the homogeneous segments in the analysis window of DACDec1 are always derived from different speakers during the recursive process, we can be confident that, at each change point, the  $H_1$  hypothesis will fit the data better than the  $H_0$  hypothesis; thus, the  $\Delta BIC$  value will be positive.

However, if two or more segments in the analysis window are derived from the same speaker, the performance of DACDec1 may decline dramatically. For example, in Fig. 4 (a), the first and third segments are derived from the same speaker (Speaker1), while the second segment is derived from another speaker (Speaker2). When applying OCD-Chen to the audio stream in Fig. 4 (a) with the same  $\lambda$  value of BIC used in the example in Fig. 2, we obtain the  $\Delta BIC$  curve in Fig. 4 (b). The curve still has two peaks at the change points  $C_1$  and  $C_2$  because the  $H_1$  hypothesis models the distribution of the data samples better at change points than it does at non-change points. We use Figs. 4 (c) and (d) to explain this perspective. Fig. 4 (c) diagrammatically illustrates the two hypotheses at  $C_2$ , where all the data samples of Speaker2 (the circles) are used with those of Speaker1 (the stars) to estimate one Gaussian in  $H_1$ . In contrast, at the non-change point  $R$  in Fig. 4 (b), as shown in Fig. 4 (d), the data samples of Speaker2 are divided into two parts, each of which is combined with the data samples of Speaker1 (one with the stars and the other with the diamonds) to estimate a distinct Gaussian in  $H_1$ . Clearly, the  $H_1$  hypothesis in Fig. 4 (c) fits the data better than that in Fig. 4 (d).

In this example, we have peaks at  $C_1$  and  $C_2$ . However, their  $\Delta BIC$  values are negative, and no change point will be output by OCD-Chen because, as illustrated in Fig. 4 (c),  $H_1$  over-fits the data samples of Speaker1 and obtains a smaller BIC value than that of  $H_0$ . We may adjust the value of  $\lambda$  so that, at  $C_2$ , the  $\Delta BIC$  value will be positive (i.e., the hypothesis test favors  $H_1$ ). However, this may result in false alarms when the recursive process continues to detect change points in a homogeneous segment. In other words, it is difficult to determine a reliable  $\lambda$  value for an audio stream like the example in Fig. 4 (a). Moreover, it is infeasible to adjust the value of  $\lambda$  for each specific audio stream in practical applications.

### B. The DACDec2 approach

To overcome the performance limitation caused by unreliable  $\Delta BIC$  measurements of the over-fitting cases in DACDec1, we developed an alternative implementation of the divide-and-conquer paradigm, called DACDec2. In this approach (Algorithm 2), the  $\Delta BIC$  value is not used to check the termination in the *Check termination* stage because it may be unreliable, as illustrated in Figs. 2 and 4. The recursive process terminates (returns) when the size of the analysis window is smaller than  $N_{min}$  samples. In the *Divide* stage, the analysis window is partitioned into two sub-windows at the time index  $\hat{t}$  that has the largest  $\Delta BIC$  value located by OCD-Chen. Then, the sub-windows are input to DACDec2 in the *Solve sub-instances* stage. In the *Combine* stage,  $\hat{t}$  is labeled as a change point if the  $\Delta BIC$  value at  $\hat{t}$  calculated in the *Divide* stage is positive; otherwise, it needs to be verified using its two neighboring segments  $\mathcal{X}$  and  $\mathcal{Y}$ . In the verification process,  $\hat{t}$  is only labeled as a change point if  $\Delta BIC_{\{\mathcal{X}, \mathcal{Y}\}}(\hat{t}) > 0$ .

Fig. 5 illustrates a recursive tree that simulates the recursive process of DACDec2 on the audio stream in Fig. 4 (a). We

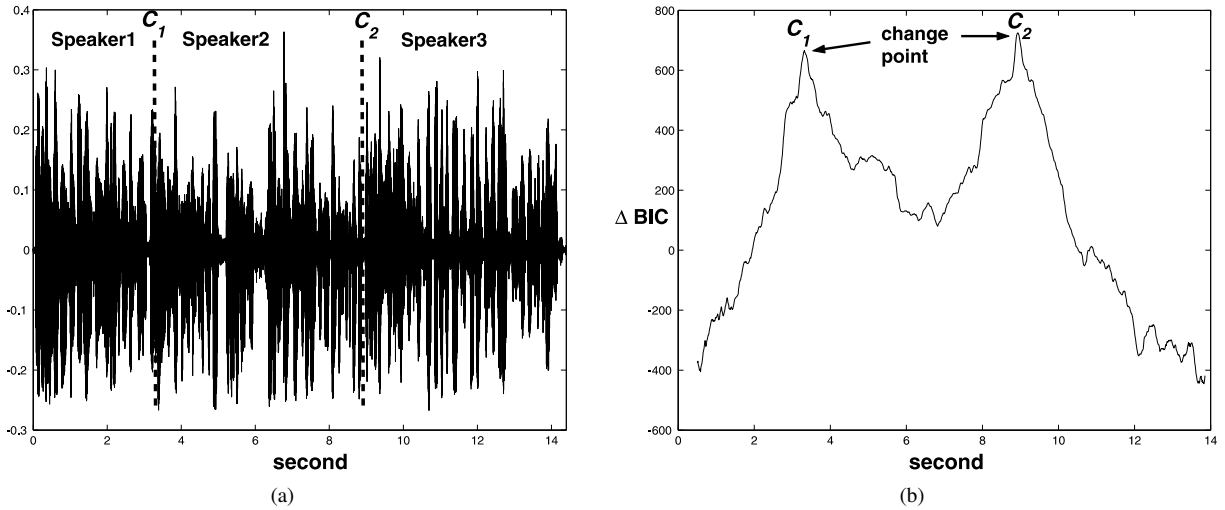


Fig. 2. (a) An audio stream comprised of three speech segments, each derived from a distinct speaker.  $C_1$  and  $C_2$  are the change points. (b) The  $\Delta BIC$  curve obtained by applying OCD-Chen to the audio stream in (a).

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**Algorithm 2**  $CP \leftarrow DACDec2(W)$ 


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**Require:**  $W$ : the analysis window

**Ensure:**  $CP$ : the set of change points detected in  $W$

Begin

- 1) //Check termination  
if (the size of  $W$  is smaller than  $N_{min}$ )  
     $CP \leftarrow \phi$ ; //empty set  
    goto End; //return
- 2) //Divide  
    apply OCD-Chen to  $W$  and let  $\hat{t}$  be the time index with the largest  $\Delta BIC$  value;  
    divide  $W$  into two sub-windows,  $W_1$  and  $W_2$ , at  $\hat{t}$ ;
- 3) //Solve sub-instances  
     $CP_{W_1} \leftarrow DACDec2(W_1)$ ;  $CP_{W_2} \leftarrow DACDec2(W_2)$ ;
- 4) //Combine  
    if ( $\Delta BIC_{\{W_1, W_2\}}(\hat{t})$  calculated in 2) is positive)  
         $CP \leftarrow \hat{t} \cup CP_{W_1} \cup CP_{W_2}$ ;  
    else  
        let  $\mathcal{X}$  be the segment on the left of  $\hat{t}$  in  $W_1$  and  $\mathcal{Y}$  be the segment on the right of  $\hat{t}$  in  $W_2$ ;  
        if ( $\Delta BIC_{\{\mathcal{X}, \mathcal{Y}\}}(\hat{t}) > 0$ ) //  $\hat{t}$  is a change point  
             $CP \leftarrow \hat{t} \cup CP_{W_1} \cup CP_{W_2}$ ;  
        else //  $\hat{t}$  is not a change point  
            merge  $\mathcal{X}$  and  $\mathcal{Y}$ ;  
             $CP \leftarrow CP_{W_1} \cup CP_{W_2}$ ;

End

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assume that there are no miss and false alarm errors in the detection process. In the figure, each tree node corresponds to a *divide-point* (i.e.,  $\hat{t}$ ) in the analysis window; the number inside the node indicates the order of the division, while the number below the node indicates the order in which the divide-point is verified in the *Combine* stage. In Fig. 4 (b), Node 1 ( $C_2$ ) has a negative  $\Delta BIC$  value in the *Divide* stage; however, it will be labeled as a change point by the verification process with segments  $\{c, d, e, f\}$  and  $\{g, h, i\}$  in the *Combine* stage. Node 2 ( $C_1$ ) has a positive  $\Delta BIC$  value in the *Divide* stage; thus, it is labeled as a change point and verification is not necessary. Segments  $\{a\}$  and  $\{b\}$  will be used for verifying Node 3; segments  $\{c, d\}$  and  $\{e, f\}$  will be used for verifying Node 4, and so on.

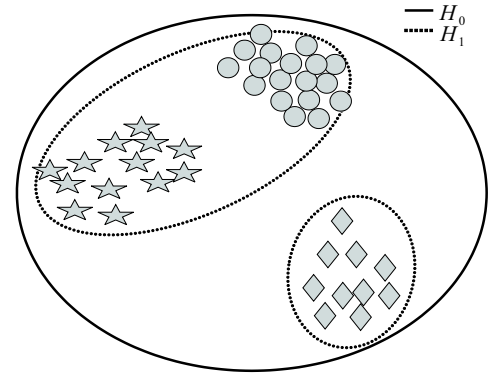


Fig. 3. An illustration that data samples distribute as three Gaussian clusters. For this case, generally, two Gaussians ( $H_1$ ) fit the distribution of the data better than one Gaussian ( $H_0$ ) if the samples belonging to the same Gaussian cluster are used together to estimate the parameters.

*1) Advantages of DACDec1 and DACDec2:* We use Fig. 6 to explain the potential advantages of using DACDec1 and DACDec2 for speaker change detection. In the figure, there are two change points,  $C_1$  and  $C_2$ . For WinGrow, if there is a false alarm error at  $F$  near  $C_1$ , the detection process restarts at  $F$ , but the false alarm error may lead to miss errors in the subsequent detection process. For example, if the three segments are derived from different speakers, like the case in Fig. 2 (a), it is very likely that  $C_2$  will be detected and  $C_1$  will be missed because the analysis window does not contain sufficient data from Seg1. On the other hand, if Seg1 and Seg3 are spoken by the same speaker and Seg2 is from another source,  $C_1$  may be missed for the same reason mentioned above. If  $C_1$  is missed, we may suffer from the unreliable  $\Delta BIC$  measurement issue as the example in Fig. 4 when OCD-Chen continues to detect  $C_2$ ; thus,  $C_2$  may also be missed.

