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Abstract

We use data from highway procurement auction subject to California's Small Business Preference program to study the effect of bid preferences on auction outcomes. Our analysis is based on an estimated model of firms' bidding and participation decisions, which allows us to evaluate the effects of current and alternative policy designs. We show that incorporating participation responses significantly alters the assessment of preferential treatment policies.

Disciplines

Business | Economic Policy | Infrastructure | Marketing | Policy Design, Analysis, and Evaluation | Public Administration | Transportation

Bid Preference Programs and Participation in Highway Procurement Auctions[†]

By ELENA KRASNOKUTSKAYA AND KATJA SEIM*

We use data from highway procurement auctions subject to California's Small Business Preference program to study the effect of bid preferences on auction outcomes. Our analysis is based on an estimated model of firms' bidding and participation decisions, which allows us to evaluate the effects of current and alternative policy designs. We show that incorporating participation responses significantly alters the assessment of preferential treatment policies. (JEL D44, H76, R42)

Public-sector procurement accounts for over 10 percent of US GDP. Across levels of government, preferential treatment programs are extensively used in procurement auctions. For example, in 2006, the federal government awarded 20 percent of its procurement dollars to favored firms.¹ One commonly used preference mechanism, a bid discount or credit, improves the bids of favored firms by a preestablished rate when determining the winner but uses the actual amount of the winner's bid in the contract.² Prominent examples include a 25 percent bid credit granted to small firms in Federal Communications Commission (FCC) spectrum auctions and a 50 percent bid penalty added to foreign bids on defense contracts.³ The aim of this paper is to improve our understanding of the effects of such preference programs on the government's cost of procurement and the distribution of profits between participants, as well as to provide an assessment of the likely magnitudes of these effects in practice. We do so empirically in the context of the California Small Business Preference program that grants small firms a 5 percent bid discount.⁴

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[†] To view additional materials, visit the article page at <http://www.aeaweb.org/articles.php?doi=10.1257/aer.101.6.2653>.

¹ See the Federal Procurement Report 2007, available at <https://www.fpds.gov/>.

² With a 10 percent bid discount, for example, a bid by a favored firm of \$440,000 is treated as a bid of \$400,000 in comparing it to the remaining, nonfavored, firms' bids. If the favored firm wins, its payment is the original amount of the bid, or \$440,000.

³ See "Implementation of the Commercial Spectrum Enhancement Act and Modernization of the Commission's Competitive Bidding Rules and Procedures," WT Docket No. 05-211, Second Report and Order and Second Further Notice of Proposed Rulemaking, 21 FCC Rcd 4753, 4766 par 36 (2006); and the Department of Defense's "Defense Federal Acquisition Regulation Supplement," Part 225: Foreign Acquisition (2008), available at <http://www.acq.osd.mil/>.

⁴ Other empirical studies of preference programs include Justin Marion (2007, 2009) who finds two specific preference programs to be costly to governments; Thomas A. Denes (1997) who provides evidence of cost decreases in

The stated goal of most preference programs is to facilitate the integration of favored participants into the marketplace. These are often groups historically discriminated against, or groups considered disadvantaged due to entry barriers, or both. They are also often considered to be less cost efficient. As preference programs result in such high-cost companies performing a larger share of work, one may expect the cost of procurement to increase. At the same time, however, these programs also provide incentives to nonfavored firms to bid more aggressively against the strengthened favored group, which mitigates the upward pressure on the cost of procurement. For some discount levels, this last effect is sufficiently strong for the cost of procurement to actually decrease (R. Preston McAfee and John McMillan 1989 and Allan Corns and Andrew Schotter 1999 show this theoretically and in experiments, respectively, for assumed numbers of bidders and cost distributions).

The key insight of this paper is that there is a third effect neglected in the literature. Bid preference programs have potentially strong effects on firms' incentives to participate in an auction. We show that accounting for a response in participation behavior significantly alters the assessment of the preference program's cost to the government and its distributional effects. While it continues to be possible to use bid discounts to lower the cost of procurement as in McAfee and McMillan (1989), both the cost-minimizing level of the discount and the group receiving the discount may change when participation effects are taken into account. The currently accepted practice of evaluating bid preference programs holding participation fixed can yield very misleading results.

The theoretical literature suggests that the magnitudes of the program's effects crucially depend on the degree of cost asymmetries between favored and other bidders. We thus base our analysis on empirically relevant distributions of firm costs recovered from data on highway procurement auctions that were awarded under a bid preference program. We use a model of firms' participation and bidding decisions in the presence of a bid discount.⁵ The firm's decision of which bid to submit reflects its private information about its cost of completing the project, which we term "project cost," and the distributions of its competitors' project costs. The participation decision instead is based on a comparison of the cost of preparing the bid, or entry cost, to the expected profit from participation. Only firms with entry costs below the expected profit ultimately submit a bid in the auction. We use this model to uncover the underlying distributions of firms' entry and project costs consistent with observed choices.

The nature and importance of our findings can be seen from Figure 1 that plots changes in the government's cost of procurement relative to no discrimination at different levels of the bid discount for a typical project in our data.⁶ We contrast the

some set-aside auctions for dredging work; and Ian Ayres and Peter Cramton (1996) who argue that preference programs yielded significant revenue increases in a small sample of FCC spectrum auctions. These papers use descriptive methods, which allow them to measure the effects of the current programs, but do not permit an evaluation of alternative program designs. Francesco Decarolis (2010) analyzes average price auctions that could be interpreted as an extreme form of preference policy where the bid closest to the average wins and the high bid is eliminated.

⁵Our analysis also contributes to a small but growing literature that empirically studies the decision to participate in auctions. Susan Athey, Jonathan Levin, and Enrique Seira (2011), Patrick Bajari and Ali Hortacsu (2003), Tong Li (2005), and Li and Xiaoyong Zheng (2009) represent recent contributions to this literature.

⁶The project's cost distributions are representative of approximately 30 percent of projects. The remaining projects are discussed in the main body of the paper.

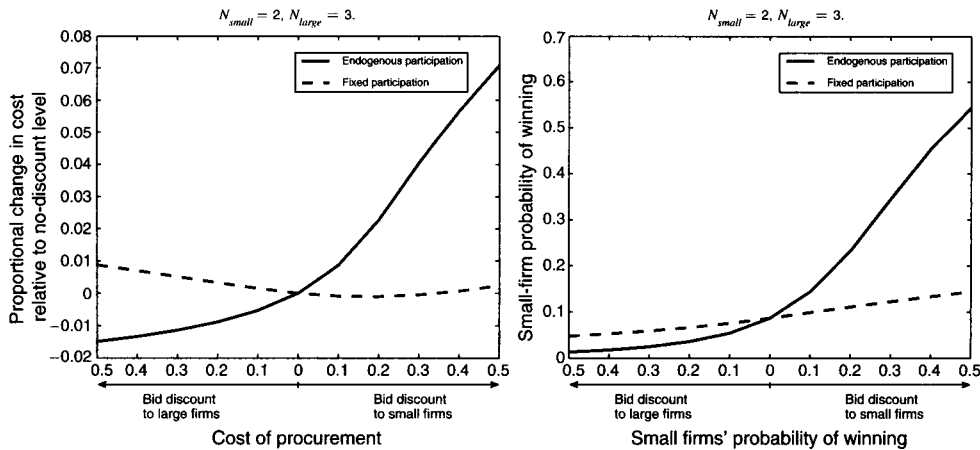


FIGURE 1. COST OF PROCUREMENT AND PROBABILITY OF WINNING UNDER FIXED AND ENDOGENOUS PARTICIPATION, SAMPLE PROJECT

cost of procurement implied by a model that does not allow firms to respond to the discount in their participation behavior with one where participation adjusts endogenously. Several patterns emerge:

- (i) Under fixed participation, the cost of procurement varies only by a limited amount as the discount changes from 50 percent to large bidders (the leftmost point in the figure) to 50 percent to small bidders (the rightmost point). The cost of procurement exhibits significantly more variation when we take participation effects into account.
- (ii) The implications for policy design differ significantly in the two cases. To minimize the cost of procurement, the model with fixed participation prescribes a discount of approximately 20 percent to small bidders. Relaxing the assumption of fixed participation suggests that offering such a discount to small bidders would actually increase the cost of procurement. Instead, a discount of 50 percent should be offered to *large* bidders to achieve substantial cost savings.
- (iii) California's Small Business Preference program aims to allocate 25 percent of procurement dollars to small firms, which we refer to as the program's "allocative goal." The fixed participation model implies that the small-firm discount required to achieve this goal is more than 50 percent for this particular project. This model predicts that such a discount yields a 0.23 percent increase in procurement cost. However, a model that takes participation adjustments into account would recognize that this substantial discount deters large-firm participation and, therefore, that the true cost increase would be 7.8 percent. Additionally, preferential treatment increases small-firm participation and in turn the group's probability of winning; hence, a bid discount of only approximately 20 percent is sufficient to achieve the allocative goal, raising the government's cost by 3.2 percent.

This example is based on a particular, albeit common, type of project in our data. An aggregate evaluation of California's preference policy needs to take into account heterogeneity in project characteristics and the competitive environment, which introduces heterogeneity in the effectiveness of a bid discount across projects. Our empirical results suggest significant differences in the degree of cost asymmetries between large and small firms across projects. For an important subset of projects in our data, we recover cost distributions for large and small firms that are very similar. As a result, small-firm participation and winning rates for these projects are high even in the absence of a bid discount. Because of the particular mix of projects, the aggregate cost of procurement at a discount level that awards 25 percent of procurement dollars to small firms is only 1.4 percent higher than the aggregate cost under no preferential treatment. It is important to note, however, that this result is specific to the California market. In other markets where the composition of projects is different, the cost of bid preference programs may be very different.

For California's current program, which uses a relatively low discount level of 5 percent, we find that the cost of procurement is within 1.5 percent of the cost of procurement in the absence of discrimination. However, the program induces substantial changes in small and large firms' participation and probabilities of winning. It results in a redistribution of 5 to 12 percent of profits from large to small firms for typical projects that differ in type of work, location, and size. At the same time the program does not achieve its goal of allocating 25 percent of procurement dollars to small firms.

We compare the bid-discount program to an alternative preference mechanism that relies on lump-sum entry subsidies and/or taxes. We find that an appropriately chosen tax/subsidy policy is more effective in lowering the cost to the government in absolute terms, as well as when constraining the policy to achieve California's allocative goal. It does so by extracting bidders' full expected surplus. Such a strong negative impact on bidders' profitability may be undesirable for government policy. Interestingly, we show that the tax/subsidy policy results in a higher cost to the government than the corresponding bid discount policy if the objective is to achieve the allocative goal while holding large-firm profits at the level under the bid discount. This result underscores an important benefit of the bid preference program: it is able to moderate the degree of profit redistribution and the increase in the cost of procurement, while delivering changes in allocation of work across bidder groups.

The paper proceeds as follows. Section I provides a brief overview of the highway procurement market in California and the details of the Small Business Preference program. Section II outlines the model of firms' joint participation and bidding decisions. Section III describes our estimation methodology, the results of which are in Section IV. Section V contains an analysis of the current and alternative programs. Section VI concludes.

I. California's Highway Procurement Market

In this section, we describe the California highway procurement market and our data. We focus on highway and street maintenance projects auctioned by the California Department of Transportation (Caltrans) between January 2002 and December 2005. California's Small Business Preference program is implemented

on state-funded projects. During the sample period, Caltrans advertised 869 state-funded projects, of which complete data are available for 697 projects.⁷ The data include information on project characteristics, the set of companies that purchased detailed project specifications and their small business status, the set of actual bidders, their bids, and, finally, the identity of the winning bidder.

A. Letting Process

Caltrans advertises projects three to ten weeks prior to the bidding date. The project advertisement usually contains only limited information, such as type of work, location, and completion time. Interested contractors must purchase detailed project plans from Caltrans' project counter at least one week before the bid opening date. Only those firms that purchased project plans (plan holders) may submit a bid on the project. Our data suggest that purchasing a plan signals interest in bidding; we observe, for example, that in their plan purchases, companies focus on similar projects based on administrative district location and type of work. We therefore assume that the group of potential bidders on a given project coincides with the group of plan holders. The list of companies that purchased plans for a given project is posted on Caltrans' Web site. Therefore, potential bidders are known to each other at the time when they prepare their bids.

To bid on a project, a company must submit by the bid opening date completed bid documents, which specify the bid amount, the list of subcontractors, their fees, and their tasks. The preparation of bid documents requires time and effort and is, therefore, costly. We treat such bid preparation costs as entry costs in our model below.