In DACDec1, the *Divide* stage partitions the audio stream into two sub-streams at the point with the largest positive

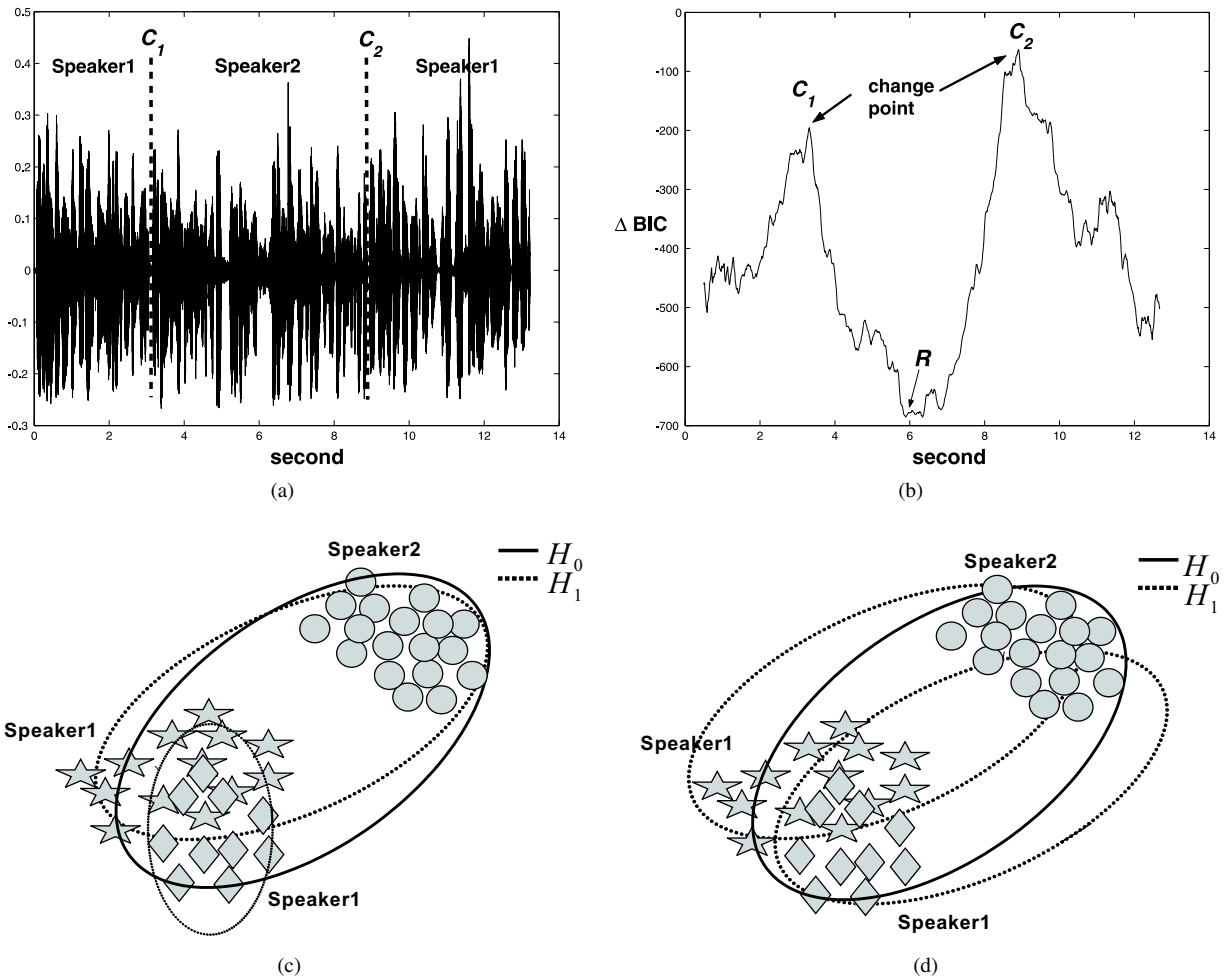


Fig. 4. (a) An audio stream comprised of three speech segments; the first and third segments are derived from the same speaker (Speaker1), while the second is derived from another speaker (Speaker2). (b) The  $\Delta BIC$  curve obtained by applying OCD-Chen to the audio stream in (a). (c) The diagram of the hypothesis test at the change point  $C_2$  in (b). (d) The diagram of the hypothesis test at the non-change point  $R$  in (b).

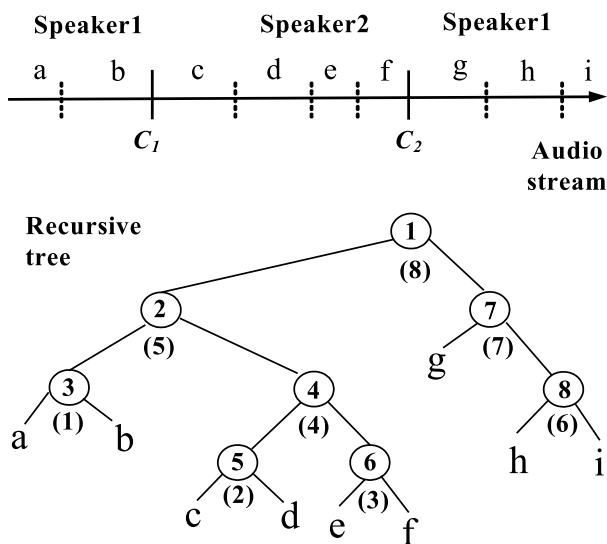


Fig. 5. A recursive tree that simulates the recursive process of DACDec2 on the audio stream in Fig. 4 (a).

$\Delta BIC$  value. As shown in Figs. 4 (c) and (d), change points usually have larger  $\Delta BIC$  values than non-change points; thus, false alarm errors may only occur after the true change points have been detected, and they will not lead to miss errors in the subsequent detection process. For example, in Fig. 6, the false alarm errors in Seg1 only occur after  $C_1$  has been detected, and so on.

In DACDec2, false alarm errors may not cause a true change point with a positive  $\Delta BIC$  value calculated in the *Divide* stage to be missed; however, the false alarm points' neighboring true change points with negative  $\Delta BIC$  values calculated in the *Divide* stage may be missed. For instance, for the example in Fig. 4, DACDec2 first divides the audio stream at  $C_2$  and generates the recursive tree shown in Fig. 5.  $C_2$  needs to be verified in the *Combine* stage because its  $\Delta BIC$  value calculated in the *Divide* stage is negative, as shown in Fig. 4 (b). However, if there is a false alarm point near  $C_2$ , it may be missed. We explain this phenomenon as follows. In Fig. 5, the boundary between segments  $\{e\}$  and  $\{f\}$  (i.e., Node 6) is verified before  $C_2$ . If it is detected as a change point,  $\{f\}$  and  $\{g, h, i\}$  are used to verify  $C_2$ . However, the number of data samples in segment  $\{f\}$  may be insufficient to



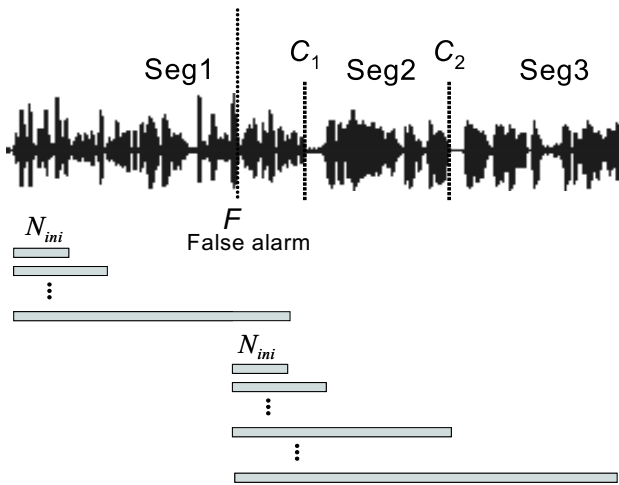


Fig. 6. An example of the WinGrow detection process. The audio stream contains two change points  $C_1$  and  $C_2$ , and the detection process generates a false alarm error at  $F$ .

obtain a reliable  $\Delta BIC$  measurement, thus  $C_2$  may be missed. On the other hand, if DACDec2 first divides the audio stream at  $C_1$  and outputs a false alarm point at  $F$  near  $C_1$ , like the case in Fig. 6,  $C_1$  may be missed for the same reason. Even so, missing  $C_1$  may not cause DACDec2 to miss  $C_2$  because, in the *Divide* stage,  $C_2$  will be determined whether it is a change point using complete, pure Seg2 and Seg3; therefore, it is very likely that the  $\Delta BIC$  value will be positive. In contrast, WinGrow may not be able to use complete, pure Seg2 and Seg3 for speaker change detection if  $C_1$  is missed.

### 2) Sequential segmentation by DACDec1 and DACDec2:

For a long audio stream, such as a one-hour broadcast news program, the segmentation task becomes computationally intractable when DACDec1 or DACDec2 are used to detect change points. Moreover, if the initial analysis window contains too many segments, it may be difficult for OCD-Chen to find an appropriate  $\lambda$  value to obtain robust  $\Delta BIC$  measurements for the various hypothesis tests in the recursive process. Therefore, in practical applications, we apply DACDec1 and DACDec2 in a large analysis window of fixed-size (e.g., 20 seconds) that moves from the beginning to the end of the audio stream to detect the speaker changes sequentially. The proposed sequential segmentation algorithms, SeqDACDec1 and SeqDACDec2, are shown in Fig. 7. In SeqDACDec1 (or SeqDACDec2), if a change point is detected in the fixed-size analysis window by DACDec1 (or DACDec2), the window is moved to the change point with the largest time index. Otherwise, it is moved forward by  $\eta L$  samples, where  $L$  denotes the window size, and  $\eta > 0$ . Note that a small  $\eta$  will allow a missed change point to be checked again by DACDec1 (or DACDec2) in the subsequent fixed-size analysis window. Like WinGrow, SeqDACDec1 and SeqDACDec2 are suitable for on-line applications.

### C. The DACDec3 approach

The third implementation (DACDec3) of the divide-and-conquer paradigm is detailed in Algorithm 3. In DACDec3,

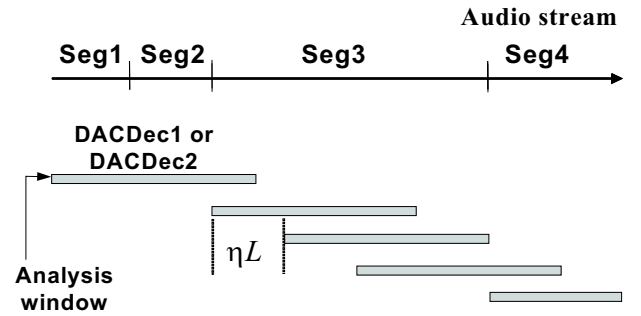


Fig. 7. Diagram of the detection process of SeqDACDec1 and SeqDACDec2. If a change point is detected in the fixed-size analysis window by DACDec1 or DACDec2, the window is moved to the change point with the largest time index. Otherwise, it is moved forward by  $\eta L$  samples, where  $L$  denotes the window size, and  $\eta > 0$ .

we use FixSlid instead of OCD-Chen to detect the divide-points of an input audio stream. As shown in Fig. 8 (a), given the distance curve obtained by FixSlid using the GLR [9] distance measure, the time index  $t$  associated with the peak that has the largest GLR value within the interval  $[t - pRange, t + pRange]$  is considered a divide-point. In this example, all the peaks except  $S$  are divide-points. Let  $DP_{set}$  be the set of divide-points obtained by FixSlid. As described in Algorithm 3, DACDec3 returns if a divide-point is not found in  $DP_{set}$ . In the *Divide* stage, the analysis window is partitioned at the time index of the divide-point with the largest GLR value. Then, in the *Combine* stage, each divide-point is evaluated to determine whether it is a change point based on the  $\Delta BIC$  measurement of its two neighboring segments  $\mathcal{X}$  and  $\mathcal{Y}$ .

The major difference between DACDec2 and DACDec3 is as follows. DACDec2 detects change points by OCD-Chen in the *Divide* stage. Then, only the divide-points with negative  $\Delta BIC$  values calculated in the *Divide* stage are verified by segment merging based on the  $\Delta BIC$  values of their neighboring segments in the *Combine* stage. In contrast, DACDec3 detects change points by verifying all the input divide-points indicated by FixSlid using segment merging. For example, if we apply FixSlid to the audio stream in Fig. 5 and obtain the distance curve in Fig. 8 (a), the recursive tree for DACDec3 will be the same as that in Fig. 5. In this case, DACDec2 finds the change point  $C_1$  using OCD-Chen in the *Divide* stage, while DACDec3 finds it in the *Combine* stage using segment merging; however, both DACDec2 and DACDec3 find the change point  $C_2$  in the *Combine* stage.

There is a close link between DISTBIC [9] and DACDec3. In DISTBIC, a distance curve is first generated by FixSlid, and then the “significant” local maximums on the distance curve are evaluated to determine whether they are change points by a sequential, left-to-right (in time order) segment merging process. As shown in Fig. 9, a local maximum is significant if  $|d(\max) - d(\min)| > \alpha\sigma$  and  $|d(\max) - d(\min)| > \alpha\sigma$ , where  $\sigma$  is the standard deviation of the distance values on the distance curve,  $\alpha$  is a positive real number, and  $\min$  and  $\max$  are, respectively, the locations associated with the right minimum and left minimum around the local maximum.

**Algorithm 3**  $CP \leftarrow \text{DACDec3}(W, DP_{set}, GLR_{set})$ **Require:**  $W$ : the analysis window $DP_{set} = \{DP_1, \dots, DP_N\}$ : the divide-points in  $W$  obtained by FixSlid using the GLR distance measure $GLR_{set} = \{GLR_1, \dots, GLR_N\}$ :  $GLR_i$  denotes the GLR value at  $DP_i$  for  $i = 1, 2, \dots, N$ **Ensure:**  $CP$ : the set of change points detected in  $W$ 

Begin

- 1) //Check termination  
if ( $DP_{set}$  is empty)  
     $CP \leftarrow \phi$ ; //empty set  
    goto End; //return
- 2) //Divide  
search in  $DP_{set}$  and let  $DP_k$  be the divide-point whose GLR value is the largest in  $GLR_{set}$ ;  
let  $\hat{t}$  be the time index of  $DP_k$ ; divide  $W$  into two sub-windows,  $W_1$  and  $W_2$ , at  $\hat{t}$ ;  
divide  $DP_{set}$  into two sub-sets,  $DP_{set1} = \{DP_1, \dots, DP_{k-1}\}$  and  $DP_{set2} = \{DP_{k+1}, \dots, DP_N\}$ ;  
divide  $GLR_{set}$  into two sub-sets,  $GLR_{set1} = \{GLR_1, \dots, GLR_{k-1}\}$  and  $GLR_{set2} = \{GLR_{k+1}, \dots, GLR_N\}$ ;
- 3) //Solve sub-instances  
 $CP_{W_1} \leftarrow \text{DACDec3}(W_1, DP_{set1}, GLR_{set1})$ ;  $CP_{W_2} \leftarrow \text{DACDec3}(W_2, DP_{set2}, GLR_{set2})$ ;
- 4) //Combine  
let  $\mathcal{X}$  be the segment on the left of  $\hat{t}$  in  $W_1$  and  $\mathcal{Y}$  be the segment on the right of  $\hat{t}$  in  $W_2$ ;  
if ( $\Delta BIC_{\{\mathcal{X}, \mathcal{Y}\}}(\hat{t}) > 0$ ) //  $\hat{t}$  is a change point  
     $CP \leftarrow \hat{t} \cup CP_{W_1} \cup CP_{W_2}$ ;  
else //  $\hat{t}$  is not a change point  
    merge  $\mathcal{X}$  and  $\mathcal{Y}$ ;  
     $CP \leftarrow CP_{W_1} \cup CP_{W_2}$ ;

End

If DISTBIC takes the divide-points of DACDec3 as change point candidates to be verified (we denote this approach as DISTBIC\_pR), it is identical to applying DACDec3 in that the recursive division is performed in a right-to-left manner, whereas the recursive segment merging is performed in a left-to-right manner. As shown in Fig. 8 (b), Node 8 is verified by segments {a} and {b} first, then Node 7 is verified by segments {a, b} and {c}, and so on.

DACDec3 should be more effective than DISTBIC\_pR because it evaluates the divide-points with smaller GLR values to determine whether they are change points before those with larger GLR values. In contrast, in DISTBIC\_pR, the divide-points are simply verified sequentially without considering the GLR information. The advantage of DACDec3 can be seen by comparing the recursive tree of DACDec3 in Fig. 5 to that of DISTBIC\_pR in Fig. 8 (b). In DACDec3,  $C_1$  may be verified with segments {a, b} and {c, d, e, f}, which are complete homogeneous segments of Speaker1 and Speaker2, respectively; whereas, in DISTBIC\_pR,  $C_1$  can only be verified with segments {a, b} and {c} or segments {b} and {c}, where only a small portion of Speaker2's data is used.

In addition to the recursive (sequential) segment merging process of DACDec3 (DISTBIC\_pR), one can use the hierarchical agglomerative clustering (HAC) to merge the segments obtained with DACDec3's divide-points [7], [8], [30]. We denote this segmentation approach as FixSlidHAC\_pR. Compared to DACDec3 (or DISTBIC\_pR), which performs segment merging locally, FixSlidHAC\_pR performs segment clustering globally. When performing HAC, each segment is considered as a cluster initially; then, in each merging step, the two clusters with the smallest distance are merged into a new cluster. The globality feature of FixSlidHAC\_pR is particularly beneficial to the speaker diarization task because the segment merging process groups the segments into clusters such that each cluster contains segments of the same speaker. However, this feature might not be as beneficial to the speaker segmen-

tation task because the goal is to merge adjacent segments into longer segments. For example, in Fig. 5, the goal of the segment merging process in the speaker segmentation task is to merge segments {a} and {b} into one larger segment and to merge segments {g}, {h} and {i} into another larger segment, rather than to merge these five segments into one cluster. In FixSlidHAC\_pR, if segment {h} is incorrectly merged with a segment of a different speaker, say {d}, the error will propagate in the following clustering process. DACDec3 might not suffer the same fate because its locality constraint enforces that segment {h} is first checked with its neighboring segment, {g} or {i}. Therefore, we think DACDec3's segment merging process meets the goal of speaker segmentation better than that of FixSlidHAC\_pR. Moreover, it is clear that the computational cost of FixSlidHAC\_pR is much larger than that of DACDec3 due to the essential computational cost of the HAC-based global clustering process.

Like DACDec1 and DACDec2, DACDec3 can also be applied sequentially in a fixed-size analysis window for on-line applications.

## IV. COMPUTATIONAL COST ANALYSIS

WinGrow, DACDec1, and DACDec2 detect acoustic changes by applying the OCD-Chen process to the analysis window. From Eq. (4), it is clear that the computational cost of  $\Delta BIC$  is mainly from the cost of calculating covariance matrices, which is proportional to the number of data samples. Let the time cost of calculating  $\Delta BIC$  with  $m$  samples be  $m\tau$ , where  $\tau$  represents the time unit; then,  $m^2\tau$  denotes the time cost of applying OCD-Chen to an analysis window of  $m$  samples<sup>1</sup>.

<sup>1</sup>As mentioned in Section II-B1, the  $\Delta BIC$  value is not computed for samples at the beginning and the end of the analysis window. However, to simplify the analysis, we assume that the  $\Delta BIC$  value is computed for each sample of the window.