During the bid preparation process, companies engage in extensive negotiations with subcontractors. It is likely that participants learn about other companies preparing bids for the same project from subcontractors. Anecdotal evidence confirms that such information leakage occurs. Discussions with industry insiders also suggest that prime contractors are careful not to reveal other information about their bid proposal, such as the cost of other contract items, quotes received from other subcontractors, etc., to potential subcontractors. Price negotiations also typically continue up until the bid submission deadline, limiting the subcontractor's ability to convey any price information to competitors.

As is evident from the bid documents, the sets of subcontractors often overlap across companies submitting bids for the same auction. Common subcontractor use can potentially induce affiliation into bidders' costs, i.e., a correlation in their costs in excess of any correlation introduced by factors known to bidders. We investigated empirically how important such subcontractor induced correlation is in explaining bid levels. Using price data and subcontractor information at the level of the individual contract item for a subsample of our bid documents, we find that the identity of the subcontractor explains approximately 6 percent of the average item price across items and contractors. This combined with the fact that the total value of items for which common subcontractors are used constitutes at most 5 percent of the overall bid suggests that the extent of affiliation due to common subcontractor use is low.

⁷ Caltrans did not preserve lists of companies that purchased bid documents for some projects.

B. Preference Program

The Small Business Preference program sets a goal of allocating 25 percent of state procurement dollars to small firms. The program is implemented using a first-price sealed-bid auction mechanism. It grants small firms a bid discount equal to 5 percent of the low nonfavored bid, reducing their bids for comparison purposes only when determining the winner. The winner is then paid the full amount of his bid.

To qualify for the discount, a company has to satisfy three conditions. It has to be independently owned and operated; have fewer than 100 employees; and have average annual gross receipts limited to \$10 million over the previous three tax years.⁸ A common concern with preference programs is the potential for abuse and manipulation. The structure of the procurement market renders such abuse more difficult than in other markets. Strict subcontracting limits are in place, and Caltrans monitors projects to ensure that the chosen contractor adheres to these limits. In addition, small contractors' competitors have a vested interest to ensure that the small-business status is used only when applicable. While the instance of abuse is rare, the state also actively prosecutes and penalizes abusers, both imposing monetary penalties and withdrawing the right to participate in future procurement auctions.

We obtained quarterly information on the certification status of companies in our dataset from the Department of General Services. In our sample, out of 672 companies that bid on at least one project, 269, or 40 percent, were certified as small businesses. Caltrans awarded 39.02 percent of contracts to qualified small businesses. The total value of these contracts accounted for only 15.45 percent of total procurement dollars, however. Most of the projects allocated to small firms are therefore small. It also means that Caltrans does not meet the program's allocative goal. The bid preference altered the identity of the winning bidder in only 5 percent of projects.

II. Model of Firms' Participation and Bidding Decisions

This section develops a model of firms' participation and bidding decisions that forms the basis for our empirical analysis below. We assume that a total of N potential contractors express interest in a single standalone project offered for bid. Bidder i 's decisions reflect two separate costs; entry costs of preparing a bid, denoted by d_i , and costs of completing the contract (project costs), denoted as c_i .

We incorporate a preference rule similar to the one used in California into our model. For the purpose of comparison, bids of favored firms are reduced by an amount equal to δ percent of the lowest nonfavored bid. A favored firm is awarded the project if its reduced bid is below the lowest nonfavored bid. For a given lowest nonfavored bid of b_l , a favored firm thus wins the project if its bid is lower than $(1 + \delta)b_l$. It receives the full amount of its bid as payment. A preference program thus introduces an asymmetry into the payoffs of favored and other firms. In our

⁸Such revenue restrictions could affect small firms' entry behavior. For example, a company may decide not to bid on a large project if winning this project brings it over or very close to the revenue threshold. In our data, however, 99 percent of small firms have yearly revenue below \$5.4 million, relative to a large project's typical size of about \$1 million. Therefore, in most cases winning one additional large project does not impact the small-firm status of a company, and we do not model such dynamic concerns about qualifying for small-firm status.

analysis we also allow for the possibility that favored (group 1) and other (group 2) firms differ systematically in their costs of preparing bids, G_D^k , and of completing the project, F_C^k . Here $k(i)$ denotes group affiliation of bidder i . We assume that project and bid preparation costs are private information of each firm and are distributed independently across all firms and identically within group.

Similar to other work on auction participation (e.g., William F. Samuelson 1985, Dan Levin and James L. Smith 1994), we model a potential bidder's decision as a two-stage process. In the first stage, each potential bidder decides whether to participate in the auction. In the second stage, actual bidders prepare and submit their bids. When deciding over participation, potential bidder i of group $k(i)$ knows his own cost of entry, d_i , the distributions of project and entry costs, F_C^k and G_D^k , $k = 1, 2$, and the numbers of potential bidders by group, $N_{k(i)}, N_{-k(i)}$. Only firms with an entry cost below the expected profit from participation choose to enter the auction. Firms that decided to enter pay bid preparation costs, become actual bidders, and submit bids. By incurring bid preparation costs, a bidder learns his costs of completing the contract, c_i , and the numbers of his actual competitors by group, $(n_{k(i)} - 1, n_{-k(i)})$.

Our model of entry resembles the setup in Levin and Smith (1994) by relying on two assumptions: (i) a potential bidder does not observe his project cost realization at the time of his participation decision but learns it through the investment of bid preparation costs; (ii) bidders know the numbers of their competitors when they decide on a bid level.⁹ An alternative to assumption (i) is presented in Samuelson (1985), where project costs are known at the time of entry.¹⁰ This alternative informational environment finds less support than the assumption we use in empirical tests of entry models.¹¹ We also carefully considered the applicability of assumption (ii) to our setting. We experimented with an alternative informational assumption that firms do not have knowledge of the numbers of bidders throughout the entire bidding process. This model generally produced markups that were significantly higher than typical highway construction markups. Assumptions (i) and (ii) greatly facilitate the computation of participation and bidding strategies, in particular given our context of asymmetric auctions where we have to find equilibrium bidding strategies numerically, as we discuss below.¹² This is what allows us to conduct an extensive counterfactual analysis, which would have to be significantly curtailed under either of the two alternative informational environments discussed here.

A. Characterization of Equilibrium in the Bidding Stage

We begin with an analysis of the bidding stage and then use the results to analyze the participation stage. We focus on group-symmetric equilibria where bidders of

⁹ Athey, Levin, and Seira (2011) also rely on these assumptions.

¹⁰ James Roberts and Andrew Sweeting (2010) analyze the properties of this and related models for second-price auctions.

¹¹ In the context of symmetric auctions, Vadim Marmer, Artyom Shneyerov, and Pai Xu (2007) and Li and Zheng (2009) perform tests of alternative models of entry using different methodologies. Both sets of authors find more statistical support for a two-stage entry model where firms are initially uninformed or only partially informed about their project costs and pay an entry cost to learn their actual realization than an alternative where project costs are known at the time of entry.

¹² Assumption (i) also simplifies the empirical implementation of the model. The lack of selection on project costs allows us to recover their full (untruncated) distribution in estimation and we are able to more easily incorporate the effect of unobserved project characteristics on firms' bidding behavior.

group k follow the same bidding strategy, $\beta_k(\cdot)$, mapping project cost, c_i , into a bid b_i , $\beta_k(\cdot) : [c, \bar{c}] \rightarrow [\underline{b}_k, \bar{b}_k]$. Due to the bid-preference program, a bidder i of group k wins the project if his bid b_i is below all competing bids adjusted by the bid discount δ where applicable. Firm i with project cost c_i and group membership $k(i)$ chooses bid b_i to maximize expected profit conditional on participating:

$$\begin{aligned} (1) \quad \pi_i(c_i) &= (b_i - c_i) \Pr(b_i \leq b_l, \forall l : k(l) = k(i)) \\ &\quad \times \Pr(b_i \leq (1 + \delta)^{1-2I(k=2)} b_l, \forall l : k(l) \neq k(i)) \\ &= (b_i - c_i) (1 - F_C^k[\beta_k^{-1}(b_i)])^{n_k-1} (1 - F_C^{-k}[\beta_{-k}^{-1}(1 + \delta)^{1-2I(k=2)} b_i])^{n-k}, \end{aligned}$$

where $I(k=2)$ is an indicator variable that equals one if firm i belongs to group 2. The first-order condition of the firm's bidding problem is:

$$\begin{aligned} (2) \quad \frac{1}{b_i - c_i} &= \frac{(n_{k(i)} - 1) f_C^{k(i)}[\beta_{k(i)}^{-1}(b_i)]}{(1 - F_C^{k(i)}[\beta_{k(i)}^{-1}(b_i)])} \frac{\partial \beta_{k(i)}^{-1}}{\partial b_i} \\ &\quad + \frac{n_{-k(i)} (1 + \delta)^{1-2I(k(i)=2)} f_C^{-k(i)}[\beta_{-k(i)}^{-1}((1 + \delta)^{1-2I(k(i)=2)} b_i)]}{(1 - F_C^{-k(i)}[\beta_{-k(i)}^{-1}((1 + \delta)^{1-2I(k(i)=2)} b_i)])} \frac{\partial \beta_{-k(i)}^{-1}}{\partial b_i}. \end{aligned}$$

The preference program introduces two interesting features into the equilibrium, reflecting the increased competitiveness of favored bidders. First, a single favored bidder with $c_i = \bar{c}$ finds it optimal to bid above his cost when bidding against several nonfavored bidders since the bid discount sufficiently lowers his effective bid to result in a nonzero probability of winning the project.¹³ In contrast, with multiple favored bidders, competitive pressure reduces the upper boundary bid to cost. Second, since the highest effective bid submitted by a favored bidder is given by $\bar{b}_1/(1 + \delta)$, nonfavored bidders with cost $c_i \in [\bar{b}_1/(1 + \delta), \bar{c}]$ can never win an auction where a small bidder is present and earn positive profit.

The behavior of bidders with boundary cost draws can be summarized as follows.

- (i) *Right-boundary condition.* Favored bidders with cost level \bar{c} bid $\bar{b}_1 = \bar{c}$ if $n_1 > 1$. If $n_1 = 1$, \bar{b}_1 is the bid level that maximizes

$$(3) \quad \pi_i = (\bar{b}_1 - \bar{c}) \left(1 - F_2\left(\frac{\bar{b}_1}{(1 + \delta)}\right) \right)^{n_2}.$$

Nonfavored bidders with $c_2 \in [\bar{b}_1/(1 + \delta), \bar{c}]$ have a zero probability of winning and, therefore, bid their cost.

¹³Note that consistent with Caltrans policy, we do not impose a reserve price. If only a single bidder chose to enter the auction, there are thus no constraints on his bid. We follow Li and Zheng (2009) and assume that in such instances, the government steps in as a second bidder, drawing its project cost from the nonfavored cost distribution. This approximates the competitive pressure that Caltrans imposes in such instances through the right to reject a bid and rescope a project. Since our data do not contain projects with only one bidder, this assumption is relevant only when computing the expected profit from entry by averaging over all possible bidder combinations.

- (ii) *Left-boundary condition.* There exists a bid level \underline{b}_1 such that for all favored firms, $\beta_1(c) = \underline{b}_1$. For all nonfavored bidders, $\beta_2(c) = \underline{b}_2 = \underline{b}_1/(1 + \delta)$.

The proof of these properties follows the standard reasoning for boundary conditions in first-price auctions. Theorem 2.1 in Philip J. Reny and Shmuel Zamir (2004) establishes the existence and uniqueness of the bidding equilibrium in this environment.

B. Characterization of Equilibrium in the Participation Stage

At the participation stage, firms compare the ex ante expected profit conditional on entry to their entry cost d_i . Firms with entry costs below their expected profit decide to incur the entry fee to learn about their cost of completing the project. Ex ante expected profit from participating is given by

$$(4) \quad \bar{\pi}_k(p_1, p_2) = \sum_{n_k-1, n_{-k} \in N_k-1, N_{-k}} \left(\int_{\underline{c}}^{\bar{c}} \pi_k(c; n_k - 1, n_{-k}) dF_C^k(c) \right) \Pr(n_k - 1, n_{-k} | N_k, N_{-k}),$$

where $\Pr(n_k - 1, n_{-k} | N_k, N_{-k})$ is the probability of observing $(n_k - 1)$ competitors of the firm's own group and n_{-k} competitors of the opposite group, given numbers of potential entrants of N_k and N_{-k} . $\pi_k(c; n_k - 1, n_{-k})$ is the expected equilibrium profit of a bidder from group k with cost realization c . It reflects that at the participation stage, the firm is uncertain about both its own project cost and the competitive environment it will face upon entry. As a result, the expected profit differs only by group k , but not by firm i . The firms assess the probability that there will be $n_k - 1$ and n_{-k} competitors in the auction as

$$(5) \quad \Pr(n_k - 1, n_{-k} | N_k, N_{-k}) \\ = C_{N_k-1}^{n_k-1} C_{N_{-k}}^{n_{-k}} (p_k)^{n_k-1} (1 - p_k)^{N_k-n_k-2} (p_{-k})^{n_{-k}} (1 - p_{-k})^{N_{-k}-n_{-k}},$$

where C_N^n denotes the binomial coefficient of choosing n firms out of N potential bidders.