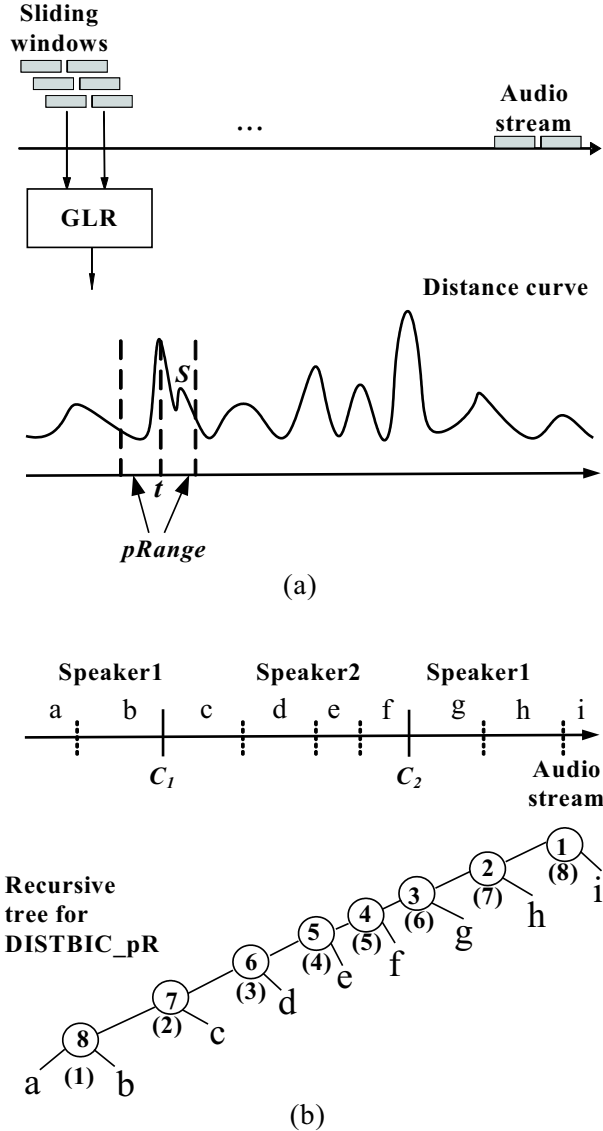


Fig. 8. (a) The distance curve obtained by FixSlid using the GLR distance measure, where the time index  $t$  associated with the peak that has the largest GLR value within the interval  $[t - pRange, t + pRange]$  is considered a divide-point in DACDec3. On this curve, all the peaks, except  $S$ , are divide-points. (b) The recursive tree representation of DISTBIC\_pR based on the divide-points in (a) for the audio stream in Fig. 5.

To simplify the analysis, we assume that each homogeneous segment in the input audio stream (i.e., the initial analysis window for DACDec1, DACDec2, and DACDec3) contains  $m$  samples. Moreover, we assume the detection process is perfect, i.e., miss and false alarm errors never occur.

1) For DACDec1: Let  $T_1(k)$  denote the time cost of applying DACDec1 to an audio stream of  $k$  change points (i.e.,  $k + 1$  homogeneous segments). When the audio stream is divided at the  $i$ -th change point, as shown in Fig. 10, we obtain the following recursive expression of  $T_1(k)$ :

$$T_1(k) = T_1(i-1) + T_1(k-i) + (k+1)^2 m^2 \tau, \quad (5)$$

where  $(k+1)^2 m^2 \tau$  is the time cost of finding the divide-point by OCD-Chen;  $T_1(i-1)$  and  $T_1(k-i)$  are the time

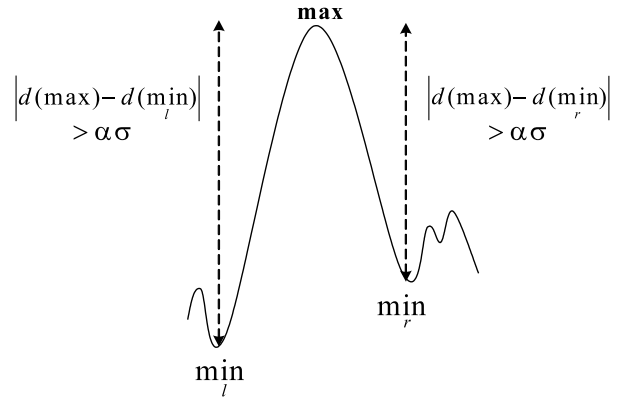


Fig. 9. A significant local maximum on the distance curve.

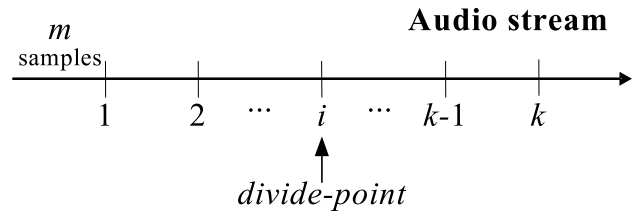


Fig. 10. An audio stream comprised of  $k + 1$  homogeneous segments, each containing  $m$  samples. The stream is divided at the  $i$ -th change point.

costs of applying DACDec1 in the left sub-stream and the right sub-stream, respectively. We have  $T_1(0) = m^2 \tau$ , since it represents the time cost of applying OCD-Chen to a  $m$ -sample homogeneous segment.

We assume that the division occurs at each change point with equal probability; therefore, the average time cost of DACDec1 is

$$T_1(k) = \frac{1}{k} \sum_{i=1}^k (T_1(i-1) + T_1(k-i)) + (k+1)^2 m^2 \tau. \quad (6)$$

After the algebraic manipulation detailed in Appendix A, we obtain

$$\begin{aligned} T_1(k) &\approx (3(k+1)^2 - 2(k+1) \ln(k+1)) m^2 \tau \\ &= O(k^2 m^2 \tau). \end{aligned} \quad (7)$$

2) For DACDec2: Compared to DACDec1, DACDec2 incurs an additional time cost in the *Combine* stage as it has to determine whether the divide-point with a negative  $\Delta BIC$  value calculated in the *Divide* stage is a change point. The cost is  $2m\tau$  because each of the divide-point's two neighboring segments contains  $m$  samples. To simplify the analysis, we assume that each divide-point must be verified, even though its  $\Delta BIC$  value calculated in the *Divide* stage is positive. Hence, the average time cost of DACDec2 is

$$T_2(k) = \frac{1}{k} \sum_{i=1}^k (T_2(i-1) + T_2(k-i)) + (k+1)^2 m^2 \tau + 2m\tau. \quad (8)$$

Unlike DACDec1, DACDec2 recursively partitions each homogeneous segment of  $m$  samples until the analysis window is smaller than the pre-defined minimum value  $N_{min}$ . Therefore,  $T_2(0)$  is equivalent to the time cost of applying DACDec2 to an  $m$ -sample stream in which each sample can be a divide-point. The cost of finding a divide-point in an  $m$ -sample stream in the *Divide* stage is  $m^2\tau$ . In the *Combine* stage, the cost of verifying the divide-point is at most  $m\tau$  because the two segments used for verification are sub-segments of the  $m$ -sample segment. Therefore, the upper bound of  $T_2(0)$  is

$$T'(m) = \frac{1}{m} \sum_{i=1}^m (T'(i-1) + T'(m-i)) + m^2\tau + m\tau, \quad (9)$$

where  $T'(0) = 0$ . After the algebraic manipulation detailed in Appendix B, we obtain

$$T_2(0) \leq T'(m) \approx (3m + 4 - 4\ln(m+1))(m+1)\tau. \quad (10)$$

Then, we can solve the recursive equation in Eq. (8) with  $T_2(0)$  in Eq. (10). After the algebraic manipulation detailed in Appendix C, we obtain

$$\begin{aligned} T_2(k) &\leq (3k + 5 - 2\ln(k+1))(k+1)m^2\tau \\ &\quad + (9 + 2\ln k - 2\ln(k+1) - 4\ln(m+1))(k+1)m\tau \\ &\quad + (4 - 4\ln(m+1))(k+1)\tau \\ &= O(k^2m^2\tau). \end{aligned} \quad (11)$$

3) *For FixSlid, DACDec3, and DISTBIC\_pR*: Suppose FixSlid uses GLR ( $\Delta BIC$ ) as the distance measure and the analysis window consists of  $\omega$  samples. Then, the time cost of FixSlid is

$$\begin{aligned} T_3(k) &= (2\omega\tau)(k+1)m \\ &= O(km\tau). \end{aligned} \quad (12)$$

DACDec3 and DISTBIC\_pR incur a higher time cost than FixSlid when verifying divide-points in the segment merging process. Suppose the audio stream is equally divided into  $\frac{(k+1)m}{\beta}$  sub-segments of  $\beta$  samples, where  $\beta > 0$ . Since we assume that the segmentation derived by DACDec3 and DISTBIC\_pR is perfect, each of the change points is also a divide-point and the time cost of segment merging verification is less than  $2m\tau$  for each divide-point. Therefore, the time cost of DACDec3 and DISTBIC\_pR is less than

$$\begin{aligned} T_4(k) &= (2\omega\tau)(k+1)m + \left(\frac{(k+1)m}{\beta} - 1\right)2m\tau \\ &= O(km^2\tau). \end{aligned} \quad (13)$$

4) *For WinGrow*: We analyze the case where the maximum window size  $N_{max}$  is large enough to ensure that the search process always restarts at a true change point<sup>2</sup>. In this case, the

analysis window  $W$  initialized with a small number of  $N_{ini}$  samples grows repeatedly by  $N_g$  samples until it contains more than  $m$  samples, so that there is at least one change point in  $W$ . Suppose  $W$  needs to grow to  $\gamma m$  samples to detect the change point, where  $\gamma > 0$ ; then, the time cost of sequentially detecting  $k$  change points will be

$$T'_1(k) = k[N_{ini}^2 + \sum_{i=1}^{(\gamma m - N_{ini})/N_g} (N_{ini} + iN_g)^2]\tau. \quad (14)$$

After the  $k$ -th change point has been detected, the detection process continues to search in the last homogeneous segment; the time cost is

$$C_s = [N_{ini}^2 + \sum_{i=1}^{(m - N_{ini})/N_g} (N_{ini} + iN_g)^2]\tau. \quad (15)$$

In practical applications, both  $N_{ini}$  and  $N_g$  are set at small values. To simplify the analysis, we assume  $N_{ini} \approx N_g$ . Then, the time cost of WinGrow is

$$\begin{aligned} T_5(k) &= T'_1(k) + C_s \\ &\approx k \left[ \sum_{i=1}^{(\gamma m - N_g)/N_g} (iN_g)^2 \right] \tau + \left[ \sum_{i=1}^{(m - N_g)/N_g} (iN_g)^2 \right] \tau \\ &= \left( \frac{\gamma^3 m^3}{3N_g} - \frac{\gamma^2 m^2}{2} + \frac{\gamma m N_g}{6} \right) k\tau \\ &\quad + \left( \frac{m^3}{3N_g} - \frac{m^2}{2} + \frac{m N_g}{6} \right) \tau \\ &= O(km^3\tau). \end{aligned} \quad (16)$$

5) *Discussion*: From Eqs. (7), (11), (12), (13), and (16), it is obvious that FixSlid, DACDec3, and DISTBIC\_pR are more efficient than DACDec1, DACDec2, and WinGrow.