The participation decision is described by group-specific entry cost thresholds, D_k , such that only firms with entry costs below their group's threshold participate in the auction. They are defined by a zero-profit rule so that $D_1(p_1, p_2) = \bar{\pi}_1(p_1, p_2)$ and $D_2(p_1, p_2) = \bar{\pi}_2(p_1, p_2)$. In equilibrium, bidders' beliefs are correct and the equilibrium entry probabilities solve the system of equations

$$(6) \quad \begin{aligned} p_1 &= G_1[D_1(p_1, p_2)] \\ p_2 &= G_2[D_2(p_1, p_2)]. \end{aligned}$$

Brouwer's Fixed Point Theorem guarantees that the group-specific equilibrium of this game exists. In general, the entry equilibrium is not unique. There may be multiple threshold pairs that solve equation (6). These equilibria are observationally equivalent in terms of submitted bids and differ only in entry probabilities. We

verify the uniqueness of the equilibrium entry probabilities numerically within the estimation routine.¹⁴

III. Estimation

The theoretical model describes group-specific participation and bidding strategies that map firms' project and participation costs and their respective distributions into observed bids and participation behavior. This section outlines the estimation methodology we use to recover parameters of the underlying distributions of entry and project costs from available data. We use a two-step estimation approach. In the first step, parameters of the bid distribution and the distribution of entry costs are estimated without imposing the full set of equilibrium restrictions. In the second step, the distribution of project costs is recovered from the equilibrium bidding first-order conditions following the procedure described in Emmanuel Guerre, Isabelle Perrigne, and Quang Vuong (2000).¹⁵

A. Empirical Model

We assume that at announcement, a project is characterized by $(\mathbf{x}_j, \mathbf{z}_j, u_j, N_{1j}, N_{2j})$. Here \mathbf{x}_j and \mathbf{z}_j denote potentially overlapping project characteristics observable to the researcher that affect the distributions of project and entry costs, respectively. There may also exist other project attributes that impact firms' bidding and participation behavior that are not present in the data. These factors are summarized by the variable u_j . As in Krasnokutskaya (2011), we assume that bidders' project costs for project j are given by $c_{ij} = \tilde{c}_{ij} u_j$. Here, \tilde{c}_{ij} is a firm-specific cost component that is private information of firm i , while u_j represents a portion of project j 's cost that is known to all bidders but is unobserved to the researcher, i.e., unobserved project heterogeneity.¹⁶ The distribution of the firm-specific cost component for group- k firms is given by $F_c^k(\cdot | \mathbf{x}_j)$, while the distribution of unobserved project heterogeneity is given by

¹⁴The equilibrium in the bidding stage results in nonfavored bidders with $c_2 \in [\bar{b}_1(1 + \delta)^{-1}, \bar{c})$ having a zero probability of winning. Such firms may decide to drop out of the auction after learning their costs. In this case, equation (6) should be adjusted to $p_k = G_k[D_k(p_1, p_2 p^{nb})]$, $k = 1, 2$, where p^{nb} denotes the probability of nonfavored bidders leaving the auction after learning their project cost realization. In estimation, the full distribution of large-firm project costs can be recovered from auctions that did not attract any small bidders. The probabilities $p_2 p^{nb}$ can be recovered from ratios of cumulative distribution functions of project costs for projects with $n_1 = \{1, 2\}$ and those with $n_1 = 0$ for interior cost levels.

¹⁵Mireia Jofre-Bonet and Martin Pesendorfer (2003) and Athey, Levin, and Seira (2011) use similar estimation methodologies. A standard procedure of estimating the distribution of project costs directly from the data poses severe computational challenges for models with asymmetric bidders. The computational burden is high because these models typically do not yield closed-form solutions for firms' bidding strategies, which are instead found numerically for every parameter guess and every project. A disadvantage of such indirect approaches is that they impose a parametric assumption on the bid distribution, which is not a primitive of the underlying model. To minimize any resulting misspecification bias, we use a flexibly specified bid distribution, controlling for a large number of project characteristics and time trends.

¹⁶The unobserved heterogeneity rationalizes correlation in bid residuals. There are two possible sources of such a correlation: (i) factors that are observable to all bidders, but not to the econometrician (unobserved heterogeneity), or (ii) factors that are unobservable to both bidders and the econometrician. The latter case is referred to as affiliation of costs. Given the current lack of results on the nonparametric identification of a model with both unobserved heterogeneity and affiliation, researchers typically focus on the more important source of correlation in their specific empirical setting. We believe that in our application, unobserved auction heterogeneity dominates, as described in Section II. Li and Bingyu Zhang (2010) describe a methodology that is appropriate for markets where affiliation in costs is more important.

$H(\cdot)$. We further assume that firms observe the realization of the unobserved project characteristic prior to making their entry decisions. It, therefore, affects both firms' participation and bidding behavior.

The firm-specific project cost components, \tilde{c}_{ij} , are mutually independent conditional on project characteristics, \mathbf{x}_j and u_j , and are independent of the unobserved auction heterogeneity component, u_j :

$$(7) \quad F_{\tilde{c}|\mathbf{x}}(\tilde{c}_1, \dots, \tilde{c}_{(N_1+N_2)} | \mathbf{x}_j, u_j) = F_{\tilde{c}|\mathbf{x}}(\tilde{c}_1, \dots, \tilde{c}_{(N_1+N_2)} | \mathbf{x}_j) = \prod_{i=1}^{N_1+N_2} F_{\tilde{c}}^{k(i)}(\tilde{c}_i | \mathbf{x}_j).$$

The unobserved heterogeneity component, u_j , is independent of project characteristics \mathbf{x}_j and \mathbf{z}_j and of the numbers of potential entrants, N_{1j} and N_{2j} , i.e., $H(\cdot | \mathbf{x}_j, \mathbf{z}_j, N_{1j}, N_{2j}) = H(\cdot)$.

Since we assume that bidders observe the numbers of their actual competitors when preparing their bid, firm i 's bidding strategy for project j depends on project characteristics, \mathbf{x}_j and u_j , and the numbers of actual bidders. Letting $\beta_k(\cdot|\cdot)$ and $\tilde{\beta}_k(\cdot|\cdot)$ denote the group- k bidding strategies associated with arbitrary draw u_j and with $u_j = 1$, respectively, under our assumed cost structure $\beta_{k(i)}(c_{ij} | \mathbf{x}_j, u_j, n_{1j}, n_{2j}) = u_j \tilde{\beta}_{k(i)}(\tilde{c}_{ij} | \mathbf{x}_j, n_{1j}, n_{2j})$. This implies $b_{ij} = \tilde{b}_{ij} u_j$, where \tilde{b}_{ij} denotes the firm-specific bid component given by $\tilde{b}_{ij} = \tilde{\beta}_{k(i)}(\tilde{c}_{ij} | \mathbf{x}_j, n_{1j}, n_{2j})$, or $\ln(b_{ij}) = \ln(\tilde{b}_{ij}) + \ln(u_j)$. Therefore, the distribution of log-bids for project j depends on $\mathbf{x}_j, u_j, n_{1j}$, and n_{2j} , with the log of the unobserved project heterogeneity acting as an additive mean shifter.

The distribution of firms' bid preparation costs, d_{ij} , is given by $G_d^{k(i)}(\cdot | \mathbf{z}_j)$. We assume that firms' bid preparation costs are independent conditional on observed and unobserved project characteristics, $\mathbf{x}_j, \mathbf{z}_j$, and u_j , and the number of potential bidders, N_{1j} and N_{2j} . The theoretical model implies that in the auction for project j firms' participation behavior is characterized by group-specific thresholds, $D_{kj}(\cdot)$, defined by equation (6). The bid preparation cost is private information. Therefore, from the researcher's and the competitors' point of view, the number of actual bidders from group k is distributed according to a binomial distribution with probability of success of $p_k(\mathbf{x}_j, u_j, \mathbf{z}_j, N_{1j}, N_{2j})$ and N_{kj} trials, where

$$(8) \quad p_k(\mathbf{x}_j, u_j, \mathbf{z}_j, N_{1j}, N_{2j}) = G_k(D_{kj}(\mathbf{x}_j, u_j, N_{1j}, N_{2j}) | \mathbf{z}_j).$$

In estimation, we make parametric assumptions about the distributions of interest because of the relatively small size of our dataset, exploiting instead the availability of a large number of covariates that potentially affect project and entry cost distributions.¹⁷ We assume that the log of the individual bid component $\ln(\tilde{b}_{ij})$ is normal with mean, $\mu_{F,kj}$, and variance, $\sigma_{F,kj}^2$, specified as:

$$(9) \quad \begin{aligned} E[\ln(\tilde{b}_{ij}) | \mathbf{x}_j, n_{1j}, n_{2j}] &= [\mathbf{x}_j, n_{1j}, n_{2j}]' \alpha_k \\ \text{Var}[\ln(\tilde{b}_{ij}) | \mathbf{x}_j, n_{1j}, n_{2j}] &= (\exp(\mathbf{y}_j' \eta_k))^2, \end{aligned}$$

¹⁷ Our parametric assumptions are motivated by prior literature (see for example Han Hong and Matthew Shum 2002, Robert H. Porter and J. Douglas Zona 1993, etc.), and by results in Krasnokutskaya (2011) that indicate that the distributions of the firm-specific bid component and of unobserved heterogeneity are close to log-normal.

where \mathbf{y}_j includes some of the project characteristics contained in \mathbf{x}_j . We further assume that $\ln(u_j)$ is distributed according to a normal distribution with mean zero and standard deviation σ_u .

Last, to ensure that entry costs are positive, we assume that they are distributed according to a normal distribution left-truncated at 0 with mean $E[d_{ij}|\mathbf{z}_j] = \mathbf{z}_j'\gamma_k$ and a constant, group-specific standard deviation σ_k^G .

B. Estimation Approach

Our empirical model yields predictions for equilibrium bids and group-specific participation probabilities. We match these to data using a generalized method of moments estimator. Here, we summarize the theoretical moment conditions that we use to estimate the parameters of the firm-specific bid component, unobserved heterogeneity, and entry cost distributions. The online Appendix contains a detailed derivation of the theoretical and empirical moment conditions we use.

To estimate the parameters of the mean of log-bids, $\ln(\tilde{b}_{ij})$, we exploit that:

$$(10) \quad m_1 = E[\mathbf{x}_j'(\ln(b_{ij}) - [\mathbf{x}_j, n_{1j}, n_{2j}]'\alpha_{k(i)})] = 0$$

$$m_2 = E[n_{kj}(\ln(b_{ij}) - [\mathbf{x}_j, n_{1j}, n_{2j}]'\alpha_{k(i)})]$$

$$= \int \int \sum_{n_1, n_2 \in N_1, N_2} n_{kj} \ln(u_j) \Pr(n_{1j}, n_{2j} | \mathbf{x}_j, \mathbf{z}_j, N_{1j}, N_{2j}, u_j) h(u_j) du_j dF(\mathbf{x}_j, \mathbf{z}_j, N_{1j}, N_{2j}).$$

The moment condition for the parameters that correspond to the numbers of bidders reflects the dependence of the joint distribution of (n_1, n_2) on u through $p_k(\mathbf{x}_j, u_j, \mathbf{z}_j, N_{1j}, N_{2j})$.

We identify the parameters of the standard deviation of $\ln(\tilde{b}_{ij})$, η_k , from the following second-order moments:

$$(11) \quad m_3 = E[(\ln(b_{ij}) - \ln(b_{i,j}))^2]$$

$$= E[(\exp(\mathbf{y}_j'\eta_{k(i_1)}))^2 + (\exp(\mathbf{y}_j'\eta_{k(i_2)}))^2] + E[(\mathbf{x}_j, n_{1j}, n_{2j}]'(\alpha_{k(i_1)} - \alpha_{k(i_2)})]^2]$$

$$m_4 = E[x_{jl}(\ln(b_{ij}) - \ln(b_{i,j}))^2]$$

$$= E[x_{jl}((\exp(\mathbf{y}_j'\eta_{k(i_1)}))^2 + (\exp(\mathbf{y}_j'\eta_{k(i_2)}))^2)] + E[x_{jl}([\mathbf{x}_j, n_{1j}, n_{2j}]'(\alpha_{k(i_1)} - \alpha_{k(i_2)}))^2].$$

Finally, the standard deviation of the distribution of unobserved project heterogeneity, σ_u , is estimated from a second-order moment condition:

$$(12) \quad m_5 = E[(\ln(b_{ij}) - [\mathbf{x}_j, n_{1j}, n_{2j}]'\alpha_{k(i)})^2] = \sigma_u^2 + E[(\exp(\mathbf{y}_j'\eta_k))^2].$$

In estimation, we also use moments of order three and four for the bid distribution.¹⁸ Their derivation is presented in the online Appendix.