DACDec1 and DACDec2 are more efficient than WinGrow when the input audio stream is composed of long homogeneous segments. For example, if the frame rate is 100 frames per second (i.e., there are 100 feature vectors for a one-second audio stream), it is appropriate to set the value of  $N_{ini}$  and  $N_g$  at 100. Moreover, the value of  $\gamma$  can be set at 1.5 generally. Then, for a 30-second audio stream (which consists of 3000 feature vectors) containing only one change point (i.e.,  $k = 1$  and  $m = 1500$ ), the speedups of DACDec1 and DACDec2 over WinGrow are 2.55 and 1.78, respectively. When there is no change point in the 30-second stream, the speedups of DACDec1 and DACDec2 over WinGrow are 10.51 and 3.51, respectively. In contrast, when the audio stream is composed of short homogeneous segments, WinGrow is more efficient than DACDec1 and DACDec2. For example, for a 30-second stream containing five change points (i.e.,  $k = 5$  and  $m = 500$ ), the speedups of DACDec1 and DACDec2 over WinGrow are 0.42 and 0.37, respectively.

## V. EXPERIMENTS ON SPEAKER SEGMENTATION

We conducted experiments on a synthetic data set using SeqDACDec1 and SeqDACDec2 to verify the unreliable

<sup>2</sup>Without this assumption, the time cost analysis for WinGrow might be intractable. However, this assumption is appropriate for many kinds of real-world data. For example, in our experiments on the broadcast news data described in Sec. V, it is appropriate to set  $N_{max}$  at 20 seconds, which is longer than most of the homogeneous segments in the data set.

$\Delta BIC$  measurement issue in DACDec1, and on two real-world broadcast news data sets to evaluate the performances of the baseline and proposed segmentation approaches.

For feature extraction, we used a 32-ms Hamming window shifted with a step of 10-ms to extract 24 mel-frequency cepstral coefficients as the acoustic features [11]. There were 100 24-dimensional feature vectors in a one-second audio stream.

For the performance evaluation, we used the Receiver Operating Characteristic (ROC) curve to show the various miss detection (MD) rates and false alarm (FA) rates yielded by adjusting the threshold parameters. A true change point  $t$  was counted as a miss detection if there was no hypothesized change point within  $[t-\xi, t+\xi]$  (a  $2\xi$ -second window centered on  $t$ ); and a hypothesized change point  $\hat{t}$  was counted as a false alarm if there was no true change point within  $[\hat{t}-\xi, \hat{t}+\xi]$ . The miss detection rate (MDR) and false alarm rate (FAR) are defined as

$$\text{MDR} = 100\% \times \frac{\text{number of MD}}{\text{number of true change points}},$$

$$\text{FAR} = 100\% \times \frac{\text{number of FA}}{\text{number of hypothesized change points}}.$$

#### A. Experiments on the synthetic data

1) *Data set description*: We used the training data of six speakers from the 2001 NIST speaker recognition evaluation corpus [34] to create three artificial audio streams of conversational speech as the synthetic data set. The speech from speaker#5077 and speaker#5232 was divided into three-second utterances and interlaced to form an audio stream of conversational speech of two speakers. In the same way, the speech from speaker#5326 and speaker#5333 was used to form the second audio stream; and the speech from speakers#5446 and speaker#5269 was used to form the third audio stream. There were 231 speaker change points in total in the three audio streams.

2) *Experiment results*: Fig. 11 shows the ROC curves obtained by running SeqDACDec1 and SeqDACDec2 on the synthetic data with different analysis window sizes.  $\eta$  was set at 0.25,  $N_{min}$  in DACDec1 and DACDec2 was set at one second (i.e., 100 samples), and the penalty factor  $\lambda$  in  $\Delta BIC$  was set at 0.7 initially and increased to 1.7 in 0.05 increments. The  $\Delta BIC$  distance was evaluated every 0.1 seconds in both approaches; that is, the resolution for change point detection was 0.1 seconds. The tolerance  $\xi$  for counting the number of miss detection or false alarm was set at 0.5 seconds. From the figure, we observe that SeqDACDec2 outperforms SeqDACDec1 for every window size. Moreover, SeqDACDec2 yields similar performances at different window sizes, whereas the performance of SeqDACDec1 declines significantly when the window size is increased from 10 seconds to 20 or 30 seconds. In other words, SeqDACDec2 is more robust to the size of the analysis window than SeqDACDec1. The experiment results conform to the discussion in Sec. III; that is, DACDec1 might not work as well as DACDec2 if the condition that the homogeneous segments in the analysis

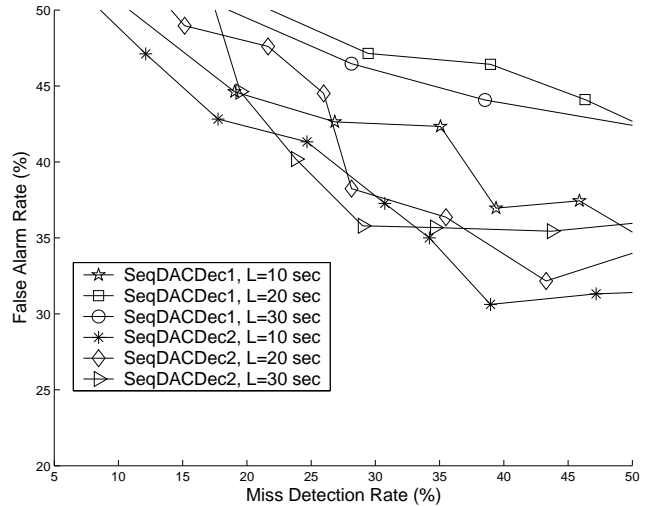


Fig. 11. ROC curves obtained by running SeqDACDec1 and SeqDACDec2 on the synthetic data using 10-second, 20-second, and 30-second analysis windows.  $L$  denotes the size of the analysis window.

window are derived from different acoustic sources is not met.

#### B. Experiments on broadcast news data

1) *Data set description*: We evaluated FixSlid, FixSlid-HAC\_pR, DISTBIC\_pR, DISTBIC, WinGrow, and the proposed methods on two broadcast news data sets. The broadcast news data in the 2003 NIST rich transcription evaluation data [32], which is comprised of six 30-minute audio streams recorded from channels ABC, NBC, CNN, PRI, VOA, and MNB, was used as the evaluation set (denoted as RT03). Three one-hour broadcast news programs (PTSND-20011203, PTSND-20011204, and PTSND-20011205) selected from the MATBN corpus [31] were used as the development set (denoted as MATBN3hr). To be consistent with RT03, each file in MATBN3hr was divided into two 30-minute audio streams in the experiments. According to the manual transcriptions, there were 1261 and 444 speaker change points in MATBN3hr and RT03, respectively. Note that, in the evaluation, we ignored the hypothesized change points that locate in the non-speech regions labeled in the transcription when evaluating the segmentation errors because the detection of acoustic changes within the non-speech regions was outside the scope of this study.

Fig. 12 shows the empirical cumulative distributions of the size of homogeneous segments in the two data sets. As shown in the figure, the average length of the segments in RT03 is longer than that in MATBN3hr.

2) *Parameter setting and system description*: For FixSlid, we used the GLR distance as the distance measure of two adjacent windows. In the experiments, the window size was fixed at two seconds; and the value of  $\alpha$  used to evaluate the “significant” local maximum, as shown in Fig. 9, was set at 0.4 initially, and increased to 2 in 0.05 increments to obtain the ROC curve. For DACDec3, DISTBIC\_pR, and FixSlidHAC\_pR, the parameter  $pRange$  was tuned with the

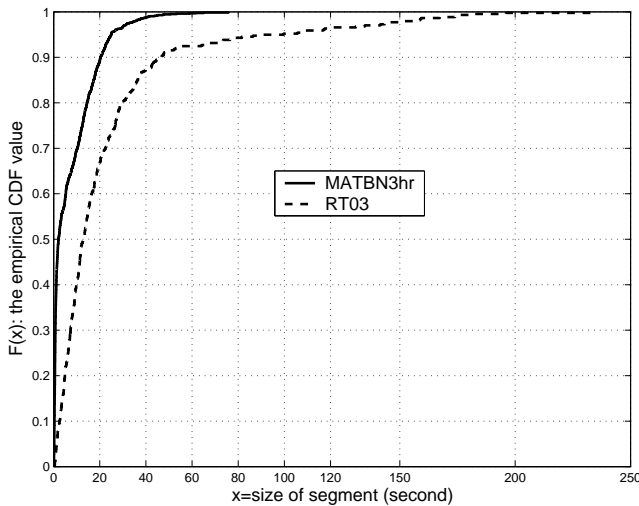


Fig. 12. The empirical cumulative distributions of the size of homogeneous segments in MATBN3hr and RT03.

development set. For WinGrow, the values of  $N_g$  and  $N_s$  were set at one second and  $N_{max}/4$  seconds, respectively; and the values of  $N_{ini}$  and  $N_{max}$  were tuned with the development set. For SeqDACDec1 and SeqDACDec2,  $\eta$  was fixed at 0.25; and  $L$  and  $N_{min}$  in DACDec1 and DACDec2 were tuned with the development set. For each BIC-based segmentation approach, various  $\lambda$  values for  $\Delta BIC$  were applied in order to obtain the ROC curve. Like the above experiments on the synthetic data, the resolution for change point detection was 0.1 seconds for all the approaches. However, the tolerance  $\xi$  for counting the number of miss detection or false alarm was set at one second rather than 0.5 seconds. Basically, we made this change because of the limited precision of human reference annotation.

For FixSlidHAC\_pR, we first applied FixSlid with the threshold parameter  $pRange$  to segment the input audio stream, then we pruned non-speech regions within the audio segments and grouped the segments using HAC with multiple stages, which have been applied in state-of-the-art speaker diarization systems [8], [7], [35], [30]. As shown in Fig. 13, we applied HAC with  $\Delta BIC$  as the inter-cluster distance measure (HAC-BIC) for initial clustering; the clustering process was stopped if the smallest  $\Delta BIC$  value among all the cluster pairs was larger than zero. Then, we classified the resultant clusters into four classes, namely, male speech with studio/wide-bandwidth condition ( $WM$ ), male speech with telephone/narrow-bandwidth condition ( $TM$ ), female speech with studio condition ( $WF$ ), and female speech with telephone condition ( $TF$ ). After the gender/bandwidth classification, we applied HAC with the cross log-likelihood ratio derived from GMMs as the inter-cluster distance measure (HAC-SID) to the four classes, individually [7]. The cross log-likelihood ratio is defined as

$$CLR_{GMM}(\pi_i, \pi_j) = \frac{1}{n_i} \log \frac{p(\pi_i|M_j)}{p(\pi_i|B)} + \frac{1}{n_j} \log \frac{p(\pi_j|M_i)}{p(\pi_j|B)}, \quad (17)$$

where  $M_i$  and  $M_j$  are, respectively, the GMMs for clus-

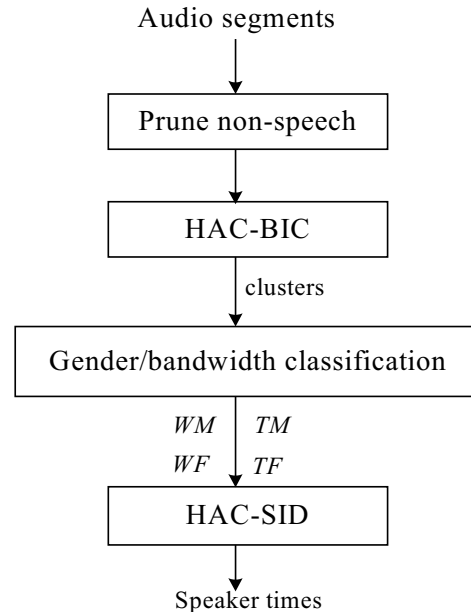


Fig. 13. A multi-stage HAC that consists of BIC clustering (HAC-BIC), gender/bandwidth classification and SID clustering (HAC-SID).

ters  $\pi_i$  and  $\pi_j$ , which are MAP-adapted from the universal background model (UBM [36])  $B$ . Here, only Gaussian mean vectors were adapted, and the relevant factor for controlling the adaptation rate was experimentally set at 16.  $CLR_{GMM}$  reveals the similarity between  $\pi_i$  and  $\pi_j$ . Therefore, when applying this measure in HAC, the two clusters with the largest  $CLR_{GMM}$  value are merged; and the clustering process is terminated when it is smaller than a pre-defined stopping threshold. We used 15 MFCCs and energy plus their delta coefficients, which were normalized by feature warping, as the speech feature for HAC-SID [7]. We used the 1998 DARPA/NIST HUB-4 broadcast news evaluation test data to train the UBMs for  $WM$  and  $WF$ , and the NIST 2000 speaker recognition evaluation corpus for  $TM$  and  $TF$ ; each of the UBMs contained 128 mixture Gaussians.

3) *Experiment results*: We first evaluated all the segmentation approaches on MATBN3hr. Fig. 14 (a) shows the ROC curves obtained by DACDec3 and DISTBIC\_pR with different  $pRange$  values. From the figure, we observe that DACDec3 outperforms DISTBIC\_pR; and the best setting of  $pRange$  for DACDec3 and DISTBIC\_pR are 0.5 seconds and one second, respectively. Table I shows the results of FixSlidHAC\_pR, where for each  $pRange$  case, various settings for  $\lambda$  and the stopping threshold in HAC-SID were evaluated to obtain the lowest equal error rate (EER). From the table, we observe that FixSlidHAC\_pR achieves the lowest EER with  $pRange = 1.5$  seconds. Both DACDec3 and DISTBIC\_pR achieve a lower EER compared to FixSlidHAC\_pR; this shows that DACDec3's recursive and DISTBIC\_pR's sequential strategies for segment merging outperform the hierarchical agglomerative approach.

We also evaluated DACDec3 using the “significant” local maximums obtained by FixSlid as the divide-points (denoted

TABLE I

THE EERS OF FIXSLIDHAC\_pR, DACDEC3, AND DISTBIC\_pR ON MATBN3HR, WHERE M AND F DENOTE THE MISS DETECTION RATE AND THE FALSE ALARM RATE, RESPECTIVELY.

Approach	$pRange$ (in second)	EER (in %)
FixSlidHAC_pR	1	M:26.05, F:24.60
	1.5	M:21.09, F:22.22
	2	M:24.35, F:25.10
DACDec3	0.5	M:17.61, F:17.46
DISTBIC_pR	1	M:19.19, F:18.44

as DACDec3\_SP). We ran DACDec3\_SP and DISTBIC with  $\alpha = 0.4$  and  $\alpha = 0.85$ . From Fig. 14 (b), it is clear that DACDec3\_SP and DISTBIC substantially outperform FixSlid, while DACDec3\_SP outperforms DISTBIC. Moreover, DACDec3 with  $pRange = 0.5$  seconds (the line marked with diamonds) slightly outperforms DACDec3\_SP. In our experience,  $pRange$  is easier to tune than  $\alpha$ . Therefore, we did not analyze DACDec3\_SP and DISTBIC further in the remaining experiments for speaker change detection.

When conducting the experiments, we found that it was appropriate to set  $N_{ini}$  at three seconds and  $N_{max}$  at 20 seconds for WinGrow. For both SeqDACDec1 and SeqDACDec2, it was appropriate to set  $N_{min}$  at two seconds and the window size  $L$  at 20 seconds. Fig. 15 (a) shows the ROC curves obtained by SeqDACDec1 with analysis windows of different size. Unlike the results for the synthetic data in Fig. 11, the results with 10-second and 20-second analysis windows are similar. This is because, in the broadcast news data, if a 10-second or 20-second analysis window contains multiple homogeneous segments, the segments are usually derived from different speakers. For SeqDACDec2, the results for 10-second, 20-second, and 30-second analysis windows are similar, as shown in Fig. 15 (b). The ROC curves obtained by the different approaches are shown in Fig. 15 (c). We observe that the proposed approaches, namely, SeqDACDec1, SeqDACDec2, and DACDec3, outperform the other approaches, while SeqDACDec2 performs the best. Table II shows the speeds of all the approaches in terms of “times real-time” (real-time factor,  $xRT^3$ ) in the EER case. All the programs were implemented with MATLAB, except that the MAP training of GMMs and calculation of mixture likelihood in FixSlidHAC\_pR was implemented with C language via MATLAB’s API. The programs were run on a machine with a 3.2GHz Intel Xeon CPU. From the table, we observe that SeqDACDec1, SeqDACDec2, and DACDec3 are more efficient than WinGrow. DACDec3 in particular runs much faster than WinGrow. Moreover, FixSlidHAC\_pR is much slower than the other approaches.

Next, we conducted experiments on RT03 with the parameters tuned with MATBN3hr. Fig. 16 shows the ROC curves for all approaches. Again, we observe that the proposed approaches, namely, SeqDACDec1, SeqDACDec2, and DACDec3, outperform the other approaches. Table III shows the real-time factor of all the approaches in the EER case. Comparing Table III to Table II, it is clear that every approach

achieves a higher speedup over WinGrow on RT03 than on MATBN3hr. This is because the homogeneous segments in RT03 are longer than those in MATBN3hr on average, as shown in Fig. 12, and these approaches achieve higher speedup over WinGrow for an audio stream comprised of longer homogeneous segments, as mentioned in Sec. IV (cf. Eqs. (7), (11), (12), (13), and (16)).

## VI. APPLICATION TO SPEAKER DIARIZATION

Speaker diarization, also known as the “who spoke when” task, aims to group together speech segments produced by the same speaker within an audio stream [8]. It has been studied in various data domains, e.g., conversational telephone speech [16], broadcast news data [7], [35], and meeting data [37].

Speaker diarization systems usually consist of two core components, namely speaker segmentation, which chops the audio stream into homogeneous segments, and speaker clustering, which groups the homogeneous segments into speaker clusters. Currently, leading speaker diarization systems usually apply hierarchical agglomerative clustering (HAC) to perform speaker clustering after segmentation [7], [35], [30]. Here, we would like to evaluate the performance of the segmentation approaches discussed above in terms of speaker diarization error by integrating them with the multi-stage HAC in Fig. 13. The diarization system that combines SeqDACDec1 and the multi-stage HAC is denoted as SeqDACDec1\_HAC. Similarly, the diarization systems based on the segmentation methods SeqDACDec2, DACDec3, WinGrow, DISTBIC\_pR, and FixSlid are denoted as SeqDACDec2\_HAC, DACDec3\_HAC, WinGrow\_HAC, DISTBIC\_pR\_HAC, and FixSlid\_HAC, respectively.

In the implementation, following the speech activity detection (SAD) method in [7], the GMMs for speech, noisy speech, speech over music, pure music, and silence/noise were trained beforehand, and the non-speech regions in the audio segments were pruned by using Viterbi decoding.

### A. Experiments on speaker diarization

1) *Data set description and performance evaluation:* We used RT03 described in Section V-B1 in the speaker diarization experiments. The audio recordings from channels ABC, NBC, and CNN were used as the development set (RT03\_Dev); while the recordings from PRI, VOA, and MNB were used as the evaluation set (RT03\_Eval).

For the performance evaluation, we used the diarization evaluation tool (md-eval-v21.pl) released by NIST [38] to evaluate the diarization error rate (DER), which takes into account three kinds of error, namely missed speech (Mis), false alarm speech (FaS), and speaker error (SpE). Readers can refer to [7] for a detailed description of these error types.