¹⁸We experimented with moments of higher order as well. However, the estimates were not substantially affected by inclusion of these moments.

A second group of moments is used to recover parameters of the entry cost distributions, γ_k and σ_k^G . We use the first and the second moments of the binomial distribution for the numbers of actual bidders.¹⁹ We specifically consider separate moments for bidder groups, k , and project size categories, $size_j$, where $size_j = \{small, medium, large\}$:

$$\begin{aligned}
 (13) \quad m_6^{kl} &= E[n_{kj} | size_j = l] \\
 &= \int \int p_k(\mathbf{x}_j, \mathbf{z}_j, u_j, N_{1j}, N_{2j}) N_{kj} h(u) du dF(\mathbf{x}_j, \mathbf{z}_j, N_{1j}, N_{2j} | size_j = l) \\
 (14) \quad m_7^{kl} &= E[n_{kj}^2 | size_j = l] \\
 &= \int \int (p_k(\mathbf{x}_j, \mathbf{z}_j, u_j, N_{1j}, N_{2j})(1 - p_k(\mathbf{x}_j, \mathbf{z}_j, u_j, N_{1j}, N_{2j}))N_{kj} \\
 &\quad + N_{kj}^2 p_k^2(\mathbf{x}_j, \mathbf{z}_j, u_j, N_{1j}, N_{2j})) h(u) du dF(\mathbf{x}_j, \mathbf{z}_j, N_{1j}, N_{2j} | size_j = l).
 \end{aligned}$$

In computing the empirical counterparts to the moment conditions in equations (10) through (14), we use Monte Carlo simulation techniques to integrate over the distribution of unobserved heterogeneity. Our reliance on simulation techniques motivates our choice of a simulated GMM estimator over a simulated maximum likelihood estimator, which is highly nonlinear in participation probabilities and therefore more sensitive to simulation error in the at times small participation probabilities (see Daniel Akerberg et al. (2007) for a discussion of the advantages of simulated GMM in similar discrete-choice settings).

To compute the value of objective function for a given guess of parameter values we follow a number of steps. First, for every draw from the distribution of unobserved heterogeneity $h(u_j)$, we use the first-order conditions for optimal bidding to recover the project cost distributions implied by the bid distribution, F_b^k , consistent with the current parameter guess (see Guerre, Perrigne, and Vuong 2000).

Next, we numerically solve the equilibrium conditions on the participation side, equation (6), using a nonlinear equation solver to find the equilibrium entry probabilities. To compute the expected profit from bidding in equation (6), we use the recovered distribution of project costs to compute the expected profit for every possible combination of competitors ($\hat{n}_{k(ij)} - 1, \hat{n}_{-k(ij)}$), $\hat{n}_{k(ij)} = 0, 1, \dots, N_{k(ij)} - 1$ and $\hat{n}_{-k(ij)} = 0, 1, \dots, N_{-k(ij)}$. Then we combine these values into an expected profit from bidding using bidder i 's beliefs about the distribution of the numbers of his competitors. We obtain moment conditions by averaging over simulation draws as described in the online Appendix. We arrive at the value of objective function by collecting moment conditions into the GMM objective function.

¹⁹We estimated specifications that rely on various combinations of first, second, and higher-order moments for the distribution of the numbers of actual bidders. The latter are derived in the online Appendix. The results are very similar across the specifications. We report results for a specification that uses all first moments and second moments for the number of small bidders. We study the fit of the model based on moments not used in estimation.

C. Model Identification

We conclude this section with a brief discussion of the econometric identification of our parameters. While we rely on parametric assumptions for the bids, entry costs, and unobserved heterogeneity, these distributions can be identified from our data nonparametrically. Krasnokutskaya (2011) contains a detailed discussion of the nonparametric identification of the firm-specific cost component's distribution in the presence of unobserved project heterogeneity. The identification argument relies on the fact that conditional on the number of actual bidders, the firm-specific cost components are independent across bidders and from the unobserved heterogeneity component. This property holds for our participation model, as we show in the online Appendix. Using the procedure from Krasnokutskaya (2011), we can nonparametrically recover the marginal distributions of the firm-specific cost components and the distribution of unobserved heterogeneity conditional on the numbers of actual bidders. The marginal distribution of unobserved heterogeneity is then obtained by integrating the numbers of bidders, using the empirical distributions of the numbers of bidders in the data.

The distribution of entry costs is also identified nonparametrically. Details of the proof are in Krasnokutskaya (2009) and are summarized in the online Appendix. It can be shown that there is a unique cumulative distribution function G that could have generated the observed participation behavior under our model of entry. The proof relies on the existence of a full-support variable that affects the distribution of project costs, but not that of entry costs.

Parametric identification of G hinges on moment condition m_6 , which represents the average numbers of bidders by project size category and group. For each group, the moments trace the average number of bidders as a function of project size. The intercept of this profile identifies the constant of the distribution of entry costs; the slope identifies the coefficient for project size; and the curvature identifies the variance of the entry cost distribution.

IV. Empirical Analysis

This section presents results of our empirical analysis. We first summarize descriptive patterns in the data that speak to the presence of cost asymmetries across groups of bidders, the heterogeneity of projects in our dataset, and the strategic response of bidders to the bid preference program. We next implement our estimation strategy. We demonstrate that the predicted bid and entry choices based on our estimated parameters fit the data well, including for groups of projects not used in estimation. The estimated parameters of the entry cost distribution imply reasonable entry costs. The results confirm the presence of substantial asymmetries across bidder groups and important variation in the degree of asymmetries that correlates with project characteristics. Small bidders have higher project and entry costs for the majority of projects. However, we also identify a sizable set of projects where small bidders have lower project or entry costs or both.

A. Descriptive Analysis

Table 1 summarizes the characteristics of the set of state-funded projects that we use in estimation. Important project characteristics include the engineer's estimate

TABLE 1—SUMMARY STATISTICS, CALTRANS PROJECTS AND BIDDERS

	Mean	Standard deviation	10th percentile	Median	90th percentile
Engineer's estimate	615.416	738.560	165.250	464.130	1,086
Working days	96.598	165.071	20	45	180
Number of small plan holders	3.947	3.485	0	3	9
Number of large plan holders	6.574	4.324	3	5	11
Number of small bidders	1.745	1.890	0	1	4
Number of large bidders	2.623	1.597	1	3	5
Small projects (n = 229; median engineer's estimate = \$207,000)					
Number of small plan holders	4.886	3.656			
Number of large plan holders	5.904	3.501			
Number of small bidders	2.502	2.137			
Number of large bidders	2.349	1.652			
Medium projects (n = 235; median engineer's estimate = \$464,000)					
Number of small plan holders	4.260	3.536			
Number of large plan holders	6.723	3.922			
Number of small bidders	1.762	1.882			
Number of large bidders	2.668	1.561			
Large projects (n = 233; median engineer's estimate = \$787,186)					
Number of small plan holders	2.714	2.829			
Number of large plan holders	7.651	6.649			
Number of small bidders	0.954	1.219			
Number of large bidders	2.929	1.645			

Notes: 697 projects. Engineer's estimate reported in \$1,000s and duration in days. Small projects denote the bottom one-third, medium projects the middle one-third, and large projects the top one-third of engineer's estimates. Plan holders are our measure of potential entrants.

of the project's total cost, the type of work involved, the project's location at the level of the administrative district, and the time allocated to complete the project. The engineer's estimate reflects Caltrans' assessment of the project's price based on similar projects auctioned in the past. We follow other procurement auction studies (e.g., Hong and Shum 2002, Jofre-Bonet and Pesendorfer 2003, Porter and Zona 1993) in using it as a proxy for the size of the project.

We split projects into five work categories: bridge work; landscaping; road repair; signs, signals, and lighting; and small building work. Road-repair projects account for 60.26 percent of contracts; small building work accounts for another 15.93 percent of contracts, while 10.04 percent of contracts are for bridge work. The remaining contracts are split roughly equally between landscaping and signs/lighting work. Across projects, the median project has an engineer's estimate of \$464,000 (standard deviation of \$740,000) and duration of 45 working days (standard deviation of 165 days). Table 1 further highlights significant heterogeneity in the competitive environment. On average a project attracts four small potential bidders and 6.5 large potential bidders with 1.7 small and 2.6 large firms submitting bids.

The bottom panel of Table 1 summarizes potential and actual entry separately for small, medium, and large projects, representing the terciles of the distribution of the engineer's estimate. The small-firm participation rate declines sharply with project size. It drops from 51 percent of small potential bidders submitting bids in small projects to only 35 percent in large projects. In contrast, the participation rate of large firms is roughly constant across project sizes, ranging from 38 percent to 40 percent.

To investigate how participation rates vary with project characteristics, we conduct a probit analysis of a potential bidder's decision to submit a bid (see Table 2).

TABLE 2—DISCRETE CHOICE MODEL OF THE DECISION TO BID

	Coefficient	Standard error	Marginal effect
$\ln(\text{Engineer's estimate}) \times I(\text{Large})$	0.0563	0.0291	0.0223
Working days $\times I(\text{Large})$	-0.0300	0.0170	-0.0119
Number of large plan holders $\times I(\text{Large})$	-0.0537***	0.0136	-0.0213
Number of small plan holders $\times I(\text{Large})$	-0.0944***	0.0089	-0.0374
$\ln(\text{Engineer's estimate}) \times I(\text{Small})$	-0.1458***	0.0338	-0.0578
Working Days $\times I(\text{Small})$	0.0538***	0.0144	0.0213
Number of large plan holders $\times I(\text{Small})$	-0.0412***	0.0074	-0.0163
Number of small plan holders $\times I(\text{Small})$	-0.0783***	0.0081	-0.0310
Rural district \times road repair $\times I(\text{Small})$	-0.7594***	0.1488	-0.2724
Rural district \times other work $\times I(\text{Small})$	-0.6199***	0.1609	-0.2273
Urban district \times road repair $\times I(\text{Small})$	-0.8823***	0.1466	-0.3135
Urban district \times other work $\times I(\text{Small})$	-0.7030***	0.1619	-0.2554
Rural district \times road repair $\times I(\text{Large})$	0.2898*	0.1366	0.1152
Rural district \times other work $\times I(\text{Large})$	0.2282	0.1804	0.0909
Urban district \times road repair $\times I(\text{Large})$	0.2516	0.1490	0.1000
Urban district \times other work $\times I(\text{Large})$	0.2062	0.1605	0.0821
Observations	6,538		

Notes: Dependent variable: indicator of participation decision. Year and month effects included. Number of competing bidders included to control for unobserved project characteristics. Standard errors account for clustering at the project level. $I(\text{Large})$ indicates a large firm, $I(\text{Small})$ a small firm. Road repair includes bridge projects.

***Significant at the 1 percent level.

**Significant at the 5 percent level.

*Significant at the 10 percent level.

We include proxies for the competitive environment and project characteristics (size, time to completion, type of work, location) and allow the coefficients to differ for small and large plan holders. We control for unobserved project characteristics by including the number of actual bidders. We divide project locations into rural and urban based on the project's administrative district, defining a project to be rural if it is located in the North Coast, North Central, South Central, or Southern Sierra districts. We also combine bridge and road work into one group, relative to the remaining contracts.

The probit analysis reveals a negative, statistically significant effect of the number of potential competitors on a firm's participation decision. This is true for potential competitors of the same group as well as of the opposite group. The presence of an additional small potential bidder decreases both a small and a large firm's propensity to submit a bid by about twice the reduction brought forth by the presence of an additional large potential bidder, a statistically significant difference. This evidence is consistent with companies' strategic response to the bid preference program.

Table 2 also suggests heterogeneity in participation across locations and type of work. We include interaction variables of the project's location (urban or rural) and the project's type of work (road repair/bridge or other) and estimate differences between small and large firms' participation rates. Across project types, small firms have statistically significantly lower participation rates than large firms. The difference is more pronounced for urban projects, which are larger on average than rural projects, in line with the results in Table 1. Small firms are also less likely to participate in road-repair than in other projects, regardless of project location; however, the

TABLE 3—ORDINARY LEAST SQUARES MODEL OF SUBMITTED BID

	Coefficient	Standard error
Small-firm indicator	0.0813**	0.0357
ln(Engineer's estimate)	0.9571***	0.0127
Working days	0.0002***	0.0001
Number of small bidders	−0.0320***	0.0074
Number of large bidders	−0.0329***	0.0069
Number of small plan holders	0.0097**	0.0041
Number of large plan holders	0.0190***	0.0038

Notes: Observations: 3,034. Adjusted R^2 : 0.8996. Dependent variable: log of submitted bid. Controls for year, month, districts, and type of work by bidder group included. Standard errors account for clustering at the project level.