2) *Parameter setting and system description:* We used RT03\_Dev to tune the parameters for each system, and then evaluated the diarization performance on RT03\_Eval. These parameters include  $\lambda$  in the  $\Delta BIC$ -based inter-cluster distance measure in HAC-BIC, the stopping threshold in HAC-SID,  $\lambda$  in BIC-based segmentation in SeqDACDec1\_HAC, SeqDACDec2\_HAC, DACDec3\_HAC, DISTBIC\_pR\_HAC and

<sup>3</sup> $xRT = T_s / T_d$ , where  $T_s$  is the system run-time and  $T_d$  denotes the time duration of the test data set.

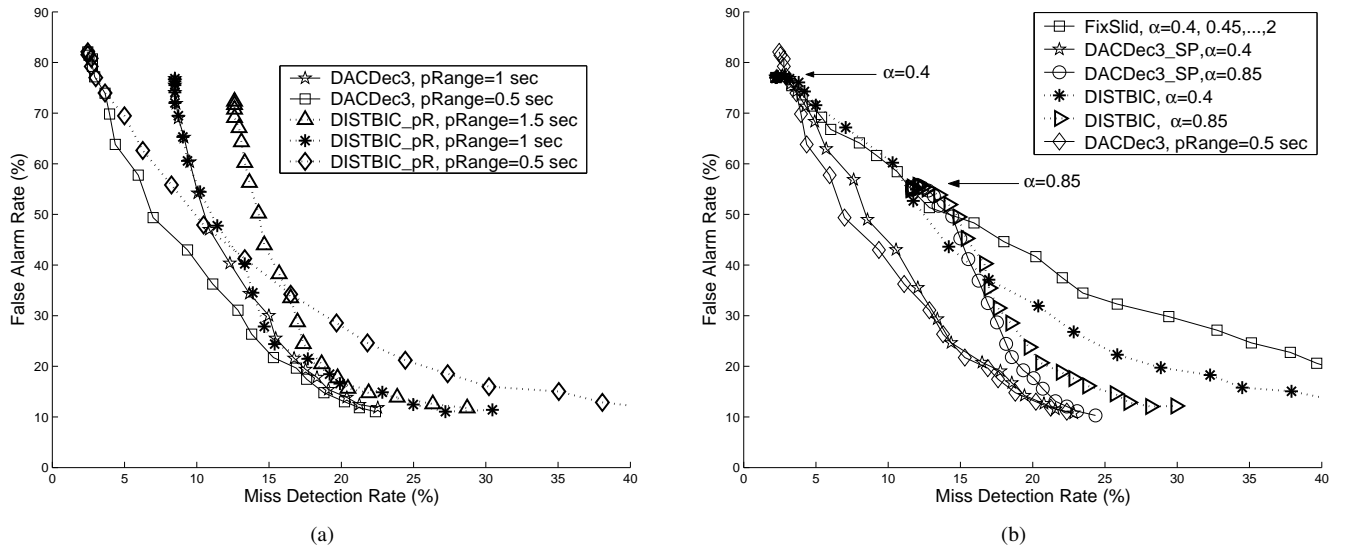


Fig. 14. ROC curves for MATBN3hr obtained by (a) DACDec3 and DISTBIC\_pR with different  $pRange$  values, and (b) FixSlid, DACDec3\_SP, DISTBIC and DACDec3.

TABLE II

THE REAL-TIME FACTOR ( $xRT$ ) OF DIFFERENT SEGMENTATION APPROACHES EVALUATED ON MATBN3HR IN THE EER CASE AND THE ASSOCIATED EERS, WHERE M AND F DENOTE THE MISS DETECTION RATE AND THE FALSE ALARM RATE, RESPECTIVELY.

Approach	WinGrow	SeqDACDec1	SeqDACDec2	DACDec3	DISTBIC_pR	FixSlid	FixSlidHAC_pR
$xRT$	0.38	0.1	0.19	0.023	0.026	0.02	1.81
Speedup over WinGrow	1	3.8	2	16.52	14.61	19	0.21
EER (in %)	M:18.08, F:18.65	M:17.84, F:17.21	M:16.42, F:15.92	M:17.61, F:17.46	M:19.19, F:18.44	M:29.42, F:29.82	M:21.09, F:22.22

TABLE III

THE REAL-TIME FACTOR ( $xRT$ ) OF DIFFERENT SEGMENTATION APPROACHES EVALUATED ON RT03 IN THE EER CASE AND THE ASSOCIATED EERS.

Approach	WinGrow	SeqDACDec1	SeqDACDec2	DACDec3	DISTBIC_pR	FixSlid	FixSlidHAC_pR
$xRT$	0.53	0.11	0.22	0.022	0.025	0.019	1.87
Speedup over WinGrow	1	4.82	2.41	24.09	21.2	27.89	0.28
EER (in %)	M:17.79, F:16.59	M:17.34, F:18.32	M:16.44, F:15.95	M:18.47, F:17.24	M:22.3, F:21.08	M:34.68, F:33.12	M:23.19, F:24.88

WinGrow\_HAC, and  $\alpha$  in FixSlid segmentation in FixSlid\_HAC. For each system, the remaining parameters in the segmentation stage were the same as those yielding the segmentation results in Figs. 15 (c) (for MATBN3hr) and 16 (for RT03).

3) *Post processing by Viterbi re-segmentation:* As reported in [35], one can use Viterbi re-segmentation after speaker clustering to improve the diarization accuracy; thus, we used this technique as a post processing step and evaluated how it effects on each diarization system. For the re-segmentation, the speech in each cluster was used to train a MAP-adapted GMM from a gender- and channel-independent UBM first, which represents one state in the applied ergodic HMM. Then, Viterbi decoding was applied to perform the re-segmentation (diarization). The GMM training and re-segmentation were done iteratively.

4) *Experiment results:* Tables IV and V show the DERs of the diarization systems without and with the Viterbi re-segmentation based post processing step, respectively. From these two tables, two observations can be drawn. First, a

more accurate speaker change detection algorithm leads to better diarization accuracy. For example, FixSlid\_HAC obtains a higher DER than the other systems. As shown in Fig. 16, its segmentation method, FixSlid, achieves a higher segmentation error. Second, Viterbi re-segmentation consistently improves the diarization accuracy of all the systems. The improvement is more significant on FixSlid\_HAC, which achieves a higher DER originally; however, its DER is still higher than those of the other systems that are based on more accurate speaker segmentation methods.

## VII. CONCLUSION

We have proposed three BIC-based speaker segmentation approaches that employ divide-and-conquer strategies for speaker change detection. In contrast to the well-known and highly accurate window-growing-based approach (WinGrow), which searches for change points in a bottom-up manner by using a sequentially growing analysis window, the proposed DACDec1 and DACDec2 approaches search for change points in a top-down manner. The proposed DACDec3 approach is



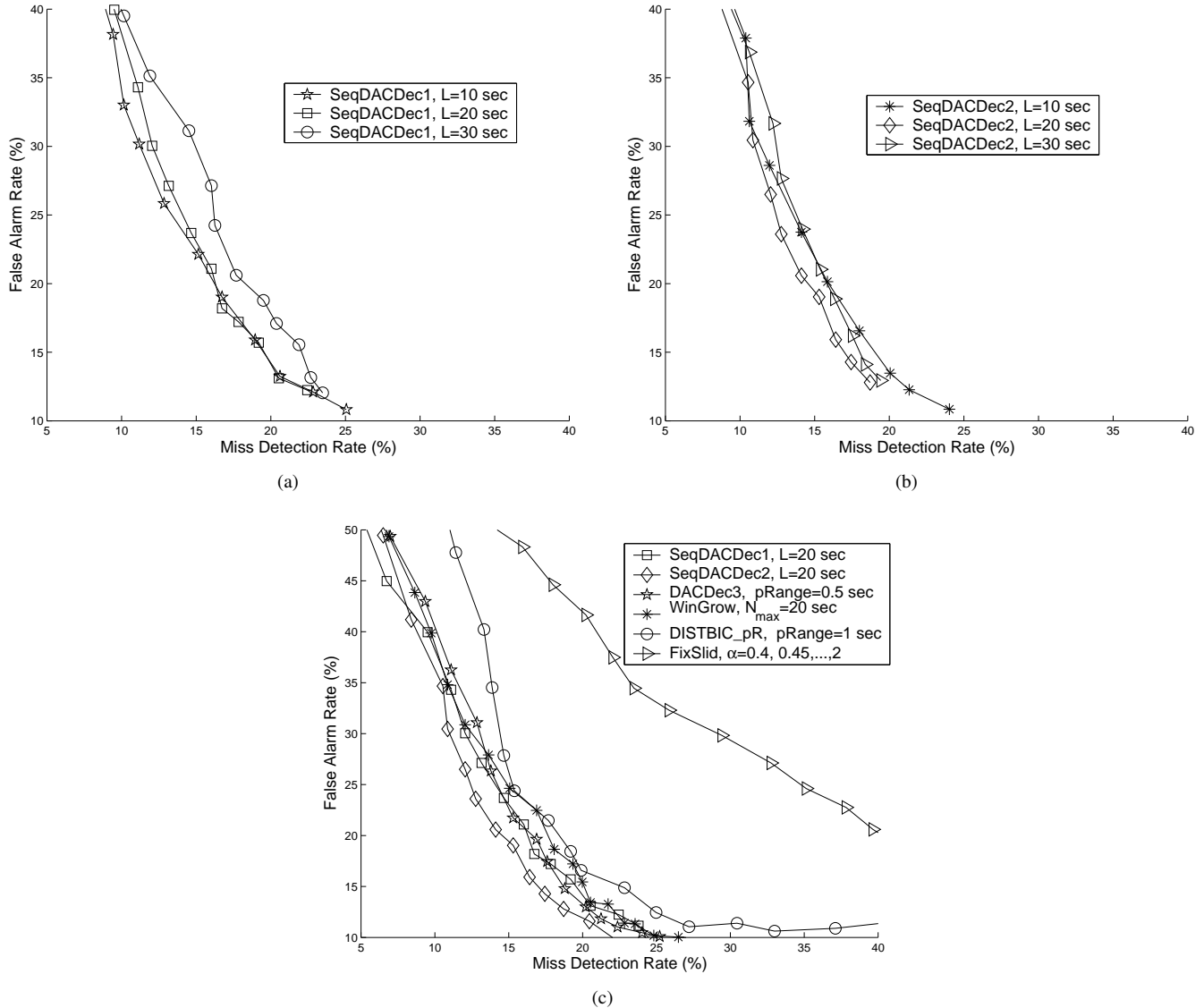


Fig. 15. The ROC curves for MATBN3hr obtained by (a) SeqDACDec1 with  $N_{min} = 2$  seconds and analysis windows of different size ( $L$ ); (b) SeqDACDec2 with  $N_{min} = 2$  seconds and analysis windows of different size ( $L$ ); and (c) SeqDACDec1 with  $N_{min} = 2$  seconds and  $L = 20$  seconds, SeqDACDec2 with  $N_{min} = 2$  seconds and  $L = 20$  seconds, DACDec3 with  $pRange = 0.5$  seconds, WinGrow with  $N_{min} = 3$  seconds and  $N_{max} = 20$  seconds, DISTBIC\_pR with  $pRange = 1$  second, and FixSlid with a 2-second sliding window.

TABLE IV  
THE DERS (IN %) OF DIFFERENT DIARIZATION SYSTEMS. VITERBI RE-SEGMENTATION IS NOT APPLIED.

Approach	RT03_Dev				RT03_Eval			
	MiS	FaS	SpE	DER	MiS	FaS	SpE	DER
SeqDACDec1_HAC	0.6	0.4	7.9	8.86	0	4	9.3	13.34
SeqDACDec2_HAC	0.6	0.4	7.7	8.7	0	4	9.4	13.39
DACDec3_HAC	0.6	0.4	7.5	8.46	0	4	9.7	13.69
WinGrow_HAC	0.6	0.4	8.3	9.29	0	4	10.1	14.12
DISTBIC_pR_HAC	0.6	0.4	8.2	9.19	0	4	9.9	13.94
FixSlid_HAC	0.6	0.4	10.5	11.52	0	4	13.3	17.57

a recursive variant of another popular approach, DISTBIC. We compared our approaches to these well-known approaches analytically by performing computational cost analysis. The results of experiments conducted on broadcast news data demonstrate that the proposed approaches are more efficient and achieve higher segmentation accuracy than the existing approaches discussed in this paper. In addition, we applied the

segmentation approaches to the speaker diarization task. The experiment results show that a more accurate segmentation approach leads to better diarization accuracy.

TABLE V  
THE DERS (IN %) OF DIFFERENT DIARIZATION SYSTEMS. VITERBI RE-SEGMENTATION IS APPLIED AS A POST PROCESSING STEP.

Approach	RT03_Dev				RT03_Eval			
	MiS	FaS	SpE	DER	MiS	FaS	SpE	DER
SeqDACDec1_HAC	0.6	0.4	7.4	8.37	0	4	9.2	13.15
SeqDACDec2_HAC	0.6	0.4	7.4	8.35	0	4	9.2	13.16
DACDec3_HAC	0.6	0.4	7	7.96	0	4	9.7	13.67
WinGrow_HAC	0.6	0.4	7.7	8.65	0	4	9.8	13.79
DISTBIC_pR_HAC	0.6	0.4	7.5	8.51	0	4	9.1	13.06
FixSlid_HAC	0.6	0.4	8.2	9.22	0	4	10.9	14.91

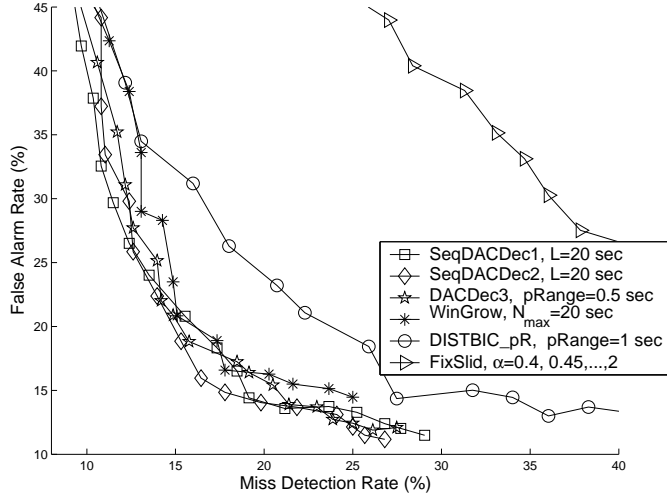


Fig. 16. The ROC curves for RT03.

## APPENDIX

### A. Compute $T_1(k)$

$T_1(k)$  is expressed as

$$\begin{aligned} T_1(k) &= \frac{1}{k} \sum_{i=1}^k (T_1(i-1) + T_1(k-i)) + (k+1)^2 m^2 \tau \\ &= \frac{2}{k} \sum_{i=1}^k T_1(i-1) + (k+1)^2 m^2 \tau, \end{aligned} \quad (18)$$

where  $T_1(0) = m^2 \tau$ . To solve this recursive equation, we can apply the technique used for analyzing the time cost of the Quicksort algorithm [39]. First, we multiply both sides of Eq. (18) by  $k$  as follows:

$$kT_1(k) = 2 \sum_{i=1}^k T_1(i-1) + k(k+1)^2 m^2 \tau. \quad (19)$$

Replacing  $k$  in Eq. (19) with  $k-1$ , we obtain

$$(k-1)T_1(k-1) = 2 \sum_{i=1}^{k-1} T_1(i-1) + (k-1)k^2 m^2 \tau. \quad (20)$$

Subtracting Eq. (20) from Eq. (19), we obtain

$$kT_1(k) - (k-1)T_1(k-1) = 2T_1(k-1) + (3k^2 + k)m^2 \tau. \quad (21)$$

Rearranging the terms in Eq. (21) yields

$$\frac{T_1(k)}{k+1} = \frac{T_1(k-1)}{k} + \frac{(3k+1)m^2 \tau}{(k+1)}. \quad (22)$$

Let  $a_k = T_1(k)/(k+1)$ , then Eq. (22) can be rewritten as

$$a_k = a_{k-1} + \left(3 - \frac{2}{k+1}\right) m^2 \tau, \quad (23)$$

where  $a_0 = m^2 \tau$ . Recursively substituting the  $a_k s'$  in Eq. (23), we obtain

$$\begin{aligned} a_k &= a_0 + \left(3k - \left(\frac{2}{2} + \frac{2}{3} + \dots + \frac{2}{k+1}\right)\right) m^2 \tau \\ &= (3k + 3 - 2 \sum_{i=1}^{k+1} \frac{1}{i}) m^2 \tau. \end{aligned} \quad (24)$$

Because  $\sum_{i=1}^{k+1} \frac{1}{i} \approx \ln(k+1)$  [39], we have

$$a_k \approx (3k + 3 - 2 \ln(k+1)) m^2 \tau. \quad (25)$$

Since  $a_k = T_1(k)/(k+1)$ ,  $T_1(k)$  can be expressed as

$$\begin{aligned} T_1(k) &= a_k (k+1) \\ &\approx (3(k+1)^2 - 2(k+1) \ln(k+1)) m^2 \tau. \end{aligned} \quad (26)$$

### B. Compute $T'(m)$

$T'(m)$  is expressed as

$$T'(m) = \frac{1}{m} \sum_{i=1}^m (T'(i-1) + T'(m-i)) + m^2 \tau + m\tau, \quad (27)$$

where  $T'(0) = 0$ . Similar to the manipulation of Eq. (18) in Appendix A, by setting  $a_m = T'(m)/(m+1)$ , we have  $a_0 = 0$  and

$$\begin{aligned} a_m &= a_{m-1} + \frac{(3m-1)\tau}{m+1} \\ &= a_{m-1} + \left(3 - \frac{4}{m+1}\right) \tau \\ &= a_0 + \left(3m - \left(\frac{4}{2} + \frac{4}{3} + \dots + \frac{4}{m+1}\right)\right) \tau \\ &\approx (3m + 4 - 4 \ln(m+1)) \tau. \end{aligned} \quad (28)$$

Since  $a_m = T'(m)/(m+1)$ , we have

$$\begin{aligned} T'(m) &= a_m (m+1) \\ &\approx (3m + 4 - 4 \ln(m+1)) (m+1) \tau. \end{aligned} \quad (29)$$

### C. Compute $T_2(k)$

$T_2(k)$  is expressed as

$$T_2(k) = \frac{1}{k} \sum_{i=1}^k (T_2(i-1) + T_2(k-i)) + (k+1)^2 m^2 \tau + 2m\tau, \quad (30)$$

where  $T_2(0) \leq (3m+4-4\ln(m+1))(m+1)\tau$ . Similar to the manipulation of Eq. (18) in Appendix A, by setting  $a_k = T_2(k)/(k+1)$ , we have

$$\begin{aligned} a_k &= a_{k-1} + \frac{(3k^2+k)m^2\tau + 2m\tau}{k(k+1)}, \\ &= a_{k-1} + \left(3 - \frac{2}{k+1}\right)m^2\tau + 2\left(\frac{1}{k} - \frac{1}{k+1}\right)m\tau, \\ &\approx a_0 + (3k+2-2\ln(k+1))m^2\tau \\ &\quad + 2(\ln k - \ln(k+1) + 1)m\tau. \end{aligned} \quad (31)$$

Substituting  $a_0 = T_2(0)$  into Eq. (31), we obtain

$$a_k \leq (3k+5-2\ln(k+1))m^2\tau + (9+2\ln k - 2\ln(k+1) - 4\ln(m+1))m\tau + (4-4\ln(m+1))\tau. \quad (32)$$

Since  $a_k = T_2(k)/(k+1)$ , we have

$$\begin{aligned} T_2(k) &\leq (3k+5-2\ln(k+1))(k+1)m^2\tau \\ &\quad + (9+2\ln k - 2\ln(k+1) - 4\ln(m+1))(k+1)m\tau \\ &\quad + (4-4\ln(m+1))(k+1)\tau. \end{aligned} \quad (33)$$

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