***Significant at the 1 percent level.

**Significant at the 5 percent level.

*Significant at the 10 percent level.

difference is statistically significant for urban projects only. Large firms, in contrast, exhibit less heterogeneity in participation choices, and we cannot reject the equality of participation rates across locations and types of work.

These regularities indicate that project size, location, and type of work affect entry in a group-specific way, potentially reflecting differences in the cost of completing a particular project or the cost of preparing bid documents. To investigate the former, we conduct a regression analysis that relates log-bid levels to project characteristics.²⁰ Table 3 summarizes the results. The estimated coefficients have the expected signs. We find that log-bids increase in the engineer's estimate and the project's duration.²¹ In addition, we find significant variation in bid levels across work types and locations, even after controlling for project size. Conditional on project characteristics, the average bid of a small bidder is 8.1 percent higher than that of a large bidder.

In summary, the descriptive evidence suggests that bidding and entry behavior differ by firm group. We find that the number of small potential bidders affects participation decisions of both groups of bidders more strongly than the number of large potential bidders. This suggests that the Small Business Preference program affects the operation of this market. At the same time, small firms submit bids significantly less frequently and, if they do, bid higher than large firms. Such participation and bidding behavior could arise due to large differences in project costs between small and large firms even if the costs of preparing bids are similar across groups. On the other hand, even without pronounced differences in project costs, small firms' bids may be higher due to the competitive advantage awarded by the preference program, while their less frequent entry is due to larger bid preparation costs.

We now turn to the results of the estimated empirical model that allows us to disentangle the role of the preference program from inherent cost differences between firms, both of which are reflected in the observed firm choices.

²⁰We include the numbers of potential bidders to control for unobserved project heterogeneity.

²¹In separate regression models (available upon request), we investigate the role of capacity constraints in explaining firm behavior, which would introduce a dynamic element to the firms' decision making. We follow Jofre-Bonet and Pesendorfer (2003) in computing a measure of backlog at the time of each bidding decision but do not find a statistically significant relationship between the capacity measure and firms' participation decisions or bids. The short time dimension of our data, which is likely to render our measure of capacity utilization imprecise, makes it difficult to interpret these findings.

B. Estimation Results

We specify the mean of log bids as a linear function of the log of the engineer's estimate, duration, the numbers of actual and potential bidders and dummies for type of work and location. We also include year dummies to control for cost inflation and monthly dummies to control for seasonal fluctuations in input prices. We allow the effects of most of these covariates to differ by bidder group. The variance of log-bids depends on the log of the engineer's estimate and the bidder's group. We assume that mean entry costs are a linear, group-specific function of the log-engineer's estimate and allow for a group-specific standard deviation.²²

The results of estimation indicate that there are important differences in project and entry costs across groups of bidders. Table 4 reports the estimated coefficients of the bid distribution. The estimated coefficients are of the expected sign and magnitude. They reflect substantial variation in the means and variances of log-bids across types of work and locations. They also imply substantial differences in log-bids across bidder groups. We estimate that a small firm submits a bid that is, on average, 5.4 percent higher than a large firm's bid for the same project. We find that the variance of the underlying log-normal distribution of bids (which equals $(\exp \sigma_F^2 - 1) \exp(2\mu_F + \sigma_F^2)$) increases in the engineer's estimate and is lower for small bidders. Unobserved project heterogeneity is important in our data. Increasing the unobserved project characteristic from a value of zero to a value equal to the estimated standard deviation of 0.17 has an effect on mean bids that is equivalent to a 20 percent increase in the engineer's estimate. The estimated bid distributions fit the data well; see Figure A-4 in the online Appendix for more detail.

We use Guerre, Perrigne, and Vuong (2000)'s methodology to recover the distribution of project costs from the distribution of bids. First, we use the first-order conditions from the firms' bidding problem to estimate inverse bid functions. Strict monotonicity of bid and inverse bid functions allows us to combine the estimated distribution of bids and inverse bid functions to obtain an estimate of the distribution of project costs. We summarize the estimated distributions of project costs in Table 5, where we report means and variances of project cost distributions as a fraction of the engineer's estimate for categories of projects defined by size, type of work, and location. Table 5 shows that mean project costs are close to the engineer's estimate. It also highlights important differences in means and variances of cost distributions across groups of bidders. We test for the statistical significance of these differences next.

We analyze differences in project costs across groups of bidders using a parametric bootstrap technique to test the hypothesis of the equality of the two groups' means (standard deviations) of their project cost distributions against two-sided and one-sided alternatives. Test results differ across projects. For some projects we cannot reject equality of means or standard deviations, whereas for other projects we

²² We also estimated several alternative specifications. First, we estimated a specification where the unobserved project heterogeneity depends on the number of potential bidders. The coefficients for the numbers of potential bidders in the standard deviation of unobserved heterogeneity are not statistically significant; the remaining coefficients are qualitatively similar to our base specification. Second, we estimated specifications that include as additional entry cost shifters a project's number of individual tasks and nonlinear size effects. These variables do not have statistically significant effects on mean entry costs.

TABLE 4—ESTIMATED PARAMETERS OF LOG-NORMAL DISTRIBUTION OF BIDS

	Coefficient	Standard error
Constant	0.0762	0.0189
I(Small)	0.0536	0.0184
ln(Engineer's estimate)	0.9274	0.0034
Working days	5.36E-05	8.89E-06
Number of small bidders	-0.0412	0.0113
Number of large bidders	-0.0386	0.0087
Number of small plan holders	-6.88E-05	0.0051
Number of large plan holders	0.0249	0.0195
Type of work		
Bridge	-0.1244	0.0039
Landscaping	-0.0406	0.0046
Road repair	-0.0630	0.0089
Signs, signals, lighting	0.0170	0.0064
Location of work		
Central Coast	0.0098	0.0045
East Central	0.1250	0.0042
Los Angeles	0.0543	0.0054
North Central	0.1387	0.0056
North Coast	0.0805	0.0052
Northern Sierras	0.1451	0.0051
San Bernardino	0.0491	0.0039
San Diego	-0.0241	0.0057
San Francisco	0.0349	0.0037
South Central	0.1432	0.0075
Southern Sierras	0.0320	0.0080
North Central \times Small	-0.0730	0.0037
North Coast \times Small	-0.0484	0.0053
South Central \times Small	-0.0718	0.0072
Southern Sierras \times Small	-0.0643	0.0076
Standard deviation of log-bids		
Constant	-1.6814	0.0438
I(Small)	-0.0999	0.0180
Engineer's estimate	-0.0550	0.0183
Standard deviation of unobserved project characteristic, σ_u	0.1684	0.0107

Notes: Specification includes year and month effects by bidder type. Log-bids and the log of the unobserved project heterogeneity are assumed to be normally distributed. Standard deviation of log-bids estimated as $\sigma = \exp(b_0 + b_1 I(\text{Small}) + b_2 \text{Engineer's estimate})$ where $I(\text{Small})$ indicates a small firm.

TABLE 5—ESTIMATED PROJECT COSTS BY PROJECT TYPE

Project type	Project count	Mean		Standard deviation	
		Small bidder	Large bidder	Small bidder	Large bidder
Small, rural, road repair/bridge	50	1.0245	1.0342	0.2341	0.2432
Medium, rural, road repair/bridge	59	0.9491	0.9660	0.2032	0.2122
Large, rural, road repair/bridge	55	0.9658	0.9739	0.2146	0.2227
Small, urban, road repair/bridge	73	1.0503	1.0182	0.2247	0.2387
Medium, urban, road repair/bridge	89	1.0152	0.9816	0.1905	0.2034
Large, urban, road repair/bridge	88	0.9764	0.9602	0.1882	0.2024
Small, rural, other work	39	1.0505	1.0624	0.2269	0.2407
Medium, rural, other work	13	0.9952	0.9798	0.1822	0.2043
Large, rural, other work	9	0.9559	0.9515	0.1572	0.1676
Small, urban, other work	55	1.1329	1.0914	0.2289	0.2452
Medium, urban, other work	51	1.0616	1.0303	0.2136	0.2272
Large, urban, other work	35	1.0556	1.0268	0.2079	0.2228

Notes: Means and standard deviations of project costs are averaged across projects of within project type and scaled by the engineer's estimate before averaging.

TABLE 6—SUMMARY OF TESTS OF EQUALITY OF MEANS OF COST DISTRIBUTIONS BY PROJECT TYPE

Project type	Project count	H_1 : small > large		H_1 : small < large		Conclusion
		Number of rejections	Percent rejections	Number of rejections	Percent rejections	
Small, rural, road repair	50	16	0.32	31	0.62	small < large
Medium, rural, road repair	59	19	0.32	36	0.61	small < large
Large, rural, road repair	55	20	0.36	29	0.53	small < large
Small, urban, road repair	73	52	0.71	13	0.18	small > large
Medium, urban, road repair	89	64	0.72	18	0.20	small > large
Large, urban, road repair	88	50	0.57	27	0.31	small > large
Small, rural, other work	39	11	0.28	26	0.63	small < large
Medium, rural, other work	12	4	0.31	5	0.39	small > large
Large, rural, other work	9	4	0.44	4	0.44	small > large
Small, urban, other work	55	44	0.80	7	0.13	small > large
Medium, urban, other work	51	38	0.75	10	0.20	small > large
Large, urban, other work	35	23	0.66	3	0.09	small > large

Notes: Columns 2 and 4 contain the count of projects for which we reject with 95 percent confidence the null hypothesis of equality of mean costs against the stated alternatives. Columns 3 and 5 report the fraction of projects in a given category for which the null hypothesis is rejected in favor of stated alternative. Similar tests for the difference in the estimated standard deviations yield rejections of the null hypothesis in favor of the standard deviation of small-firm costs being smaller than that of large-firm costs for more than 75 percent of projects in every category. Road repair includes bridge work.

reject equality in favor of either group's having a lower mean (or standard deviation). We aggregate the test results to the level of the project category (defined in Table 5) to document how cost differences between small and large bidders vary with project characteristics. In particular, for every project category, we compute the fraction of projects for which equality is rejected in the favor of two-sided or one of the one-sided alternatives. See Table 6.

We find that with a two-sided alternative we reject the equality of means (and standard deviations) across bidder groups for most projects in our dataset. We, therefore, do not report the results of this test in the table. The tests with one-sided hypotheses are more interesting. We can reject an equality of means of the project cost distributions in favor of small bidders having a higher mean than large bidders for the majority of projects in most categories. For rural road work and small rural other work, however, we more frequently reject the null of equal means in favor of small bidders having lower mean project costs than large bidders. We also reject the null of equal standard deviations in favor of small bidders having lower standard deviations than large bidders for most projects in our dataset. There are thus important project cost differences between small and large firms. However, small firms are not always weaker players in the market. With several exceptions,²³ empirical auction studies rely on the assumption of symmetric bidders. Here, we document significant, and at times unexpected, differences between bidder groups. Such cost differences are important in our application since the use of discrimination is most effective in environments with asymmetric bidders.

Next, we turn to the estimated coefficients for the cost of entry distribution reported in Table 7. All coefficients have the expected signs and are statistically significantly different from zero. We have also estimated specifications that include conditional

²³For example, John Asker (2010), Athey, Levin, and Seira (2011), Bajari (2001), and Jofre-Bonet and Pesendorfer (2003).

TABLE 7—ESTIMATED PARAMETERS OF TRUNCATED NORMAL DISTRIBUTION OF ENTRY COSTS

	Coefficient	Standard error
I(Small)	−0.6863	0.0116
(ln(Eng. estimate)) × I(Small)	0.4818	0.0111
I(Large)	−0.5589	0.1166
(ln(Eng. estimate)) × I(Large)	0.3788	0.0435
Standard deviation of entry costs		
I(Small)	0.1373	0.0042
I(Large)	0.1679	0.0097

Notes: The estimated specification allows for unobserved heterogeneity in the bid distribution; the estimated parameters are recorded in Table 4. I(Large) indicates a large firm; I(Small) a small firm.

TABLE 8—MODEL FIT: ENTRY PREDICTIONS BY PROJECT TYPE

		Small firms		Large firms	
	Number of projects	Predicted	Actual	Predicted	Actual
<i>Moment conditions: number of bidders</i>					
Small projects	229	2.5199	2.5616	2.3140	2.3877
Medium projects	235	1.9451	1.8962	2.6781	2.6766
Large projects	233	1.2598	1.2222	2.9008	2.8528
<i>Moments conditions not used in estimation: number of bidders</i>					
Bridge projects	70	2.1046	2.0714	2.5269	2.9286
Road-repair projects	420	1.6739	1.5578	2.7271	2.8565
Small and road-repair projects	258	2.5095	2.2844	2.0533	2.3527
Medium and road-repair projects	439	1.6145	1.7215	2.9769	2.8115
Large and road-repair projects	107	2.1737	2.0612	2.4518	2.6321
Rural projects	143	1.7948	1.6167	2.7744	2.9091
Urban projects	170	1.1778	1.1172	2.8597	2.9527
<i>Second-order moment conditions</i>					
Small projects	229			1.6195	1.7164
Medium projects	235			1.9341	1.7500
Large projects	233			1.7478	1.6997

Notes: The second moments compare the expectation of the number of small and large bidders squared as predicted by the model to the sample equivalent.

moments based on the type of work and location in addition to size classes. We use these additional moments to perform a test of overidentifying restrictions. The overidentifying restrictions could not be rejected on the basis of our estimates, and the estimated parameters vary little across specifications.

Table 8 reports the fit for our base specification. The top panel shows the fit for the moments that we use in the estimation. The lower panel reports average and predicted numbers of actual bidders for other project groupings that were not used to form moment conditions in estimation. While the literature has not established a benchmark for assessing the fit of the entry part of our model, our fit appears to be good.

Table 9 reports the implied mean cost of entry and mean cost as a fraction of the engineer's estimate across bidder groups and project size categories. We estimate that mean entry costs amount to 2.2 percent to 3.9 percent of the engineer's estimate. This ratio increases with project size for small bidders but decreases in size for large bidders. Our estimates are comparable to estimates obtained in the academic

TABLE 9—ESTIMATED ENTRY COSTS BY PROJECT SIZE

Project size	Small firms			Large firms			K-S test (<i>p</i> -value)
	Mean cost	Standard deviation of cost	Cost/ engineer's estimate	Mean cost	Standard deviation of cost	Cost/ engineer's estimate	
Small	4.495	4.146	0.022	6.905	6.156	0.033	0.210 (0.000)
Medium	13.129	9.270	0.028	14.216	10.514	0.031	0.053 (0.109)
Large	29.503	13.046	0.039	24.215	14.017	0.032	0.231 (0.000)

Notes: Costs reported in \$1,000s. The K-S test reports the test statistic and corresponding *p*-value of a Kolmogorov-Smirnov test of the equality of the estimated cost distributions within each size category.

literature (Bajari, Hong, and Stephen Ryan 2010) and suggested magnitudes from general construction manuals.²⁴ We also test the equality of the two groups' cost of entry distributions. We reject equality for all but one project size category. The results of the test are reported in the last column of Table 9.

V. Counterfactual Analysis

We use the estimation results to assess the effect of the preferential treatment of small firms on participation, the cost to the government, and the probability that a project is awarded to a small firm. After a brief overview of the counterfactual approach, we first contrast the outcomes of a preference auction under endogenous and fixed participation under a range of discount values. This allows us to investigate whether a bid discount could serve as an effective tool to lower the government's cost of procurement or to achieve California's allocative goal. Due to the computational cost of numerically deriving equilibrium bidding strategies, we do so for select representative projects only. We then study the current program as a detailed example of policy effects at a relatively low discount level, before considering an entry tax or subsidy as a preferential treatment mechanism that targets the participation margin directly.

To compare behavior in alternative environments, we need to derive the appropriate bidding strategies that solve the system of differential equations defined by the first-order conditions in equation (2). Except for special cases, this system of differential equations does not have a closed-form solution and has to be solved numerically. We apply and extend the method proposed by Robert C. Marshall et al. (1994) to our setting.²⁵

²⁴Daniel Halpin (2005) and others suggest that estimating costs (cost of time and effort expended to develop a total bid price and submit a proposal) typically range between 0.25 percent and 2 percent of the total project cost but vary widely depending on the complexity, type of job, and type of work being estimated.

²⁵Bajari (2001) and Marshall et al. (1994) provide details on numerical solution algorithms for asymmetric auctions. Marshall et al. (1994) use polynomial approximations to the cost distributions and employ a forward recursive algorithm to solve the resulting set of difference equations with an upper boundary condition. We extend their approach as follows. We embed the recursive algorithm in a search routine for a starting point that satisfies the upper boundary conditions. We approximate the estimated cost distributions by polynomial splines, which we found to produce more stable results than the original Taylor approximations. Finally, we extend their setup in which a single asymmetric bidder competes against a second group of bidders to settings with arbitrary numbers of bidders within the two groups, which entails solving a larger-dimensional system of differential equations. As in estimation, we use Monte Carlo simulation to integrate over the distribution of unobserved heterogeneity.

As a performance check, we initially compare the simulated entry probabilities for the 5 percent discount level to the entry probabilities implied by our estimation routine. The estimation routine computes expected profits conditional on participation using the observed bid distributions directly (see Guerre, Perrigne, and Vuong 2000), thus avoiding the simulation step. The simulation routine produces entry probabilities that match closely the ones used in estimation. Table A-1 in the online Appendix contains a detailed comparison by project category.

A. The Role of Participation

We use the numerical routine to simulate auction outcomes under a large set of discount values for five typical projects that vary in small and large firms' relative project and entry costs. We consider two scenarios; in (i) we hold participation fixed at the zero discount level, and in (ii) we allow participation to adjust with the discount level. Figure 2 illustrates for two most typical (yet very dissimilar) types of projects the changes that participation adjustments introduce into the relationship between the discount and auction outcomes, such as the cost of procurement (or the expected winning bid), the small-firm probability of winning, and the expected numbers of bidders. Both the probability of small-firm award and the cost of procurement have flatter profiles under fixed than under endogenous participation. The fixed participation case isolates the response of bidding strategies to alternative discount levels. With endogenous entry, the bid response is enhanced through a decline in large-firm and an increase in small-firm participation associated with increasing discounts to small firms. Hence, the probability of small-firm award rises not only because a given small bidder's probability of winning increases, but also because the proportion of small participants increases.²⁶ In turn, the cost of procurement increases as a higher proportion of contracts is awarded to small bidders who charge higher prices due to their high costs and the bid discount. The fixed and endogenous participation scenarios also differ in their implications for the discount levels needed to achieve procurement cost minimization or an allocative goal such as California's.

As shown in Figure 2, the implications of accounting for endogenous participation are quite different for the two projects because they are characterized by different degrees of asymmetry between small and large bidders. Project 2 belongs to a group of projects where small firms' project and entry costs are very similar to the costs of large bidders. In addition, in these projects the variances of the project costs distributions tend to be lower than for the average project. As a result, a nonnegligible share of large bidders is priced out of the auction and chooses not to bid once they observe their project cost. This effect, which is significant for this group of projects, largely mimics the participation adjustment effect. As a result, the relationships under fixed and endogenous participation are similar. Most small projects, and medium rural road work projects, share these properties.

In contrast, project 1 is exemplary of medium and large urban projects where small firms are the less efficient group in both entry and project costs. Because of

²⁶Note that in our counterfactuals, we hold the pool of potential entrants fixed. These results thus do not reflect that the discount may change the incentive of a firm of either group to become a potential bidder, which is likely to reinforce the latter effect.

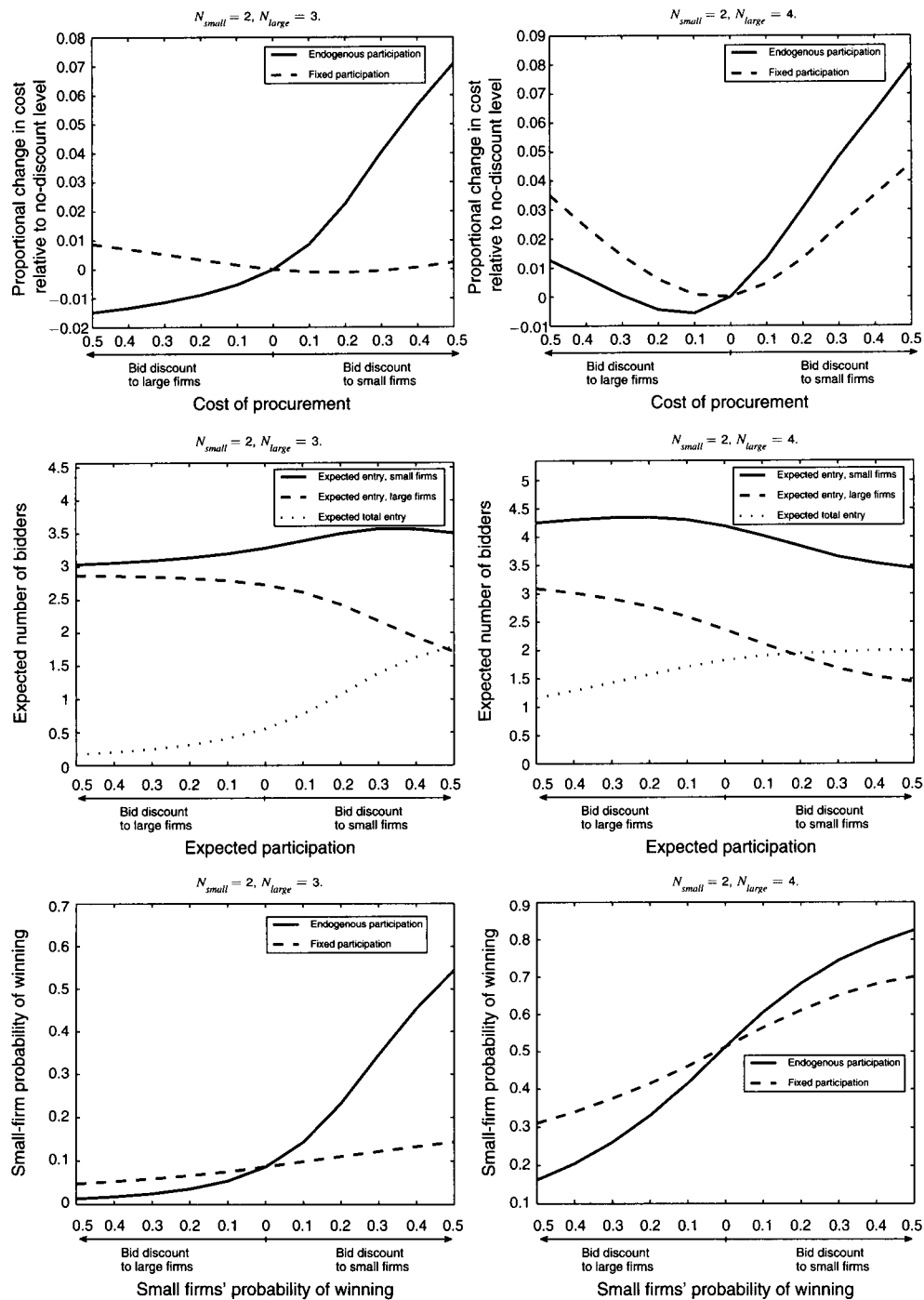


FIGURE 2. EXPECTED COST AND ENTRY UNDER ALTERNATIVE BID DISCOUNTS, SAMPLE PROJECTS

substantial asymmetry there is unlikely to be a significant mass of large bidders whose bid is beaten by all, including the highest-cost, small bidders. That is why the share of large bidders dropping out after observing their project costs is much smaller than in the case of project 2. This implies that under fixed participation the group of viable bidders does not change very much as the discount level changes.

TABLE 10—BID PREFERENCE PROGRAM DESIGNS UNDER ALTERNATIVE OBJECTIVES, SAMPLE PROJECTS

	Project				
	1	2	3	4	5
(N_{sm}, N_{lg})	(2, 3)	(2, 4)	(2, 4)	(2, 4)	(2, 5)
Project cost difference: $\bar{c}_{sm} - \bar{c}_{lg}$	0.50	-0.1	-0.57	0.90	0.30
Entry cost difference: $\bar{d}_{sm} - \bar{d}_{lg}$	0.05	-0.08	0.12	0.10	0.06
Cost to the government, $\delta_{lg} = \delta_{sm} = 0$	4.75	1.41	9.77	8.61	5.90
<i>Cost-minimizing policy</i>					
(i) Endogenous entry					
$(\delta_{lg}^E, \delta_{sm}^E)$ (percent)	(50, 0)	(10, 0)	(0, 0)	(50, 0)	(50, 0)
Change in government cost (percent)	-2.19	-0.52	0.00	-0.15	-1.28
(ii) Entry fixed at $\delta = 0$ -levels					
$(\delta_{lg}^F, \delta_{sm}^F)$ (percent)	(0, 20)	(5, 0)	(5, 0)	(0, 15)	(0, 10)
Change in government cost under fixed entry (percent)	-0.11	-0.04	-0.02	-0.03	-0.18
Change in government cost under endogenous entry at δ^F (percent)	3.22	0.56	0.05	0.41	1.08
<i>Policy targeting 25 percent small-firm award rate</i>					
(i) Endogenous entry					
$(\delta_{lg}^E, \delta_{sm}^E)$ (percent)	(0, 20)	(0, 0)	(0, 0)	(0, 45)	(0, 10)
Change in government cost (percent)	3.22	0.00	0.00	2.44	1.08
(ii) Entry fixed at $\delta = 0$ -levels					
$(\delta_{lg}^F, \delta_{sm}^F)$ (percent)	(0, 50)	(0, 0)	(0, 0)	(0, 75)	(0, 50)
Change in government cost under fixed entry (percent)	0.23	0.00	0.00	1.05	0.55
Change in government cost under endogenous entry at δ^F (percent)	7.82	0.00	0.00	13.180	8.34

Notes: Costs reported in \$100,000s. Change in government cost computed relative to cost under $\delta_{lg} = \delta_{sm} = 0$. The change in government cost with endogenous entry in the fixed-participation panels measured the cost change that results from using δ chosen under fixed entry, but allowing participation to respond to the discount. Project 1 is in the category of medium urban road-repair work, project 2 in small rural road-repair work, 3 in large urban road-repair work, 4 in large urban other work, and 5 in medium rural road-repair work.

B. Cost-Minimizing Discount

We use the five projects to explore the potential of a bid discount to lower the cost of procurement. Table 10 shows that discounts of 5 percent to large bidders for projects 2 and 3 minimize government cost under fixed participation since large bidders are less efficient for these projects. The model with fixed participation prescribes 20 percent, 20 percent and 10 percent discounts to small bidders for projects 1, 4, and 5 where small firms have higher project costs. In contrast, the cost-minimizing policy that takes participation adjustments into account does not generally favor the group with the highest project costs, but reflects entry cost differences as well. It implies that very high discounts should be given to large firms (which would induce small firms not to participate) on projects 1, 4, and 5; that a 10 percent discount should be given to large firms on project 2; and that no discount should be awarded to either firm group on project 3. It is worth noting that if the government followed the prescriptions of the fixed-participation model, the cost of procurement would actually increase rather than decrease in four out of the five cases after participation adjusts.

Under the model with participation adjustment the program affects not only bidding behavior but also the composition of bidders. The bid preference generates the highest cost savings to the government for projects 1 and 4 where small firms' project and entry costs are much higher than the corresponding costs of large firms.

In these projects large firms impose substantial competitive pressure on the market. In response to a bid discount, the equilibrium participation of large bidders grows, and this competitive pressure intensifies, even though the equilibrium participation of small bidders declines at the same time. This holds for all large-firm participation levels that arise in equilibrium under a large-firm bid discount, regardless of the magnitude of the discount. The reverse is true if a discount is granted to small firms: the associated decline in large-firm equilibrium participation adversely affects the competitive intensity despite the increased presence of small firms. It is therefore optimal for the government to use the discount to encourage entry by large bidders (see the online Appendix for details on the optimal policy for these projects).

C. Other Discount Levels

Most preference programs pursue goals other than pure cost minimization and therefore are likely to produce procurement cost increases. As Figure 2 indicates, such increases can be quite large, ranging for both projects from 1 percent for discounts as low as 10 percent to as much as 7 percent with higher discounts of 40 percent.

We assess the likely magnitudes of cost increases associated with the preference program's objectives using the allocative goal of the California Small Business Preference program as an example. The second panel of Table 10 reports the discount rates necessary to achieve this goal and the associated cost increases for the five projects discussed earlier. The resulting cost increases range from 0 percent to 3.2 percent, with the largest increases being associated with projects where small bidders are substantially less efficient than large bidders (in either project or entry costs). Significantly, the fixed participation model suggests that a much higher (by a factor of two) discount level should be used. Choosing this discount level without recognizing the changed participation incentives is costly: procurement costs rise by approximately 7.8 percent to 13 percent across projects.

Given the heterogeneity of cost asymmetries across projects in the data, we also compute an aggregate measure of the cost of allocating 25 percent of the state's procurement load to small firms. We find that a 15 percent discount approximately satisfies the aggregate award goal (see Table 11). This results in an approximate increase of 1.4 percent in the cost of procurement relative to no government intervention.²⁷ In contrast, if we held participation fixed, we would conclude that a much higher discount of 45 percent is needed to achieve the allocative goal. The model with fixed participation substantially underestimates the cost increase associated with this discount level predicting that the cost would go up by only 1.43 percent. This assessment ignores participation effects, which would bring the cost increase to 6.6 percent.

The modest aggregate cost increase for discount levels prescribed by the endogenous participation model reflects the composition of projects in the data, which

²⁷ We find δ that sets, across projects j , $\sum_j p_{sm,j}^{win}(\delta) GovCost_j = 0.25 \sum_j GovCost_j$, where $p_{sm,j}^{win}$ denotes the small-firm probability of winning auction j . We approximate the probability of winning for each individual project by the equivalent for a representative project in its project category (for project categories, see Table 12). We similarly approximate the cost of procurement for a given project by the cost for the representative project.

TABLE 11—EFFECT OF DISCOUNT LEVEL ON AGGREGATE PROCUREMENT COST AND ALLOCATION OF WORK TO SMALL FIRMS

$(\delta_{lg}, \delta_{sm})$ (percent)	Aggregate cost to government	Small firms' percent of work
(25, 0)	0.995	3.3
(15, 0)	0.996	4.9
(10, 0)	0.997	7.6
(5, 0)	0.998	10.5
(0, 0)	1.000	12.5
(0, 5)	1.005	15.6
(0, 10)	1.008	20.4
(0, 15)	1.021	31.9
(0, 25)	1.041	44.4

Note: Cost to the government reported as a percent of the cost under no government intervention.

contain a significant share of projects where small and large firms have similar costs, as in project 2. In these projects small firms are efficient competitors and have a high award rate even in the absence of a discount. It seems that the government could reduce its cost of procurement even further by granting discounts only for projects where small bidders are typically inefficient and thus have low participation and award rates.

D. Evaluation of Current Policy

Next we turn to an analysis of the bid preference program currently in place in California, which uses a relatively low discount of 5 percent. We compare auction outcomes in the current environment to the counterfactual setting where the state does not use a preference program and instead treats bidders equally. Tables 12 and 13 contain the results of this analysis. We simulate auction outcomes for a larger subset of 119 projects to capture project heterogeneity more finely based on project size, location, and type of work.²⁸

Table 12 reports changes in the cost to the government measured as an expected winning bid. The cost to the government does not change very much as a result of the preferential treatment of small bidders. While the cost to the government goes up in some cases and goes down in others, these effects barely amount to a 0.5 percent change for many project categories as well as for most individual projects. At the same time, the change is between 1 percent and 2 percent in three out of 11 categories.

Table 13 compares probabilities of entry by project category. The preferential treatment produces the expected increased small-firm and reduced large-firm participation. The magnitudes of these effects are economically significant, however, and differ substantially across project categories. Small-firm entry probabilities increase by between 2 and 7 percentage points, or 2.7 percent and 21 percent, while large-firm entry probabilities decline by between 3 and 5 percentage points, or 4.4 percent and 9.9 percent. The changes in the groups' participation are close to offsetting, however: total entry is virtually unchanged across project categories, with increases or decreases in overall participation of only approximately 1 percent.

²⁸Ten projects in each category and all nine projects for large rural other work projects.

TABLE 12—COUNTERFACTUAL ANALYSIS OF PREFERENCE PROGRAM:
COMPARISON OF PROFIT AND GOVERNMENT COST BY PROJECT TYPE

Project type	$\delta_{sm} = 0$			Average change (percent) $\delta_{sm} = 0 \rightarrow 0.05$		
	$E[\Pi_{sm}]$	$E[\Pi_{lg}]$	$E[\text{win bid}]$	$E[\Pi_{sm}]$	$E[\Pi_{lg}]$	$E[\text{win bid}]$
Small, rural, road repair/bridge	0.082	0.085	5.004	11.258	-7.831	-0.915
Medium, rural, road repair/bridge	0.173	0.175	12.095	11.603	-9.527	-0.285
Large, rural, road repair/bridge	0.257	0.341	13.399	15.752	-7.301	2.357
Small, urban, road repair/bridge	0.063	0.094	5.800	9.858	-6.822	-0.430
Medium, urban, road repair/bridge	0.078	0.190	9.819	10.482	-5.560	0.966
Large, urban, road repair/bridge	0.280	0.337	14.926	14.685	-6.475	1.409
Small, rural, other work	0.049	0.053	6.460	4.499	-11.499	0.602
Medium, rural, other work	0.127	0.112	13.026	6.230	-10.065	-0.104
Small, urban, other work	0.044	0.138	6.140	6.595	-7.805	1.155
Medium, urban, other work	0.130	0.164	13.930	13.354	-6.389	0.387
Large, urban, other work	0.239	0.506	15.485	10.072	-9.560	1.620

Notes: $E[\Pi_{sm}]$ ($E[\Pi_{lg}]$) denote small (large) firms' expected profits. $E[\text{win bid}]$ denotes the expected winning bid, which measures the expected cost of procurement to the government. Expected profits and winning bid in \$100,000s.

TABLE 13—COUNTERFACTUAL ANALYSIS OF PREFERENCE PROGRAM:
COMPARISON OF PREDICTED ENTRY BY PROJECT TYPE

Project type	$\delta_{sm} = 0$				
	Entry probability		Actual bidders		
	p_{sm}	p_{lg}	n_{sm}	n_{lg}	n_t
<i>Panel A. Entry in the absence of bid discount</i>					
Small, rural, road repair	0.764	0.645	2.255	2.406	4.660
Medium, rural, road repair	0.600	0.602	2.169	2.574	4.744
Large, rural, road repair	0.513	0.749	1.036	3.055	4.091
Small, urban, road repair	0.596	0.671	1.961	2.918	4.879
Medium, urban, road repair	0.353	0.667	1.649	3.197	4.846
Large, urban, road repair	0.488	0.737	1.171	3.058	4.229
Small, rural, other work	0.608	0.498	5.270	1.626	6.896
Medium, rural, other work	0.530	0.458	4.608	2.499	7.107
Small, urban, other work	0.530	0.632	2.963	2.416	5.379
Medium, urban, other work	0.482	0.605	1.783	3.490	5.272
Large, urban, other work	0.387	0.875	1.522	2.538	4.059
Average change $\delta_{sm} = 0 \rightarrow 0.05$					
	Δp_{sm}	Δp_{lg}	$\% \Delta p_{sm}$	$\% \Delta p_{lg}$	$\% \Delta n_t$
<i>Panel B. Entry response to introduction of 5 percent bid discount</i>					
Small, rural, road repair	0.030	-0.030	4.175	-5.422	-0.539
Medium, rural, road repair	0.057	-0.045	9.892	-8.982	-0.320
Large, rural, road repair	0.072	-0.037	20.971	-6.446	-0.142
Small, urban, road repair	0.027	-0.028	4.461	-4.408	-0.133
Medium, urban, road repair	0.037	-0.026	10.294	-4.635	0.620
Large, urban, road repair	0.062	-0.037	13.861	-5.884	-0.101
Small, rural, other work	0.017	-0.044	2.893	-9.723	0.192
Medium, rural, other work	0.027	-0.040	6.002	-9.870	0.746
Small, urban, other work	0.016	-0.026	2.684	-5.059	0.043
Medium, urban, other work	0.051	-0.032	11.594	-5.855	0.385
Large, urban, other work	0.027	-0.031	9.338	-3.832	0.967

Notes: p_{sm} (p_{lg}) denote small (large) firms' entry probabilities. n_{sm} , n_{lg} , and n_t denote the expected number of small, large, and total bidders, respectively. Δ denotes absolute changes in going from $\delta_{sm} = 0$ to $\delta_{sm} = 0.05$, while $\% \Delta$ denotes percentage changes. Road repair includes bridge work.

TABLE 14—COUNTERFACTUAL ANALYSIS OF PREFERENCE PROGRAM:
CHANGE IN SMALL-FIRM AWARD RATES BY PROJECT TYPE

	Average change $\delta_{sm} = 0 \rightarrow 0.05$	
	Fixed entry	Endog. entry
Small, rural, road repair/bridge	0.0237	0.0482
Medium, rural, road repair/bridge	0.0223	0.0625
Large, rural, road repair/bridge	0.0166	0.0581
Small, urban, road repair/bridge	0.0185	0.0386
Medium, urban, road repair/bridge	0.0145	0.0424
Large, urban, road repair/bridge	0.0149	0.0460
Small, rural, other work	0.0188	0.0421
Medium, rural, other work	0.0193	0.0512
Small, urban, other work	0.0181	0.0402
Medium, urban, other work	0.0182	0.0538
Large, urban, other work	0.0146	0.0372

Notes: Column 2 shows the average percentage point change in the small-firm probability of winning when entry is held fixed at the level under $\delta_{sm} = 0$. Column 3 shows percentage point changes when entry is allowed to adjust to the bid discount.

The participation effects contribute significantly to the increase in small firms' probabilities of winning. As Table 14 shows, the change in probability of winning under endogenous participation is twice the change generated by the discount only (under fixed participation). Finally, the program also increases small potential bidder's expected profit prior to participating by 5 percent to 16 percent, with an average of 10.4 percent, while decreasing large firms' profits by 5 percent to 12 percent, with an average of 8 percent (see Table 12). The preferential treatment thus results in a nontrivial redistribution of profits from large to small firms at almost no cost to the government.

The changes in entry and profits differ substantially in magnitude across project types. Two potential sources of such differences are (i) variation in cost asymmetries and (ii) differences in market thickness, or the number of potential bidders. We investigate how these factors affect the magnitude of the program's impact on small bidders' participation in Table 15. The table reports the results of an OLS projection of the absolute change in small bidders' probability of entry on project characteristics, potential entry, and the moments of the two groups' entry and project cost distributions.

The results suggest that small-firm participation responds more strongly for larger projects, for projects where small firms have lower average project costs than large firms, and for projects where the within-group variation in entry costs is lower, in particular for large firms. Last, the program has stronger effects for projects with fewer small potential bidders, but a higher number of large potential bidders. These effects are intuitive. Larger projects produce a larger absolute gain from the program that offsets entry costs. Low variance of the entry cost distribution implies that a given change in expected profit from participating affects the entry behavior of a larger mass of firms. The number of potential bidders reflects the competitive intensity and the size of the set over which the program's profit gains or losses are divided.

The second specification in Table 15 shows that after controlling for small firms' base probability of entry at $\delta = 0$, only project costs and potential competition play a statistically significant, now larger, role in promoting participation. The results

TABLE 15—ANALYSIS OF THE MAGNITUDE OF COUNTERFACTUAL EFFECTS:
SMALL FIRMS' ENTRY RESPONSE

	Coefficient	Standard error	Coefficient	Standard error
c_{sm}	0.0450***	0.0091	0.0610***	0.0110
$c_{lg} - c_{sm}$	0.0590***	0.0110	0.0800***	0.0140
d_{sm}	1.3700***	0.4200	0.7440	0.5800
σ_{sm}^G	-8.8200***	3.6300	-4.6600	3.9200
$\sigma_{lg}^G - \sigma_{sm}^G$	-19.1600***	8.3100	-12.1900	8.5400
Number of small plan holders	-0.0020***	0.0006	-0.0030***	0.0006
Number of large plan holders	0.0051***	0.0008	0.0050***	0.0007
$p_{sm}(\delta_{sm} = 0)$			-0.0340***	0.1400

Notes: Dependent variable is the change in the probability of entry for small firms. c_{lg} and c_{sm} denote large and small firms' mean projects costs; d_{sm} denote small firms' mean entry costs; σ_{lg}^G and σ_{sm}^G denote the standard deviation of large and small firms' entry costs; and $p_{sm}(\delta_{sm} = 0)$ denotes the small-firm probability of entry under $\delta_{sm} = 0$.

also indicate that gains in small-firm participation are larger in projects where their participation would have been low in the absence of preferential treatment. The program thus appears to be more effective for projects where participation of small firms is impeded without preferential treatment.

This analysis is related to Marion (2007) who provides an alternative estimate of the effect of the California Small Business Preference program on the cost of procurement. He measures this effect by comparing a set of state-funded projects where the program is implemented to a set of federally funded projects. He finds that the average winning bid on state-funded projects exceeds that on federally funded projects by 3.8 percent. Attributing this difference to the program is complicated by the fact that federally funded projects have another preferential treatment program in place that restricts bidders' subcontracting choices. In addition, federally and state-funded projects differ along observable dimensions, suggesting that they may also differ on unobservable characteristics that would affect firms' cost distributions and, thus, the magnitudes of the effects of a preference program. If this were the case, the observed difference in participation patterns between the two sets of auctions would similarly not represent the changes in participation brought forth by the program.

E. Subsidy

Our analysis so far shows that increases in small-firm participation translate into increases in the group's probability of project award. This additional effect is often stronger than the direct effect of the discount, which works through the change in bidding strategies. Our analysis further suggests that differences in bid preparation costs contribute significantly to the difference in participation rates across bidder groups. Hence, a direct entry subsidy of small firms (or tax of large firms) could alternatively help to achieve small-firm award goals. A subsidy would increase the cost of procurement to the government, whereas a tax may reduce government outlays.

Table 16 summarizes lump-sum subsidy or tax policies that achieve alternative government goals for the five sample projects discussed above. We find that the

TABLE 16—COMPARISON OF ALTERNATIVE SUBSIDY PROGRAMS, SAMPLE PROJECTS

	Project				
	1	2	3	4	5
Optimal subsidy					
Government cost	4.23	1.3	9.14	8.14	5.51
Δ Government cost (percent)	-8.93	-7.10	-7.97	-5.60	-5.95
Subsidy—small	-0.20	-0.10	-0.80	-0.30	-0.20
—large	-0.20	-0.20	-1.31	-0.30	-0.20
Expected number of bidders—small	0.00	1.96	1.96	0.00	0.00
—large	2.55	0.00	0.00	3.01	3.14
Subsidy targeting small-firm probability of winning					
Case 1					
Δ Government cost (percent)	-4.57	-7.59	-7.97	-0.75	-3.04
Δ Large-firm profit (percent)	-100	-100	-100	-100	-100
Subsidy—small	-0.40	-0.10	-0.81	-0.81	-0.61
—large	-0.90	-0.20	-1.31	-1.72	-1.02
Case 2					
Δ Government cost (percent)	13.83	0.00	0.00	9.89	11.14
Δ Large-firm profit (percent)	0.00	0.00	0.00	0.00	0.00
Subsidy—small	0.30	0.00	0.00	0.30	0.30
—large	0.10	0.00	0.00	0.20	0.10
Benchmarks					
Government cost (minimum)	4.65	1.40	9.93	8.62	5.85
Government cost (allocation target)	4.90	1.41	9.93	8.85	5.95

Notes: The subsidy amounts denote a subsidy payment to an individual firm were it to enter, with negative amounts denoting a tax. Government cost and subsidy payments in \$100,000s. Case 1 shows subsidy levels that produce a 25 percent probability of winning for small firms. Case 2 displays subsidy levels which achieve that same small firm probability of winning as above but also constrain large-firm profits to be at least as large as those under a bid discount with a 25 percent small-firm probability of winning. The changes in costs and expected profits are computed relative to the respective magnitudes under the above bid discount.

unconstrained cost-minimizing policy (panel 1) involves taxing both groups.²⁹ It reflects the trade-off between tax rate and tax base: higher tax rates increase per-firm tax receipts, but lower participation, putting upward pressure on the expected winning bid. The government minimizes its cost of procurement by choosing tax rates so only the more efficient group participates in bidding, where efficiency reflects both project and entry costs. Participation is reduced relative to the no-intervention case; yet the cost of procurement decreases due to the tax receipts. For a detailed, graphical example of the relationship between the tax and the total cost of procurement, see Figure A-5 in the online Appendix.

We next turn to a policy that achieves California's goal of allocating 25 percent of procurement dollars to small firms (see panel 2 of Table 16). A subsidy to small firms that achieves this objective is less costly to the government than the equivalent bid discount. It realizes cost savings of 0.7 percent to 8 percent relative to a bid discount that achieves the same small-firm award rate. These cost savings are realized in part by taxing large firms and come at the cost of that group's profits.

²⁹With high tax levels, participation may drop to zero, resulting in a nonaward of the project. The true economic cost of a nonaward and later readvertising of a possibly rescoped project is difficult to estimate. We assume, however, that it exceeds the cost of awarding the project immediately. In our simulations, we simply set the government's cost in this case equal to the particular project's engineer's estimate, an amount that across projects exceeds the minimum cost to the government.

Such high penalties on large firms may be undesirable. We compare instead the cost of tax/subsidy policies and bid discounts that both achieve the small-firm award goals and entail identical, less severely reduced, large-firm profit levels. In both cases, we allow large-firm profit to decline to the amount associated with the bid discount under the allocative goal. Interestingly, we find that under these constraints, a tax/subsidy policy results in higher cost of procurement for all five projects (see panel 3 in Table 16). This result highlights an unexpected benefit associated with bid preference programs: they limit profit redistribution given a target probability of winning for the preferred group. Bid preference programs are designed to artificially increase the probability of winning of the preferred group, an effect that is further enhanced by the participation responses to the program. In the absence of such a mechanism, the tax/subsidy policy has to increase the probability of winning solely through increases in the preferred group's participation. For a given preferred-group probability of winning, the participation responses are necessarily more significant than under the bid discount. This, in turn, reduces the nonpreferred group's profit margins below the level associated with the bid discount program. To achieve a target probability of winning while holding large-firm profit at the corresponding bid preference level, the government has to subsidize the participation of both small and large firms.³⁰ These subsidy expenditures offset the cost reductions brought about by the increased participation.

VI. Conclusion

This paper provides evidence based on the California Small Business Preference program on the channels through which bid discounts affect procurement outcomes, separating adjustments in firms' participation behavior from those in their bidding decisions. Within our empirical context, we find that the response in firms' bidding behavior (conditional on participation) to alternative discount levels changes aggregate procurement costs by only a limited amount relative to more substantial changes resulting from participation adjustments. This is of critical importance to policy design; we show, for example, that taking firms' participation incentives into account alters the bid discounts that achieve the government's procurement goals and the assessment of the costs increases associated with different discount levels.

California's current program generates only small increases in procurement costs. While promoting small-firm participation at the expense of large-firm participation and profit, it does not achieve the state's allocative goal. Our results imply that for the set of projects in our data, a higher discount of 15 percent is needed to reach the allocative target. This discount level does not come at substantial cost increases, however, raising the aggregate cost of procurement by 1.4 percent relative to no intervention. It is important to note that these results depend crucially on the mix of projects in California's highway procurement market. In other markets allocative goals may lead to larger or smaller cost increases.

³⁰ A subsidy may provide incentives for firms to submit uncompetitive bids for the sole purpose of collecting subsidy payments. Instead, the subsidy could be awarded only to the winning bidder, while a tax can be applied to all entrants from the taxed group. The subsidy level has to be adjusted to account for this modification. The magnitudes of all effects remain unchanged.

We consider the cost implications of broader policy redesign. In line with theoretical predictions for environments with fixed participation, we find that a bid discount can be used to lower the government's cost of procurement. If the degree of cost asymmetries between small and large firms is high, the cost-minimizing auction design prevents the inefficient group—typically small firms—from participating by granting a large discount to the other group. Since projects where small firms are very inefficient are easily identifiable by observable attributes, the government may prefer to use the set-aside auctions common in the timber industry in such instances. In our dataset, however, even the cost-minimizing discount generates only modest cost reductions, while discounts that depart from this level—but remain within the range of typically used bid discounts—can result in significant cost increases for at least a subset of projects.

We find large heterogeneity in the effect of the bid discount across types of projects. This suggests that the government should optimally employ a more nuanced preferential treatment, tailoring the discount rate to the project type, similar to the approach taken by the FCC. This can result in substantial cost savings while facilitating the implementation of the state's allocative goals.

Our findings suggest further that a lump-sum entry fee is more effective than a bid discount at reducing the cost of procurement. This reduction in government cost is achieved at the expense of large bidders whose profit margins are significantly reduced. In contrast, for a given allocative goal and large-firm profit levels, a tax/subsidy policy drives the cost to the government above the level attained by a bid preference program.

Our results demonstrate that a preference program evaluation depends critically on capturing firms' participation responses to the policy. While our findings are based on the highway procurement market, we believe that this insight, as well as our technique for predicting participation responses, is pertinent to other auction markets where discriminatory policies are used. A number of open questions remain. We focus on the short-run effects of the program but do not assess its dynamic, long-run implications. This includes adjustments to the set of potential bidders, which we hold fixed throughout our analysis. Due to the complexities of analyzing asymmetric auctions in a dynamic game, we also do not formally consider the importance of capacity constraints that could affect project costs and thus both bids and participation incentives. Following Caltrans' current practice, we do not introduce a reserve price into our analysis. Similar to the bid discount, a reserve price limits the participation of favored and nonfavored bidders with high project costs. At the same time, it induces favored firms to bid more aggressively than under the bid discount alone, thus limiting the redistribution of profits to favored firms. This raises a number of interesting issues, including the optimal policy design in the presence of possibly group-specific reserve prices and the importance of participation responses in the optimal policy. We leave these to future research.

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